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Precision Measurement of the $B \to X_s \gamma$ Photon Energy Spectrum, Branching Fraction, and Direct CP Asymmetry $A_{CP}(B \to X_s \gamma$)

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The photon spectrum in the inclusive electromagnetic radiative decays of the $B$ meson, $B \to X_s \gamma$, is studied using a data sample of $(382.8 \pm 4.2) \times 10^6 \gamma(4S) \to B\bar{B}$ decays collected by the BABAR experiment at SLAC. The spectrum is used to extract the branching fraction $B(B \to X_s \gamma) = (3.21 \pm 0.33) \times 10^{-4}$ for $E_\gamma > 1.8$ GeV and the direct $CP$ asymmetry $A_{CP}(B \to X_s \gamma) = 0.057 \pm 0.063$. The effects of detector resolution and Doppler smearing are unfolded to measure the photon energy spectrum in the $B$ meson rest frame.

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In the standard model (SM), the electromagnetic radiative decays of the $b$ quark, $b \to s \gamma$ and $b \to d \gamma$, proceed via a loop diagram at leading order. A wide variety of new physics (NP) scenarios such as supersymmetry may cause new contributions to the loop [1–8] at the same order as the SM, resulting in significant deviations for both the branching fractions and the direct $CP$ asymmetry

$$A_{CP} = \frac{\Gamma[b \to (s + d)\gamma] - \Gamma[b \to (\bar{s} + \bar{d})\gamma]}{\Gamma[b \to (s + d)\gamma] + \Gamma[b \to (\bar{s} + \bar{d})\gamma]}$$

Inclusive hadronic branching fractions (BF) $B(B \to X_s \gamma)$ and $B(B \to X_d \gamma)$ can be equated with the perturbatively calculable partonic BF $B(b \to s \gamma)$ and $B(b \to d \gamma)$ at the level of a few percent [9], allowing theoretically clean predictions. At next-to-next-to-leading-order (four-loop), the SM calculation gives $B(B \to X_s \gamma) = (3.15 \pm 0.23) \times 10^{-4}$ ($E_\gamma > 1.6$ GeV) [10], where $E_\gamma$ is the photon energy measured in the rest frame of the $B$ meson. $B(B \to X_d \gamma)$ is suppressed by a factor of $|V_{td}/V_{ts}|^2 = 0.04$, where $V_{ij}$ are the elements of the Cabbibo-Kobayashi-Maskawa (CKM) quark-mixing...
matrix. NP with nonminimal flavor violation can also significantly enhance $A_{CP}$ [11], which is approximately \(10^{-6}\) in the SM [12–14]. Consequently the precision measurement of these decays has long been identified as important in the search for NP. They are central to the program of the future Super $B$ factories [15–17], which will probe NP mass scales up to 100 TeV.

In this letter, new precise measurements of $B(B \to X_c \gamma)$ and $A_{CP}$ are presented. The analysis has been significantly improved from our previous result [18], which it supersedes. In addition, the shape of the photon energy spectrum is measured in the $B$ meson rest frame. It is insensitive to NP [19] but can be used to determine the heavy quark expansion parameters $m_b$ and $\mu^2_2$ [20,21], related to the mass and momentum of the $b$ quark within the $B$ meson. These parameters are used to reduce the uncertainty in the extraction of the CKM elements $|V_{cb}|$ and $|V_{ub}|$ from semileptonic $B$ meson decays [22–25].

