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# Effect of vacancies on the structure and properties of $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$

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$\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  belongs to a family of materials with large intrinsic vacancy concentrations that are being actively studied due to their potential for diverse applications that include thermoelectrics and phase-change memory. In this article, the  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  structure is investigated via synchrotron x-ray diffraction, electron microscopy, and x-ray absorption experiments. Diffraction and microscopy measurements showed that the extent of vacancy ordering in  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  is highly dependent on thermal annealing. It is posited that stoichiometric vacancies play a role in local atomic distortions in  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  (based on the fine structure signals in the collected x-ray absorption spectra). The effect of vacancy ordering on  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  material properties is also examined through band gap and Hall effect measurements, which reveal that the  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  band gap redshifts by  $\approx 0.05$  eV as the vacancies order and accompanied by gains in charge carrier mobility. The results serve as an encouraging example of altering material properties via intrinsic structural rearrangement as opposed to extrinsic means, such as doping.

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## I. INTRODUCTION

$\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  is a compound semiconductor that belongs to a class of III–VI materials that exhibit a cubic zincblende crystal structure ( $F\bar{4}3m$  space group) dominated by stoichiometric or structural vacancies (otherwise known as defect zincblende). These defects arise due to the valence mismatch between the anion and cation sites forcing 1/3 of the cation sites to be vacant in order to electrically stabilize the crystal. Recent investigations on binary III–VI materials with defect zincblende structures have shown that their stoichiometric vacancies can lead to material properties that are suitable for a vast number of applications. Examples include observing ordered vacancy planes in  $\text{Ga}_2\text{Te}_3$  that serve as effective phonon scatterers that decrease thermal conductivity, which is crucial for thermoelectric applications.<sup>1–3</sup> Additional work on  $\text{Ga}_2\text{Te}_3$  has also shown it could be an attractive material for phase-change random access memory applications as it shows better data retention ability, low power consumption, and high dynamical electric switching ratios when compared to the more widely studied  $\text{Ge}_2\text{Sb}_2\text{Te}_5$ .<sup>4</sup> The presence of stoichiometric vacancies in this class of material also leads to a loose crystal structure, which allows for anomalously high radiation stability by minimizing Frenkel pair production from incident radiation; parameters, such as charge carrier concentration, charge carrier mobility, and microhardness measured before and after irradiation showed little or no change.<sup>5–7</sup> As a result, such materials may also have potential as nuclear particle detectors for high energy physics or security applications.

The ternary  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  compound ( $\approx 800$  °C melting point) is expected to display properties analogous to III–VI binary zincblende compounds but with the added benefit of band gap engineering;<sup>8</sup> though one must be aware of the solid state immiscibility in the Se rich region of the  $\text{Ga}_2\text{Te}_3$ – $\text{Ga}_2\text{Se}_3$  phase diagram.<sup>9</sup> Nevertheless, there is a paucity of information on the  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  compound semiconductor; here, we present an experimental investigation to study the influence of stoichiometric vacancies on the structure and physical properties of  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$ . We utilize high-resolution single crystal diffraction experiments and transmission electron microscopy (TEM) to characterize the basic crystal structure of  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$ . Then we attempt to probe the effect of vacancies on local structure via extended x-ray absorption fine structure (EXAFS) experiments. Finally, we examine the effect of stoichiometric vacancies on material properties by correlating our structural results with band gap and charge carrier mobility measurements.

## II. EXPERIMENTAL METHODS

$\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  single crystals were grown using a modified Bridgman method from stoichiometric amounts of 8N Ga, 6N Se, and 6N Te based on a procedure we reported elsewhere.<sup>10</sup> Specimens harvested from the solidified ingot were subjected to three thermal treatments (similar treatments have been observed to alter the vacancy distributions in powder  $\text{Ga}_2\text{Te}_3$  specimens<sup>11</sup>): (1) 735 °C anneal for 28 days followed by quenching to 0 °C, (2) 435 °C for 28 days followed by slow cooling in the furnace, and (3) sample in the as-grown state.

