Lawrence Berkeley National Laboratory

LBL Publications

Title

Intruder configurations of excited states in the neutron-rich isotopes P33 and P34

Permalink

https://escholarship.org/uc/item/11p3x7fd

Journal

Physical Review C, 97(4)

ISSN

2469-9985

Authors

Lubna, RS Tripathi, Vandana Tabor, SL et al.

Publication Date

2018-04-01

DOI

10.1103/physrevc.97.044312

Peer reviewed

Intruder configurations of excited states in the neutron-rich isotopes ³³P and ³⁴P

R. S. Lubna,* Vandana Tripathi, S. L. Tabor, P.-L. Tai, K. Kravvaris, P. C. Bender,† and A. Volya Department of Physics, Florida State University, Tallahassee, Florida 32306, USA

M. Bouhelal

Laboratoire de Physique Appliquée et Théorique, Université Labri Tébessa, Tébessa, Algeria

C. J. Chiara[‡]

Argonne National Laboratory, Argonne, Illinois 50439, USA and Chemistry and Biochemistry, University of Maryland, College Park, Maryland 20742, USA

M. P. Carpenter, R. V. F. Janssens, T. Lauritsen, E. A. McCutchan, and S. Zhu *Argonne National Laboratory, Argonne, Illinois 50439, USA*

R. M. Clark, P. Fallon, A. O. Macchiavelli, S. Paschalis, and M. Petri Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA

W. Reviol and D. G. Sarantites

Chemistry Department, Washington University, St. Louis, Missouri 63130, USA

(Received 9 August 2017; revised manuscript received 27 November 2017; published 16 April 2018)

Excited states in the neutron-rich isotopes ^{33}P and ^{34}P were populated by the $^{18}O+^{18}O$ fusion-evaporation reaction at $E_{\rm lab}=24$ MeV. The Gammasphere array was used along with the Microball particle detector array to detect γ transitions in coincidence with the charged particles emitted from the compound nucleus ^{36}S . The use of Microball enabled the selection of the proton emission channel. It also helped in determining the exact position and energy of the emitted proton; this was later employed in kinematic Doppler corrections. 16 new transitions and 13 new states were observed in ^{33}P and 21 γ rays and 20 energy levels were observed in ^{34}P for the first time. The nearly 4π geometry of Gammasphere allowed the measurement of γ -ray angular distributions leading to spin assignments for many states. The experimental observations for both isotopes were interpreted with the help of shell-model calculations using the $(0+1)\hbar\omega$ PSDPF interaction. The calculations accounted for both the 0p-0h and 1p-1h states reasonably well and indicated that 2p-2h excitations might dominate the higher-spin configurations in both ^{33}P and ^{34}P .

DOI: 10.1103/PhysRevC.97.044312

I. INTRODUCTION

In recent years, the structure of nuclei in the vicinity of the island of inversion has attracted experimental attention in order to untangle the properties of the intruder configuration(s). Phosphorus isotopes, with Z=15 and neutrons occupying the upper sd shell, are of considerable interest in this regard as they exhibit an interplay between normal and intruder shell structure at low excitation energies: this can be informative to understand the evolution of shell gaps with a gradual increase in neutron number. Two phosphorus isotopes, odd-mass ^{34}P and even-mass ^{34}P , have been chosen in the present work to

contribute to the understanding of the upper sd shell nuclei and their intruder configurations.

Numerous studies have previously been conducted on ³³P including β decay of ³³Si [1,2] and particle-transfer reactions like (α, p) , (t, p), and $(d, {}^{3}\text{He})$ [3–15] to study the excited states. Currie et al. [3] observed the first three levels for the first time by means of the ${}^{30}\mathrm{Si}(\alpha, p){}^{33}\mathrm{P}$ reaction. Later, Moss et al. [13] assigned spins to those states. Berkowitz et al. [8] and Davis et al. [12] extended the level scheme up to 6.56 MeV and 10.12 MeV, respectively. The mean lifetimes for the first two excited states were measured first by Currie et al. [6] by means of the Doppler shift attenuation method (DSAM) using the (α, p) reaction. Further lifetime analyses had been performed later by Carr et al. [10] using (α, p) reaction and also by Poletti et al. [16] and Wagner et al. [17] using the $(t, p\gamma)$ reaction employing the DSAM method. The fusion-evaporation reactions $^{18}O(^{18}O, p2n\gamma)^{33}P$ [18] and 26 Mg(13 C, $pn\alpha$) 33 P [19] were conducted recently in order to study higher-energy and higher-spin states.

^{*}Corresponding author: rebeka.sultana.00@gmail.com

[†]Present address: Physics and Applied Physics, University of Massachusetts, Lowell, Massachusetts 01854 USA.

[‡]Present address: US Army Research Laboratory, Adelphi, Maryland 20783, USA.

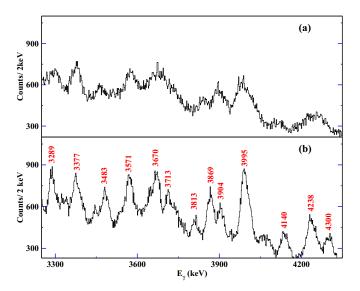


FIG. 1. Comparison between portions of two spectra in coincidence with protons and 429-keV γ rays in ^{34}P illustrating the power of kinematic reconstruction in improving the resolution; (a) and (b) Doppler corrected spectrum before and after kinematic reconstruction, respectively.

Most of the previous experimental works on ^{34}P have been summarized in Refs. [20] and [21]. A binary grazing reaction was conducted by Chapman *et al.* [22] to populate the excited states of ^{34}P , where they verified most of the previous transitions and states and compared them with PSDPF shell model calculations. The same data set as the one used in the current work had been used to study ^{34}P in Ref. [21]. The improved analysis with the kinematic Doppler correction of ^{33}P encouraged us also to re-examine ^{34}P and this proved productive. A number of new γ transitions and states has been observed, and spin assignments to some states have been proposed.

This paper is devoted to the experimental investigation and the understanding of excited states of ^{33}P and ^{34}P with the help of shell-model calculations. The use of large γ and particle detector arrays along with the heavy-ion beam offered a powerful tool to study the structure of these two sd shell nuclei and the associated intruder configurations. The experimental details relevant for this work are presented in Sec. II. The results and data analyses are discussed in Sec. III. Finally, the experimental results were compared to large-scale shell-model calculations in Sec. IV, while Sec. V presents a summary of the work.

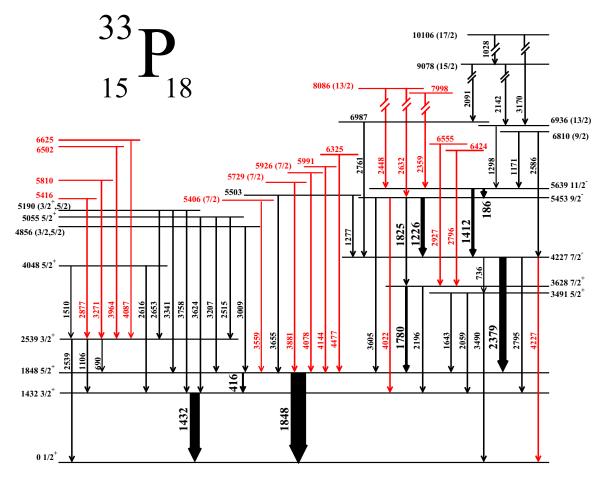


FIG. 2. The level scheme of 33 P established from the current analysis. States and transitions in red (gray) have been observed for the first time. The spins in the figure are from the current analysis and also from the literature. The arrow widths are proportional to the relative intensities of the γ -ray transitions. Those with less than 5% intensity are drawn with the same width.