This Letter summarizes a fully inclusive analysis of $B \to X_c \gamma$ decays collected from $e^+e^- \to Y(4S) \to B\bar{B}$ events. Full details are given in Ref. [26]. The photon from the decay of one $B$ meson is measured, but $X_c$ is not reconstructed. This avoids large uncertainties from the modeling of the $X_c$ system, at the cost of large backgrounds, which need to be strongly suppressed. The principal backgrounds are from other $B\bar{B}$ decays containing a high-energy photon and from continuum $q\bar{q}$ ($q = u\bar{d}, s\bar{c}$) and $\tau^+\tau^-$ events. The continuum background, including a contribution from initial-state radiation, is suppressed principally by requiring a high-momentum charged lepton ("lepton tag") from the nonsignal $B$ decay, and also by discriminating against events with a more jetlike topology. The $B\bar{B}$ background to high-energy photons, dominated by $\pi^0$ and $\eta$ decays, is reduced by vetoing reconstructed $\pi^0$ or $\eta$ mesons. The residual continuum background is subtracted using off-resonance data collected at a center-of-mass (c.m.) energy 40 MeV below the $Y(4S)$, while the remaining $B\bar{B}$ background is estimated using a Monte Carlo (MC) simulation that has been corrected using data control samples. The photon energy spectrum is measured in the $Y(4S)$ rest frame. Quantities measured in this frame are denoted by an asterisk, e.g., $E^*_{\gamma}$.

The data were collected with the BABAR detector [27] at the PEP-II asymmetric-energy $e^+e^-\to$ collider. The on-resonance integrated luminosity is 347.1 fb$^{-1}$, corresponding to (382.8 $\pm$ 4.2) $\times 10^6$ $B\bar{B}$ events. Additionally, 36.4 fb$^{-1}$ of off-resonance data are used. The BABAR MC simulation, based on GEANT4 [28], EVTGEN [29], and JETSET [30], is used to generate samples of $B^+B^-$ and $B^0\bar{B}^0$ (excluding signal channels), $q\bar{q}$, $\pi^+\pi^-$, and signal events. The signal models used to compute efficiencies are based on QCD calculations in the "kinetic scheme" [20], "shape function scheme" [21], and in an earlier model [19]. These calculations approximate the $X_c$ resonance structure with a smooth distribution in the hadronic mass $m_X$. The portion of the $m_X$ spectrum below 1.1 GeV/$c^2$, where the $K^*(892)$ dominates, is replaced by a Breit-Wigner $K^*(892)$ distribution. The analysis is performed "blind" in the range $1.8 < E^*_\gamma < 2.9$ GeV; that is, the on-resonance data are not examined until all selection requirements are finalized and the corrected $B\bar{B}$ backgrounds determined. The signal range is limited by large $B\bar{B}$ backgrounds at low $E^*_\gamma$.

The event selection begins by requiring at least one photon candidate with $1.53 < E^*_\gamma < 3.50$ GeV. A photon candidate is an electromagnetic calorimeter (EMC) energy cluster with a lateral profile consistent with that of a single photon, isolated by 25 cm from any other cluster, and well contained in the calorimeter. Photons that are consistent with originating from an identifiable $\pi^0$ or $\eta \to \gamma\gamma$ decay are vetoed. Hadronic events are selected by requiring at least three reconstructed charged particles and the normalized second Fox-Wolfram moment $R_2$ to be less than 0.9. To reduce radiative Bhabha and two-photon backgrounds, the number of charged particles plus half the number of photons with energy above 0.08 GeV is required to be at least 4.5.

About 20% of $B$ mesons decay semileptonically to either $e$ or $\mu$. Leptons from these decays are emitted isotropically and tend to have higher momentum than the continuum background in which the lepton and photon candidates also tend to be anticollinear. To suppress the continuum background a tagging lepton ($\ell = e, \mu$) is required to have momentum $p^*_\ell > 1.05$ GeV/$c$ and an angle relative to the photon $\cos\theta^*_\ell > -0.7$. The tag requirement does not compromise the inclusiveness of the $B \to X_c \gamma$ selection since the lepton comes from the recoiling $B$ meson. The presence of a relatively high-energy neutrino in semileptonic $B$ decays is used to further suppress the background by requiring the missing energy of the event to satisfy $E^*_{\text{miss}} > 0.7$ GeV.

