A non-parametric approach for co-analysis of multi-modal brain imaging data: Application to Alzheimer's disease

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**Abstract:**
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explicitly modeling the correlation between modalities. We applied our approach to structural and perfusion MRI data from an Alzheimer's disease (AD) study. Our approach identified areas of concordance, where both gray matter (GM) density and perfusion decreased together, and areas of dissociation, where GM density and perfusion did not decrease together. In conclusion, these results demonstrate the utility of this new non-parametric method to quantitatively assess the relationships between multiple modalities. (c) 2005 Elsevier Inc. All rights reserved.

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A non-parametric approach for co-analysis of multi-modal brain imaging data: Application to Alzheimer’s disease

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We developed a new flexible approach for a co-analysis of multi-modal brain imaging data using a non-parametric framework. In this approach, results from separate analyses on different modalities are combined using a combining function and assessed with a permutation test. This approach identifies several cross-modality relationships, such as concordance and dissociation, without explicitly modeling the correlation between modalities. We applied our approach to structural and perfusion MRI data from an Alzheimer’s disease (AD) study. Our approach identified areas of concordance, where both gray matter (GM) density and perfusion decreased together, and areas of dissociation, where GM density and perfusion did not decrease together. In conclusion, these results demonstrate the utility of this new non-parametric method to quantitatively assess the relationships between multiple modalities.

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Keywords: Permutation; Combining function; Multiple modalities; Conjunction

Introduction

Often in neuroimaging studies, images from multiple imaging modalities are acquired from the same set of subjects. Even within MRI, for example, high-resolution structural images are often acquired together with low-resolution images of brain chemistry, blood flow, or function. Nevertheless, images produced by different modalities are often analyzed separately. To address this issue, different analysis methods, including multivariate (Chen et al., 2004; McIntosh et al., 1996) and univariate (i.e., voxel-by-voxel) (Pell et al., 2004; Richardson et al., 1997) approaches, have been suggested. In general, multivariate methods are preferable for exploring patterns and interregional networks in multi-modal data because they place few restrictions on patterns of associations (McIntosh and Lobaugh, 2004). For example, Chen et al. (2004) implemented a partial least square technique (McIntosh et al., 1996) for co-analyzing PET and structural MRI data. However, statistical inference based on multivariate methods often holds only in a global test for the entire brain and has limited ability to localize signals (Kherif et al., 2002; Worsley et al., 1997).

On the other hand, although model-based univariate methods make assumptions about associations, they are sometimes better suited for statistical inference. Several model-based univariate methods have been suggested for statistical inference of multiple modality images. In one approach (Richardson et al., 1997), images from different modalities were scaled to the same intensity range, and a linear regression model was fitted with different modalities modeled by indicator variables. Differences between modalities were assessed by contrasting these modality variables within the linear model (Richardson et al., 1997; Van Laere and Dierckx, 2001). Another approach in multi-modal co-analysis is the conjunction method, which identifies areas where significant changes overlap in multiple t statistic maps. This method, widely used in functional neuroimaging analyses (Friston et al., 1999; Nichols et al., 2005), was extended to multiple imaging modalities to identify conjunction (Pell et al., 2004).

A limitation of linear model and conjunction approaches is that these methods only identify one specific type of relationship between different modalities. The linear model approach only identifies areas where changes in one modality are larger than that of another, while the conjunction method only identifies the overlap of significant changes across modalities. Neither of these methods can be generalized to other types of relationships, including both positive and negative correlation.

Therefore, to overcome this shortcoming, we propose a general and flexible univariate non-parametric method, implementing co-analysis and identifying cross-modality relationships with combin-
ing functions and permutation testing (Hayasaka and Nichols, 2004). Furthermore, this method enables statistical inference without explicitly modeling the correlation across different imaging modalities (Hayasaka and Nichols, 2004; Lazar et al., 2002; Pesarin, 2001), since the cross-modality correlation is implicitly accounted for.