Single crystal x-ray diffraction experiments were performed at room-temperature on the bending magnet beam line 33-BM at the Advanced Photon Source (APS) at Argonne National Laboratory (ANL) employing a focused beam of 15 keV x rays. Single crystal  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  specimens were mounted on a four-circle diffractometer in an off-specular geometry utilizing a scintillation area detector for data collection. Detailed information on the instrument setup has been reported elsewhere.<sup>12</sup>

Electron microscopy was carried at the National Center for Electron Microscopy (NCEM) at Lawrence Berkeley National Laboratory. Images were collected using a modified Philips CM300FEG/UT electron microscope at an operating voltage of 300 kV. Sample preparation involved dispersing crushed  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  single crystals in an isopropanol solution on conventional Au TEM grids.

EXAFS experiments were performed at the 05-BM bending magnet beam line at the APS and the 4-1 bending magnet beam line at the Stanford Synchrotron Radiation Lightsource (SSRL) at SLAC National Accelerator Laboratory. Powders ground from single crystal  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  specimens (measured in the single diffraction experiments) and sieved to  $60\ \mu\text{m}$  were dispersed onto scotch tape and mounted onto the x-ray beam in a transmission geometry. Scans were taken by tuning the beam to the Ga (10.367 keV), Se (12.658 keV), and Te (31.814 keV) K-edges (five scans were taken at each x-ray energy to minimize statistical errors). Data analysis was done via the SIXpack software package.<sup>13</sup>

The band gaps of  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  samples were measured using a Perkin-Elmer 950 Lambda spectrophotometer. Transmission and reflectance data from the polished  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  single crystal samples were used to plot

