

# Opportunistic Cooperations: A New Communication Approach for MANETs

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**Abstract**—We introduce a collaboration-driven approach to the sharing of the available bandwidth in wireless ad hoc networks, which we call *opportunistic cooperation*. Transmissions are divided in frequency and codes according to nodal locations, and successive interference cancellation (SIC) is used at receivers to allow them to decode and use all transmissions from strong interfering sources. We show that both the link’s Shannon capacity and the per source-destination throughput scale like  $O(n^{\frac{\alpha}{2}})$  (upper-bound) and  $\Omega[f(n)]$  (lower-bound), for  $n$  nodes in the network, a path loss parameter  $\alpha > 2$ , and  $1 \leq f(n) < n^{\frac{\alpha}{2}}$ .

## I. INTRODUCTION

Communication protocols used in wireless ad hoc networks today are meant to support reliable communication among senders and receivers that are *competing* with one another for the use of the shared bandwidth. This “competition-driven” view of bandwidth sharing has had profound implications on network architectures and methods used to access the channel and disseminate information. Gupta and Kumar [1] showed that, in a wireless connected network with static nodes, the throughput for each node degrades as the number of nodes increases under the competition-driven view of networking. That is, it scales as  $\Theta(1/\sqrt{n \log(n)})$ ,<sup>1</sup> where  $n$  is the number of nodes in the network.

Grossglauser and Tse [2] analyzed a two-hop, single-relay forwarding scheme for MANETs in which a source passes a packet to a relay that in turn delivers it to the destination when the two nodes are close to each other. This and many subsequent studies on how to make MANETs scale by using mobility [2], [3], [4], consider each transmission as competing with all the other concurrent transmissions in the network. However, because a relay cooperates with a source by storing the source’s packet until it is close enough to the intended destination, the throughput of MANETs can be increased.<sup>2</sup>

Recently, Toumpis and Goldsmith [5] have shown that the capacity regions for ad hoc networks are significantly increased when multiple access schemes are combined with spatial reuse (i.e., multiple simultaneous transmissions), multihop routing (i.e., packet relaying), and SIC, even without performing power

control. Also, SIC circuits with simple implementation and low complexity have been introduced recently [6], and code division multiple access (CDMA) [7] and global positioning system (GPS) [8] technologies have been already integrated into a single IC chip [9].

In this paper, we present an integrated approach to cooperative bandwidth sharing in MANETs and propose what we call *opportunistic cooperation*.<sup>3</sup> We show that with opportunistic cooperation, nodes access the available channel(s) and forward information across a MANET in such a way that concurrent transmissions become useful at destinations or relays. Hence, sender-receiver pairs collaborate, rather than compete, with others. Therefore, a better network performance is possible.

Section II summarizes the basic network model that has been used recently to analyze the capacity of wireless networks [1], [2], [3], [4], [10]. Section III describes the *opportunistic cooperation* implementation. Section IV presents the link’s Shannon capacity, the per source-destination throughput, and the bandwidth requirement. Section V concludes the paper.

## II. NETWORK MODEL

The term *cell* denotes the set of nodes located inside a defined area of the network. The *receiver range* of a node is defined as the radius, measured from the node, which contains all other nodes of the same cell. The *cluster* associated with a given node is the set of cells reached by the receiver range of this node.

Our assumptions are consistent with prior work [1], [2], [10]. Also, in this paper, nodes are considered to have SIC capability.

The modeling problem we address is that of a MANET in which  $n$  mobile nodes move in a unit square area. To simplify our analysis, we assume that cells have square shapes, each with area equal to  $a(n) = \frac{1}{\phi n}$ , in which  $\phi \in (0, 1)$  is the cell area parameter of the network. We consider that the communication occurs only among those nodes that are close enough (i.e., in same cell), so that interference caused by farther nodes is low, allowing reliable communication. In other words, the receiver chooses the closest nodes because they present the best channel, in a respective order, due to the assumption of the simple path propagation model, i.e., the receiver takes advantage of

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<sup>1</sup>  $\Omega$ ,  $\Theta$  and  $O$  are the standard order bounds.  $\log(\cdot)$  is the natural logarithm.