We evaluated the performance of this approach in a simulation-based validation. We also applied this approach to a multiple modality imaging data set of Alzheimer’s disease (AD) (Johnson et al., 2005) which is known to alter both brain structure as well as brain function (Karas et al., 2003; Matsuda et al., 2002; Minoshima et al., 1997). We investigated local changes in gray matter (GM) volume and cerebral perfusion, obtained by T1-weighted structural MRI and arterial spin labeling (ASL) perfusion MRI, respectively. Since changes in these two modalities do not necessarily occur in the same locations (Matsuda et al., 2002), we identified areas where structural and perfusion changes occur together (concordance) and areas where only one of these is observed but not the other (dissociation).

**Methods**

**Combining functions**

Our approach combines information from separate \( t \) images by a combining function, a function to combine multiple tests into a single test (Lazar et al., 2002; Pesarin, 2001), which is subsequently used in a statistical test. For example, for two modalities each with a \( t \) statistic image, \( S_1 \) and \( S_2 \), a combining function is defined, at an arbitrary voxel \( v \in \{(x, y, z)\} \), in a form

\[
W(v) = f(S_1(v), S_2(v))
\]

where \( S_1(v) \), \( S_2(v) \), and \( W(v) \) correspond to voxel values of \( t \) images \( S_1 \) and \( S_2 \), and the combining function image \( W \), respectively. The function \( f \) is chosen so that a large value of \( W(v) \) corresponds to a relationship of interest between \( S_1(v) \) and \( S_2(v) \). For instance, let \( W(v) = S_1(v) \times S_2(v) \), the product of two \( t \) values, which becomes large when both \( S_1(v) \) and \( S_2(v) \) increase or decrease together. When thresholded, \( W(v) \) defines a hyperbolic-shaped critical region in a 2D space of \( S_1(v) \) and \( S_2(v) \), sensitive to concordance between them, as seen in Fig. 1. By thresholding the combining function image \( W \), areas where the relationship of interest occurs are identified. For interested readers, we present some suggestions of combining functions for different scenarios in Appendix A.

**Permutation test framework**

Since the voxel value distribution of a combining function image is often unknown, we employ a permutation test for statistical inference (Holmes et al., 1996; Nichols and Holmes, 2002). Furthermore, when a combining function and a permutation test are used together, the correlation between \( t \) images is implicitly accounted for (Hayasaka and Nichols, 2004; Pesarin, 2001).

The permutation test works by generating the distribution of a test statistic based on random re-assignment, or permutation, of data labels. In our method, it operates in several steps. As an example, let us consider a two-group comparison setting on two imaging modalities, as illustrated in Fig. 2. First, group labels (A or B) are randomly reassigned to images of both modalities 1 and 2. Based on this random reassignment, two \( t \) statistic images, \( S_1 \) and \( S_2 \), are calculated on modalities 1 and 2, respectively. From these \( t \) images, a combining function image \( W \) is calculated. Although each voxel value \( W(v) \) can be considered as a test statistic, for multiple comparison correction, a summary statistic describing topological characteristics of \( W \) image needs to be selected. Such statistic – local maximum, cluster size, or some other statistics – is used in the subsequent test as a test statistic, rather than each voxel value \( W(v) \). Only the largest of such test statistics is recorded in each permutation, in order to control the family-wise error (FWE) rate to correct for multiple comparisons (Hayasaka and Nichols, 2003; Holmes et al., 1996). The entire process is repeated for a sufficient number of times, typically between 1000 and 3000 permutations for sufficient confidence in the permutation distribution, each with a different permutation of As and Bs. In the last permutation, the data labels are correctly assigned: As for A images and Bs for B images. Finally, an empirical distribution of the test statistic is generated by creating a histogram of all the recorded statistics. Corrected \( P \) values can be assessed by comparing the test statistic from the final permutation, the one with the correct group labels, to this empirical distribution.

