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Publication Date

1985-02-01



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F.E. Anderson and J.M. Prausnitz

February 1985

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INHIBITION OF NATURAL-GAS HYDRATES

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February 1985

This work was supported by The Director, Office of Energy Research,
Office of Basic Energy Sciences, Chemical Sciences Division of the
U.S. Department of Energy under Contract DE-AC03-76SF00098.

Abstract

A molecular-thermodynamic correlation has been developed for calculating the inhibition effect of methanol on formation of hydrates in moist natural gas mixtures. Six phases are potentially present in these mixtures: gas, aqueous liquid, hydrocarbon liquid, ice, and hydrate structures I and II. For a given temperature and system composition, the molecular-thermodynamic method described here allows computation of the hydrate-point pressure as well as relative amounts and compositions of all coexisting phases. Good agreement is obtained when calculated results are compared with diverse experimental data reported in the literature. The correlation given here is useful for computer-aided design for natural-gas processing and transportation.

Scope

Numerous published articles are concerned with natural-gas/hydrate phase equilibria (Berecz and Balla-Achs, 1983). Where no inhibitor is present, correlations for hydrate systems are restricted to several parts of the general multiphase-multicomponent problem. A number of these studies are directed at the three-phase hydrate/vapor/aqueous-liquid or ice problem (Parrish and Prausnitz, 1972; Ng and Robinson, 1976). Others have treated as a separate problem the two-phase hydrate/gas region of the phase diagram (Sloan et al., 1976; Ng and Robinson, 1980; Aoyagi et al. 1980; Song and Kobayashi, 1982). Limited studies of the three-phase hydrate/aqueous-liquid/hydrocarbon-liquid portion of the problem have been made (Ng and Robinson, 1976, 1977). While several proprietary correlations exist (Gas Processors Assn.), no thermodynamically-consistent overall multicomponent-multiphase correlation for this hydrate-inhibition problem has appeared in the literature. Previous correlations for the effects of inhibitors on hydrate formation (Menten et al., 1981) have assumed that only condensed aqueous phases coexist with the gas and hydrate phases. This work covers all of the above mentioned equilibria in a unified framework suitable for computer-aided process design.

Conclusions and Significance

This work presents a method for predicting the amount of inhibitor which must be added to prevent hydrate formation in natural-gas processing. The method, based on molecular-thermodynamic models and a computational framework, calculates hydrate-point pressures and coexisting-phase fractions and compositions for natural-gas/water/methanol mixtures between 220 and 320°K and pressures to 500 bar. Consideration is given to the possible existence of all of the six potential phases: gas, aqueous liquid, hydrocarbon liquid, ice, and hydrate structures I and II; these phases may occur in various combinations. The calculation procedure accommodates nitrogen, methane, ethane, propane, n-butane, isobutane, n-pentane, carbon dioxide, and hydrogen sulfide along with methanol and water.

Fugacities of all components in the gas phase are calculated using a modification of the Redlich-Kwong (1949) equation of state similar to that of de Santis et al. (1974). Fugacities for all condensable components are calculated using activity coefficients derived from a modified version of the UNIQUAC equation where energy-of-interaction parameters are taken to be linearly temperature dependent. Liquid-phase fugacities for supercritical components are calculated using Henry's law. These molecular-thermodynamic models provide a good representation of the vapor-liquid-liquid equilibria present in natural-gas/water/methanol systems. Fugacities of all components in the hydrate phases are calculated using the theory of van der Waals-Platteeuw (1959).

At a given temperature and composition, the hydrate-point pressure is that where the fugacity of water in the hydrate phase is equal to that in all coexisting phases. The multiphase equilibrium computation

routine uses four sequentially-nested iterative procedures. Several special cases exist which allow elimination of one or two of these iterative routines.

Calculated results show good agreement with a wide variety of experimental data. The correlation presented here is compared with data for vapor-liquid-liquid equilibria, with methanol-water freezing-point depression, and with hydrate-formation pressures in both the gas/hydrate and condensed-fluid/hydrate regions of the phase diagram. The correlation is useful for computer-aided chemical-process design.

Introduction

At low temperatures and high pressures, solid hydrates can precipitate from moist natural gases, interfering with natural-gas processing and transportation. Hydrate-formation can be inhibited by the addition of a hydrophilic fluid which lowers the fugacity of water; a suitable and inexpensive fluid is methanol.

This work presents a molecular-thermodynamic method for calculating phase equilibria in systems containing water, natural gas and methanol as a function of temperature, pressure and composition. Such calculations are useful first, to determine operating conditions required to avoid hydrate formation and second, to determine the amount of methanol required to prevent hydrate formation at fixed operating conditions.

The thermodynamics of hydrate formation has been discussed by numerous authors, notably by Parrish and Prausnitz (1972), Sloan et al. (1976), Ng and Robinson (1976,1977,1980), Holder et al. (1980), Dharmawardhana et al. (1980), and by Menten et al. (1981). These discussions make use of a statistical-thermodynamic theory presented by van der Waals and Platteeuw (1959); that theory is also used here. However, previous work has been restricted to selected parts of the general multiphase problem; this work treats the entire multiphase problem within a molecular-thermodynamic framework.

Hydrates are members of the general class of solid inclusion compounds called clathrates. They are formed when low-molecular-weight components are in equilibrium with water at low temperature or high pressure. Water molecules form regular crystalline lattices which contain cavities (Byk and Fomina,1968). These cavities encage gas molecules which stabilize the lattice by van der Waals forces. Hydrates

occur in two distinct structures, I and II which differ in cavity size. Inhibitors, such as methanol, act by lowering the fugacity of water in coexisting phases; as a result, hydrates are formed at lower temperatures and higher pressures than those encountered in the absence of methanol. This behavior is analogous to the freezing-point depression of ice by methanol.

Hydrates are most frequently encountered in natural-gas transportation and processing. Natural gas, as withdrawn from the well, is typically saturated with water. In cold climates, the water content of such natural gas is often sufficiently high to cause hydrate formation in downstream transportation networks. Hydrate formation in these piping systems is undesired as it causes large pressure drops through the lines, and can halt the flow of the natural gas. Hydrate formation also occurs in association with natural-gas cryogenic liquefaction and separations. To prevent hydrate formation in these transportation networks and separation operations, two alternatives are available. The first, removal of the water at the well head, is expensive, as the level to which removal must be accomplished is often very low. The second, addition of a component to the natural gas-water mixture to prevent hydrate formation, can often be accomplished economically using methanol.

Molecular Thermodynamic Models and Data Reduction

Figure 1 shows phase equilibrium behavior of a natural-gas/water/methanol mixture. In Figure 1, line ECF represents the vapor pressure of the hydrate-forming gas. Lines ABCD represent the locus of hydrate-formation conditions for the case where no methanol is present. Below temperature T^0 , ice coexists with a gas phase below line AB, while above AB a gas phase coexists with a hydrate phase. At point B (lower quadruple point), four phases (gas, ice, aqueous liquid, and hydrate) coexist. Line BC describes the locus of three-phase gas-aqueous liquid-hydrate states. At point C (upper quadruple point), four phases (gas, hydrocarbon liquid, aqueous liquid, and hydrate) coexist. Line CD describes the locus of three-phase hydrocarbon-liquid/aqueous-liquid/hydrate states. When methanol is added to the binary mixture, lines BCD shift to the left, and lines GHI now express the locus of equilibrium states.

Condensed phases need not coexist with the hydrate phase; hydrate formation may occur directly from a gas phase. In such cases, the inhibition effect of methanol is greatly reduced since water and methanol are only sparingly soluble in the gas phase.

At equilibrium, the fugacity f of any component i is the same in all phases:

$$f_i^G = f_i^{L1} = f_i^{L2} = f_i^{H1} = f_i^{H2} = [f_w^a] \quad (1)$$

where G stands for gas, L1 for aqueous liquid, L2 for hydrocarbon liquid, H1 and H2 for hydrate structures I and II and a for ice. The fugacity of water in the ice phase is in parentheses to indicate that the ice phase is assumed to be pure. Methanol is not incorporated into

the hydrate structure, as indicated by Davidson et al. (1980). Given temperature, overall composition of the mixture, and expressions for the fugacities of each component in each phase, Equation 1 is solved to obtain the pressure where hydrate first forms (hydrate-point pressure) and to determine the proportions and compositions of each of the coexisting phases. Necessary molecular-thermodynamic models used for each of the six possible phases are described below.

Gas-Phase Fugacities

The fugacity of any component i in the gas phase is calculated using fugacity coefficient ϕ_i :

$$f_i^G = y_i \phi_i P \quad (2)$$

where y_i is the gas-phase mole fraction and where ϕ_i is obtained from a modification of the Redlich-Kwong (1949) equation of state:

$$P = \frac{\rho RT}{(1 - b_M \rho)} - \frac{a(T)_M \rho^2}{T^{1/2} (1 + b_M \rho)} \quad (3)$$

Conventional mixing rules relate mixture constants $a(T)_M$ and b_M to the composition and to pure-component constants $a(T)_{ii}$ and b_i :

$$a(T)_M = \sum_i \sum_j y_i y_j a_{ij} \quad (4)$$

and

$$b_M = \sum_i y_i b_i \quad (5)$$

Indices i and j in Equations 4 and 5 run over all components in the mixture.

Parameter b_i is evaluated for all components using the

corresponding-states expression of Chueh and Prausnitz (1968). Following de Santis et al. (1974), we separate the temperature dependent $a(T)_{ii}$ parameter into nonpolar and polar contributions:

$$a(T)_{ii} = a_i^{(0)} + \frac{a_i^{(1)}}{T^3} \quad (6)$$

For nonpolar components, $a_i^{(1)}$ is zero; for water, methanol, hydrogen sulfide and carbon dioxide $a_i^{(1)} > 0$. For nonpolar components $a_i^{(0)}$ is evaluated using critical properties. Redlich-Kwong constants $a(T)_{ii}$ and b_i are related to the second virial coefficient, B_{ii} :

$$B_{ii} = b_i - \frac{a(T)_{ii}}{RT} \quad (7)$$

Similarly,

$$B_{ij} = \frac{(b_i + b_j)}{2} - \frac{a(T)_{ij}}{RT} \quad (8)$$

Following de Santis et al., for polar components, $a_i^{(0)}$ and $a_i^{(1)}$ are evaluated using Equation 7 and data for the temperature dependence of the second virial coefficient. Table 1 gives $a_i^{(0)}$ and $a_i^{(1)}$ for all polar components.

For polar-polar binaries a_{ij} is calculated from:

$$a(T)_{ij} = \left[(a_i^{(0)} a_j^{(0)})^{1/2} + \frac{[a_i^{(1)} a_j^{(1)}]^{1/2}}{T^3} \right] (1 - k_{ij}) \quad (9)$$

All other a_{ij} parameters are calculated from:

$$a(T)_{ij} = (a_i^{(0)} a_j^{(0)})^{1/2} (1 - k_{ij}) \quad (10)$$

Binary parameters k_{ij} are fixed using two methods. Most k_{ij} values were obtained using second-virial cross-coefficient data and Equation 8. For some binaries, however, such second-virial cross-coefficient data

are unavailable. For these systems, k_{ij} were obtained from a fit of our model to binary VLE data. In a few cases, the k_{ij} values obtained from second-virial cross-coefficient data gave poor representations of VLE data; in these cases the k_{ij} values were modified to improve agreement with VLE data. Table 2 presents all k_{ij} values used in this work.