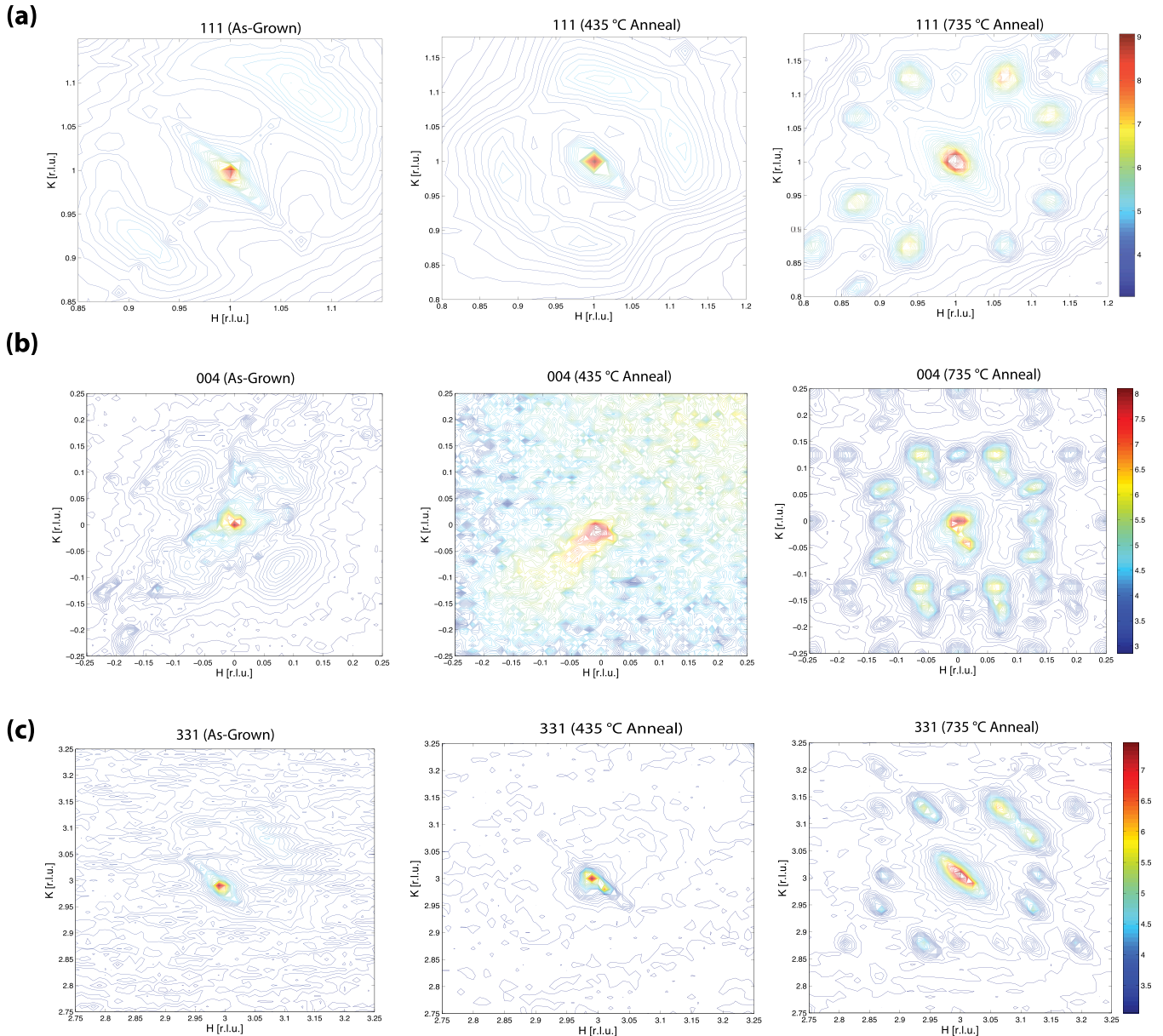


FIG. 1. Reciprocal lattice scans at the 111 (a), 004 (b), and 331 (c) Bragg reflections for as-grown, 435 °C, and 735 °C annealed  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  single crystals.

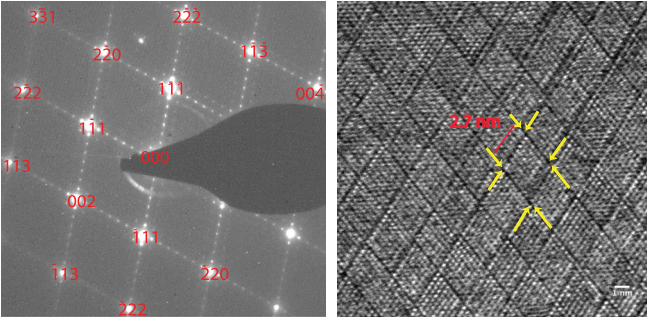


FIG. 2. Electron diffraction pattern and dark field TEM image of 735 °C annealed  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  in the  $[110]$  zone axis. Ordered two-dimensional vacancy structures are represented by a periodic dark line contrast that propagates in  $\langle 111 \rangle$  directions at 2.7 nm intervals. This correlates with the electron diffraction pattern, where the satellite reflections occur at  $1/8$  of the lattice spacing in reciprocal space.

optical absorption edges, where the rise in absorption was used to determine the band gap.

Electrical properties of  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  were measured via Hall effect using  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  single crystals with surface area of  $\approx 4 \text{ mm}^2$  and thickness of  $\approx 1 \text{ mm}$ . A four-probe van der Pauw geometry (utilizing contacts made from silver paste) was implemented. Measurements were done under a field of 1.0 T using a 1 nA excitation current.