**Simulation**

To examine the performance of our method, we carried out a simulation-based validation. In each of 1000 realizations in this simulation, two sets of twenty \( 36 \times 36 \times 20 \) voxel images were generated. Each of the two sets was thought to be from one modality. To 10 images in each set, a sphere-shaped signal of radius \( r = 8 \) voxels was added. The locations of the signals were different in two modalities, with 3 different settings for the distance between the center of the signals: 0, \( r/2 \), and \( r \) (see Fig. 3). Larger distance means less overlap between the signals. Within each modality, a \( t \) image was calculated from a two-sample \( t \) test comparing images with and without the signal. The
resulting \( t \) images from the two modalities, \( S_1 \) and \( S_2 \), with large \( t \) values at the locations of the respective signals, were combined by a combining function. The resulting combining function image was used as a statistic image in a permutation test with 100 permutations. In the permutation test, the cluster mass (Bullmore et al., 1999) was used as a test statistic, which is defined as the integration of the image intensity above the cluster defining threshold, calculated at each cluster. The cluster mass statistic is robust and sensitive to various signals, including localized high-intensity signals and spatially extended signals (Hayasaka and Nichols, 2004). The number of rejections at 0.05 significance level (FWE corrected) was recorded to calculate the power.

We employed two combining functions in the simulation to assess the spatial relationship between signals in the two modalities. To assess the overlap of signals, we considered the concordance combining function \( W_c(v) \) defined as

\[
W_c(v) = \begin{cases} 
S_1(v) \times S_2(v) & \text{if } S_1(v) > 0 \text{ and } S_2(v) > 0 \\
0 & \text{otherwise}
\end{cases}
\]

(1)

This combining function is sensitive for large values of \( S_1(v) \) and \( S_2(v) \) occurring together. Critical regions of the concordance combining function are shown in Appendix A. We chose cluster defining thresholds to be 8 for \( W_c(v) \). To assess the signal

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**Fig. 2.** A schematic of the permutation test with a combining function. First, group labels (A/B) are randomly reassigned to images (1). Then based on this permutation of labels, \( t \) images are calculated separately (2). From the \( t \) images, a combining function is calculated (3), and the test statistic is recorded on the resulting combining function image (4). The entire process is repeated, each with a different permutation of labels (5). In the last permutation, data labels are correctly assigned (6). Finally, an empirical distribution of the test statistic is generated by creating a histogram of the test statistics (7). \( P \) values can be assessed by comparing the results from step (6) to the distribution found in step (7).

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**Fig. 3.** Locations of the signals in modalities 1 and 2. The distance between the centers of the signals were set to 0, \( r/2 \), and \( r \), where \( r = 8 \) voxels is the radius of each signal.
occuring only in modality 1, we considered the dissociation combining function \( W_d(v) \), defined as

\[
W_d(v) = S_1(v) - (iS_2(v))^\eta.
\]

(2)

The width parameter \( \lambda \), a positive number, controls the width of the critical region, whereas the shape parameter \( \eta \), a positive integer, controls the shape of the critical region. A large (small) value of \( \lambda \) produces a narrow (wide) critical region, and a large (small) value of \( \eta \) widens (narrows) the base of the critical region, producing a rectangular (wedge) shaped critical region. The parameter \( \eta \) is multiplied by 2 to ensure concise critical regions. The critical regions corresponding to various values of \( \lambda \) and \( \eta \) are found in Appendix A. In this simulation, we used different values of \( \lambda (\lambda = 1/3, 1/2, \text{and } 2/3) \) and \( \eta (\eta = 1, 2, \text{and } 3) \). This combining function \( W_d(v) \) is sensitive to large values of \( S_1(v) \) and near-zero values of \( S_2(v) \) occurring together. The function \( W_d(v) \) can be seen as the value of \( S_1(v) \) penalized by the term \((iS_2(v))^\eta\), for \( S_2(v) \) deviating from 0 (i.e., a change in modality 2). We chose the cluster-defining threshold to be 3 for \( W_d(v) \).

In a multiple-modality imaging study, it is possible that images in two different modalities have different smoothness despite smoothing. Thus, we considered a case where two imaging modalities have the same smoothness (FWHM = 6 and 6 voxels), and different smoothness (FWHM = 3 and 6 voxels for modalities 1 and 2, respectively).

**Application**

Our non-parametric method was applied to a co-analysis of GM volume changes in T1-weighted structural MRI and perfusion changes in ASL perfusion MRI. Twenty patients with a clinical diagnosis of probable AD according to the NINCDS-ADRDA (National Institute of Neurological and Communicative Disorders and Stroke–Alzheimer’s Disease and Related Disorder’s Association) criteria (McKhann et al., 1984) and 22 cognitively normal (CN) controls were included in this study. Their characteristics are summarized in Table 1.

