## Title

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## Measurements of the Branching Fractions and Bounds on the Charge Asymmetries of Charmless Three-Body Charged $B$ Decays

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We present measurements of branching fractions and charge asymmetries for charmless $B$-meson decays to three-body final states of charged pions and kaons. The analysis uses $81.8 \mathrm{fb}^{-1}$ of data collected at the $\mathrm{Y}(4 S)$ resonance with the BABAR detector at the SLAC PEP-II asymmetric $B$ Factory. We measure the branching fractions $\mathcal{B}\left(B^{+} \rightarrow \pi^{+} \pi^{-} \pi^{+}\right)=(10.9 \pm 3.3 \pm 1.6) \times 10^{-6}$, $\mathcal{B}\left(B^{+} \rightarrow K^{+} \pi^{-} \pi^{+}\right)=(59.1 \pm 3.8 \pm 3.2) \times 10^{-6}, \quad$ and $\quad \mathcal{B}\left(B^{+} \rightarrow K^{+} K^{-} K^{+}\right)=(29.6 \pm 2.1 \pm 1.6) \times$ $10^{-6}$ and provide $90 \%$ C.L. upper limits for other decays. We observe no charge asymmetries for these modes.

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The study of charmless hadronic $B$ decays can make important contributions to the understanding of $C P$ violation in the standard model, as well as to models of hadronic decays. Reference [1] proposes that the interference between various charmless decays and the $\chi_{c 0}$

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resonance can be used to measure the Cabibbo-Kobayashi-Maskawa (CKM) angle $\gamma$, while the decay $B^{+} \rightarrow \pi^{+} \pi^{-} \pi^{+}$can be used to reduce the uncertainties in the measurement of the CKM angle $\alpha$ [2]. We present branching fractions and charge asymmetries of
charged- $B$-meson decays to three-body final states of charged pions and kaons [3], with no assumptions about intermediate resonances and with charm contributions subtracted, which allows us to set a tight bound on the charmless contribution to the measurement of $\gamma$ [1]. Upper limits and measurements of some of these branching fractions have been obtained previously with smaller statistics [4].

The data used in this analysis were collected at the PEP-II asymmetric $e^{+} e^{-}$storage ring with the BABAR detector, described in detail elsewhere [5]. The onresonance data sample consists of $88.8 \times 10^{6} B \bar{B}$ pairs collected at the $\Upsilon(4 S)$ resonance during the years $1999-2002$. We also use $9.6 \mathrm{fb}^{-1}$ of off-resonance data, collected 40 MeV below the $\mathrm{Y}(4 S)$ resonance, to characterize the backgrounds from $e^{+} e^{-}$annihilation into light $q \bar{q}$ pairs. We assume that the $Y(4 S)$ decays equally to neutral and charged $B$ meson pairs.

Hadronic events are selected based on track multiplicity and event topology. Backgrounds from nonhadronic events are reduced by requiring the ratio of Fox-Wolfram moments $H_{2} / H_{0}[6]$ to be less than 0.98 . Candidate $B$ decays are formed by combining three charged tracks, where each track is required to have at least 12 hits in the tracking chamber, a minimum transverse momentum of $100 \mathrm{MeV} / c$, and to be consistent with originating from the beam spot.

Signal decays are identified using two kinematic variables: (i) the difference $\Delta E$ between the center-of-mass (CM) energy of the $B$ candidate and $\sqrt{s} / 2$, where $\sqrt{s}$ is the total CM energy, and (ii) the beam-energy substituted mass $m_{E S}=\sqrt{\left(s / 2+\mathbf{p}_{i} \cdot \mathbf{p}_{B}\right)^{2} / E_{i}^{2}-\bar{p}_{B}^{2}}$, where the $B$ momentum $\mathbf{p}_{B}$ and the four-momentum of the initial state $\left(E_{i}, \mathbf{p}_{i}\right)$ are defined in the laboratory frame. The $\Delta E$ and $m_{E S}$ distributions of signal events are Gaussian with resolutions of 20 MeV and $2.7 \mathrm{MeV} / c^{2}$, respectively. The typical $\Delta E$ separation between modes that differ by substituting a kaon for a pion in the final state is 45 MeV , assuming the pion mass hypothesis.

Charged pions and kaons are identified using energy loss $(\mathrm{d} E / \mathrm{d} x)$ in the silicon detector and tracking chamber and, for tracks with momenta above $700 \mathrm{MeV} / c$, the Cherenkov angle and number of photons measured by the Cherenkov detector. The efficiency of selecting kaons is approximately $80 \%$, which includes the geometrical acceptance, while the probability of misidentifying pions as kaons is below $5 \%$, up to a laboratory momentum of $4.0 \mathrm{GeV} / c$. Pions are required to fail both the kaon selection and an electron selection algorithm based on information from $\mathrm{d} E / \mathrm{d} x$, shower shapes in the calorimeter, and the ratio of the shower energy and track momentum.