### III. RESULTS AND DISCUSSION

X-ray diffraction experiments on as-grown, 435 °C, and 735 °C annealed  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  crystals show a cubic zincblende structure with a lattice constant of  $a = 5.77 \text{ \AA}$ . However, high-resolution reciprocal lattice mapping (shown in Figure 1) reveals that specimen thermal history has a profound effect on the secondary structural characteristics of  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$ . Mainly, in the 735 °C annealed specimen, well-defined satellite reflections are observed around the fundamental Bragg reflections. These occur in pairs at  $1/16[2\ 1\ 0]$  in equivalent directions from the centrally located Bragg peak. These ancillary reflections originate from superstructures associated with the stoichiometric vacancies in the defect zincblende crystal system. Their locations in reciprocal space suggest long-range modulated structure parallel to  $\langle 210 \rangle$ . However, dark field TEM imaging (see Figure 2) shows only

the presence of two-dimensional vacancy structures parallel to  $\langle 111 \rangle$  directions that order at  $\approx 2.7 \text{ nm}$  intervals or about eight lattice units (we have reported results from high-resolution TEM investigation on  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  elsewhere<sup>14</sup>). Such a discrepancy has been previously observed in as-grown  $\text{Ga}_2\text{Te}_3$ .<sup>15–17</sup> Hence, the x-ray data suggest that the stoichiometric vacancy structures in  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  are based on coupled displacive (as directly observed via TEM) and atomic modulations.

Inspecting the reciprocal lattice maps for the as-grown and 435 °C annealed  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  crystals, we see an absence of distinct satellite reflections. Here, in the as-grown condition, the two-dimensional vacancy structures in these crystals lose their long-range spatial ordering. Nevertheless, they retain their proclivity to diffract x rays evidenced by the diffuse scattering features present around the main Bragg reflections, which is indicative of short-range periodicity.

A common feature across all samples in the reciprocal lattice maps is the streaking of the Bragg peaks diagonally in  $h$ - $k$  space, alluding to crystal distortions arising from the stoichiometric-based vacancy structures, though global symmetry of the Bravais lattice associated with a zincblende crystal is preserved. This is captured in the reciprocal lattice maps and TEM micrographs shown in Figures 1 and 2. As a result, we believe that the elongation of the Bragg peaks arises from local symmetry distortions. To confirm this, we performed extended x-ray absorption fine structure measurements to probe the local structure of  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$ . This is done by tuning an incident x-ray beam to the K-edge energies (i.e., energy required to eject the  $1s$  electrons from the K shell) of the constituent atoms of the specimen; when x rays are absorbed by the atom, a photoelectron is emitted and propagates in the lattice as a spherical wave where interference can occur between outgoing and backscattered waves.<sup>18</sup> This phenomenon gives rise to oscillations in the observed absorption cross-section, which yields information on the local structure of the absorbing atom. Taking the Fourier transform of the fine structure oscillations in the absorption spectra yields radial distribution functions with peaks corresponding to the nearest neighbor atomic shells around the absorbing atom. These are shown in Figure 3 at the Te, Se, and Ga K-edge energies, which correspond to the local structure around Te, Se, and Ga atoms, respectively.