<sup>2</sup> In [2], the per source-destination throughput scales as  $\Theta(1)$ .

<sup>3</sup> The term “opportunistic” is used here to indicate that the number of nodes cooperating with one another in a cell during a communication session is a random variable.

multiuser diversity [11]. Our model resembles the one introduced by Grossglauser and Tse [2], who consider a packet to be delivered from source to destination via one-time relaying.

The position of node  $i$  at time  $t$  is indicated by  $X_i(t)$ . Nodes move according to the *uniform mobility model* [3], in which the steady-state distribution of the mobile nodes is uniform.

Each node simultaneously transmits and receives data during a communication time period, through different frequency bands, since each data link is assumed half-duplex. This period of communication is called a *communication session*. Furthermore, each session is divided into two parts. A neighbor discovery protocol is used by nodes during the first part to obtain their neighbors information (e.g., node identification (ID)), and the transmission of data is performed during the second part. Each node has a unique ID that does not change with time, and each node can simultaneously be a source (or relay) while transmitting and a destination (or relay) while receiving, during a session. Each source node picks a single arbitrary destination to whom it sends packets.

### III. OPPORTUNISTIC COOPERATION

In *opportunistic cooperation*, many nodes transmit concurrently to many other neighbor nodes, and all such transmissions are decoded. Thus, a node may concurrently send to and receive from many nodes. Since full-duplex data communication in the same frequency band is not practical, we present an example of how *opportunistic cooperation* can be implemented with a scheme based on frequency division multiple access (FDMA) and CDMA that supports many-to-many communication.

#### A. Bandwidth Allocation

We use two types of channels. *Control* channels are used by nodes to obtain such information as the identities of strong interference sources, the data packets expected by destinations, and the state of data channels (by virtue of training sequences). Nodes employ conventional digital transceivers for the control channels. *Data* channels are used to transmit data taking advantage of SIC at the receivers. Thus, there are two separate transmitter (receiver) circuits in each node. One circuit is intended to transmit (receive) control packets, and the other is used to transmit (receive) data packets.

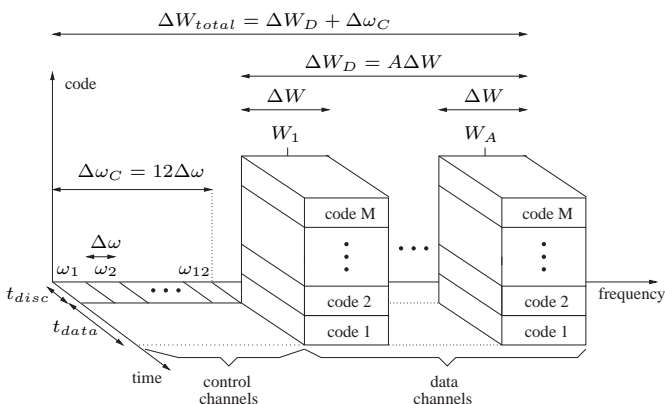


Fig. 1. Data and control channels spectra for the network.

**Control (or Signaling) Channels:** Each cell is allocated a control frequency band from twelve non-overlapping control fre-

quency bands required (and available),  $\omega_1$  to  $\omega_{12}$ , to enable frequency reuse while avoiding interference in the control channels from nearby cells. Each control frequency band  $\omega_i$  has a size of  $|\omega_i| = \Delta\omega$  for  $i = 1, \dots, 12$ . Hence, the total bandwidth required for the control channels is  $\Delta\omega_C = 12\Delta\omega$  (see Fig. 1).

The maximum number of cells in a cluster associated to a given node is twelve. The number of cells and the cluster shape are chosen such that if the receiver range has maximum value, i.e., almost  $\sqrt{2a(n)}$ , then the receiver range reaches all these cells. Also, two cells employing the same control frequency band are kept at least  $\sqrt{5a(n)}$  units away from each other, i.e., a safe guard-zone separation, thus guaranteeing asymptotic constant non-zero signal-to-noise and interference ratio (SNIR) as  $n \rightarrow \infty$  [4] in the control channel, making signaling feasible and allowing control frequency reuse.

