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Visual Learning By Integrating Descriptive and Generative Methods

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Abstract

This paper presents a mathematical framework for visual learning that integrates two popular statistical learning paradigms in the literature: I). Descriptive learning, such as Markov random fields and minimax entropy learning, and II). Generative learning, such as PCA, ICA, TCA, and HMM. We apply the integrated learning framework to texture modeling, and we assume that an observed texture image is generated by multiple layers of hidden stochastic processes with various texture elements called “textons”. Each texton is expressed as a window function like a mini-template or a wavelet, and each hidden stochastic process is a spatial pattern with a number of textons subject to affine transformations. The hidden layers are characterized by minimax entropy models, and they generate images by occlusion or linear addition. Thus given a raw input image, the learning framework achieves four goals: i). Computing the appearance of the textons. ii). Inferring the hidden stochastic processes. iii). Learning Gibbs models for each hidden stochastic process. and iv). Verifying the learnt textons and models through random sampling. The integrated framework subsumes the minimax entropy learning paradigm and creates a richer class of probability models for visual patterns. Furthermore we show that the integration of descriptive and generative methods is a natural path of visual learning. We demonstrate the proposed framework and algorithms on many real images.

1 Introduction

In Bayesian statistical image analysis, an important task is to learn probabilistic models that characterize visual patterns in real images. In the literature, existing methods for learning statistical models are divided into two categories. In this paper, we call one the *descriptive method* and the other *generative method*. Descriptive method characterizes visual patterns by imposing statistical constraints and thus learns models at a “signal” level. This includes Markov random fields, minimax entropy learning[15], deformable

models[1]. For example, recent work on texture modeling all fall in this category[15, 13]. Despite the success of descriptive models in texture modeling, these models are built on pixel intensities through complex interactions between image features, and they do not capture high level semantics in the patterns. For example, a Gibbs model can realize a cheetah skin pattern but it does not have explicit notion of individual blobs. In contrast to descriptive method, generative method infers hidden causes (or semantics) from raw signal, and thus learns hierarchical models. Examples of generative method are principle component analysis (PCA), independent component analysis (ICA), transformed component analysis (TCA)[4], image coding[11], and hidden Markov models (HMM). As a recent review paper[12] shows, existing generative models mentioned above suffer from the simplified assumption that hidden variables are independent and identically distributed. Therefore they are not powerful enough to model realistic visual patterns. For example, an image coding model cannot synthesize a texture patterns through random sampling.

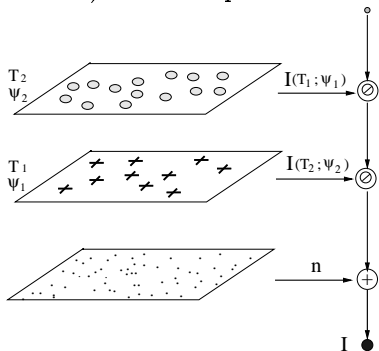
In this paper, we present a visual learning paradigm that integrates both descriptive and generative method and we apply this learning paradigm to modeling texture and texton patterns.

In early vision, a fundamental observation, dated back to Marr’s primal sketch[10], is that natural visual patterns consist of multiple layers of stochastic processes. An example is shown in Fig. 1.a. When we look at this pattern, we perceive not only the texture “impression” and pixels but also the repeated elements for the ivy and bricks. In psychology, basic texture elements are called “texton” or “texel” vaguely[7], and a precise mathematical definition has yet to be found. In this paper, we propose to study a multiple layer generative model as Fig. 1 illustrates. It has three stochastic processes — two for the ivy and brick patterns respectively with two distinct “textons” and the third for noise process. The stochastic processes are hidden and

the image is the only observable signal.



a). A visual pattern



b). A generative model

Figure 1: Multiple layers of texton image $\mathbf{I}(\mathbf{T}_i; \psi_i)$, $i = 1, 2, \dots, k$ are superimposed with additive noise \mathbf{n} to generate image \mathbf{I} .

Given an input image, the integrated learning framework achieves the following four objectives.

1. Learn the texton element for each stochastic process. A texton is represented as a window function of a mini-template or wavelets.
2. Inferring the hidden stochastic processes each being a spatial pattern with a number of textons subject to affine transformations.
3. Learning minimax entropy models for the hidden processes.
4. Verifying the learnt textons and generative models through random sampling.

Furthermore we find that descriptive models are precursors of generative models. Learning process evolves by discovering hidden causes. Therefore the two learning paradigms must be integrated. For hidden layers, if there is no further hidden layer behind, the hidden variables must be characterized by the descriptive method, i.e. the minimax entropy models. Iid models are special cases of Gibbs distribution.

