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PHYSICAL CONSTANTS

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PHYSICAL CONSTANTS.

A. Distances (in cm)

SYMBOL	FORMULA	MEANING	VALUE
r_0	e^2/mc^2	clas. radius of elect.	2.8183×10^{-13}
λ_0	$\hbar/mc$	Compton wavelength	3.8619×10^{-11}
a_0	$\hbar^2/mc^2$	first Bohr radius	5.2920×10^{-9}
d_{20°	-----	calcite grating space, 20°	3.0357×10^{-8}
---	-----	internuclear distance in H_2	0.7414×10^{-8}

Table of wavelengths for various energies.
For the electron, proton, and neutron $\lambda = \hbar/p$ is given, while for the photon λ itself is given.

E	kT_{20°	1 ev	1 Mev
Electron	12.280×10^{-8}	1.9518×10^{-8}	1.3875×10^{-11}
Proton	$.28655 \times 10^{-8}$	$.045543 \times 10^{-8}$	4.5531×10^{-13}
Neutron	$.28635 \times 10^{-8}$	$.045512 \times 10^{-8}$	4.5501×10^{-13}
Photon	.0049068	$12,395.4 \times 10^{-8}$	$.012395 \times 10^{-8}$

B. Velocities (in cm/sec)

	v	$\beta = v/c$
C = velocity of light in vacuo	2.99776×10^{10}	1
$V_0 = e^2/\hbar$ = velocity of electron in first Bohr orbit	2.1877×10^8	.0072977
Velocity of electron with energy of kT_{20°	9.4277×10^6	.00031449
1 ev	5.9317×10^7	.0019787
1 Mev	2.8212×10^{10}	.94110

	v	$\beta = v/c$
Velocity of proton with energy of kT_{20°	2.1999×10^5	7.3384×10^{-6}
1 ev	1.3841×10^6	4.6172×10^{-5}
1 Mev	1.3830×10^9	.046135
Initial velocity of a RaC' alpha particle	1.9215×10^9	.064098

C. Dimension-less Constants

$$\alpha = \text{fine - structure constant} = e^2 / \hbar c = .0072977 = 1/137.030$$

$$M_p/m = \text{ratio of masses of proton and electron} = 1836.5_-$$

D. Energy and Mass.

$$\text{Energy of repulsion of two electrons one cm. apart} = 1.4397 \times 10^{-7} \text{ ev.}$$

$$\begin{aligned} kT_{0^\circ\text{C}} &= 0.02354 \text{ ev} = 3.771 \times 10^{-14} \text{ erg} \\ kT_{15^\circ\text{C}} &= 0.02483 \text{ ev} = 3.978 \times 10^{-14} \text{ erg} \\ kT_{20^\circ\text{C}} &= 0.02526 \text{ ev} = 4.047 \times 10^{-14} \text{ erg} \end{aligned} \quad \begin{array}{l} \text{(electron} \\ \text{volts are} \\ \text{absolute)} \end{array}$$

$$mc^2 = \text{rest energy of electron} = 0.51083 \text{ Mev} = 8.1837 \times 10^{-7} \text{ erg}$$

$$E_0 = me^4/\hbar^2 = e^2/a_0 = mc^2 \times \alpha^2 = \text{potential energy of first Bohr orbit} = 27.205_- \text{ ev} = 4.3583 \times 10^{-11} \text{ erg.}$$

I_H = Ionization potential of H^1 =

$$\frac{1}{2} E_0 (1 + \alpha^2/4)(1 + m/M_p) - 1 = 13.595 \text{ ev}$$

Energy of first vibrational quantum of H_2^1
= 0.5150 ev.