Liquid-Phase Fugacities

Natural-gas/water/inhibitor mixtures contain two types of components: condensible components (eg. water, methanol, propane) and non-condensable components (methane and nitrogen). For condensible components, we calculate fugacities in any liquid phase from:

$$f_i^L = x_i \gamma_i f_i^O \quad (11)$$

where f_i^O is the fugacity of pure liquid i at system temperature. Activity coefficients, γ_i , are obtained from a modification of the UNIQUAC equation (Abrams and Prausnitz, 1975); binary UNIQUAC energy-of-interaction parameters ($\frac{\Delta U_{ij}}{R}$ and $\frac{\Delta U_{ji}}{R}$) are taken to be linearly dependent on temperature:

$$\frac{\Delta U_{ij}}{R} = U_{ij}^{(0)} + U_{ij}^{(1)}T \quad (12)$$

With the exception of the water-methanol binary, coefficient $U_{ij}^{(1)}$ is taken as zero for binary systems where no LLE exists. Binary parameters are obtained by fitting binary VLE and LLE data. Figure 2 shows a correlation of vapor-liquid-liquid equilibria (VLLE) for the water-propane system and Figure 3 shows a correlation for the water/hydrogen-sulfide binary. Table 3 gives all UNIQUAC parameters used in this work.

UNIQUAC parameters for the water-methanol system are of particular importance because the fugacity of water in the aqueous liquid phase is

the key quantity that determines hydrate inhibition. Parameters for this binary were obtained from a fit to water-methanol freezing-point-depression data (Miller and Carpenter, 1964; Ross, 1954) and from data on methanol inhibition of methane hydrate (Ng and Robinson, 1983,1984). Figure 4 shows a correlation for the freezing-point depression of water by methanol.

An economic analysis of any hydrate-inhibition process using methanol is intimately tied to the amount of methanol required per mole of water in the natural-gas mixture. Methanol losses in most processes are directly related to the solubility of methanol in natural-gas liquids. Using binary methanol-hydrocarbon VLE, LLE and ternary VLLE for methanol-hydrocarbon-water systems (Noda et al.,1975; Ng and Robinson, 1983), methanol-hydrocarbon UNIQUAC parameters were determined to maximize the accuracy of the predicted partition coefficient of methanol between aqueous and natural-gas liquid phases.

For condensible components, the standard-state fugacity is given by:

$$f_i^o = P_i^{\text{Sat}} \phi_i^{\text{Sat}} \exp \left[\frac{v_i^L (P - P_i^{\text{Sat}})}{RT} \right] \quad (13)$$

where P_i^{Sat} is the vapor pressure of i , ϕ_i^{Sat} is the fugacity coefficient of saturated gas i and v_i^L is the molar volume of i . For all components except water, vapor pressures are given by the Antoine equation. For water above the ice point, the equation of Bain (1964) is used for vapor pressure. The molar volume, corrected for temperature and pressure variations, was obtained from pure-component data where possible, and elsewhere from the liquid-density correlation of Chueh and Prausnitz (1969).

Below the ice-point temperature, the fugacity of pure

hypothetical-liquid water is calculated from:

$$f_w^o = f_w^a(T, p_w^{\text{Sat}, a}) \exp \left[\frac{\Delta h_w^{\text{Fus}}(T_t)}{RT} \left[1 - \frac{T}{T_t} \right] + \frac{1}{RT} \int_{T_t}^T \Delta C_p^{L-a} dT - \int_{T_t}^T \frac{\Delta C_p^{L-a}}{RT} dT \right] \exp \left[\frac{v_w^L (P - p_w^{\text{Sat}, a})}{RT} \right] \quad (14)$$

Above the ice-point temperature Equation 13 is used for f_w^o . The heat-capacity difference between ice and liquid water is calculated from:

$$\Delta C_p^{L-a} = \Delta C_p^{(0)} + \frac{\Delta C_p^{(1)}}{T} + \frac{\Delta C_p^{(2)}}{T^2} + \frac{\Delta C_p^{(3)}}{T^3} \quad (15)$$

The constants in Equation 15 are evaluated using the heat-capacity data of Angell et al. (1973) for subcooled liquid water and the heat-capacity data of Giauque and Stout (1936) for ice. This treatment produces excellent agreement with the data of Kraus and Greer (1984) for the vapor pressure of subcooled liquid water. Table 4 gives the enthalpy of fusion and the constants $\Delta C_p^{(0)}$, $\Delta C_p^{(1)}$, $\Delta C_p^{(2)}$ and $\Delta C_p^{(3)}$. The fugacity of water in the ice phase is calculated from:

$$f_w^a = p_w^{\text{Sat}, a} \phi_w^{\text{Sat}, a} \exp \left[\frac{v_w^a (P - p_w^{\text{Sat}, a})}{RT} \right] \quad (16)$$

The vapor pressure of ice is given by Jansco et al. (1970).

For components which are supercritical in part of the temperature range of interest (carbon dioxide and ethane), f_i^o is calculated using the corresponding-states method of Lyckman et al. (1968). This correlation is used for all temperatures. For such components, the reference pressure for Poynting corrections is taken to be zero consistent with the work by Lyckman et al. (1968).

For supercritical components (nitrogen and methane), fugacities in the liquid phase are obtained from a pressure-corrected Henry's Law:

$$f_i^L = x_i H_{iM} \exp \left[\frac{\bar{v}_i^\infty P}{RT} \right] \quad (17)$$

where H_{iM} Henry's constant of component i in the liquid mixture, is related to Henry's constants of components i in pure condensible components j , H_{ij} , by:

$$\ln H_{iM} = \sum_j \ln H_{ij} \left[\frac{x_j \bar{v}_j^L}{\sum_k x_k \bar{v}_k^L} \right] \quad (18)$$

Indices j and k are carried over all condensible components in the mixture. Mole fractions x_j and x_k are normalized such that they reflect only condensible components in the liquid phase. The partial molar volume of component i at infinite dilution, $\bar{v}_i^\infty$ is evaluated from the method presented by Lyckman et al. (1968). For the temperature range of interest here, Henry's constants are given by:

$$\ln H_{ij} = H_{ij}^{(0)} - \frac{H_{ij}^{(1)}}{T} \quad (19)$$

where the fitting constants are obtained from vapor-liquid equilibrium data for each binary pair. These constants are listed in Table 5.

Hydrate-Phase Fugacities

As discussed by van der Waals and Platteeuw (1959), hydrate-forming molecules are viewed as adsorbed in the cavity sites; this adsorption is described by a Langmuir adsorption model. The van der Waals-Platteeuw theory uses the Gibbs-Duhem equation to provide a model for the fugacity

of water in a hydrate phase as a function of f_j , the fugacities of hydrate-forming components in coexisting phases. Each cavity is envisioned as spherical, and the gas-cavity wall interaction is described by the Kihara potential function. The reference fugacity for water f_w^β , is that in the hypothetical empty hydrate lattice. The fugacity of water f_w^H in the hydrate phase is found from:

$$f_w^H = f_w^\beta \exp \left[\frac{-\Delta\mu_w^{\beta-H}}{RT} \right] \quad (20)$$

where

$$\Delta\mu_w^{\beta-H} = \mu_w^\beta - \mu_w^H \quad (21)$$

The difference in chemical potential, $\Delta\mu_w^{\beta-H}$ is obtained from the van der Waals-Platteeuw expression (Parrish and Prausnitz, 1972, van der Waals and Platteeuw, 1959):

$$\Delta\mu_w^{\beta-H} = -RT \sum_m \nu_m \ln \left[1 + \sum_j C_{mj} f_j \right] \quad (22)$$

Langmuir constant, $C_{mj}(T)$ accounts for gas-water interactions in the hydrate cavities. The Langmuir constant is calculated from:

$$C_{mj}(T) = \frac{4\pi}{kT} \int_0^\infty \exp \left[\frac{-\omega_{mj}(r)}{kT} \right] r^2 dr \quad (23)$$

As shown by McKoy and Sinanoglu (1963), a sum of all gas-water interactions in the cavity yields $\omega_{mj}(r)$, the spherically-symmetric cell-potential function in terms of Kihara parameters ϵ_j , σ_j , and a_j . The integral in Equation 23 is evaluated using Gaussian integration. The Kihara hard-core parameter a_j , is determined from second-virial-coefficient data (Parrish and Prausnitz, 1972), while Kihara energy and size parameters ϵ_j and σ_j are determined by a fit of the model to

hydrate-dissociation-pressure data. All Kihara parameters are given in Table 6.

The fugacity of water f_w^β in the empty hydrate lattice is calculated as a function of temperature and pressure using the difference in chemical potential of water between the empty hydrate lattice and ice (or liquid water) following the method outlined by Holder et al. (1980). If the temperature is below the ice point, we define:

$$\Delta\mu_w^{\beta-\alpha} = \mu_w^\beta - \mu_w^\alpha \quad (24)$$

and if the temperature is above the ice point, we define:

$$\Delta\mu_w^{\beta-L} = \mu_w^\beta - \mu_w^L \quad (25)$$

We calculate f_w^β from:

$$f_w^\beta = f_w^\alpha \exp\left[\frac{\Delta\mu_w^{\beta-\alpha}}{RT}\right] \quad (26)$$

or

$$f_w^\beta = f_w^{L^0} \exp\left[\frac{\Delta\mu_w^{\beta-L}}{RT}\right] \quad (27)$$

depending on the temperature. The chemical potential differences defined by Equations 24 and 25 are calculated using the method outlined by Holder et al. (1980):

$$\frac{\Delta\mu_w^{\beta-\alpha}}{RT} = \frac{\Delta\mu_w^0}{RT^0} - \int_{T^0}^T \frac{\Delta h_w^{\beta-\alpha}}{RT^2} dT + \int_0^P \frac{\Delta v_w^{\beta-\alpha}}{RT} dP \quad (28)$$

and

$$\frac{\Delta\mu_w^{\beta-L}}{RT} = \frac{\Delta\mu_w^0}{RT^0} - \int_{T^0}^T \frac{\Delta h_w^{\beta-\alpha} + \Delta h_w^{Fus}}{RT^2} dT + \int_0^P \frac{\Delta v_w^{\beta-\alpha} + \Delta v_w^{Fus}}{RT} dP \quad (29)$$

Molar volume differences here are assumed to be temperature independent; however, the molar enthalpy difference is given by:

$$\Delta h_w^{\beta-\alpha} = \Delta h_w^{\beta-\alpha^0} + \int_{T^0}^T \Delta C_P^{\beta-\alpha,L} dT \quad (30)$$

Values of $\Delta \mu^0$ and $\Delta h_w^{\beta-\alpha}$ determined by Dharmawardhana et al. (1980) were used. The heat-capacity difference in Equation 30 is correlated using the expression provided by Holder et al. (1980).