We remove $B$ candidates when the invariant mass of the combination of any two of its daughter tracks (of opposite charge) are within $6 \sigma$ of the mass of the $D^{0}$ meson or within $3 \sigma$ of the mass of the $J / \psi, \psi(2 S)$ or $\chi_{c 0}$ mesons
[7]. Here, $\sigma$ is $10 \mathrm{MeV} / c^{2}$ for $D^{0}, 15 \mathrm{MeV} / c^{2}$ for $J / \psi$ and $\psi(2 S)$, and $18 \mathrm{MeV} / c^{2}$ for $\chi_{c 0}$.

To suppress background from light-quark and charm continuum production, two event-shape variables are computed in the CM frame. The first is the cosine of the angle $\theta_{T}^{*}$ between the thrust axis of the selected $B$ candidate and the thrust axis of the rest of the event, i.e., all charged tracks and neutral particles not assigned to the $B$ candidate. For jetlike continuum backgrounds, $\left|\cos \theta_{T}^{*}\right|$ is strongly peaked towards unity, while it is essentially uniform for signal events. For each signal mode we fix an upper limit on $\left|\cos \theta_{T}^{*}\right|$, between 0.575 and 0.850 . This rejects between $95 \%$ and $85 \%$ of the background, depending on the decay mode.

The second event-shape variable is a Fisher discriminant [8], which is formed from the summed scalar momenta of all charged and neutral particles from the rest of the event within nine $10^{\circ}$-wide nested cones coaxial with the thrust axis of the $B$ candidate. The coefficients of the Fisher discriminant are chosen to maximize the separation between signal and continuum background events and are calculated for each signal mode separately using Monte Carlo simulated signal and continuum events. A further $50 \%$ to $75 \%$ of the remaining background is rejected, depending on the decay mode, by applying selection requirements on this variable.
$B$ decay candidates passing the above selection criteria are required to lie in a signal region defined as follows: $\left|m_{E S}-m_{B}\right|<8 \mathrm{MeV} / c^{2}$ and $|\Delta E-\langle\Delta E\rangle|<60 \mathrm{MeV}$, where $\langle\Delta E\rangle=7 \mathrm{MeV}$ is the mean value of $\Delta E$ measured from on-resonance data for the calibration sample $B^{-} \rightarrow$ $D^{0} \pi^{-}, D^{0} \rightarrow K^{-} \pi^{+}$, and $m_{B}$ is the nominal mass of the charged $B$ meson [7]. Figure 1 shows the projections of the on-resonance data in the signal region onto the $\Delta E$ and $m_{E S}$ axes. Each plot shows the expected levels of continuum and $B \bar{B}$ background, where the latter is parametrized from Monte Carlo samples.

The residual continuum background level is estimated from the observed number of events in the grand sideband (GSB) region, defined to be $5.21<m_{E S}<5.25 \mathrm{GeV} / c^{2}$ and $|\Delta E-\langle\Delta E\rangle|<100 \mathrm{MeV}$, and extrapolating into the signal region. The shape of the $m_{E S}$ distribution of the background is parametrized according to the phenomenologically motivated ARGUS function [9] and is measured using off-resonance data and the upper sideband in the $\Delta E$ variable in on-resonance data $(0.10<\Delta E<$ 0.25 GeV ). A quadratic function is used to parametrize the $\Delta E$ distribution of the background. The ratio of the integrals over the signal and GSB regions of the product of the $\Delta E$ and $m_{E S}$ shape functions, $R$, gives the ratio of the number of background events in the two areas.

The branching fraction for each channel is measured over the whole Dalitz plot, which is divided into $28 \times 28$ cells of equal area $\left(1 \mathrm{GeV}^{2} / c^{4}\right)^{2}$ to enable us to find the selection efficiency as a function of position in the Dalitz plot. Taking $\epsilon_{i}$ to be the efficiency of reconstructing the signal in the $i$ th bin of the Dalitz plot, determined from


FIG. 1. Projections of $\Delta E$ and $m_{E S}$ for $B^{+} \rightarrow \pi^{+} \pi^{-} \pi^{+}$(a) and (b), $B^{+} \rightarrow K^{+} \pi^{-} \pi^{+}$(c) and (d), $B^{+} \rightarrow K^{+} K^{-} \pi^{+}$(e) and (f), $B^{+} \rightarrow K^{+} K^{-} K^{+}$(g) and (h), $B^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$(i) and (j), and $B^{+} \rightarrow K^{+} K^{+} \pi^{-}(\mathrm{k})$ and (l) in the signal region. The signal region requirement was made on the orthogonal variable in each case. The dashed curves show the continuum background, while the solid lines include the $B \bar{B}$ background.