The sample is separated into electron and muon tags. For each, $p^*_{\ell\gamma}$ and $\cos\theta^*_\ell \gamma$ are then combined in a neural network (NN) with eight event-shape variables that exploit the difference in topology between isotropic $B\bar{B}$ events and jetlike continuum events. The NN is trained to separate signal-like events from continuum background using MC samples. The $B\bar{B}$ background sample is excluded from the training because it is used for background subtraction and is topologically similar to the signal. The NN is validated with a $B \to X_c \pi^0$ data sample.

The selection criteria are optimized for statistical precision. This was done iteratively for five variables: the two NN outputs, the energies of the lower-energy photon in the $\pi^0$ and $\eta$ vetoes, and $E^*_{\text{miss}}$. The signal efficiency for the entire selection depends on $E^*_\gamma$, falling at lower values. This effect is significantly reduced from our previous analysis, lessening the uncertainty due to the assumed signal model ("model-dependence"). The efficiency integrated over the range $1.8 < E^*_\gamma < 2.9$ GeV is about 2.5%,...
while only 0.0005% of the continuum and 0.013% of the \( B\bar{B} \) background remain in the sample.

The remaining continuum background is estimated with off-resonance data scaled to the on-resonance luminosity and adjusted to account for the 40 MeV c.m. energy difference. The \( B\bar{B} \) background is estimated with the \( B\bar{B} \) MC sample. It consists predominantly of photons originating from \( \pi^0 \) or \( \eta \) decays (≈ 80% in the signal region), electrons (≈ 10%) that are misreconstructed, not identified, or undergo hard bremsstrahlung, \( \omega \) and \( \eta' \) decays (≈ 4%), and \( \bar{\pi}^0 \)’s (≈ 2%) that fake photons by annihilating in the EMC. Each of the significant components is corrected by comparison with data control samples. The \( \pi^0 \) and \( \eta \) background simulations are compared to data using the same selection criteria as for \( B \rightarrow X_s \gamma \) but removing the \( \pi^0 \) and \( \eta \) vetos. For this comparison the high-energy photon requirement is relaxed to \( E_\gamma^* \geq 1.03 \) GeV to increase the size of the sample. The yields of \( \pi^0 \) and \( \eta \) are measured in bins of \( E_{\gamma^*}^{\pi(\eta)} \) by fitting the \( \gamma\gamma \) mass distributions in on-resonance data, off-resonance data, and \( B\bar{B} \) simulation. Correction factors to the \( \pi^0 \) and \( \eta \) components of the \( B\bar{B} \) simulation are derived from these yields. An additional correction is applied to account for data-MC differences in the low-energy photon detection yields. An additional correction is applied to account for data-MC differences in the low-energy photon detection efficiency. This has an opposite effect on the control-sample \( \pi^0 \) and \( \eta \) selection than on the standard event selection, where finding a \( \pi^0 \) or \( \eta \) results in the event being vetoed.

As an antineutron control sample could not be isolated, this source of \( B\bar{B} \) background is corrected by comparing simulation to data for inclusive antiproton yields in \( B \) decay and, using \( \bar{\Xi} \rightarrow \pi^0 \pi^+ \) samples, for the EMC response to \( \bar{\pi}^0 \)’s. The misreconstructed electron background is measured using \( B \rightarrow X \ell \bar{\nu}(e^+e^-) \) data. This sample closely models the particle multiplicity in \( B \rightarrow X_s \gamma \) events. Bremsstrahlung in the detector is reliably simulated by GEANT4, so no correction is necessary. The small contributions from \( \omega \) and \( \eta' \) decays are corrected in bins of \( E_\gamma^* \) using inclusive \( B \) decay data. Nearly all of the tagging leptons arise from \( B \rightarrow X_s \ell \nu \). The yield of such events in the simulation is corrected as a function of lepton momentum according to previous BABAR measurements [31,32]. The complete \( B\bar{B} \) background estimation incorporates the correction factors and uncertainties and includes correlations between \( E_\gamma^* \) bins. The dominant uncertainties originate from the \( \pi^0 \), \( \eta \), and misreconstructed electron corrections.