Every node is assumed to know its own position (but not the position of any other node) by utilizing a GPS circuit [8], and to store a geographical map of the cells in the network with its associated control frequencies. The GPS is also used to provide an accurate common time reference to keep all nodes synchronized.

Each node uses the control channel receiver to listen to the control channel of the cell as well as to the other 11 control channels, in order to obtain the IDs and training sequences of the other nodes in its cell and in the cluster it perceives, while not transmitting during the neighbor discovery phase.

**Data Channels:** To allow code reuse in the data channels while reducing the negative effects of interference, each cell is allocated a set of PN sequences (or codes) from the twelve different code sets available,  $\xi_1$  to  $\xi_{12}$ , for communication in each data channel. Accordingly, each non-overlapping data channel is a half-duplex link of bandwidth  $\Delta W$ . If  $A$  is the maximum number of nodes allowed to communicate in any cell, then  $\Delta W_D = A\Delta W$  is the data bandwidth required for the entire network and  $M = 12A$  distinct PN sequences are needed for local data communication.  $M$  is also called the spreading factor (or processing gain). Also,  $\Delta W = BM$ , where  $B$  is the original data bandwidth before spreading [7].

Because a PN sequence can be associated to a sequence of bits [7], they can be ordered and grouped as follows.  $\xi_1 = \{C_1, \dots, C_A\}$ ,  $\xi_2 = \{C_{A+1}, \dots, C_{2A}\}$ , ...,  $\xi_{12} = \{C_{11A+1}, \dots, C_{12A}\}$ , in which  $C_i$  stands for the  $i^{th}$  PN sequence (or code). In this way, any set of twelve cells, numbered from 1 to 12, has a different set of codes. Therefore, by construction, the cluster seen by any node is composed of cells having distinct numbers, and consequently, different codes.

As we discuss in Section III-B, the signaling in the control channel provides each node in a cell  $i$  knowledge of who the other nodes in this same cell are, and the node uses this information to choose a data channel to receive data, as well as to select a code for transmission from the available PN sequences in  $\xi_i$  based on its own and neighbor IDs, in the following order<sup>4</sup>: (i) The node with the highest ID in cell  $i$  is associated with the data channel  $\Delta W$  centered at  $W_1$ , as well as it is assigned the first PN sequence in  $\xi_i$ . (ii) The node with the second highest ID in cell  $i$  is associated with the data channel  $\Delta W$  centered at

<sup>4</sup>For simplicity, we indicate  $W_j$  as the data channel associated to node  $j$ .

$W_2$ , as well as it is assigned the second PN sequence in  $\xi_i$ , and this continues for all nodes in cell  $i$ . (iii) The data channels not utilized become idle in cell  $i$ . It happens in those cells where the number of nodes is less than  $A$ .

At time  $t$ , each cell has  $Z$  nodes such that the data communication is  $Z$ -to- $Z$ , i.e., many-to-many communications (see Fig. 2), where  $Z$  is a random variable. Each node employs a multi-user transmitter DS-CDMA [7] (i.e., it transmits up to  $Z - 1$  simultaneous data packets per session in which, due to FDMA, each packet is sent through a different data channel, as illustrated in Fig. 2(downlink)), spreading the data using the PN sequence associated to its ID. The node can transmit a different data packet in each channel or choose to send the same data packet in all (non-idle) channels, or a combination of both, depending on the fact that the node has packet for any destination in the same cell it is located. Thus, multi-copies of the same packet can be simultaneously relayed to reduce delay [4].

Given that each node is endowed with a multi-user detector (the SIC circuit) for its associated receiving data channel, it is able to decode the  $Z - 1$  simultaneous transmissions from all nodes in its cell (see Fig. 2(uplink)).