**Image acquisition and processing**

All the subjects were scanned on a Siemens 1.5T Vision scanner (Erlangen, Germany). T1-weighted structural images were acquired using an MPRAGE (magnetization prepared rapid acquisition gradient-echo) sequence with TR/TE/TI = 10/7/300 ms, FA = 15°, and slice thickness = 1.4 mm. Perfusion weighted images (PWI) were acquired using the DIPLOMA (double inversion) sequence with TR/TE/TI = 10/7/300 ms, FA = 15°, and slice thickness = 1.4 mm. Perfusion weighted images were acquired with a single-shot gradient-echo EPI (echo-planar imaging) sequence. Details on the PWI acquisition can be found elsewhere (Johnson et al., 2005). Each PWI was co-registered to its corresponding T1-weighted image and corrected for partial volume effect (PVE) using a three-compartment model (Müller-Gärtner et al., 1992; Quarrelli et al., 2004).

T1-weighted and perfusion images were spatially normalized to a study-specific template. The study-specific template was created by averaging all the centered and aligned T1-weighted images. The T1-weighted images were also segmented (Ashburner and Friston, 1997; Ashburner and Friston, 2000), smoothed (6 mm isotropic Gaussian), and averaged to create tissue specific templates for GM, white matter (WM), and cerebrospinal fluid (CSF). Using these templates, T1-weighted images were normalized, segmented, and modulated according to the optimized voxel-based morphometry (VBM) protocol (Good et al., 2001) in SPM2 (Wellcome Department of Imaging Neuroscience; London, UK). Of the segmented images, only GM probability images were used in the subsequent analyses. The normalization parameters from the optimized VBM protocol (Ashburner and Friston, 1999; Good et al., 2001), both affine (12 parameters) and non-linear (10 × 9 × 10 discrete cosine basis functions), were applied to perfusion images to achieve normalization in the same template space. Normalized perfusion images were re-sliced to 2 × 2 × 2 mm voxel size for better use of spatial information and smoothed with a 12-mm Gaussian kernel to account for imperfection in co-registration and normalization. The GM images were similarly smoothed and re-sliced.

**Statistical analysis**

For each of the GM and perfusion data sets, a two-sample \( t \) test was performed separately to compare AD < CN. The GM \( t \) test was adjusted for age and total intra-cranial volume as covariates in an ANCOVA (analysis of covariance) model. In the resulting \( t \) image \( S_{GM} \), a large \( t \) value corresponded to GM loss in AD. The perfusion \( t \) test was adjusted for age and reference perfusion as covariates in an ANCOVA model. The mean perfusion value of the motor cortex was chosen as reference perfusion for each subject because this region is relatively spared from AD pathology (Braak et al., 1999). In the resulting \( t \) image \( S_{perf} \), a large \( t \) value corresponded to reduced perfusion, or hypoperfusion, in AD.

In the permutation test, we applied the concordance combining function \( W_c(v) \) and the dissociation combining function \( W_d(v) \) to two \( t \) images from the GM and perfusion \( t \) tests. In particular, we defined

\[
U(v) = \begin{cases} 
S_{GM}(v) \times S_{perf}(v) & \text{if } S_{GM}(v) > 0 \text{ and } S_{perf}(v) > 0 \\
0 & \text{otherwise} 
\end{cases}
\]

(3)

\[
V(v) = S_{perf}(v) - (iS_{GM}(v))^\eta
\]

(4)

\[
W(v) = S_{GM}(v) - (iS_{perf}(v))^\eta
\]

(5)

The combining function \( U(v) \) is sensitive to concordance between GM loss and hypoperfusion. On the other hand, \( V(v) \) and \( W(v) \) are sensitive to dissociation between GM and perfusion.
changes; while $V(v)$ is sensitive to hypoperfusion without GM change, $W(v)$ is sensitive to GM loss without perfusion change. Fig. 4 shows examples of critical regions defined by these combining functions in terms of $S_{GM}(v)$ and $S_{per}(v)$. In (4), we chose $\lambda = 0.5$ so that the critical region spans roughly from $S_{GM}(v) = -2$ to 2, and a typical $t$ test fails to reject the null at $P = 0.05$ uncorrected significance level in such a critical region. Also in (4), we chose $\eta = 2$ for a wider critical region than a typical parabola at its base, enhancing sensitivity in that area. In (5), the width and shape parameters were similarly chosen as $\lambda = 0.5$ and $\eta = 2$. For interested readers, more discussions on parameters $\lambda$ and $\eta$, as well as the shape of critical regions, can be found in Appendix A.