Figure 1 shows the measured \( E_\gamma^* \) spectrum after subtracting both continuum and \( B\bar{B} \) backgrounds. The systematic errors are due to the \( B\bar{B} \) subtraction uncertainty. The region \( 1.53 < E_\gamma^* < 1.80 \) GeV is dominated by \( B\bar{B} \) background, while the higher-energy range \( 2.9 < E_\gamma^* < 3.5 \) GeV contains only continuum background. These regions are used to validate the background subtraction procedure. In the higher-energy range there are \(-100 \pm 138\) (stat) events.

In the lower-energy region there are \( 1252 \pm 272\) (stat) \( \pm 841\) (syst) events. Allowing for an average of 275 signal events from a range of plausible signal models, and for correlations between the bins, the latter result is consistent with zero to within 1 standard deviation (1\( \sigma \)).

To extract BFs and the shape of the spectrum, it is necessary to first correct for efficiency. Theoretical predictions are made for the true \( E_\gamma \) in the \( B \) meson rest frame, whereas the \( E_\gamma^* \) is measured in the \( Y(4S) \) frame. Hence it is also necessary to correct for the asymmetry EMC resolution and the Doppler smearing due to the motion of the \( B \) meson in the \( Y(4S) \) rest frame. The efficiency and smearing corrections depend upon the assumed signal shape due to the effects of bin migration. In both the kinetic and shape function schemes, this shape is parametrized by \( m_h \) and \( \mu^* \). The Heavy Flavor Averaging Group (HFAG) [33] has extracted values and uncertainties in the kinetic scheme by fitting moments of inclusive distributions in \( B \rightarrow X_s \ell \nu \) decays and previous \( B \rightarrow X_s \gamma \) measurements, and has also translated them to the shape function scheme. These results define the nominal signal model (kinetic scheme) used for the BF measurement, along with a model-dependence uncertainty (kinetic and shape function schemes). To provide an independent measurement of the shape of the spectrum, the measured spectrum is unfolded using an iterative technique that reduces sensitivity to the signal model. In this case the initial signal model and model-dependence uncertainty are based on the data rather than the HFAG parameters. The effects of efficiency and smearing cancel in the \( A_{CP} \) measurement so it is extracted directly from the measured \( E_\gamma^* \) yield separated by lepton tag charge.

The BF is computed from

\[
\mathcal{B}(B \rightarrow X_s \ell \nu) = \frac{\alpha S}{2N_{BB} \epsilon_{\text{sig}}},
\]

where \( S \) is the signal yield integrated over the \( E_\gamma^* \) ranges \( 1.8, 1.9, 2.0 \) to 2.8 GeV, \( \epsilon_{\text{sig}} \) is the signal efficiency, and
the efficiency (3.1%), predominantly due to the high-energy photon and NN selections. The most significant systematic error is from the corrections to the $B \bar{B}$ background simulation, which in the range 1.8 GeV < $E_{\gamma}$ < 2.8 GeV contributes 7.8% to a total systematic uncertainty of 9.0%. Additional contributions added in quadrature, all energy-dependent, arise from uncertainties in the selection efficiency (3.1%), predominantly due to the high-energy photon and NN selections, the semileptonic BF for $B$ meson decays, and the modeling of the $X_s$ system. Correlations between the $B \bar{B}$ and the signal efficiency systematic errors contribute an additional 2.9% uncertainty. Finally, there is a 1.1% uncertainty in $N_{B\bar{B}}$.

