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# Characterizing protein kinase A (PKA) subunits as macromolecular regulators of PKA RI $\alpha$ liquid–liquid phase separation

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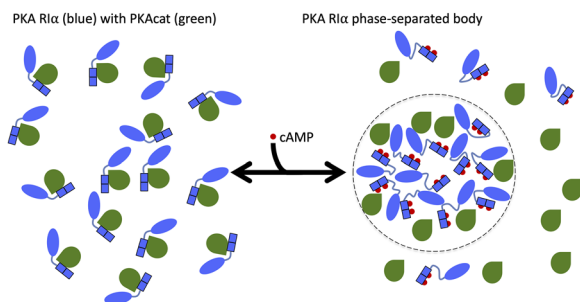
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The ubiquitous small molecule cyclic adenosine monophosphate (cAMP) controls a diverse set of cellular processes by binding and regulating several enzymes such as protein kinase A (PKA). The PKA holoenzyme consists of a dimer of regulatory subunits and a pair of catalytic (PKA<sub>cat</sub>) subunits. Binding of cAMP to PKA regulatory subunits induces the release and activation of PKA<sub>cat</sub>. This binding event also increases the structural disorder of the type I regulatory subunit RI $\alpha$ .<sup>1</sup> As liquid–liquid phase separation (LLPS) is driven, in part, by intrinsic disorder, the more disordered, cAMP-bound form of RI $\alpha$  more readily phase separates, while the more ordered, PKA<sub>cat</sub>-bound form of RI $\alpha$  resists phase separation<sup>2</sup> (Fig. 1). By sequestering many cAMP molecules, RI $\alpha$  phase separation is a crucial driver for compartmentalizing cAMP; disruption of the phase-separated bodies leads to oncogenic effects. As RI $\alpha$  LLPS is intricately regulated by its binding partners, we aimed to explain these complex effects through computational modeling.

Previously, Ghosh, Mazarakos, and Zhou<sup>3</sup> reported a combined experimental and computational study to define three classes of macromolecular regulators: volume-exclusion promoters, weak-attraction suppressors, and strong-attraction promoters. Volume-exclusion regulators promote LLPS by taking up volume in the bulk phase and displacing the protein molecules undergoing LLPS to form liquid droplets. Weak-attraction regulators, on the other hand,

suppress LLPS by being weakly attracted to the protein molecules undergoing LLPS and disrupting liquid droplet formation. Strong-attraction regulators (at low concentrations) promote LLPS by forming stronger attraction with the protein molecules undergoing LLPS inside liquid droplets. By comparing *in vitro* phase diagrams of RI $\alpha$  liquid droplet formation under various conditions shown in Ref. 2 with phase diagrams of the three macromolecular regulators shown in Ref. 3, we can categorize the different macromolecules into one of the three regulator classes. Polyethylene glycol (PEG) 4000, which was used to mimic cellular conditions for RI $\alpha$  in *in vitro* experiments and was shown to be necessary for liquid droplets to form, can be categorized as a volume-exclusion promoter. On the other hand, PKA<sub>cat</sub> in the presence of cAMP can be categorized as a strong-attraction promoter, and PKA<sub>cat</sub> bound to cAMP-free RI $\alpha$  can be categorized as a weak-attraction suppressor for RI $\alpha$  phase separation. Computationally, the phase diagrams in Ref. 3 were obtained on patchy particle models of the same size; it is thus difficult to use them for quantitative modeling of experimental systems.

