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## Fixed Beamline Optimization for Intensity Modulated Carbon-Ion Therapy

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### Abstract

A major obstacle for the adoption of heavy ion therapy is the cost and technical difficulties to construct and maintain a rotational gantry. Many heavy ion treatment facilities instead choose to construct fixed beamlines as a compromise, which we propose to mitigate with optimized treatment couch angle. We formulate the integrated beam orientation and scanning spot optimization problem as a quadratic cost function with a group sparsity regularization term. The optimization problem is efficiently solved using fast iterative shrinkage-thresholding algorithm (FISTA). To test the method, we created the fixed beamline plans with couch rotation (FBCR) and without couch rotation (FB) for intensity modulated carbon-ion therapy (IMCT) and compared with the ideal scenario where both the couch and gantry have 360 degrees of freedom (GCR). FB, FBCR, and GCR IMCT plans were compared for ten pancreas cases. The FBCR plans show comparable PTV coverage and OAR doses for each pancreas case. In conclusion, the dosimetric limitation of fixed beams in heavy ion radiotherapy may be largely mitigated with integrated beam orientation optimization of the couch rotation.

### Index Terms—

beam orientation; carbon ion; gantry; heavy ion; optimization

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## I. Introduction

Carbon-ion therapy has been increasingly garnering attention worldwide due to its superior physical dose distributions and high relative biological effectiveness (RBE). Compared to photon and electron beams, proton and carbon ion beams are more conformal to tumors because they deliver most of their dose in well-defined Bragg peaks, therefore possessing the ability to localize their deposition of energy within deep-seated tumors [1–3]. About 85% of cancer patients receiving particle therapy are irradiated with protons, which have physical advantages compared to photons, but a similar biological response [2]. Carbon ions, however, have a steeper lateral fall-off and smaller penumbra than proton beams, which offers a better potential for targeting tumors that are close to critical structures [4]. The radiobiological effectiveness (RBE) of carbon ion rise substantially along the beam direction and reaches its maximum near the Bragg peak, further increasing the therapeutic ratio compared with the proton beams whose RBE varies more moderately. Heavy ions are particularly attractive for treating radioresistant tumors, and carbon ion therapy may promote immune response and reduce angiogenesis and metastatic potential [2,5,6]. Through clinical studies, carbon ion beams have been able to reduce treatment time and toxicities [1], making it the desirable treatment modality in terms of efficiency and dosimetry.

However, the access to carbon-ion therapy is greatly hampered by its prohibitive cost, engineering challenges and space requirement, despite its unique potential to treat hypoxic and radioresistant tumors. Among the facilities of carbon-ion therapy, the fully rotational gantry is especially expensive, complex and space consuming due to the large magnets needed to bend the high energy carbon ion beams with high magnetic rigidity. Compared with protons, to reach the same depth, the magnetic rigidity of carbon ions is 2.5 times greater, demanding corresponding more powerful and larger magnets for beam bending and steering. As a result, the carbon gantry in the Heidelberg Ion Therapy (HIT) facility occupies 22 m long and 14 m high space and weights a total of 600 tons [7]. Equipment and building costs, in particular, are extremely high [8,9]. The gantry weight can be reduced using superconducting magnets. For example, the superconducting carbon ion gantry at the National Institute of Radiological Sciences (NIRS) in Japan weighs 300 tons [10,11] due to the use of superconducting magnets, which are costly to build and operate, and still significantly heavier than a proton gantry. Further engineering challenges include maintaining the targeting accuracy with gantry rotation. There are limited existing solutions available for equipment and treatment planning software troubleshooting by suppliers.

The current debate at many cancer treatment centers in relation to carbon ion therapy is whether the installation of a gantry is feasible. Compared with the gantry systems, fixed-beam port systems significantly simplify the system design for carbon ion therapy and are more widely employed in most carbon ion centers for treatment delivery at the moment. However, the fixed beam line design has been considered a significant compromise in flexibility and achievable dosimetry. Once built, the directions of fixed beamlines cannot be modified. The unclear magnitude of performance degradation and lack of systematic approach to mitigate the compromise could dampen the enthusiasm for carbon ion system adoption.

