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<u>Summary.</u> A brief review is given of the various self-field phenomena associated with the longitudinal motion of particles in storage rings.

Introduction

Although there are some high-intensity phenomena for which the coupling of longitudinal and transverse motion is essential, such as, for example, the headtail effect; the great majority of high-intensity phenomena primarily involve either longitudinal or transverse degrees of freedom. In this review, we restrict our attention to phenomena which are essentially longitudinal in nature.

It is convenient to consider separately the behavior of unbunched (coasting) and bunched (external RF system in operation) beams. Detailed experimental information on coasting beams has been obtained on the ISR, on the (old) CERN electron model CESAR, and on electron ring accelerators. All high-energy electron storage rings have bunched beams and, of course, so do synchrotrons, so that there are a large number of sources of experimental information about the longitudinal motion of bunched beams.

Unbunched Beams

The primary phenomenon, due to self-field effects, in the longitudinal motion of a coasting beam is spontaneous formation of longitudinal density variations. For a storage ring operating above the transition energy (so that df/dE is negative) the effect is physically very simple (the "negative mass instability"), and both growth rates in the linear regime and thresholds were theoretically derived¹ prior to the phenomenon being observed on a variety of machines.²

Although the original negative mass theory considered bunching arising from self-forces associated with a beam in a smooth, perfectly conducting, and essentially straight vacuum chamber, it was soon realized that the beam-surroundings played an essential role in the instability. In particular, unexcited RF cavities,³ resistive walls,⁴ and ceramic chambers⁵ were shown to be able to greatly enhance the phenomenon (even to cause it below transition where the mass is positive), and hence the beam environment became of considerable concern to builders of storage rings.

It is convenient to introduce a longitudinal coupling impedance Z_n defined by 6

$$Z_n = -\frac{2\pi R E_n}{I_n}, \qquad (1)$$

where E_n is the <u>n</u>th harmonic of the azimuthal electric field at the beam, I_n is the <u>n</u>th harmonic of the beam current and R is the orbit radius. An approximate criterion for stability of a coasting beam against self-bunching at the frequency n ω_{rev} is 1,4,7

$$\frac{|\mathbf{Z}_{n}|}{n} \leq \frac{\eta \gamma \mathbf{U}_{0}}{\mathbf{I}_{0}} \left(\frac{\Delta \mathbf{E}}{\mathbf{E}}\right)^{2}, \qquad (2)$$

where $\omega_{rev} = \beta c/R$ is the particle revolution frequency,

$$\eta = \left| \frac{1}{\gamma_t^2} - \frac{1}{\gamma_t^2} \right|,$$

with γ_t the transition energy in units of m_0c^2 and γ the particle energy in units of m_0c^2 so that $E = \gamma m_0c^2$, $U_0 = m_0c^2/e = 0.511$ MV for electrons and 938 MV for protons, $I_0 = Ne f_{rev}$ is the circulating beam current, and $\Delta E/E$ is the full width of the beam energy distribution at half maximum. This stability criterion arises from the balance between the instability-driving forces characterized by Z_n and the Landau damping associated with energy (and hence frequency) spread.

At the present time a considerable body of knowledge exists concerning the coupling impedance Z_n . Theoretical calculations have been performed by a large number of workers for a variety of structures (see references cited in Ref. 6.), and methods have even been devised for measuring $Z_n \cdot \frac{8}{2}$

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Recently, there have been detailed experimental studies of the onset of azimuthal instabilities.^{9,10} The work on electron ring accelerators so-far provides only qualitative accord with the criterion (2), but the observations on the ISR are in remarkably good quantitative agreement with (2). Spontaneous beam bunching due to interaction of a coasting beam with an unexcited RF cavity has been observed on the AGS, and avoided either by increasing the beam energy spread or by de-tuning; i.e., reducing the cavity contribution to Z_n .¹¹

The experimental observations are particularly interesting because the phenomenon of beam bunching can be observed in the nonlinear regime where the theory, presently, is far from complete.¹² Generally, it is observed² that the instability is selfstabilizing; i.e., a certain degree of bunching occurs, and, subsequently the beam again becomes longitudinally uniform (but with a larger energy spread than it had initially). Because this process leads to beam widening it is generally bad as it results in particle loss if there are aperture stops, and in the case of the electron ring accelerator to degraded ring quality.