Parameters for the molar-volume difference between the empty hydrate lattice and ice are slightly different from those used by Dharmawardhana et al. (1980). For structure-I hydrate we follow Dharmawardhana et al. and use $3.0 \text{ cm}^3/\text{mole}$ but for structure-II hydrate we use $1.2 \text{ cm}^3/\text{mole}$ instead of the previously reported $3.4 \text{ cm}^3/\text{mole}$. This change is necessary to calculate equilibria in the liquid-hydrocarbon/hydrate region of the propane-water phase diagram. In this region, the fugacity of propane in the liquid phase is used in Equation 22. The Poynting corrections contained in the liquid-propane fugacity and in the empty-hydrate-lattice fugacity cause the hydrate-phase water fugacity to increase with pressure. Without our modification, the increase of the hydrate-phase water fugacity with pressure is greater than that of water in the liquid phases and calculation of phase equilibria is not possible. This modification is only important for propane hydrate due to its particularly rapid increase of hydrate-formation pressure with temperature. The volume-difference parameters used by Dharmawardhana et al. were obtained from x-ray crystallographic studies on filled hydrate lattices of von Stackelberg and Muller (1954).

Results and Discussion

Figure 5 shows the inhibiting effect of methanol on the formation of methane hydrate. Calculated results agree well with methanol-inhibition data of Ng and Robinson (1983,1984). Figure 6 shows the water content of methane gas in equilibrium with liquid water and hydrate for several isobars. At low inverse temperature calculated results are compared with the dew-point data of Olds et al. (1942) and at high inverse temperature our correlation is compared to the hydrate-point data of Aoyagi et al. (1980). In both cases, slight discrepancies occur at low temperature due to inadequacies of the van der Waals-Platteeuw model. At low temperatures, calculated water fugacities are based on Kihara parameters obtained from experimental high temperature data.

Figure 7 shows calculated gas-phase fugacities which correspond to the smoothed hydrate-point compositions given by Aoyagi et al. (1980). For each composition, points denote the hydrate-formation pressure measured by Aoyagi et al. (1980). Figure 7 also gives the calculated fugacity of water in the hydrate phase based on Kihara parameters determined from experimental three-phase hydrate/aqueous-liquid/gas data. Intersections of fugacity curves correspond to the equilibrium conditions shown in Figure 6. To match the data of Aoyagi et al. (1980), calculated intersections must occur at the pressures denoted by points in Figure 7. For such matching, the pressure dependence of the hydrate-phase water fugacity must be different. An accurate fit of all experimental data is limited by results of the van der Waals-Platteeuw theory.

Ng and Robinson (1976) proposed an empirical modification of the van der Waals-Platteeuw model directed toward improving the fit of

hydrate pressures for gas mixtures. However, since Ng and Robinson (1980) found that their empirical modification is insufficient to fit the data of Aoyagi et al. (1980), they proposed an ad hoc method for correcting their hydrate-phase fugacities. Unfortunately, this method is thermodynamically inconsistent. The thermodynamic ambiguity arises from two different methods for calculation of f_w^β . Ng and Robinson (1980) calculated $\Delta\mu_w^{\beta-H}$ based on previously determined Kihara potential parameters (Ng and Robinson, 1977). To determine these Kihara parameters, Ng and Robinson (1977) used the method for calculation of $\Delta\mu_w^{\beta-a,L}$ proposed by Parrish and Prausnitz (1972); this is thermodynamically equivalent to the assumption of a function for f_w^β . Based on their previously defined Kihara parameters and the hydrate/gas data of Aoyagi et al. (1980), Ng and Robinson (1980) fit new functional forms for f_w^β for both hydrate structure types. Presumably, Ng and Robinson (1980) use their new functions for f_w^β in the hydrate/gas region of the phase diagram and the method outlined by Parrish and Prausnitz for the hydrate/gas/aqueous-liquid or ice region of the phase diagram.

Sloan et al. (1976) and Aoyagi et al. (1980) used the van der Waals-Platteeuw model for hydrate-phase fugacities and the virial equation for gas-phase fugacities. In their work, the virial equation was truncated after the third term. Applicability of their treatment was limited to the methane-water system; no attempt was made to calculate phase equilibria for other systems. Using their hydrate/gas data and previously determined Kihara and empty hydrate phase parameters, Sloan et al. (1976) and Aoyagi et al. (1980) fit second and third virial cross-coefficients for the methane-water system. However, no comparison was given of calculated and experimental dew-points for the methane-

water system.

Song and Kobayashi (1982) extended the work of Aoyagi et al. (1980) by measuring the water content above the hydrate of a methane-propane gas mixture. They used the Soave modification of the Redlich-Kwong equation of state for gas-phase fugacities. They were forced to resort to pressure-dependent k_{ij} values to fit their data for the water content of a methane-propane gas mixture in equilibrium with hydrate. Unfortunately, pressure dependent k_{ij} values lead to thermodynamic inconsistency.

Figures 8-11 show the calculated inhibition effect of methanol on hydrate formation in the ethane, propane, hydrogen sulfide, and carbon dioxide-water systems. Agreement with experimental data is good. For the propane and carbon dioxide systems, slight discrepancies are due to several factors. First, Kihara parameters obtained from high-temperature data are used to calculate equilibria at low temperatures. Second, UNIQUAC parameters based on high-temperature data are extrapolated to low temperature. UNIQUAC parameters for aqueous binaries are based on VLE and LLE data; these data must be obtained above the ice-point temperature. Some extrapolation is therefore necessary to make low-temperature calculations. Finally, binary UNIQUAC parameters are used for multicomponent systems. This "scale-up" approximation is probably responsible for the discrepancies in Figure 11.

For a methane-propane gas mixture, Figure 12 shows calculated results that are in good agreement with the data of Ng and Robinson (1983,1984). However, agreement between calculations and other gas-mixture data of Ng and Robinson (1984) is generally not as good as that shown in Figure 12. A possible source of disagreement follows from the

"scale-up" approximation: Kihara parameters based on binary data are used to calculate multicomponent equilibria.

Computational Procedure

Given a natural-gas/water/methanol mixture of known overall composition and temperature, the phase-equilibrium computation routine calculates the hydrate-formation pressure and the relative amounts and compositions of all coexisting phases. The phase-equilibrium computation routine uses four sequentially-nested iterative-calculational procedures. The first iterative routine solves for the density (Topliss, 1985) of a gas mixture at a given temperature, pressure, and composition using the equation of state. Based on this density, we calculate fugacity coefficients. K-factors are then calculated using these fugacity coefficients with the other molecular-thermodynamic models. The second iterative procedure uses these K-factors to perform flash calculations yielding the relative amounts and compositions of the phases: gas, aqueous liquid, and hydrocarbon liquid. The third iterative routine iterates around the flash routine to solve for the fraction of the total water in the ice phase. The fourth and final routine iterates around the other routines to solve for the hydrate-point pressure where the fugacity of water in the hydrate phase is equal to that in any other phase. Several special cases exist which allow simplification of this general procedure.

Amount of Methanol Needed for Inhibition

Some hydrate-inhibition applications require a method for calculating the amount of methanol needed to prevent hydrate formation at a

fixed pressure, temperature and gas composition. Since the program calculates hydrate-formation pressures at a given temperature and methanol composition, for the gas mixture of interest we must first prepare a plot similar to Figure 12. Using these graphical data, we prepare a cross-plot giving hydrate-formation temperature as a function of methanol concentration for the isobars of interest. Figure 13 shows several isobars for the gas mixture of Figure 12. Figure 13 is similar to the freezing-point depression diagram shown in Figure 4. Figure 13 enables us to obtain the desired methanol composition. To illustrate, let us assume that we have a gas mixture of the composition of Figures 12 and 13, saturated with water at 20 bar and 300°K. We now wish to compress this gas to 50 bar and then cool it to 270°K without hydrate formation. By performing a flash calculation, we find that the initial gas contains 1.889×10^{-3} mole fraction water. Using Figure 13, we find that to prevent hydrate-formation at 270°K and 50 bar, we require 0.336 weight fraction (0.221 mole fraction) methanol in the aqueous-liquid phase. Hence, conservatively assuming that all of the water in the initial gas condenses into the liquid phase we must add at least 4.184×10^{-4} moles of methanol per mole of inlet gas.

Acknowledgment

This work was supported by the Director, Office of Energy Research, Office of Basic Energy Sciences, Chemical Sciences Division of the U.S. Department of Energy under contract DE-AC03-76SF00098.

Notation

- a = Kihara hard-core parameter for component j
 $a(T)$ = Redlich-Kwong constant
 B_{ii} = second virial coefficient of component i
 b = Redlich-Kwong constant
 $C_{mj}(T)$ = Langmuir adsorption constant for component j on cavity type m
 f = fugacity
 f_w^a = fugacity of water in ice phase
 f_i^o = reference state fugacity for pure liquid i
 f_w^β = fugacity of water in the hypothetical empty-hydrate lattice
 f_w^H = fugacity of water in the hydrate phase
 H_{ij} = Henry's constant for component i in liquid j
 Δh_w^{Fus} = enthalpy of fusion of water
 $\Delta h_w^{\beta-\alpha}$ = enthalpy difference between empty hydrate lattice and ice
 k = Boltzmann's constant
 k_{ij} = binary parameter for Redlich-Kwong $a(T)_M$
 P = pressure (absolute)
 p_i^{Sat} = vapor pressure of component i
 R = gas constant
 r = radial distance in hydrate cavity
 T = temperature (absolute)
 T_t = triple-point temperature of water
 v_w^a = molar volume of ice
 $\bar{v}$ = partial molar volume at infinite dilution
 $\Delta v_w^{\beta-\alpha}$ = difference in volume between empty hydrate lattice and ice
 Δv_w^{Fus} = change in volume of water upon fusion
 x = liquid phase mole fraction

y = gas phase mole fraction

Greek Letters

γ = activity coefficient

ϵ = Kihara energy parameter

ν_m = number of cavities of type m per water molecule in hydrate

μ_w^α = chemical potential of water in ice phase

μ_w^β = chemical potential of water in empty hydrate lattice

μ_w^H = chemical potential of water in hydrate phase

$\Delta\mu_w^0$ = standard-state chemical potential difference between hydrate and ice

$\Delta\mu_w^{\beta-H}$ = difference in chemical potential of water between empty and filled hydrate lattice

$\Delta\mu_w^{\beta-\alpha}$ = difference in chemical potential of water between empty hydrate lattice and ice

$\Delta\mu_w^{\beta-L}$ = difference in chemical potential of water between empty hydrate lattice and pure liquid water

ρ = molar density

σ = Kihara size parameter

ϕ = fugacity coefficient

$\omega_{mj}(r)$ = cavity potential function for component j in cavity type m

Superscripts

α = ice phase

β = hypothetical empty hydrate lattice phase

$\beta-\alpha$ = difference between empty hydrate lattice and ice

$\beta-H$ = difference between empty and filled hydrate lattices

- β -L = difference between empty hydrate lattice and pure liquid water
- G = gas phase
- H1 = hydrate structure I phase
- H2 = hydrate structure II phase
- L- α = difference between liquid and ice
- L1 = aqueous liquid phase
- L2 = natural gas liquid phase
- Sat = saturation conditions
- o = standard state
- (0) = reference term in perturbation expansion
- (1) = first term in perturbation expansion
- (2) = second term in perturbation expansion
- (3) = third term in perturbation expansion