The integrated learning framework makes three interesting contributions to visual learning. 1). It subsumes the minimax entropy learning paradigm by extending from pixels to textons and creates a richer class of probability models for visual patterns. It is easy to show that existing texture models are degenerated cases of this model where the textons are single pixels. 2). It introduces the minimax entropy learning paradigm for modeling hidden variables in generative models, and thus subsumes and extends existing generative models such as PCA, ICA, and TCA[4]. 3). It can automatically learn the textons from images as the transformed components under the generative model. Our work is different from [8, 9] which used the clustering method in feature spaces without a generative model. As a result, texton elements at various translations, rotations and scales are treated as distinct textons.

We demonstrate the proposed framework and algorithms on a number of real images.

2 Background on Visual Learning

Given a set of M observable signals $S = \{\mathbf{I}_1^{\text{obs}}, \mathbf{I}_2^{\text{obs}}, \dots, \mathbf{I}_M^{\text{obs}}\}$. Without loss of generality, we assume the observable signals are raw images. The goal of visual learning is to estimate a probabilistic model $p(\mathbf{I})$ from S so that $p(\mathbf{I})$ approaches the underlying frequency $f(\mathbf{I})$, which governs the ensemble of signals in an application, in terms of minimizing a Kullback-Leibler divergence $KL(f(\mathbf{I})||p(\mathbf{I}))$ between f and p . This leads to the standard maximum likelihood estimator (MLE).

$$p^* = \arg \min_{p \in \Omega_p} KL(f(\mathbf{I})||p(\mathbf{I})) \approx \arg \max_{p \in \Omega_p} \sum_{i=1}^M \log p(\mathbf{I}_i^{\text{obs}}). \quad (1)$$

Ω_p is the family of distributions where p^* is searched for. One general procedure is to search for p in a sequence of nested probability families,

$$\Omega_0 \subset \Omega_1 \subset \dots \subset \Omega_k \rightarrow \Omega_f \ni f.$$

k indexes the dimensionality of the space, for example, k could be the number of free parameters in a model. As k increases, the probability family should be general enough to contain the true distribution $f(\mathbf{I})$.

There are two choices of families Ω_p in the literature and both are general enough for approximating any distributions $f(\mathbf{I})$.

The first choice is the exponential family of models, which is derived by descriptive method, and has deep root in statistical mechanics following the maximum entropy principle. A descriptive method extracts a set

of K features as *deterministic constraints*, and computes the statistics for these features across images in S . The statistics are denoted by $\phi_j(\mathbf{I}), j = 1, 2, \dots, K$. Then it constructs a model p through *descriptive constraints* so that p reproduces the observed statistics while having maximum entropy. This leads to the following Gibbs form with $\beta = (\beta_1, \dots, \beta_K)$ are the parameters for the model,

$$p(\mathbf{I}; \beta) = \frac{1}{Z(\beta)} \exp\left\{-\sum_{j=1}^K \beta_j \phi_j(\mathbf{I})\right\}.$$

Thus, a descriptive method augments the dimension of the space Ω_p by increasing the number of feature statistics and generating a sequence of exponential families,

$$\Omega_1^d \subset \Omega_2^d \subset \dots \subset \Omega_K^d \rightarrow \Omega_f.$$

This family includes all the MRF and minimax entropy models for texture.

The second choice is the mixture family of models, which is derived from integration or summation over some hidden variables $W = (w_1, w_2, \dots, w_k)$.

$$p(\mathbf{I}; \Theta) = \int \cdot \int p(\mathbf{I}, w_1, w_2, \dots, w_k; \Theta) \prod_{i=1}^k dw_i.$$

In this way, we assume that there exists a joint probability distribution $f(\mathbf{I}, W)$, and that W generates \mathbf{I} and W should be *inferred* from \mathbf{I} , instead of deterministic transforms. This generative method incrementally adds hidden variables to augment the space Ω_p and thus generates a sequence of mixture families

$$\Omega_1^g \subset \Omega_2^g \subset \dots \subset \Omega_K^g \rightarrow \Omega_f \ni f.$$

For example, in PCA, ICA (independent component analysis) and image coding[11], a simply generative model is a linear superposition of some window functions $\Psi_i, i = 1, 2, \dots, M$, such as over-complete wavelet bases, eigen vectors plus iid Gaussian noise \mathbf{n} .

$$\mathbf{I} = \sum_{i=1}^M a_i \Psi_i + \mathbf{n}; \quad \alpha_i \sim p(\alpha) \forall i.$$

In this example, the parameters are the M bases (or eigen vectors) $\Theta = \{\Psi_1, \dots, \Psi_M\}$ and the hidden variables are the M coefficients of bases (or eigen vectors) plus the noise $W = (a_1, a_2, \dots, a_M, \mathbf{n})$.