Monte Carlo simulated events, the branching fraction for each signal mode is given by

$$
\begin{equation*}
\mathcal{B}=\frac{1}{N_{B \bar{B}}}\left(\sum_{i} \frac{\left(N_{1 i}-R N_{2 i}-N_{x} p_{i}\right)}{\epsilon_{i}}-n_{x}-n_{b}\right), \tag{1}
\end{equation*}
$$

where $N_{1 i}$ and $N_{2 i}$ are the number of events observed in the signal and GSB regions, respectively, while $N_{x} p_{i}, n_{x}$, and $n_{b}$ are background contributions that are defined below. $N_{B \bar{B}}$ is the total number of $B \bar{B}$ pairs in the data sample. No significant differences were found for the value of $R$ (defined earlier) in different regions of the Dalitz plot, so an average value is used for all bins.

The probability of a kaon being misidentified as a pion is $20 \%$. This means there is significant cross feed into the signal region from the decay mode that has one more kaon, which is subtracted for each bin $i$. This is represented by the $N_{x} p_{i} / \epsilon_{i}$ term in Eq. (1), where $N_{x}$ is the total number of events that is the source of the cross feed, and $p_{i}$ is the probability for the cross feed events to pass the selection criteria for the $i$ th bin, which is estimated from Monte Carlo samples. The $B^{+} \rightarrow K^{+} K^{-} K^{+}$mode has $N_{x}=0$, since it has no cross feed backgrounds. For the other decays, $N_{x}$ is obtained by multiplying $N_{B \bar{B}}$ by the branching fraction of the signal mode that has a kaon substituting a pion in the final state. There is also secondorder cross feed where either two kaons are misidentified as pions (probability of $4 \%$ ), or one of the pions is misidentified as a kaon (probability of $2 \%$ ). This is represented by the $n_{x}$ term in Eq. (1).

Finally, the $n_{b}$ term represents the small number of other $B \bar{B}$ backgrounds that are subtracted. For all signal modes except $B^{+} \rightarrow K^{+} K^{-} K^{+}, n_{b}$ is obtained from the number of $D^{0}$ and $\bar{D}^{0}$ candidates whose invariant mass is beyond the $6 \sigma$ range. For $B^{+} \rightarrow K^{+} \pi^{-} \pi^{+}$, there is also a contribution from $B^{ \pm} \rightarrow \eta^{\prime}\left(\rightarrow \rho^{0} \gamma\right) K^{ \pm}$decays, which is estimated from the selection efficiency from Monte Carlo simulated decays, and the branching fraction quoted in Ref. [7]. By using a mixture of Monte Carlo-simulated charm and charmless decays, we found that there were no other significant $B \bar{B}$ backgrounds.

We do not divide the Dalitz plot into cells for the standard model-suppressed modes $B^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$and $B^{+} \rightarrow K^{+} K^{+} \pi^{-}$and instead use the average values of the signal efficiency and cross feed terms.

The branching fraction results are summarized in Table I, where the first four rows show the total number of events in the signal and GSB regions, the average signal efficiencies $\langle\epsilon\rangle$, and the values of $R$ for each mode. The absolute efficiency variation across the Dalitz plot typically varies between $\pm 2 \%$ and $\pm 5 \%$ from $\langle\epsilon\rangle$.

Rows A and B represent the total number of events and the amount of continuum background in the signal region, corrected for efficiency. The uncertainties for row A come from the statistical errors in $N_{1 i}$, while the uncertainties for row B correspond to the statistical errors in $N_{2 i}$ and the systematic errors from $R$, which arise from the limited statistics in the sideband region and offresonance data.

Row C shows the expected background from cross feed events. The first and second uncertainties of these quantities represent the systematic errors in $p_{i}$ and $N_{x}$, respectively, except for the channel $B^{+} \rightarrow K^{+} K^{+} \pi^{-}$, where the uncertainty represents the average of the $p_{i}$ and $N_{x}$ contributions. The second-order cross feed terms $n_{x}$ are shown in row D . Note that the $n_{x}$ term for $B^{+} \rightarrow K^{+} \pi^{-} \pi^{+}$is negative, which corrects for the $B^{+} \rightarrow K^{+} K^{-} K^{+}$cross feed into $B^{+} \rightarrow K^{+} K^{-} \pi^{+}$, which in turn contributes to the cross feed background for $B^{+} \rightarrow K^{+} \pi^{-} \pi^{+}$.

