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### Authors

Kim, Kunhwi

Rutqvist, Jonny

Birkholzer, Jens

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# Lattice modeling of excavation damage in argillaceous clay formations: influence of deformation and strength anisotropy

Kunhwi Kim<sup>a,\*</sup>, Jonny Rutqvist<sup>a</sup>, Jens Birkholzer<sup>a</sup>

<sup>a</sup>*Earth & Environmental Sciences Area, Lawrence Berkeley National Laboratory  
1 Cyclotron Road, Berkeley, CA 94720, USA*

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## Abstract

This paper presents modeling of mechanical anisotropy in argillaceous rocks using an irregular lattice modeling approach, namely the rigid-body-spring network. To represent the mechanical anisotropy, new schemes are implemented in the modeling framework. The directionality of elastic deformation is resolved by modifying the element formulation with anisotropic elastic properties. The anisotropy of strength and failure characteristics is facilitated by adopting orientation-dependent failure criteria into the failure model. The verification of the improved modeling procedures is performed against theoretical model predictions for unconfined compression tests with various bedding orientations. Furthermore, excavation damage and fracturing processes in rock formations are simulated for different geomechanical configurations, such as rock anisotropy and tectonic heterogeneity. The simulated excavation damage characteristics are realistic and comparable with the actual field observation at a tunnel located in an argillaceous clay formation. The simulation results provide insights into the excavation damage zone

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\*Corresponding author.

*Email address:* KunhwiKim@lbl.gov (Kunhwi Kim)

phenomena with an explicit representation of fracturing processes.

*Keywords:* Mechanical anisotropy, Argillaceous clay formation, Excavation damage zone, Fracture modeling, Rigid-body-spring network.

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## 1 **1. Introduction**

2       The investigation of damage development around underground excavations is  
3 a key issue in a variety of geoenineering fields, including mining, tunneling, and  
4 nuclear waste disposal (Bäckblom and Martin, 1999; Tsang et al., 2005; Hudson  
5 et al., 2009). Similar stability problems of underground openings, such as well  
6 boreholes, are crucial in the reservoir engineering and drilling industry related to  
7 hydrocarbon extraction and geothermal energy exploitation (Zoback, 2007). Es-  
8 pecially, in the field of deep geological disposal of nuclear waste, the excavation  
9 damage zone (EDZ) may have an adverse impact on the mechanical and hydro-  
10 logical properties of rock mass, thus affecting the isolation performance, and fur-  
11 thermore, the long-term safety of the repository (Levasseur et al., 2010).

12       Argillaceous clay formations are considered as potential host or cap rocks for  
13 deep geological disposal of nuclear waste due to their superior isolation and con-  
14 finement characteristics. These characteristics include low permeability and dif-  
15 fusivity, high retention capacity for radionuclides, self-sealing features, and long-  
16 term stability of the geological environment (Marschall et al., 2006; Blümling  
17 et al., 2007). However, special geomechanical conditions in rock formations,  
18 such as low strength and mechanical anisotropy and unfavorable high degree of  
19 anisotropy of in-situ stresses at depth, increase vulnerability to excavation dam-  
20 age and fracture development around a tunnel or a shaft, which often brings about  
21 serious engineering difficulties during the construction and operation of deep un-

22 derground repositories (Steiner, 1996; Martin et al., 1999; Bossart et al., 2004).  
23 Therefore, rational understanding of the geomechanical settings and the corre-  
24 sponding EDZ phenomena could help conducting more reliable performance and  
25 safety assessment of the deep clay-based repositories.

26 The mechanical behavior of argillaceous clay formations, such as shale, is  
27 greatly influenced by mechanical anisotropy, which is typically observed as a  
28 variation of elastic response, strength characteristics, and failure mechanisms with  
29 sample bedding orientation in laboratory experiments (McLamore and Gray, 1967;  
30 Niandou et al., 1997; Naumann et al., 2007). At a larger scale, this mechanical  
31 anisotropy directly affects the stability of underground structures and the observed  
32 failure behavior. Field observations from the Mont Terri underground research  
33 laboratory (URL) located in an indurated, over-consolidated clay shale, namely  
34 Opalinus Clay, indicate that the geometry and extent of the EDZ around tunnels  
35 are largely dependent on the relative orientation between bedding planes and the  
36 excavation axis (Marschall et al., 2006; Blümling et al., 2007; Labiouse and Vi-  
37 etor, 2014).

38 In this study, the mechanical anisotropy of argillaceous rocks is modeled within  
39 the rigid-body-spring network (RBSN) framework. A rock mass is rendered as a  
40 network of numerous spring sets connected with distinct one-dimensional ele-  
41 ments (i.e., lattice elements), and the global mechanical behavior, including dis-  
42 crete fracturing process, is represented by the collection of local deformation and  
43 breakage of the spring sets. To represent the mechanical anisotropy within the  
44 modeling procedures, formulation of the element stiffness matrix is modified with  
45 anisotropic elastic configurations, and orientation-dependent failure criteria are  
46 introduced. Details of the proposed modeling schemes are presented in Section 2.

47 The improved modeling procedures are applied to simulate unconfined compression tests in Section 3, where variations of Young’s modulus, uniaxial compressive strength, and fracture pattern with the bedding orientation are evaluated and verified against the theoretical model predictions. Furthermore, in Section 4, simulations of the EDZ evolutions are conducted for different geomechanical settings, and comparisons of the simulated EDZ features are made as a validation process.

## 53 **2. Representation of mechanical anisotropy**

54 The rigid-body-spring network (RBSN) approach has been used to investigate mechanics and fracture processes of geological systems, for which a rock mass is modeled as an assemblage of simple, two-node elements in a lattice structure. The irregular geometry of the lattice structure is defined by the dual Delaunay–Voronoi tessellation of a set of nodal points randomly generated in the domain (Okabe et al., 59 2000). This section presents methodologies for implementation of deformation and strength anisotropy in the lattice model.

### 61 *2.1. Anisotropy of elastic deformability*

62 Figure 1 compares the formation of ordinary lattice elements and their modification for anisotropic elasticity. A 2D case is herein illustrated for plain description, but this scheme has been developed within the 3D modeling framework. A lattice element is formed from two neighboring nodes,  $i$  and  $j$ , which are connected via rigid-body constraints to a zero-size spring set located at the center of the common Voronoi facet.

68 In the ordinary lattice model, the spring sets are oriented to their individual local  $x$ – $y$  coordinates defined by the Voronoi diagram (Fig. 1a). The spring coef-

70 ficients are defined as (Kawai, 1978)

$$\begin{aligned}
 k_x &= \alpha_1 E \frac{A_{ij}}{h_{ij}} \\
 k_y &= \alpha_2 k_x \\
 k_\phi &= E \frac{I_\phi}{h_{ij}}
 \end{aligned}
 \tag{1}$$

71 where  $A_{ij}$  is the area of the common Voronoi facet;  $h_{ij}$  is the distance between the  
 72 element nodes; and  $I_\phi$  is the moment of inertia of the facet area. Factors  $\alpha_1$  and  $\alpha_2$   
 73 are adjusted to obtain global representation of Young's modulus  $E$  and Poisson's  
 74 ratio  $\nu$ . For the special case of  $\alpha_1 = \alpha_2 = 1$ , the lattice model provides an elasti-  
 75 cally homogeneous and isotropic representation of  $E$ , although the corresponding  
 76 value of  $\nu = 0$  (Bolander and Saito, 1998; Yip et al., 2005). In the new scheme for  
 77 anisotropic representation, by comparison, the spring sets are aligned to the direc-  
 78 tion of bedding planes in  $N$ - $P$  coordinates (Fig. 1b). The stiffness coefficients in  
 79 Eq. 1 can be modified for anisotropic elastic properties about the orthogonal  $N$ -  
 80 and  $P$ -axes:

$$\begin{aligned}
 k_N &= E_N \frac{A_{ij}}{h_{ij}} \\
 k_P &= E_P \frac{A_{ij}}{h_{ij}} \\
 k_\varphi &= E_N \frac{I_\phi}{h_{ij}}
 \end{aligned}
 \tag{2}$$

81 where  $E_N$  and  $E_P$  are Young's moduli normal and parallel to bedding, respectively,  
 82 which can be directly adopted from laboratory measurements.