Each of these combining function images was used as a statistic image in the permutation test. In the permutation test, the cluster mass was used as a test statistic. To implement the permutation test, we used a modified version of SnPM2b package (SnPM Authors, the University of Michigan; Ann Arbor, MI, USA), a non-parametric toolbox for SPM2. For each permutation test, 1000 permutations were carried out. Since the accuracy of $P$ value estimates does not improve dramatically by running more permutations (e.g., standard error (SE) = 0.007 for 1000 permutations compared to SE = 0.004 for 3000 permutations, for a cluster with corrected $P = 0.05$ (Hayasaka and Nichols, 2003)), we limited the test to 1000 permutations in order to conserve time and disk space.

Sensitivity analysis

A sensitivity analysis was carried out in order to understand how much the analysis results are influenced by the choice of the width and shape parameters $\lambda$ and $\eta$ in the dissociation combining functions (4) and (5). In particular, a bootstrap analysis (Efron and Tibshirani, 1993) was performed in order to examine how the distribution of the largest cluster mass changes when $\lambda$ and $\eta$ are changed. In each of 100 bootstrap samples generated, combining functions (4) and (5) were calculated with different values of $\lambda$ ($\lambda = 1/4, 1/3, 1/2, 2/3, or 3/4$) and $\eta$ ($\eta = 1, 2, 3, 4, 5$), and the largest cluster mass was recorded for each combination of $\lambda$ and $\eta$. The same cluster defining thresholds were used as in the actual analyses above.

Computing environment

The data analyses were performed on a Dell PC with a 3GHz Pentium 4 processor and 1GB of RAM, using MATLAB 6.5 (MathWorks; Natick, MA, USA). For each permutation test, computation time was under 20 min. The simulation and sensitivity analyses were performed on a Linux workstation using MATLAB 6.5.

Results

Simulation

Fig. 5 shows the plots of power for $W_c(v)$ and $W_d(v)$ for different signal settings, with two modalities having the same smoothness (a) and different smoothness (b).

The concordance combining function was sensitive when the overlap between the signals was large. However, the power decreased as the distance increased and the area of overlap decreased. The concordance combining function seemed slightly more powerful when two modalities have different smoothness.

The dissociation combining function became more sensitive when the overlap between the signals became smaller. It appeared that, the larger the value of $\lambda$, more powerful the test became. In terms of $\eta$, the combining function was slightly more sensitive when $\eta = 1$ compared to $\eta = 2$ or 3. However, the difference in power between $\eta = 2$ and $\eta = 3$ was negligible. These findings were consistent in both smoothness settings (same or different smoothness), and the difference in power between these two settings was negligible.

These results indicate that the concordance and dissociation combining functions are calibrated to detect the relationship of interest between the two modalities.

Separate GM and perfusion analyses

The results from the separate GM and perfusion $t$ tests are shown in Fig. 6a, in which areas of GM loss (green) and hypoperfusion (red) are shown. A liberal threshold was used in these results ($P < 0.001$ uncorrected) to give an overview of regional patterns of GM loss and hypoperfusion. The pattern of GM loss was consistent with similar VBM studies of AD (Baron et al., 2001; Karas et al., 2003), with large areas of GM loss seen in the bilateral inferior and posterior parietal areas, as well as in the bilateral posterior cingulate cortices (PCc). The pattern of hypoperfusion was consistent with similar studies using PET and SPECT (Matsuda et al., 2002; Minoshima et al., 1997), with large areas of hypoperfusion in the right PCc and in the right posterior parietal area. Also a large area of hypoperfusion was
seen in the right middle frontal gyrus with some extension into the superior frontal gyrus.

