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### Authors

Nottrott, Anders  
Kleissl, Jan  
Keeling, Ralph

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1 **Modeling passive scalar dispersion in the atmospheric boundary layer with**  
2 **WRF large-eddy simulation**

3  
4 Anders Nottrott<sup>1,\*</sup>, Jan Kleissl<sup>1</sup>, Ralph Keeling<sup>2</sup>

5  
6 <sup>1</sup>University of California, San Diego, Department of Mechanical and Aerospace Engineering

7 <sup>2</sup>University of California, San Diego, Scripps Institute of Oceanography, Geosciences Research  
8 Division

9  
10 *\*Corresponding Author*

11 Anders Nottrott  
12 University of California, San Diego  
13 Department of Mechanical and Aerospace Engineering  
14 9500 Gilman Dr  
15 EBU II - 362  
16 La Jolla, CA 92093-0411  
17 Email: anottrot@ucsd.edu  
18 Tel.: (805) 252-9606

## 19 **Abstract**

20

21 The ability of the Weather Research and Forecasting, large-eddy simulation model (WRF-LES)  
22 to model passive scalar dispersion from continuous sources located at ground-level and in the  
23 surface layer of convective and neutral atmospheric boundary layers was investigated. WRF-LES  
24 accurately modeled mean plume trajectories and concentration fields. WRF-LES statistics of  
25 concentration fluctuations in the daytime convective boundary layer were similar to data  
26 obtained from laboratory experiments and other LES models. However, poor turbulence  
27 resolution near the surface in neutral boundary layer simulations caused overestimation of  
28 concentration variance in the neutral surface layer. A gradient in the intermittency factor for  
29 concentration fluctuations was observed near the surface downwind of ground-level sources in  
30 the daytime boundary layer. That observation suggests that the intermittency factor is a  
31 promising metric for the estimation of source-sensor distance in practical source determination  
32 applications.

33

34 **Keywords:** WRF model; large-eddy simulation; passive scalar; dispersion; atmospheric  
35 boundary layer; concentration fluctuations

## 36 **1. Introduction**

### 37 *1.1 Motivation*

38 The development of a method to quantify greenhouse gas (GHG) emissions from distributed  
39 sources using long-term, continuous measurements remains an open problem with important  
40 applications for the control, regulation and financial valuation of GHG emissions. California's  
41 Global Warming Solutions Act (California AB 32), for example, established a GHG Cap-and-  
42 Trade program which includes an enforceable GHG emissions cap and tradable permits to large  
43 GHG emitters such as refineries, power plants, and industrial facilities (CARB, 2013). The  
44 California Cap-and-Trade Offset Verification Program will rely primarily on a bottom-up  
45 framework for regulatory verification of all GHG reductions and removal enhancements.  
46 However, the credibility of such a regulatory framework for GHG emissions depends on a  
47 reliable method for independent verification and long term monitoring of the actual emissions of  
48 market participants. The recent development of a robust and accurate cavity ring-down  
49 spectrometer (CRDS; Crosson, 2008) – and the associated field calibration systems (Welp et al,  
50 2012) – has made long-term, continuous field measurements of CO<sub>2</sub> and CH<sub>4</sub> concentrations  
51 feasible on national, regional and local spatial scales (Sloop & Novakovskaia, 2013). With the  
52 proliferation of CRDSs, and the availability of large volumes of continuous GHG concentration  
53 data, a new problem has arisen; namely a lack of capable modeling tools and strategies to  
54 interpret the measurements in the context of top-down inventories.

55

56 This paper is an assessment of the capability of the Weather Research and Forecasting (WRF)  
57 Large-eddy simulation software (hereafter WRF-LES) to model passive scalar dispersion, and  
58 thereby GHG dispersion, in the atmospheric boundary layer (ABL). The advantage of WRF-LES  
59 over other LES codes is that WRF-LES is integrated within the broader WRF source code which  
60 has multi-scale (synoptic to mesoscale) weather simulation capabilities. Two-way nesting of  
61 mesoscale and local (LES) scale boundary conditions will be feasible for operational modeling in  
62 the near future (Talbot et al, 2012). This capability will facilitate realistic simulations of

63 dispersion from distributed, local scale GHG emissions sources; a process which is significantly  
64 impacted by mesoscale forcing. A recent investigation of the influence of different subgrid-scale  
65 (SGS) stress models on ABL turbulence simulation in WRF-LES by Kirkil et al (2012) showed  
66 that representation of surface layer turbulence at the resolved scale is *especially* poor in WRF-  
67 LES, particularly in the neutrally stratified ABL. Poor representation of surface layer turbulence  
68 occurred regardless of the chosen SGS model and was attributed to excessive artificial diffusion  
69 in the numerical differencing scheme (E. Bou-Zeid, Personal communication, 2012). Thus the  
70 goals of this assessment are twofold. The first is to conduct a detailed investigation and  
71 validation of passive scalar dispersion in the ABL modeled using WRF-LES. The second is to  
72 understand how WRF-LES can be used as a modeling tool to interpret and derive source  
73 information from long-term GHG concentration time series measured in the ABL.

74  
75 The WRF-LES model and setup for numerical experiments are discussed in Section 2. Results of  
76 WRF-LES simulations are presented in Section 3. The vertical structure of boundary layer  
77 turbulence statistics are discussed in Sections 3.1 and 3.2, mean dispersion trajectories and  
78 concentration profiles investigated in Sections 3.3 and 3.4 and concentration fluctuations are  
79 investigated in Sections 3.5 and 3.6. A discussion of the results and conclusions are presented in  
80 Sections 4 and 5, respectively.

## 81 *1.2 Literature Review*

82 Pioneering experiments on scalar dispersion in a laboratory scale model of the convective  
83 atmospheric boundary layer (CBL) were conducted by Wills & Deardorff (1976, 1981). Data  
84 from those experiments established trajectories for plume rise and spread in the CBL downwind  
85 of a localized point source of a pollutant. Wills & Deardorff (1976) demonstrated that Taylor's  
86 frozen turbulence hypothesis can be applied to transform the dispersion field from a continuous  
87 point source (CPS) to that of an instantaneous line source (ILS). That result is important for  
88 numerical simulation of ABL dispersion because it can be leveraged to reduce computational  
89 cost in turbulent dispersion simulations if the numerical domain is spatially homogeneous in the  
90 horizontal directions (see Section 2.3). Later experiments (Deardorff & Willis, 1984)  
91 investigated concentration fluctuations downwind of localized scalar sources in the CBL. Large  
92 concentration fluctuations occurred and the magnitude of those fluctuations decayed rapidly as a  
93 function of downwind distance from the source due to small scale mixing. Shaughnessy &  
94 Morton (1977) and Fackrell & Robbins (1982) studied dispersion from CPSs in neutrally  
95 stratified boundary layers. Profiles of mean concentration and concentration fluctuations  
96 downwind of ground level sources in the neutral ABL maintain a self-similar shape, while  
97 dispersion fields from elevated releases preserve downwind self-similarity only in the crosswind  
98 direction. Those experiments also showed that, for elevated sources in the neutral boundary  
99 layer, the nature of concentration fluctuations downwind of point sources is strongly dependent  
100 on the ratio of source size to characteristic length scale of turbulent structures. However, this  
101 effect was less apparent for ground level sources. Venkatram and Wyngaard (1988) present an  
102 excellent review of parameterizations and experiments on scalar dispersion in the ABL.

103  
104 ABL dispersion processes span a wide range of length scales, from the integral scale down to the  
105 smallest inertial scales and the dissipation range. The large-eddy simulation (LES) technique  
106 resolves turbulent structures down to the inertial scales and is well suited to investigate the multi-  
107 scale nature of dispersion. Nieuwstadt (1992) studied dispersion from a CPS in a LES of the  
108 CBL, and decomposed the dispersion field into two components: a small scale component due to

109 the mixing action of inertial scale eddies and a meandering component caused by large scale  
 110 motions in the ABL. Nieuwstadt found that meandering was the dominant driver of mean plume  
 111 spreading near the source, but became small relative to the small scale component as the vertical  
 112 and crosswind dimensions of the plume approach the integral length scale of the boundary layer.  
 113 Henn & Sykes (1992) used LES to study concentration fluctuations downwind of a CPS  
 114 (modeled as volume source at grid resolution) dispersing in a convective boundary layer. Henn  
 115 & Sykes observed large variability in scalar concentration due to the formation of “concentration  
 116 filaments” generated by vortical structures in the ABL turbulence field. Yee & Chan (1997)  
 117 expanded the work of Henn & Sykes and developed a model probability distribution function for  
 118 concentration fluctuations using a gamma distribution. The LES study of Dosio et al (2003)  
 119 investigated passive scalar dispersion over a wide range of stability conditions from near neutral  
 120 to strongly convective and developed new parameterizations for mean dispersion that are valid  
 121 from neutral through strongly convective conditions.

