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Permalink
https://escholarship.org/uc/item/0tj5w7ht

Journal
GEOTHERMICS, 74

ISSN
0375-6505

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Publication Date
2018-07-01

DOI
10.1015/j.geothermics.2018.02.011

Peer reviewed
Simulations of carbon dioxide push-pull into a conjugate fault system modeled after Dixie Valley—Sensitivity analysis of significant parameters and uncertainty prediction by data-worth analysis

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Highlights

• We investigate CO₂ push-pull into faults zones at Enhanced Geothermal Systems for improved characterization of major flow features.

• We developed a conceptual and numerical reservoir model of two intersecting faults based on the Dixie Valley geothermal system in Nevada, USA.

• We perform forward modeling along with sensitivity and data-worth analyses of scCO₂ push-pull to investigate the CO₂ distribution in the faults.

• Formal sensitivity analysis determines the most controlling unknown parameters in the fault zones.

• Data-worth analysis reveals the most valuable output response to be measured for the best prediction of CO₂ distribution in the faults.

Abstract

Characterizing the faults and fractures that provide flow pathways for efficient geothermal energy production is critical for design of sustainable geothermal energy production. Both natural faults and stimulated fractures in enhanced geothermal systems (EGS) are difficult to image and map by seismic methods because hot brine filling the fractures and faults does not create a strong seismic property contrast relative to surrounding rock. We investigate here the technical feasibility of using supercritical CO₂ (scCO₂) injection into faults in a single-well push-pull scenario to characterize the
hydraulic properties of the fault zone by emplacing scCO$_2$ that can serve as a contrast fluid for seismic monitoring. We develop a conceptual and numerical reservoir model of two intersecting faults based on the Dixie Valley geothermal system in Nevada, USA. The 2D conceptual model consists of a system with a main fault and an intersecting conjugate fault. The corresponding numerical model is discretized using irregular grid blocks with fine discretization around the slip plane, gouge, and damage zones. We perform forward modeling along with sensitivity and data-worth analyses of scCO$_2$ push-pull to investigate the CO$_2$ distribution in the fault gouge during 30 days of push (injection) and 30 days of pull (production). Formal sensitivity analysis is conducted to determine the most controlling unknown parameters in the fault zones. Using the selected set of unknown parameters and output responses, we perform data-worth analysis to reveal the most valuable output response to be measured for the best prediction of CO$_2$ distribution in the fault zones and its uncertainty. From the results of data-worth analysis, we determine the optimal properties to target in monitoring, their locations, and the minimum observation time. Our results provide information on the optimal design of scCO$_2$ push-pull testing in a conjugate fault system modeled after Dixie Valley that can be used to enhance monitoring by active seismic and well-logging methods to better characterize the transmissive fault(s).

Keywords
Enhanced geothermal sites (EGS)
CO$_2$ push-pull
Dixie Valley geothermal system
Sensitivity analysis
Data-worth analysis

1. Introduction

Networks of naturally occurring and engineered fractures and faults must be explored and characterized in order to optimize exploitation of geothermal energy from enhanced geothermal sites (EGS). However, faults and fractures occurring in many EGS sites are difficult to image with traditional seismic and well-logging tools because they are filled with hot brine and not easily distinguishable from the surrounding formation. Previous research showed that the injection (push) of supercritical CO$_2$ (scCO$_2$) into (i) a fracture zone at a geologic carbon sequestration site with active source seismic...
monitoring (e.g., Zhang et al., 2015) and (ii) into a fault zone at a prototypical EGS site
with active-source seismic monitoring and well-logging allowed seismic detection of the
transmissive zones (Borgia et al., 2017; Oldenburg et al., 2016). After imaging the
fracture and fault zone following injection, fluid production (pull) from the fault zone
allows partial recovery of the injected scCO₂.
There are several advantages to using scCO₂: (1) much higher compressibility of
scCO₂ relative to water facilitates seismic detection by changing the stiffness tensor
components; (2) the non-wetting characteristic of scCO₂ tends to exclude the scCO₂ from
the matrix leaving it preferentially within the fractures and faults; (3) the smaller viscosity
of scCO₂ relative to brine helps it to easily permeate into the fractures and faults; and (4)
the higher density of scCO₂ relative to other gases mitigates the buoyancy effect and
enables the better recovery of injected CO₂ during the pull phase (Borgia et al., 2017).
In this study, we investigate the technical feasibility of a scCO₂ push-pull test in the
conjugate faults system of the geothermal resource at Dixie Valley in central Nevada,
USA. The geothermal system in the Dixie Valley is of basin-and-range type, and the
temperature of the field is estimated to approach a 260 °C at a depth of 3 km, based on
measured well data (Blackwell et al., 2007; Iovenitti et al., 2016). The geothermal
system in the Dixie Valley is believed to be a promising EGS site owing to high
temperature range at relatively shallow depth, existence of faults and brittle fractured
zones for permeability, and favorable stress regime at the depth of 1–3 km for EGS
development (Iovenitti et al., 2016).
In the forward modeling of scCO₂ push-pull in this study, we simulate the injection and
production of scCO₂ into the junction of two conjugate faults in the Dixie Valley
Geothermal System (DVGS). We investigate the efficacy of injecting and producing
CO₂ so that it spreads in the fault zones where it can be useful for improving imaging
and characterization by seismic methods.
We conduct a sensitivity analysis to evaluate the factors affecting CO₂ inflow into the
faults and outflow from the faults. The sensitivity coefficient of each influential parameter
on the system response is quantified. We conduct a data-worth analysis to predict the
uncertainty of CO₂ distribution after the push and pull phases by measuring the system
responses. In this procedure, the data worth of each measurement is computed to
indicate the relative importance for the prediction of future system behavior.
From this study, we determine (1) technical feasibility of CO₂ push-pull in the DVGS fault
zones, (2) important flowing parameters in fault zones that affect the efficiency of
CO₂ push-pull in the Dixie Valley geothermal system, (3) system responses that should
be measured to predict CO$_2$ distribution after push-pull, and (4) prediction uncertainty of CO$_2$ distribution in the conjugate faults.