Carbon ion centers are employing the use of a single horizontal beam ( $90^\circ$ ), some with an additional vertical beam ( $0^\circ$ ) [12,13]. Kosaki et al. compared intensity modulated proton therapy (IMPT) plans for the treatment of skull base meningioma and found that excellent dose distributions can still be achieved with one fixed beam [13]. To determine if there is a superior fixed beamline configuration for a typical two beamline configuration, Koom et al. performed a dosimetric comparison among seven fixed beam angles ( $340^\circ$ ,  $315^\circ$ ,  $0^\circ$ ,  $20^\circ$ ,  $45^\circ$ ,  $90^\circ$ ,  $180^\circ$ ) in the prone position with carbon ion pencil beam scanning for pancreatic cancer[14]. CTV or GTV coverage among the 7 beams did not widely differ. Dose to the descending duodenum were high with  $45^\circ$  and  $90^\circ$ , but lower for the ascending duodenum compared to the  $180^\circ$  beam.  $20^\circ$  and  $315^\circ$  seemed to be better for the stomach. Some facilities add a rotating couch to up to  $45^\circ$  as a non-gantry solution [15]. The addition of a  $45^\circ$  beam to the  $90^\circ$  beam in our study would allow for variability in the couch rotation, while keeping the value of a vertical beam.

The current study attempts to answer a different question using a carbon ion system with 360 degrees as the reference, which is the potential to mitigate or eliminate the dosimetric disparity with optimized combination of the fixed beam and couch angles. Although the combination has a relatively limited solution space compared with a full gantry system, it still includes more than a hundred available beam directions for optimization.

To achieve the optimization goal, we exploited the couch rotation freedom with an automated IMCT beam orientation optimization (BOO) method.

## II. Methods

### A. Beam Geometry

The gantry-based plan starts with 1162 non-coplanar beams uniformly distributed across the  $4\pi$  steradians with  $6^\circ$  separation between adjacent beams combining the gantry and couch rotational degrees-of-freedom. Beam screening is performed to remove beams with infeasible energies or impractical entries into the body, such as those going through the head or feet, leaving 420 beams in the candidate set. For the fixed-beamline plans, we select by hand a total of 90 beams, 30 from the  $90^\circ$  gantry angle, and 60 from the  $45^\circ$  angle. From this, we compared plans with no couch kick against plans with couch angles ranging from  $0^\circ$  to  $360^\circ$  with  $6^\circ$  interval. Note that the possible gantry angles for fixed beam plans, with couch rotation (FBCR) and without (FB), are not an exact subset of the angles for the gantry couch rotation (GCR) plan as shown in Fig. 1 due to discretization and finite spacing between beams.

For each candidate beam, carbon ion pencil beam dose calculation for the scanning spots covering the PTV and a 5mm margin was performed using matRad [16,17], a MATLAB-based 3D treatment planning toolkit. The physical dose calculation matrix  $A$ , which includes all candidate beams, was generated in this calculation, with an isotropic resolution of 2.5 mm, along with  $\alpha$  and  $\beta$  matrices for carbon ion, characterizing the radiosensitivity of the tissue based on the linear quadratic model for survival fraction. Our optimization was formulated to select one or two beams from the candidate beam pool.

## B. Beam Orientation Optimization

Beam orientation optimization (BOO) was performed for GCR, FB, and FBCR plans under the same optimization framework [18,19]. Assuming  $\mathcal{B}$  is the set containing all the feasible candidate beams, the BOO problem is described as follows:

$$\begin{aligned} & \underset{\mathbf{x}}{\text{minimize}} \sum_{k \in \mathcal{T}} \alpha_k \|A_k \mathbf{x} - p_k\|_2^2 + \sum_{k \in \mathcal{O}} \alpha_k \|(A_k \mathbf{x} - q_k)_+\|_2^2 + \sum_{b \in \mathcal{B}} \lambda_b \|\mathbf{x}_b\|_2^{1/2} \\ & \text{subject to } \mathbf{x} \geq 0 \end{aligned} \quad (1)$$

where  $\mathbf{x}_b$  is a vector that represents the scanning spot intensities for each candidate beam  $b$ , and the optimization variable  $\mathbf{x}$  is the concatenation of all the vectors  $\mathbf{x}_b (b \in \mathcal{B})$ . The dose calculation matrix  $A$  includes all the candidate beams along the column direction, with the product of  $A$  and  $\mathbf{x}$  being dose to each voxel.  $\mathcal{T}$  is the set including the target volumes and  $\mathcal{O}$  is the set including the organs at risk (OAR). Once a fluence map was obtained, the plans were weighted with RBE values calculated for each structure  $k$  from the  $\alpha$  and  $\beta$  matrices, using the following model [20]:

$$-\ln(S) = (\beta_C D_C + \alpha_C) D_C$$

$$D_{bio} = \sqrt{-\frac{\ln(S)}{\beta_x} + \left(\frac{\alpha_x}{2\beta_x}\right)^2} - \frac{\alpha_x}{2\beta_x} \quad (2)$$