<b>Nomenclature</b>		$x$	along wind (streamwise) direction
$c$	scalar concentration	$y$	crosswind horizontal direction
$c^*$	dimensionless scalar concentration	$z$	vertical direction
$e$	Coriolis parameter; vertical component	$\bar{z}$	mean plume vertical centerline height
$F$	forcing term in the Navier-Stokes equations	$z_i$	inversion height
$f$	Coriolis parameter; horizontal component	$z_l$	local plume vertical centerline height
$K_\phi$	scalar eddy diffusivity coefficient	$z_o$	aerodynamic roughness
$L$	Obukhov length	<i>Greek Symbols</i>	
$L_x, L_y, L_z$	streamwise, crosswind horizontal and vertical dimensions of the numerical domain	$\gamma$	intermittency factor
$M$	mean wind speed	$\Delta$	numerical grid spacing
$M_p$	mean wind at the average vertical centerline height of the plume	$\theta$	potential temperature
$m_z$	meandering component of dispersion	$\nu$	kinematic viscosity
$N_x, N_y, N_z$	streamwise, crosswind horizontal and vertical number of grid points in the numerical domain	$\rho$	fluid density
$p$	pressure	$\sigma$	plume width
$S$	continuous source term in the scalar advection-diffusion equation	$\tau$	subgrid scale stress tensor
$s_z$	spreading component of dispersion	$\phi$	scalar mass
$t$	time since instantaneous line source release	<i>Superscript</i>	
$U_g$	geostrophic wind speed	$'$	fluctuation velocity component (as in Reynolds average) or plume width relative to source location
$u$	along wind (streamwise) component of velocity ( $u_1$ )	<i>Subscript</i>	
$u^*$	friction velocity	$i, j$	component indices for vector quantities
$v$	crosswind horizontal component of velocity ( $u_2$ )	$p$	quantity measured on the plume centerline
$w$	vertical component of velocity ( $u_3$ )	$s$	quantity at the surface
$w^*$	Deardorff convective velocity scale	$T$	threshold value
$w_m$	modified velocity scale	$t$	with respect to time
$X$	dimensionless downwind distance	<i>Symbols</i>	
$X_m$	modified dimensionless downwind distance	$\sim$	filtered variable
		$-$	ensemble or time averaged variable

## 2. Methodology

### 2.1 Background

The Weather Research and Forecasting model (WRF; Skamarock & Klemp, 2008) is a community model developed by the National Center for Atmospheric Research (NCAR) and the National Oceanic and Atmospheric Administration (NOAA). WRF has multi-scale, nested simulation capability (from synoptic to local scales), includes real-world land-use and topographic data, and has the capability to ingest regional-scale meteorological forcing data. WRF is designed to run on massively parallel computers, and it is well documented with a broad user base and support group. The Advanced Research WRF (ARW) implements a fully compressible, Euler non-hydrostatic dynamics solver that is conservative for scalar variables. ARW can run in a LES mode (WRF-LES).

Large-eddy simulation provides a framework to obtain turbulence data for ABL wind and scalar fields at greater spatiotemporal resolution than mesoscale atmospheric models or direct measurements. The LES technique directly resolves large turbulent motions in three-dimensions by computing a numerical solution to the filtered Navier-Stokes equations, while the effects of small scale motions are parameterized with a SGS model. The filtered mass conservation and Navier-Stokes equations are (Deardorff, 1970)

$$\partial_i \tilde{u}_i = 0, \quad (1)$$

$$\partial_t \tilde{u}_i + \partial_j \tilde{u}_i \tilde{u}_j = \nu \partial_j \partial_j \tilde{u}_i - \frac{1}{\rho} \partial_i \tilde{p} - \partial_j \tau_{ij} + \tilde{F}_i, \quad (2)$$

where  $\tilde{u}_i$  is the  $i^{th}$  component of filtered velocity field,  $\tilde{p}$  is the filtered pressure and  $\tau_{ij}$  is the subgrid-scale stress tensor.  $\nu$  and  $\rho$  are the fluid kinematic viscosity and density, respectively.  $\tilde{F}_i$  is a general forcing term, e.g. Coriolis force due the earth's rotation.  $\partial_j$  represents a spatial derivative while  $\partial_t$  is a derivative with respect to time. Einstein's summation notation is used in Eqs. 1 and 2 where  $i, j \in [1,2,3]$ . Closure of Eq. 2 is obtained by modeling  $\tau_{ij}$  (for more details of SGS models in WRF-LES see Kirkil et al, 2012). Eqs. 1 and 2 are written for incompressible flow and represent an approximation the full compressible solution that is solved in WRF-LES. The WRF-LES dynamical core uses finite differences (rather than a pseudospectral method) to compute spatial derivatives. Passive scalar dispersion is modeled in WRF-LES by solving the filtered advection-diffusion equation for the atmospheric boundary layer

$$\partial_t \tilde{\phi} + \tilde{u}_j \partial_j \tilde{\phi} = -\partial_j \tilde{u}_j \phi + S(x_j), \quad (3)$$

where  $\tilde{\phi}$  is the resolved (filtered) scalar mass concentration,  $\tilde{u}_j \phi$  is the SGS scalar mass flux and  $S(x_j)$  is the continuous source function. Molecular diffusion is assumed to be negligible in the high Reynolds number limit. The SGS scalar flux is modeled as  $\tilde{u}_j \phi = -K_\phi \partial_j \tilde{\phi}$ , where  $K_\phi$  is the SGS scalar eddy diffusivity coefficient.

Nieuwstadt (1992) defined the downwind trajectory of a scalar concentration field in terms of the centroid and first moment of the spatial distribution of the concentration field. The parameters used in this paper to describe the downwind plume trajectory in the  $x$ - $z$  plane are (see Figure 1): the local (or instantaneous) plume centerline height ( $z_l$ ), the average plume centerline height ( $\bar{z}$ ), the total vertical dispersion ( $\sigma_z$ ), the total vertical dispersion relative to the source height ( $\sigma_z'$ ), the spreading component about the local centerline height ( $s_z$ ) and the meandering component about the average centerline height ( $m_z$ ). Analogous parameters are also defined for the

161 crosswind trajectory in the  $x$ - $y$  plane. The reader is referred to Nieuwstadt (1992) and Appendix  
 162 A for mathematical definitions of these variables.

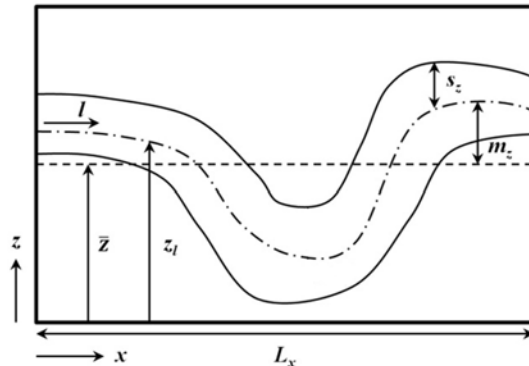


Figure 1 – A schematic of a dispersing ILS illustrating the parameters that describe the downwind trajectory of the scalar field. The  $x$ -axis is aligned with the mean wind  $M = (\bar{u}^2 + \bar{v}^2)^{1/2}$ . The parameters shown here are functions in the  $x$ - $z$  plane, and the equivalent parameters in the  $x$ - $y$  plane are analogous. Adapted from Nieuwstadt (1992).

163 *2.2 WRF configuration*

<b>Namelist Option</b>	<b>Setting (Value)</b>
Turbulence and mixing (diff_opt)	Mixing in physical space; full diffusion (2)
Eddy coefficient (km_opt)	3D Smagorinsky first order closure (3)
Subgrid-scale model (sfs_opt)	Nonlinear backscatter and anisotropy (0)
Damping layer option (damp_opt)	w-Rayleigh damping (3)
w-Rayleigh damping coefficient (dampcoef)	0.2
Coriolis force (pert_coriolis)	Coriolis only acts on wind departures from geostrophic balance (true)
Lateral boundary conditions (periodic_x, periodic_y)	Periodic lateral boundary conditions (true)
Upper boundary condition (top_lid)	Rigid lid (true)
Surface layer option (sf_sfclay_physics)	Monin-Obukhov scheme (1)
Surface heat and moisture fluxes (isfflx)	Specified surface heat flux (2)
Scalar advection option (scalar_adv_opt)	Positive-definite advection of scalars (1)

Table 1 – Configuration of namelist options for WRF-LES

164  
 165 The WRF-LES ‘namelist’ configuration used in this study is listed in Table 1. Fifth and third-  
 166 order finite difference schemes for momentum and scalars were used in the horizontal and  
 167 vertical directions, respectively. The third order Runge-Kutta scheme was used for time  
 168 integration. The passive scalar for ABL dispersion simulations was activated by setting the  
 169 ‘tracer\_opt’ namelist parameter to a value of ‘2’. A mass source of passive scalar was initialized  
 170 by modifying the tracer variable loop in ‘solve\_em.F’ subroutine. Periodic lateral boundary  
 171 conditions were enforced for the velocity, temperature and scalar, and a no  
 172 penetration/absorption condition was enforced for the scalar at the lower and upper boundaries  
 173 so that the total scalar mass within the domain was conserved.