2. Dixie Valley geothermal system

The DVGS is one of the most thoroughly characterized geothermal systems in the U.S. The data include geological cross-sections, gravity-magnetic surveys, lithologic and resistivity models, seismic models of P-wave velocity and S-wave velocity, and thermal numerical models (Blackwell et al., 2009; Iovenitti et al., 2016; Iovenitti et al., 2013; Smith et al., 2011).

The DVGS occupies an area of approximately 170 km$^2$ within the larger project area of 2500 km$^2$ (Iovenitti et al., 2016). In the geothermal system, there are a number of N-to NE-trending fault systems identified from thermal anomalies (Fig. 1(a)), which are formed by well-connected normal and associated conjugate faults of 1–3 km-depth.
Fig. 1. The Dixie Valley Geothermal System as depicted by (Iovenitti et al., 2016): (a) structural intersections of faults (dark blue lines) identified by thermal anomalies (dashed red lines) in the geothermal field, (b) geologic cross section following DD', (c) isotherms along the profile DD'. The blue outline box superimposed on the cross-sections of Iovenitti et al. (2016) shows our model domain boundary. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

The geologic cross section DD' is shown in Fig. 1(b). Here, brittle and permeable zones within the Tbf (basin-filling sediments), Tmb (Miocene basalt), Jz (Jurassic mafic volcanics), and Tr (Triassic meta-sediments) provide the flow pathways of fluid and heat. Hot brine rises along the main faults giving rise to the isotherms shown in Fig. 1(C) (Smith et al., 2011). Regarding the system temperature, depth, and the distributions of high-permeability zones, we define our model domain area of 2750 m × 2750 m as shown in Fig. 2.

Fig. 2. Lithology structure and size of the 2D model domain based on the DVGS.

3. Development of the conceptual and numerical models
We developed a 2D cross-sectional conceptual model of the DVGS involving the main and conjugate faults. The conceptual model includes the geometry of reservoir rocks and faults, as well as simplified representation of system heterogeneity, initial conditions, and transport properties. Although the conceptual model is very simplified, it includes the essential components that affect flow of injected CO₂ and therefore retains the fundamental fault-flow-related aspects of the system. We chose to use a 2D model over a 3D model for computational efficiency. This choice is justified by the observation that a CO₂ plume in a steeply dipping fault zone expands more easily upward than horizontally due to buoyancy as observed in a 3D simulation study (Borgia et al., 2017). Fig. 3(a) shows the grid we developed for the 2D domain using WinGridder (Pan, 2008) corresponding to the cross section DD’ (Fig. 1(a)). The model contains a total of 10,728 grid blocks. This irregular grids system has elements connected along the fault zones parallel to flow directions, rather than staggered connections that result from regular rectangular grids system. The expanded view at the junction of the faults is shown in Fig. 3(b). The width and height of the elements in the fault zones are 2.5 m and 10 m, respectively.
To characterize the fault zones, we use the conceptual model of a generic fault developed by Gudmundsson et al. (2002), which contains a few meter-thick fault gouge, a slip plane within the fault gouge, and a damage zone outside the fault gouge (Fig. 4(a)). Our model includes 32.5 m-thick and 22.5 m-thick fault zones in the main and conjugate faults, respectively (Fig. 4(b)). The main fault zone has a thicker fault gouge than the conjugate fault zone has. Fault zones are conceptualized as being composed of brittle rocks and contain cracks, which provide flow pathways for fluid and heat.
Fig. 4. A generic model of a fault zone: (a) concept of a fault zone involving fractured fault gouge and damage zone (Gudmundsson et al., 2002); (b) dimensions of fault zones in our model. Note that ‘G’ and ‘S’ in the grid block containing slip plane indicate the fault gouge and slip plane, respectively.

Fig. 5 shows the initial pressure and temperature distributions. The system is initially filled with brine; and a hydrostatic pressure gradient of 9.79 kPa/m is applied. The initial temperature distribution shows the effect of rising flow of fluid and heat through the main fault, which was obtained by running a natural-state simulation, which started with the temperature distribution of Fig. 1(c), for sufficiently long time of $10^6$ days to get steady-state condition. Constant pressure and temperature are set at the top boundary; and the other three sides are set at no flow condition of heat and fluid, in light of the short time of our push-pull test.
Fig. 5. Reservoir initial conditions: (a) pressure distribution, (b) temperature distribution. Hydrogeologic properties of the system for the numerical simulations are provided in Table 1. Potentially influential and unknown parameters for the flow of injected CO$_2$ in the fault zones are indicated with *—the absolute permeability, and the input parameters for the relative permeability and capillary pressure functions in the fault slip plane, fault gouge, and damage zone. Sensitivity and data-worth analyses will be performed for these parameters after the forward modeling section.

Table 1. Properties of the DVGS (Borgia et al., 2017; Oldenburg et al., 2016). Rock grain density = 2650 kg m$^{-3}$, pore compressibility = $7.25 \times 10^{-12}$ Pa$^{-1}$, rock grain specific heat = 1000 J kg$^{-1}$K$^{-1}$, and formation thermal conductivity = 2.1 W m$^{-1}$K$^{-1}$, respectively. Note that $1/P_0$ is proportional to the square root of the absolute permeability.