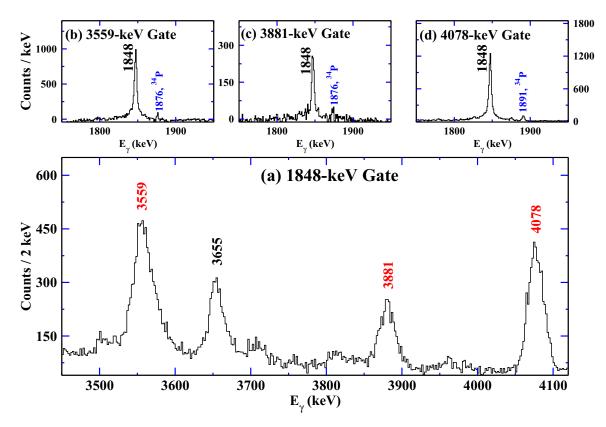


FIG. 3. Coincident spectra showing some γ transitions in ³³P. (a) 1848 gate, the newly observed γ peaks are labeled in red (gray) whereas the previously observed ones are labeled in black. (b) 3559 keV, (c) 3881 keV, and (d) 4078 keV gates, showing the reverse coincidence. The very strong ³⁴P line appears weakly in the broad high energy ³³P gates because of overlaps from broad lines in ³⁴P. ³³P and ³⁴P result from *pn* and 2*pn* evaporation and are not separated by the proton detection.

II. EXPERIMENTAL DETAILS AND PROCEDURES

Excited states in 33 P and 34 P were populated in reactions of 18 O ions, accelerated to 24 MeV by the ANL ATLAS accelerator, incident onto an 18 O target. A target layer of $260\,\mu\text{g/cm}^2$ thickness was prepared by the electrolysis of water enriched to 97% in 18 O, backed by a 12.7 μ m tantalum (Ta) foil.

The de-exciting γ rays were detected by Gammasphere [23], which consisted of 101 Compton-suppressed HPGe detectors arranged in 16 rings, each corresponding to a constant polar angle θ with respect to the beam axis. In the Gammasphere cavity, the nearly 4π detector Microball [24], an array of 95 CsI(Tl) scintillators, was installed to detect and identify protons and other evaporated light charged particles.

A 152 Eu source has been used in order to perform the energy calibration, which was verified later by using peaks with higher energies from room background and induced activities. The calibration remained very linear up to 4122.5 keV with deviations of less than 0.2 keV. Events were selected offline, in which exactly one proton was detected. The correlated γ rays were sorted into γ - γ coincidence matrices of various types (see below). As the neutrons were not detected, new transitions in 33 P and 34 P were assigned by their coincidence relationships with known γ rays. The energies and approximate angles with respect to the beam axis of the recoiling evaporation-residue nuclei were determined event-by-event by a kinematic reconstruction procedure using the measured proton energies

and angles [25]. This information was subsequently used to improve the Doppler-shift corrections of the γ -ray energies, where applicable. This procedure significantly improved the energy resolution of the γ spectra even though the effect on the recoil angle by the evaporated neutron(s) could not be included in the reconstruction. Figure 1 illustrates how much the energy resolution was improved, and, hence, the importance of the reanalysis of ³⁴P after the kinematic reconstruction.

Another issue in the analysis was introduced by the thick target backing. Decays from the long-lived states occurred after the residual nucleus had come to rest (no Doppler shift), while transitions from shorter-lived states were nearly fully shifted. To make full use of the data, three types of proton-gated γ - γ matrices were produced from the data without any or only one axis or both axes Doppler corrected.

The nearly 4π geometry of Gammasphere provided the ability to measure angular distributions for many of the transitions seen in the present work. The angular distribution analysis was performed with the data sorted into asymmetric coincidence matrices, which contained the γ energies recorded in a set of detectors in an individual ring along one axis, and the energies deposited in all other detectors along the other axis. The γ intensities were normalized based on a 152 Eu source. In the analysis, the magnetic substate distribution of the initial state was treated as a Gaussian distribution with a width $\sigma = 1.4$. This parameter value was kept constant for all the states, following the argument presented by Taras *et al.* [26].

TABLE I. Observed excitation energies and spins together with the associated transitions and their relative intensities for levels in ³³P. The spins which could not be measured in the current analysis are not listed in this table. The new states and transitions are shown in boldface (normal text).

E_x (keV)	J^{π}	E_{γ} (keV)	I_{γ}
1431.8 (4)	3/2+	1431.8 (4)	64.2 (1)
1847.8 (4)	5/2 ⁺	1847.8 (4)	100.0 (1)
1017.0 (1)	3/2	416.0 (4)	13.0 (1)
2538.8 (11)		2539.2 (20)	5.2 (1)
2550.0 (11)		1106.4 (15)	2.1 (1)
		690.4 (10)	1.6 (2)
3490.7 (11)	5/2+	3490.4 (14)	0.3 (2)
3470.7 (11)	3/2	2058.7 (12)	1.2 (2)
		1643.2 (10)	2.3 (3)
3627.9 (14)	7/2+	2196.3 (15)	13.5 (4)
3027.7 (14)	1/2	1779.9 (13)	7.3 (7)
4048.3 (21)	5/2+	2616.2 (21)	7.1 (1)
4046.3 (21)	3/2	1509.9 (19)	0.4 (1)
4226.6 (10)	7/2-	4227.0 (15)	0.4 (1)
4220.0 (10)	1/2	2794.6 (13)	0.4 (1)
		2378.6 (9)	47.3 (4)
		* *	
1856 3 (25)		735.9 (5) 3008.5 (25)	4.4 (3)
4856.3 (25)	5 /2+		2.4 (3)
5054.5 (23)	5/2+	3623.8 (26)	1.3 (2)
		3206.5 (25)	2.5 (2)
£190.7 (22)		2514.7 (20)	0.3 (1)
5189.7 (23)		3757.8 (25)	1.4 (3)
		3340.9 (28)	0.8 (3)
540 < 4 (35)	(7.10)	2652.8 (20)	0.3 (1)
5406.4 (25) 5415.9 (29)	(7/2)	3558.6 (25)	4.1 (5)
5415.8 (28)	0.72-	2877.0 (26)	0.4 (1)
5452.8 (12)	$9/2^{-}$	4021.6 (17)	0.2 (1)
		3605.1 (16)	0.4 (1)
		1825.4 (8)	2.4 (1)
5502 1 (21)		1226.4 (6)	27.5 (3)
5503.1 (21)		3655.3 (25)	1.3 (3)
5600 0 (10)	11./0-	1276.7 (18)	1.0 (2)
5638.8 (12)	$11/2^{-}$	1412.2 (7)	20.7 (3)
5500 ((05)	(7.10)	185.9 (8)	15.9 (2)
5728.6 (25)	(7/2)	3880.8 (25)	1.4 (3)
5810.1 (28)	(7.10)	3271.3 (26)	0.10 (5)
5925.6 (26)	(7/2)	4077.8 (26)	3.0 (2)
5991.4 (30)		4143.6 (30)	0.7 (3)
6324.9 (30)		4477.1 (30)	0.8 (3)
6423.7 (27)		2795.8 (23)	2.3 (5)
6502.4 (30)		3963.6 (28)	0.10 (5)
6555.3 (28)		2927.4 (24)	1.2 (3)
6625.3 (30)	(0.10)	4086.5 (28)	0.2 (2)
6809.9 (27)	(9/2)	2586.2 (30)	0.8 (3)
(02(1/22)	(10.10)	1170.9 (24)	1.0 (4)
6936.4 (22)	(13/2)	1297.6 (18)	4.6 (2)
6987.4 (21)		2760.8 (19)	0.4 (2)
7998.0 (23)	(12.12)	2359.2 (20)	0.4 (2)
8086.3 (25)	(13/2)	2632.0 (24)	0.6 (3)
00=0 0 45=:		2448.0 (22)	1.0 (3)
9078.3 (27)		2142.0 (17)	0.2 (1)
10106 4 (20)		2090.7 (15)	0.10 (5)
10106.4 (29)		3170.3 (19)	0.2 (1)
		1027.6 (13)	0.7 (3)