Combining function thresholds

A scatter plot of all the voxel values of \( S_{GM} \) and \( S_{perf} \) is shown in Fig. 7, with the cluster defining thresholds for the concordance and dissociation analyses overlaid. Each of these thresholds was chosen so that it was low enough for clusters to form, yet high enough for spatial localization of clusters.

Concordance (GM loss and hypoperfusion)

Areas of concordance, GM loss and hypoperfusion occurring together, are shown in Fig. 6b \((P < 0.05 \text{ corrected})\). Large clusters for concordance were mainly found in the bilateral PCC with some extension into the precunei, as well as in the right posterior parietal area. Some small clusters were also found in the left posterior parietal lobe and in the bilateral superior prefrontal areas. These concordance clusters identified the areas of overlap between GM loss and hypoperfusion seen in Fig. 6a.

Dissociation (hypoperfusion without GM change)

Areas of dissociation, hypoperfusion without GM change, are shown in Fig. 6c \((P < 0.05 \text{ corrected})\). A large dissociation cluster was found in the right PCC and precuneus, located superior to the concordance cluster found earlier. Another large dissociation cluster was found in the right middle frontal gyrus with some extension into the superior frontal gyrus.

Dissociation (GM loss without perfusion change)

Areas of dissociation, GM loss without perfusion change, are shown in Fig. 6d \((P < 0.05 \text{ corrected})\). Large dissociation clusters were found in the bilateral inferior parietal areas, and a few small dissociation clusters were seen in the bilateral PCC and precunei inferior to the concordance cluster found earlier.

Sensitivity analysis

Fig. 8 shows plots of the median of the largest cluster mass from bootstrap samples, as well as the inter-quartile range, for various values of the width parameter \( \lambda \) (top) and the shape parameter \( \eta \) (bottom). These results are from the dissociation combining function for hypoperfusion without GM change (4), but the results are similar for the combining function for GM loss without perfusion change (5) (not shown). From the figure, it can be seen that a change in \( \lambda \) influenced the distribution of the largest cluster mass. A small value of \( \lambda \) produced larger clusters, possibly due to a wide critical region. On the other hand, a large value of \( \lambda \) produced smaller clusters, possibly due to a narrow
critical region. The value of $\eta$ seems to have only a slight influence on the analysis results.

**Discussion**

The proposed new method quantitatively assesses different relationships between GM and perfusion changes, using a simple and flexible non-parametric framework consisting of a combining function and a permutation test. In contrast to previous methods for analysis of multi-modality imaging, our approach is highly versatile; different cross-modality relationships are examined using the same permutation test framework just by selecting appropriate combining functions. Even though different combining functions were used in different analyses, no explicit modeling of voxel value distribution and cross-modality correlation was needed, as these were modeled implicitly in a combining function and a permutation test. Implicit modeling of the inter-modality correlation was particularly an important property in our analyses, since it
is reasonable to assume that perfusion and GM volume are somewhat correlated (Ibañez et al., 1998; Kanetaka et al., 2004; Matsuda et al., 2003).

In our concordance analysis, we found GM loss and hypoperfusion (despite PVE correction) in the posterior parietal lobe and PCC. Thus, hypoperfusion in these areas is greater than that expected from GM loss (Ibañez et al., 1998). From our dissociation analyses, we found hypoperfusion without GM change in the PCC (superior to the concordant region) and middle frontal gyrus. Such hypoperfusion may be due to deafferentation of these regions resulting from GM loss in other remotely connected brain regions (Braak et al., 1999; Meguro et al., 2001; Mielke et al., 1996). We also found GM loss without perfusion change in inferior parietal areas and in the PCC inferior to the concordant region. In these areas, perfusion loss may not be reduced beyond the level expected from GM loss. Overall, our findings were consistent with the results of a previous neuroimaging study using MRI and SPECT (Matsuda et al., 2002), in which areas of reduced GM volume and cerebral perfusion were observed in the posterior part of the brain, while hypoperfusion was more apparent than GM loss in frontal brain regions. Further studies are needed to investigate the clinical significance of these findings.

