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Interfacial Magnetic Vortex Formation in Exchange-Coupled Hard-Soft Magnetic Bilayers

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Abstract

The exchange coupling between a hard magnetic layer MnBi and a soft magnetic layer Co-Fe has been found to significantly improve the maximum energy product. In this work, the spin structure of exchange-coupled MnBi:Co-Fe bilayers is experimentally investigated by X-ray magnetic circular dichroism (XMCD) and polarized neutron reflectometry (PNR). We find that the out-of-plane magnetization reversal process of the MnBi:Co-Fe bilayer structure involves formation of a curling-type twisting of the magnetization in the film plane at low or intermediate reversal fields. Micromagnetic simulations are further performed to provide a detailed view of the spins at the curling center. Reminiscent of chiral spin structures known as spin bobbers, this curling in the exchange-coupled hard-soft magnetic bilayers is a new type of skyrmionic spin structure and worth further investigation.

Manganese-bismuth (MnBi) is an intriguing alloy for several scientific and technological reasons. It is a magnetic model system characterized by complicated atomic [1,2,3], electronic [4,5], and magnetic [2,6,7] structures and with potential applications in permanent magnetism [8,9,10,11]. The technological fascination is fueled by the fact that both Mn and Bi are inexpensive elements, as compared to Pt and rare-earth metals. However, the magnetization of MnBi is relatively low, and attempts have been made to use hard-soft nanostructuring [12,13,14] to improve the energy product. Perpendicularly exchange-coupled MnBi:Co-Fe thin films, where MnBi is the hard phase and Co-Fe (cobalt-iron alloy) is the soft phase, are suitable for this purpose, and we have recently achieved an energy product enhancement from 98 kJ/m³ to 172 kJ/m³ in such a structure [11]. This is the highest nominal energy product achieved in a magnet without expensive or rare-earth elements.

The practical limitation of the hard-soft exchange-coupling approach is to maintain coercivity, that is, to avoid magnetization reversal in relatively small reverse fields [10,13]. This question has experimental and theoretical components: experimentally, the challenge is to avoid nucleation centers or to create pinning centers, which requires careful sample processing; theoretically, it is important to understand the magnetization reversal in the composite structure. The reversal starts in the soft phase and penetrates into the hard phase. Here, we show that our X-ray magnetic circular dichroism results, polarized neutron reflectometry results, and micromagnetic simulations all suggest that curling-type spin structures are formed during the magnetization reversal process.

At room temperature, the MnBi compound is in a low temperature phase (LTP) characterized by a hexagonal NiAs-like structure [1,15,16,17], and upon heating to 360 °C, bulk MnBi undergoes a structural transition into a high temperature phase (HTP) characterized by a Ni₂In-like structure

[18]. The structural transition is accompanied by a magnetic transition from a ferromagnetic phase at low temperatures to an antiferromagnetic phase at high temperatures [19]. Strikingly, the temperature dependent coercivity of the LTP MnBi exhibits an anomalous increase with increasing temperature [20]. The energy product of MnBi and its composites is therefore expected to increase with temperature over a wide range [21].

To prepare the MnBi films on which the MnBi:Co-Fe bilayer structures are based on, a Bi layer and a Mn layer were sequentially deposited on a Si (100) substrate at room temperature in a magnetron sputtering system with a base pressure below 2.7×10^{-6} Pa, and the bilayer structure was then post-annealed under high vacuum to form a Mn-Bi film. The Mn:Bi ratio of the film, tuned by controlling the thickness of each material layer during the deposition process, was quantitatively determined through wavelength dispersive X-ray spectroscopy measurements, and the microstructure of the films was studied by X-ray diffraction (XRD) using a diffractometer equipped with an area detector (Figure S1(a)). In addition, the hysteresis loop (Figure S1(b)) of each film was measured by a vibrating-sample magnetometer (VSM), and the film with a Mn:Bi ratio of 50:50 was found to show the highest perpendicular coercivity and the highest magnetization (Note: throughout this paper, the term MnBi refers to a Mn-Bi film with a Mn:Bi ratio of 50:50). Further, a thickness dependent study (Figure S1(c)) indicated that the equiatomic saturation magnetization of the MnBi films reaches a maximum value at a thickness of ~ 20 nm and an annealing-temperature study (Figure S1(d)) indicated that films annealed at temperatures equal to or slightly below 270 °C show the highest saturation magnetization. Please refer to Supplementary Material for detailed characterization results of Mn-Bi films.