83 As seen in Fig. 1b, the kinematics of the nodes and elements can be repre-  
 84 sented in three distinct coordinate systems: global  $X$ - $Y$  coordinates based on do-  
 85 main construction; local  $x$ - $y$  coordinates for individual elements; and global  $N$ - $P$   
 86 coordinates related to the bedding orientation. The anisotropic material matrix

87  $\mathbf{D} = \text{diag}[k_N, k_P, k_\varphi]$  for each lattice element is established in  $N$ - $P$  coordinates,  
 88 then transformed to the spring set stiffness matrix in local  $x$ - $y$  coordinates using  
 89 the coordinate transformation (McGuire and Gallagher, 1979):

$$\mathbf{k}_s = \mathbf{\Gamma}^T \mathbf{D} \mathbf{\Gamma} \quad (3)$$

90 where  $\mathbf{\Gamma}$  is the  $3 \times 3$  coordinate transformation matrix from  $x$ - $y$  coordinates to  
 91  $N$ - $P$  coordinates:

$$\mathbf{\Gamma} = \begin{bmatrix} N_x & N_y & 0 \\ P_x & P_y & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad (4)$$

92 The first  $2 \times 2$  entries in  $\gamma$  are the direction cosines between the bedding orientation  
 93 and the local element axes.

94 The element stiffness matrix  $\mathbf{k}_e$ , relating the generalized local forces and el-  
 95 ement nodal displacements, is derived from  $\mathbf{k}_s$  pre- and post-multiplied by the  
 96 geometric matrix (Bolander and Saito, 1998; Berton and Bolander, 2006):

$$\mathbf{k}_e = \mathbf{B}^T \mathbf{k}_s \mathbf{B} \quad (5)$$

97 The conversion of  $\mathbf{k}_e$  to the global coordinates is obtained by another coordinate  
 98 transformation:

$$\mathbf{K}_e = \mathbf{T}^T \mathbf{k}_e \mathbf{T} \quad (6)$$

99 where  $\mathbf{T}$  is the transformation matrix relating local  $x$ - $y$  and global  $X$ - $Y$  coor-  
 100 dinate systems. The transformed element stiffness matrices, built for individual  
 101 lattice elements, are assembled into the global stiffness matrix to solve the system  
 102 equilibrium equations.

103 2.2. *Anisotropy of strength*

104 This study employs a Mohr–Coulomb model to determine brittle failure of lat-  
105 tice elements. The stress state of each lattice element is represented as a Mohr cir-  
106 cle in the stress space, which is assessed by a limiting surface for possible failure  
107 conditions. Herein, a weak-plane failure model is used to provide anisotropic fail-  
108 ure characteristics. This model assumes that the strength anisotropy is attributed  
109 to conditional failure on a particular orientation of a plane, where the material  
110 strength is significantly weaker. This model concept has a physical basis because  
111 the bedding planes in sedimentary rocks are generally recognized as planes of  
112 weakness (Pariseau, 2006; Fjær et al., 2008).

113 Figure 2 illustrates two distinct situations of orientation-dependent failure in  
114 the Mohr–Coulomb model. The material has two failure criteria—one intrinsic,  
115 isotropic criterion and one for the weak planes—and correspondingly two failure  
116 surfaces (Jaeger, 1960). The intrinsic failure criterion is given by the cohesive  
117 strength  $c$ , internal friction angle  $\phi$ , and tension cut-off  $f_t$ . Analogously, the weak-  
118 plane failure criterion is defined by lower values of the strength parameters  $c_w$ ,  $\phi_w$ ,  
119 and  $f_{t,w}$ . Consider the stress state in the rock specimen is such that the Mohr circle  
120 intersects the weak-plane failure surface at two points with angles  $2\psi_1$  and  $2\psi_2$   
121 (Fig. 2a), and the material with a bedding orientation  $\psi_1 < \beta < \psi_2$  will fail along  
122 the bedding planes at a lower stress level. However, if the bedding orientation  $\beta$  is  
123 projected below the weak-plane failure surface, as shown in Fig. 2b, the material  
124 will fail across the bedding planes with the failure angle  $\psi = 45^\circ + \phi/2$  at a higher  
125 stress level.

126 For the confined stress configuration ( $\sigma_1 > \sigma_2 = \sigma_3 > 0$ ), the two failure  
127 criteria limit the stress states, which can be theoretically defined as follows (Jaeger



128 et al., 2007):

$$\sigma_1 - \sigma_3 = 2 \frac{c \cos \phi + \sigma_3 \sin \phi}{1 - \sin \phi} \quad (7)$$

129 for the intrinsic failure criterion; and

$$\sigma_1 - \sigma_3 = 2 \frac{c_w \cos \phi_w + \sigma_3 \sin \phi_w}{\sin 2\beta \cos \phi_w - (1 + \cos 2\beta) \sin \phi_w} \quad (8)$$

130 for the weak-plane failure criterion. The criterion that predicts the lowest strength  
131 for a given orientation  $\beta$  is always the relevant criterion in the failure model. In  
132 that sense, the anisotropic strength could vary with the bedding orientation of the  
133 sample.

### 134 3. Unconfined compression tests

135 The proposed modeling schemes are verified in the simulations of unconfined  
136 compression tests for transversely isotropic rock specimens. Consider a cylindri-  
137 cal core sample subjected to a uniaxial compression load, in which the bedding  
138 planes form an angle  $\theta$  from the axial loading direction (see Fig. 3a). We have  
139 conducted simulations for eight cases of angles to bedding:  $\theta = -15^\circ$ ;  $0^\circ$  (paral-  
140 lel to loading axis);  $15^\circ$ ;  $30^\circ$ ;  $45^\circ$ ;  $60^\circ$ ;  $75^\circ$ ; and  $90^\circ$  (normal to loading axis). As  
141 shown in Fig. 3b, a core sample with a diameter of 50 mm and a height of 100 mm  
142 is discretized with 15,047 nodes and 76,730 elements. Extra layers of nodes and  
143 elements are padded at the top and bottom of the cylinder to provide uniform ax-  
144 ial strain along the section, where a displacement controlled boundary condition  
145 is applied to deform the sample up to 0.3 mm in compression. The anisotropic  
146 properties of the core material are adopted from the experimental results for the  
147 Opalinus Clay samples (Bossart, 2011), which are listed in Table 1.

148 The resulting stress-strain curves for the eight cases of bedding orientations  
 149 are plotted in Fig. 4. The stress response is calculated by averaging the sum of  
 150 reaction forces monitored at the padding layers over the cross sectional area of the  
 151 sample. The height of the core sample is taken as the gauge length to derive global  
 152 axial strain from the boundary displacements. The stress linearly increases with  
 153 the strain to the peak stress and sharply decreases over the peak, involving brittle  
 154 failure. The linear slope and the peak of the response curve vary with the bedding  
 155 orientation, which reflects the mechanical anisotropy of the rock material. Note  
 156 that the response curves for  $\theta = -15^\circ$  and  $15^\circ$  coincide closely with each other  
 157 because of the symmetric bedding orientations with the same angle from the  
 158 loading axis.