Subscripts

- i, j = component
- M = mixture
- m = cavity type
- w = water

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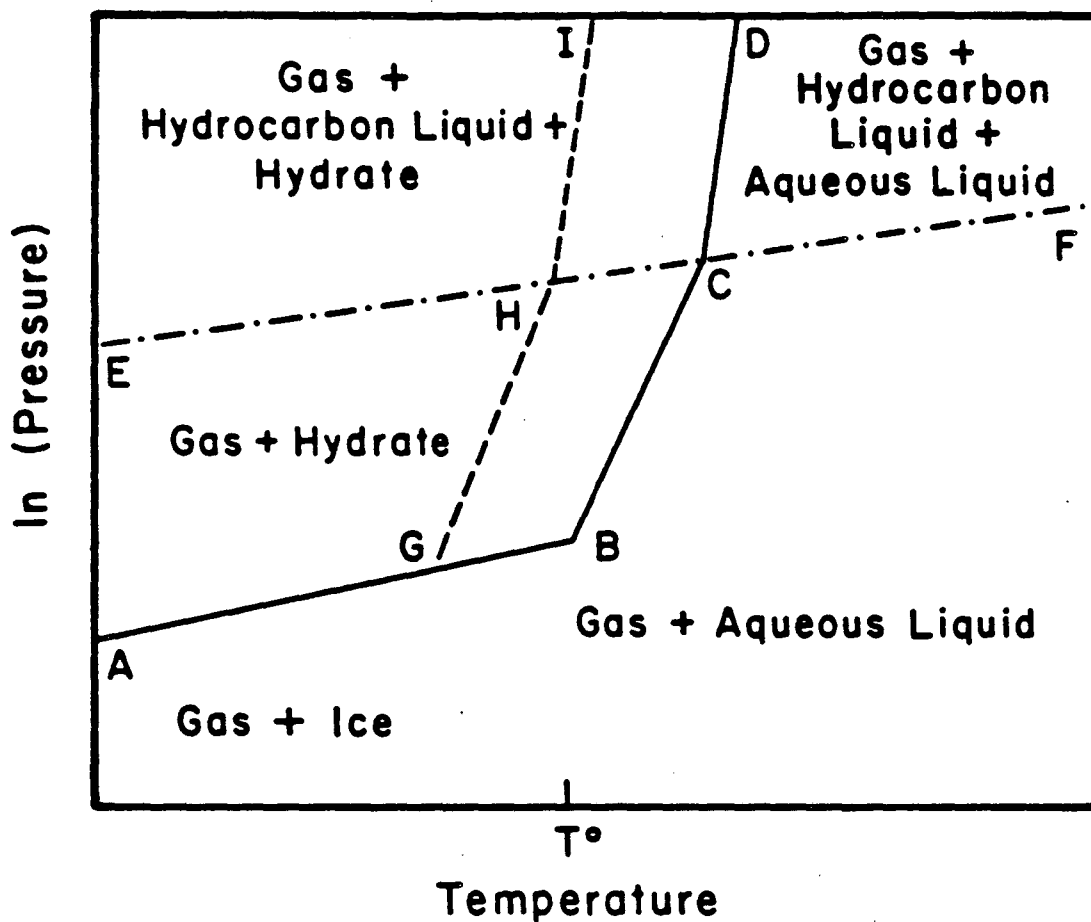
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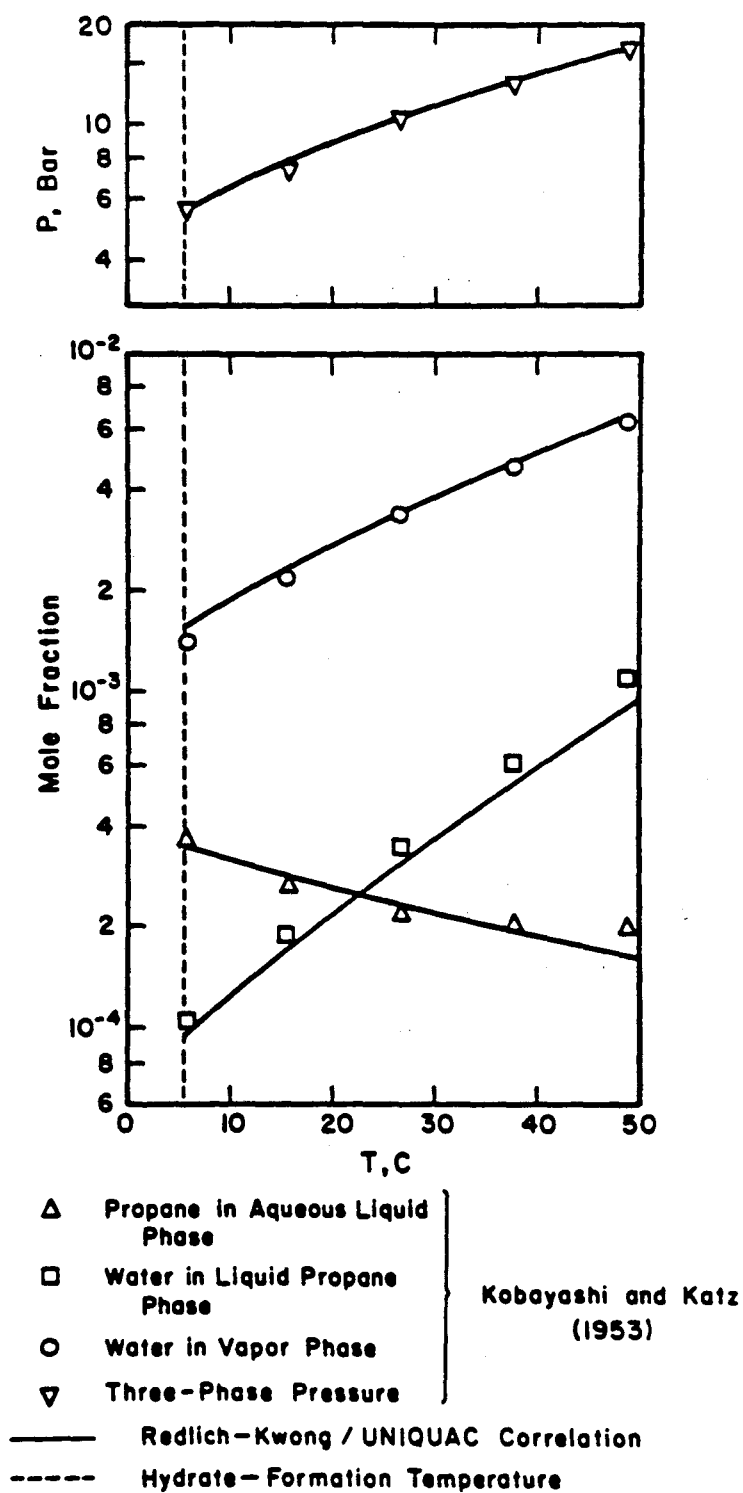
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- Hydrate-Formation Pressure :
No Methanol Present
- Hydrate-Formation Pressure :
Methanol is Present
- .-.-.- Vapor Pressure of Hydrate
Forming Gas

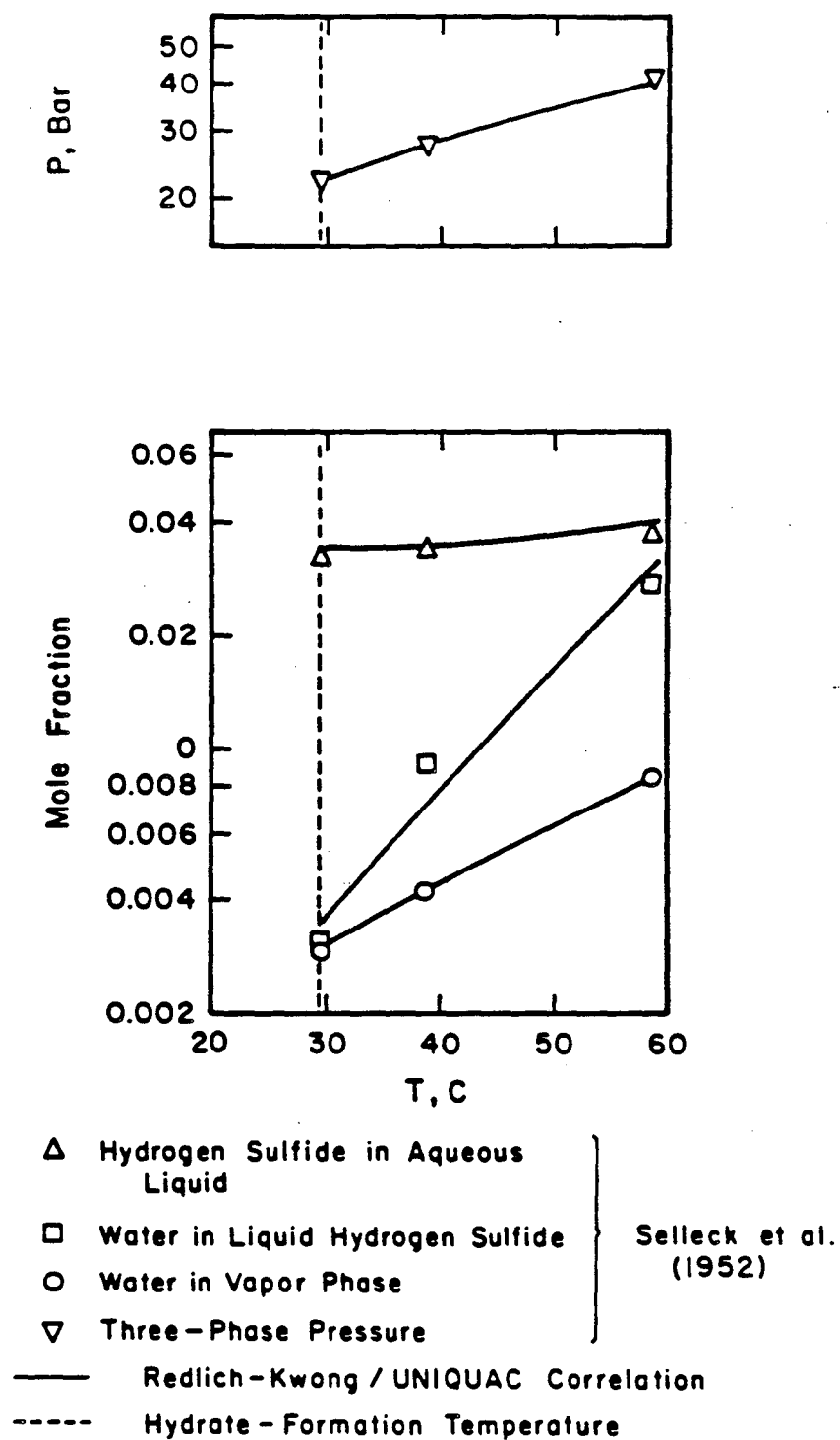
Hydrate-Formation Conditions in
Natural-Gas / Water / Methanol Mixtures