<table>
<thead>
<tr>
<th>Zone</th>
<th>Porosity [vol. frac.]</th>
<th>Permeability [m$^2$]</th>
<th>Parameters of capillary pressure</th>
<th>Parameters of relative permeability</th>
</tr>
</thead>
<tbody>
<tr>
<td>Slip plane</td>
<td>0.30</td>
<td>$2 \times 10^{-1}$</td>
<td>None</td>
<td>Corey$^<em>$, $S_0^</em> = 0$. 3; $S_r^* = 0.05$</td>
</tr>
</tbody>
</table>
4. Forward simulations

We simulated the processes of scCO$_2$ push-pull into the faults of DVGS by using TOUGH2-ECO2N (Pan et al., 2015), a fluid property module for mixtures of CO$_2$, water, and NaCl. Push and pull of scCO$_2$ continued for $t = 0$–30 days and $t = 30$–60 days, respectively. In the numerical simulations, a small mass fraction of NaCl in aqueous phase ($=1 \times 10^{-7}$) was used.

In the push phase, CO$_2$ was injected by using a 0.3 MPa constant overpressure above the local hydrostatic pressure in the injection grid blocks in the fault slip plane and fault gouge of the main fault at Z-coordinates between −3018 m and −3024 m, which is just
below the junction of the main and conjugate faults. The injection grid blocks contain 100% CO₂. Temperature of injected CO₂ was same as the local **ambient temperature** of 265 °C. In the pull phase, fluid was produced by 0.3 MPa underpressure at the same locations as the injection.

Results of numerical simulations are provided in **Fig. 6, Fig. 7, Fig. 8, Fig. 9, Fig. 10, Fig. 11, Fig. 12**. **Fig. 6** shows the distribution profiles of pressure, temperature, and gas saturation in the reservoir, after push (a–c) and pull processes (d–f). After the 30 days of push, the system pressure slightly increased along the faults (**Fig. 6(a)**). Similarly, system pressure slightly decreased along the faults after the subsequent 30-day pull process (**Fig. 6(d)**). System temperature insignificantly changed in the faults after the push and pull, as the CO₂ was injected at the ambient temperature (**Fig. 6(b)** and (e)). (From the preliminary simulation using lower temperature-CO₂, we still observed that the system temperature including **fault planes** hardly changed because of the high effective **heat capacity** of the formation.)
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Fig. 6. Reservoir profiles after 30 days-push and following 30 days of pull: (a) pressure distribution after push, (b) temperature distribution after push, (c) gas saturation distribution after push, (d) pressure distribution after pull, (e) temperature distribution after pull, (f) gas saturation distribution after pull. Note that in the plots of gas saturation distributions (c) and (f), different extents of the domain (different $X$ and $Z$ limits) were used relative to those for the pressure and temperature plots.
Fig. 7. Vectors of CO$_2$ mass flow (kg/s) during push-pull. Note that different length scales of vectors were used in push (a and b) and pull (c and d).

Fig. 8. Observed pressure as a function of time at three different locations in the main and conjugate faults: (a) $Z = -2925$ m, (b) $Z = -2520$ m, (c) $Z = -2100$ m.

Fig. 9. Observed temperature as a function of time at three different locations in the main and conjugate faults: (a) $Z = -2925$ m, (b) $Z = -2520$ m, (c) $Z = -2100$ m.
Fig. 10. Observed gaseous phase saturation as a function of time at three different locations in the main and conjugate faults: (a) $Z = -2925$ m, (b) $Z = -2520$ m, (c) $Z = -2100$ m.
Fig. 11. Gas saturation profiles after 30 days of push: (a) heterogeneous reservoir case (shown in Fig. 2), (b) homogeneous reservoir case without high-permeability zones.

![Gas saturation profiles after 30 days of push](image)

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Fig. 12. Total CO$_2$ mass in place in the fault zones during 30-day-push and 30-day pull: (a) main fault, (b) conjugate fault. Note that the thickness of the 2D model is 10 m in the Y-direction.

The gas saturation profiles in Fig. 6(c) show that the injected CO$_2$ reached upward to $Z = -2070$ m and $-1890$ m in the main and conjugate faults, respectively, i.e., reached a higher level in the smaller conjugate fault. Injected CO$_2$ flowed upward more easily in the conjugate fault than in the main fault because the conjugate fault contacts formations with high permeability over a larger surface area than the main fault does, as shown in Fig. 2, providing less resistance for water in the conjugate fault to flow into the formation as it is displaced by CO$_2$. Accordingly, the vectors of CO$_2$ mass flow in Fig. 6(c) show a more significant rise in the conjugate fault compared to the main fault.
show that more vigorous CO₂ flow was observed in the conjugate fault than in the main fault early in the push phase. After the pull phase, CO₂ had risen by buoyancy to \(Z = -1345\) m and \(-1440\) m in the main and conjugate faults, respectively (Fig. 6(f)). From the CO₂ mass flow vectors in Fig. 7, it is observed that CO₂ still flowed upward in the early time period of the pull phase in both the conjugate and main faults, and slightly flowed down afterward. We observed the pressure, temperature, and saturation of gaseous phase in the gouge of fault zones, where the most injected CO₂ passed along during push and pull. The observation positions are at three different locations at \(Z = -2925\) m, \(-2520\) m, and \(-2100\) m in the main and conjugate faults. The observation results are shown in Fig. 8, Fig. 9, Fig. 10. Note that pressure in the fault zones promptly reacted to the injection and production of CO₂, while temperature and saturation of gaseous phase reacted slower than pressure did.