The forms of a mixture model $p(\mathbf{I}; \Theta)$ are decided by the distribution of the hidden variables W . The latter must be from descriptive families. However, in the literature, hidden variables $a_i, i = 1, 2, \dots, M$ are

assumed to be iid Gaussian or Laplacian distributed. Thus the concept of descriptive models are trivialized.

In the following section, we study a learning paradigm that integrates both families and some interesting relationships are revealed.

3 An Integrated Learning Framework

3.1 A generative model of texture

In this section, we study a multi-layer generative model as Fig 1.b shows. We assume that a texture image \mathbf{I} is generated by L layers of stochastic processes while each layer consists of a finite number of distinct elements, called “textons”, which are image patches transformed from one square image template Ψ_i . The j th texton in layer i is represented by six transform variables on the template Ψ_i as

$$T_{ij} = (x_{ij}, y_{ij}, \sigma_{ij}, \tau_{ij}, \theta_{ij}, A_{ij}),$$

where (x_{ij}, y_{ij}) represents the texton center location. σ_{ij} is the scale of the size, τ_{ij} is called “shear” compressing the width of the texton, θ_{ij} is the orientation, and A_{ij} denotes photometric transforms such as lighting variability. The transformation on T_{ij} is denoted by $G[T_{ij}]$. The pixel domain in which the texton T_{ij} covers is denoted as $D_{ij} = D[T_{ij}]$. Thus the image patch $\mathbf{I}_{D_{ij}}$ of a texton T_{ij} is derived by

$$\mathbf{I}_{D_{ij}} = G[T_{ij}] \odot \Psi_i,$$

where \odot denotes the transformation operation. Texton examples at different scales, shears, and orientations are shown in Fig. 2.

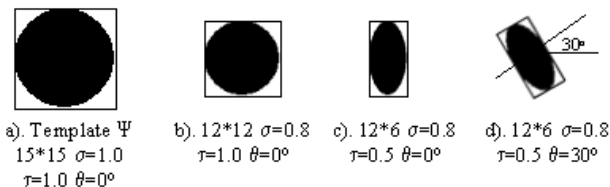


Figure 2: Texton examples at different scales, shears, and orientations.

We define all the distinct textons in layer i as a “texton map”

$$\mathbf{T}_i = (n_i, \{T_{ij}, j = 1 \dots n_i\}), i = 1 \dots L,$$

where n_i is the number of textons in layer i .

In each layer, the texton map \mathbf{T}_i and the template Ψ_i generate an image $\mathbf{I}_i = \mathbf{I}(\mathbf{T}_i; \Psi_i)$ deterministically. If several textons overlap at site (x, y) in \mathbf{I}_i , the pixel value is averaged as

$$\mathbf{I}_i(x, y) = \frac{\sum_{j=1}^{n_i} \delta((x, y) \in D_{ij}) \mathbf{I}_{D_{ij}}(x, y)}{\sum_{j=1}^{n_i} \delta((x, y) \in D_{ij})},$$

where $\delta(\bullet) = 1$ if \bullet is true, otherwise $\delta(\bullet) = 0$. In image \mathbf{I}_i , pixels not covered by the textons are transparent. Then the final image \mathbf{I} is generated by the following model as

$$\mathbf{I} = \mathbf{I}(\mathbf{T}_1; \Psi_1) \otimes \mathbf{I}(\mathbf{T}_2; \Psi_2) \otimes \dots \otimes \mathbf{I}(\mathbf{T}_L; \Psi_L) + \mathbf{n}. \quad (2)$$

The symbol \otimes denotes occlusion or linear addition, i.e. $\mathbf{I}_1 \otimes \mathbf{I}_2$ means \mathbf{I}_1 occludes \mathbf{I}_2 . In this generative model, the hidden variables are

$$\mathbf{T} = (L, \{(\mathbf{T}_i, d_i) : i = 1, 2, \dots, L\}, \mathbf{n}),$$

where d_i indexes the order (or relative depth) of the i -th layer. The pixel value at site (x, y) in the image \mathbf{I} is the same as the toppest layer image at that point, while uncovered pixels are only modeled by noises.