159 The linear slope of each stress-strain curve is taken as the global Young's mod-  
 160 ulus of the sample and compared with a theory in Fig. 5. The Young's modulus  
 161 of a transversely isotropic material with an angle  $\theta$  from the loading axis to the  
 162 bedding is theoretically obtained by Pariseau (2006):

$$\frac{1}{E} = \frac{\cos^4 \theta}{E_P} + \left( \frac{1}{G_a} - \frac{2\nu_a}{E_P} \right) \sin^2 \theta \cos^2 \theta + \frac{\sin^4 \theta}{E_N} \quad (9)$$

163 where  $G_a$  and  $\nu_a$  are the relevant shear modulus and Poisson's ratio for the anisotropic  
 164 case, respectively. With an approximation of  $G_a = 1 / \left( \frac{1}{E_P} + \frac{1}{E_N} \right)$  for zero Poisson's  
 165 ratio, Eq. 9 can be rewritten as

$$\frac{1}{E} = \frac{\cos^2 \theta}{E_P} + \frac{\sin^2 \theta}{E_N} \quad (10)$$

166 The variation of Young's modulus from the simulations shows a good agreement  
 167 with the theoretical model prediction.

168 The peak stress captured from the stress-strain response can be regarded as  
 169 the uniaxial compressive strength. Figure 6 shows the simulated uniaxial com-

170 pressive strengths for the cases of different angles to bedding. The orientation-  
 171 dependent failure criteria presented in Section 2.2 limit the critical stress state of  
 172 the anisotropic material. By imposing the lateral unconfined condition ( $\sigma_3 = 0$ )  
 173 and substituting the relevant strength parameters into Eqs. 7 and 8, the theoretical  
 174 uniaxial compressive strength at an angle to bedding  $\theta = 90^\circ - \beta$  can be determined  
 175 as the lowest strength between

$$UCS = \frac{2c_P \cos \phi_P}{1 - \sin \phi_P} \quad (11)$$

176 and

$$UCS = \frac{2c_N \cos \phi_N}{\sin 2\theta \cos \phi_N - (1 - \cos 2\theta) \sin \phi_N} \quad (12)$$

177 This theoretical model prediction is also plotted as a function of the angle to bed-  
 178 ding  $\theta$  in Fig. 6, which is perfectly in line with the simulated uniaxial compressive  
 179 strengths. However, the material exhibits anisotropic strengths only when the bed-  
 180 ding orientations fall in a certain range for the weak-plane failure and otherwise a  
 181 constant strength involved with the intrinsic isotropic failure, which is attributed  
 182 to the discontinuous set of a single plane of weakness in the failure model. More  
 183 sophisticated models such that weak planes and the corresponding strength  
 184 param-eters vary continuously with the bedding orientation could provide more  
 185 realistic representation of rock anisotropy (McLamore and Gray, 1967; Hoek and  
 186 Brown, 1980; Pietruszczak and Mroz, 2001).

187 Figure 7 presents fracture patterns within the samples at the final loading stage  
 188 (0.003 of axial strain). Overall, cracks tend to propagate in the direction of bed-  
 189 ding planes, especially for the cases of low inclination angles of bedding planes  
 190 from the loading axis. In these cases, weak-plane failure along the bedding planes  
 191 is selected as the relevant mechanism to proceed the material failure. A com-  
 192 parison of Figs. 7a and c indicates that symmetric bedding orientations about the

193 loading axis naturally lead to symmetric patterns of fracture development. In the  
194 exceptional case with  $45^\circ$  to bedding (Fig. 7e), the fractures align perpendicular  
195 to the bedding planes, which form a thick shear band across the sample.

196 In the simulations of unconfined compression tests, the elastic deformability  
197 and failure characteristics of the anisotropic rock material are rationally demon-  
198 strated. Various bedding orientations of the core samples are represented with-  
199 out the need of orientation-dependent mesh geometry, but rather with inherent  
200 anisotropy of lattice elements. Also, the mechanical parameters are uniformly  
201 assigned to the elements irrespective of their local orientations, which contrasts  
202 to other modeling approaches using heterogeneous parameters dependent on the  
203 direction of element (Lisjak et al., 2014, 2015). In the next section, the modeling  
204 procedures are further validated through simulations of excavation damage and  
205 fracturing processes in rock formations.

## 206 **4. Excavation damage and fracture development in argillaceous clay forma-** 207 **tions**

### 208 *4.1. HG-A microtunnel at the Mont Terri site*

209 The evolution of excavation damage zone (EDZ) near a tunnel is simulated  
210 and validated against the field observation at the HG-A test site. A circular micro-  
211 tunnel with the length of 13 m and the diameter of 1.04 m is located at the Mont  
212 Terri URL near Saint-Ursanne, Switzerland. The host rock, Opalinus Clay, is  
213 relatively homogeneous in meter-scale, but pronounced anisotropy with bedding  
214 planes is discovered at millimeter-scale (Yong et al., 2010). The rock formation  
215 surrounding the HG-A tunnel is highly fractured with a sub-meter spatial fre-  
216 quency although the fracture permeability is not significant, which indicates that

217 fractures are mostly closed under natural stress conditions (Marschall et al., 2006,  
218 2008).

219 One main purpose of the HG-A test is to provide data on the geomechanical  
220 and hydrogeological effects due to the presence of the EDZ around the tunnel.  
221 Although the long-term physical features observed in the test are related to cou-  
222 pled hydro-mechanical processes, herein the problem is simplified by assuming  
223 a constant uniform pore pressure such that the excavation damage and fractur-  
224 ing processes can be reckoned as short-term mechanical-only responses. This  
225 assumption is valid up until an early tunneling stage, where mechanical deforma-  
226 tions occur much more quickly than water flow and hydrological processes in the  
227 rock formation, and the mechanical equilibrium is held within a rapid (undrained)  
228 excavation (Liu et al., 2013). In the actual excavation of the HG-A tunnel, the  
229 drilling progress was rather quick and smooth (Marschall et al., 2006), so pure  
230 mechanical simulations are applicable to this case, where relevant EDZ phenom-  
231 ena could be captured.

232 Figure 8 shows excavation damage around the microtunnel. Anisotropic prop-  
233 erties of the rock material and heterogeneity of tectonic fault formations, as well  
234 as anisotropic in-situ stress conditions, result in non-uniform damage around the  
235 tunnel. Major buckling and spalling phenomena between 10 and 11 o'clock  
236 and less distinct buckling at about 5 o'clock are observed along the tunnel wall,  
237 which indicates that the tunnel is running parallel to the strike of inclined bedding  
238 planes (Marschall et al., 2006). On the other hand, wedge-shaped damage struc-  
239 tures with extension joints mapped on the side surfaces (3 to 4 o'clock and 9 to 10  
240 o'clock) are identified as stress-induced breakouts.

241 In this study, we investigate the effects of rock anisotropy and tectonic hetero-

242 geneity on the EDZ phenomena. Figure 9 presents three simulations cases with  
243 different geomechanical settings: (I) in-plane isotropy and intact formation; (II) in-  
244 plane anisotropy and intact formation; and (III) in-plane anisotropy and fault  
245 formation. Anisotropic in-situ stresses of  $\sigma_v = 6.5$  MPa in the vertical direction  
246 and  $\sigma_h = 4.5$  MPa in the horizontal direction are adopted as a confinement condi-  
247 tion (Martin and Lanyon, 2003), and a uniform pore pressure of 1.5 MPa is applied  
248 in the modeling domain. For Cases II and III, the bedding planes are oriented at  
249  $45^\circ$  from the horizontal axis (Figs. 9b and c), and additionally for Case III three  
250 discrete fault planes are placed around the tunnel (Fig. 9c).