174 *2.3 Description of Numerical Experiments*

175 Seven simulation cases were run for a range of ABL stability conditions from neutral through  
 176 strongly convective, and six different domain configurations were used. The aerodynamic

177 roughness length was set to  $z_o = 0.15$  m for all domains and the Coriolis parameters were  $f =$   
178  $8.5 \cdot 10^{-5}$  Hz and  $e = 0$  Hz corresponding to an approximate latitude of  $36^\circ\text{N}$ . All simulations  
179 were spun up until surface averaged shear stress and domain averaged turbulence kinetic energy  
180 were nearly constant in time. Turbulence and boundary layer parameters for all simulations are  
181 listed in Table 2. The upper 250 meters of the domain for the CBL cases was allocated as  
182 damping layer to prevent the reflection of gravity waves, and the inversion height ( $z_i$ ) ranged  
183 from about 900 m to 1200 m depending on the amount of surface heat flux and time in the  
184 simulation. Empirical testing of WRF-LES for the neutral ABL simulations demonstrated that a  
185 deep neutral boundary layer could not be maintained because turbulent mixing at the inversion  
186 caused warm air from above the inversion to be entrained downward into the boundary layer.  
187 This resulted in the formation of a stable temperature profile throughout the boundary layer after  
188 a few hours of simulation time (when the boundary layer turbulence was fully developed).  
189 Therefore, a damping layer of thickness 250 m was applied at the top of the domain to maintain a  
190 deep neutral BL and to simulate dynamic effects of a temperature inversion in the neutral ABL  
191 simulation. The domain resolution was varied to investigate the resolution dependence of  
192 concentration fluctuations and observed errors in turbulence fields.

Name	$L_x, L_y$ [m]	$L_z$ [m]	$\Delta x, \Delta y$ [m]	$\Delta z$ [m]	$U_g$ [m s <sup>-1</sup> ]	$\overline{w'\theta'_s}$ [m s <sup>-1</sup> K <sup>-1</sup> ]	$z_i$ [m]	$u^*$ [m s <sup>-1</sup> ]	$w^*$ [m s <sup>-1</sup> ]	$L$ [m]	$-z_i/L$
B1	7680	1750	30	8	0.5	0.05	1000	0.12	1.19	-2.69	380
B5	7680	1750	30	8	5	0.1	1000	0.28	1.48	-18.6	59
B5HR	3040	1500	10	2.75	5	0.1	900	0.29	1.48	-19.2	52
SB2	7680	1750	30	8	10	0.1	1000	0.49	1.48	-109	11
SB2HR	3040	1500	10	2.75	10	0.1	900	0.50	1.48	-100	10
N	8640	1067	30	8	15	0	815	0.6	0	$-\infty$	0
NHR	7680	1067	15	4	15	0	815	0.6	0	$-\infty$	0

Table 2 – Domain and boundary layer parameters for different numerical experiments in this study.  $\Delta z$  values are approximate because WRF uses vertical pressure coordinates. The simulation names are similar to those in Dosio et al (2003). The inversion heights listed in this table were the initial values at the start of each simulation.

193 Continuous point sources of a passive scalar were modeled as instantaneous line sources aligned  
194 parallel to the streamwise direction under the assumption of Taylor's hypothesis. This approach  
195 reduces the computational cost of dispersion simulations (for domains that are spatially  
196 homogeneous in the horizontal directions) because dispersion at long downwind distances can be  
197 modeled with a relatively small numerical domain by increasing the run time of the simulation  
198 instead of the spatial extent of the domain. Ensemble average statistics of scalar concentration at  
199 any downwind location can be computed from instantaneous spatial transects of scalar  
200 concentration in the domain taken at the appropriate moment in time. The transformation from  
201 CPS to ILS is also compatible with periodic boundary conditions because it eliminates the need  
202 for sponge boundary conditions for the scalar on the lateral domain boundaries. Different source  
203 heights ( $z_s$ ) were used for passive scalar releases to facilitate comparison of data from the present  
204 LES study with data from previous laboratory and numerical experiments. Source heights  $z_s =$   
205  $0.0033z_i$ ,  $0.07 z_i$ ,  $0.19 z_i$  were used in simulations B3 and B5,  $z_s = 0.0033 z_i$ ,  $0.07 z_i$  in simulation  
206 SB2 and  $z_s = 0.0043 z_i$ ,  $0.07 z_i$  in simulation N.  $z_s = 0.0025 z_i$ ,  $0.07 z_i$  in simulation NHR and  $z_s =$   
207  $0.0033z_i$  in simulations B5HR and SB2HR. Sources in domains B3, B5, SB2 and N were  
208 represented using 1 grid cell in the crosswind horizontal direction and 2 grid cells in the vertical  
209 direction (after Henn & Sykes, 1992 and Dosio et al 2003). Sources in domains B5HR and  
210 SB2HR were represented with 3 grid cells in the crosswind horizontal direction and 6 grid cells  
211 in the vertical direction, while in domain NHR the source occupied 2 grid cells in the crosswind



212 horizontal direction and 4 grid cells in the vertical direction The initial source volume and scalar  
 213 mass were constant in all simulations, but sources were represented by more grid points in the  
 214 higher resolution domains.

### 215 3. Results

#### 216 3.1 Variance profiles

217 Figures 2 and 3 show normalized vertical profiles of the Reynolds stresses, temperature variance,  
 218 kinematic heat flux for CBL and neutral ABL (cases B3, N and NHR) compared with data from  
 219 established LES codes, laboratory experiments and aircraft data. Good agreement was observed  
 220 between WRF-LES and validation data for the CBL (Figure 2). The peak in the vertical velocity  
 221 variance occurred around  $0.4z_i$  and the vertical profile of kinematic heat flux was linear over the  
 222 depth of the boundary layer. Agreement between WRF-LES and validation data was also  
 223 reasonable for the neutral ABL simulations (Figure 3). The magnitude of the maximum  
 224 streamwise velocity variance in WRF-LES is larger than the other data, however, Moeng et al  
 225 (2007) (using a less realistic SGS model) observed streamwise velocity variances as large as  
 226  $9u_*^2$  in WRF-LES. The peak in the vertical velocity variance occurred above the surface layer at  
 227 a height of  $0.2z_i$  in the low resolution domain (case N), but occurred closer to the surface around  
 228  $0.1z_i$  in the high resolution domain (case NHR). This observation is consistent with the results of  
 229 Kirkil et al (2012), and indicates that the SGS model is under-dissipative resulting in large  
 230  $\partial\bar{u}/\partial z$ . Bou-Zeid et al. (2005) demonstrated that the Lagrangian scale-dependent dynamic SGS  
 231 model produces a streamwise velocity and variance profile consistent with similarity theory and  
 232 observations; however this model is not available in the public release of WRF-LES. The  
 233 variance profiles in Figure 3 are all within the range of the LES code inter-comparison presented  
 234 in Andren et al (1994).

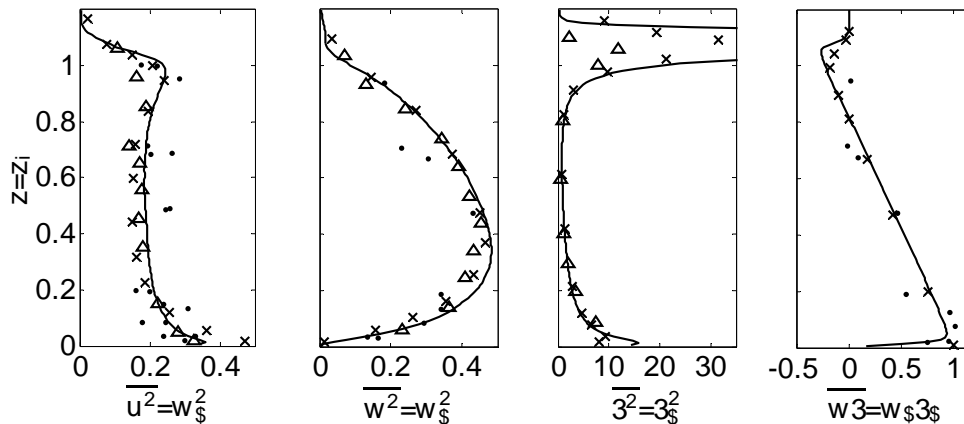


Figure 2 – Vertical profiles of resolved velocity variance, temperature variance and temperature flux normalized by the convective velocity scale and/or convective temperature scale for the CBL (WRF-LES case B3). WRF-LES resolved scales (solid line); LES of Raasch & Etling (1991; crosses); water channel data of Willis & Deardorff (1976; triangles); aircraft data of Lenschow et al (1980; dots).