To simplify computation, we assume that $L = 2$ and the two stochastic layers, called “background” and “foreground”, are independent of each other. We find that this assumption holds true for most of the texture patterns. Thus we study the mixture model for image \mathbf{I} .

$$\begin{aligned} p(\mathbf{I}; \Theta) &= \int p(\mathbf{I}|\mathbf{T}; \Psi) p(\mathbf{T}; \beta) d\mathbf{T} \\ &= \int p(\mathbf{I}|\mathbf{T}_1, \mathbf{T}_2; \Psi) \prod_{i=1}^2 p(\mathbf{T}_i; \beta_i) d\mathbf{T}_1 d\mathbf{T}_2 dd_1 dd_2, \quad (3) \end{aligned}$$

where $\Theta = (\Psi, \beta)$ with $\Psi = (\Psi_1, \Psi_2)$ and $\beta = (\beta_1, \beta_2)$, and d_1 and d_2 denote the layer order (background or foreground). The model $p(\mathbf{I}|\mathbf{T}_1, \mathbf{T}_2; \Psi)$ is simply Gaussian distributed as

$$p(\mathbf{I}^{\text{obs}}|\mathbf{T}_1, \mathbf{T}_2; \Psi) \propto \exp \frac{-\|\mathbf{I}^{\text{obs}} - \mathbf{I}(\mathbf{T}_1, \mathbf{T}_2; \Psi)\|^2}{2\sigma^2}, \quad (4)$$

where $\mathbf{I}(\mathbf{T}_1, \mathbf{T}_2; \Psi)$ is the *reconstructed image* from the hidden layers without noise (see eq. (2)).

$p(\mathbf{T}_i; \beta_i), i = 1, 2$ are also exponential models which characterize the spatial relationships through a set of feature statistics. The details are discussed in the next subsection.

3.2 A descriptive model of texton map

The construction of descriptive model for texton maps follows the minimax entropy learning paradigm[15]. We only briefly discuss it and refer to a companion paper for detailed study[2].

For a given texton map \mathbf{T}_i with n_i elements, we first define some neighborhood structures for each texton, and measure a set of features which characterize important spatial relationship between each elements in a local neighborhood. For example, the orientation and scale of a single texton, the distance and

relative orientations and sizes of two neighboring textons. We then calculate the histograms of these features $H_j(\mathbf{T}_i), j = 1, 2, \dots, K$.

A Gibbs (maximum entropy) model is then obtained by descriptive method[15],

$$p(\mathbf{T}_i; \beta_i) = \frac{1}{Z(\beta_i)} \exp\{-\beta_{i0}n_i - \sum_{j=1}^K \langle \beta_{ij}, H_j(\mathbf{T}_i) \rangle\}.$$

In $p(\mathbf{T}_i; \beta_i)$, β_{i0} controls the density of textons n_i on a given unit area, and $\beta_{ij}, j = 1, 2, \dots, K$ are vector valued Lagrange multipliers.

$p(\mathbf{T}_i; \beta_i)$ governs a texton ensemble which corresponds to a so-called grand-canonical ensemble in statistical mechanics. It can be simulated by a Markov chain Monte Carlo algorithm which utilizes Gibbs sampler for the position, scale, shear, and orientation of the textons and also reversible jumps[5] which simulate the death/birth of textons. The selection of important features is done by the minimum entropy principle[15].

Of course, the entire descriptive learning is an ML-estimator that maximizes the log-likelihood by steepest ascent,

$$\beta^* = \arg \max \log p(\mathbf{T}_i; \beta_i); \quad \frac{\log p(\mathbf{T}_i; \beta_i)}{\partial \beta_i} = 0. \quad (5)$$

3.3 The Integrated Learning Paradigm

To learn a generative model $p(\mathbf{I}; \Theta)$ in eq. (3), we follow the ML-estimate in eq. (1).

$$\Theta^* = \arg \max_{\Theta \in \Omega_K} \log p(\mathbf{I}^{\text{obs}}; \Theta).$$

The parameters Θ include both the texton templates Ψ_i and the Lagrange multipliers $\beta_i, i = 1, 2$ for the Gibbs model at each layer of texton map.

$$\Theta = (\Psi, \beta), \quad \Psi = (\Psi_1, \Psi_2), \quad \text{and} \quad \beta = (\beta_1, \beta_2).$$

Note that Θ characterizes the visual pattern and the whole ensemble governed by $p(\mathbf{I}, \mathbf{T}; \Theta)$, while \mathbf{T} is associated with only an image instance \mathbf{I} .

To maximize the log-likelihood, we take the derivative with respect to Θ , and set it to zero. Let $\mathbf{T} = (\mathbf{T}_1, \mathbf{T}_2)$,

$$\begin{aligned} & \frac{\partial \log p(\mathbf{I}^{\text{obs}}; \Theta)}{\partial \Theta} \\ &= \int \frac{\partial \log p(\mathbf{I}^{\text{obs}}, \mathbf{T}; \Theta)}{\partial \Theta} p(\mathbf{T}|\mathbf{I}^{\text{obs}}; \Theta) d\mathbf{T} \\ &= \int \left[\frac{\partial \log p(\mathbf{I}^{\text{obs}}|\mathbf{T}; \Psi)}{\partial \Psi} + \sum_{i=1}^2 \frac{\partial \log p(\mathbf{T}_i; \beta_i)}{\partial \beta_i} \right] \\ & \quad p(\mathbf{T}|\mathbf{I}^{\text{obs}}; \Theta) d\mathbf{T} \\ &= E_{p(\mathbf{T}|\mathbf{I}^{\text{obs}}; \Theta)} \left[\frac{\partial \log p(\mathbf{I}^{\text{obs}}|\mathbf{T}; \Psi)}{\partial \Psi} + \sum_{i=1}^2 \frac{\partial \log p(\mathbf{T}_i; \beta_i)}{\partial \beta_i} \right] \end{aligned}$$