Since nanoscale exchange coupling is an attractive path to achieve large energy products [12,13,22,23], Co-Fe layers were deposited at room temperature on MnBi films, which were

annealed at 270 °C and cooled to room temperature under vacuum. Then, a Pt or SiO₂ layer with a thickness of 5 nm was deposited on the Co-Fe layer to prevent oxidation. As described in Supplementary Material and in Ref. 11, we optimized the maximum energy product of the bilayer structure by changing the chemical composition of the Co-Fe alloy layer and/or changing the thicknesses of the soft layer and the hard layer respectively (Figure S2), and determined that the maximum energy product $(BH)_{max}$ of MnBi/Co-Fe bilayer structures can reach a value as high as 172 kJ/m³.

Our previous polarized neutron reflectometry (PNR) experiments [11] have shown that after the magnetization of the bilayer structure is saturated in an out-of-plane direction, a moderate reverse field causes the magnetization to continuously rotate from the out-of-plane direction (i.e., the initial saturation direction) in the MnBi layer to the in-plane direction in the Co-Fe layer [11]. It is well-known that magnetization reversal of thin films with perpendicular magnetic anisotropy starts by magnetization curling in the film plane [24,25,26]. Such curling is a magnetic vortex caused by magnetostatic self-interactions (flux closure) and represents an exact solution for some single-phase geometries. In recent years, magnetic vortex has become a topic of great interest in fundamental research due to its intrinsic stability [27] and unique topology-driven dynamics [28,29,30], and practical applications based on the structure, such as vortex-type magnetic random-access memories [31,32] and spin-torque vortex oscillators [33,34], have also been extensively investigated. In this study, our focus is on investigating the spin configurations in the MnBi/Co-Fe two-phase system by room-temperature X-ray magnetic circular dichroism (XMCD) and PNR [35,36,37], and by micromagnetic simulations using the *mumax* program package [38].

The XMCD and PNR measurements allow a layer-resolved analysis and the probing of magnetization components in different directions, and thus reflect the evolution of vortex states

through a magnetization reversal process. Figure 1(a) shows both in-plane and out-of-plane hysteresis loops of a MnBi(20 nm)/Co₇₀Fe₃₀(3 nm) bilayer structure obtained from VSM measurements. A schematic cross-sectional view of the sample, including the Si substrate and the capping layer, is shown in the inset of Figure 1(a) and the X-ray reflectivity (XRR) result (Figure S3) confirms the thickness of each layer. Figures 1(b) and 1(c) show the respective element-specific XMCD hysteresis loops of Mn and Fe in the bilayer structure. The magnetic field is applied parallel to the polarized X-ray beam and perpendicular to the sample surface. The loops yield out-of-plane coercivities of 1.15 T for MnBi and 0.1 T for Fe, consistent with the VSM measurements. The coercivity of Fe (and Co, not shown here) is due to the exchange coupling between the MnBi and Co₇₀Fe₃₀ layers. Without this coupling, the coercivity of the Co-Fe layer would be virtually zero.

In Figure 1(d), in-plane XMCD hysteresis loops of Fe in the MnBi(20 nm)/Co₇₀Fe₃₀(5 nm) sample were obtained by applying a magnetic field in the film plane and using an X-ray beam grazed 30° to the film surface. The magnetization components M_x , M_y , and M_z are parallel, transverse, and perpendicular to the magnetic-field direction, respectively. The "conventional" M_x hysteresis loop indicates that the Fe is predominantly magnetized in the film plane, and the perpendicular magnetization component M_z shows a typical hysteretic behavior in a field range between +100 mT and -100 mT. This confirms the exchange-coupling picture elaborated above. The small transverse in-plane component M_y peaks near the coercivity field ($H = \pm H_C$) which, similar to that in other thin-film systems [39,40,41,42], is consistent with dynamic formation of chiral spin structures or possibly vortices by the Fe and Co moments during magnetization reversal in the *x* direction. Specifically, the non-equilibrium magnetization reversal process induces a small unbalanced magnetization in the *y* direction due to coherent rotation of spins.