In order to examine the effects of the low-permeability and high-permeability (brittle) zones surrounding the fault zone, we performed a simulation of push-pull assuming a homogeneous reservoir of low permeability. The gas saturation profiles of the heterogeneous (original) case and the homogeneous low-permeability case are shown in Fig. 11. In the homogeneous reservoir case, injected CO₂ reached \(Z = -2060\) m and \(-2040\) m in the main and conjugate faults, respectively. Fig. 12 shows the CO₂ mass in place during push-pull in the fault zones. Both in the main and conjugate faults, the majority of injected CO₂ flowed into the fault gouge during the push phase. During the pull phase, the majority of CO₂ flowed upward through the damage zone driven by buoyancy effects, and only a small amount of CO₂ was produced through the fault slip plane and fault gouge. Comparing the cases of heterogeneous and homogeneous rock, we observe that the existence of highly permeable zones significantly affected the CO₂ flow in the fault zones during push and pull, especially in the conjugate fault.

5. Sensitivity and data-worth analyses

We use the PEST protocol of iTOUGH2 to perform sensitivity and data-worth analyses, along with the forward simulation of TOUGH2-ECO2N (Finsterle, 1999; Finsterle and Zhang, 2011). We conduct a formal sensitivity analysis of system responses in the fault zones to the unknown parameters shown in Table 1. From the formal sensitivity analysis, we determine the most influential unknown parameters and the most sensitive system responses. Next, we conduct data-worth analysis to determine the most
valuable data to be measured for better prediction of CO$_2$ distribution in the fault zones, with respect to the influential unknown parameters.

5.1. Formal sensitivity analysis

We performed a set of formal sensitivity analyses for the push and pull processes. Both processes are continued for 30 days using constant pressure of injection (+0.3 MPa) and production (-0.3 MPa). By perturbing unknown parameters, we observe system responses and compute the scaled sensitivity coefficients described as:

$S_{ij} = \frac{\partial z_i}{\partial p_j} \cdot \frac{\sigma_{pj}}{\sigma_{zi}}$

(Wainwright and Finsterle, 2016) where, $S_{ij}$ is the scaled sensitivity; $\partial z_i/\partial p_j$ is the partial derivative of output variable ($z_i$) with respect to the unknown parameter ($p_j$); $\sigma_{pj}$ is the parameter scaling factor, which can be a parameter variation or standard deviation; and $\sigma_{zi}$ is the output scaling factor, which can be an expected uncertainty of output.

The initial values and the scaling factors of parameters are listed in Table 2. There are 15 unknown values in the fault zones; and the scaled sensitivity coefficients of measurable system responses to the parameters are computed. We observe the following system responses using geothermal well logging tools: pressure and temperature at three different locations at $Z = -2925$ m, $-2520$ m, and $-2100$ m in the main fault and conjugate fault. The system responses were measured from 2 days to 30 days with a measurement frequency of 1 day, both in push and pull. Scaling factors of pressure and temperature were $1 \times 10^4$ Pa and 0.5 °C, respectively (Steingrímsson, 2013). (Considering that the two measurement points at $Z = -2520$ m in the main fault and $Z = -2925$ m in the conjugate fault would already be drilled (Fig. 1), four more wells would be needed for the additional measurements. Drilling wells for such monitoring will generate cost, and these additional costs for drilling have not been addressed in this study. Note further that the kind of data-worth analysis demonstrated here can be used to minimize the number of additional wells and monitoring points needed to constrain various fault-zone properties.)

Table 2. Initial value (and variation in parentheses) of 15 unknown parameters. Note that the absolute permeability ($K$) is in Log distribution, and the variation of Log$_{10}(K)$ is indicated. No capillary pressure is considered in the fault slip planes. Note that $1/P_0$ is proportional to the square root of the absolute permeability.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Slip plane</th>
<th>Fault gouge</th>
<th>Damage zone</th>
</tr>
</thead>
<tbody>
<tr>
<td>Log$_{10}(K[\text{m}^2])$</td>
<td>11.699 (0.2)</td>
<td>11.699 (0.2)</td>
<td>14.699 (0.2)</td>
</tr>
<tr>
<td>$S_r$</td>
<td>0.30 (0.05)</td>
<td>0.30 (0.05)</td>
<td>0.30 (0.05)</td>
</tr>
</tbody>
</table>
As results of formal sensitivity analysis after push and pull processes, Table 3 shows the sum of absolute scaled sensitivity coefficients, which were obtained from 2 days to 30 days with a measurement frequency of 1 day. For each parameter and output response, the sum was computed as follows.

$S_{\text{sum}} = \sum_{i,t} |S_{ij,t}|$

where, $S_{\text{sum}}$ is the sum of scaled sensitivity coefficients of parameter $p_i$, $S_{ij}$ is the sum of scaled sensitivity coefficients of output response $z_j$ and $S_{ij,t}$ is the scaled sensitivity coefficient of $z_j$ to $p_i$ obtained at each measurement time $t$, respectively.