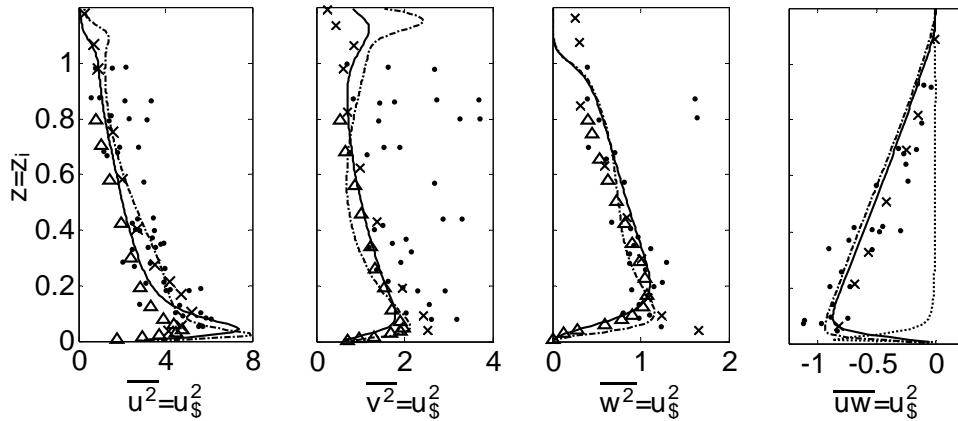


Figure 3 – Vertical profiles of velocity variance and momentum flux normalized by the surface shear stress in the neutral ABL (WRF-LES case N). WRF-LES simulation N resolved scales (solid line) and subgrid-scales (dotted line); WRF-LES simulation NHR resolved scales (dash-dotted line); LES of Moeng & Sullivan (1994; crosses); WRF-LES with nonlinear backscatter and anisotropy SGS model Kirkil et al (2012; triangles) with  $\Delta x = \Delta y = 32$  m and  $\Delta z = 8$  m; aircraft data from Grant (1986; dots).

### 236 3.2 Validity of CPS to ILS transformation

237 Continuous point source releases of passive scalars were modeled as instantaneous line sources  
 238 under the assumption of Taylor’s hypothesis (Willis & Deardorff, 1976). The transformation  
 239 between downwind distance and time is  $x = M_p t$ , where  $M_p$  is the mean wind speed at the  
 240 average vertical centerline height of the plume  $\bar{z}$ . This transformation is only valid when the  
 241 intensity of turbulent velocity fluctuations is small compared to the mean wind speed, i.e.  
 242  $\overline{u_i^2} / M_p^2 \ll 1$ . Figure 4 shows vertical profiles of velocity variances divided by mean wind  
 243 speed for all simulations. The assumption of Taylor’s hypothesis is not valid for case B3 but is  
 244 reasonable for the other cases. Dosio et al (2003) found that, although the CPS to ILS  
 245 transformation was not strictly valid for their B3 case, the mean downwind trajectory of the  
 246 dispersion field matched experimental data quite well. Nevertheless, Figure 4 indicates that  
 247 concentration fluctuations from the ILS dispersion field in the B3 boundary layer may not be  
 248 directly comparable to concentration fluctuations from a CPS released in the same turbulence  
 249 field, so data from the B3 case was not used to investigate scalar concentration fluctuations.

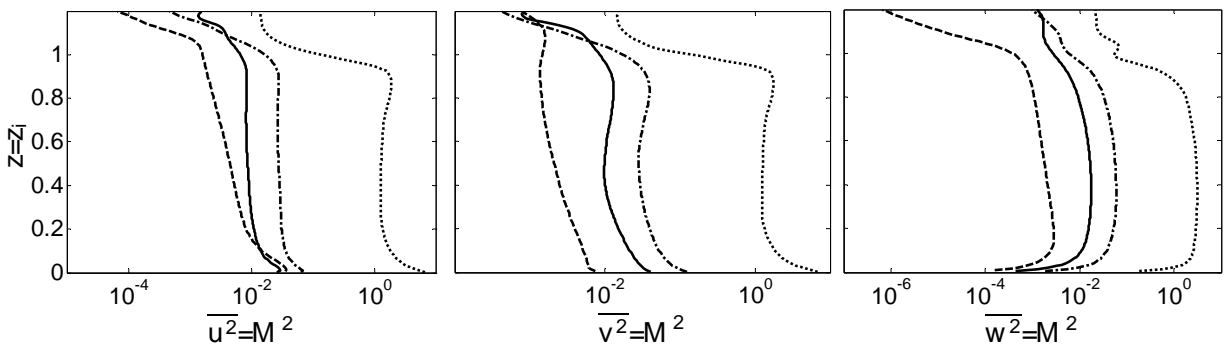


Figure 4 – Vertical profiles of velocity variance to mean wind speed ratio for all simulation cases. B3 (short dash line), B5 (dash-dot line), SB2 (solid line) and N (long dash line). Data for case NHR are not shown because they are similar to those for case N.

### 250 3.3 Plume trajectories

251 A dimensionless downwind distance parameter

$$X = \frac{w_*}{z_i} \frac{x}{M_p} = \frac{w_*}{z_i} t, \quad (4)$$

252 is defined after Willis & Deardorff (1976), where  $x$  is the downwind distance from the source  
 253 and  $t$  is the downwind travel time (consistent with the transformation described in Section 3.2).  
 254 A modified dimensionless downwind distance  $X_m$  is defined by substituting the convective  
 255 velocity scale in Eq. 3 with a mixed velocity scale  $w_m$ .  $w_m$  applies when the buoyant and shear  
 256 turbulent production are of similar magnitude. Moeng & Sullivan (1994) proposed the  
 257 relationship  $w_m^3 = w_*^3 + 5u_*^3$ . Figure 5 shows the components of mean dispersion parameters  
 258 (see Figure 1) modeled with WRF-LES for a surface layer release in the CBL compared with  
 259 data from laboratory experiments. The modeled mean dispersion parameters generally fall within  
 260 the range of the experimental data, with the exception of the total horizontal crosswind  
 261 dispersion (Figure 5c) which becomes smaller than the experimental data for  $X > 1.25$ . This  
 262 behavior was also observed in the LES study of Dosio et al (2003). It is interesting that the  
 263 contribution of the meandering component ( $m_y$ ) to  $\sigma_y$  becomes relatively constant downwind of  $X$   
 264  $> 1.25$  although  $\sigma_y$  continues to grow. This observation indicates that beyond  $X > 1.25$  the  
 265 horizontal crosswind dispersion is primarily driven by the spreading component of dispersion  
 266 ( $s_z$ ).

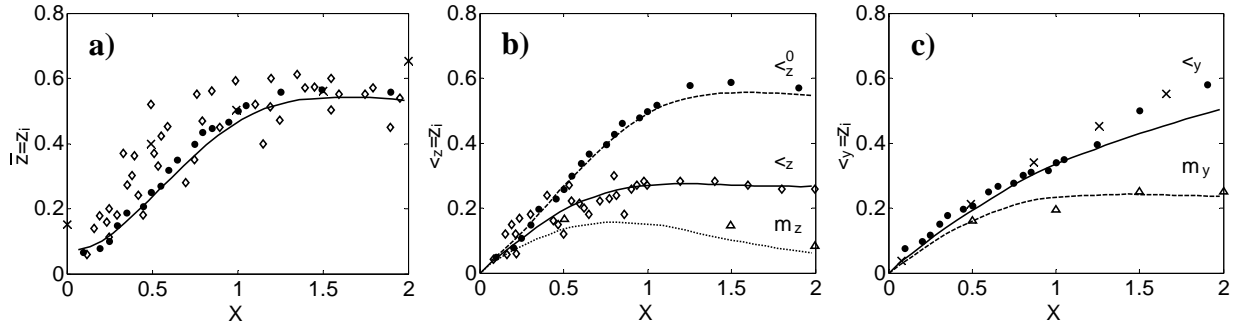


Figure 5 – Validation of mean dispersion parameters for a passive scalar release in the CBL (case B3) plotted as a function of dimensionless downwind distance  $X$  (Eq. 4). The source was located at  $X = 0$  and  $z_s = 0.07z_i$ . **a)** Mean plume height, **b)** total vertical dispersion and vertical meandering component, and **c)** total horizontal crosswind dispersion and crosswind meandering component. WRF-LES results are plotted as continuous lines and experimental data are plotted as symbols; Willis & Deardorff (1976; dots), Briggs (1993; diamonds) and Weil et al (2002; crosses and triangles). Each line in Figure 5b,c shows a different component of dispersion, and the label above each line indicates the variable that corresponds to the appropriate component of dispersion (refer to Section 2.1, Figure 1 and Appendix A for descriptions of these variables).