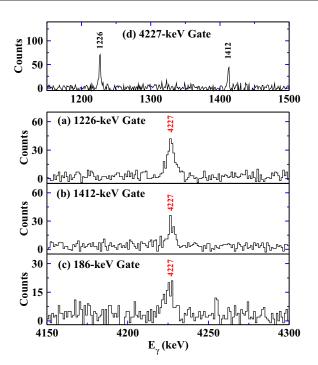


FIG. 4. Coincidence spectra confirming the placement of the 4227-keV transition in 33 P; (Top) the gate is on the 4227-keV γ ray itself, (a–c) gates on three transitions in coincidence with the 4227-keV line. Note the change in energy scale between the top spectrum and the three others.

Theoretical angular distributions were calculated using the code AD [27] as a function of spin hypotheses and mixing ratios δ using the formalism of Rose and Brink [28]. The goodness of fit χ^2 was measured as a function of possible mixing ratios ranging from minus to plus infinity for different spin hypotheses. All the fits from the angular distribution whose goodness of fit χ^2 were below the 0.1% confidence limit were considered to be acceptable, except for E2 decay hypotheses where only $\chi^2 < 0.1\%$ for $\delta = 0$ was considered acceptable.

III. RESULTS AND ANALYSES

Prior to this work, an experiment was conducted by Chakrabarti *et al.* [18] using the same reaction to study both ³³P and ³⁴P. In that work, five clover detectors with no particle detector were used. As stated above, the use of Microball in the current measurement enabled us to perform a kinematic Doppler correction, and achieved better energy resolution of the fast transitions. Gammasphere being an array of large number of detectors offered better event statistics as well. A number of new lines and states were thus added in both isotopes. The level schemes were updated and extended, and spin assignments to some states are proposed.

A. ³³P

Figure 2 presents the level scheme of 33 P constructed in the current work. Most of the previously reported transitions and states have been confirmed, and 16 new γ transitions and 13 new states have been observed: these are all marked in red

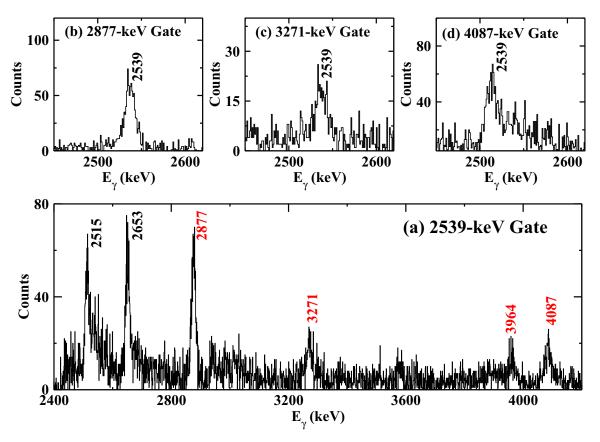


FIG. 5. Coincident spectra showing some transitions in (a) the 2539-keV gate in the Doppler-corrected matrix of 33 P. The newly observed γ lines are labeled in red, whereas the previously observed ones are labeled in black; (b) 2877-keV, (c) 3271-keV, and (d) 4087-keV gates, showing the reverse coincidence relationships.

(gray). In a recently published paper [19], 33 P was studied with the fusion-evaporation reaction 26 Mg(13 C, $np\alpha$) 33 P, where the level scheme was extended up to 10106-keV excitation energy. In the present work, a number of new states which decay to the 1848- and 2539-keV levels were observed for the first time, in addition to the levels reported in [19]. The level energies along with the corresponding transitions, spins, parities, and relative intensities are summarized in Table I.

Some examples of the newly observed γ transitions are given in Fig. 3. The spectrum in panel (a) was gated on the 1848-keV γ line from the non-Doppler corrected axis of the γ - γ matrix projecting onto the Doppler corrected one. The spectra in parts (b) through (d) were gated by some of the individual peaks in panel (a) and demonstrate the clear presence of the 1848-keV peak in spectra with no Doppler correction.

Two new γ transitions at 4022- and 4227-keV were observed in the decays of previously reported states at 5453 (9/2⁻) and 4227 (7/2⁻) keV, respectively. According to the assigned spins of the parent and the daughter states, both the transitions are of E3 character which is less common. The coincidence spectra confirming the placement of the 4227 transition are presented in Fig. 4.

Two new states at 6424 and 6555 keV were established by observing the transitions at 2796 and 2927 keV, decaying to the 3628-keV level. It should be pointed out that the 2796-keV transition is a doublet with the previously known 2795-keV

line which feeds the 1432-keV state. This was confirmed by the observation of narrow lines at 2795 keV in the 1226-, 1412-, and 1432-keV coincidence gates and broader lines at a similar energy in the 1780-, 1848-, and 2196-keV ones.

A state at 6807 keV was established by Fu *et al.* [19] through the observation of two γ transitions at 1168 and 2581 keV. These transitions are confirmed in the present work, although with slightly higher energies of 1171 and 2586 keV, suggesting an energy of 6810 keV for the parent state. Both of the transitions involved are fully Doppler shifted, and were observed in different gates of the Doppler corrected matrix.

The coincidence spectrum obtained by gating on the well-established 2539-keV transition while projecting on the Doppler-corrected axis has confirmed the previously observed γ rays at 1510, 2515, and 2653 keV and revealed new lines at energies of 2877, 3271, 3964, and 4087 keV, as shown in Fig. 5. These new transitions give rise to the new states at 5416, 5810, 6502, and 6625 keV, respectively. A state at 5410 keV with two decay branches to the 1848- and 2539-keV levels was reported [15] based on a $(t, p\gamma)$ measurement using NaI scintillators. Almost simultaneously, the same group published another $(t, p\gamma)$ measurement [16] using a small volume Ge(Li) detector which provided higher-energy resolution, but lower efficiency than the NaI scintillator. Only the stronger decay branch was reported in that paper with an energy of 3557.4 (28) keV. In the present Gammasphere experiment, both decays

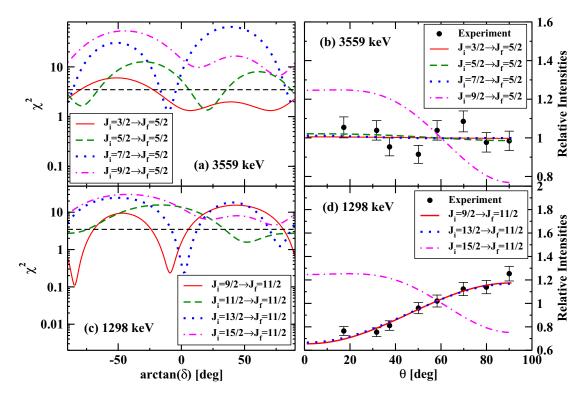


FIG. 6. (a), (c) χ^2 fits to the measured angular distribution for different spin hypotheses are plotted as function of mixing ratio, δ , for γ transitions in 33 P indicated in the panels. (b), (d) Angular distributions of 3559 and 1298-keV transitions for different spin hypotheses.

are observed, but their energies suggest two states at 5406 and 5416 keV. A single state solution can not be completely ruled out, but is less likely.