Table 3. Sum of scaled sensitivity coefficients in descending order during the push and pull processes.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Push</th>
<th>Parameters</th>
<th>Pull</th>
<th>Output responses</th>
<th>Push</th>
<th>Output responses</th>
<th>Pull</th>
</tr>
</thead>
<tbody>
<tr>
<td>$1/P_{FG}$</td>
<td>4142.86</td>
<td>$S_{p,FG}$</td>
<td>1320.0</td>
<td>$P_{M,2100m}$</td>
<td>4280.89</td>
<td>$P_{M,2100m}$</td>
<td>1988.90</td>
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<tr>
<td>$\lambda_{FG}$</td>
<td>2140.6</td>
<td>0</td>
<td>$1/P_{FG}$</td>
<td>942.86</td>
<td>$P_{C,2100m}$</td>
<td>3868.49</td>
<td>$P_{C,2100m}$</td>
</tr>
<tr>
<td>$S_{p,FG}$</td>
<td>1280.0</td>
<td>0</td>
<td>$S_{p,FS}$</td>
<td>700.00</td>
<td>$P_{M,2520m}$</td>
<td>3102.24</td>
<td>$P_{C,3250m}$</td>
</tr>
<tr>
<td>$S_{p,DZ}$</td>
<td>1270.0</td>
<td>0</td>
<td>$S_{p,DZ}$</td>
<td>370.25</td>
<td>$P_{C,3250m}$</td>
<td>1697.08</td>
<td>$P_{C,3250m}$</td>
</tr>
<tr>
<td>$S_{p,FZ}$</td>
<td>1220.0</td>
<td>0</td>
<td>$K_{DZ}$</td>
<td>462.82</td>
<td>$P_{M,3250m}$</td>
<td>927.11</td>
<td>$P_{M,3250m}$</td>
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<td>$K_{FG}$</td>
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<td>$K_{DZ}$</td>
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<td>$\lambda_{DZ}$</td>
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<td>$S_{p,DZ}$</td>
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<td>$T_{M,3250m}$</td>
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<td>$T_{M,3250m}$</td>
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<tr>
<td>$S_{p,DZ}$</td>
<td>50.00</td>
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<td>$T_{M,2100m}$</td>
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<td>$T_{C,3250m}$</td>
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<td>$S_{p,FZ}$</td>
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<td>$S_{p,FZ}$</td>
<td>399.94</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

From the sum of scaled sensitivity coefficients, we can narrow down the most influential unknown parameters in the push and pull phases. In the push phase, we select the five most influential unknown parameters—capillary pressure parameters in fault gouge.
In the pull phase, the five most influential unknown parameters are irreducible saturation of gaseous phase in fault gouge ($S_{gr,FG}$), capillary pressure parameter in fault gouge ($1/P_{0,FG}$), irreducible saturation of gaseous phase in fault gouge and damage zone ($S_{gr,FG}$, $S_{gr,DZ}$), and permeability in damage zone ($K_{DZ}$).

From the sum of scaled sensitivity coefficients of output responses, we find that pressure is much more sensitive than temperature to the unknown parameters, both in push and pull.

In the next section of data-worth analysis, the most influential parameters will be used to predict the uncertainty of CO$_2$ distribution in the faults. We will also analyze the impact of monitoring time for data observation and measurement uncertainty on the relative data worth of each data set.

5.2. Data-worth analysis

Data-worth analysis estimates the value of each measurement point by conducting a formal sensitivity analysis with respect to unknown parameters (Finsterle, 2015; Wainwright and Finsterle, 2016). It can be used either in the evaluation of the worth of calibration data to reduce the uncertainty of parameter estimation, or to reduce the prediction uncertainty. In this study, we apply the data-worth analysis to reduce the prediction uncertainty of CO$_2$ distributions in the fault zones.

The procedure for the data-worth analysis is as follows (Finsterle, 2015; Wainwright and Finsterle, 2016):

1) Select observable variables to be calculated by the forward model.

2) Select parameters affecting the prediction of interest.

3) By running forward simulations, evaluate the sensitivity coefficients, $\partial z_i/\partial p_j$ of all observations and predictions.

4) Evaluate the covariance matrix of the estimated parameters, $C_{pp}$, using the following equation.

$C_{pp} = s_{p2}(JTC_{zz}−1J)^{-1}$
where, \( s_{02} \) is the estimated error variance, which is set to 1 in cases without actually measured data; \( J \) is the Jacobian matrix, which contains the sensitivity coefficients of \( \partial z_i/\partial p_j \). \( C_{zz} \) is the covariance matrix of measurement errors and expected errors of predictions (\( \sigma z_i \)), which has \( \sigma z_i \) as its diagonal components.

1) Propagate the uncertainty of the estimated parameters, \( C_{pp} \), to the uncertainty of predictions,

\[
C_{\hat{z}\hat{z}} = J^* C_{pp} J^* T
\]

where, \( J^* \) is the Jacobian matrix only involving sensitivity coefficients of the predictions.

1) Remove one actual observation datum labeled \( k \) and re-estimate the covariance matrix of parameter, \( C_{p,\cdot \cdot k} \).
2) Re-evaluate the covariance matrix of the model predictions, \( C_{\hat{z}\hat{z}}, \cdot \cdot k \).
3) Scale the prediction matrices by using the acceptable prediction uncertainty and get \( C^- z^- z^- \) and \( C^- z^- z^- , \cdot \cdot k \).
4) Evaluate the data-worth as a relative increase of prediction uncertainty by removing the existing observation data as in the following equation:

\[
\omega - k = 1 - \text{tr}(C^- z^- z^-) \text{tr}(C^- z^- z^- , \cdot \cdot k)
\]

where, \( \omega - k \) is the data worth of observation data labeled \( k \); \( \text{tr} \) gives the trace of matrix, which is the sum of the diagonal components.

In step (1), the observable variables were categorized into the actual observations and predictions. In our case, the actual observations were the pressure and temperature in the fault zones. The prediction variables were the CO\(_2\) distributions in the fault zones, which were described by using the gaseous phase saturation in a two-phase condition. We measured the observation variables starting from \( t = 2 \) days until \( t = 20 \) days with a measurement frequency of 1 day, and predicted the CO\(_2\) distributions in the fault zones at 30 days, in each case of push and pull.

For step (2), we already selected the most influential unknown parameters affecting observation variables from the previous sensitivity analysis. In step (3), these influential parameters were perturbed, and the variable observations and predictions were
calculated. Because we selected the five most influential parameters, six forward simulation runs including one unperturbed standard case plus five perturbed-parameter cases were performed in each of data-worth analyses in the push and pull phases.