267  
 268 Figure 6 shows mean dispersion trajectories downwind of point sources in moderately  
 269 convective (case SB2) and neutral (case N) atmospheric boundary layers, compared with results  
 270 from the LES of Dosio et al (2003). The mean plume height (Figure 6a) and total vertical  
 271 dispersion (Figure 6b) are in close agreement with Dosio et al for both the SB2 and N boundary  
 272 layers. The total horizontal crosswind dispersion ( $\sigma_y/z_i$ ; Figure 6c) for the WRF-LES SB2 case is  
 273 similar to the Dosio et al data for  $X_m < 1.25$ , but begins to diverge farther downwind. However,  
 274  $\sigma_y/z_i$  in the WRF-LES simulation N is significantly smaller than the Dosio et al data. We  
 275 investigated the dependence of  $\sigma_y(X)$  on SGS scalar flux by setting the  $-\partial_j \widetilde{u_j \phi}$  term in Eq. 3 to  
 276 zero. Excluding the  $-\partial_j \widetilde{u_j \phi}$  term caused a 5% decrease in  $\sigma_y(X)$  at  $X = 2.5$ .  $\sigma_y(X)$  was about 10%  
 277 larger at  $X = 2.5$  for the surface layer release ( $z_s = 0.07z_i$ ) in the N case when compared with the  
 278 NHR case. This result suggests a systematic model bias for  $K_{\phi,h}$  (see Section 4).

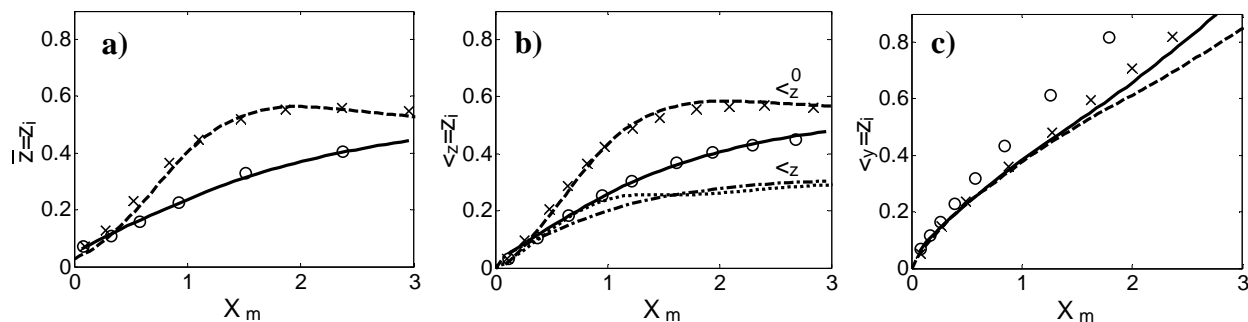


Figure 6 – Validation of mean dispersion parameters for a passive scalar release in moderately convective (case SB2) and neutral atmospheric boundary layers (case N) plotted as a function of dimensionless downwind distance  $X_m$  (Eq. 4). The source was located at  $X_m = 0$  and  $z_s = 0.07z_i$ . **a)** Mean plume height, **b)** total vertical dispersion, and **c)** total horizontal crosswind dispersion. WRF-LES results are plotted with continuous lines (SB2 long and short dash lines; N solid and dash-dot lines). WRF-LES dispersion fields are compared with LES data from Dosio et al (2003) plotted with crosses for SB2 and circles for N. Each pair of lines in Figure 6b (long dash/solid and short dash/dash-dot) shows a different component of dispersion. The label above indicates the variable that corresponds to the appropriate component of dispersion (refer to Section 2.1, Figure 1 and Appendix A for descriptions of these variables).

### 279 3.4 Mean concentration profiles

280 Figure 7 shows contours of dimensionless mean concentration  $c_* = \bar{c}(x, y, z)z_i^2 M_p / S$  for a  
 281 surface layer source in the B3 simulation. Figure 7a is a vertical cross-section along the plume  
 282 centerline, while Figure 7b shows total  $c_*$  from the surface to the inversion height. The  
 283 magnitude and shape of  $c_*$  contours are very similar to the laboratory measurements of Willis &  
 284 Deardorff (1976), although the plume width (Figure 7b) is slightly underestimated by WRF-LES  
 285 for  $X > 1.25$  (consistent with Figure 5c). Profiles of average scalar concentration in the CBL do  
 286 not exhibit self-similar behavior when normalized  $\sigma_y$  or  $\sigma_z$ , because CBL turbulence is dominated  
 287 by large coherent structures and therefore non-Gaussian (for example refer to the laboratory data  
 288 presented in Willis & Deardorff, 1976).

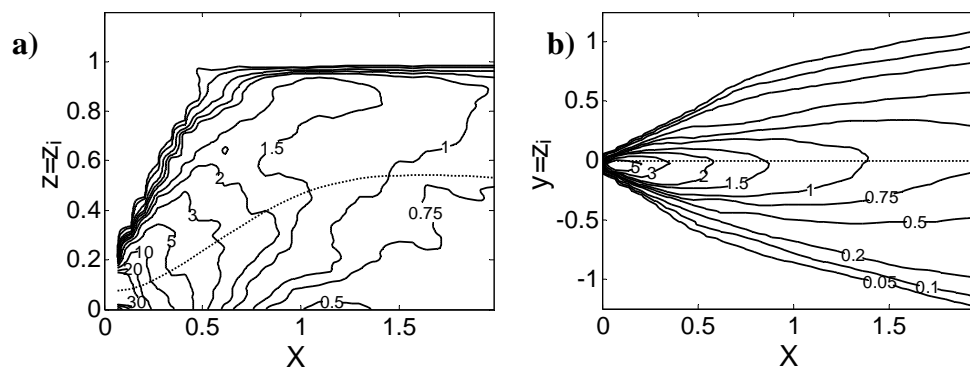


Figure 7 – Contours of dimensionless mean concentration  $c_* = \bar{c}(x, y, z)z_i^2 M_p / S$  for a surface layer ( $z_s = 0.07z_i$ ) release in the B3 simulation. **a)** Vertical cross-section along the plume centerline; **b)** integrated over the  $z$ -direction from the surface to the inversion height. The dashed lines indicate the plume centerline ( $\bar{z}$  and  $\bar{y}$ ).

289  
 290 Figure 8 shows vertical profiles of mean concentration along the plume centerline at different  
 291 locations downwind of sources released at ground-level and in the surface layer for simulation  
 292 case N. Figure 8a shows the expected self-similarity of the mean concentration field due to the  
 293 presence of the ground. Consistent with the water channel experiments of Fackrell & Robins  
 294 (1982) self-similarity does not occur in the vertical direction for surface layer releases (Figure

295 8b). Figure 9 confirms self-similarity of the crosswind horizontal concentration profiles in the  
 296 neutral boundary layer simulation (Shaughnessy & Morton, 1977). The slight negative skewness  
 297 apparent in Figure 9 occurred because the mean wind direction was not exactly parallel to the  
 298 direction of the ILS when the source was initialized due to the Coriolis force. Although the data  
 299 shown in Figure 9 are for a surface layer source, self-similarity was also observed for the ground  
 300 level source.

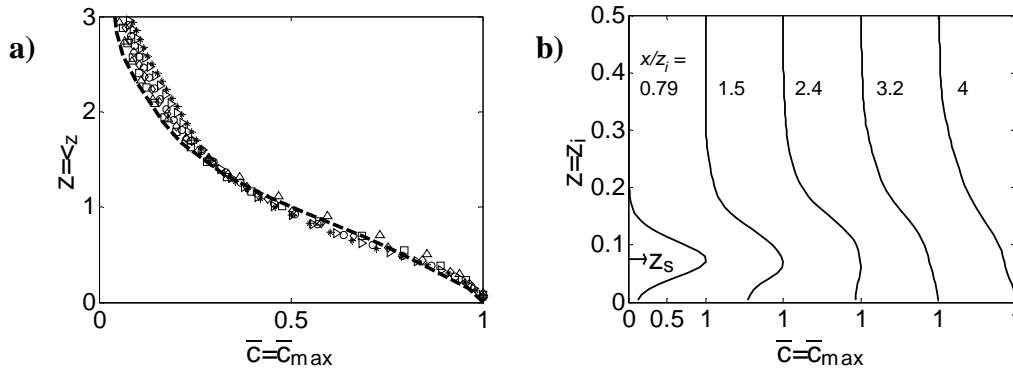


Figure 8 – Vertical profiles of mean concentration at various downwind locations along the plume centerline for **a)** a ground-level source ( $z_s = 0.0043z_i$ ), and **b)** a source in the surface layer ( $z_s = 0.07z_i$ ) in the N simulation. The mean concentration is normalized by the maximum mean concentration at each downwind location. Figure 8a:  $x/z_i = 2.1$  (triangles); 3.0 (squares); 3.9 (diamonds); 4.7 (circles); 5.6 (leftward arrows); 6.5 (stars). Data from Fackrell & Robbins (1982) are shown as the dashed line in Figure 12a. Profiles in Figure 8b are offset by  $\bar{c}/\bar{c}_{max} = 1$  for readability.