To characterize the degree of attraction between different protein partners, here we developed a method called fast Fourier transform (FFT)-based Modeling of Atomistic Protein–protein interactions applied to cross second virial coefficient  $B_{23}$  (FMAPB23). FMAPB23 is an extension of FMAPB2,<sup>4–7</sup> which calculates the



**FIG. 1.** Illustration of the regulation of PKA RI $\alpha$  phase separation by different binding partners. Binding of two cAMP molecules (red) per RI $\alpha$  subunit (blue) leads to dissociation (and activation) of PKA<sub>cat</sub> (green). The increased disorder in the RI $\alpha$  linker region [between the N-terminal dimerization and docking (D/D) domain in oval and tandem cAMP-binding domains in rectangle] and the action of the dissociated PKA<sub>cat</sub> promote the formation of phase-separated bodies (highlighted on the right with a dotted boundary). In contrast, PKA<sub>cat</sub> in the absence of cAMP suppresses RI $\alpha$  phase separation by binding to and rigidifying RI $\alpha$  (shown on the left). For clarity, only a half of a holoenzyme, consisting of a single PKA<sub>cat</sub> subunit and a single RI $\alpha$  subunit, is illustrated.

second virial coefficient  $B_2$  for all-atom proteins in an implicit solvent.  $B_2$  is determined by the interaction energy between two molecules of the same protein, which includes steric, electrostatic, and non-polar components. Specifically,  $B_2$  is the integration of the Mayer  $f$ -function or  $e^{-\beta U(\mathbf{R}, \Omega, X)} - 1$ ,

$$B_2 = -\frac{1}{2} \frac{1}{8\pi^2} \frac{1}{\mathcal{V}_X} \int d\mathbf{R} d\Omega dX \left[ e^{-\beta U(\mathbf{R}, \Omega, X)} - 1 \right], \quad (1)$$

where  $\mathbf{R}$  denotes the relative position vector between the two molecules,  $\Omega$  denotes three relative rotation angles, such as the Euler angles,  $X$  denotes internal degrees of freedom (in flexible molecules),  $U(\mathbf{R}, \Omega, X)$  denotes the intermolecular interaction energy, and  $\mathcal{V}_X = \int dX$ . A potential of mean force (PMF)  $W(R)$  is obtained by averaging over all but the intermolecular distance  $R$ ,

$$\begin{aligned} e^{-\beta W(R)} &\equiv \frac{1}{4\pi} \frac{1}{8\pi^2} \frac{1}{\mathcal{V}_X} \int d\theta d\phi d\Omega dX \sin \theta e^{-\beta U(\mathbf{R}, \Omega, X)} \\ &\equiv \langle e^{-\beta U(\mathbf{R}, \Omega, X)} \rangle_{\theta, \phi, \Omega, X}, \end{aligned} \quad (2)$$

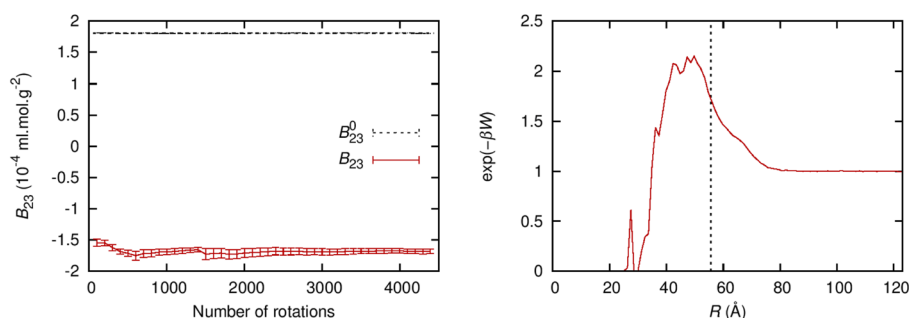
where  $\theta$  and  $\phi$  denote the polar and azimuthal angles of the relative position vector  $\mathbf{R}$ . Note that from Eq. (1), it is apparent that repulsive interactions [i.e., positive  $U(\mathbf{R}, \Omega, X)$ ] will make  $B_2$  more positive, whereas attractive interactions [i.e., negative  $U(\mathbf{R}, \Omega, X)$ ] will make  $B_2$  more negative. The terms of the interaction energy are then expressed as correlation functions and calculated by using FFT. In comparison,  $B_{23}$  is determined by the interaction energy between two **different** protein molecules. The calculations of  $B_2$  and  $B_{23}$  are thus identical, except that the interaction energy is between two of the **same** kind of molecule for the former but between two **different** kinds of molecules for the latter. FMAPB2 has a scaling parameter ( $\nu_s$ ) for non-polar interactions that depends on protein molecular weight  $M$  (in kD). We took the geometrical mean of the molecular weights of the two protein molecules as  $M$  for calculating  $\nu_s$  in FMAPB23.