$$= 0. \quad (6)$$

In the literature, there are two well-known methods for solving the above equations. One is the EM algorithm[3], and the other is data augmentation[14]. We propose to use a stochastic gradient algorithm[6] which is more effective than the EM-algorithm and data augmentation.

A Stochastic Gradient Algorithm

Step 0. Initialize the hidden layers \mathbf{T} and the templates Ψ from \mathbf{I}^{obs} using a data driven (clustering) method discussed in the next section. Set $\beta = 0$.

Step I. Given current $\Theta = (\Psi, \beta)$, it *samples typical* texton maps from the posterior probability $\mathbf{T}^{\text{syn}} = (\mathbf{T}_1^{\text{syn}}, \mathbf{T}_2^{\text{syn}}, d_1, d_2) \sim p(\mathbf{T}|\mathbf{I}^{\text{obs}}; \Theta)$. This is the Bayes *perceptual inference*. The sampling process is realized by a Monte Carlo Markov chain which simulates a random walk with two types of dynamics.

- I.a). A *diffusion dynamics* realized by a Gibbs sampler — sampling (relaxing) the transform group for each texton. For example, move textons in locations, scale and rotate them etc.
- I.b). A *jump-dynamics* — adding or removing a texton (death/birth) by reversible jumps[5] using Metropolis-Hastings method. Also the layer order d_1 and d_2 are sampled between background and foreground.

Step II. We treat \mathbf{T}^{syn} as “observation”, and estimate the integration in eq. (6) by importance sampling. Thus we have

$$\frac{\partial \log p(\mathbf{I}^{\text{obs}}|\mathbf{T}; \Psi)}{\partial \Psi} + \sum_{i=1}^2 \frac{\partial \log p(\mathbf{T}_i; \beta_i)}{\partial \beta_i} = 0$$

We learn $\Theta = (\Psi, \beta)$ the texton and Gibbs model respectively by gradient ascent in two steps.

- II.a). Computing the texton templates Ψ by maximizing $\log p(\mathbf{I}^{\text{obs}}|\mathbf{T}^{\text{syn}}; \Psi)$, and this is often done by regression. In our experiment, each texton is represented by a 15×15 window with 225 unknowns. Also each point in the window could be transparent, and thus the shape of the texton could change during the learning process.
- II.b). Computing $\beta_i, i = 1, 2$ by maximizing $\log p(\mathbf{T}_i^{\text{syn}}; \beta_i)$. This is exactly the maximum entropy learning process in descriptive method (see eq. (5)).

The algorithm iterates steps I and II. If the learning rate in steps II.a and II.b is slow enough, the expectation is estimated by importance sampling through samples \mathbf{T}^{syn} over time. It has been proved in statistics[6] that such algorithm converges to the optimal Θ if the step size in step II satisfies some mild conditions.

In summary, the authors feel that the following observations are especially revealing.

1. Descriptive models and descriptive method are inherent part (Step II.b) in generative models and generative method. Existing generative models, such as image coding have weak (iid) descriptive models instead of the Gibbs model and this limits their expressive power.

2. Bayesian vision inference is a sub-task (step I) of generative learning.

3.4 Initialization by Data Clustering

Both the hidden texton maps $\mathbf{T} = (\mathbf{T}_1, \mathbf{T}_2)$ and the texton templates $\Psi = (\Psi_1, \Psi_2)$ need to be initialized in order to start the bootstrap procedure in the previous section. In this section, we present a stochastic algorithm to obtain the initial \mathbf{T}^0 and Ψ^0 by decoupling some variables with two simplifications from the model in eq. (3).

Firstly, we decouple the texton elements in the prior $p(\mathbf{T}_i; \beta_i)$. In the two texton maps \mathbf{T}_1 and \mathbf{T}_2 , $n_1 + n_2$ is fixed to an excessive number, thus we don’t need to simulate the death-birth process. β_1 and β_2 are set to be 0, therefore $p(\mathbf{T}_i; \beta_i)$ becomes a uniform distribution and all texton elements are decoupled from interactions.