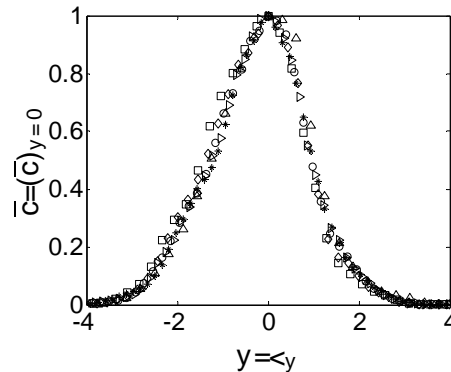


Figure 9 – Self-similarity of horizontal crosswind profiles of mean concentration at various downwind locations at the height of the plume vertical centerline ( $\bar{z}$ ) for a surface layer ( $z_s = 0.07z_i$ ) source in case N. The mean concentration is normalized by the maximum mean concentration (i.e. mean concentration at  $y = 0$ ) at each downwind location.  $x/z_i = 2.4$  (triangles); 3.2 (squares); 4.0 (diamonds); 4.9 (circles); 5.8 (leftward arrows); 6.6 (stars).

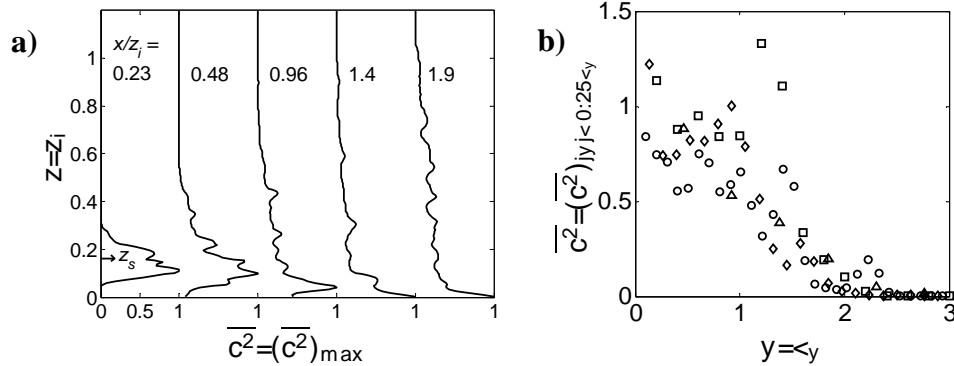


Figure 10 - Vertical and horizontal profiles of normalized concentration variance at different distances downwind of an elevated release located at  $z_s = 0.19z_i$  in the B5 simulation. **a)** Vertical profiles of concentration variance normalized by the maximum variance at each downwind position. **b)** Crosswind horizontal profiles of concentration variance at the vertical centerline height normalized by the mean variance in the region  $|y| < 0.25\sigma_y$ .  $x/z_i = 0.23$  (triangles);  $0.70$  (squares);  $1.2$  (diamonds);  $1.6$  (circles). Profiles in Figure 10a are offset by  $\overline{c^2} / (\overline{c^2})_{max} = 1$  for readability.

302

303 Available data on concentration fluctuations in the CBL are somewhat unstructured making  
 304 direct validation of the present LES experiments challenging. Figure 10 shows vertical and  
 305 horizontal profiles of normalized concentration variance at different distances downwind of an  
 306 elevated release located at  $z_s = 0.19z_i$  in the B5 simulation. The variance profiles in Figure 10a  
 307 illustrate downward motion of the plume (i.e. looping) downwind of the source which is a  
 308 characteristic feature of neutrally buoyant releases from elevated sources in the CBL (Henn &  
 309 Sykes, 1992). Figure 10b shows crosswind horizontal profiles of concentration variance,  
 310 normalized by the mean variance in the region  $|y| < 0.25\sigma_y$ , at the centerline height of the  
 311 plume. The WRF-LES model correctly captures the peak in the concentration variance that  
 312 occurs in the range  $0.5 < y/\sigma_y < 1.5$  although there is considerable scatter in the LES data  
 313 (Venkatram & Wyngaard, 1988). Figure 11 shows a comparison of ground-level concentration  
 314 fluctuation standard deviation from the same elevated release as in Figure 10 with data from  
 315 Henn & Sykes (1992). The data do not match exactly because the sources were located at  
 316 slightly different heights in the boundary layer, however, the magnitudes of the data are similar.  
 317 The larger standard deviation of the WRF-LES data may also be due to the higher spatial  
 318 resolution used in our simulations compared to Henn & Sykes.

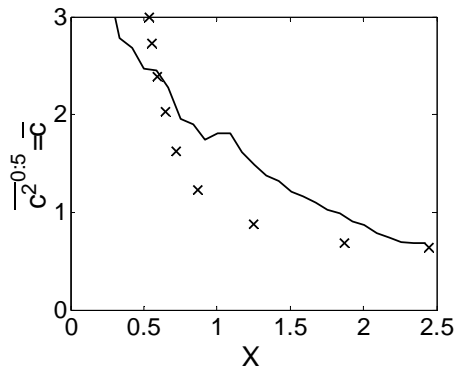


Figure 11 – Standard deviation of ground-level concentration fluctuations downwind of an elevated source normalized by the mean ground level concentration. The solid line shows WRF-LES data for a source located at  $z_s =$

0.19 $z_i$  in the B5 simulation. The crosses are LES data from Henn & Sykes (1992) who modeled an elevated source at  $z_s = 0.25z_i$  with LES.

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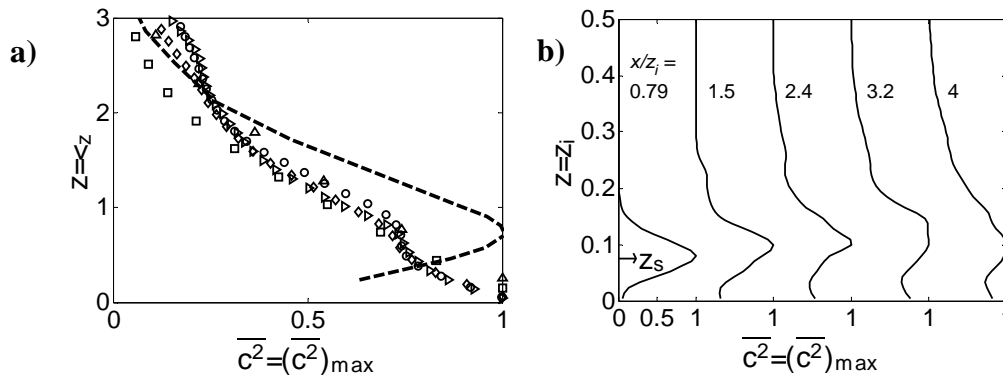


Figure 12 - Vertical profiles of concentration variance at different downwind locations along the plume centerline for **a**) a ground-level source ( $z_s = 0.0043z_i$ ), and **b**) a source in the surface layer ( $z_s = 0.07z_i$ ) in the N simulation. The concentration variance is normalized by the maximum variance at each downwind location. Figure 12a:  $x/z_i = 0.59$  (triangles); 1.3 (squares); 3.9 (diamonds); 4.7 (circles); 5.6 (arrows). Data from Fackrell & Robbins (1982) are shown as the dashed line in Figure 12a. Profiles in Figure 12b are offset by  $\bar{c}/\bar{c}_{max} = 1$  for readability.

320

321 Figure 12 shows vertical profiles of normalized concentration variance for ground-level and  
 322 surface layer sources in the neutrally stratified boundary layer (simulation N). The wind tunnel  
 323 experiments of Fackrell & Robbins (1982) showed that vertical profiles of normalized variance  
 324 for ground-level sources are self-similar along the plume centerline axis with a maximum value  
 325 at  $z/\sigma_z \approx 0.75$ . Fackrell & Robbins also hypothesized that the value of  $\bar{c}^2$  should tend toward zero  
 326 at the surface although their lowest measurements did not extend below  $0.05z_i$ . The WRF-LES  
 327 data in Figure 12a are approximately self-similar. However, although there is a local maximum  
 328 in the vertical profiles at  $z/\sigma_z \approx 0.75$ , the normalized variance approaches a value of 1 at the  
 329 surface rather than 0. The vertical profiles for the surface layer source (Figure 12b) exhibit the  
 330 correct upward trend for  $(\bar{c}^2)_{max}$ , but also show a local maximum in concentration variance at  
 331 the surface. Figure 13 shows crosswind horizontal profiles of normalized concentration variance  
 332 at different distances downwind at the height of plume vertical centerline for the surface layer  
 333 release ( $z_s = 0.07z_i$ ). The data in Figure 13 exhibit the weak peak in concentration variance that  
 334 occurs at  $y/\sigma_y \approx 0.5$  consistent with wind tunnel data (see Figure 7 in Fackrell & Robbins; 1982).  
 335 The data in Figure 13 are not expected to preserve self-similarity.

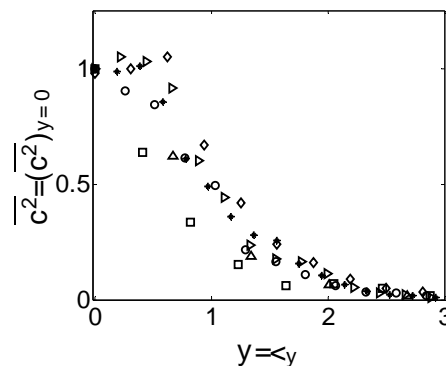


Figure 13 – Crosswind horizontal profiles of concentration variance at the height of the plume vertical centerline, normalized by the variance at the horizontal centerline of the plume (i.e. the variance at  $y = 0$ ) for a surface layer

release  $z_s = 0.07z_i$ ,  $x/z_i = 0.79$  (triangles); 1.5 (squares); 2.4 (diamonds); 3.2 (circles); 4.0 (leftward arrows); 4.9 (stars).