251 Figure 10 depicts the Voronoi discretizations of a 10 m square domain for the  
252 excavation damage simulations. Predicted EDZ area around the tunnel is finely  
253 meshed, and the nodal density is graded towards the domain boundaries for com-  
254 putational efficiency. The circular tunnel with 1.04 m diameter is initially filled  
255 with the Voronoi cells and lattice elements. The excavation process is realized by  
256 gradually reducing the spring stiffnesses, internal element forces, and pore pres-  
257 sure of the elements to void the tunnel domain, for which an exponential decay is  
258 assumed to set the reduction of the values to  $10^{-6}$  of the original values at the end  
259 of 100 loading steps. Herein, gravity loads are ignored throughout the simula-tions  
260 because the gravity forces may have a minor influence compared to the effect of  
261 in-situ stresses in case of relatively deep, small excavations (Carranza-Torres and  
262 Fairhurst, 1997). As shown Fig. 10b, fault planes are explicitly represented in the  
263 mesh, and low strength parameters are assigned to the corresponding el-ements:  
264 tensile strength  $f_{t,f} = 0.5$  MPa; cohesion  $c_f = 1.0$  MPa; and friction angle  $\phi_f = 23^\circ$ .  
265 Rock properties are set as listed in Table. 1. Note that while clay shale may exhibit  
266 plastic deformations or residual stress responses under confined

267 stress conditions (Parisio et al., 2015), this study simply assumes the rock material  
268 around the tunnel opening undergoes brittle failure with unconfined conditions.

#### 269 4.2. Discussion on simulation results

270 From the simulations of the EDZ evolutions, the resulting damage patterns  
271 and the contours of the magnitudes of the major principal stress and the minor  
272 principal stress are given in Figures 11 to 13. For Case I with isotropic rock  
273 properties, excavation-induced cracks stretch out in the direction perpendicular  
274 to the major confining stress to result in the formation extensive breakouts or v-  
275 shaped notches (see Fig. 11a), which is a failure pattern frequently found under  
276 anisotropic in-situ stress conditions (Martin et al., 1999; Read, 2004; Perras and  
277 Diederichs, 2016). As seen in Figs. 11b and c, the in-situ stress field is altered  
278 by the excavation. The failed zones exhibit low magnitudes of stresses due to  
279 softening and weakening effects of the fractures, however, the redistribution of  
280 stresses is highly concentrated close to the notch tips. In the outer region, the  
281 disturbed stress field displays quite symmetric contours about the vertical and  
282 horizontal axes crossing at the center of the tunnel.

283 The simulation results for Case II, presented in Fig. 12, show failure charac-  
284 teristics influenced by the anisotropy of deformability and strength. As shown in  
285 Fig. 12a, more pronounced cracks and breakouts at the tunnel wall are concen-  
286 trated and oriented along the direction normal to the bedding planes. Compared  
287 to the stress contours in the previous case, the contour patterns are asymmetric  
288 and inclined towards the bedding orientation (see Figs. 12b and c), which may be  
289 attributed to the anisotropic rock properties and the inclined failed zones.

290 For Case III with anisotropic rock properties and fault planes, the EDZ evolu-  
291 tion involves more complex failure processes. Distinct shear failures occur along

292 the fault planes in the early stage of excavation, and then rock cracking grows from  
293 the fault planes. The failed zones illustrated in Fig. 13a conform to the estimation  
294 of damaged zones from the field observation (see Fig. 8). One notable feature  
295 in the fractured damage pattern is that the crack growth in the rock is somewhat  
296 controlled by the fault planes, so that the cracks do not propagate across the faults.  
297 Figures 13b and c show the stress field perturbed by the fault planes, where dis-  
298 continuous stress contours are spotted in the fractured zones and extended along  
299 the fault planes.

## 300 **5. Conclusions**

301 The evolution of excavation damage zone (EDZ) and the failure features around  
302 the tunnel excavation are found to be strongly related to the lithological proper-  
303 ties of the rock formations, i.e., rock anisotropy due to the bedding planes. In  
304 this study, the rigid-body-spring network (RBSN) approach is used to simulate  
305 the mechanically anisotropic behavior of argillaceous rocks. Since the original  
306 RBSN models generally provide the descriptions of isotropic systems, the model-  
307 ing procedures have been modified and improved with new modeling schemes to  
308 represent the mechanical anisotropy. The spring coefficients of individual lattice  
309 elements are systematically formulated based on the bedding orientation, and in  
310 addition, a simple weak-plane failure model is adopted into the Mohr–Coulomb  
311 criteria to determine the local failure along the bedding planes. The improved  
312 modeling procedures can readily represent the anisotropic elasticity and effec-  
313 tively capture the orientation-dependent failure features and strength anisotropy.

314 Using the new schemes in the RBSN model, unconfined compression tests  
315 are simulated for transversely isotropic rock specimens, and the simulation results



316 are verified against analytical solutions. Various bedding orientations of the sam-  
317 ples can be reflected on the identical mesh without modifying or re-constructing  
318 the mesh geometry. From the stress-strain responses for the simulated cases,  
319 the global Young's moduli and the uniaxial compressive strengths are evaluated,  
320 which fall in line with the analytically determined values of anisotropic properties.  
321 Moreover, anisotropic failure characteristics are observed from the orientation of  
322 fracture development relative to the direction of bedding planes.

323 Next, the modeling procedures are applied to simulate the tunnel excavation  
324 in rock formations, where three cases of geomechanical settings are considered to  
325 make a comparative study on the EDZ phenomena. Several observations can be  
326 highlighted:

- 327 • The EDZ evolution in the isotropic rock formation is largely influenced by  
328 the in-situ stress field. Major failure and extensive breakouts are generated  
329 to build v-shaped notches from the tunnel wall in the direction perpendicular  
330 to the major principal compressive stress.
- 331 • In the presence of rock anisotropy, excavation-induced fractures are inclined  
332 to develop on the tunnel walls tangential to the bedding planes. Due to the  
333 anisotropic elastic properties, stress contours around the tunnel are asym-  
334 metric about the principal axis of in-situ stress and inclined to the bedding  
335 orientation.
- 336 • Tectonic faults can contribute to the heterogeneous excavation damage,  
337 where distinct shear failures occur along the fault planes and the stress  
338 contours are divided into discontinuous regions. The resulting fracture  
339 pattern in the damaged zones is also affected by the fault planes.

340 In summary, the simulations presented in this paper confirm the validity of the  
341 RBSN approach to model the EDZ evolutions in argillaceous rocks. The EDZ  
342 phenomena reproduced in the simulations are realistic and comparable with the  
343 actual EDZ observation at the HG-A microtunnel. The simulation results provide  
344 insights into the characterizations of excavation damage with an explicit represen-  
345 tation of fracturing processes.