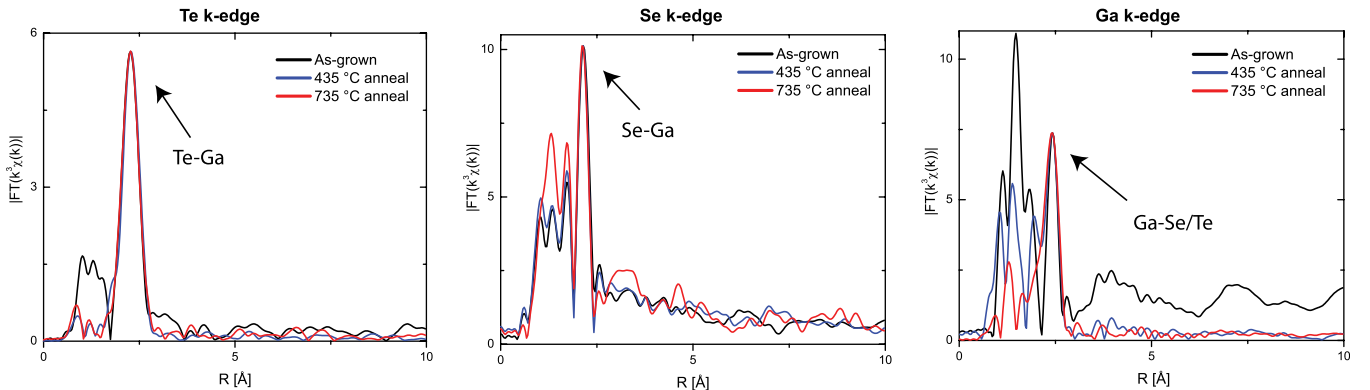


FIG. 3. Radial distribution functions obtained from EXAFS oscillations that show the local structure around the absorbing Te, Se, and Ga atoms. The common peak corresponding to nearest neighbor Ga-Te and Ga-Se bonds in the zincblende crystal is arrowed.



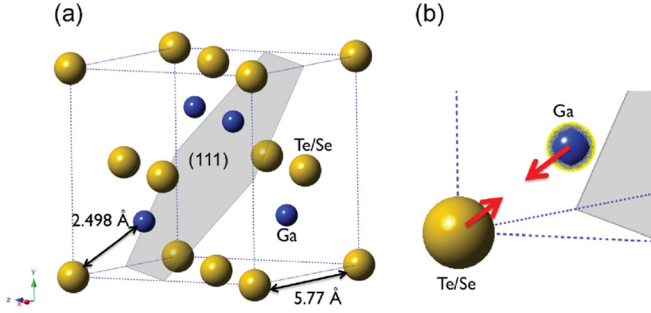


FIG. 4. (a) Schematic of the  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  unit cell representative of the undistorted zincblende structure. The (111) plane is sketched to highlight the direction of the observed vacancy planes. (b) Contraction of the cation-anion bond distance observed via EXAFS measurements.

Since  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  is formed via Ga-Te and Ga-Se tetrahedra packed in the zincblende structure, we expect the nearest neighbor shells around the Ga, Se, and Te atoms to correspond to the cation-anion (Ga-Se or Ga-Te) bond distance, which is 2.498 Å. Inspecting the Te K-edge for the as-grown and annealed samples, however, the dominant scattering shell occurs at  $\approx 2.27$  Å, indicative of a contraction of the Ga-Te atomic dumbbell (a schematic illustrating this effect is shown in Figure 4). Similarly at the Se K-edge, the common peak is observed at  $\approx 2.14$  Å, representing the Ga-Se bond length. Compared with Ga-Te bond length, a larger contraction is likely because the Se atom is lighter. Additionally, real scattering shells are observed at  $\approx 1.80$  Å for all  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  samples not associated with the cubic lattice at the Te and Se K-edge energies, suggestive of additional local structural distortions. Such distortions are more prominent as we inspect the radial distribution functions for the Ga K-edge; this is not surprising as the stoichiometric vacancies in  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  originate at the Ga site. Here, the common peak corresponding to the cation-anion dumbbell occurs at  $\approx 2.43$  Å, once again suggesting local atomic contraction. The mechanism driving such distortions and the role of vacancy periodicity remain uncertain. Earlier studies on  $\text{Ga}_2\text{Te}_3$  have posited that stoichiometric Ga vacancies can induce Jahn-Teller lattice distortions that drive a transition to a tetragonal structure.<sup>15–17</sup> We were not able to verify this for  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$ , but based on our