### 336 3.6 Intermittency factor for ground-level sources

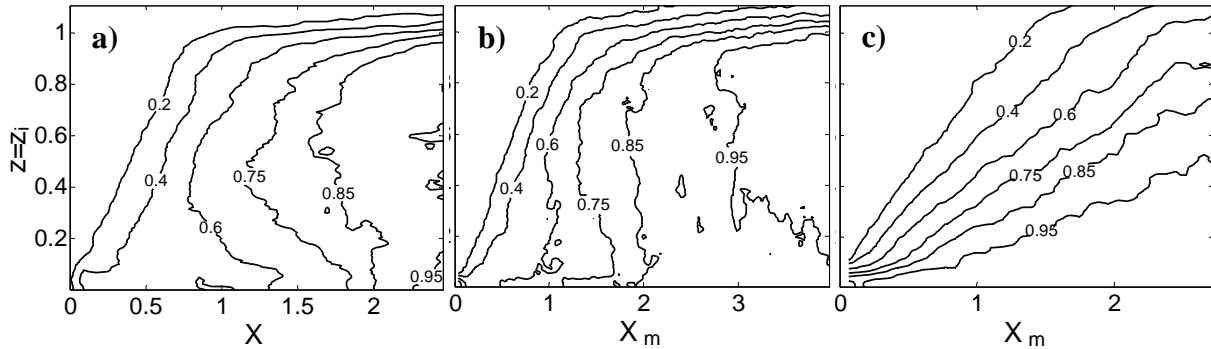


Figure 14 - Contours of the intermittency factor ( $\gamma$ ) in the  $x$ - $z$  plane along the horizontal centerline of the plume for ground-level releases located at  $X = 0$ . **a)** simulation B5 ( $z_s = 0.0033z_i$ ); **b)** simulation SB2 ( $z_s = 0.0033z_i$ ); **c)** simulation N ( $z_s = 0.0043z_i$ ). The threshold was  $c_T = 0.1\bar{c}$ .

337  
 338 The intermittency factor ( $\gamma$ ) for a timeseries of an arbitrary scalar ( $c$ ) is defined as the fraction of  
 339 time during which the magnitude of  $c$  exceeds some threshold value ( $c_T$ ):  $\gamma \equiv \tau/T$ ,  $T$  is the total  
 340 length of the timeseries and  $\tau$  is the total length of time during which  $c > c_T$ . The intermittency  
 341 factor is an alternative metric to standard statistical moments for quantifying concentration  
 342 variability in timeseries of measurements. Figure 14 shows contours of  $\gamma$  in the  $x$ - $z$  plane along  
 343 the horizontal centerline of the plume for ground-level releases in simulations B5, SB2 and N.  
 344 Direct comparison of  $\gamma$  with data from experiments or other LES studies is difficult because  $\gamma$   
 345 depends on both source area relative to the characteristic length scale of turbulence (Fackrell &  
 346 Robbins, 1982) and the velocity of the source gas (Venkatram & Wyngaard, 1988). Nevertheless  
 347 the magnitude and shape of contours downwind of the source in Figure 14a are comparable to  
 348 convection tank data from the experiments of Willis & Deardorff (presented in Venkatram &  
 349 Wyngaard, 1988). The intermittency factor profile for the B5HR simulation was nearly identical  
 350 to Figure 14a, although the profile for SB2HR showed a weaker downwind gradient in the  
 351 intermittency factor near the surface than observed in SB2 (Figure 14b). A value of  $\gamma \geq 0.95$   
 352 downwind of a ground-level source in the neutral boundary layer (Figure 14c) is also consistent  
 353 with the wind tunnel data of Fackrell & Robbins (1982). The most interesting feature of Figure  
 354 14 is the gradient in  $\gamma$  that occurs near the surface downwind of sources in the convective  
 355 boundary layer (Figures 14a,b). That gradient may provide the ability to estimate the source-  
 356 sensor distance for sources upwind of an in situ concentration measurement in the daytime  
 357 atmospheric surface layer.

## 358 4. Discussion

359  
 360 WRF-LES is a useful and relatively accessible tool for simulating turbulence and passive scalar  
 361 dispersion in the atmospheric boundary layer. There are some real practical advantages of WRF-  
 362 LES when compared with other LES codes including, the regular/modular structure of the source  
 363 code, extensive documentation and example simulations, widely connected user base and helpful  
 364 support group. The most significant disadvantage of WRF-LES appears to be excessive



365 numerical diffusion in the dynamic solver which causes poor resolution of surface layer  
366 turbulence in shear driven boundary layers (Kirkil et al, 2012). We have shown that this problem  
367 can be mitigated by increasing the spatial resolution of the numerical grid (Figure 3), but the  
368 computational cost of that solution is usually prohibitive.

369  
370 WRF-LES accurately modeled mean dispersion parameters for passive scalars in the CBL.  
371 However, as the relative contribution of shear production to buoyant production increased (i.e.  
372  $L \rightarrow -\infty$ ) WRF-LES tended to underestimate the growth of the crosswind horizontal plume  
373 width as a function of downwind distance. This error was especially significant in the purely  
374 shear driven (neutral) turbulent boundary layer (Figure 6c). The underestimation of  $\sigma_y/z_i$  in the  
375 WRF-LES simulation N was caused by a bias in the horizontal eddy diffusivity coefficient for  
376 scalars ( $K_{\phi,h}$ ) because WRF-LES assumes  $K_{\phi,h} = 3K_{m,h}$ , where  $K_{m,h}$  is the horizontal eddy  
377 diffusivity for momentum and  $K_{m,h}$  is calculated by the SGS model for the momentum equation  
378 (Eq. 2). This claim is supported by the fact that a 10% increase in  $\sigma_y/z_i$  was observed when a  
379 source of identical volume was modeled in case NHR instead of case N. It is unlikely that the  
380 underestimation of  $\sigma_y(X)$  was related to poor resolution of the source because the bias increases  
381 with downwind distance where the plume is resolved by O(10) grid cells. The observed bias in  
382 the scalar field is also consistent with the under estimation of the streamwise and crosswind  
383 horizontal turbulent velocity variances in Figure 4. Future WRF-LES research should focus on  
384 improving parameterizations for the eddy diffusivity coefficients in the wall-layer where a zonal  
385 approach like the Two-Layer Model (TLM; Piomeli & Balaras, 2002) may be more appropriate  
386 for common grid spacing of O(10 m).

387  
388 That self-similarity was preserved in the mean concentration profiles downwind of the ground-  
389 level source in the neutral simulations (Figures 8a and 9) indicates that *relative* plume dispersion  
390 was modeled correctly. As an aside, replacing  $w_m$  by  $u_*$  results in better agreement between the  
391 neutral boundary layer data in Figure 6c (not shown;  $w_m = 1.0 \text{ m s}^{-1}$  see Eq. 4,  $u_* = 0.6 \text{ m s}^{-1}$  for  
392 the N and NHR cases), however, a direct comparison to Dosio et al (2003) is not possible  
393 because they did not provide values of the friction and convective velocities. Therefore, there is  
394 an issue with this commonly used velocity scale for forced convection not being an appropriate  
395 velocity scale for normalizing the downwind distance variable in neutral and near-neutral  
396 boundary layers

397  
398 One disadvantage of LES for dispersion simulations is that the minimum source size is limited  
399 by the spatial resolution of the numerical grid. Due to the high computational cost of LES, the  
400 smallest source volume that can be practically represented in full scale simulations of the ABL is  
401 around  $1000 \text{ m}^3$ . The effect of this limitation on concentration timeseries modeled with LES is a  
402 low pass filtering of the true signal. Weil et al (2012) addressed this issue by incorporating a  
403 stochastic, Lagrangian particle dispersion model into an LES of the CBL. Validation of scalar  
404 concentration fluctuations modeled with WRF-LES was also complicated by the fact that  
405 measures of concentration variability depend on source size, effluent velocity and grid  
406 resolution; all of which vary considerably among data presented in existing literature.  
407 Reasonable agreement was observed between concentration variance profiles calculated from the  
408 LES data of Henn & Sykes (1992) and data from the present study in the CBL (Figures 10 and  
409 11). However, for case N WRF-LES greatly overestimates the magnitude of the concentration  
410 variance in the neutral surface layer compared to wind tunnel experiments (Figure 12a). This

411 issue is likely related to poor turbulence resolution in the neutral surface layer, because smaller  
412  $\bar{u}_t$  causes less dispersion of concentration filaments which results in large concentration  
413 fluctuations near the surface and thereby increased concentration variance. Timeseries of scalar  
414 concentration in the atmospheric boundary layer are non-stationary and non-Gaussian. Therefore  
415 the intermittency factor ( $\gamma$ ) is a useful alternative metric to mean and variance for quantifying  
416 concentration variability, because the relationship between the low order moments of a  
417 timeseries of concentration measurements and the probability distribution for the instantaneous  
418 concentration magnitude is not straightforward (Yee & Chan, 1997).