where  $D_C$  is fractional carbon physical dose,  $\alpha_x$  and  $\beta_x$  are biological parameters of the LQ model for photon as a reference radiation and  $\alpha_C$  and  $\beta_C$  are the parameters for carbon ion. For pancreatic cancer,  $\alpha_x$  is  $0.015 \text{ Gy}^{-1}$  and  $\beta_x$  is  $0.0016 \text{ Gy}^{-2}$  [21]. For the gastrointestinal tract and spinal cord, respectively,  $\alpha_x$  values are  $[0.087, 0.0445] \text{ Gy}^{-1}$  and  $\beta_x$  values are  $[0.013, 0.0135] \text{ Gy}^{-2}$  [22].

The first two terms in (1) represent dose fidelity. The first term penalizes any dose deviation from prescription dose  $p_k$  for target  $k$  to ensure a homogeneous physical dose distribution in the target. The second term encourages any dose in the OAR  $k$  to not exceed the maximum allowable dose for that OAR,  $q_k$ . The last term  $\sum_{b \in \mathcal{B}} \lambda_b \|\mathbf{x}_b\|_2^{1/2}$  is an L2,1/2-norm group sparsity term. We set the value for the weighting hyperparameter,  $\lambda_b$ , for each beam such that most  $\mathbf{x}_b$  are penalized to be identically zero. Subsequently, most of the candidate beams were turned off, leaving only one or two beams active. Weighting for group sparsity is turned off when further fluence map optimization is performed once beams are selected.

Carbon ion beam angle selection and fluence map optimization were performed simultaneously to generate a plan with acceptable dosimetry. FISTA, an accelerated proximal gradient method known as the Fast Iterative Shrinkage-Thresholding Algorithm [23] was used to solve this non-differentiable problem.

## C. Patient Evaluations

We compared the GCR, FB, and the proposed FBCR method for ten pancreatic cases initially planned for photon radiotherapy. The original prescription dose was 33 Gy with selective simultaneous integrated boost (SIB) dose to 40 and 50 Gy. Since the prescription dose is not used for carbon ion and the purpose of the study was not to compare with the

photon doses, all plans were prescribed to a total dose of 52.8 GyRBE in 12 fractions [24]. The goal for the PTV dose was to cover 90% of the PTV with 95% of the prescription dose. The target volumes and average spot count per beam for each patient are shown in Table I. For all plans, biological dose (GyRBE) was evaluated. Similar structure weighting was used across plans to ensure unbiased comparison. For each pancreatic case, PTV homogeneity, D95%, and mean dose to the PTV, as well as the maximum dose received by 2cc of the stomach, bowel and duodenum was evaluated. The PTV homogeneity index (HI) is defined as  $D95\%/D5\%$ . The mean and maximum doses for OARs were also evaluated. Maximum dose is defined as the dose to 2% of the structure volume, D2%, following the recommendation by ICRU 83 [25]. The upper clinical goal for all gastrointestinal tract (GI) organs was 46 GyRBE. Maximum dose to the spinal cord limit was 30 GyRBE [24].

### III. Results

#### A. Runtime and Optimization of Beams

The dose calculation and optimization processes were performed on an 8-core CPU workstation. To calculate the dose and biological parameter matrices for all candidate beams for each approach, the MATLAB Parallel Computing Toolbox was used to accelerate the computation. The times spent on dose calculation and BOO are listed in Table II along with the gantry and couch angles chosen during beam selection. Since the number of candidate beams for the fixed beam approaches were significantly reduced, dose calculation time was cut down by a factor of about 5. The FBCR plans have the potential to reduce beam orientation and fluence map optimization times with the pancreatic cases. For difficult FBCR plans, optimization may require a larger regularization parameter for the group sparsity term and possibly more time than a GCR plan to force convergence from 90 beams to only one or two beams while maintaining dosimetric integrity. While the addition of more beams will reduce the effort, we require that all plans select 1–2 beams for ease of delivery and comparison. In general, total effort for GCR plans takes on average 28 more minutes than FBCR plans. FBCR only takes about 30 more seconds compared to FB to select beams.

#### B. Dose Comparison

The optimized FBCR delivery is compared with the GCR and FB deliveries. An isodose comparison in the transverse, coronal, and sagittal planes can be viewed in Fig. 2. Overall, PTV coverage and OAR sparing varies between plans. A dose-volume histogram representing patient F is shown in Fig. 3 to compare biological dose structure-by-structure.