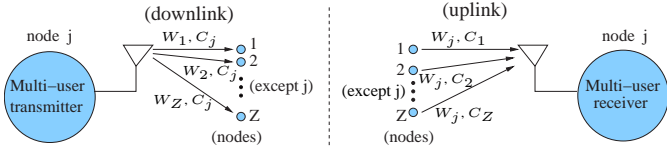


Fig. 2. Downlink and uplink description for data channels in a cell. Communication is  $Z$ -to- $Z$  (i.e., many-to-many).

### B. Channel Access and Data Packet Forwarding

A detailed description of channel access can be found in [12], and Fig. 3 provides its time series representation.

The nodes in each cell use the “neighbor discovery”  $t_{disc}$  time to find their neighbors (i.e., to obtain their IDs) and the period for transmission of data  $t_{data}$  to send information.  $t_{disc}$  and  $t_{data}$  are constant and independent of the number of nodes in the network ( $n$ ). Together, they compose a “communication session.” The common time reference for communication sessions is obtained through the GPS circuit.  $t_{disc}$  is subdivided into  $N$  slots, each of length  $T$ . Each time the discovery pe-

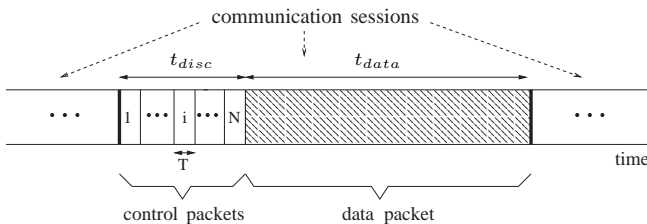


Fig. 3. Time series representation of control and data packets.  $t_{disc}$  is the neighbor discovery phase.  $t_{data}$  is the time period for transmission of data.  $t_{disc}$  plus  $t_{data}$  form a communication session.

riod is about to begin, each node randomly chooses one of the  $T$  mini-slots and transmits its control packet. If there is no collision, i.e., if the other nodes in the same cell choose different mini-slots to transmit, then all the other nodes in the cell will receive this packet. A collision happens every time two or more nodes in the same cell choose to transmit in the same mini-slot. Let  $Z_i$  be the number of nodes in the same cell choosing the

mini-slot  $i$  to transmit their control packets. Let  $Z_{max}$  be the maximum number of nodes in any cell. The probability of collision  $\mathbb{P}_c$  is given by

$$\mathbb{P}_c = \mathbb{P}\{Z_i \geq 2\} = 1 - \left(1 - \frac{1}{N}\right)^{Z_{max}} - \frac{Z_{max}}{N} \left(1 - \frac{1}{N}\right)^{Z_{max}-1}, \quad (1)$$

where it can be shown that  $Z_{max} = \left\lceil \frac{3 \log(n)}{\log(\log(n^\phi))} \right\rceil$  [13]. The criterion used to choose  $N$  is as follows. We calculate  $N$  such that there is no collision with probability approaching 1 as  $n \rightarrow \infty$ , for example, with probability  $\geq 1 - \frac{\log(\log(n))}{\log(n)}$ . From (1),

$$\mathbb{P}_c \leq 1 - \left(1 - \frac{1}{N}\right)^{Z_{max}}. \quad \text{Accordingly, we choose}$$

$$\mathbb{P}_c \leq 1 - \left(1 - \frac{1}{N}\right)^{Z_{max}} \leq \frac{\log(\log(n))}{\log(n)}$$

$$\implies N \geq \left\lceil \left[ 1 - \left(1 - \frac{\log(\log(n))}{\log(n)}\right)^{\frac{1}{Z_{max}}} \right]^{-1} \right\rceil = N_{min}, \quad (2)$$

in which  $\lceil x \rceil$  stands for the ceil function (i.e., the smallest integer greater than or equal to  $x$ ), and  $N_{min}$  is the actual value to be implemented for  $N$ . Thus, we have

$$T = \frac{t_{disc}}{N_{min}}. \quad (3)$$

Data packet forwarding consists of two phases [2], [4]: The packet is transmitted from the source to possibly several relay nodes during *Phase 1* (i.e., multi-copies can be forwarded), and it is delivered later to its destination by only one of the relay nodes during *Phase 2*. Both phases occur concurrently, but *Phase 2* has priority in all communications. These multiple one-time relays for the same packet provide better delay performance since the copies of the same packet follow different random routes, looking for the destination, reducing delay [4].