The results of data-worth analysis are provided in Table 4 and Fig. 13. In the push phase, $P_{M,2520m}$ showed the highest data worth for reducing prediction uncertainty, followed by $P_{C,2520m}$, $P_{C,2100m}$, and $P_{M,2100m}$. By summing up the data-worth values, we found that the measurement of these four observation data reduced the prediction uncertainly by 86.45%. In addition to these four observations, measurement of $P_{M,2925m}$ reduced the prediction uncertainty even more. The measurement of temperature was not necessarily recommended for the reduction of prediction uncertainty, owing to their low data-worth values. The reason for this result is the much higher sensitivity coefficients of pressure than temperature, which arise because of the faster and more active response of pressure relative to temperature during the push process, as can be seen in Fig. 10.

Table 4. Results of the data-worth analysis in descending order. Note that the observation was made every 1 day starting from $t = 2$ days until $t = 20$ days, in both push and pull phases. Also note that the sum of all data-worth is 1 (=100%).

<table>
<thead>
<tr>
<th>Observation data</th>
<th>Data worth ($\omega$) in push [%]</th>
<th>Observation data</th>
<th>Data worth ($\omega$) in pull [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P_{M,2520m}$</td>
<td>38.81</td>
<td>$P_{C,2100m}$</td>
<td>50.71</td>
</tr>
<tr>
<td>$P_{C,2520m}$</td>
<td>16.73</td>
<td>$P_{M,2100m}$</td>
<td>19.32</td>
</tr>
<tr>
<td>$P_{C,2100m}$</td>
<td>16.52</td>
<td>$P_{C,2520m}$</td>
<td>17.82</td>
</tr>
<tr>
<td>$P_{M,2100m}$</td>
<td>14.39</td>
<td>$P_{M,2520m}$</td>
<td>12.12</td>
</tr>
<tr>
<td>$P_{M,2925m}$</td>
<td>11.15</td>
<td>$T_{M,2520m}$</td>
<td>0.01</td>
</tr>
<tr>
<td>$P_{C,2925m}$</td>
<td>2.29</td>
<td>$T_{C,2100m}$</td>
<td>0.01</td>
</tr>
<tr>
<td>$T_{C,2925m}$</td>
<td>0.11</td>
<td>$P_{M,2925m}$</td>
<td>0.00</td>
</tr>
<tr>
<td>$T_{M,2925m}$</td>
<td>0.00</td>
<td>$P_{C,2925m}$</td>
<td>0.00</td>
</tr>
<tr>
<td>$T_{M,2100m}$</td>
<td>0.00</td>
<td>$T_{M,2100m}$</td>
<td>0.00</td>
</tr>
<tr>
<td>$T_{C,2925m}$</td>
<td>0.00</td>
<td>$T_{M,2925m}$</td>
<td>0.00</td>
</tr>
<tr>
<td>$T_{C,2100m}$</td>
<td>0.00</td>
<td>$T_{C,2520m}$</td>
<td>0.00</td>
</tr>
<tr>
<td>$T_{C,2520m}$</td>
<td>0.00</td>
<td>$T_{C,2520m}$</td>
<td>0.00</td>
</tr>
</tbody>
</table>
Fig. 13. Data worth values at each observation point: (a) in push phase, (b) in pull phase. The plots of domain were obtained from the profiles of gas saturation distributions after push and pull, respectively.

In the pull phase, $P_{C,2100m}$ showed the highest data worth, followed by $P_{M,2100m}$, $P_{C,2520m}$, and $P_{M,2520m}$. The measurement of these four observation data reduced the prediction uncertainly by 99.97%. Other measurement data showed insignificant data worth below 0.01%.

Note that the results of data-worth analysis are significantly affected by the objective of the data-worth analysis. Specifically, if the objective is the reduction of estimation uncertainty of parameters, the data worth of measurement would be quite different.

Table 5 shows the output predictions and prediction uncertainty obtained by the data-worth analysis. Selection of the measurement data and measurement time will be significantly affected by the allowable prediction uncertainty. The most uncertain predictions were of $S_{G,M,2100m}$ and $S_{G,C,2925m}$ as noted by their highest standard deviations after push and pull phases, respectively.

Table 5. Output predictions of gaseous phase saturation in the faults after push and pull, and prediction uncertainty indicated by standard deviations.

<table>
<thead>
<tr>
<th>Output prediction</th>
<th>Prediction at t = 30 days (after push)</th>
<th>Standard deviation (after push)</th>
<th>Prediction at t = 60 days (after pull)</th>
<th>Standard deviation (after pull)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$S_{G,M,2100m}$</td>
<td>0.0016</td>
<td>2.701E-02</td>
<td>0.1542</td>
<td>2.051E-04</td>
</tr>
<tr>
<td>$S_{G,M,2520m}$</td>
<td>0.4534</td>
<td>4.793E-04</td>
<td>0.1327</td>
<td>2.408E-04</td>
</tr>
<tr>
<td>$S_{G,M,2925m}$</td>
<td>0.4624</td>
<td>5.194E-04</td>
<td>0.0865</td>
<td>2.649E-04</td>
</tr>
<tr>
<td>$S_{G,C,2100m}$</td>
<td>0.2887</td>
<td>5.585E-04</td>
<td>0.1434</td>
<td>2.321E-04</td>
</tr>
<tr>
<td>$S_{G,C,2520m}$</td>
<td>0.2666</td>
<td>6.168E-04</td>
<td>0.1233</td>
<td>2.388E-04</td>
</tr>
<tr>
<td>$S_{G,C,2925m}$</td>
<td>0.2465</td>
<td>5.719E-04</td>
<td>0.0800</td>
<td>2.729E-04</td>
</tr>
</tbody>
</table>

To see the effect of monitoring time for data measurement, we conducted data-worth analysis of push and pull processes with variable monitoring times: starting from 2 days until 12 days, 16 days, 20 days (standard case), and 24 days, with a measurement frequency of 1 day. Fig. 14 shows the evolution of pressure data worth during push and pull, as a function of monitoring time. In the push phase, $P_{C,2100m}$ and $P_{M,2520m}$ showed the biggest increase and the biggest decrease in data worth with increasing monitoring.
In the pull phase, \(P_{C,2100m}\) and \(P_{M,2100m}\) showed the biggest increase and the biggest decrease in data worth with increasing monitoring time, respectively.