TABLE I. Branching fraction results for on-resonance data. The quantities and their uncertainties are explained in the text.

| Signal Mode | $\pi^{ \pm} \pi^{\mp} \pi^{ \pm}$ | $K^{ \pm} \pi^{\mp} \pi^{ \pm}$ | $K^{ \pm} K^{\mp} \pi^{ \pm}$ | $K^{ \pm} K^{\mp} K^{ \pm}$ | $K^{\mp} \pi^{ \pm} \pi^{ \pm}$ | $K^{ \pm} K^{ \pm} \pi^{\mp}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $\sum_{i} N_{1 i}$ | 1029 | 1502 | 733 | 646 | 494 | 209 |
| $\sum_{i} N_{2 i}$ | 5577 | 5209 | 4012 | 1308 | 3268 | 1025 |
| $\langle\epsilon\rangle(\%)$ | $12.7 \pm 0.5$ | $12.8 \pm 1.4$ | $13.9 \pm 0.9$ | $14.9 \pm 0.9$ | $18.5 \pm 0.9$ | $15.3 \pm 0.7$ |
| $R$ | $0.144 \pm 0.003$ | $0.146 \pm 0.003$ | $0.150 \pm 0.003$ | $0.158 \pm 0.006$ | $0.155 \pm 0.003$ | $0.157 \pm 0.006$ |
| A) $\sum_{i} N_{1 i} / \epsilon_{i}$ | $7597 \pm 275$ | $11056 \pm 327$ | $5071 \pm 216$ | $4011 \pm 182$ | $2670 \pm 120$ | $1366 \pm 94$ |
| B) $\sum_{i} R N_{2 i} / \epsilon_{i}$ | $5938 \pm 94 \pm 117$ | $5604 \pm 89 \pm 111$ | $4041 \pm 72 \pm 80$ | $1381 \pm 46 \pm 55$ | $2738 \pm 48 \pm 53$ | $1052 \pm 33 \pm 40$ |
| C) $\sum_{i} N_{x} p_{i} / \epsilon_{i}$ | $474 \pm 33 \pm 40$ | $22 \pm 1 \pm 30$ | $671 \pm 15 \pm 59$ | $\cdots$ | $\cdots$ | $344 \pm 31$ |
| D) $n_{x}$ | $\ldots$ | $-189 \pm 34$ | $110 \pm 128$ | $\cdots$ | $\cdots$ | $53 \pm 5$ |
| E) $D^{0}$ Bkgnd | $216 \pm 24$ | $268 \pm 28$ | $47 \pm 6$ | $\cdots$ | $33 \pm 5$ | $31 \pm 5$ |
| F) $\eta^{\prime} K$ Bkgnd | $\cdots$ | $106 \pm 30$ | $\ldots$ | $\cdots$ | $\cdots$ | $\cdots$ |
| G) Signal Yield | $970 \pm 291 \pm 130$ | $5246 \pm 339 \pm 127$ | $202 \pm 227 \pm 163$ | $2630 \pm 188 \pm 55$ | $-101 \pm 129 \pm 53$ | $-114 \pm 100 \pm 51$ |
|  | $\pm 22 \pm 50$ | $\pm 39 \pm 247$ | $\pm 16 \pm 9$ | $\pm 12 \pm 124$ | $\pm 0 \pm 5$ | $\pm 0 \pm 5$ |
| $\mathcal{B}\left(\times 10^{-6}\right)$ | $10.9 \pm 3.3 \pm 1.6$ | $59.1 \pm 3.8 \pm 3.2$ | $2.3 \pm 2.6 \pm 1.8$ | $29.6 \pm 2.1 \pm 1.6$ | $-1.1 \pm 1.5 \pm 0.6$ | $-1.3 \pm 1.1 \pm 0.6$ |
| Significance $(\sigma)$ | 5.7 | $>6$ | 1.1 | $>6$ | $\cdots$ | $\cdots$ |
| $90 \%$ C.L. | $\cdots$ | $\cdots$ | $<6.3$ | $\cdots$ | $<1.8$ | $<1.3$ |

Rows E and F show the expected backgrounds from $D^{0}$ and $\eta^{\prime} K$ decays, which include the uncertainties from the selection efficiencies and the branching fractions of the background decays [7]. The sum of these two rows gives the value of $n_{b}$ in Eq. (1).