Fig. 4 shows PTV homogeneity (HI), mean, and maximum biological dose to the PTV for all plans. PTV coverage was significantly better with GCR and FBCR compared to FB. Paired t-test was performed between GCR and FBCR, showing p-values of [0.19, 0.29, 0.12] for HI, mean, and maximum biological dose, respectively. The result indicates that the PTV metric differences are statistically insignificant between GCR and FBCR. On the other hand, the comparison between FBCR and FB had p-values of [0.02, 0.02, 0.35], indicating significantly higher HI and mean PTV doses with FBCR. Table III lists OAR statistics for the gastrointestinal tract and spinal cord, which are lowest, in general, with the GCR plan. In all plans in which GCR met the clinical standard of less than 46 GyRBE to the GI

tract, FBCR was able to do so as well. Compared with FB plans, FBCR reduced bowel, duodenum, and stomach doses by [27%, 12%, 23%] and GCR reduces the doses by [35%, 16%, 43%]. P-values for bowel, duodenum, and stomach were [0.02, 0.16, 0.05] between GCR and FBCR and [0.07, 0.33, 0.12] between FBCR and FB, showing mostly minor improvements in dose from FB to FBCR and from FBCR to GCR. For liver and kidneys, mean dose difference between all plans is less than 1 GyRBE. All plans met the clinical limit of 30 GyRBE for the maximum dose to the spinal cord. We have shown a significant improvement of FBCR over FB plans. The OAR sparing gains by FBCR were [77%, 75%, 53%] of that by GCR for the bowel, duodenum, and stomach, respectively.

#### IV. Discussion

We performed the study to investigate the dosimetric implications of fixed beamlines vs. gantry IMCT plans for the pancreatic cancer treatment. We adopted our previously published beam orientation optimization method to solve a new problem, which is the carbon ion beam orientation optimization with fixed beamlines. The new problem can be considered a subproblem of the full BOO problem with limited degrees of freedom. The additional degree of freedom reduced the gap in solution spaces between the gantry and fixed beamline plans. The large solution space precludes effective manual beam orientation selection. We solved the integrated BOO and scanning spot optimization problems using group sparsity regularization for both the GCR and FBCR plans. We showed that the dosimetric difference between gantry and fixed beamline IMCT may be substantially narrowed if the couch rotation can be fully exploited by solving the optimization problem.

In this study, we specifically choose  $45^\circ$  and  $90^\circ$  polar beamlines for our fixed-beam approach. While it is possible that changing the combination of beamline angles may result in tumor coverage and normal tissue sparing, this effect can be dependent on patient characteristics and local anatomy configurations. In theory,  $90^\circ$  beam allow sampling of the most widespread of the spherical space in combination with the couch rotation. Smaller angles would reduce the radiological path lengths for oblique beams, but too small a polar angle would result in a collapsed cone and degenerated solution space. Therefore, the  $45^\circ$ – $90^\circ$  orientations seem to be a well-balanced and generalizable combination. A rigorous conclusion for the fixed-beamline orientation selection problem needs to be drawn based on a statistical analysis of the dosimetry for many more patient types and cases.

Besides limited patient cases, another limitation is that geometrically undesired beams and beams of infeasible energies were only partially excluded from the 1162-beam candidate set. These beams with long radiological pathlength are eliminated in BOO due to undesired geometry. Simulations that model three-dimensional collisions of large gantries with the patient and couch for different treatment zones have been performed for proton [26], but to our knowledge, no studies of this kind have yet been published for carbon ion gantries. Once carbon beam log data is available, more accurate beam screening should be performed for carbon gantries to assess the impact on beam selection and resulting dosimetry.

Solutions to the problem of having limited beam angles with fixed beamlines for carbon ion include rotating the couch along the long axis [27]. Couch rotation is commonly

used in clinical practice. With robotic couch, sub-millimeter movement accuracy has been demonstrated [28]. However, the couch motion may increase the probability of patient shift, which can be managed by immobilization and surface, X-ray, and tomographic imaging monitoring.

Due to the prohibitively long time required to calculate dose for 1162 candidate beams using Monte Carlo, the current study uses an analytical method, which is acceptable for dose comparison [19,29], but may have inaccuracies for further studies with biological objective functions due to its inability to account for fragmentation or secondary particles [30–32]. Either fast CPU- or GPU-based Monte Carlo for carbon-ion radiation therapy may be better suited for that goal [33,34]. Physical dose conformality is our current optimization objective with an estimate of variable RBE applied. This is likely an oversimplification for the carbon ion beams. Because of the drastic changes in RBE along the beam path, different beams may be selected if more accurate RBE is modeled within the BOO problem. For instance, RBE-weighted dose using the local effect model (LEMIV), repair-misrepair-fixation (RMF) model, or microdosimetric kinetic model (MKM) [35,36], can be used to explore the effectiveness of a biological dose optimization framework with the fixed beamline approach.