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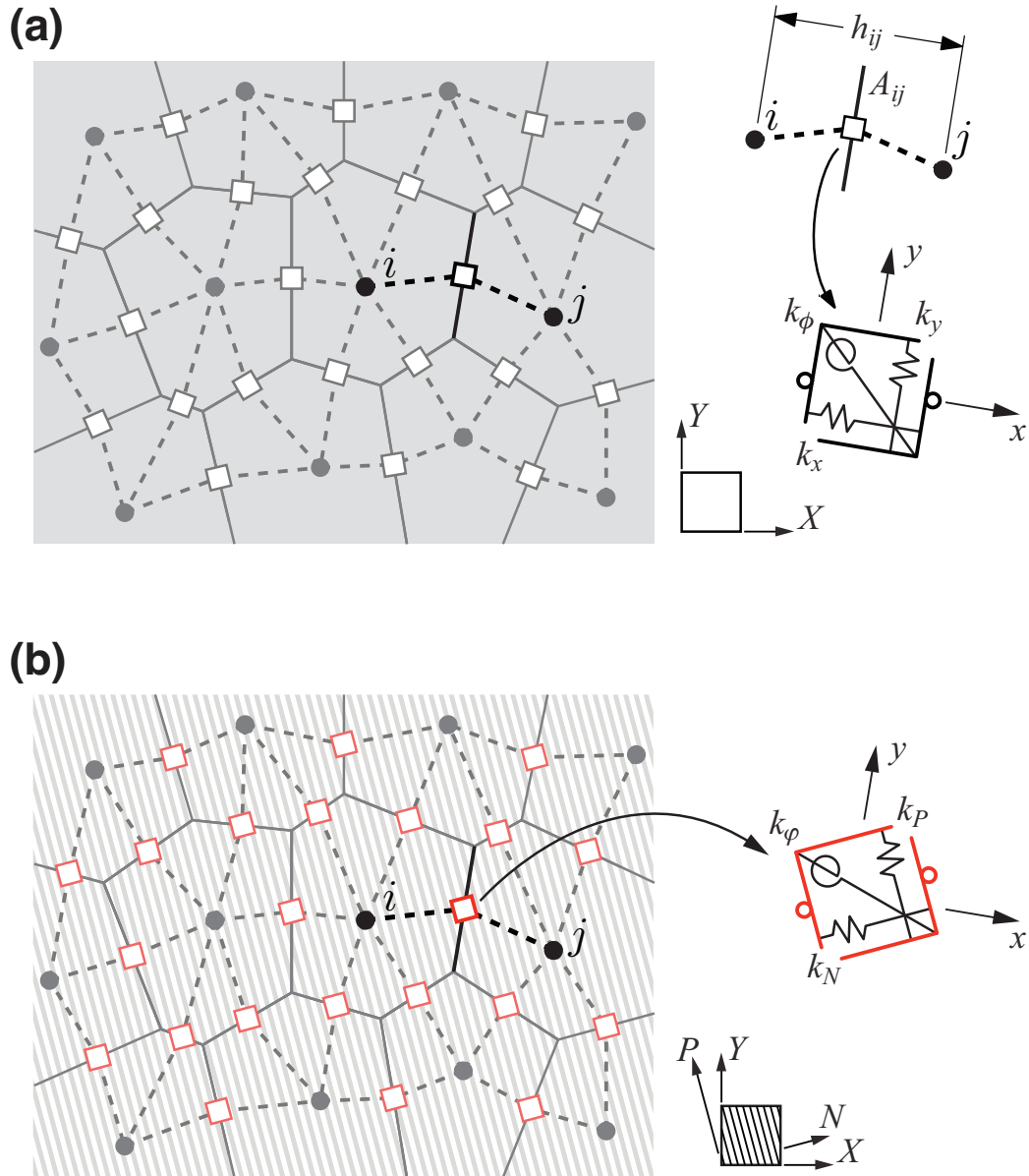


Figure 1: Modification of rigid-body-spring elements in an identical lattice structure: (a) original spring sets based on the direction of Voronoi facets (local  $x$ - $y$  coordinate systems); and (b) spring sets aligned to the global bedding orientation ( $N$ - $P$  coordinate system).



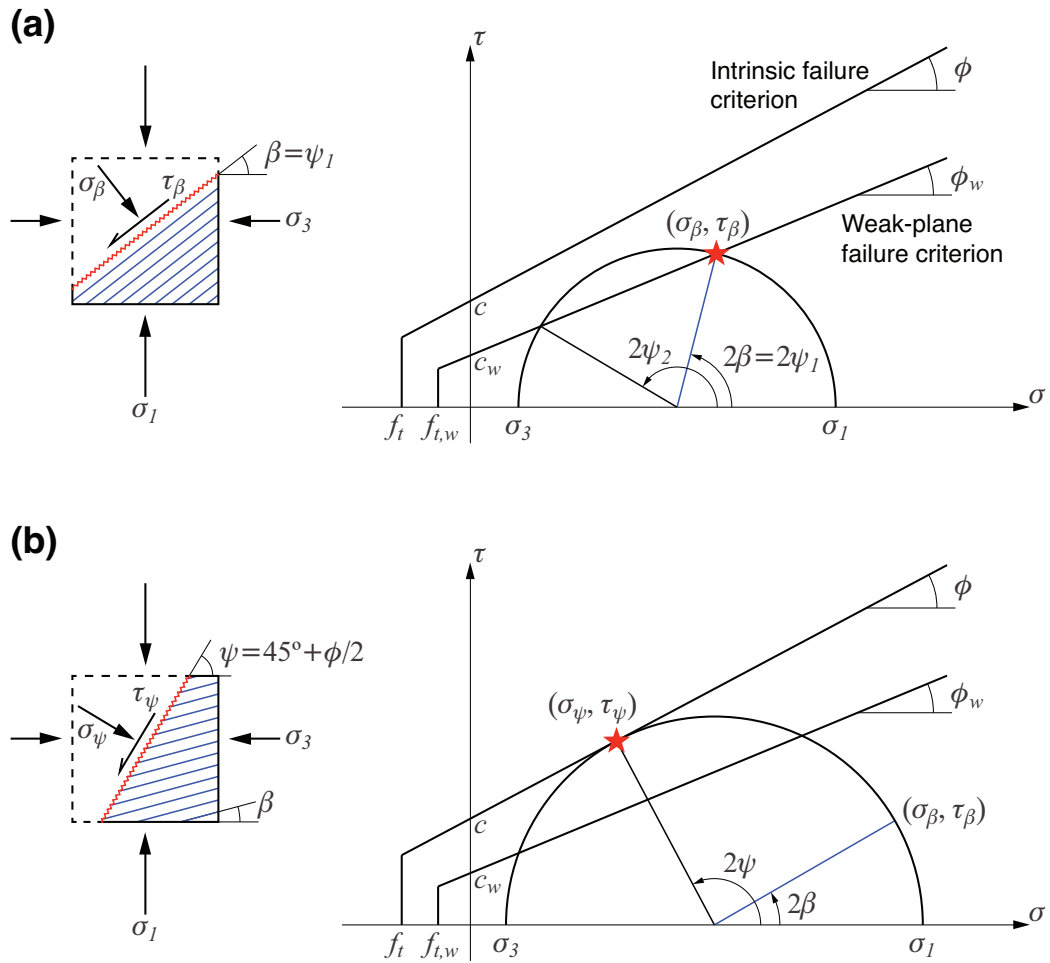


Figure 2: Orientation-dependent failure criteria in Mohr-Coulomb model: (a) weak-plane failure along the bedding; and (b) intrinsic failure across the bedding.