Figure 1



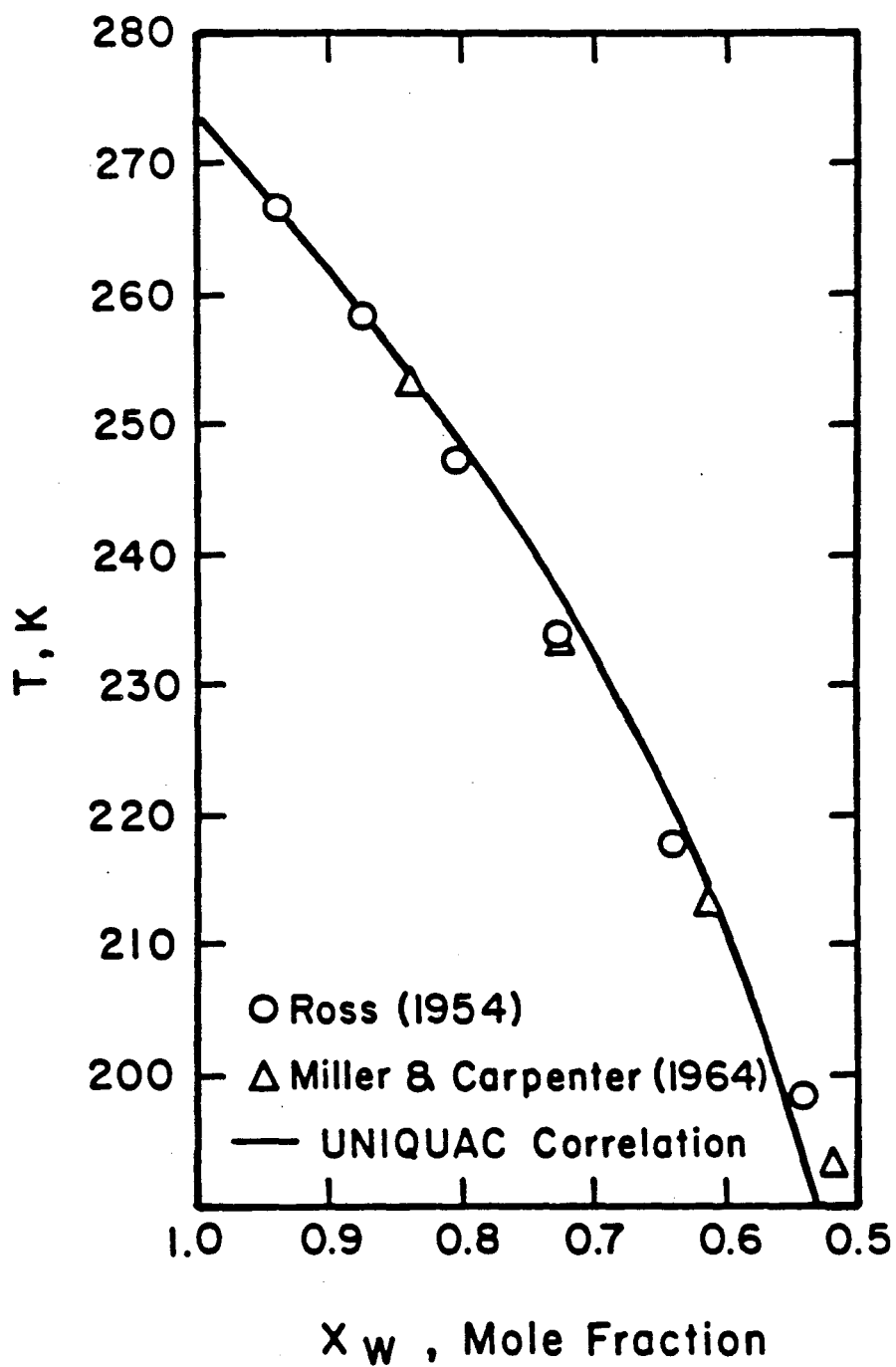
Three-Phase Compositions and Pressures for
Water-Propane Mixtures

Figure 2



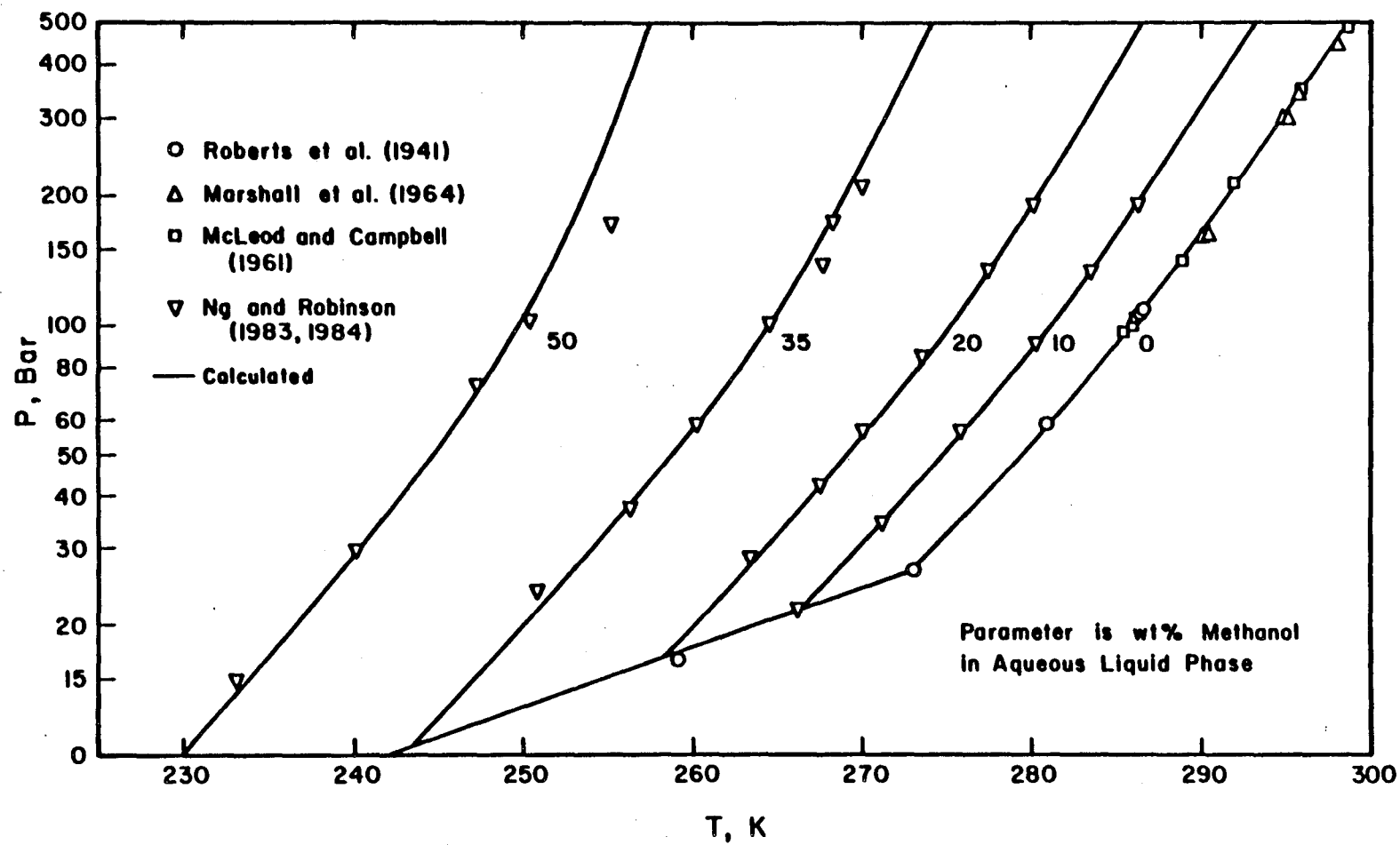
Three-Phase Compositions and Pressures for
Water/Hydrogen-Sulfide Mixtures

Figure 3



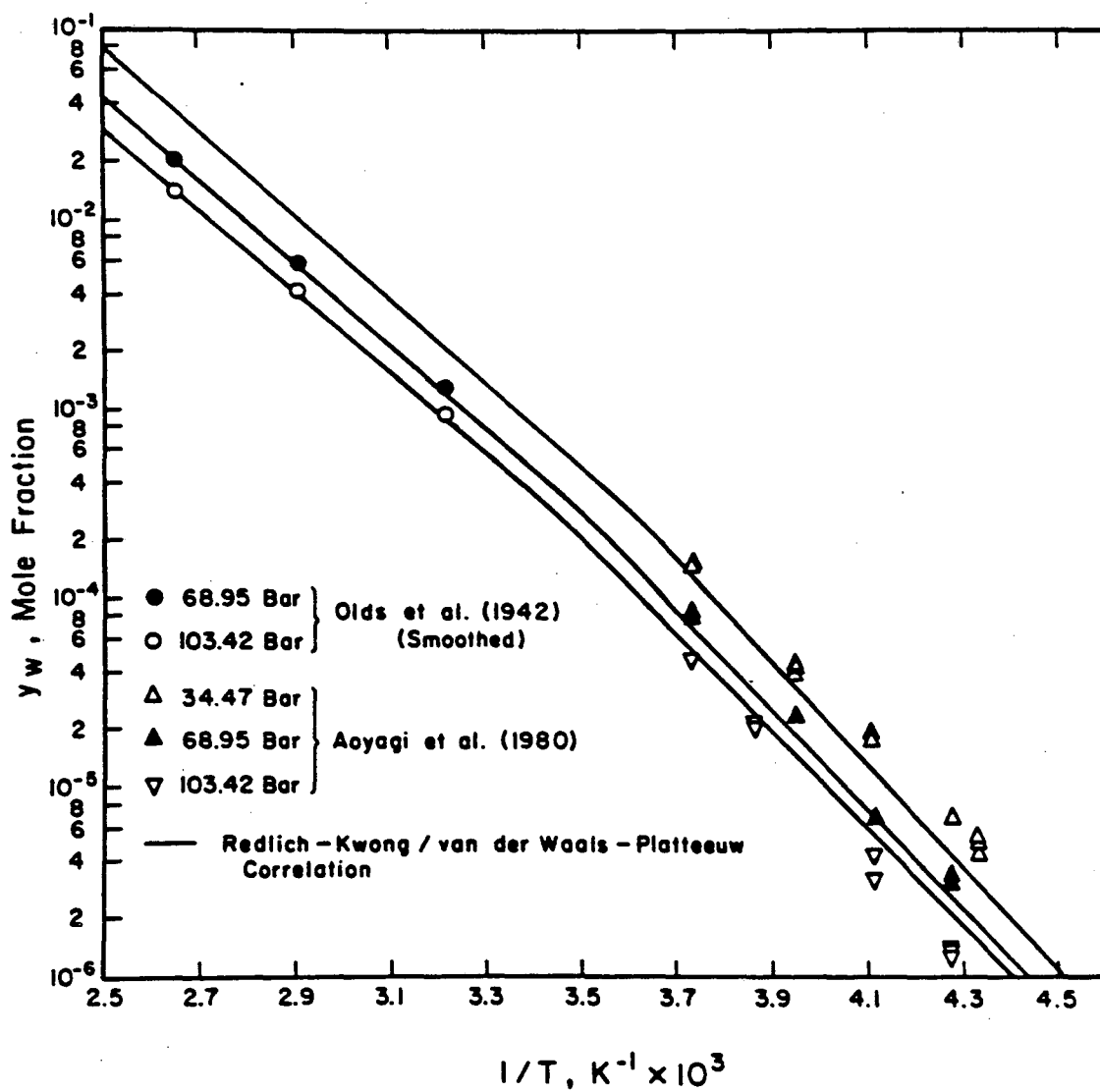
Freezing Point of Water – Methanol Solutions