In the PNR measurements, we independently measured the non-spin-flip (NSF) reflectivities R^{++} , R^- and the spin-flip (SF) reflectivities R^{++} , R^{++} as a function of magnetic field parallel to the sample surface after the sample was perpendicularly saturated in an off-line magnetic field of 1.6 T. In an NSF reflection process, the polarized neutrons do not change direction after interacting with the film. The NSF reflectivities are sensitive to the chemical compositional depth profile averaged across the sample plane, and the difference between R^{++} and R^- originates from the depth-dependent component of the in-plane magnetization parallel to the field. In the SF reflectivities are sensitive to the component of the in-plane magnetization perpendicular to the field. Together, the NSF and SF cross sections reveal the in-plane vector magnetization depth profile. In the in-plane field geometry, we measured the reflectivity of the MnBi(25 nm)/Co₇₀Fe₃₀(5 nm) bilayer structure at different magnetic fields incrementally from 0.004 T to 0.77 T. Figure 2(a) shows typical PNR results and corresponding fits (solid lines) for MnBi/Co₇₀Fe₃₀ with an in-plane field of 0.5 T.

Figures 2(b)-2(d) show the structural and magnetic depth profiles of the bilayer structure generated from the fits to the measured reflectivity data shown in Figure 2(a). The structural profile in Figure 2(b) matches that obtained from complementary PNR measurements in an out-of-plane field [11]. The fits indicate that the MnBi and Co₇₀Fe₃₀ thickness are 25 nm and 5 nm, respectively, though the boundary between them is smeared due to the interfacial roughness. In addition, the topmost section of the MnBi layer has reduced scattering length density (SLD) possibly indicative of voids or Mn-rich regions. Note that the structural depth profile is consistent with that obtained from X-ray reflectivity (XRR) measurements (Figure S4).

Figure 2(c) shows the corresponding depth-dependent profile of the in-plane magnetic SLD, which is directly proportional to the in-plane magnetization magnitude, at 0.5 T. The angle of the magnetization relative to the applied field (at 0°) as a function of depth is plotted in Figure 2(d). In a lower field of 0.004 T, the depth profile of the magnetization resembles that shown in Figure 2(c) for 0.5 T, but with a small in-plane magnetization mostly confined to the nominal Co-Fe layer. Upon increasing the in-plane field to 0.25 T and 0.5 T, Figure 2(c), a small component of the magnetization parallel to the in-plane field develops throughout the entire MnBi layer. This component emerges as a result of the application of the external field perpendicular to the out-of-plane *c*-axis of the MnBi (see, e.g., Refs. 8 and 43), the effect of which is somewhat enhanced by the exchange coupling to the Co-Fe layer.

The splitting in the NSF data along with the coexisting peak in the SF scattering near the critical angle is best fit [Figure 2(a)] with a model that displays a twist of the in-plane magnetization throughout the Co-Fe layer. Specifically, the in-plane magnetization component at the bottom MnBi/Co-Fe interface is nearly parallel to the field but the magnetization component at the top Co-Fe/Pt interface is nearly perpendicular to the in-plane field, as shown in Figure 2(d) (Note that the magnitude of the in-plane transverse magnetization obtained from the fit may be smaller than its actual value since the spin flip scattering at low values of the wavevector Q_z is shifted from the specular position due to the Zeeman effect [44]). The model used to fit the data in Figure 2(a) relies on the assumption that the sample vector magnetization is essentially homogenous across the sample plane. In this case, interpretation of the magnetic depth profile shown in Figures 2(c) and 2(d) is straightforward - the *net* magnetization averaged over the entire plane of the sample has an in-plane component that is twisted from the top of the MnBi

layer through the CoFe layer. Such a twist could be the result of inherent differences in anisotropy between the two layers.