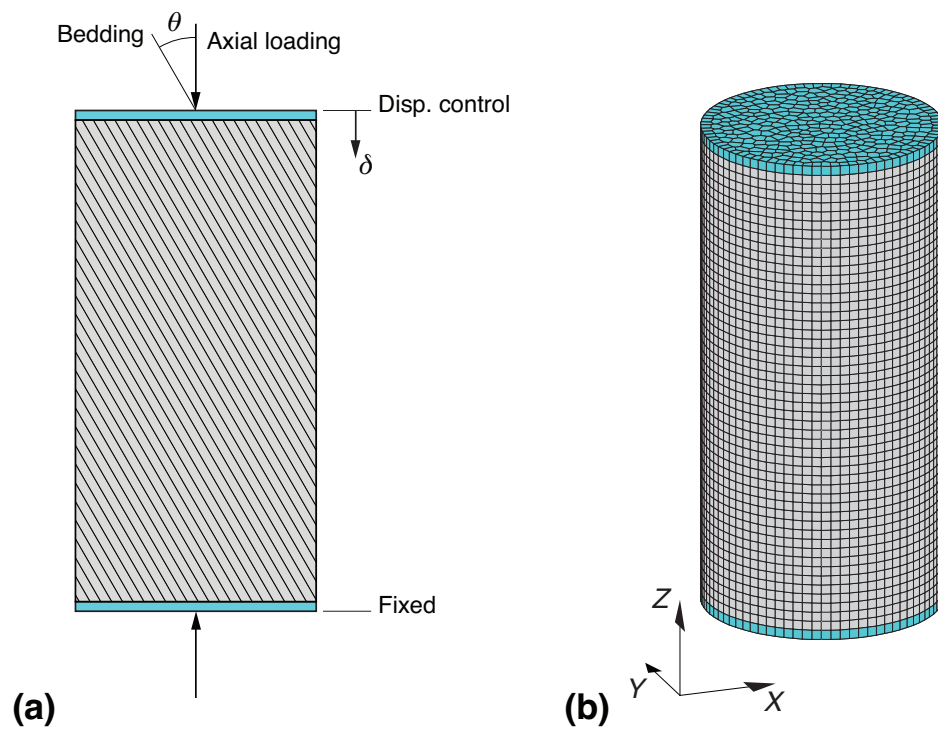


Figure 3: Uniaxial compression tests: (a) schematic drawing of the test program; and (b) 3D Voronoi discretization of a specimen model.

Table 1: Anisotropic mechanical properties of Opalinus Clay (Bossart, 2011)

Rock properties	Parallel to bedding	Normal to bedding
Young's modulus	$E_P = 15.5 \text{ GPa}$	$E_N = 9.5 \text{ GPa}$
Uniaxial tensile strength	$f_{t,P} = 2.0 \text{ MPa}$	$f_{t,N} = 1.0 \text{ MPa}$
Cohesion <sup>†</sup>	$c_P = 5.5 \text{ MPa}$	$c_N = 2.2 \text{ MPa}$
Internal friction angle	$\phi_P = 25^\circ$	$\phi_N = 25^\circ$

<sup>†</sup> Bossart (2011) suggested three different values for cohesion or shear strength: maximum value of 5.5 MPa (parallel to bedding); minimum value of 2.2 MPa (normal to bedding); and the third value of 1 MPa (shear strength of bedding planes). In this study, 2.2 MPa is taken as a cohesive strength normal to bedding, as stated.

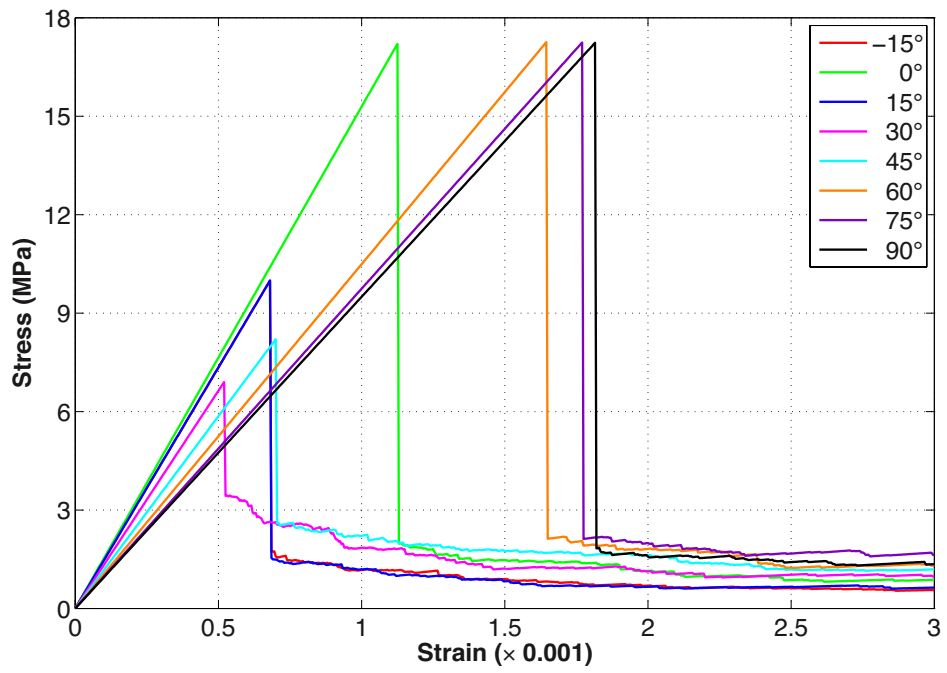


Figure 4: Stress-strain responses for various angles to bedding.

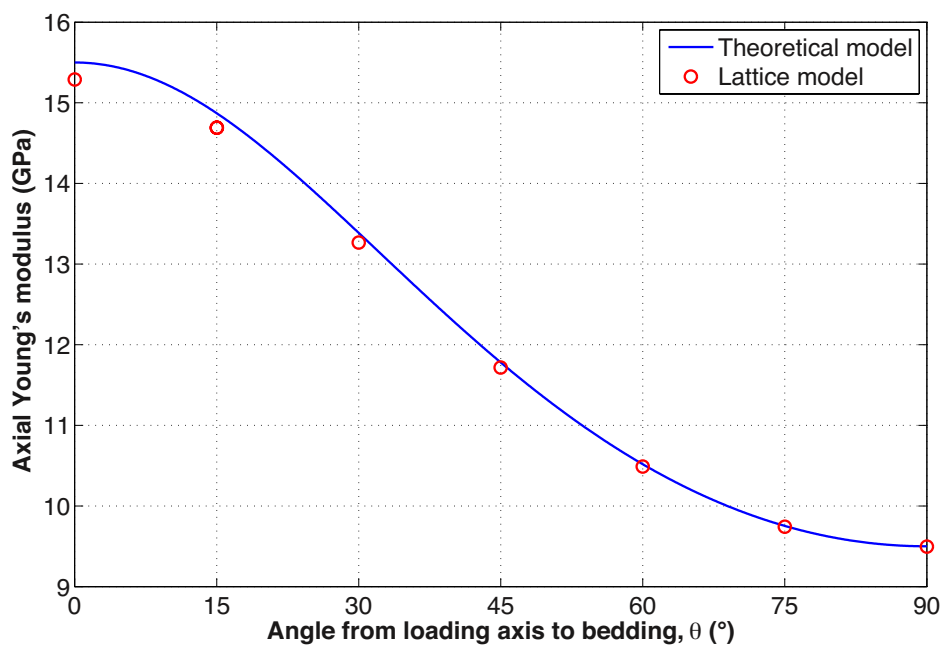


Figure 5: Comparison of simulated Young's modulus with the theoretical model prediction (Eq. 10) for different bedding orientations.