Energy of first rotational quantum of H_2^1
= 0.01471 ev

Energy of dissociation of H_2^1 = 4.4776 ev

Initial energy of a Ra C' alpha particle =
7.6802 Mev

	Mass (gm)	At. wt (physical)	Rest energy (Mev)	Mass/m
Electron	9.1066×10^{-28}	0.00054862	0.51083	1
Proton	1.67247×10^{-24}	1.00757	938.17	1836.5
H Atom	1.67338×10^{-24}	1.00812	938.68	1837.5
Neutron	1.67472×10^{-24}	1.00893	939.43	1839.0
Deuteron	3.34330×10^{-24}	2.01416	1875.41	3671.3
Alpha particle	6.64424×10^{-24}	4.00280	3727.07	7296.1
Unit Mass	1.65990×10^{-24}	1	931.12	1822.7
Chemical mass	1.66035×10^{-24}	1.000272	931.37	1823.2

E. Energy Conversion Factors

	abs ev	ergs	cm	cal (15°)	cal/mde
1 ev =	1	1.60203×10^{-12}	8067.49	3.8276×10^{-20}	23,052.8
1 erg =	6.2421×10^{11}	1	5.035×10^{15}	2.3892×10^{-8}	1.4390×10^{16}
1 cm =	1.2395×10^4	1.9858×10^{16}	1	4.7444×10^{-24}	2.8575
1 cal (15°) =	2.6126×10^{19}	4.1855×10^7	2.107×10^{23}	1	6.0228×10^{23}
1 erg/mole =	1.0364×10^{12}	1.6603×10^{-24}	8.3612×10^{-9}	3.9669×10^{-32}	2.3892×10^{-8}
1 cal/mole =	4.3379×10^{-5}	6.9494×10^{-17}	0.3495	1.6603×10^{-24}	1

F. Miscellaneous

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$$e = \text{charge of electron} = 4.8025 \times 10^{-10} \text{ abs esu} \\ = 1.60203 \times 10^{-20} \text{ abs emu.}$$

$$e^2 = 1.4397 \times 10^{-7} \text{ abs ev cm} = 2.3064 \times 10^{-19} \\ (\text{abs esu})^2 = 2.56650 \times 10^{-40} (\text{abs emu})^2$$

$$e^4 = 5.31948 \times 10^{-38} (\text{abs esu})^4$$

$$e/m = \text{"specific" electron charge} = 1.7592 \times 10^7 \\ \text{emu/gm} = 5.2737 \times 10^{17} \text{ esu/gm}$$

$$e/h = 7.2499 \times 10^{16} \text{ esu/erg sec} = 2.4185 \times 10^6 \\ \text{emu/erg sec.}$$

$$h = \text{Planck's constant} = 6.624_2 \times 10^{-27} \text{ erg sec} \\ = 4.134_9 \times 10^{-15} \text{ ev sec.}$$

$$\hbar = h/2\pi = 1.0543 \times 10^{-27} \text{ erg sec} = 6.580_8 \times 10^{-16} \\ \text{ev sec.}$$

$$\pi = 3.1415927, \quad 2\pi = 6.2831853$$

$$\pi^2 = 9.8696044, \quad 2\pi^2 = 19.7392088$$

$$4\pi = 12.5663706, \quad 4\pi^2 = 39.4784176$$

$$1/\pi = 0.3183099, \quad 1/2\pi = 0.1591549$$

$$1/4\pi = 0.0795775$$

$$\pi/2 = 1.5707963, \quad \pi/4 = 0.7853982$$

$$\epsilon = 2.71828 \quad 18285$$

$$\text{Log}_\epsilon 10 = 2.30258509$$

$$hc = 1.23954 \times 10^{-4} \text{ ev cm} = 1.98578 \times 10^{-16} \text{ erg cm}$$

$$\hbar/m = 1.1577 \text{ erg sec/gm.}$$

$$T_0 = \text{Temperature of "absolute zero"} = -273.16^\circ\text{C}$$

$$A_0 = \text{Pressure of standard atmosphere} \\ = 1.0132 \times 10^6 \text{ dynes/cm}^2$$

F = Faraday constant = 96,501 Coulombs per gram equivalent.

R = Gas constant = 8.31436 joules/mole degree
 = 1.98647 cal/mole deg.
 = 8.20545×10^{-2} liter atm/mole degree

K = Boltzmann constant = 1.38047×10^{-16}
 erg/deg = 3.2982×10^{-24} cal/deg
 = 8.6170×10^{-5} ev/deg.

k/h = 2.0840×10^{10} /deg sec.

k/hc = 0.69518/deg cm

hc/k = 1.4385 deg cm = second radiation constant.