### C. Interference in a Data Channel

Although the nodes are synchronized, data packets are received at a given node asynchronously due to the different distances from each transmitting node. Besides, fading effects can amplify the asynchronous nature of packet reception. Thus, even if the codes are orthogonal, they exhibit partial cross-correlation at the receiver, which results in multiple access interference (MAI) [7].

The interference in the data channel at a node  $j$ , regarding node  $i$  transmitting to node  $j$  through  $W_j$ , is defined as the signals coming from all transmitting nodes in the network, via  $W_j$ , except node  $i$ . It can be decomposed in the following two types.

*Destructive Interference (DEI)* for the node  $j$  comes from nodes, transmitting in  $W_j$ , outside the receiver range of  $j$ . *DEI* constitutes the part of the interference that will not be decoded.

*Constructive Interference (COI)* comes from nodes, transmitting in  $W_j$ , within the receiver range of  $j$ . By construction (see Section III-A), the nodes within the receiver range of  $j$ , transmitting in  $W_j$ , use different codes exhibiting partial cross-correlation due to the asynchronous nature of the uplink channel [7]. *COI* constitutes the decodable part of the interference.

If node  $i$  transmits data to  $j$  at time  $t$ , via  $W_j$ , the SNIR at the receiver  $j$ , without SIC, is given by (4) [2], where *range*<sup>5</sup> is the set of nodes transmitting in  $W_j$  and reached by the receiver range of node  $j$ ,  $C_i$  is the PN sequence used by sender

<sup>5</sup>  $k \notin \text{range}$  means the nodes outside the receiver range of node  $j$  transmitting in  $W_j$ .

$$SNIR = \frac{P_{ij}(t)g_{ij}(t)}{BN_0 + \underbrace{\frac{1}{M} \sum_{\substack{k \in \text{range} \\ k \neq i}} P_{kj}(t)g_{kj}(t)}_{COI} + \underbrace{\frac{1}{M} \sum_{\substack{k \notin \text{range} \\ C_k \neq C_i}} P_{kj}(t)g_{kj}(t) + \sum_{\substack{k \notin \text{range} \\ C_k = C_i}} P_{kj}(t)g_{kj}(t)}_{DEI}}. \quad (4)$$

node  $i$ ,  $P_{ij}(t) = P \forall (i, j)$  is the transmit power chosen by node  $i$  to transmit to node  $j$  (i.e.,  $P_{ij}(t)$  is constant for all pair  $(i, j)$ ),  $g_{ij}(t)$  is the channel path gain from node  $i$  to  $j$ ,  $B$  is the original bandwidth of the data signal (before spreading),  $BN_0$  is the noise power (where  $N_0$  is the noise power spectral density),  $M$  is the spreading factor,  $COI$  and  $DEI$  are the total interference in  $W_j$  at node  $j$ . The summation terms in the denominator of (4) containing the factor  $1/M$  constitute the multiple access interference ( $MAI$ ) [7], and the last summation term (without the factor  $1/M$ ) is consequence of code reuse in the network and we call it *same code interference* ( $SCI$ ). Thus,  $SCI = \sum_{\substack{k \notin \text{range} \\ C_k = C_i}} P_{kj}(t)g_{kj}(t)$ , such that,  $MAI + SCI = COI + DEI$ .  $MAI$  and  $SCI$  presentations are easier for calculating SNIR as explained later.

The channel path gain  $g_{ij}$  is assumed to be a function of the distance only (i.e., the simple path propagation model) [1], [2], therefore,  $g_{ij}(t) = \frac{1}{|X_i(t) - X_j(t)|^\alpha} = \frac{1}{r_{ij}^\alpha(t)}$ , in which  $\alpha$  is the path loss parameter, and  $r_{ij}(t)$  is the distance between  $i$  and  $j$ .