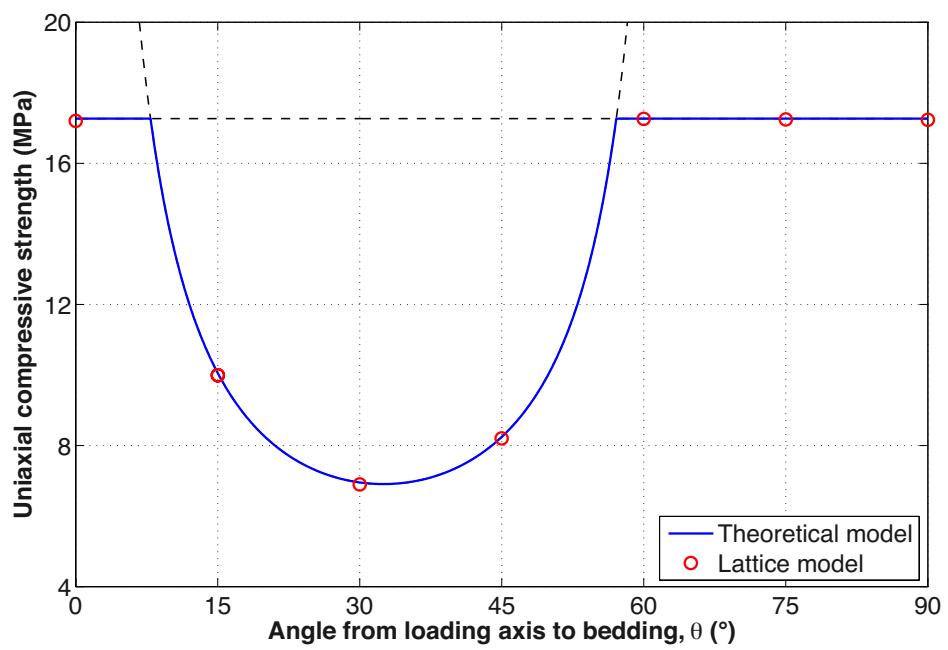


Figure 6: Comparison of simulated uniaxial compressive strength with the theoretical model prediction (determined by Eqs. 11 and 12) for different bedding orientations.

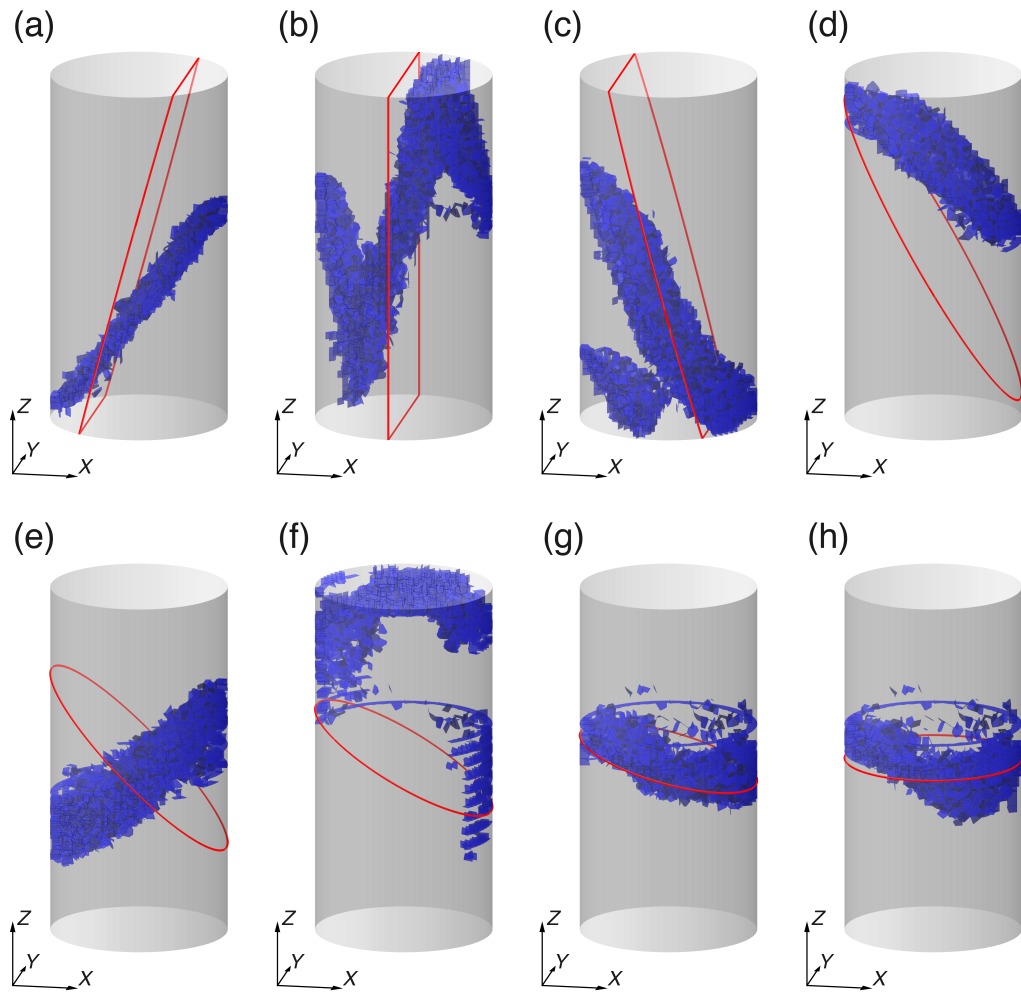


Figure 7: Comparison of fracture patterns for angles to bedding,  $\theta =$  (a)  $-15^\circ$ ; (b)  $0^\circ$ ; (c)  $15^\circ$ ; (d)  $30^\circ$ ; (e)  $45^\circ$ ; (f)  $60^\circ$ ; (g)  $75^\circ$ ; and (h)  $90^\circ$ . Note that the red contour of cylindric section for each case refers to the representative bedding plane.

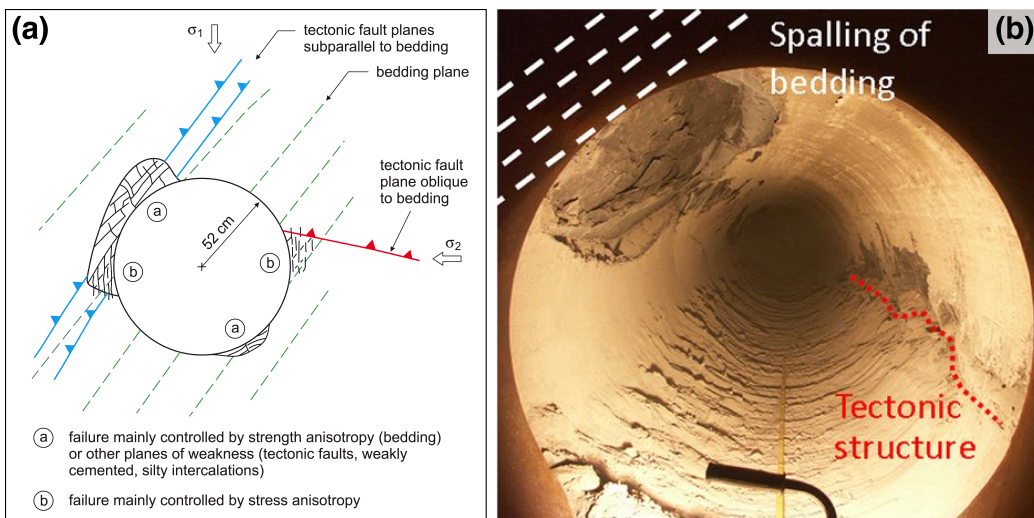


Figure 8: Excavation damage of the HG-A microtunnel: (a) conceptual diagram of the damaged zones and fault traces around the tunnel; and (b) observed damage formation along the tunnel (adapted from Marschall et al. 2006).