To use FMAPB23 in practice, the program requires as input the ionic strength, temperature, and structure files of the two protein molecules in the PQR format. The PQR files can be converted using PDB2PQR<sup>8</sup> from structural files downloaded from the Protein Data Bank (PDB). The atomic partial charges for protein residues are from the PARSE set.<sup>9</sup> The output from FMAPB23 is similar to that of FMAPB2, which includes  $B_{23}$ , its steric component  $B_{23}^0$ , and the PMF over distance  $R$  between the two protein molecules, as shown in Fig. 2. In calculating the steric component  $B_{23}^0$ , the two protein molecules are assumed to only have steric repulsion, corresponding to an infinite interaction energy whenever any atom of one molecule clashes with any atom of the other molecule. As with FMAPB2,<sup>7</sup> at low temperatures,  $B_{23}$  can be dominated by a few low energy configurations, potentially leading to significant errors. In addition, a grid spacing around 0.6 Å is necessary for discretization in FFT calculations in order to get converged energies, which limits how large the proteins can be for the available memory of a computer.

The cross second virial coefficient  $B_{23}$  was calculated for Mg<sup>2+</sup>-bound PKA<sub>cat</sub> [denoted as PKA<sub>cat</sub>(Mg<sup>2+</sup>)] and cAMP-bound RI $\alpha$  [denoted as RI $\alpha$ (cAMP)]. Five structures for the first molecule were taken from PDB: 6NO7 chains E and G, 3O7L chain B, and 4NTT chains A and B; two structures for the second molecule were taken from 4MX3 chains A and B. The results from the total of ten runs were used to calculate a mean value and a standard error of the mean (see Table I). Note that Mg<sup>2+</sup> was taken as an integral part of molecule 1, while cAMP was taken as an integral part of molecule 2. Partial charges for Mg<sup>2+</sup> and cAMP were unavailable from the PARSE set. For Mg<sup>2+</sup>, we assumed a charge of +2 as a crude treatment; partial charges of cAMP were obtained from the R.E.D. Server.<sup>10</sup>  $B_{23}$  was also calculated for the PKA<sub>cat</sub>(Mg<sup>2+</sup>)-RI $\alpha$  complex and cAMP-free RI $\alpha$ . The structures were from PDB: 6NO7, with chains EF or GH for molecule 1 and chains B, D, F, or H for molecule 2. We assume that PKA<sub>cat</sub>(Mg<sup>2+</sup>) is tightly bound to RI $\alpha$  in the absence of cAMP as experimental results indicate, and thus, we treat the entire complex as molecule 1. Finally, for sake of comparison, we calculated  $B_{23}$  for PKA<sub>cat</sub>(Mg<sup>2+</sup>) and cAMP-free RI $\alpha$  (see Fig. 2). The structures were the same as for the preceding set of calculations, except that molecule 1 only contained chain E or G. All RI $\alpha$  structures started at residue 105 to ensure a fair comparison across the different molecular pairs; the truncated residues, including the dimerization and docking (D/D) domain and part of the linker region, were not resolved in cAMP-bound RI $\alpha$  structures due to disorder.