μ = Bohr (atomic) magneton = $e\hbar/2mc$ =
 9.273×10^{-21} erg/gauss

μ_n = Bohr (nuclear) magneton = $e\hbar/2M_p C$ =
 5.049×10^{-24} erg/gauss

G = Gravitational constant = 6.670×10^{-8}
 dyne cm/gram²

g_0 = Acceleration due to gravity (stand.)
 = 980.665 cm/sec²

G. Number of Molecules

		NO	LOG ₁₀
No	Avogadro's no.; 1 mole	6.0228×10^{23}	23.77980
no	Loschmidt's no.; lcc of ideal gas at 0°C, 1 atm	2.6870×10^{19}	19.42927
--	lcc of ideal gas at 15°C, 1 atm	2.5471×10^{19}	19.40605
--	lcc of ideal gas at 20°C, 1 atm	2.5037×10^{19}	19.39858
--	lcc of dry air (MW = 28.967) at 15°C, 1 atm	2.5483×10^{19}	19.40625

H. Volumes

Vol. of 1 mole ideal gas, 0° C, 1 atm = 22,414.6 cc

" " " " " " 15° C, 1 atm = 23,645 "

" " " " " " 20° C, 1 atm = 24,056 "

" " " " dry air, 15° C, 1 atm = 23,635 "

I. Time (in seconds)

τ_0 = period of first Bohr orbit = $2\pi a_0 / v_0$

$$= 2\pi \hbar^3 / me^4 = 1.5198 \times 10^{-16}$$

t_0 = time required for light to move a distance of one classical electron

$$\text{radius} = e^2 / mc^3 = 9.4013 \times 10^{-24}$$

J. Frequencies (in reciprocal seconds)

$$1/\tau_0 = me^4 / 2\pi \hbar^3 = 6.5798 \times 10^{15}$$

$$R_{\infty} C = me^4 / 4\pi \hbar^3 = 3.28988 \times 10^{15}$$

K. Wave Numbers (in reciprocal cm)

S_0 = wave no. of photon of lev energy
= 8067.5

$k T_{20^\circ} / hc$ = wave no. of photon at thermal energy = 203.80

R_H = Rydberg constant for H^1 = 109,677.581

R_D = " " " H^2 = 109,707.419

R_{He} = " " " He^4 = 109,722.263

R_{∞} = " " " infinite mass
= 109,737.303

L. Some Fundamental Quantities Expressed in Various Systems of Units.

		C.G.S.	Electron	Atomic (Hartree)
Mass	Mass of Electron	m	1	1
	Mass of Proton	M_p	1836.5	1836.5
Length	Radius of Electron	$e^2/mc^2 = r_0$	1	$1/137^2$
	Radius of H Atom	$\hbar^2/me^2 = a_0$	137^2	1
	Compton wavelength	$\hbar^2/mc = \lambda_0$	137	$1/137$
Time	Time required for light to pass r_0	$e^2/mc^3 = t_0$	1	$1/137^3$
	Period of first Bohr orbit	$2\pi\hbar^3/me^4 = t_0$	$137^3 2\pi$	2π
Energy	Rest energy of electron	mc^2	1	137^2
	Potential energy of H Atom	$me^4/\hbar^2 = E_0$	$1/137^2$	1
Velocity	Velocity of light	c	1	137
	Velocity of Is II electron	$e^2/\hbar = v_0$	$1/137$	1
Frequency	$1/t_0$	mc^3/e^2	1	137^3
	$1/t_0$	$me^4/2\pi\hbar^3$	$1/137^3 2\pi$	$1/2\pi$
Angular Momentum	-----	e^2/c	1	$1/137$
	Planck's constant	$\hbar$	137	1
Electric Charge	Charge of electron	e	1	1
Momentum		mc	1	137
		$me^2/\hbar$	$1/137$	1