Fig. 14. Data worth of pressure observation in the fault zones as a function of monitoring time: (a) push phase, (b) pull phase.

Table 6 shows the evolution of temperature data worth during push and pull, as a function of monitoring time. In overall, data worth of temperature measurement was insignificant throughout all cases of different monitoring times.

Table 6. Data worth of temperature observation in the fault zones as a function of monitoring time.

<table>
<thead>
<tr>
<th>Observation data</th>
<th>End of monitoring time (Push)</th>
<th>End of monitoring time (Pull)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(t = 12)days</td>
<td>(t = 16)days</td>
</tr>
<tr>
<td>(T_{M,2100m})</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>(T_{M,2520m})</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>(T_{M,2925m})</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>(T_{C,2100m})</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>(T_{C,2520m})</td>
<td>0.00</td>
<td>0.00</td>
</tr>
</tbody>
</table>
**Fig. 15** shows the evolution of prediction uncertainty of gaseous phase saturation in the fault zones. Prediction uncertainty is indicated by the standard deviation of predictions. We observe the monotonic decrease of prediction uncertainty with increasing monitoring time. The prediction uncertainty was generally higher in the push phase than the pull phase, because the system output responses were more sensitive to the unknown parameters in the push phase as shown in Table 3. Note that the prediction uncertainty of $S_{G \_M \_2100m}$ was much higher than the other predictions in the push phase, as can be seen in Table 5 as well. This was because the injected CO$_2$ approached $Z = -2070$ m in the main fault after the push, and $S_{G \_M \_2100m}$ was very sensitive to the unknown parameters.
Next we show results of data-worth analysis with variable measurement uncertainty of observation data. We conducted data-worth analysis of push and pull processes with variable measurement error of pressure measurement, because the pressure measurement turned out to be very important. We used the values of $1.0 \times 10^4$ Pa (standard case), $1.5 \times 10^4$ Pa, and $2.0 \times 10^4$ Pa for the measurement error of pressure. Fig. 16 shows the changing data worth of temperature observations with respect to the measurement error of pressure. $T_{C_{2925m}}$ in the push phase and $T_{C_{2100m}}$ and $T_{M_{2520m}}$ in the pull phase showed increasing data worth with increasing measurement error of pressure observation, respectively, but their data worth remained insignificant throughout all cases of different measurement errors of pressure observation.

Table 7 shows the evolution of pressure data worth during push and pull, as a function of measurement error of pressure observation. Data worth of each pressure observation slightly decreased with its increasing measurement error.
Table 7. Data worth of pressure observation in the fault zones as a function of its measurement uncertainty. Note that the data worth of $P_{C,2520m}$ showed slight increase with increasing measurement uncertainty, which resulted from decrease of the other observations of pressure.

<table>
<thead>
<tr>
<th>Observation data</th>
<th>Measurement uncertainty of pressure (Pa)</th>
<th>Measurement uncertainty of pressure (Pa)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$1.0 \times 10^4$</td>
<td>$1.5 \times 10^4$</td>
</tr>
<tr>
<td>$P_{M,2100m}$</td>
<td>14.39</td>
<td>14.38</td>
</tr>
<tr>
<td>$P_{M,2520m}$</td>
<td>38.81</td>
<td>38.74</td>
</tr>
<tr>
<td>$P_{M,2925m}$</td>
<td>11.15</td>
<td>11.14</td>
</tr>
<tr>
<td>$P_{C,2100m}$</td>
<td>16.52</td>
<td>16.46</td>
</tr>
<tr>
<td>$P_{C,2520m}$</td>
<td>16.73</td>
<td>16.75</td>
</tr>
<tr>
<td>$P_{C,2925m}$</td>
<td>2.29</td>
<td>2.29</td>
</tr>
</tbody>
</table>

Fig. 17 shows the evolution of prediction uncertainty of gaseous phase saturation in the fault zones. We observe the monotonic increase of prediction uncertainty with increasing measurement error of pressure. As we observed in the cases of different monitoring times, it's found that the prediction uncertainty of $S_{G,M,2100m}$ was much higher than the other predictions in the push phase, throughout all cases of different measurement errors of pressure.

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Fig. 17. Prediction uncertainty as a function of measurement uncertainty of pressure observation: (a) push phase, (b) pull phase.

6. Conclusions

In this study, we investigated the technical feasibility of scCO₂ push-pull testing in a conjugate fault system modeled after the EGS site in Dixie Valley, Nevada, USA. We performed forward numerical simulations of scCO₂ push-pull processes that could be carried out to emplace CO₂ as a contrast agent for seismic and well-logging characterization of the fault zones. Along with the forward simulations, we performed sensitivity analysis and data-worth analysis. From the formal sensitivity analysis, we determined the most influential parameters in the fault zones on the measurable system responses such as pressure and temperature, and the most sensitive system responses among them. From the data-worth analysis, we determined the most valuable observation data to be measured for the best prediction of CO₂ distribution in the faults. These results can be used to guide field monitoring efforts to measure CO₂ saturation in order to calibrate and constrain active seismic monitoring used to characterize the extent and properties of fault zones relevant to EGS objectives.