To facilitate comparison across different molecular pairs, we normalized  $B_{23}$  by its steric component,  $B_{23}^0$ . The latter is dictated by the molecular size. The mean of  $B_{23}/B_{23}^0$  and standard error of the mean for each of the three molecular pairs described in the preceding paragraph are listed in Table I. All of the normalized  $B_{23}$  values are negative, with the PKA<sub>cat</sub>(Mg<sup>2+</sup>)-RI $\alpha$  complex and cAMP-free RI $\alpha$  pair having the least negative value, whereas the PKA<sub>cat</sub>(Mg<sup>2+</sup>) and RI $\alpha$ (cAMP) pair having the most negative value. This contrast matches with the PKA<sub>cat</sub>(Mg<sup>2+</sup>)-RI $\alpha$  complex in the absence of cAMP being a weak-attraction suppressor and PKA<sub>cat</sub>(Mg<sup>2+</sup>) in the presence of cAMP being a strong-attraction promoter for RI $\alpha$  phase separation. Specific binding with RI $\alpha$  prevents PKA<sub>cat</sub>(Mg<sup>2+</sup>) to form strong additional interaction with RI $\alpha$ , thus explaining why the PKA<sub>cat</sub>(Mg<sup>2+</sup>)-RI $\alpha$  complex is a weak-attraction suppressor of RI $\alpha$  phase separation. Indeed, as measured by  $B_{23}/B_{23}^0$ ,

Ionic Strength	Temperature	Molecular Weight A	Molecular Weight B	Net Charge A	Net Charge B	$\nu_s$	$B_{23}^0$	$B_{23}$
(M)	(°C)	(Da)	(Da)	(e)	(e)		( $10^{-4}$ ml.mol.g $^{-2}$ )	( $10^{-4}$ ml.mol.g $^{-2}$ )
0.150	25.00	39207	30631	7	-10	0.140	$1.806 \pm 0.0007$	$-1.684 \pm 0.0363$



[Radial Distribution Data](#); [Residue Interaction Energy](#)

**FIG. 2.** Output from the FMAPB23 server for PKA<sub>cat</sub>(Mg<sup>2+</sup>) (PDB: 6NO7 E) and RI $\alpha$  (PDB: 6NO7 H; with residues up to residue 104 truncated). Along with the calculated results for  $B_{23}^0$  and  $B_{23}$  presented in a table, the output includes plots of (*left panel*) the convergence of  $B_{23}$  as a function of the number of rotations of the probe molecule and (*right panel*) the radial distribution function. The two molecules are labeled as A and B; A is static, whereas B is rotated many times (as specified by “Number of rotations”) to evaluate the integration over  $\Omega$ . Error bars represent standard deviations among the different rotations. The radial distribution function is the Boltzmann factor of the potential of mean force along the distance  $R$  between the two protein molecules. The vertical dashed line in the radial distribution function plot represents the contact distance of two spheres with the same  $B_{23}^0$  value as the two protein molecules. Links to the raw data for the radial distribution function and the residue interaction energy (“Radial Distribution Data” and “Residue Interaction Energy”) are also created on the output page.

nonspecific interactions of PKA<sub>cat</sub>(Mg<sup>2+</sup>) alone with RI $\alpha$  are almost as strong as with RI $\alpha$ (cAMP). Had we not considered the specific binding and hence not used the entire PKA<sub>cat</sub>(Mg<sup>2+</sup>)-RI $\alpha$  complex as molecule 1 in calculating  $B_{23}$  with RI $\alpha$ , we would have concluded PKA<sub>cat</sub>(Mg<sup>2+</sup>) to be a strong-attraction promoter for RI $\alpha$  LLPS, which would have contradicted with experimental results.