#### D. Hybrid FDMA/CDMA Data Transceiver

From Fig. 4(a) (see also Fig 2(downlink)), the FDMA/CDMA data transmitter in node  $j$  selects packets previously relayed to node  $j$  which have their destination nodes present in the same cell, spread the data using the code  $C_j$  assigned to node  $j$ , and transmits each one of them through each different frequencies associated to each distinct destination node. If the node assigned to a data channel is not a destination for a relayed packet, then the transmitter selects a new packet generated locally by node  $j$ .

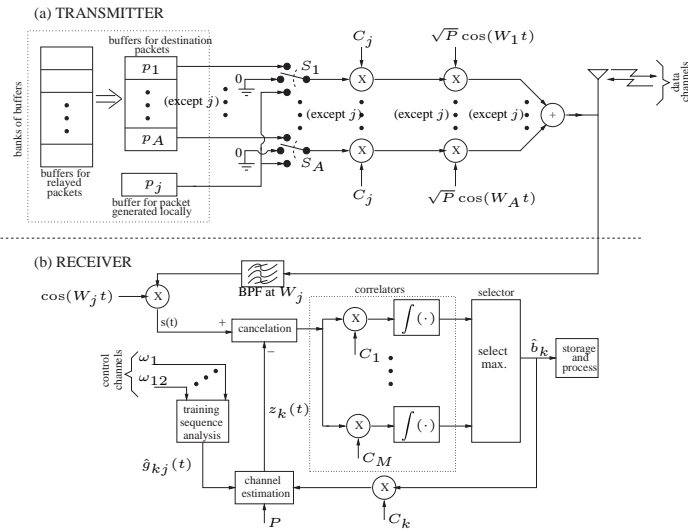


Fig. 4. Hybrid FDMA/CDMA data transceiver scheme for node  $j$ . (a) FDMA/CDMA transmitter. (b) CDMA successive interference cancellation receiver.

The basic decoding scheme of the CDMA-SIC data receiver scheme is given in Fig. 4(b) (see also Fig. 2(uplink)), in which the decoding is performed successively from the strongest signal to the weakest. The use of training sequences obtained

through the control channels allow to obtain a local estimation of the wireless channel. Thus, with the simple path propagation model assumed, the strongest signal decoded first comes from the closest neighbor to node  $j$  (not necessarily in the same cell of  $j$  but in the cluster it perceives), while the weakest (decoded last) is the farthest node to node  $j$  in the cell node  $j$  is located. Let  $MAI'$  be the remaining multiple access interference at node  $j$  after applying SIC up to node  $i$ , i.e.,

$$MAI' = \frac{1}{M} \sum_{\substack{k: g_{kj} < g_{ij} \\ C_k \neq C_i}} P_{kj}(t)g_{kj}(t). \quad (5)$$

Therefore, the resulting SNIR (called  $SNIR'$ ) from node  $i$  to node  $j$  after applying SIC is given by

$$SNIR' = \frac{P_{ij}(t)g_{ij}(t)}{BN_0 + MAI' + SCI}. \quad (6)$$

Note that, depending on the position of the node  $j$ , it may have nodes transmitting from adjacent cells closer than a far node in the same cell. Therefore,  $j$  has to be able to decode the data signals from these adjacent cell nodes before decoding the signal from the far node of the same cell. This explains why each node also needs to obtain the training sequences from the other nodes located outside its cell but still within its receiver range. The receiver uses the information obtained during the neighbor discovery phase to retain the data packets from nodes in the same cell as  $j$ , dropping the outside cell packets since node  $j$  cannot keep track of all nodes in adjacent cells to see if this packet is for relaying or destination.