To obtain an $E_{\gamma}$ spectrum in the $B$ rest frame, the $E_{\gamma}$ spectrum shown in Fig. 1 is corrected for selection efficiency, and the resolution smearing and Doppler smearing are unfolded. A simplified version [35] of an iterative unfolding technique [36] is used. The method starts with an initial signal model that, when passed through the detector simulation and event selection, closely resembles the data (shape function scheme with $m_b = 4.51$ GeV, $\mu^2 = 0.46$ GeV$^2$). This model is used to correct for efficiency and unfold the data. A fraction, determined by a bin-dependent regularization function, of the difference between the unfolded data and the initial signal model is used to adjust the signal model, and the process is iterated until it converges. Only one iteration is necessary. The results are shown in Fig. 2. This technique preserves fluctuations in the spectrum and reduces the model error. The model-dependence uncertainty is computed using an initial model that is approximately 1σ lower than the data in Fig. 1 in the region with significant $B \bar{B}$ background (1.8 < $E_{\gamma}$ < 2.1 GeV). The error is the absolute value of the difference bin by bin after unfolding. It is small except near the kinematic limit, $E_{\gamma} \approx m_b/2$, where the sharply falling edge leads to strongly anticorrelated differences in adjacent bins. To reduce this effect, the 100-MeV bins between 2.4 and 2.8 GeV are combined into 200-MeV bins. The spectral shape and the full covariance matrix, provided in Ref. [26], are used to compute the first and second moments in Table I. They can also be used to fit any theoretical prediction for the spectral shape. The BFs computed from the sum of the $\Delta B$ in Fig. 2 are consistent with the values given in Table I [26].

Finally the $E_{\gamma}$ sample is divided into $B$ and $\bar{B}$ decays, using the charge of the lepton tag, to measure $A_{CP}^2 (B \rightarrow X_{s+d}\gamma) = (N^+ - N^-)/(N^+ + N^-)$, where $N^+$($N^-$) are the positively (negatively) tagged signal yields. $A_{CP}$ is then given by $A_{CP} = A_{CP}^{\text{meas}}/(1 - 2\omega)$, where $\omega$ is the mistag fraction. To maximize the statistical precision a requirement of $2.1 < E_{\gamma} < 2.8$ GeV is made. This is determined from simulation and does not bias the SM prediction for the asymmetry [37]. The yields are $N^+ = 2620 \pm 158$(stat) and $N^- = 2389 \pm 151$(stat). The bias on $A_{CP}$ due to charge asymmetry in the detector response or $B \bar{B}$ background is measured to be $\Delta A_{CP}^{\text{meas}}(B \rightarrow X_{s+d}\gamma) = -0.004 \pm 0.013$, using events in the $B \bar{B}$ control region to check for a background asymmetry, and using several event samples ($e^+ e^- \rightarrow e^+ e^- \gamma$, $e^+ e^- \rightarrow \mu \mu \gamma$, and $B \rightarrow K^{(*)} J/\psi(\ell^+ \ell^-)$) to check for a lepton tag asymmetry. The mistag fraction $\omega = 0.133 \pm 0.006$ is dominated by $B^0 \bar{B}^0$ mixing, which contributes 0.093 ± 0.001 [34], with

\[
\Delta A_{B(B \rightarrow X_{s+d}\gamma)}(10^{-4}) \quad \langle E_{\gamma} \rangle \quad \langle (E_{\gamma} - \langle E_{\gamma} \rangle)^2 \rangle \quad (\text{GeV}) \quad (\text{GeV}^2)
\]