We can gain further insight into the effects of intermolecular interactions on LLPS by calculating the second virial coefficient  $B_2$  for each protein molecule using FMAPB2.<sup>7</sup>  $B_2$  results were obtained for PKA<sub>cat</sub>(Mg<sup>2+</sup>) (6NO7 E, 6NO7 G, 3O7L B, 4NTT A, and 4NTT B), cAMP-free RI $\alpha$  (6BYR B, 6BYR D, 6BYS B, 6BYS D, 6BYS F, 6BYS H, 6NO7 B, 6NO7 D, 6NO7 F, and 6NO7 H), RI $\alpha$ (cAMP) (4MX3 A and 4MX3 B), and PKA<sub>cat</sub>(Mg<sup>2+</sup>)-RI $\alpha$  complex (6NO7 EF and 6NO7 GH). The mean and standard error of the mean for the normalized  $B_2$  value, i.e.,  $B_2/B_2^0$ , calculated from the multiple input structures for each protein are listed in Table II. Several observations can be made by comparing the normalized  $B_2$  values against the normalized  $B_{23}$  values. First off,  $B_2/B_2^0$  is

slightly positive for the PKA<sub>cat</sub>(Mg<sup>2+</sup>)-RI $\alpha$  complex, whereas  $B_2/B_2^0$  for either of the two subunits and  $B_{23}/B_{23}^0$  between the subunits are negative. This contrast indicates that residues in the interface of the PKA<sub>cat</sub>(Mg<sup>2+</sup>)-RI $\alpha$  complex make major contributions to the self- and cross-attraction of the subunits, thus corroborating the above statement that “specific binding with RI $\alpha$  prevents PKA<sub>cat</sub>(Mg<sup>2+</sup>) to form strong additional interaction with RI $\alpha$ .” More importantly, it is the relative strengths between self- and cross-interactions that dictate the classification of regulator effects on LLPS.<sup>3</sup> We propose that self- and cross-interactions are captured by  $B_2/B_2^0$  and  $B_{23}/B_{23}^0$ , respectively. For the phase separation of RI $\alpha$ (cAMP) under regulation by PKA<sub>cat</sub>(Mg<sup>2+</sup>), the relevant  $B_2/B_2^0$  [for RI $\alpha$ (cAMP)] is  $-0.480$ , whereas the relevant  $B_{23}/B_{23}^0$  [between PKA<sub>cat</sub>(Mg<sup>2+</sup>) and RI $\alpha$ (cAMP)] is  $-1.002$ . The latter more negative value puts PKA<sub>cat</sub>(Mg<sup>2+</sup>) in the category of strong-attraction promoter. In contrast, for the phase separation of RI $\alpha$  under regulation by PKA<sub>cat</sub>(Mg<sup>2+</sup>)-RI $\alpha$ , the relevant  $B_2/B_2^0$  (for RI $\alpha$ ) is  $-0.467$ , whereas the relevant  $B_{23}/B_{23}^0$

**TABLE I.**  $B_{23}$  results.

Molecule no. 1	Molecule no. 2	$B_{23}/B_{23}^0$
PKA <sub>cat</sub> (Mg <sup>2+</sup> )-RI $\alpha$	RI $\alpha$	$-0.321 \pm 0.038$
PKA <sub>cat</sub> (Mg <sup>2+</sup> )	RI $\alpha$ (cAMP)	$-1.002 \pm 0.029$
PKA <sub>cat</sub> (Mg <sup>2+</sup> )	RI $\alpha$	$-0.978 \pm 0.031$

**TABLE II.**  $B_2$  results.

Molecule	$B_2/B_2^0$
PKA <sub>cat</sub> (Mg <sup>2+</sup> )	$-0.583 \pm 0.127$
RI $\alpha$	$-0.467 \pm 0.038$
RI $\alpha$ (cAMP)	$-0.480 \pm 0.143$
PKA <sub>cat</sub> (Mg <sup>2+</sup> )-RI $\alpha$	$0.078 \pm 0.011$

[between  $\text{PKA}_{\text{cat}}(\text{Mg}^{2+})\text{-RI}\alpha$  and  $\text{RI}\alpha$ ] is  $-0.321$ . The latter less negative value puts  $\text{PKA}_{\text{cat}}(\text{Mg}^{2+})\text{-RI}\alpha$  in the category of weak-attraction suppressor.