An interesting pattern appears in the widths of γ rays from the states above 5 MeV. The lines from the 5453 and 5639 keV levels are narrow, e.g., consistent with the reported [11] mean lifetimes of 24 and 9.7 ps. However most of the γ rays from the levels above this energy are broad and clearly visible only after implementation of the kinematic Doppler correction. But the transitions from the highest two states observed at 9078 and 10106 keV are narrow, exhibiting no Doppler shift. This could signify a different configuration for the highest energy state at 10106 keV, whose slow decay results in a narrow gamma peak from the 9078 keV level.

Some examples of angular distributions and fits are presented in Fig. 6. The χ^2 fit for the 3559-keV line de-exciting the 5406-keV state, to the $5/2^+$, 1848-keV level is consistent with $\Delta J=1$ or 0, but not $\Delta J=2$ decay. The tendency of fusion-evaporation reaction to populate higher-lying high-spin states suggests spin of 7/2 for the state. Positive parity is likely since they decay to a positive-parity level, rather than to the 4227-keV, $7/2^-$ state.

The 6936-keV state was first reported by Chakrabarti *et al.* [18] through the observation of a 1298-keV γ ray, which they reported to be of quadrupole character, and assigned spin 15/2 to this level. However, Fu *et al.* [19] have shown the transition to be of dipole character by employing the $\gamma\gamma$ angular correlation method, hence, suggesting spin 9/2 or 13/2. In the current study, the angular distribution of the 1298-keV line clearly ruled out a $\Delta J=2$ transition [Figs. 6(c) and 6(d)] favoring

a $\Delta J = 1$ multipolarity instead. From the χ^2 fit, it can be seen that both spins 9/2 and 13/2 are equally acceptable. The tendency of fusion-evaporation reactions to favor higher-spin states makes a 13/2 assignment more likely.

B. 34 P

Results for ³⁴P from an earlier analysis of the same data set were published in Ref. [21]. In the present analysis, the Doppler correction has been improved by kinematic reconstruction, as displayed in Fig. 1. As a result, 20 additional excited states have been discovered. The level scheme, presented in Fig. 7, displays all the known states along with the decay paths of the newly discovered ones which are marked in red (gray). It is worth mentioning that all the new transitions were observed while gating around a narrow peak and projecting onto the Doppler corrected axis of the matrix, implying that the new states are short lived. The level energies of the new states, along with the corresponding transitions, spins, parities and relative intensities are summarized in Table II.

Most of the new states were observed to decay to the lowest 3^- , 4^- , and 5^- levels, although three decays proceed directly to the 2^+ level at 429 keV. Many of these transitions can be seen in the portion of the γ spectrum in coincidence with the 429-keV line of Fig. 1(b). The coincidence relations have been confirmed by gating on the new γ rays, examples of which are presented in Figs. 8(a) and 8(b). In the earlier analysis [21], a transition at 2960 keV was reported and placed on the top of the 2321-keV state. However, with the improved Doppler-corrected spectra, it is clear that the

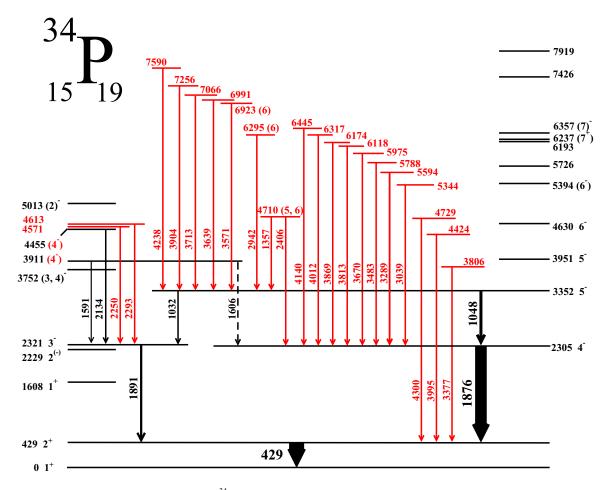


FIG. 7. The proposed, updated, level scheme of ^{34}P constructed from the present analysis. The newly observed states and transitions are marked in red (gray). The spins in the figure are from the current analysis and also from the literature. The arrow widths are proportional to the γ emission relative intensities. The transitions that were observed in the earlier analysis (see Fig. 1 in Ref. [21]) from the same data set, but not in coincidence with the newly observed transitions, are also verified, but not shown here for simplicity. Transitions with less than 5% intensity are drawn with the same width.

transition energy is 2942 keV, and decaying into the 3352-keV state instead (Fig. 9). Also with the better resolution after kinematic Doppler-correction, we could not confirm 2828 keV transition observed in Ref. [21], and hence decided not to include this transition and the corresponding level at 6180 keV in our updated level scheme. The level at 4447 keV was updated as 4455 keV with the improved resolution.

 χ^2 graphs of the measured angular distributions for transitions at 1357, 3571, 2134 keV are compared as functions of the mixing ratio δ for several possible spin sequences in Fig. 10. The corresponding angular distributions have also been presented. The χ^2 fits rule out $\Delta J=2$ transitions for the 1357 and 3571 keV lines, which is also reflected in the corresponding angular distributions. This, along with the fact that fusion evaporation reactions favor higher spin states, suggests that J=6 is most likely for the 4710 and 6923 keV states. The angular distribution of the 2134 keV line is consistent with the previous suggestion of $J=(4^-)$, but does not rule out J=3 by itself.

IV. SHELL-MODEL CALCULATIONS AND DISCUSSION

The experimental results have been compared to theoretical predictions generated by shell-model calculations using the code COSMO [29]. The PSDPF interaction of Ref. [30], developed in the p-sd-pf model space outside a closed 4 He core, has been used to interpret the available data. The interaction enabled us to calculate not only the $0\hbar\omega$ excitations, but also the $1\hbar\omega$ ones which include both the lower 0p and upper fp shells. A key question is whether enough states with quantum number consistent with the energy and decay patterns are predicted to account for the newly observed states as well as the previously reported ones. Tables III and IV answer this question in the affirmative. There is at least one good theoretical candidate for each experimental state. We emphasize that this correspondence is not always unique and should not be considered firm.