Our approach can be easily implemented in co-analyses of other MRI imaging modalities or even extended to other modalities such as PET or SPECT imaging. Furthermore, this method can be generally extended to more than two modalities. For instance, in addition to GM loss and hypoperfusion in our example, an investigator might be interested in functional decline associated with these structural as well as physiological changes. In such case, the investigator may examine concordance among three modalities, structural MRI, ASL perfusion MRI, and BOLD functional MRI, by using a combining function

\[ X(v) = S_{GM}(v) \times S_{perf}(v) \times S_{fMRI}(v) \]

where \( S_{fMRI} \) corresponds to a t image associated with functional decline among AD patients. This combining function is sensitive for GM loss, hypoperfusion, and functional decline occurring together. Our method is also useful in longitudinal studies to capture changes of different modalities over time, which might provide deeper insight in disease progression.

In this approach, there are obstacles and limitations that should be mentioned. First, as in other multi-modality imaging methods, co-registering and normalizing different imaging modalities are not simple, since some imaging modalities are more prone to distortions and artifacts than other modalities. A limitation specific to our approach is that selection of combining functions is arbitrary and subjective. A combining function is chosen according to a user’s interest, and there is an infinite number of possible combining functions to choose from. For our dissociation combining functions \( V(v) \) and \( W(v) \), for example, there are many possibilities for the choice of parameters \( \lambda \) and \( \eta \) in (4) and (5). Furthermore, in addition to a polynomial form as seen in these functions, there are other possible forms of combining functions, such as trigonometric, logarithmic, or exponential functions, and combinations thereof. Clearly it is impossible to evaluate all possible combining functions objectively, but a combining function can be chosen from a handful of candidates. As it can be seen from
In conclusion, we have developed a non-parametric method for co-analysis of multi-modal brain imaging data and demonstrated its effectiveness in structural and perfusion MRI data. This approach can be implemented in co-analyses of other MRI, PET, or SPECT imaging modalities, improving analyses and interpretation of findings in multi-modal imaging studies.

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Appendix A. Examples of combining functions

To facilitate selection of appropriate combining functions, we present examples of combining functions for four possible scenarios. In a study with two modalities 1 and 2, let $S_1$ and $S_2$ be the $t$-statistic images based on the contrast of interest, respectively. Then we consider situations where our interests are:

1. Changes or effects in the same direction in both modalities
2. Changes or effects in opposite directions
3. Changes or effects observed in one of the modalities, but not the other
4. Comparing the magnitude of changes or effects between modalities

In our simulation and sensitivity analysis, we can evaluate sensitivity and robustness of combining functions from a simulation and a sensitivity analysis, respectively. Interested readers can also choose a combining function from the ones suggested in Appendix A according to their hypotheses. Another limitation specific to our approach is lack of weighting mechanism to correct for variability difference between modalities. For example, in our concordance combining function $U(v)$, there is no weighting for $S_{GM}(v)$ or $S_{perf}(v)$, even though $S_{GM}(v)$ seems to be less variable than $S_{perf}(v)$ (see Fig. 7). A difference in degrees of freedoms could also result in variability difference between modalities. To correct this problem, some sort of weighting mechanism (Hayasaka and Nichols, 2004) could be employed, but determining optimal weights could raise another challenge.
A.1. Changes in the same direction

To identify changes or effects in the same direction in both modalities 1 and 2, we need to define a combining function which becomes large when both $S_1$ and $S_2$ are highly positive or negative at the same time. In such cases, we should choose combining functions whose critical regions are in the top-right quadrant or in the bottom-left quadrant, as seen in Fig. 9a. If we are interested in both $S_1$ and $S_2$ being positive (negative), then the critical region should be in the top-right (bottom-left) quadrant. The concordance combining function

$$X(v) = S_1(v) \times S_2(v)$$

is a possible combining function in this setting. Critical regions of this combining function can be limited to positive changes in the top-right quadrant by constraining $S_1(v) > 0$ and $S_2(v) > 0$ (Fig. 9b), or to negative changes in the bottom-left quadrant by constraining $S_1(v) < 0$ and $S_2(v) < 0$. Another possible combining function is the conjunction combining function

$$X(v) = \min(S_1(v), S_2(v)).$$

This is a non-parametric equivalent of the conjunction method mentioned in the Introduction (Nichols et al., 2005). This combining function identifies the overlap of areas $S_1(v) > w$ and $S_2(v) > w$, for an arbitrary threshold value $w$ (Fig. 9c).