Row G shows the signal yield, obtained by subtracting rows B to F from row A . The first uncertainty is the combination of the statistical errors of the number of events in the signal and GSB regions. The second uncertainty corresponds to the sum in quadrature of all the systematic errors from rows B to F . The third error is from the bin-by-bin uncertainty of the selection efficiency. This is zero for $B^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$and $B^{+} \rightarrow K^{+} K^{+} \pi^{-}$, where we use only the average efficiencies. The last uncertainty originates from global systematic errors in the signal efficiencies due to charged-particle tracking ( $0.8 \%$ per track), event-shape variable selections (1.0 to $2.5 \%$ ), and from particle identification ( $1.4 \%$ and $1.0 \%$ per pion and kaon track, respectively).

The next row in Table I shows the branching fraction results, where the first uncertainties are from the statistical errors in the number of events, while the second uncertainties are the sum in quadrature of all systematic errors mentioned above.

The significance of each branching fraction result, under the null hypothesis, is defined as the ratio of the signal yield to the total (statistical and systematic) uncertainty of the background in the signal region. We observe significant signals for the modes $B^{+} \rightarrow \pi^{+} \pi^{-} \pi^{+}$, $B^{+} \rightarrow K^{+} \pi^{-} \pi^{+}$, and $B^{+} \rightarrow K^{+} K^{-} K^{+}$and provide $90 \%$ C.L. upper limits for the other channels, using the formalism in Ref. [10]. The branching fraction of the control sample $B^{-} \rightarrow D^{0} \pi^{-}, D^{0} \rightarrow K^{-} \pi^{+}$, which has the same final state as $B^{+} \rightarrow K^{+} \pi^{-} \pi^{+}$, is measured to be $(190 \pm 3 \pm 10) \times 10^{-6}$, which agrees with the average of published measurements $(201 \pm 20) \times 10^{-6}$ [7].

We have also measured the charge asymmetries for the modes with observed signals using a method similar to
that used for the branching fraction measurements. The charge asymmetries are defined as $\mathcal{A}=\left(N^{-}-N^{+}\right) /$ $\left(N^{-}+N^{+}\right)$, where $N^{-}\left(N^{+}\right)$is the signal yield for negatively (positively) charged $B$ candidates, as defined by row G in Table I. The normalization factor $N_{B \bar{B}}$ cancels out in the asymmetry ratio, while the cross feed and $B \bar{B}$ background contributions cancel in the asymmetry numerator. The measured charge asymmetries are $\mathcal{A}\left(B^{+} \rightarrow\right.$ $\left.\pi^{+} \pi^{-} \pi^{+}\right)=-0.39 \pm 0.33 \pm 0.12, \mathcal{A}\left(B^{+} \rightarrow K^{+} \pi^{-} \pi^{+}\right)=$ $0.01 \pm 0.07 \pm 0.03, \quad$ and $\mathcal{A}\left(B^{+} \rightarrow K^{+} K^{-} K^{+}\right)=0.02 \pm$ $0.07 \pm 0.03$, where the first uncertainties are statistical and the second are systematic, which include the charge bias of the tracking and particle identification selection requirements (1\%).

In summary, we have measured the branching fraction of $B^{+} \rightarrow \pi^{+} \pi^{-} \pi^{+}$for the first time, which is smaller than that assumed in Ref. [1], and we have also observed the channels $B^{+} \rightarrow K^{+} \pi^{-} \pi^{+}$and $B^{+} \rightarrow K^{+} K^{-} K^{+}$. We observed no charge asymmetries in these decays.

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[1] B. Bajc et al., Phys. Lett. B 447, 313 (1999).
[2] A. E. Snyder and H. R. Quinn, Phys. Rev. D 48, 2139 (1993).
[3] Throughout this Letter, flavor-eigenstate decay modes imply also their charge conjugate.
[4] CLEO Collaboration, T. Bergfeld et al., Phys. Rev. Lett. 77, 4503 (1996); BELLE Collaboration, A. Garmash et al., Phys. Rev. D 65, 092005 (2002).
[5] BABAR Collaboration, B. Aubert et al., Nucl. Instrum. Methods Phys. Res., Sect. A 479, 1 (2002).
[6] G. C. Fox and S. Wolfram, Phys. Rev. Lett. 41, 1581 (1978).
[7] Particle Data Group, K. Hagiwara et al., Phys. Rev. D 66, 010001 (2002).
[8] CLEO Collaboration, D. M. Asner et al., Phys. Rev. D 53, 1039 (1996).
[9] ARGUS Collaboration, H. Albrecht et al., Z. Phys. C: Part. Fields 48, 543 (1990).
[10] G. J. Feldman and R. D. Cousins, Phys. Rev. D 57, 3873 (1998).


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