Configurations associated with the lower-energy, positiveparity states of ³³P involve the valence nucleons confined to

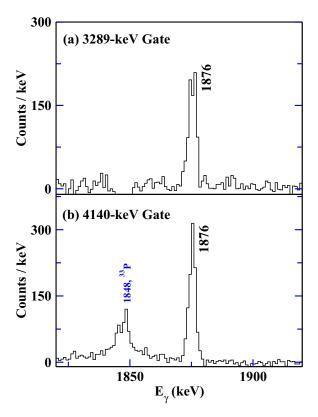


FIG. 8. Confirmation of the coincidence relationship of some newly assigned γ rays in ³⁴P, observed in the 429-keV gate projected on the Doppler-corrected axis in Fig. 1(b). One of the strongest ³³P lines appears weakly in (b), because of the overlap of 4144-keV line in ³³P with the 4140-keV one.

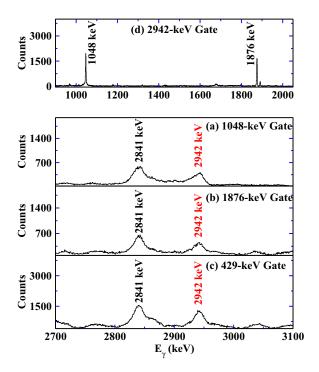


FIG. 9. (a) 1048-, (b) 1876-, and (c) 429-keV gates showing the new position of the 2942-keV transition in 34 P. (d) 2942-keV gate illustrating the consistency in coincidence relations.

TABLE II. Observed excitation energies and spins together with the associated transitions and their relative intensities for levels in ³⁴P. The spins which could not be measured in the current analysis are not listed in this table. The new states and transitions are shown in boldface (normal text). States above 3352 keV that were observed in Ref [21] and verified in the present work are not shown in the table.

E_x (keV)	J^π	E_{γ} (keV)	I_{γ}
429.1 (4)	2+	429.1 (4)	100.0 (1)
2304.9 (6)	4^{-}	1875.8 (6)	77.7 (1)
2320.6 (7)	3-	1891.5 (7)	12.2(1)
3352.4 (10)	5-	1047.3 (8)	20.2(1)
		1031.6 (9)	0.64(2)
3806.3 (26)		3377.2 (26)	1.2 (2)
4424.0 (27)		3994.9 (27)	4.7 (2)
4570.7 (21)		2250.1 (20)	1.0(3)
4613.1 (22)		2292.5 (21)	0.8 (2)
4710.0 (21)	(6)	2405.5 (20)	6.3 (3)
		1356.9 (23)	2.1 (7)
4729.3 (30)		4300.2 (30)	0.5 (2)
5344.2 (29)		3039.3 (28)	2.6 (6)
5594.1 (26)		3289.2 (25)	1.1 (5)
5788.3 (29)		3483.4 (28)	1.1 (8)
5975.3 (30)		3670.4 (29)	1.5 (5)
6118.2 (31)		3813.3 (30)	0.8 (6)
6174.2 (29)		3869.3 (28)	1.3 (3)
6294.6 (24)		2942.2 (21)	4.0 (8)
6316.5 (31)		4011.6 (30)	0.60 (5)
6444.7 (31)		4139.8 (30)	1.3 (8)
6923.0 (28)	(6)	3570.6 (26)	0.60 (9)
6990.9 (30)		3638.5 (28)	0.8 (3)
7065.6 (27)		3713.2 (25)	0.20 (5)
7256.1 (27)		3903.7 (25)	0.30 (5)
7590.4 (33)		4238.0 (31)	1.0 (4)

the sd shell. The positive-parity states up to 4048 keV are in satisfactory agreement with the calculated ones (with $\Delta E \approx$ 150 keV) generated with no particle-hole excitation; i.e., they correspond to $0\hbar\omega$ excitations. Even beyond this energy, the differences between the experiment and theory are less than 300 keV. The newly observed state at 5729 keV matches best with a calculated one at 5912 keV, according to the decay pattern and the suggested spin. Also, the new levels at 6424, 6502, 6555, and 6625 keV can be compared to the calculated ones at 6510, 6364, 6554, and 6536 keV, respectively. Since no angular distribution measurement was possible for the reported states, only excitation energies were considered in order to match data with their theoretical counter parts. Negative-parity states in ³³P can be obtained by promoting one particle from the orbital 0p to the sd shell or from the sd to the fp shell, giving rise to 1p-1h intruder states. The first negative-parity level at 4227 keV was originally reported by Davies et al. [9], where the state was found to be populated by a $\ell=3$ transfer by measuring the proton angular distribution. In that work, spin-parity values of 7/2 were suggested, representing a 1p-1h excitation, although no theoretical counterpart could be calculated at that time. Later, the spin of the state was confirmed to be 7/2 by Harris et al. [7] employing a proton- γ

TABLE III. Possible correspondences between states calculated in the shell model for ^{33}P using the PSDPF interaction and the observed states. The calculation comprises both 0p-0h (positive-parity) and 1p-1h (negative-parity) states. The newly observed experimental states are shown in boldface (normal text). The last column expresses the energy difference between experimental and estimated states (ΔE).

J_i^π	PSDPF (keV)	Exp (keV)	$\Delta E \text{ (keV)}$
3/2+	1441	1432	
$5/2_1^+$	1905	1848	-57
$3/2_{2}^{+}$	2679	2539	-140
$5/2_{2}^{+}$	3508	3491	-17
$7/2_1^+$	3778	3628	-150
$5/2_3^+$	3971	4048	77
$7/2_1^-$	4471	4227	-244
$5/2_4^+$	5012	5055	43
$3/2_4^+$	5075	4856	-219
$5/2_1^-$	5167	5190	23
$9/2_1^+$	5471	5503	32
$5/2_2^-$	5560	5416	-144
$7/2_{2}^{-}$	5639	5406	-233
$9/2_1^-$	5696	5453	-243
$11/2_1^-$	5813	5639	-174
$7/2_2^+$	5912	5729	-183
$5/2_3^-$	5915	5810	-105
$7/2_3^-$	5991	5926	-65
$7/2_4^-$	6135	5991	-144
$7/2_3^+$	6210	6325	115
$3/2_5^+$	6364	6502	138
$9/2_2^+$	6510	6424	-86
$5/2_5^+$	6536	6625	89
$7/2_4^+$	6554	6555	1
$9/2_4^-$	6722	6810	88
$11/2_2^-$	6976	6987	11
$13/2_1^-$	7222	6936	-286
$11/2_4^-$	7850	7998	148
$13/2_2^-$	7991	8086	95
$\frac{15/2_1^-}{}$	9094	9078	-16

angular correlation. Until Fu et al. [19] calculated this level with the PSDPF interaction, no satisfactory description of this state could be achieved. In a naive picture, it can be predicted that this level is formed by the promotion of an unpaired proton from the $1s_{1/2}$ orbital to the $0f_{7/2}$ orbital, giving rise to the $7/2^-$ spin and parity. But the calculations presented here suggest that this state does not correspond to a pure proton excitation, rather, it has a mixed configuration with 32% $vf_{7/2}$ and 46% $\pi f_{7/2}$ occupancy. The observed yrast $9/2^{-}$ and $11/2^{-}$ states at 5453 and 5639 keV, on the other hand, are dominated by a one neutron excitation, according to the calculations. The experimental level at 6936 keV can be compared to the calculated 7222-keV state with a configuration dominated by a one-neutron excitation to the $0 f_{7/2}$ orbital with some rearrangements of the population of nucleons inside the sd shell. The state at 9078 keV was observed by Fu et al. [19] and their $\gamma \gamma$ angular correlation analysis restricted the possible spin to (7/2, 11/2, 15/2). A $15/2^-, 9094$ -keV state was obtained in the calculations and is likely to be the

TABLE IV. Possible correspondences between states calculated in the shell model for ^{34}P using the PSDPF interaction and the observed states. The calculation comprises both 0p-0h (positive-parity) and 1p-1h (negative-parity) states. The newly observed experimental states are shown in boldface (normal text). The last column expresses the energy difference between experimental and estimated states (ΔE).