In addition to the final  $B_{23}$ , the intermediate results of FMAPB23 can also be used to determine residue-level decomposition of interaction energies. From the billions of intermolecular poses sampled in a typical FMAPB23 calculation, we collected the 1000 configurations with the lowest intermolecular interaction energies. The contributions of individual residues to the interaction energies were then averaged over the 1000 selected poses. The results are illustrated in Fig. 3 for the cross-interaction between  $\text{PKA}_{\text{cat}}(\text{Mg}^{2+})$  and cAMP-free  $\text{RI}\alpha$ . Confirming the foregoing conclusion that residues in the interface of the  $\text{PKA}_{\text{cat}}(\text{Mg}^{2+})\text{-RI}\alpha$  complex make major contributions to the cross attraction of the subunits, four of the top five  $\text{PKA}_{\text{cat}}(\text{Mg}^{2+})$  contributors (Lys192, Arg194, Trp196, and Lys213) and three of the top five  $\text{RI}\alpha$  contributors (Glu168, Tyr205, and Arg355) are interface residues. The residue-level contributions to the self-interaction energy of cAMP-free  $\text{RI}\alpha$  are shown in Fig. 4. This time, all of the experimentally resolved residues in cAMP-free  $\text{RI}\alpha$  are used (6BYR B, 6BYR D, 6BYS B,

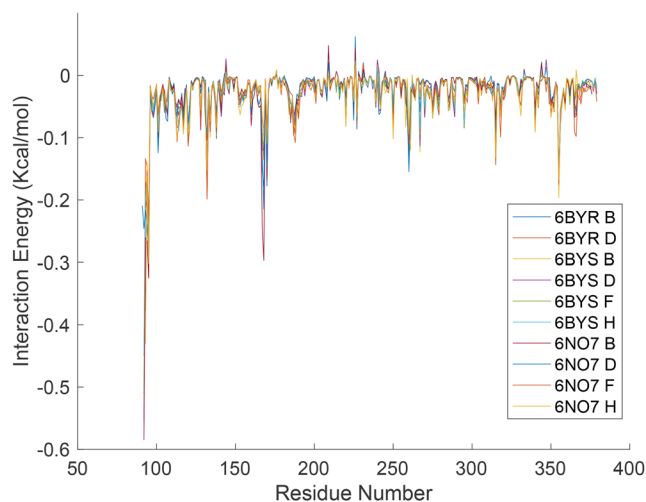
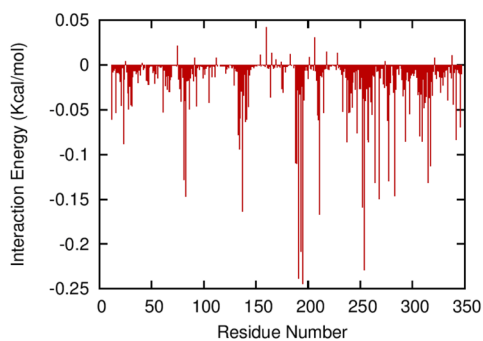


FIG. 4. Residue-level decomposition of the self-interaction energy for PKA  $\text{RI}\alpha$ . The legend indicates the PDB files used as input.

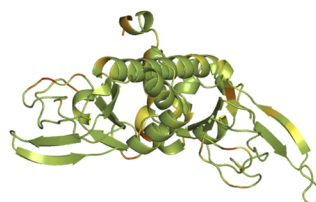
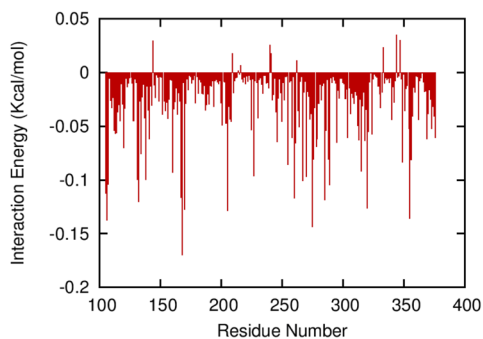
## Residue Interaction Energy