Figure 4



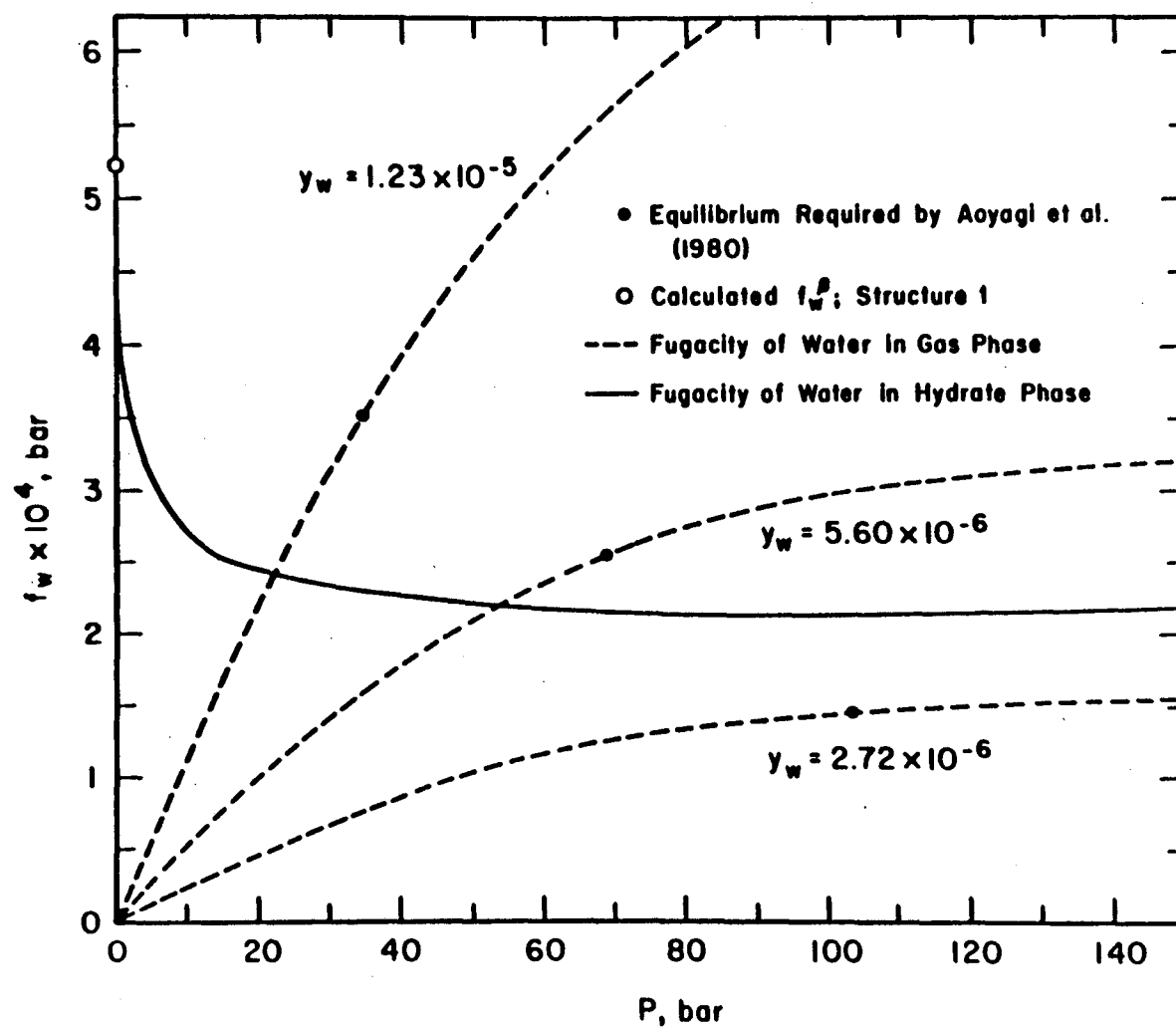
Inhibition of Methane Hydrate by Methanol

Figure 5



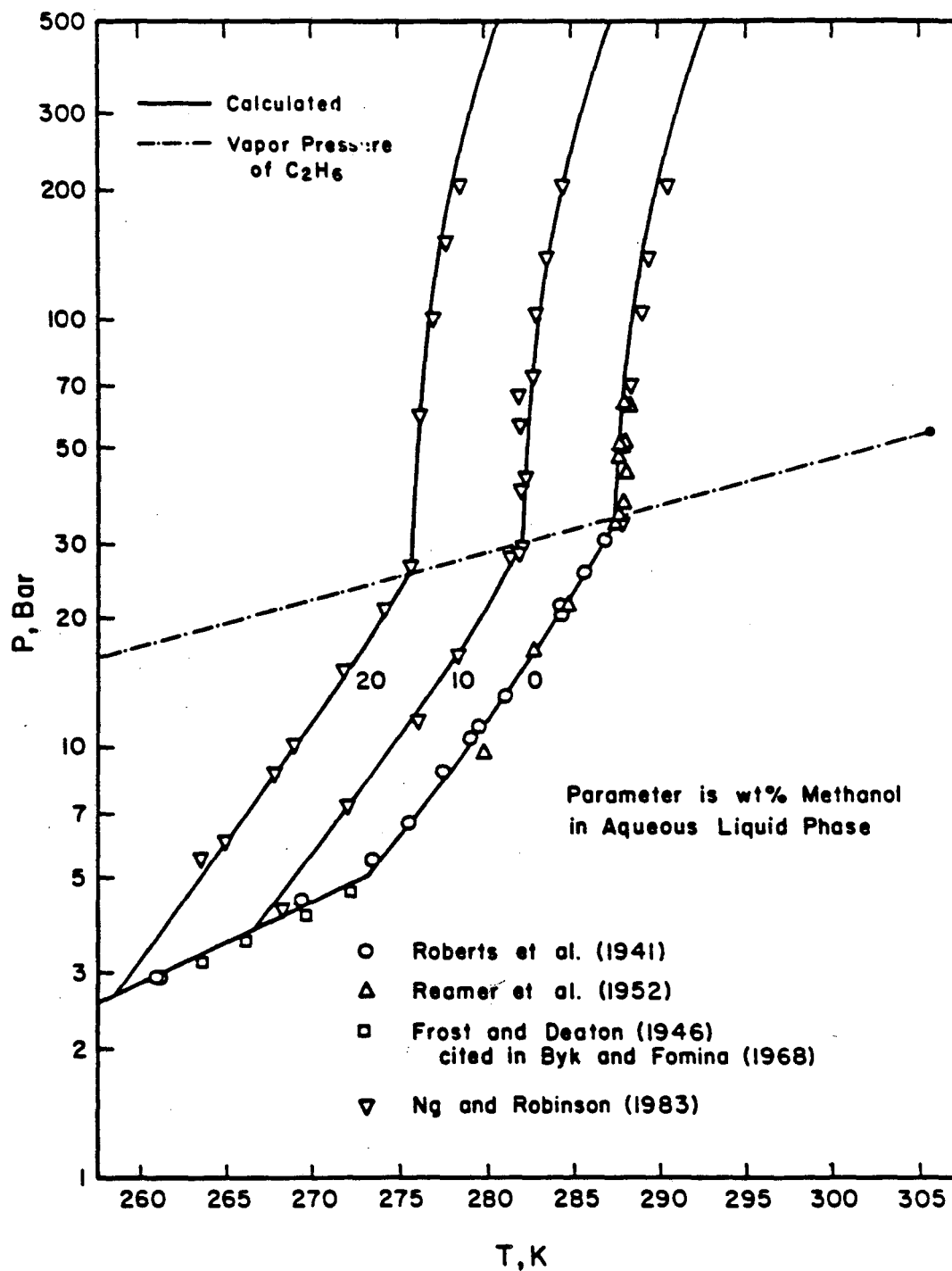
Water Content of Saturated Methane Gas

Figure 6



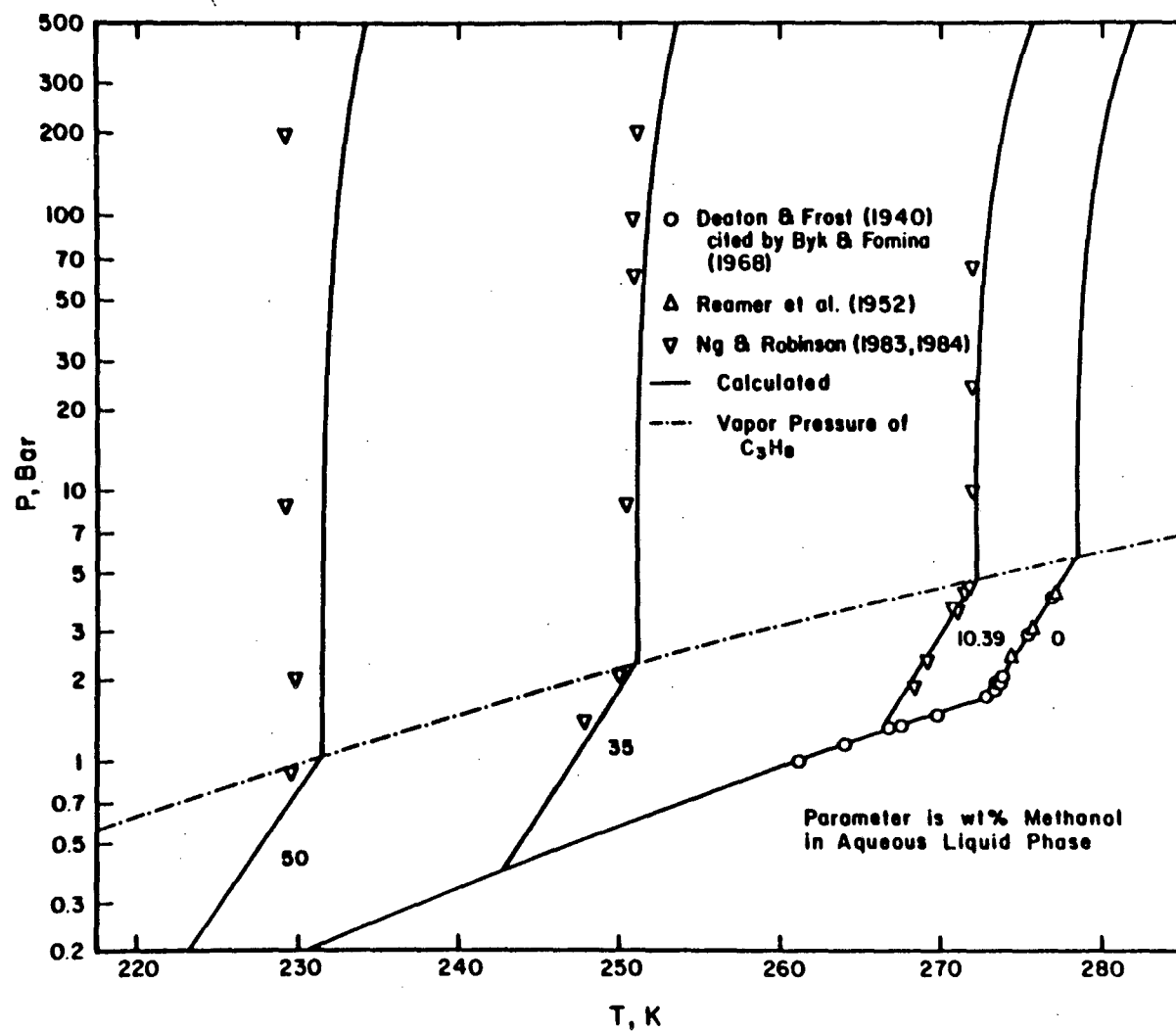
Calculated Fugacities in Methane Gas and Hydrate Phase
at 240 °K