However, there is a plausible alternative interpretation of the data that does not require a net inplane component of the magnetization perpendicular to the field across the entire sample. Specifically, incident neutron wavepackets scattered from individual magnetic regions with dimensions that exceed the neutron coherence length which is $\approx 100 \ \mu m$ parallel to the beam (x direction) and is $\approx 1 \ \mu m$ transverse to the beam (y direction) [45,46]. This results in an incoherent addition of scattering from different regions in the detector. Put differently, one would measure the average of different scattering patterns from distinct regions, rather than a single scattering pattern corresponding to the average in-plane structure. In this size regime, domains with oppositely-oriented perpendicular components would produce identical scattering patterns (Figure 3). Thus, an incoherent addition of scattering from those two types of domains would be virtually indistinguishable from that originating from an effectively single domain sample with a net in-plane magnetization component perpendicular to the field. In this alternate case, the twisting of the in-plane magnetization as a function of depth is consistent with the presence of magnetization curling. Since neutron reflectivity averages across the sample plane, these measurements would not be sensitive to the curling structure if the radius of the curling structure R is less than the coherence length of the neutron. Figures 3(a) and 3(b), respectively, show a possible ordered spin structure that might form in small and moderate in-plane fields. The film plane (x-y plane) is the neutron scattering plane and the neutron wave vector Q_z is parallel to the surface normal. The slits are narrow in the x-direction (along the beam direction) but wide in the y-direction (perpendicular to the beam path and parallel to the applied field), and the horizontal resolution (in the x-direction) is such that the neutron coherence length extends up to approximately 100 μ m [45]. Specular Q_z scans thus average coherently across the *x*-direction in the sample plane over distances that include multiple in-plane curling domains. The vertical resolution (*y*-direction) is coarse, and the neutron coherence length is only of the order of 0.1-0.5 μ m. As a result, the Q_z specular scan might actually be a composite of incoherent sums from regions along the *y*-axis of the sample that scatter independently, like individual samples.

In analogy to the reflectivity model for skyrmions in patterned multilayers [40], the sample in this model can be crudely divided into three regions (I - Curling domain top and surrounding sample, II - Curling domain bottom and surrounding sample, III - Region between domains, if any) as shown in Figure 3(a). The scattering from each region should add incoherently. For specular reflectivity scans, the difference in coherence lengths along the *x* and *y* directions means that the up/down spins on the sides of the curling domains in regions I and II will average to a net magnetization of zero if the applied field is small, as depicted in Figure 3(a). However, the top and bottom magnetizations in the curling domains will give rise to SF scattering if the curling domain size is larger than the vertical (y) coherence length (< 1 μ m). If the curling domains are random in-plane, rather than ordered, then the top and bottom magnetizations will generate SF scattering only if the domain size is greater than the horizontal (*x*) coherence length (approximately 100 μ m).

The "up - down" symmetry, however, is broken within the sample plane in large in-plane fields which act to align the MnBi and CoFe magnetizations and to distort the curled structure. When a magnetic field H is applied along the y-direction (represented by grey arrow), the "up" domains in the red area in Figure 3(b) will be expanded and the "down" domains will be shrunk in the green area. The distortion of the curling domain shown in Figure 3(b) will result in a net component of the magnetization (e.g., averaged over the coherence length along the *x* direction)

in the Co-Fe layer that is parallel to the in-plane field, and this component from regions I and II will contribute equally to the splitting of the NSF scattering that is evident in the 0.5 T reflectivity data in Figure 2(a). Since the MnBi/Co-Fe bilayer structure experimentally shows a very high out-of-plane coercivity, we can reasonably assume that the size of the curling domains within the layer is larger than the coherence length in the *y*-direction, in which case the top and bottom of each domain in regions I and II for this ordered structure should generate SF scattering of equal magnitude. Similar arguments again apply to a structure with curls that are disordered in-plane, though the curling domain size needs to exceed the large coherence length in the *x*-direction to produce SF scattering.

In practice, we fit the average "composite" structure and did not explicitly extract the characteristics of the magnetic structure in each of the three regions shown in Figure 3 to avoid over-parameterization since the sample exhibits an interfacial roughness of ~ 1.5 nm. The depth profile of the vector magnetization [Figures 2(c) and 2(d)] suggests that the magnetization throughout the depth of the bilayer varies from an angle of almost (but not quite) 90° at the top of the Co-Fe layer to an angle of 0° relative to the field direction in the MnBi layer. By scattering symmetry, the data could be fit with magnetization that twists from an angle of almost (but not quite) 270° (-90°) at the top of the Co-Fe layer to an angle of 360° (0°) relative to the field in the MnBi layer. So, the fit is consistent with the expected scattering from *both* regions I and II, Figure 3(b), of the curling domain in which the Co-Fe magnetization winds through its depth toward the applied field direction, which corresponds to the direction of the in-plane component of the MnBi net magnetization. Since the expected reflectivity contributions from regions I and II are identical, however, we cannot definitively determine if the measured scattering originates from curling domains or just from randomly oriented in-plane domains with dimensions larger

than the x and y neutron coherence lengths solely based on the PNR results. We note that our previous complementary measurements of the PNR investigations in an out-of-plane field (reported in Ref. 11) support either interpretation, though we would not expect to see any direct evidence of the curling twist in PNR measurements with the perpendicular measurement geometry.