Secondly, we further decouple the texton elements in the likelihood $p(\mathbf{I}^{\text{obs}}|\mathbf{T}; \Psi)$. Instead of using the image generating model in eq. (2) which implicitly imposes couplings between texton elements through eq. (4), we adopt a constraint-based model

$$p(\mathbf{I}^{\text{obs}}|\mathbf{T}, \Psi) \propto \exp\left\{-\sum_{i=1}^2 \sum_{j=1}^{n_i} \|\mathbf{I}_{D_{ij}}^{\text{obs}} - G[T_{ij}] \odot \Psi_i\|^2 / 2\sigma^2\right\}, \quad (7)$$

where $\mathbf{I}_{D_{ij}}^{\text{obs}}$ is the image patch of the domain D_{ij} in the observed image. For pixels in \mathbf{I}^{obs} not covered by any textons, a uniform distribution is assumed to introduce a penalty.

So far all the textons are decoupled of each other by simplifying the generative model of eq. (3) to eq. (7) without the integration of \mathbf{T} . Consequentially the searching problem of \mathbf{T}^0 and Ψ^0 turns into a conventional clustering issue.

We start with random texton maps and the algorithm iterates the following two steps. I). Given Ψ_1 and Ψ_2 , it runs a Gibbs sampler to change each texton

T_{ij} respectively, by moving, rotating, scaling the rectangle, and changing the cluster into which each texton falls according to the simplified model of eq. (7). Thus the texton windows intend to cover the entire observed image, and at the same time try to form tight clusters around Ψ . II). Given \mathbf{T}_1 and \mathbf{T}_2 , it updates the texton Ψ_1 and Ψ_2 by averaging as

$$\Psi_i = \frac{1}{n_i} \sum_{j=1}^{n_i} G^{-1}[T_{ij}] \odot \mathbf{I}_{D_{ij}}^{\text{obs}}, \quad i = 1, 2,$$

where $G^{-1}[T_{ij}]$ is the inverse transformation. The layer order d_1 and d_2 are not needed for the simplified model.

This initialization algorithm for computing (T^0, Ψ^0) resembles transformed component analysis (TCA). It is also inspired by a clustering algorithm by (Leung and Malik, 1999)[9], which did not engage hidden variables, and thus compute a variety of textons Ψ at different scale and orientations. We also experimented with representing the texton template Ψ by a set of Gabor bases instead of a 15×15 window. However, the results were not encouraging.

4 Experiments

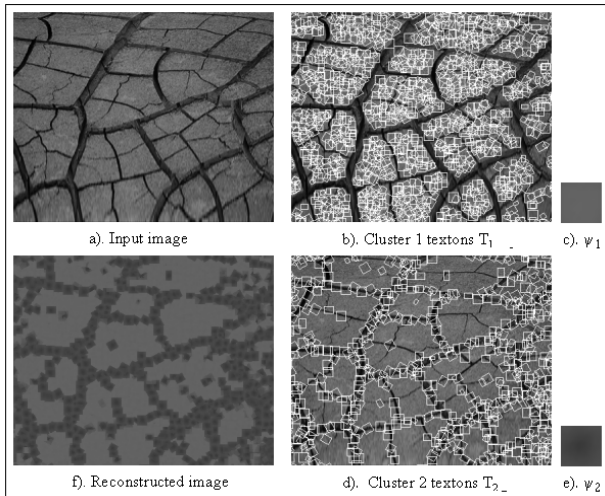


Figure 3: Result of the initial clustering algorithm.

Experiment I: Initialization by Clustering. Fig. 3 shows an experiment on the initialization algorithm for a crack pattern. 1055 textons are used with the template size of 15×15 . The number of textons is as twice as necessary to cover the whole image. In optimizing the likelihood in eq. (7), an annealing scheme is utilized with the temperature decreasing from 4 to 0.5. The sampling process converged to a result shown in Fig. 3.

Fig. 3.a is the input image; Figs 3.b and Figs 3.d are the texton maps \mathbf{T}_1 and \mathbf{T}_2 of two clusters respectively. Fig. 3.c and Fig. 3.e are the cluster centers Ψ_1 and Ψ_2 , shown by rectangles respectively. Fig. 3.f is the reconstructed image. The results demonstrate that the clustering method provides a rough but reasonable starting solution for generative modeling.

Experiment II: Integrated Learning

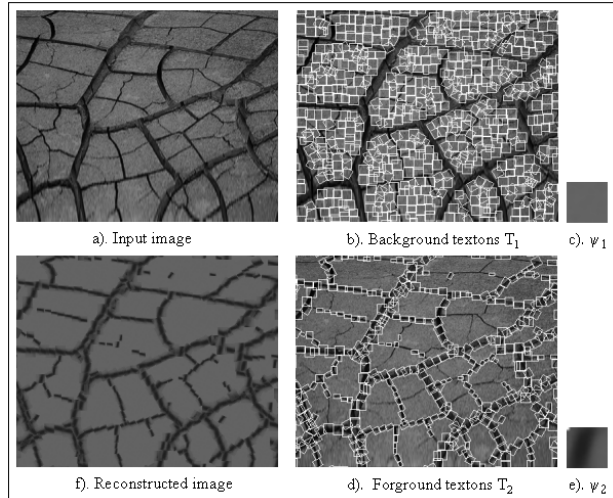


Figure 4: Generative model learning result for the dry land image. a) input image, b) and d) are background and foreground textons discovered by the generative model, c) and e) are the templates for the generative model, f) is the reconstructed image from the generative model.