## IV. CAPACITY AND BANDWIDTH ANALYSIS

### A. Link's Shannon Capacity

The link's Shannon capacity  $R_{ij}$  in the data channel  $W_j$ , in which node  $j$  receives from node  $i$ , after  $j$  applying SIC up to node  $i$ , from (6), is given (in units of nats) by [14]

$$R_{ij} = B \log(1 + SNIR') = B \log\left(1 + \frac{P_{ij}(t)g_{ij}(t)}{BN_0 + MAI' + SCI}\right). \quad (7)$$

From [12], the total remaining interference after SIC at node  $j$  is upper-bounded by

$$MAI' + SCI \leq \frac{c_1 n^{\frac{\alpha}{2}}}{M} + c_2 n^{\frac{\alpha}{2}}, \quad (8)$$

where  $c_1$  and  $c_2$  are positive constants.

If we consider the expansion  $B = f(n)$  of the original data bandwidth, such that  $1 \leq f(n) < n^{\frac{\alpha}{2}}$ , then, a lower-bound for  $R_{ij}$  can be obtained by using the maximum interference. Thus, from (7) and (8), the corresponding link's Shannon capacity lower-bound as  $n \rightarrow \infty$ , for node  $j$  receiving from node  $i$ , is obtained by

$$R_{ij} \geq f(n) \log \left( 1 + \underbrace{\frac{c_3 n^{\frac{\alpha}{2}}}{f(n)N_0 + \frac{c_1 n^{\frac{\alpha}{2}}}{M} + c_2 n^{\frac{\alpha}{2}}}}_{n \rightarrow \infty c_4} \right) = c_4 f(n), \quad (9)$$

in which  $c_3$  and  $c_4$  are positive constants. In (9), interference dominates noise for the bandwidth expansion  $1 \leq B < n^{\frac{\alpha}{2}}$ .

On the other hand, if we consider a scenario such that there is no limitation on available bandwidth, then we can obtain an upper-bound for  $R_{ij}$ . Accordingly, from (7),

$$R_{ij} = B \log \left( 1 + \frac{c_3}{\frac{BN_o}{n^{\frac{\alpha}{2}}} + \frac{1}{n^{\frac{\alpha}{2}}}(MAI' + SCTI)} \right). \quad (10)$$

Now, from (8) and (10), and by taking  $B \geq c_5 n^{\frac{\alpha}{2}}$ , for some positive constant  $c_5$  and  $n$  sufficiently large, it results that

$$\frac{1}{n^{\frac{\alpha}{2}}}(MAI' + SCTI) \leq \frac{c_1}{M} + c_2 \leq \frac{BN_o}{n^{\frac{\alpha}{2}}}. \quad (11)$$

Thus, the term  $\frac{BN_o}{n^{\frac{\alpha}{2}}}$  becomes dominant in the denominator of (10) when  $B \geq c_5 n^{\frac{\alpha}{2}}$  and  $n \rightarrow \infty$ . From (10) and (11), for  $B \geq c_5 n^{\frac{\alpha}{2}}$ , we have the following upper-bound for the link's Shannon capacity as  $n \rightarrow \infty$

$$R_{ij} = \underbrace{n^{\frac{\alpha}{2}} \frac{B}{n^{\frac{\alpha}{2}} \log \left( 1 + \frac{c_3}{\frac{BN_o}{n^{\frac{\alpha}{2}}} + \frac{1}{n^{\frac{\alpha}{2}}}(MAI' + SCTI)} \right)}_{n \rightarrow \infty c_6} = c_6 n^{\frac{\alpha}{2}}, \quad (12)$$

in which  $c_6$  is a positive constant. *Here, noise dominates interference due to the large bandwidth expansion.*

Thus, (9) and (12) describe two limiting cases. The former is the minimum capacity attained if we use the bandwidth expansion  $1 \leq B < n^{\frac{\alpha}{2}}$ . The latter is the maximum capacity reachable if the available bandwidth is large such that  $B \geq c_5 n^{\frac{\alpha}{2}}$ . Note that any increase in  $B$  beyond  $c_5 n^{\frac{\alpha}{2}}$  will not change the order of the upper-bound of the capacity.