A.2. Changes in opposite directions

To identify changes or effects in opposite directions in modalities 1 and 2, we need to define a combining function which becomes large when either $S_1$ or $S_2$ is highly positive, and the other is highly negative at the same time. In such cases, we should choose combining functions whose critical regions are in the top-left quadrant or in the bottom-right quadrant, as seen in Fig. 10. Critical regions on the bottom-right quadrant are sensitive to $S_1(v)$ being highly positive and $S_2(v)$ being highly negative occurring together, while critical regions on the top-left quadrant are sensitive to $S_1(v)$ being highly negative and $S_2(v)$ being highly positive occurring together. This can be achieved by negating either $S_1(v)$ or $S_2(v)$ in combining functions (6) and (7).
For example, by negating $S_1(v)$, the concordance combining functions (6) becomes

$$X(v) = -S_1(v) \times S_2(v). \quad (8)$$

Similar to (6), critical regions for (8) can be limited to the bottom-right quadrant ($S_1(v) > 0$ and $S_2(v) < 0$) or top-left quadrant ($S_1(v) < 0$ and $S_2(v) > 0$), as seen in Figs. 11a and b, respectively. The critical regions for the conjunction combining function are in the bottom-right quadrant if $S_2(v)$ is negated (9), and in the top-left quadrant if $S_1(v)$ is negated (10),

$$X(v) = \min(S_1(v), -S_2(v)) \quad (9)$$

$$X(v) = \min(-S_1(v), S_2(v)) \quad (10)$$

as seen in Figs. 11c and d, respectively.

### A.3. Changes in one modality only

If we are interested in, for instance, changes occurring in modality 1 but not in modality 2, we need to choose a combining function whose critical regions are along the horizontal axis toward highly positive value of $S_1(v)$ (Fig. 12). Such combining function is sensitive to highly positive values of $S_1(v)$ (i.e., a large change in modality 1) and near-zero values of $S_2(v)$ (i.e., little change in modality 2). The dissociation combining function is suitable for such situation, which is defined as

$$X(v) = S_1(v) - (\lambda S_2(v))^\eta \quad (11)$$

where $\lambda$ is the width parameter, and $\eta$ is the shape parameter. The width parameter $\lambda$, a positive number, controls the width of the critical region; a large (small) value of $\lambda$ produces a narrow (wide) critical region (Fig. 13a). The shape parameter $\eta$, a positive integer, controls the shape of the critical region; a large (small) value of $\eta$ widens (narrows) the base of the critical region, producing a rectangular (wedge) shaped critical region (Fig. 13b). The parameter $\eta$ is multiplied by 2 so that the critical region is concave. Though it is not feasible to perform an exhaustive search to determine the optimal values of $\lambda$ and $\eta$, it is possible to decide these values among a list of possible values a priori by a simulation as demonstrated above.

### A.4. Comparing changes between modalities

If we are interested in comparing changes between two modalities, we can choose combining functions whose critical region is above or below the $S_1(v) = S_2(v)$ line (Fig. 14), depending on the inequality ($S_1(v) < S_2(v)$ or $S_1(v) > S_2(v)$, respectively). For example, if we hypothesize that $S_1(v)$ is larger than $S_2(v)$ (i.e., changes in modality 1 is larger than that of modality 2), then we can define a combining function

$$X(v) = S_1(v) - S_2(v). \quad (12)$$

This is a non-parametric equivalent of Richardson et al.’s (1997) method discussed in the Introduction. Fig. 14 shows examples of critical regions for this combining function.

This combining function is also useful in a longitudinal study setting. For example, if images are acquired on two different time points, then $r$ images at the 1st and 2nd time points can be compared using (12). One advantage of such approach over a paired $t$ test is that covariates, such as neuropsychological test scores, can vary across the two time points.

### References