As shown in Figure 3(a), the formation of in-plane curling domains in the Co-Fe layer *inevitably* leads to vertically-orientated spins at the center of each curling domain structure, suggesting that a chiral spin structure should be formed at the 'wind eye' of the curling domains. Within each chiral spin structure, the out-of-plane component of the spins in the Co-Fe layer gradually increases from the boundary to the center. Therefore, the magnetization of the Co-Fe layer has a finite out-of-plane component. As indicated in Figures 1(b) and 1(c), when an external magnetic field returns to zero after saturating the magnetization of the bilayer structure in an out-of-plane direction, the magnetization of the MnBi layer remains substantially along the out-of-plane direction, while the magnetization of the Co-Fe layer is reduced to a finite value in the out-ofplane direction, consistent with the formation of chiral spin structures. When a reversal field is applied, the out-of-plane component of the spins in the chiral spin structures starts to change the sign [11], and eventually leads to magnetization reversal of the MnBi layer and annihilation of the chiral spin structures at the out-of-plane coercivity field. This chiral spin structure formed in the exchange-coupled hard-soft magnetic bilayer is reminiscent of magnetic bobbers [47,48,49,50,51,52,53], which were discovered in the context of flux-closure domains [6,54] and have since attracted much attention, as exemplified by Refs. [8,55,43]. Magnetic bobbers are chiral in the sense of the spin texture topology [56], that is, the spins in a magnetic bobber can form left- or right-handed rotation structures. The current interest in magnetic bobbers is linked to Dzyaloshinskii-Moriya interactions in B20 [48] and related materials, which make these structures easier to stabilize on small length scales.

To further illustrate the formation of the chiral spin structures in the soft-hard magnetic bilayers, we perform micromagnetic simulations. The curling mode $M = M_{\rm C}(z, \rho) (\cos\phi \mathbf{e}_y - \sin\phi \mathbf{e}_x)$ originates from the competition between exchange energy and magnetostatic self-interaction [57,58,59,60,61]. The former favors coherent rotation, and the latter favors the partial flux closure inherent in the curling mode but costs exchange energy. Since exact solutions are available for simple systems only, it is convenient to use micromagnetic simulations. Figure 4 shows the curling-type spin structure for a MnBi(20 nm)/Co₇₀Fe₃₀(3 nm) thin-film patch in remanence after application of an out-of-plane saturation field. The simulations were performed using mumax [38]. The anisotropies of $K_1 = 0.9 \text{ MJ/m}^3$ and $K_1 = 0$ for Co₇₀Fe₃₀ have been taken, and the computational cell size, equal to the distance between the arrows, is 1 nm in the zdirection and 2 nm in the x- and y-directions. Figure 4 shows a simulation region of 40 nm \times 40 nm (in the film plane), which represents the "central point" of each curling domain structure illustrated in Figure 3. Note that the curling mode is symmetric with respect to x and y in Figure 4, but not in Figure 1(d) because of the symmetry-breaking field applied in the x-direction. The chiral spin structure is primarily confined to the soft Co-Fe layer but somewhat penetrates into the hard MnBi layer. The curling intensity decays exponentially in the hard phase. The decay length of soft-into-hard penetration is generally of the order of $\delta_0 = \sqrt{A/K_1}$ [61], that is, about 3 nm for MnBi. This resistance to soft-hard penetration is the main reason for the high coercivities and energy products of the present MnBi/Co-Fe thin films. When the MnBi layer becomes too small, then two things happen. First, the film quality deteriorates due to the loss of Bi. Second, an unrelated magnetic effect is that the bottom part of the chiral spin structure starts to pierce the bottom of the MnBi layer, thereby facilitating magnetization reversal and causing coercivity and energy product to decrease.