Finally, it should be noted that recently observations have been made on electron rings of RF signals without noticeable beam degradation, 9 which, perhaps, is related to a prior theoretical calculation on mini-instabilities.¹³

Bunched Beams

In a stored bunched beam there are two classes of high intensity effects; namely coherent bunch motion, and alterations in bunch size and shape. Coherent Bunch Motion

The simplest coherent mode of a single bunch is the dipole mode (m = 1); i.e. rigid-bunch motion. Most of the analysis in the literature is confined to this mode, although some authors have considered higher order modes (m > 1) $.^{14,15}$ For the simple case in which the phase of the bunch center ϕ_i for bunch i, may be treated in linear approximation and in which there is no external feedback we have 11,16,17,18

$$\ddot{\phi}_{i} + \omega_{s}^{2} \phi_{i} = \sum_{j=1}^{B} A_{ij} \phi_{j}, \qquad (3)$$

where B is the number of bunches, ω_s is the frequency of small phase oscillations, and the coefficients A_{ii} are given by

$$A_{ij} = -\frac{\omega_s^2}{V\cos\phi_s} \frac{\partial V_{ij}}{\partial\phi_j}.$$
 (4)

In Formula (4), V is the voltage gain per turn, ϕ_s is the stable phase angle, and V_{ij} is the voltage on bunch i caused by bunch j. Clearly V_{ij} can be expressed in terms of a coupling impedance.¹⁷

If all the bunches are equal then the A_{ij} are only functions of i-j and the B normal modes are simply the B-roots of unity: 11,17,19

$$\phi_{1} = e^{i\omega_{n}(1)t}$$

$$\phi_{j} = \phi_{1} e^{in(j-1)2\pi/B},$$
(5)

where $n = 1, \dots B$ characterizes the mode and

$$\omega_{n}^{(1)} \approx \omega_{s} - \frac{1}{2\omega_{s}} \sum_{j=1}^{B} A_{j1} e^{in(j-1)2\pi/B}.$$
 (6)

Clearly if $\operatorname{Im} \omega_n^{(1)} < 0$ the <u>n</u>th mode is unstable. If the nonlinear nature of the synchrotron motion is included, then a dispersion analysis shows ^{14,15,18} that the <u>n</u>th mode will be stable, even if $\operatorname{Im} \omega_n^{(1)} < 0$, provided

$$|\omega_n^{(1)} - \omega_s| < s/4 \tag{7}$$

where S is the full-spread in the synchrotron oscillation frequency of particles in a bunch.

The analysis for unequal bunches has resulted in a condition for decoupling of the bunches; namely that the spread in individual bunch frequencies must be greater than the shift in frequency due to coupling. Stability requires, in addition, that a condition analogous to (7) be satisfied;¹⁵ namely that for the <u>m</u>th order mode, having frequency $\omega^{(m)}$,

$$|\omega^{(\mathbf{m})} - \mathbf{m}\omega_{s}| < \frac{\sqrt{\mathbf{m}}}{4} s. \qquad (8)$$

Also, in the literature, are numerical studies of unequal bunches and analysis of the influence of beam control systems and active feed-back damping.¹⁷

Observations have been made on the CERN PS,¹⁷ the AGS,¹¹ and the CEA,²⁰ as well as on the storage rings in Novosibirsk and Frascati. In general there is

good agreement between the observations and theory, although in some cases the actual values of the A_{ij} have been larger than was a priori expected. Bunch Size and Shape

It was first observed, at Orsay and Frascati, that the length of bunches in the storage rings was a function of the stored current. No such effect was observed at Stanford or Novosibirsk.²¹ Recent observations at CEA,²⁰ SLAC,²² and Frascati¹⁹ have indicated that both bunch length and width increases with increasing stored current. The parametric dependence of bunch length, \triangle , on beam current, I, beam energy, E, and RF voltage, V, is (approximately) for bunch length large compared to the natural (low-current) bunch length, \triangle_0 , (as has been summarized in Ref. 21):

$$\Delta(ns) = \frac{0.46 \, I \, (mA)^{1/3}}{E(GeV)^{7/6}} \left[\frac{30}{V(keV)} \right]^{1/6} \Delta_0(ns)^{2/3} .$$
(9)

Prior to the observation of bunch widening, a general equilibrium theory of bunch length was developed.²³ This theory included the effect of coherent synchrotron radiation as well as the electrical interaction of a beam with various resonant structures that might be present in a storage ring. The parametric dependence of bunch length was found to be in good agreement with (9), and numerical estimates--based upon reasonable guesses for the characteristics of resonant structures--were in substantial agreement with (9). This theory, however, predicted no bunch widening which isn't necessarily a defect of the theory since the two phenomena may be unrelated.

An alternative, and older, theory suggested that the instability of internal coherent synchrotron oscillations could explain bunch lengthening.²⁴ However, the parametric dependence deduced in this work is not in good accord with observations, although the theory does predict both bunch lengthening and widening.

In some work which is still in progress, the present writer has, in the spirit of Ref. 24, developed a theory of the behavior of a beam whose natural energy width--resulting from the balance between quantum fluctuations and classical radiation damping --is less than that required for the stability of collective modes. It is shown that in this circumstance there is a turbulent equilibrium state in which the wave diffusion (due to stable collective modes with finite amplitudes) augments the quantum diffusion so as to yield a bunch of increased width and length. The theory, perhaps when combined with the equilibrium theory of Ref. 23, appears capable of explaining the observations, but it is too early to be sure that the proposed explanation is indeed correct.

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