## V. Conclusions

We show that the dosimetry compromise due to the fixed beamlines vs. a full gantry for carbon-ion therapy can be largely mitigated for pancreatic cases with the beam orientation optimization exploiting the couch rotation freedom. With further investigation on other disease sites, this work indicates the potential to significantly simplify gantry design for carbon-ion therapy, thus overcoming a major hurdle in availing this technology.

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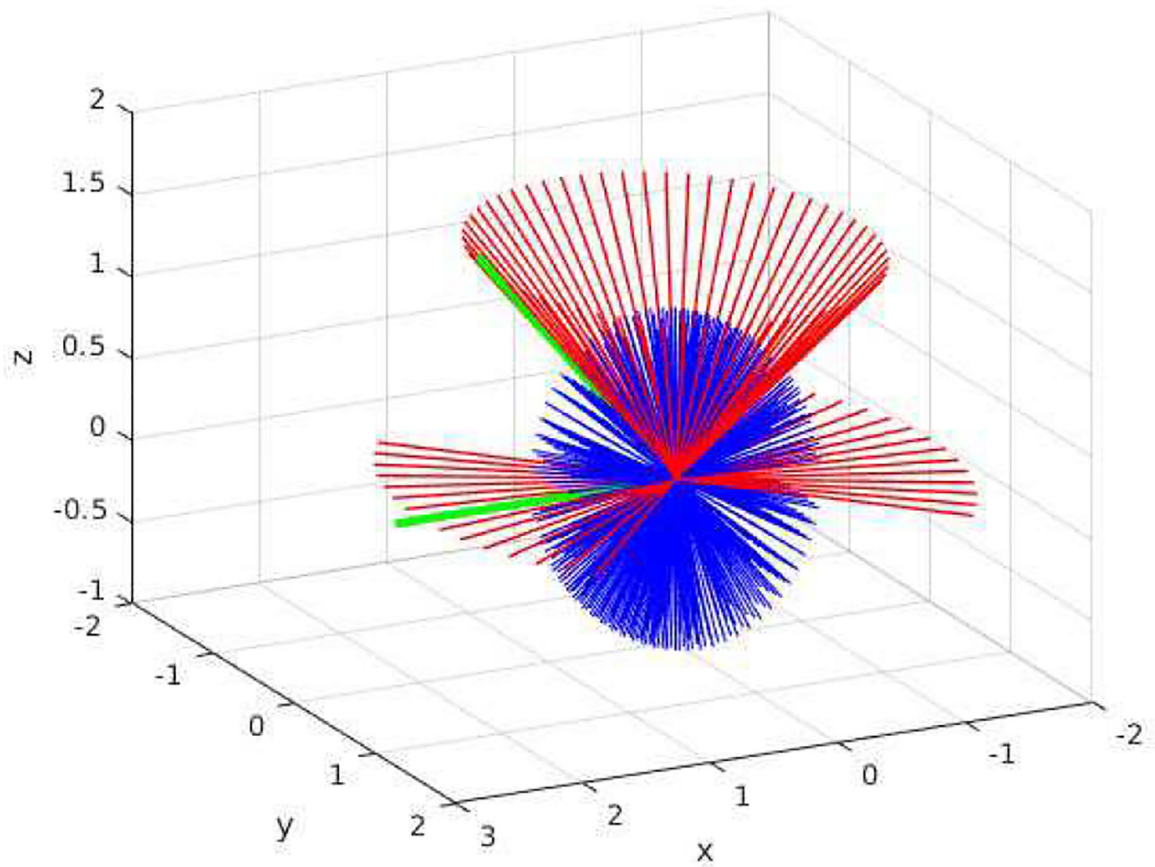
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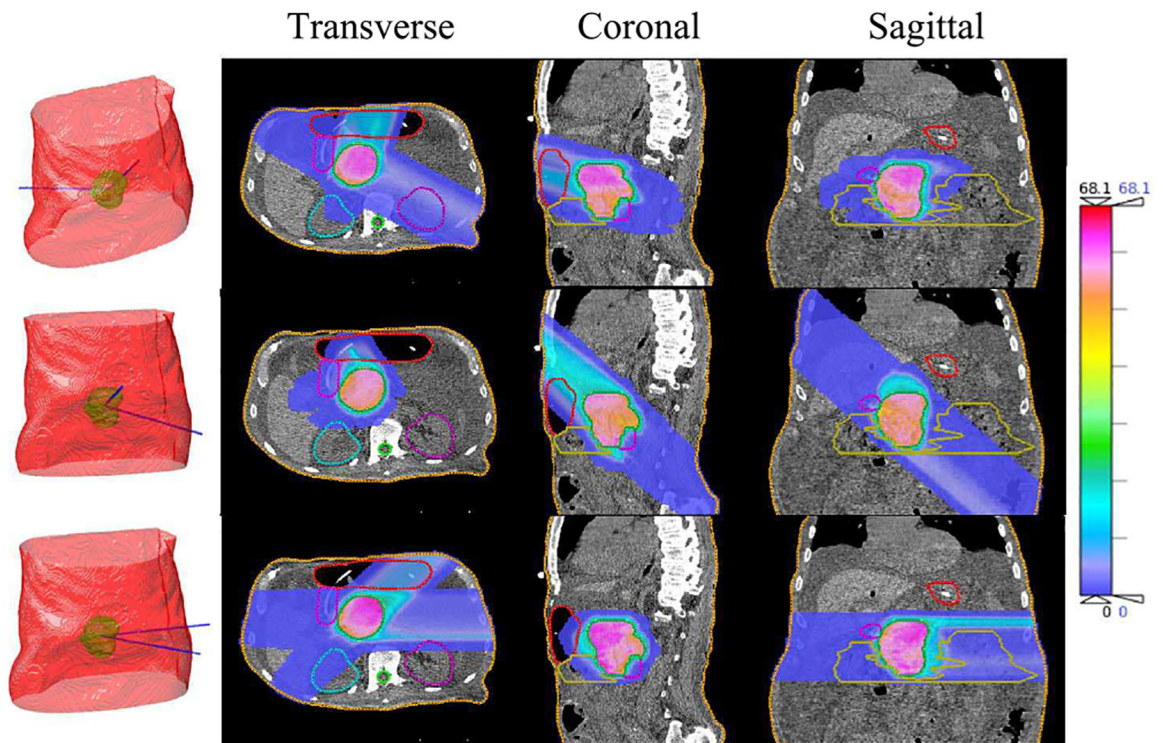