The results of the forward simulations of 30 days of push and subsequent 30 days of pull revealed several interesting findings. First, injected CO₂ reached a higher depth in the conjugate fault than the main fault after the push. CO₂ was injected at $Z$ between $-3018 \text{ m}$ and $-3024 \text{ m}$, and reached $Z = -2070 \text{ m}$ and $-1890 \text{ m}$ in the main and conjugate faults, respectively. This was because the high-permeability zones of the country rock were concentrated around the conjugate fault allowing displaced water to leave the fault zone and CO₂ to flow upward in the fault zone. To quantify the effect of high-permeability zones in the system, we simulated the push-pull processes in a homogeneous reservoir without the high-permeability zones of country rock. This case showed that the CO₂ approached $Z = -2060 \text{ m}$ and $-2040 \text{ m}$ in the main and conjugate faults, respectively. The second main observation is that most of the injected CO₂ flowed into the highly permeable fault gouge both in the main and conjugate faults during the push phase. In the following pull phase, some of the injected CO₂ was produced back through the fault slip plane and fault gouge, while significant amounts of CO₂ continued to flow upward through the damage zones by the buoyancy effect.

The results of the formal sensitivity analysis presented quantitatively the effects of unknown parameters of the fault zones on the system responses. The unknown
parameters included the absolute permeability, and the parameters of the relative permeability and capillary pressure functions in the fault slip plane, fault gouge, and damage zone. During the push phase, the most influential parameters were the capillary pressure parameters and irreducible saturations of gaseous and aqueous phases in the fault gouge, and irreducible saturation of gaseous phase in slip plane. During the pull phase, the most influential parameters were the irreducible saturation of gaseous phase and capillary pressure parameter in fault gouge, irreducible saturation of gaseous phase in slip plane, and irreducible saturations of gaseous phase and permeability in damage zone. During both push and pull phases, pressure observations were much more sensitive than temperature observations. However, temperature observation will hardly generate significant additional cost relative to the major cost which will occur in drilling wells rather than in monitoring system response.

With the most influential parameters and output responses, we conducted a data-worth analysis in each of push and pull phases. The objective of the data-worth analysis was to minimize the prediction uncertainty of CO$_2$ distribution in the main and conjugate faults. The results of the data-worth analysis showed that the most valuable measurement data were the pressure of the main fault at $Z = -2520$ m and the pressure of the conjugate fault at $Z = -2100$ m in the push and pull phases, respectively. We varied observation time and measurement uncertainty of pressure observation, in order to assess their impact on the data-worth analysis. Data observation time significantly affected the data worth and prediction uncertainty both in push and pull phases, while the effect of measurement uncertainty was not as significant. Once the allowable prediction uncertainty and expected measurement uncertainty are determined, we can decide the minimum monitoring time and the observation data to be measured for the best prediction of CO$_2$ distribution in the fault zones.

The purpose of data-worth analysis in this study was to minimize the prediction uncertainty of CO$_2$ distribution in the fault zones. The relative data worth of each measurement would change if the purpose of the data-worth analysis were the reduction of uncertainty in the estimation of unknown parameters. Still, the impact of the unknown parameters can be effectively managed in our proposed approach to reduce the prediction uncertainty because the prediction uncertainty arises from the unknown parameters.

Although this study was carried out in an idealized 2D model system, the approach we describe is applicable to any system and can be used to design monitoring approaches to collect the most valuable data. These data can then be used to make point measurements to calibrate and constrain active seismic, well logging, or other
monitoring data collected in campaigns aimed at better characterizing permeable faults and fractures critical for EGS. Our envisioned work flow includes active seismic monitoring at Dixie Valley coupled with the data on pressure, temperature, and saturation during the push-pull process.

Acknowledgements

This work was supported by the Office of Energy Efficiency and Renewable Energy, Geothermal Technologies Office, U.S. Department of Energy, and additionally supported by the Assistant Secretary for Fossil Energy (DOE), Office of Coal and Power Systems, through the National Energy Technology Laboratory (NETL), by Lawrence Berkeley National Laboratory under Department of Energy Contract No. DE-AC02-05CH11231, and by EDRA. The authors appreciate Mr. Joe Iovenitti (consulting geoscientist and principal geologist) for providing the fine resolution images of cross sections of geological structure in Fig. 1.

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3) By running forward simulations, evaluate the sensitivity coefficients, \( \partial z_i / \partial p_j \) of all observations and predictions.

4) Evaluate the covariance matrix of the estimated parameters, \( C_{pp} \), using the following equation.

\[
C_{pp} = s_0^2 \left( J^T C_{zz}^{-1} J \right)^{-1}
\]  

(4)

where, \( s_0^2 \) is the estimated error variance, which is set to 1 in cases without actually measured data; \( J \) is the Jacobian matrix, which contains the sensitivity coefficients of \( \partial z_i / \partial p_j \). \( C_{zz} \) is the covariance matrix of measurement errors and expected errors of predictions (\( \sigma_{z_i} \)), which has \( \sigma_{z_i} \) as its diagonal components.

1) Propagate the uncertainty of the estimated parameters, \( C_{pp} \), to the uncertainty of predictions,

\[
C_{\hat{z} \hat{z}} = \tilde{J} C_{pp} \tilde{J}^T
\]  

(5)

where, \( \tilde{J} \) is the Jacobian matrix only involving sensitivity coefficients of the predictions.

1) Remove one actual observation datum labeled \( k \) and re-estimate the covariance matrix of parameter, \( C_{pp} \), \(-k\).

2) Re-evaluate the covariance matrix of the model predictions, \( C'_{\hat{z} \hat{z}, -k} \).