$\Delta E \text{ (keV)}$	Exp (keV)	PSDPF (keV)	J_i^π
46	429	383	2_{1}^{+} 1_{2}^{+} 2_{1}^{-}
129	1608	1479	12
47	2229	2182	$2\frac{1}{1}$
109	2305	2196	$4^{\frac{1}{1}}$
-33	2321	2354	$3\frac{1}{1}$
23	3352	3329	$5\frac{1}{1}$
28	3752	3724	$\begin{array}{c} 3_1^- \\ 5_1^- \\ 3_2^- \\ 5_2^- \\ 4_3^- \\ 1_4^+ \\ 2_4^+ \\ 4_4^- \\ 3_2^+ \\ 2_7^- \\ 3_6^- \end{array}$
15	3951	3936	$5\frac{2}{2}$
-61	3911	3972	$4\frac{2}{3}$
-248	3806	4054	14
218	4424	4206	2_{4}^{+}
67	4455	4388	$4^{\frac{1}{4}}$
203	4729	4526	$3^{\frac{7}{4}}$
-17	4571	4588	$2^{\frac{2}{7}}$
-71	4613	4684	3-
-145	4630	4775	6_{1}^{-}
-101	4710	4811	5-
-20	5013	5033	2-
115	5344	5219	2 ₈ 5 ₄ 6 ₂ 5 ₅ 6 ₃
-28	5394	5422	$6\frac{1}{2}$
125	5594	5469	$5\frac{2}{5}$
16	5726	5710	$6\frac{1}{2}$
-48	5788	5836	$5\frac{3}{6}$
-18	5975	5993	4_{11}^{-}
-25	6118	6143	412
-98	6174	6272	4_{13}^{-2}
-108	6193	6301	$5^{\frac{13}{7}}$
-14	6357	6371	$7\frac{1}{1}$
-98	6317	6415	5-2
-100	6445	6545	4_{14}^{-}
-328	6295	6623	6_{4}^{-14}
144	6923	6779	6_{5}^{-}
40	6991	6951	$7\frac{3}{2}$
16	7066	7050	$5\frac{2}{10}$
0	7256	7256	$7\frac{10}{3}$
22	7426	7444	6_{7}^{-}
-24	7590	7614	6_{8}^{-}
150	7919	7769	$7\frac{8}{4}$

theoretical counter-part of the observed one. The calculated levels corresponding to the observed negative-parity states, except the first $7/2^-$ state, appear to be mainly associated with a neutron excitation to the fp shell, predominantly to the $0\,f_{7/2}$ orbital.

The nonyrast states at 5406, 5416, 5810, 5926, 5991, 7998, and 8086 keV in ^{33}P observed in the present work did not appear to have theoretical counterparts in calculations with nucleons confined to the sd shell, i.e., limited to $0\hbar\omega$ excitations. Shell-model calculations with the PSDPF interaction could predict these states as $1\hbar\omega$ excitation, where the config-

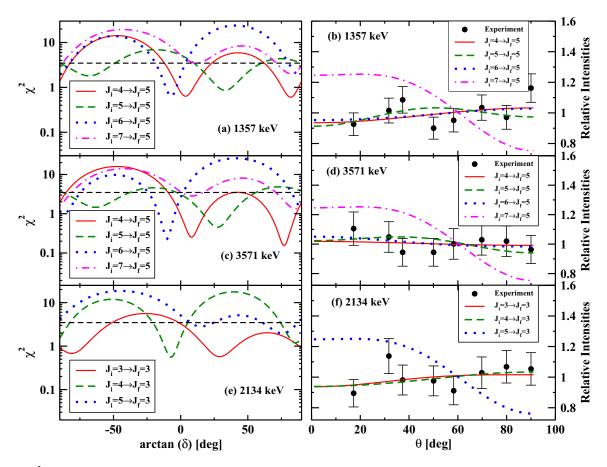


FIG. 10. χ^2 fits to the measured angular distribution for different spin hypotheses are plotted as a function of mixing ratio δ for selected transitions in ³⁴P indicated in the panels. The corresponding angular distributions for different spin hypotheses are plotted alongside.

urations are dominated by one-neutron excitations from the sd to the fp shell.

Figure 11 illustrates the observed yrast negative-parity states and the corresponding PSDPF levels along with the fpshell occupancies for ³³P and nearby odd-mass phosphorus isotopes. It can be seen that the first negative-parity states of all the isotopes are $7/2^-$ levels as expected, and are generated by a mixed proton-neutron excitation from the sd shell. For ^{31}P , an unpaired proton and a pair of neutrons occupy the $0s_{1/2}$ orbital in the ground-state configuration. So, it is expected that the first negative-parity 7/2 state of ³¹P will correspond predominantly to a proton excitation across the sd-pf shell gap. However, shell-model calculations with the PSDPF interaction indicate that the state has almost equal contributions from protons and neutrons. The energy of the level is overestimated by more than 300 keV. This corresponds to the cost of breaking a pair of neutrons and having a significant occupation of the $0 f_{7/2}$ orbital. All other yrast, negative-parity states in ^{31}P are also described by equal contributions of proton and neutron excitations to the fp shell. Unlike ^{31}P , the yrast negative-parity states in ³³P and ³⁵P are dominated by one-neutron excitations to the fp shell, except the first $7/2^-$ level.

The highest observed state at 10106 keV was first reported by Fu *et al.* [19] and is confirmed in the current work. The angular correlation measurement in Ref. [19] restricted

possible spin values to (13/2, 17/2). The shell-model calculations predict two nearby levels at $10554 (13/2^+)$ and 11239(17/2⁻) keV. A 13/2 spin was considered more probable in Ref. [19]. However, the possibility of spin 17/2 cannot be excluded, as an yrast or near-yrast decay sequence should be anticipated when a fusion-evaporation reaction is used, as in the case here, although the first calculated $17/2^-$ state is predicted to lie more than 1 MeV higher. The nearest 0p-0h, $17/2^+$ state computed with the PSDPF interaction is at 14460 keV. This overestimation might be an indication that a $2\hbar\omega$ excitation towards the fp shell needs to be considered. Following the arguments above about the 6936-and 9078-keV states being of 1p-1h character, the 10106-keV level may well correspond to a 2p-2h configuration which decays via the 1p-1h excitations. This would be consistent with the electromagnetic operator being a one body operator. Also, the narrow width of γ transitions emitted from the 10106-keV level indicate a relatively long lifetime for this state and this supports the argument. A similar feature was observed in ³¹P [31], where the experimental $15/2^+$ and $17/2^+$ states at energies 10520and 11297 keV, respectively, could not be explained by $0\hbar\omega$ excitations within calculations with the USD interaction. The use of the SDPF-M interaction [32] described the Op-0h positive-parity states well up to the yrast 13/2⁺ state. This interaction calculated the $15/2^+$ and $17/2^+$ levels as resulting