Figure 7



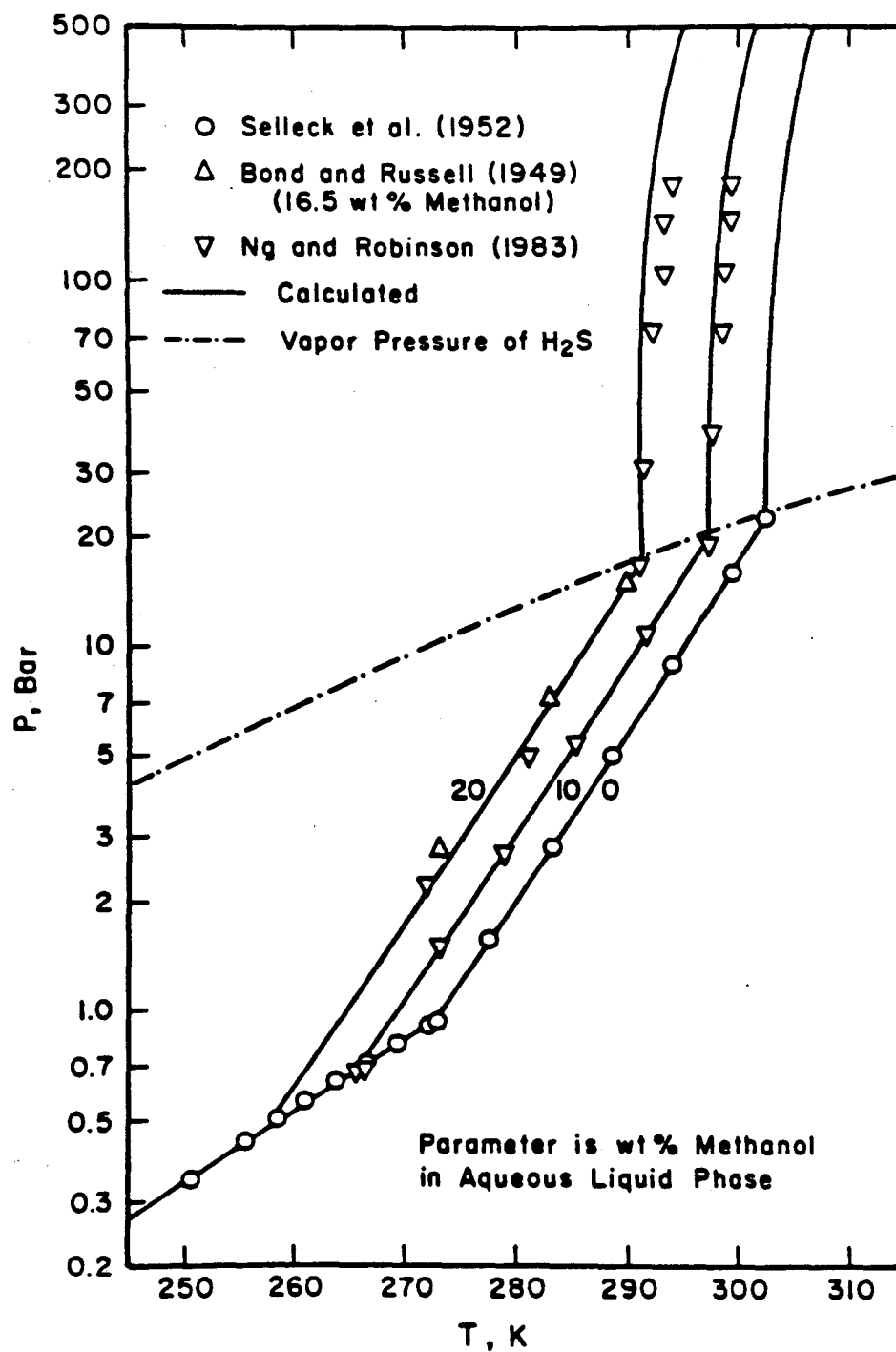
Inhibition of Ethane Hydrate by Methanol

Figure 8



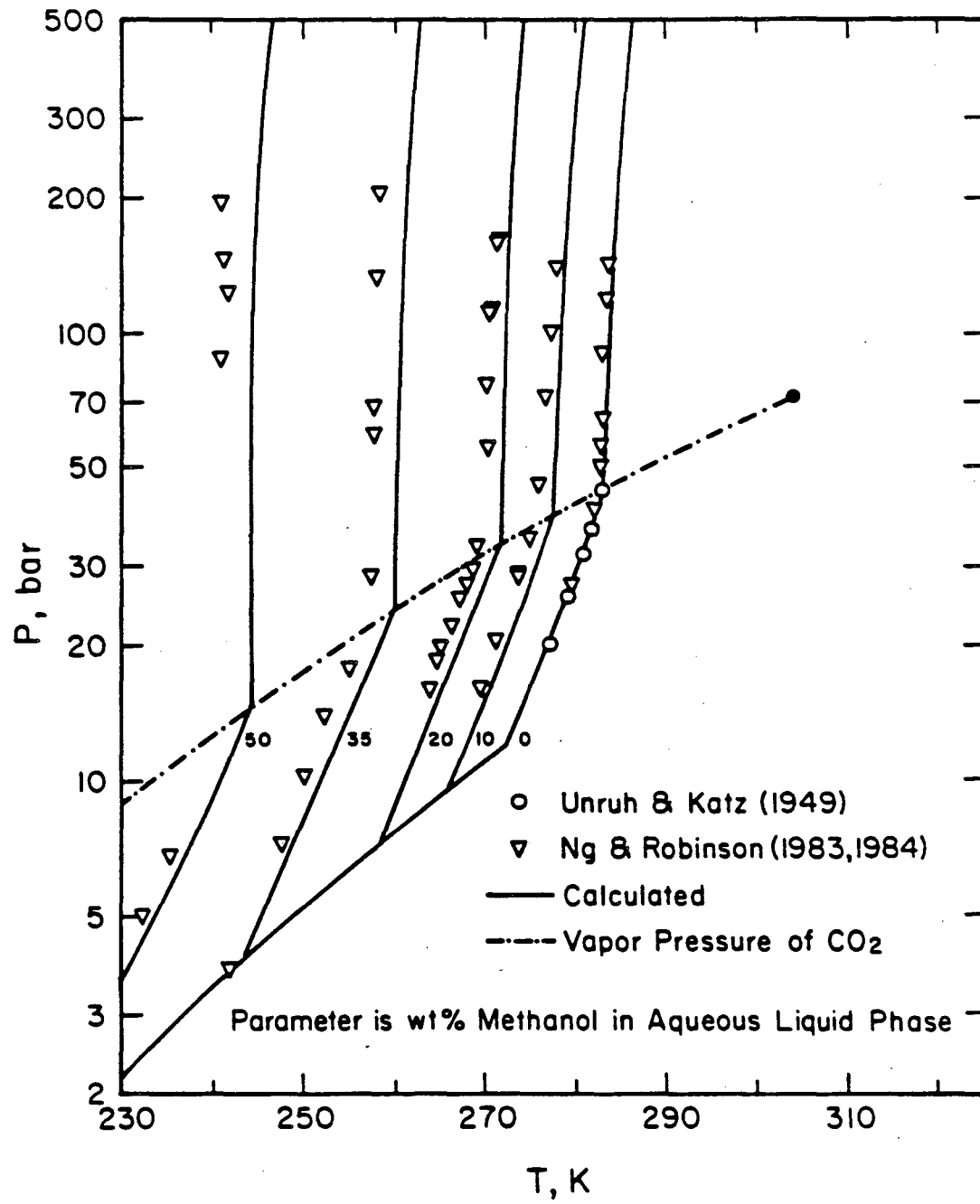
Inhibition of Propane Hydrate by Methanol

Figure 9



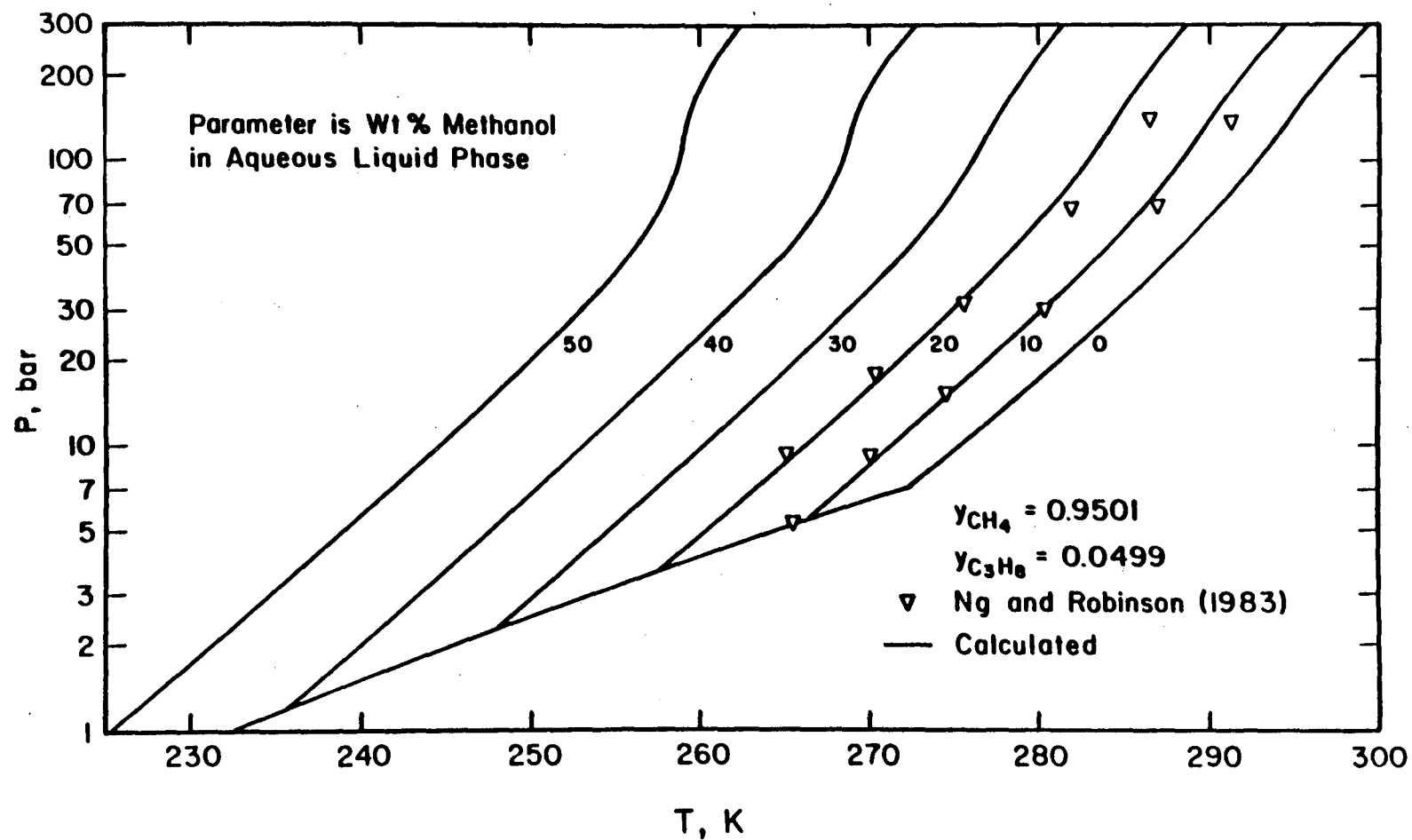
Inhibition of Hydrogen-Sulfide Hydrate by Methanol