### B. Per Source-Destination Throughput

From Section III-B, each node accesses the data channel at a constant rate  $\delta = \frac{t_{data}}{t_{disc} + t_{data}}$  with probability approaching 1 as  $n \rightarrow \infty$ , such that each source sends one packet per session to its destination. Each node is guaranteed, in each data channel, a communication rate of  $R_{ij}$  lower- and upper-bounded by (9) and (12), respectively. Also, this available communication rate has to be divided among all routes the node must serve per session per channel. However, due to the mobility and the routing scheme, each node serves only one route per session per data channel, i.e., the node either relays a new packet or it delivers a packet to a destination. Thus, the number of routes every node has to service per session per data channel is (# of served routes) = 1. Moreover, all cells containing at least two nodes are able to execute FDMA/CDMA and SIC successfully. From (1) and [12],  $\mathbb{P}\{Z \geq 2\} \approx (1 - e^{-1/\phi} - \frac{1}{\phi} e^{-1/\phi})$ . Hence, with probability approaching 1 as  $n \rightarrow \infty$ , the per source-destination throughput  $\lambda(n)$  is obtained by [4]

$$\lambda(n) = \frac{R_{ij} \delta \mathbb{P}\{Z \geq 2\}}{\# \text{ of served routes}} = c_7 R_{ij}, \quad (13)$$

where  $c_7$  is a positive constant for given  $t_{disc}$ ,  $t_{data}$ , and  $\phi$ . From (9), (12), and (13), we proved the following Theorem.

**Theorem 1** *By employing mobility, CDMA, SIC, one-time relaying of packets, and bandwidth expansion using opportunistic cooperation, the ad hoc network attains, with probability approaching 1 as  $n \rightarrow \infty$ , the upper- and lower-bound per source-destination throughput given respectively by*

$$\lambda(n) = O(n^{\frac{\alpha}{2}}) \text{ and } \lambda(n) = \Omega[f(n)], \quad (14)$$

where  $1 \leq f(n) < n^{\frac{\alpha}{2}}$ .

The Theorem shows that, by using *opportunistic cooperation*, the per source-destination throughput increases with  $n$ . Furthermore, the throughput upper-bound is the highest reported in the literature for ad hoc networks.

### C. Bandwidth Scalability

The total bandwidth requirement ( $\Delta W_{total}$ ) for the entire network has two components (see Fig. 1). One from the control channels ( $\Delta \omega_C$ ), and the other from the data channels ( $\Delta W_D$ ).

From (2) and (3), and noting that  $\Delta \omega$  in each control channel equals  $2/T$ , due to the Nyquist rate, it results that

$$\Delta \omega_C = \frac{24N_{min}}{t_{disc}} = \Theta \left[ 1 - \left( 1 - \frac{\log(\log(n))}{\log(n)} \right)^{\left\lceil \frac{1}{\log(\log(n^\phi))} \right\rceil} \right]^{-1}. \quad (15)$$

From Section III-A,  $\Delta W = BM = 12AB$  [7]. Thus, the bandwidth scalability in each data channel associated to the upper- and lower-bound capacity is given respectively by

$$\Delta W = \Omega(n^{\frac{\alpha}{2}}) \text{ and } \Delta W = \Theta[f(n)], \quad (16)$$

where  $1 \leq f(n) < n^{\frac{\alpha}{2}}$ .

The total bandwidth for the entire network is obtained by

$$\Delta W_{total} = \Delta W_D + \Delta \omega_C = A\Delta W + \Delta \omega_C, \quad (17)$$

where  $\Delta W$  and  $\Delta \omega_C$  are given above.

## V. CONCLUSIONS

It was shown that we can obtain Shannon capacity and per source-destination throughput increasing with the total number of nodes  $n$  in wireless ad hoc networks, by employing mobility, FDMA/CDMA, SIC, and one-time relaying of packets taking advantage of opportunistic cooperation among nodes. Accordingly, interference from close neighbors is no longer harmful, but rather endowed with valuable data that we can take advantage of. This technique also allows for code reuse and reduces the bandwidth scalability of the network. In addition, because multi-copy relaying of packets is employed, the delay performance is improved and follows the description given in [4].

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