## 419 **5. Conclusion**

420  
421 WRF-LES accurately modeled mean plume trajectories and concentration fields of passive scalar  
422 dispersion from continuous point sources. WRF-LES modeled statistics of concentration  
423 fluctuations in the convective boundary layer and the neutral boundary layer showed reasonable  
424 agreement with laboratory experiments and other LES. However, poor turbulence resolution near  
425 the surface in neutral atmospheric boundary layer simulations caused overestimation of  
426 concentration variance in the neutral surface layer. A gradient in the intermittency factor ( $\gamma$ ) was  
427 observed near the surface downwind of ground-level sources in the daytime convective boundary  
428 layer. This finding indicates that  $\gamma$  is a promising metric for the estimation of source-sensor  
429 distance in practical, local-scale source determination applications where the location of upwind  
430 sources within the concentration footprint of a measurement sensor is unknown. However, the  
431 relationship between  $\gamma$  and source-sensor range may depend on mesoscale forcing, topography  
432 and/or source area effects which would have to be quantified with site specific models.

## 433 **Acknowledgements**

434  
435  
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439 atmospheric boundary layer turbulence and numerical simulation of turbulent flows.

440 **Appendix A**

441

442 Mathematical definitions of the variables that define the trajectory of a scalar concentration field  
 443 downwind of the source (refer to Section 2.1 and Figure 1). Eqs. A1-A6 are reproduced from  
 444 Nieuwstadt (1992).  
 445

$$z_l = \frac{\iint_{A(x)} cz \, dy \, dz}{\iint_{A(x)} c \, dy \, dz}, \quad (\text{A1})$$

$$\bar{z} = \frac{\int_V cz \, dx \, dy \, dz}{\int_V c \, dx \, dy \, dz}, \quad (\text{A2})$$

$$s_z^2 = \frac{\int_V c(z - z_l)^2 \, dx \, dy \, dz}{\int_V c \, dx \, dy \, dz}, \quad (\text{A3})$$

$$m_z^2 = \frac{\int_V c(z_l - \bar{z})^2 \, dx \, dy \, dz}{\int_V c \, dx \, dy \, dz}, \quad (\text{A4})$$

$$\sigma_z^2 = s_z^2 + m_z^2 \quad (\text{A5})$$

$$\sigma_z'^2 = \frac{\int_V c(z - z_s)^2 \, dx \, dy \, dz}{\int_V c \, dx \, dy \, dz} \quad (\text{A6})$$

446

447  $z_l$  is the local (or instantaneous) plume centerline height,  $\bar{z}$  is the average plume centerline  
 448 height,  $s_z$  is the spreading component about the local centerline height and  $m_z$  is the meandering  
 449 component about the average centerline height,  $\sigma_z$  is the total vertical dispersion,  $\sigma_z'$  is the total  
 450 vertical dispersion relative to the source height.  $A(x)$  in Eq. A1 refers to the cross-sectional area  
 451 of the numerical domain in  $y$ - $z$  plane,  $V$  in Eqs. A2-A6 is the total volume of the numerical  
 452 domain and  $z_s$  is the source height. The same variables may also be used to define the crosswind  
 453 horizontal trajectory of the plume. Note that  $\sigma_y^2 = \sigma_y'^2$ , because  $y_s = 0$  by definition.

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## References

1. Andren A., Brown A.R., Graf J., Mason P.J., Moeng C-H., Nieuwstadt F.T.M., Schumann U., 1994, Large-eddy simulation of a neutrally stratified boundary layer: A comparison of four computer codes, *Quarterly Journal of the Royal Meteorological Society* 120, pp. 1457-1484.
2. Bou-Zeid E., Meneveau C., Parlange M., 2005, A scale-dependent Lagrangian dynamic model for large eddy simulation of complex turbulent flows, *Physics of Fluids* 17, pp. 025105.
3. California Environmental Protection Agency, Air Resources Board (CARB), "Cap-and-Trade Program", Available online at <<http://www.arb.ca.gov/cc/capandtrade/capandtrade.htm>>, Accessed March 18<sup>th</sup>, 2013.
4. Crosson E.R., 2008, A cavity ring-down analyzer for measuring atmospheric levels of methane, carbon dioxide, and water vapor, *Applied Physics B: Lasers and Optics* 92(3), pp. 403-408.
5. Deardorff J.W., 1970, A numerical study of three-dimensional turbulent channel flow at large Reynolds numbers, *Journal of Fluid Mechanics* 40(2), pp. 453-480.
6. Deardorff J.W., Willis G.E., 1984, Groundlevel concentration fluctuations from a buoyant and a non-buoyant source within a laboratory convectively mixed layer, *Atmospheric Environment* 18(7), 1297-1309.
7. Dosio A., Arellano J.V-G., Holtslag A.A.M., Builtjes P.J.H., 2003, Dispersion of a passive tracer in buoyancy- and shear-driven boundary layers, *Journal of Applied Meteorology* 42, pp. 1116-1130.
8. Fackrell J.E., Robins A.G., 1982, Concentration fluctuations and fluxes in plumes from point sources in a turbulent boundary layer, *Journal of Fluid Mechanics* 117, pp. 1-26.
9. Grant A.L.M., 1986, Observations of boundary layer structure made during the 1981 KONTUR experiment, *Quarterly Journal of the Royal Meteorological Society* 112, pp. 825-841.
10. Henn D.S., Sykes R.I., 1992, Large-eddy simulation of dispersion in the convective boundary layer, *Atmospheric Environment* 26A(17), pp. 3145-3159.
11. Kirkil G., Mirocha J., Bou-Zeid E., Chow F.K., Kosović B., 2012, Implementation and evaluation of subfilter-scale stress models for large-eddy simulation using WRF, *Monthly Weather Review* 140, pp. 266-284.
12. Moeng C-H., Sullivan P.P., 1994, A comparison of shear- and buoyancy-driven planetary boundary layer flows, *Journal of the Atmospheric Sciences* 51(7), pp. 999-1022.
13. Moeng C-H., Dudhia J., Klemp J., Sullivan P., 2007, Examining two-way grid nesting for large eddy simulation of the PBL using the WRF model, *Monthly Weather Review* 135, pp. 2295-2311.
14. Nieuwstadt F.T.M., 1992, A large-eddy simulation of a line source in a convective atmospheric boundary layer – I. dispersion characteristics, *Atmospheric Environment* 26A(3), pp. 485-495.
15. Piomelli U., Balaras E., 2002, Wall-layer models for large-eddy simulations, *Annual Review of Fluid Mechanics* 34, pp. 349-374.
16. Shaughnessy E.J., Morton J.B., 1977, Laser light-scattering measurements of particle concentration in a turbulent jet, *Journal of Fluid Mechanics* 80(1), pp. 129-148.
17. Skamarock W.C., Klemp J.B., 2008, A time-split nonhydrostatic atmospheric model for weather research and forecasting applications, *Journal of Computational Physics* 227(7), pp. 3465-3485.

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18. Sloop C., Novakovskaia E., Continuous GHG monitoring at local to statewide scales, 4<sup>th</sup> NACP All-  
Investigators Meeting, Albuquerque, New Mexico.
  19. Venkatram A., Wyngaard J.C. (Eds), 1988, Lectures on air pollution modeling, American Meteorological  
Society, Boston, 390 pgs.
  20. Weil J.C., Synder W., Lawson Jr. R.E., Shipman M.S., 2002, Experiments on buoyant plume dispersion in  
a laboratory convection tank, *Boundary Layer Meteorology* 102, pp. 367-414.
  21. Weil J.C., Sullivan P.P., Patton E.G., Moeng C-H., 2012, Statistical variability of dispersion in the  
convective boundary layer: ensembles of simulations and observations, *Boundary-Layer Meteorology* 145,  
pp. 185-210.
  22. Welp L.R., Keeling R.F., Weiss R.F., Paplawsky W., Heckman S., 2012, Design and performance of a  
Nafion dryer for continuous operation at CO<sub>2</sub> and CH<sub>4</sub> air monitoring sites, *Atmospheric Measurement  
Techniques Discussions* 5, pp. 5449-5468.
  23. Willis G.E., Deardorff J.W., 1976, A laboratory model of diffusion into the convective planetary boundary  
layer, *Quarterly Journal of the Royal Meteorological Society* 102(432), pp. 427-445.
  24. Willis G.E., Deardorff J.W., 1981, A laboratory study of dispersion from a source in the middle of the  
convectively mixed layer, *Atmospheric Environment* 15(2), pp. 109-117.
  25. Yee E., Chan R., 1997, A simple model for the probability density function of concentration fluctuations in  
atmospheric plumes, *Atmospheric Environment* 31(7), pp. 991-1002.