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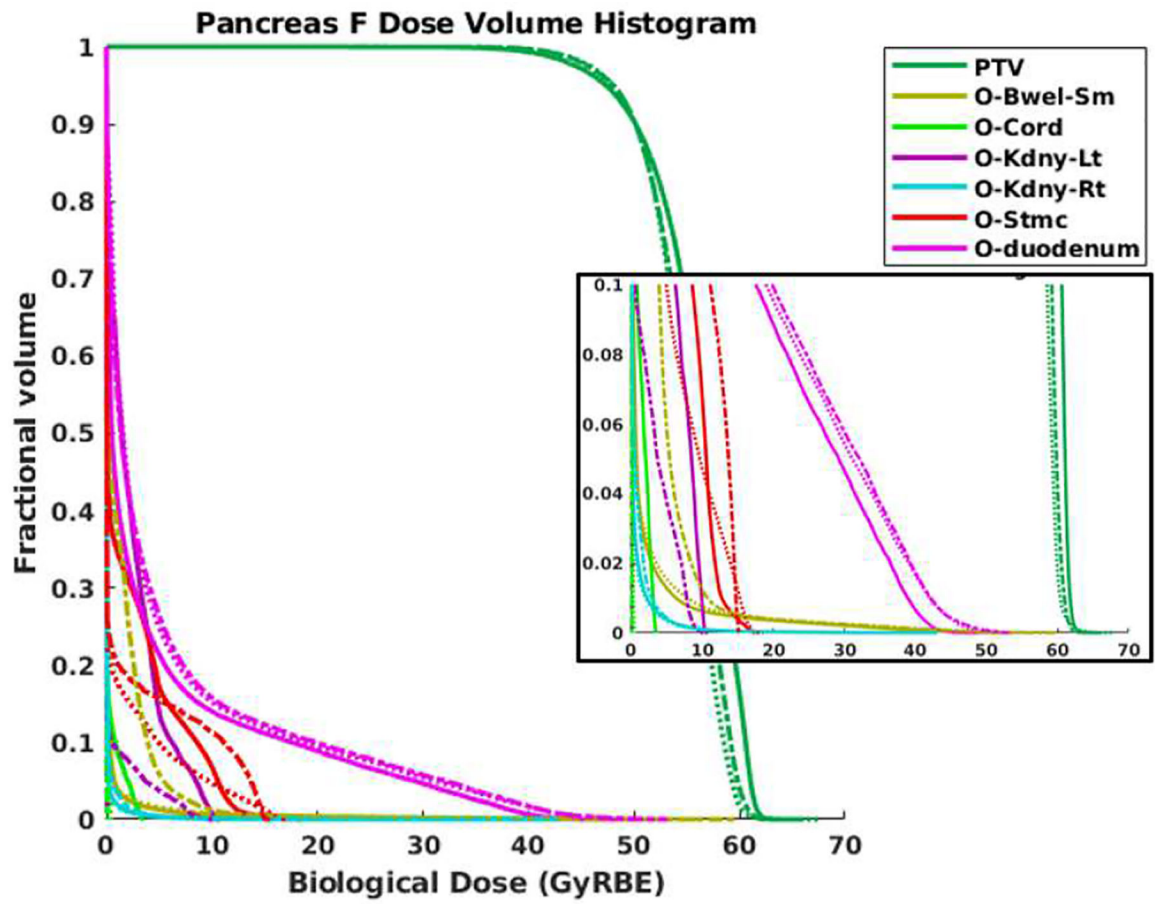
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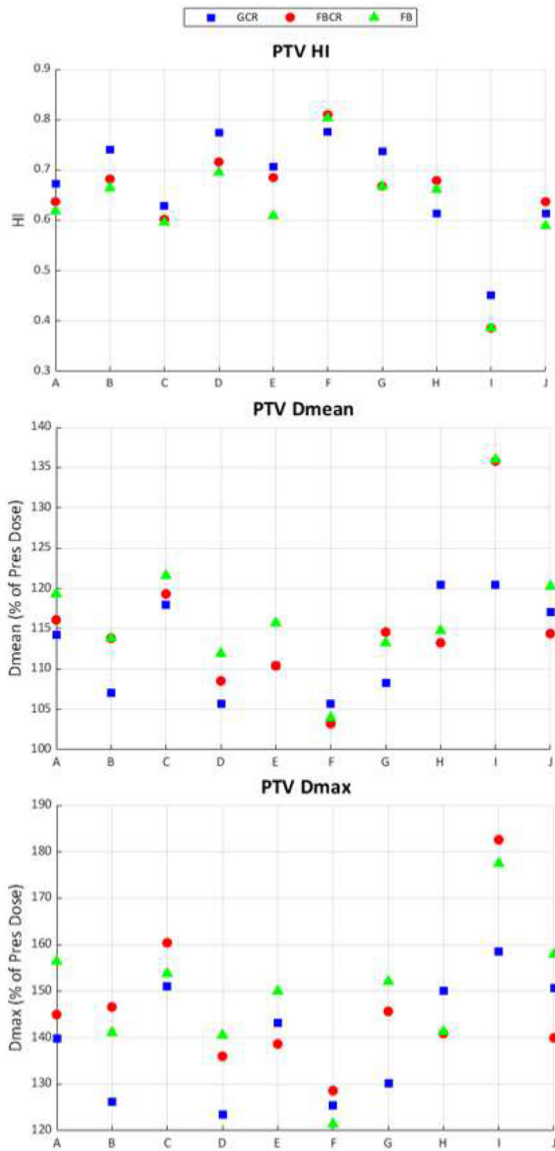
**Fig. 1.** Candidate beams for GCR (blue), FBCR (red), and FB (green). The gantry-based plan includes 420 non-coplanar beams. FBCR includes 60 couch angles from the 45° and 30 from the 90° polar angles, and the FB plan includes one 45° and one 90° gantry angle, both with couch at 0°.