Fig. 4 shows the result for the crack image obtained by the stochastic gradient algorithm, following the initial solution shown in Fig. 3. It took about 80 iterations of the two steps. Fig. 4.b and Fig. 4.d are the background and foreground texton maps \mathbf{T}_1 and \mathbf{T}_2 respectively. Fig. 4.c and Fig. 4.e are the learned textons Ψ_1, Ψ_2 respectively. Fig. 4.f is the reconstructed image from learned textons and templates. Compared to the results in Fig. 3, the results in Fig. 4 have more precise texton maps and texton templates due to an accurate generative model. The foreground texton Ψ_2 is a bar, and one pixel at corner of the left-top is transparent.

The integrated learning results for a cheetah skin image are shown in Fig. 5. It can be seen that in the foreground template, the surround pixels are transparent and the blob is exactly figured out as the texton. The bars in a cloth image of Fig. 6 are captured as textons with the corners of the cloth template being rounded by transparency. Fig. 7 are the results for a brick image. No point in the template is transparent for the gap lines between bricks. An example of a pine

corn image is shown in Fig. 8. The seeds and the black intervals are separated cleanly, and the reconstructed image keeps most of the pine structures. However the pine corn seeds are learnt as the background textons and the gaps between pine corns are treated as foreground textons.

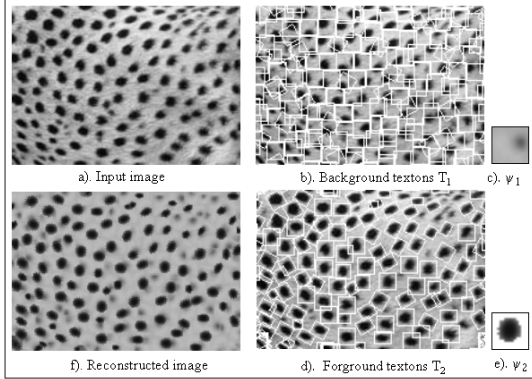


Figure 5: Generative model learning result for a cheetah skin image. The notations are the same as in Fig. 4.

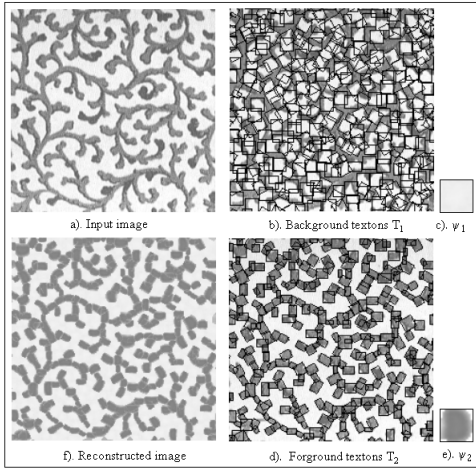


Figure 6: Generative model learning result for a cloth image. The notations are the same as in Fig. 4.

Experiment III: Random texture sampling and synthesis.

After the parameters Ψ and β of a generative model are discovered for a type of texture images, new random samples could be drawn from the generative model. This proceeds in three steps: Firstly, texton maps are sampled from the Gibbs models $p(\mathbf{T}_1; \beta_1)$ and $p(\mathbf{T}_2; \beta_2)$ respectively. Secondly, background and foreground images are synthesized from the texton maps and texton templates. Thirdly, the final image is generated by combining these two images according to the

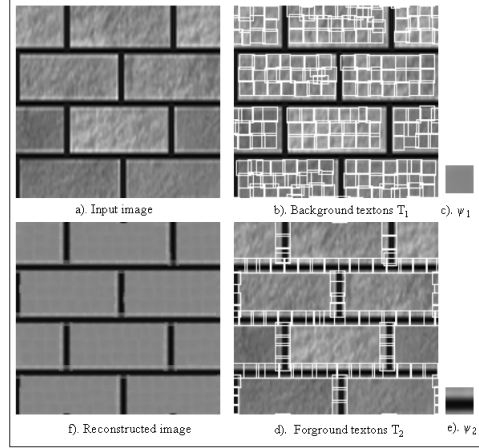


Figure 7: Generative model learning result for a brick image. The notations are the same as in Fig. 4.