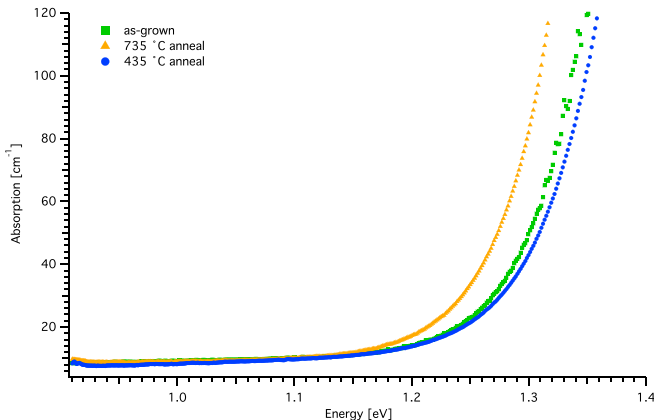


FIG. 5. Absorption edges of as-grown, 435 °C annealed, and 735 °C annealed  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  single crystals.

TABLE I. Electrical properties of  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$ .

Thermal history	$\rho$ [M $\Omega$ cm]	Type	$\mu$ [cm <sup>2</sup> /Vs]
As-grown	0.71	p	15
735 °C	0.028	n	30
435 °C	3.1	n	0.8

x-ray absorption data, we confirm that distortions caused by stoichiometric vacancies are real and occur locally within the crystal.

Our x-ray measurements show that thermal history plays a prominent role in the distribution of stoichiometric vacancies in  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$ . Yet information on how the distribution of stoichiometric vacancies affects material properties remains scarce (recent work has shown that the two-dimensional vacancy structures in  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  can influence pressure-induced amorphization behavior<sup>19</sup>). Here, we attempted to correlate the effect of stoichiometric vacancy ordering on the electrical properties of  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  via band gap and Hall effect measurements. First, we measured the band gap of an as-grown  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  single crystal. The sample then underwent the 735 °C annealing treatment and was remeasured under identical conditions. Finally, a  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  single crystal under the 435 °C annealing treatment was measured. The results are shown as absorption spectra in Figure 5, where the rise in absorption occurs at the band gap energy. The as-grown and 435 °C sample have a band gap of  $\approx 1.27$  eV. As the vacancies in  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  become fully ordered (via the 735 °C annealing treatment), the band gap of  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  decreases to  $\approx 1.22$  eV. While this measured band gap change is slight, it appears to be an encouraging example of controlling intrinsic material parameters to engineer electronic structure (in contrast to extrinsic means like doping).

Electrical properties of  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  obtained from Hall effect experiments are shown in Table I. The 435 °C sample had a resistivity of 3.1 M $\Omega$  cm, the as-grown had  $\approx 0.71$  M $\Omega$  cm, and the 735 °C sample  $\approx 0.028$  M $\Omega$  cm. Similarly, the 735 °C showed the highest carrier mobility (30 cm<sup>2</sup>/Vs, *n*-type) when compared to the as-grown and 435 °C samples. Based on these results, it appears that vacancy ordering improves the charge carrier transport properties, although other effects might be at play. For example, crystal quality can vary tremendously across a single ingot and the large concentrations of stoichiometric vacancies lead to a large number of free anions causing  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  to be a highly compensated semiconductor, which explains why both *p*-type and *n*-type conductivities were observed. Consequently, more detailed electrical measurements that include temperature dependent Hall effect and directional resistivity measurements must be performed to further assess the effects of vacancy distribution on the electrical properties of  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$ .

#### IV. CONCLUSION

The spatial distribution of stoichiometric vacancies appears to have measurable effects on the structure and

properties of  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$ . X-ray diffraction and electron microscopy showed the formation two-dimensional structures, where their spatial ordering is highly dependent on specimen thermal history. X-ray absorption data show that the vacancies in  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$  also give rise to local distortions within the zincblende lattice though the overall cubic symmetry is preserved. Band gap and Hall effect measurements indicate that vacancy ordering may play a role in improving the electrical transport properties of  $\text{Ga}_2(\text{Se}_{0.33}\text{Te}_{0.67})_3$ , providing an encouraging demonstration of engineering material electronic structure through intrinsic means.

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