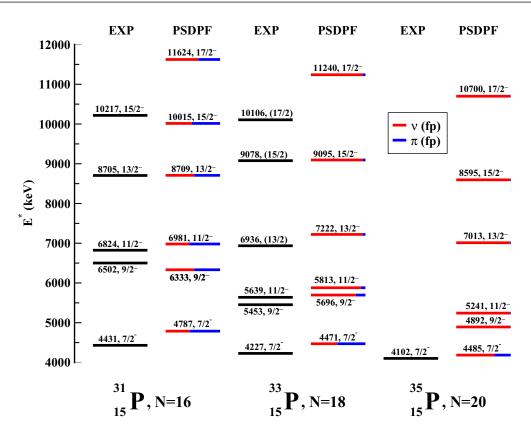


FIG. 11. Experimental negative-parity yrast states and their shell-model counter parts calculated with the PSDPF interaction along with the fp shell occupancy in the odd-mass phosphorus isotopes, ^{31}P , ^{33}P , and ^{35}P . The red (light gray) and blue (dark gray) colors represent neutron and proton fp shell occupancies, respectively.

from the promotion of one proton and one neutron from the sd to the fp shell, and the computed energies of 10230 and 11720 keV, respectively, were close to the observed states. Also, the configuration of the states supported the decay pattern observed in the experiment. With a very similar yrast sequence in 33 P, and considering the features discussed above, the level at 10106 keV is likely to be associated with a 2p-2h intruder state in 33 P. This is, however, beyond the scope of the calculations presented in this paper.

The agreement between theory and experiment in ³³P was the motivation to use the same approach with the PSDPF interaction to describe ³⁴P as well. Again, the spectrum for this isotope is well described with this interaction. In fact, all the experimentally observed states in the present work have a likely PSDPF counterpart (see Table IV), except the state at 6237 keV, which will be discussed later. As in other such nuclei, the positive-parity states are characterized as $0\hbar\omega$ excitations and the negative-parity levels correspond to $1\hbar\omega$ ones, with the PSDPF interaction being limited to only one-particle excitations either from the 0p to the sd shell or from the sd shell to the pf one above it. Though the PSDPF interaction results in a wide range of 0p-0h levels, only a few positive-parity state were observed in earlier work, and those are described satisfactorily. Three new levels were observed here which decay to the first excited state at 429 keV (2⁺). Considering their decay pattern, those are assumed to have positive parity. There are likely positive-parity theoretical counterparts with energy differences of less than 250 keV for them. All other new states decay to the negative-parity levels. Their decay patterns and the angular distribution measured from some transitions suggest that those states are of negative parity and, hence, arise from one-particle excitations from the sd to the fp shell. All the theoretical counter-parts of these states have configurations dominated by neutron excitations, mainly to the $0f_{7/2}$ orbital.

Like for the odd-mass phosphorus nuclei, Fig. 12 depicts the comparison between the experimental and theoretical yrast negative-parity states along with the fp shell occupancies of the even-mass ^{32}P and ^{34}P isotopes. For both nuclei, all the states calculated with the PSDPF interaction, plotted in the picture are mainly associated with a neutron excitation. This is expected as ^{32}P and ^{34}P both have one unpaired proton occupying the $s_{1/2}$ orbital and one unpaired neutron residing in the $d_{3/2}$ one. Being energetically efficient, the excitations of the unpaired neutron across the fp shell are favored and give rise to the negative-parity intruder states.

The state observed at 6237 keV was first reported by Ollier *et al.* [33], where they proposed a stretched 7^+ $\pi(f_{7/2})$ $\nu(f_{7/2})$ configuration. Later, Bender *et al.* [21] verified the energy and the spin of the level using the present data set, and those authors agreed with the previous argument that the level likely corresponds to a 2p-2h intruder, 7^+ excitation. Also, the first 7^+ state in the PSDPF calculation is at 10712 keV, and is a 0p-0h state, i.e., there is no good candidate for the observed state in the present theoretical spectrum, in line with the suggestion of a 2p-2h configuration.

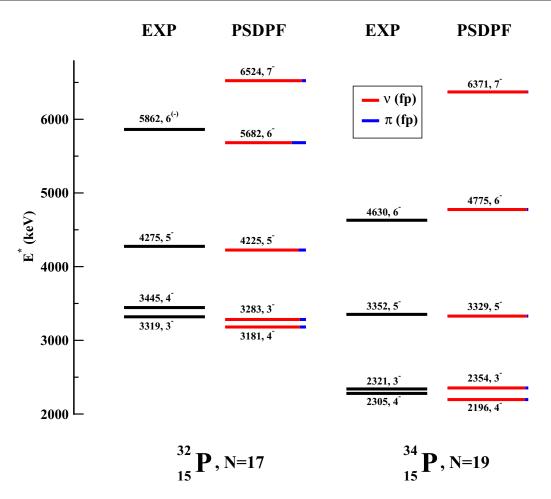


FIG. 12. Experimental negative-parity yrast states and their shell-model counter parts calculated with the PSDPF interaction along with the fp shell occupancy in the even-mass phosphorus isotopes, ^{32}P and ^{34}P . The red (light gray) and blue (dark gray) colors represent neutron and proton fp shell occupancies, respectively.

V. SUMMARY

A detailed investigation of the structure of ^{33}P has been performed using the Gammasphere array combined with the Microball particle detector array. The level scheme of ^{33}P has been extended with the identification of 16 new transitions and 13 new states. The improved Doppler correction achieved by employing kinematic reconstruction of emitted charged particles also encouraged us to reanalyze ^{34}P . This resulted in the addition of 21 new transitions and 20 new levels to the level scheme. Spin assignments for some of the states in both the isotopes have been proposed based on the measured angular distributions of the emitted transitions. Large-scale shell-model calculations using the $(0+1)\hbar\omega$ PSDPF interaction have been performed in order to interpret the results. In both isotopes, these calculations provide good candidates for the observed positive- and negative-parity states. The decay

pattern and the likely long lifetime of a level at 10106 keV is understood as a likely $2\hbar\omega$ configuration in ³³P. A similar feature had been previously proposed in ³⁴P for a level at 6237 keV. In the future $2\hbar\omega$ shell-model calculations would be desirable to better understand the intruder configurations for sd-shell nuclei.

ACKNOWLEDGMENTS

This work was supported by US National Science Foundation under Grant No. NSF 140-1574 and the US Department of Energy Office of Science, Office of Nuclear Physics under Grants No. DE-SC0009883 (FSU), No. DE-AC02-05CH-11231 (LBNL), No. DE-AC02-06CH-1137 (ANL), No. DE-FG02-88ER-40406 (W.U.), and No. DE-FG02-94ER-40834 (UMD). This research used resources of ANL's ATLAS facility, which is a DOE Office of Science User facility.

^[1] D. R. Goosman and D. E. Alburger, Phys. Rev. C 5, 1252 (1972).

^[2] D. R. Goosman, C. N. Davids, and D. E. Alburger, Phys. Rev. C 8, 1324 (1973).

^[3] W. M. Currie and J. E. Evans, Phys. Lett. B 24, 399 (1967).