**Fig. 2.** Beam orientation along with isodose comparison between GCR (top), FBCR (middle), and FB (bottom) plans for pancreas patient F.



**Fig. 3.** Dose-volume histogram for pancreas patient F. Solid lines represent the GCR, dotted lines represent FBCR, and dashed lines represent FB.



**Fig. 4.** PTV statistics for all pancreatic cases. Dmax and Dmean are biological dose values represented as a percent of the prescribed dose to the PTV volume.

**TABLE I**

PTV volumes, and average number of spots per beam for each case.

Case	PTV Volume (cc)	Average Number of Spots per Beam
A	50.4	2044
B	128.2	4538
C	48.9	2037
D	41.0	1737
E	99.2	3475
F	268.0	7937
G	8.7	562
H	62.2	2393
I	91.3	3317
J	60.1	2309

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**TABLE II**

Dose calculation and optimization times (minutes) with beam angles (degrees) selected for each plan. For GCR plans, both gantry and couch angles were determined by the BOO algorithm. For FBCR plans, couch angles were determined by BOO, and for FB plans, both beams were fixed.

	Dose Calculation Time, BOO Time (min)			Beams Selected (gantry, couch)		
	GCR	FBCR	FB	GCR	FBCR	FB
A	15.5	3.1	3.1	(210,39)	(45,246)	(45,0)
	2.9	2.0	1.2	(140,29)	(90,222)	(90,0)
B	55.1	12.1	12.1	(140,331)	(45,54)	(45,0)
	6.6	3.0	2.8	(35,33)	(45,174)	(90,0)
C	14.0	2.8	2.8	(205,46)	(45,276)	(45,0)
	2.3	2.5	1.1	(25,346)	(90,222)	(90,0)
D	14.5	2.9	2.9	(54,0)	(45,114)	(45,0)
	2.4	0.9	0.8	(322,340)	(45,354)	(90,0)
E	36.3	7.6	7.6	(25,314)	(45,78)	(45,0)
	5.2	3.9	2.1	(149,348)	(45,294)	(90,0)
F	117	19.0	19.0	(135,26)	(45,258)	(45,0)
	12.9	5.6	5.4	(220,331)	(90,42)	(90,0)
G	5.6	1.1	1.1	(153,332)	(45,126)	(45,0)
	0.5	0.3	0.4	(315,334)	(45,144)	(90,0)
H	29.9	6.3	6.3	(125,345)	(90,215)	(45,0)
	3.0	2.9	1.9	(198,270)	(90,330)	(90,0)
I	28.7	6.8	6.8	(330,39)	(45,198)	(45,0)
	4.9	2.8	2.1	(161,288)	(45,276)	(90,0)
J	17.3	4.0	4.0	(155,346)	(45,342)	(45,0)
	2.6	1.4	1.2	(347,333)	(90,138)	(90,0)



**TABLE III**

OAR dose results for the pancreatic cases.

	Structure	GCR	FBCR	FB
A	Bowel	<b>3.5</b>	7.1	13.7
	Duodenum	<b>1.0</b>	2.6	3.1
	Stomach	<b>0.2</b>	0.6	3.9
	Spinal Cord	5.8	0.2	<b>0.1</b>
B	Bowel	<b>0.1</b>	0.8	10.4
	Duodenum	<b>36.0</b>	40.0	37.4
	Stomach	<b>0.1</b>	<b>0.1</b>	<b>0.1</b>
	Spinal Cord	1.9	<b>0.1</b>	<b>0.1</b>
C	Bowel	<b>0.1</b>	<b>0.1</b>	<b>0.1</b>
	Duodenum	<b>40.8</b>	43.0	42.4
	Stomach	<b>0.3</b>	0.8	4.7
	Spinal Cord	9.6	<b>0.1</b>	<b>0.1</b>
D	Bowel	<b>0.1</b>	<b>0.1</b>	<b>0.1</b>
	Duodenum	5.1	<b>2.9</b>	4.9
	Stomach	0.2	<b>0.1</b>	0.3
	Spinal Cord	<b>0.1</b>	<b>0.1</b>	<b>0.1</b>
E	Bowel	<b>6.1</b>	9.3	13.7
	Duodenum	24.4	<b>24.0</b>	24.6
	Stomach	<b>25.0</b>	27.4	27.6
	Spinal Cord	14.5	<b>0.1</b>	<b>0.1</b>
F	Bowel	<b>31.7</b>	34.2	35.2
	Duodenum	<b>34.1</b>	36.5	37.2
	Stomach	15.1	16.2	<b>14.9</b>
	Spinal Cord	3.6	<b>0.1</b>	<b>0.1</b>
G	Bowel	0.4	<b>0.1</b>	4.6
	Duodenum	<b>7.6</b>	8.6	12.9
	Stomach	<b>0.7</b>	2.2	4.6
	Spinal Cord	2.1	<b>0.1</b>	<b>0.1</b>
H	Bowel	49.1	49.6	<b>47.8</b>
	Stomach	<b>0.3</b>	1.4	0.7
	Spinal Cord	5.5	<b>0.1</b>	<b>0.1</b>
I	Bowel	<b>25.5</b>	30.0	28.6
	Stomach	<b>6.8</b>	12.5	22.3
	Spinal Cord	11.7	0.3	<b>0.1</b>
J	Bowel	<b>28.5</b>	28.9	30.4
	Duodenum	<b>12.4</b>	<b>12.4</b>	13.3
	Stomach	<b>0.1</b>	<b>0.1</b>	<b>0.1</b>
	Spinal Cord	11.1	<b>0.1</b>	<b>0.1</b>

Maximum biological dose received by 2cc (D2cc) of bowel, duodenum, and stomach and maximum biological dose (Dmax) to spinal cord. All values are reported in GyRBE.