<table>
<thead>
<tr>
<th>$E_{\gamma}$ Range (GeV)</th>
<th>$\mathcal{B}(B \rightarrow X_{s+d}\gamma)$</th>
<th>$\langle E_{\gamma} \rangle$</th>
<th>$\langle (E_{\gamma} - \langle E_{\gamma} \rangle)^2 \rangle$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.8 to 2.8</td>
<td>$3.21 \pm 0.15 \pm 0.29 \pm 0.08$</td>
<td>$2.267 \pm 0.019 \pm 0.032 \pm 0.003$</td>
<td>$0.0484 \pm 0.0053 \pm 0.0077 \pm 0.0005$</td>
</tr>
<tr>
<td>1.9 to 2.8</td>
<td>$3.00 \pm 0.14 \pm 0.19 \pm 0.06$</td>
<td>$2.304 \pm 0.014 \pm 0.017 \pm 0.004$</td>
<td>$0.0362 \pm 0.0033 \pm 0.0033 \pm 0.0005$</td>
</tr>
<tr>
<td>2.0 to 2.8</td>
<td>$2.80 \pm 0.12 \pm 0.14 \pm 0.04$</td>
<td>$2.342 \pm 0.010 \pm 0.008 \pm 0.005$</td>
<td>$0.0251 \pm 0.0021 \pm 0.0013 \pm 0.0009$</td>
</tr>
</tbody>
</table>

$N_{B\bar{B}}$ is the number of $B \bar{B}$ pairs in the sample. The factor $\alpha$, which is close to unity, corrects for resolution and Doppler smearing and is computed with the nominal signal model. The model-dependence errors on the BF associated with the efficiency and the smearing correction are fully correlated. The results for the three energy ranges are given in Table I. The BFs have been corrected by a factor $1/(1 + (|V_{td}|/|V_{ts}|)^2) = 0.958 \pm 0.003$ [34] to remove the contribution from $B \rightarrow d\gamma$. This model is used to correct for efficiency and the smearing correction are fully correlated. The results for the three energy ranges are given in Table I [26].
an additional $0.040 \pm 0.005$ arising from wrong-sign leptons from the $B$ decay chain and from misidentification of hadrons as leptons. After correcting for charge bias and mistagging it is found

$$A_{CP} = 0.057 \pm 0.060\text{(stat)} \pm 0.018\text{(syst).}$$

The systematic error includes relative uncertainties from the $BB$ background subtraction (2.2%) and mistagging (1.8%). The uncertainty due to differences in the $B \to X_s \gamma$ and $B \to X_\gamma\gamma$ spectra is negligible.

In summary, the photon spectrum of $B \to X_{s,d}\gamma$ decays has been measured and used to extract the branching fraction, spectral moments, and $A_{CP}$. Previous inclusive measurements of $B \to X_s \gamma$ have been presented by the CLEO [38], BABAR [18], and Belle [39] Collaborations. The measured branching fraction $B(B \to X_s \gamma) = (3.21 \pm 0.15 \pm 0.29 \pm 0.08) \times 10^{-4}$ (1.8 $< E_\gamma < 2.8$ GeV) is comparable in precision to the Belle result, $(3.56 \pm 0.13 \pm 0.25 \pm 0.01) \times 10^{-4}$, but with a data set that has 60% smaller integrated luminosity. The BF for $1.8 < E_\gamma < 2.8$ GeV is extrapolated to the range $E_\gamma > 1.6$ GeV using a factor of $1/(0.968 \pm 0.006)$ determined by HFAG. This results in $B(B \to X_s \gamma) = (3.31 \pm 0.16 \pm 0.30 \pm 0.09) \times 10^{-4}$ for $E_\gamma > 1.6$ GeV, in good agreement with the SM prediction. The extrapolated $B(B \to X_s \gamma)$ can be used to constrain NP. For example, in a type-II two-Higgs-doublet model [10,40] the region $M_{H^\pm} < 327$ GeV is excluded independent of $\tan\beta$ at 95% confidence level. This limit is far more stringent than that from direct searches at the LHC [41,42]. The $A_{CP}$ measurement is the most precise to date and can be used to constrain nonminimal flavor-violating models [11]. The measured moments and spectra provide input to improve the precision on the HFAG estimation of $m_b$ and $M_B^2$, which will result in a reduced error on $|V_{ub}|$. Finally, the improved technique presented in this Letter can be applied with increased precision at future Super $B$ factories.

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