^[4] R. C. Bearse, D. H. Youngblood, and J. L. Yntema, Phys. Rev. 167, 1043 (1968).

- [5] G. Hardie, R. E. Holland, L. Meyer-Schützmeister, F. T. Kuchnir, and H. Ohnuma, Nucl. Phys. A 134, 673 (1969).
- [6] W. M. Currie, L. G. Earwaker, J. Martin, and A. K. Sen Gupta, Phys. Lett. B 28, 480 (1969).
- [7] W. R. Harris, K. Nagatani, and J. W. Olness, Phys. Rev. C 2, 1412 (1970).
- [8] E. H. Berkowitz, Nucl. Phys. A 140, 173 (1970).
- [9] W. G. Davies, J. C. Hardy, and W. Darcey, Nucl. Phys. A 128, 465 (1969).
- [10] P. E. Carr, D. C. Bailey, J. L. Durell, L. L. Green, A. N. James, J. F. Sharpey-Schafer, and D. A. Viggars, J. Phys. A 6, 685 (1973).
- [11] M. R. Nixon, G. D. Jones, P. R. G. Lornie, A. Nagel, P. J. Nolan, H. G. Price, and P. J. Twin, Nucl. Phys. 1, 430 (1975).
- [12] N. J. Davis and J. M. Nelson, Nucl. Phys. 13, 375 (1987).
- [13] C. E. Moss, R. V. Poore, N. R. Roberson, and D. R. Tilley, Phys. Rev. 174, 1333 (1968).
- [14] S. Khan, G. Mairle, K. T. Knöpfle, Th. Kihm, Liu-Ken Pao, P. Grabmayr, G. J. Wagner, and L. Friedrich, Nucl. Phys. A 481, 253 (1988).
- [15] A. R. Poletti, T. T. Bardin, R. E. McDonald, and J. G. Pronko, Phys. Rev. C 7, 1479 (1973).
- [16] A. R. Poletti, T. T. Bardin, J. G. Pronko, and R. E. McDonald, Phys. Rev. C 7, 1433 (1973).
- [17] P. Wagner, J. P. Coffin, M. A. Ali, D. E. Alburger, and A. Gallmann, Phys. Rev. C 7, 2418 (1973).
- [18] R. Chakrabarti, S. Mukhopadhyay, Krishichayan, A. Chakraborty, A. Ghosh, S. Ray, S. S. Ghugre, A. K. Sinha, L. Chaturvedi, A. Y. Deo, I. Mazumdar, P. K. Joshi, R. Palit, Z. Naik, S. Kumar, N. Madhavan, R. P. Singh, S. Muralithar, B. K. Yogi, and U. Garg, Phys. Rev. C 80, 034326 (2009).
- [19] B. Fu, M. Seidlitz, A. Blazhev, M. Bouhelal, F. Haas, P. Reiter, K. Arnswald, B. Birkenbach, C. Fransen, G. Friessner, A. Hennig, H. Hess, R. Hirsch, L. Lewandowski, D. Schneiders, B. Siebeck, T. Steinbach, T. Thomas, A. Vogt, A. Wendt, K. Wolf, and K. O. Zell, Phys. Rev. C 94, 034318 (2016).
- [20] P. C. Bender, C. R. Hoffman, M. Wiedeking, J. M. Allmond, L. A. Bernstein, J. T. Burke, D. L. Bleuel, R. M. Clark, P. Fallon, B. L. Goldblum, T. A. Hinners, H. B. Jeppeson, S. Lee, I.-Y. Lee, S. R. Lesher, A. O. Macchiavelli, M. A. McMahan, D. Morris, M. Perry, L. Phair, N. D. Scielzo, S. L. Tabor, V. Tripathi, and A. Volya, Phys. Rev. C 80, 014302 (2009).

- [21] P. C. Bender, S. L. Tabor, V. Tripathi, C. R. Hoffman, L. Hamilton, A. Volya, R. M. Clark, P. Fallon, A. O. Macchiavelli, S. Paschalis, M. Petri, M. P. Carpenter, R. V. F. Janssens, T. Lauritsen, E. A. McCutchan, D. Seweryniak, S. Zhu, C. J. Chiara, X. Chen, W. Reviol, D. G. Sarantites, and Y. Toh, Phys. Rev. C 85, 044305 (2012).
- [22] R. Chapman, A. Hodsdon, M. Bouhelal, F. Haas, X. Liang, F. Azaiez, Z. M. Wang, B. R. Behera, M. Burns, E. Caurier, L. Corradi, D. Curien, A. N. Deacon, Zs. Dombrádi, E. Farnea, E. Fioretto, A. Gadea, F. Ibrahim, A. Jungclaus, K. Keyes, V. Kumar, S. Lunardi, N. Mărginean, G. Montagnoli, D. R. Napoli, F. Nowacki, J. Ollier, D. O'Donnel, A. Papenberg, G. Pollarolo, M.-D. Salsac, F. Scarlassara, J. F. Smith, K. M. Spohr, M. Stanoiu, A. M. Stefanini, S. Szilner, M. Trotta, and D. Verney, Phys. Rev. C 92, 044308 (2015).
- [23] GAMMASPHERE, https://www.phy.anl.gov/gammasphere/.
- [24] D. G. Sarantites, P.-F. Hua, M. Devlin, L. G. Sobotka, J. Elson, J. T. Hood, D. R. LaFosse, J. E. Sarantites, and M. R. Maier, Nucl. Instrum. Methods Phys. Res. A 381, 418 (1996).
- [25] P.-L. Tai, Ph.D. thesis, Florida State University, 2016 (unpublished).
- [26] P. Taras and B. Haas, Nucl. Instrum. Methods 123, 73 (1975).
- [27] E. F. Moore, Ph.D. thesis, Florida State University, 1988 (unpublished).
- [28] H. J. Rose and D. M. Brink, Rev. Mod. Phys. 39, 306 (1967).
- [29] A. Volya, http://www.volya.net/.
- [30] M. Bouhelal, S. Haas, E. Caurier, F. Nowacki, and A. Bouldjedri, Nucl. Phys. A 864, 113 (2011).
- [31] M. Ionescu-Bujor, A. Iordachescu, D. R. Napoli, S. M. Lenzi, N. Mărginean, T. Otsuka, Y. Utsuno, R. V. Ribas, M. Axiotis, D. Bazzacco, A. M. Bizzeti-Sona, P. G. Bizzeti, F. Brandolini, D. Bucurescu, M. A. Cardona, G. de Angelis, M. De Poli, F. D. Vedova, E. Farnea, A. Gadea, D. Hojman, C. A. Kalfas, T. Kröll, S. Lunardi, T. Martínez, P. Mason, P. Pavan, B. Quintana, C. R. Alvarez, C. A. Ur, R. Vlastou, and S. Zilio, Phys. Rev. C 73, 024310 (2006).
- [32] Y. Utsuno, T. Otsuka, T. Glasmacher, T. Mizusaki, and M. Honma, Phys. Rev. C 70, 044307 (2004).
- [33] J. Ollier, R. Chapman, X. Liang, M. Labiche, K.-M. Spohr, M. Davison, G. de Angelis, M. Axiotis, T. Kröll, D. R. Napoli, T. Martinez, D. Bazzacco, E. Farnea, S. Lunardi, A. G. Smith, and F. Haas, Phys. Rev. C 71, 034316 (2005).