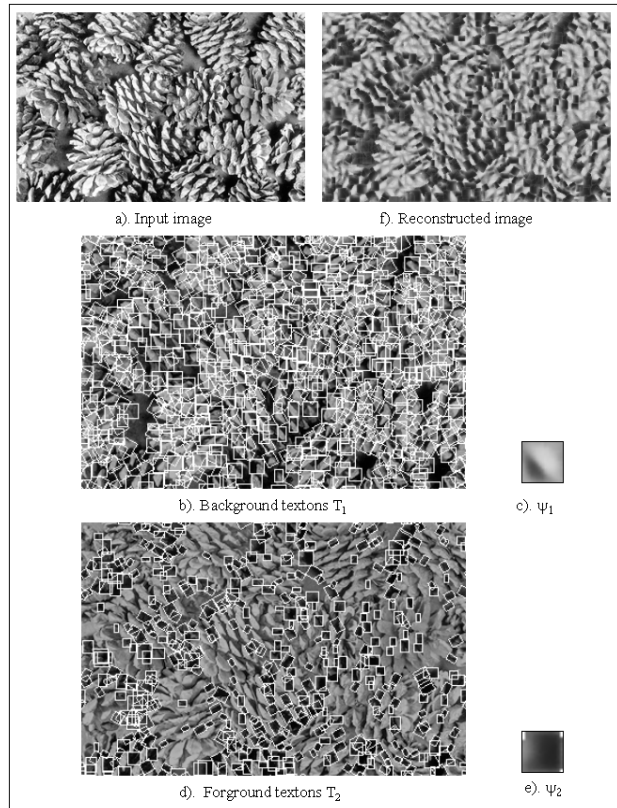


Figure 8: Generative model learning result for a pine corn image. The notations are the same as in Fig. 4.

occlusion model. Fig 9 and Fig. 10 are two examples of the two layered model synthesis for the cheetah skin pattern. The templates used here are the learned results in Fig 5.

The lighting condition is not considered in current

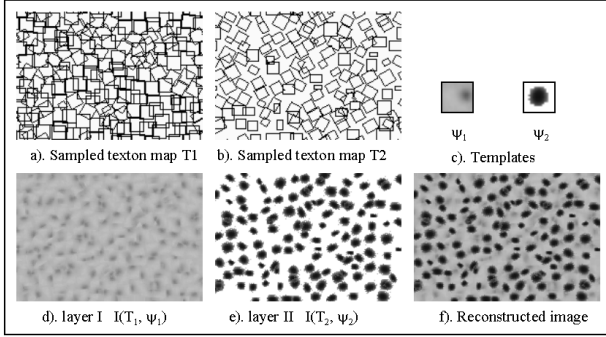


Figure 9: An example of a randomly synthesized cheetah skin image. a) and b) are the background and foreground texton maps sampled from $p(\mathbf{T}_i; \beta_i)$; d) and e) are synthesized background and foreground images from the texton map and templates in c); f) is the final random synthesized image from the generative model.

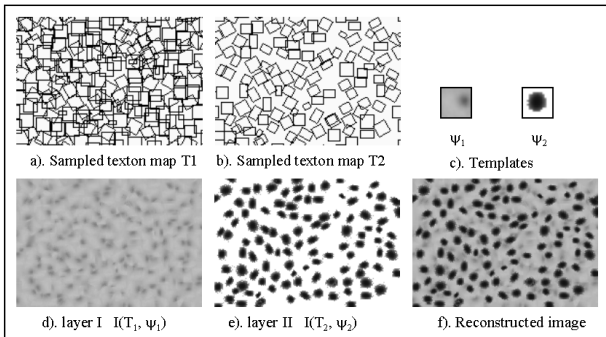


Figure 10: Another example of a randomly synthesized cheetah skin image. Notations are the same as in Fig. 9.

experiments. For some texture images, e.g. the cheetah skin image and the pine corn image, the lighting globally changes. However, such information is lost in the generative model results. Future experiments will pay attention to this issue.

5 Discussion

The generative method has advantages over previous descriptive method with Markov random fields on pixel intensities.

I). In representation: The neighborhood in the texton map are much smaller than the pixel neighborhood in previous descriptive model [15]. The generative method captures more semantically meaningful features on the texton map.

II). In computation: The Markov chain operating in the texton map can move blobs according to affine transforms and can add or delete a blob through death/birth dynamics, and thus is much more effec-

tive than the Markov chain used in traditional Markov random fields which flips one pixel intensity at a time.

Furthermore we show that the integration of descriptive and generative methods is a natural and inevitable path for visual learning. We argue that a vision system should evolve by progressively replacing descriptive models with generative models, which realizes a transition from *empirical and statistical models* to *physical and semantical models*. The work presented in this paper provides a step towards this goal.

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