Figure 10



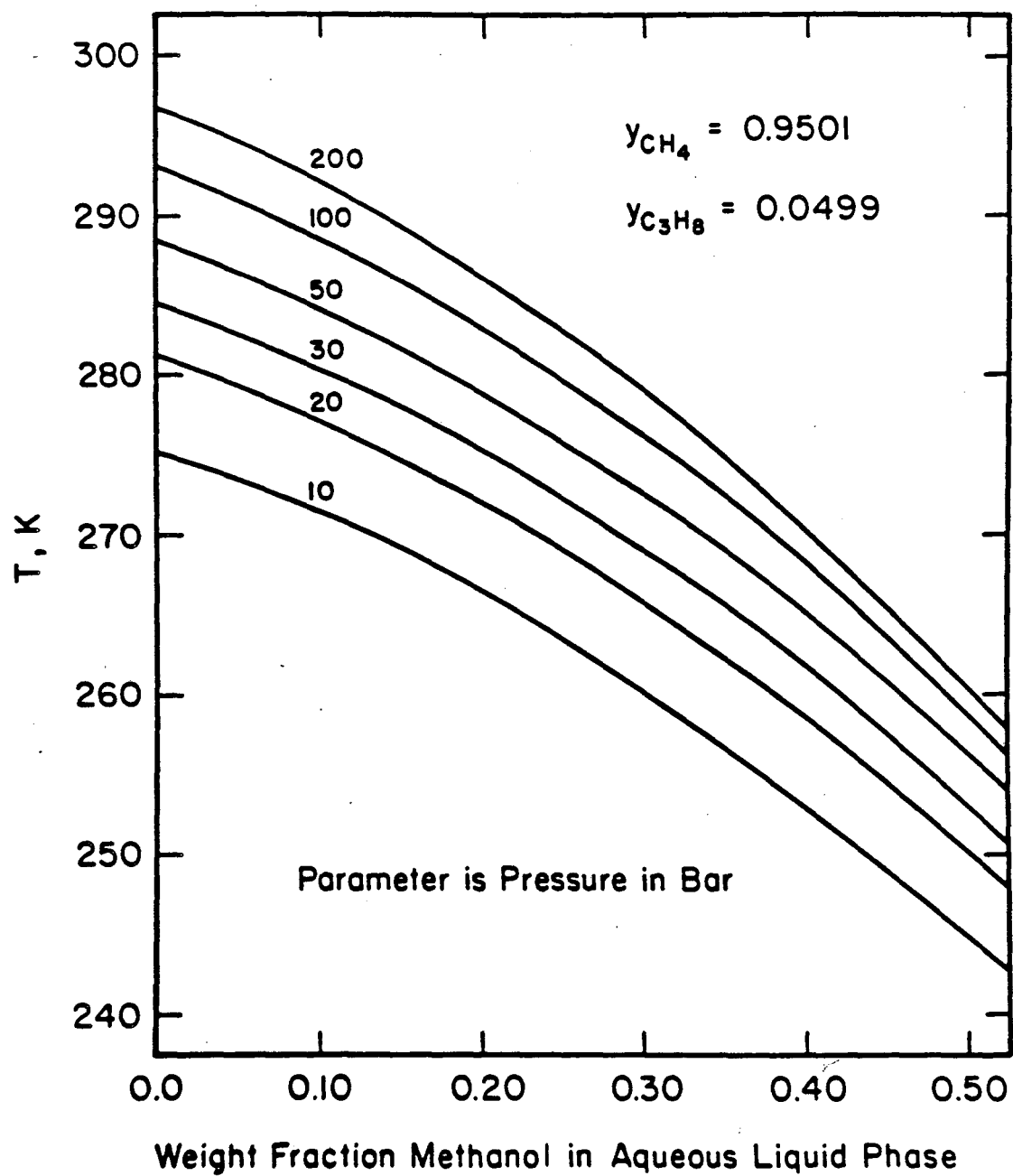
Inhibition of Carbon-Dioxide Hydrate by Methanol

Figure 11



Inhibition of a Gas-Mixture Hydrate by Methanol

Figure 12



Hydrate-Point Depression by Methanol
for a Gas Mixture

Figure 13

Table 1

Redlich-Kwong $a(T)$ Parameters for Polar Components

(Valid between 220 and 320 K)

	$a_i^{(0)} \left[\frac{10^{-7} \text{ cm}^6 \text{ Bar}}{\text{mole}^2} \right]$	$a_i^{(1)} \left[\frac{10^{-14} \text{ cm}^6 \text{ Bar K}^3}{\text{mole}^2} \right]$
Water	4.38	122.0
Methanol	43.1	226.9
Hydrogen Sulfide	7.75	6.395
Carbon Dioxide	6.03	1.680

Table 3

Parameters for Modified UNIQUAC Model

(Valid between 220 and 320 K for Equation 12; $U_{ij}^{(0)}$ in K, $10^2 U_{ij}^{(1)}$ in K²)

	R	Q		H ₂ O	CH ₃ OH	H ₂ S	CO ₂	C ₂ H ₆	C ₃ H ₈	n-C ₄ H ₁₀	i-C ₄ H ₁₀	n-C ₅ H ₁₂
H ₂ O	.9200	1.400	(0)	-	365.7	-378.1	-105.3	-770.7	-736.3	-284.5	-283.5	-168.0
			(1)	-	-38.06	363.2	197.4	521.6	471.6	304.7	299.4	257.2
CH ₃ OH	1.4311	1.432	(0)	-184.0	-	-13.48	54.77	-425.0	109.1	-276.7	158.7	96.77
			(1)	-26.85	-	-	-	200.5	-	125.1	-	-34.91
H ₂ S	1.0000	1.000	(0)	4813.	412.1	-	345.3	112.4	91.85	-65.50	81.34	-50.08
			(1)	-1300.	-	-	-	-	-	-	-	-
CO ₂	1.3200	1.280	(0)	1577.	540.5	-28.85	-	74.71	19.70	-23.30	-13.57	281.0
			(1)	-235.3	-	-	-	-	-	-	-	-
C ₂ H ₆	1.8022	1.696	(0)	3468.	576.9	230.4	114.5	-	156.0	-76.10	68.55	11.55
			(1)	-112.7	-6.31	-	-	-	-	-	-	-
C ₃ H ₈	2.4766	2.236	(0)	3338.	860.0	225.9	169.3	-104.5	-	-18.15	43.74	-235.9
			(1)	-662.9	-	-	-	-	-	-	-	-
n-C ₄ H ₁₀	3.1510	2.776	(0)	4155.	1109.	352.5	286.0	131.6	15.64	-	-42.15	-155.2
			(1)	-919.8	-125.8	-	-	-	-	-	-	-
i-C ₄ H ₁₀	3.1502	2.772	(0)	4754.	239.4	186.2	261.4	-30.02	-62.13	42.17	-	-206.3
			(1)	-1140.	-	-	-	-	-	-	-	-
n-C ₅ H ₁₂	3.8254	3.316	(0)	3402.	176.1	368.1	61.38	83.76	520.9	257.5	348.7	-
			(1)	-690.8	-429.4	-	-	-	-	-	-	-

Table 4

Thermophysical Properties of Water

(Equations 14 and 15; Valid between 220 and 273.15 K)

$$\frac{\Delta h_{\text{fus}}}{R} = 7.225 \times 10^2 \text{ K}$$

$$\frac{\Delta c_p^{(0)}}{R} = -2.054 \times 10^3$$

$$\frac{\Delta c_p^{(1)}}{R} = 1.638 \times 10^6 \text{ K}$$

$$\frac{\Delta c_p^{(2)}}{R} = -4.348 \times 10^8 \text{ K}^2$$

$$\frac{\Delta c_p^{(3)}}{R} = 3.852 \times 10^{10} \text{ K}^3$$

Table 5

Parameters for Henry's Constants

(Valid between 220 and 320 K for Equation 19; $H_{ij}^{(0)}$ is dimensionless with reference pressure of 1.01325 bar, $H_{ij}^{(1)}$ in K)

Solvent	Nitrogen		Methane	
	$H_{ij}^{(0)}$	$10^{-2}H_{ij}^{(1)}$	$H_{ij}^{(0)}$	$10^{-2}H_{ij}^{(1)}$
Water	14.11	8.032	13.99	10.12
Methanol	8.003	-1.163	14.50	19.36
Hydrogen Sulfide	4.215	-9.196	5.154	-2.096
Carbon Dioxide	3.752	-5.202	5.265	3.315
Ethane	3.259	-5.627	6.036	4.388
Propane	5.267	-1.849	5.780	2.819
n-Butane	4.069	-6.566	6.580	4.745
iso-Butane	3.951	-6.913	5.455	1.459
n-Pentane	5.892	-1.312	7.130	5.996

Table 6

Kihara Parameters for Hydrate-Gas Interactions

Gas	$\epsilon/k, K$	$10^2 \sigma, nm$	$10^2 a, nm$
Methane	153.39	32.578	3.00
Nitrogen	128.57	32.677	3.50
Ethane	175.94	34.381	4.00
Propane	189.84	36.002	6.80
iso-Butane	207.04	32.422	8.00
Hydrogen Sulfide	199.34	32.561	3.60
Carbon Dioxide	169.44	29.561	7.20

This report was done with support from the Department of Energy. Any conclusions or opinions expressed in this report represent solely those of the author(s) and not necessarily those of The Regents of the University of California, the Lawrence Berkeley Laboratory or the Department of Energy.

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