### subA



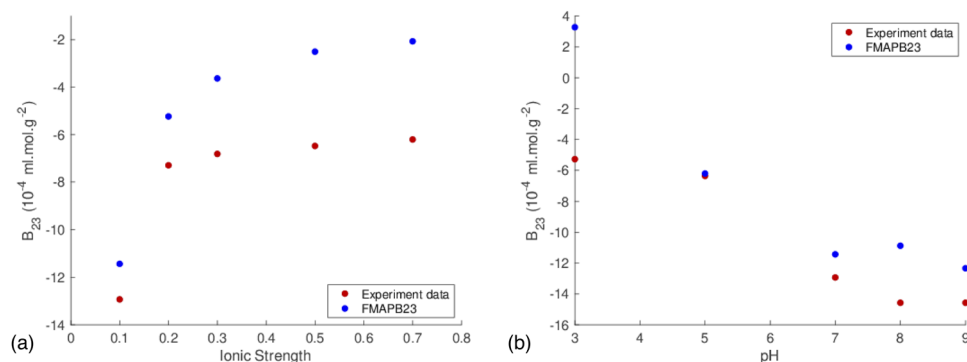
[Residue Interaction Energy](#); same information presented in the B-factor column of a PDB file.

### subB



[Residue Interaction Energy](#); same information presented in the B-factor column of a PDB file.

FIG. 3. Residue interaction energy output from FMAPB23 for  $\text{PKA}_{\text{cat}}(\text{Mg}^{2+})$  (6NO7 E; subA) and cAMP-free  $\text{RI}\alpha$  (6NO7 H with residues truncated up to residue 104; subB). The results are plotted as a bar graph and also displayed on a structure, with green, yellow, and red showing small, medium, and large contributions, respectively. Links to the raw data (“Residue Interaction Energy” and “same information presented in the B-factor column of a PDB file”) are also created on the output page.



**FIG. 5.** Calculated  $B_{23}$  values by FMAPB23 vs experimental data for the BSA-lysozyme system. (a)  $B_{23}$  values at different ionic strengths (NaCl concentrations in M), 25 °C, and pH 7.0. (b)  $B_{23}$  values at different pHs, 25 °C, and 0.1 M NaCl concentration.

6BYS D, 6BYS F, 6BYS H, 6NO7 B, 6NO7 D, 6NO7 F, and 6NO7 H), including the linker residues before residue 105. Note that disorder-prone residues in the linker region make the greatest contributions to the RI $\alpha$  self-interaction energy, even more than the other interface residues (Lys132, Glu168, Trp260, and Arg355). This linker region was indeed found to be important for RI $\alpha$  LLPS.<sup>2</sup>

Finally,  $B_{23}$  calculated by FMAPB23 can be directly compared against experimental measurements. The calculated results for the bovine serum albumin (BSA)-lysozyme pair at different ionic strengths and at different pHs are shown in Figs. 5(a) and 5(b), respectively, along with the corresponding experimental data.<sup>11</sup> Although the calculated and experimental values do not match up exactly, the trends do match up quite well. These results showcase the utility of the FMAPB23 program to study protein-protein non-specific interactions. Importantly, our results suggest that interaction energies between RI $\alpha$  and PKA<sub>cat</sub>, in the presence and absence of cAMP, can explain the unique properties of RI $\alpha$  LLPS. Overall, this study demonstrates how computational modeling can give insight into complex protein assemblies, such as phase-separated protein droplets.

FMAPB23 is available as a web server at <http://pipe.rcc.fsu.edu/fmapb23>, and FMAPB2 is available as a web server at <http://pipe.rcc.fsu.edu/fmapb2>.

S.-H.A. and S.Q. contributed equally to this work.

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## DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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