Our calculations also show that the spin structure in Figure 4 carries a topological charge Q. This charge reflects the skyrmion-like noncollinearity of the spin structure and is obtained by integration over the skyrmion density $\Phi = M \cdot (\partial M / \partial x \times \partial M / \partial y) / 4\pi M_s^3$ [62]. The charge is fielddependent and reaches a sharp maximum in the chiral spin structure state near the coercivity, where the noncollinearities are most pronounced. In very high fields, Q = 0, because all spins are parallel and $\Phi = 0$. These spin structures are present at room temperature, due to the high T_C values of MnBi and Co₇₀Fe₃₀. In addition, feature sizes in the spin structure are quite small, of the order of 10 nm. This is in the range of being potentially interesting in spin electronics [63,64,65,66]. One suggestion for future research is to investigate the topological charge experimentally. This can be done by Hall-effect measurements, because Q corresponds to a Berry phase acquired by conduction electrons [67] and therefore to a topological Hall effect (THE) contribution [68] to the Hall resistivity. Another suggestion is to look at thin-film nanostructures made from other inversion-symmetric materials. Note that both MnBi and Co₇₀Fe₃₀ are macroscopically centrosymmetric, so no Dzyaloshinskii-Moriya interactions are necessary or involved in the formation of the chiral spin structures. In terms of Figure 4, rightand left-handed chiral spin structures are both possible and yield the same Q and THE, irrespective of the chirality of the spin structure.

In conclusion, we have investigated the in-plane magnetization components in bilayers of *c*-axisaligned hard MnBi and soft Co-Fe. These components play an important role in the understanding of the high coercivities and nominal energy products of MnBi:Co-Fe bilayers. Our VSM, XMCD and PNR experiments, combined with micromagnetic simulations, indicate that the magnetization has the character of topologically charged chiral spin structures. Compared to conventional spin bobbers, this new type of spin structure has a curling or vortex structure that touches the ground (the hard phase in the magnetic analogy) and partially penetrates it. Exchange-coupled nanostructures are therefore not only an option towards high-performing rare-earth-free permanent magnets but can also be used to create small-scale topological vortex structures at room temperature.

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Figure Captions

Figure 1. Hysteresis loops of a MnBi(20 nm)/Co₇₀Fe₃₀(3 nm) bilayer sample. (a) the in-plane and out-of-plane hysteresis loops obtained by VSM; and element-sensitive room-temperature XMCD hysteresis loops: (b) out-of-plane loop for Mn, (c) out-of-plane loop for Fe, and (d) in-plane loops for Fe with M_x (black), M_y (red) and M_z (blue) components. Note that the scale of M_y and M_z is magnified by a factor of 10.

Figure 2. Polarized neutron reflectivity measurements. (a) experimental results and corresponding fits (solid lines) for all four cross sections, R++ (blue), R+- (purple), R-+ (green) and R-- (red) obtained in a field of 0.5 T applied parallel to the sample plane of a MnBi(25 nm)/Co₇₀Fe₃₀(5 nm) bilayer after saturation in a perpendicular field of 1.6 T (Note: error bars displayed here indicate 1 standard deviation); and (b)-(d) depth profiles of a MnBi(25 nm)/Co₇₀Fe₃₀(5 nm) bilayer: (b) structural scattering length density (SLD), (c) magnetic scattering length density which is proportional to the in-plane component of the magnetization, and (d) angle of the in-plane magnetization component relative to the 0.5 T in-plane field at 0° obtained from fits to polarized neutron reflectometry measurements. The rotation of the in-plane magnetization as a function of depth from 0° near the MnBi/Co-Fe interface to 90° near the Co-Fe/Pt interface is consistent with presence of the curling mode.

Figure 3. Cartoon of magnetization reversal with curling model in the topmost of $Co_{70}Fe_{30}$ layer (X-Y plane) at initial state in a low field (a) and after applying a large field (b). The white arrows represent magnetization, and the grey arrows represent the strength and the direction of the magnetic field. Each of the three regions in (a) and (b) scatter coherently, and the resultant reflectivity is an incoherent sum of the scattering from each region.

Figure 4. Magnetization curling in MnBi(20 nm)/Co₇₀Fe₃₀(3 nm) determined from micromagnetic calculations. A 40 nm \times 40 nm area is shown in the figure as an enlarged view of a "wind eye" where red, blue, green, and yellow regions meet in Figure 3. The arrows represent orientations of local spins, and the colors (i.e., red, blue, green, and yellow) represent the local in-plane magnetization direction (consistent with Figure 3). Arrows in the top-most region are mainly in plane as they are in the Co₇₀Fe₃₀ layer, and then gradually change to out of plane in the depth direction as they transition to the MnBi layer.



Figure 1



Figure 2



Figure 3



Figure 4