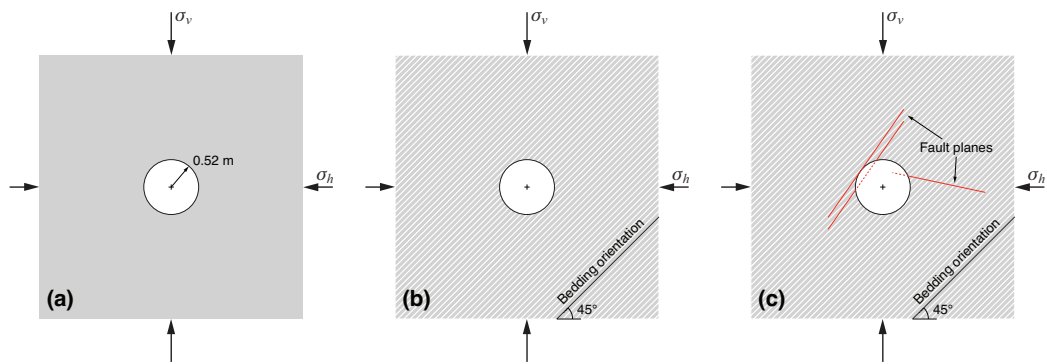


Figure 9: Modeling cases for three different geomechanical settings: (a) Case I for in-plane isotropy and intact formation; (b) Case II for in-plane anisotropy and intact formation; and (c) Case III for in-plane anisotropy and fault formation.

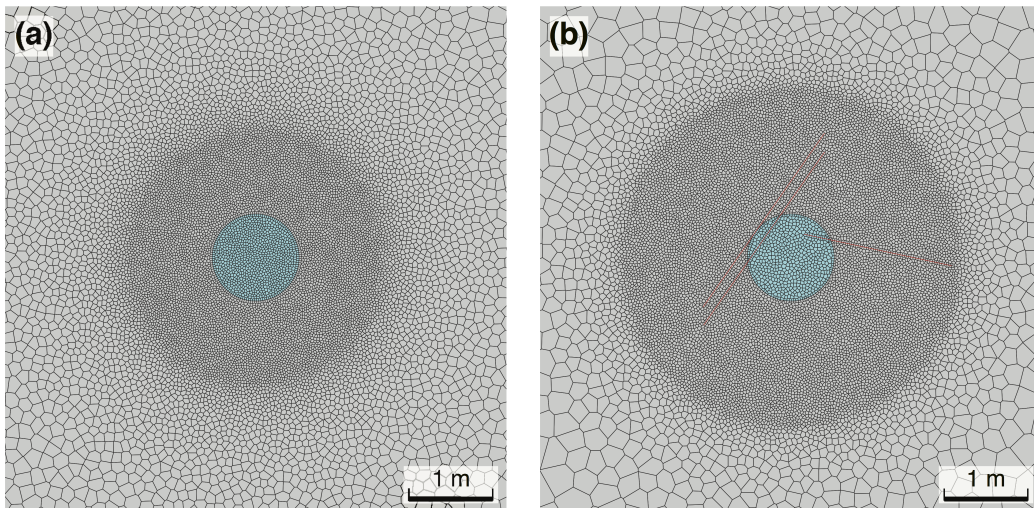


Figure 10: Voronoi discretizations for modeling tunnel geometries in (a) intact formation (Cases I and II) and (b) fault formation (Case III).

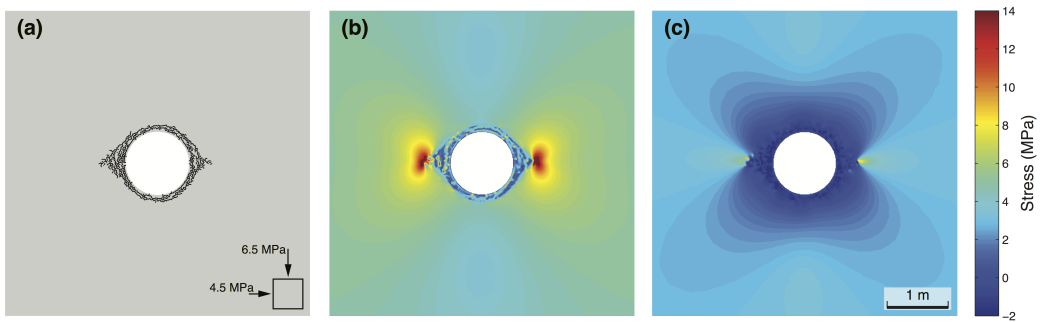


Figure 11: Results at the final stage of the simulation for Case I with in-plane isotropy and intact formation: (a) fracture pattern; (b) major principal stress; and (c) minor principal stress.

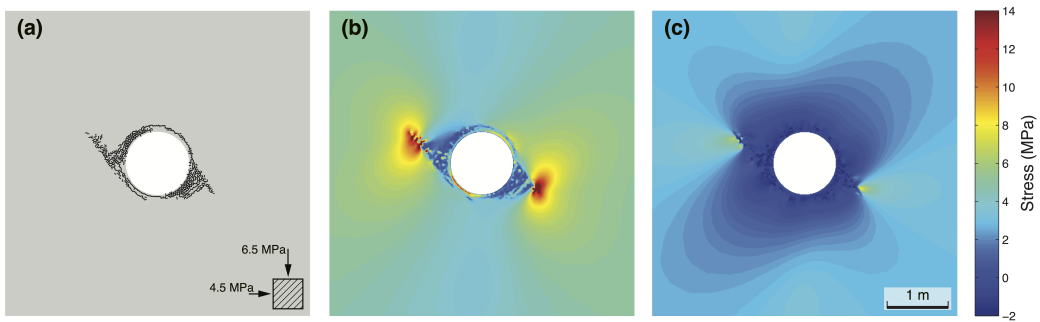


Figure 12: Results at the final stage of the simulation for Case II with in-plane anisotropy and intact formation: (a) fracture pattern; (b) major principal stress; and (c) minor principal stress.

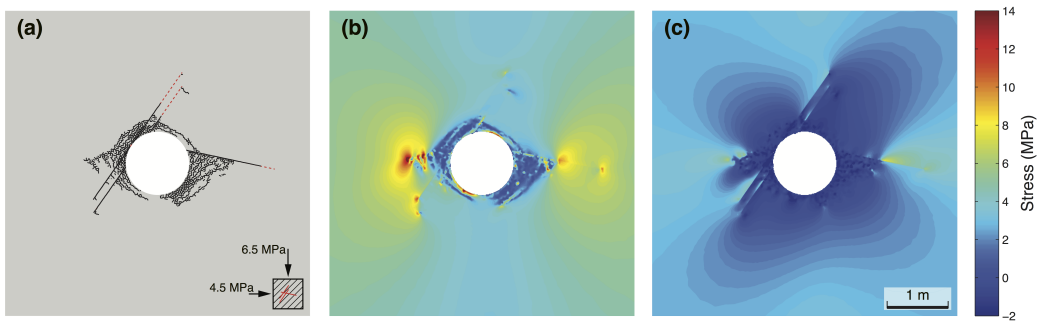


Figure 13: Results at the final stage of the simulation for Case III with in-plane anisotropy and fault formation: (a) fracture pattern; (b) major principal stress; and (c) minor principal stress.