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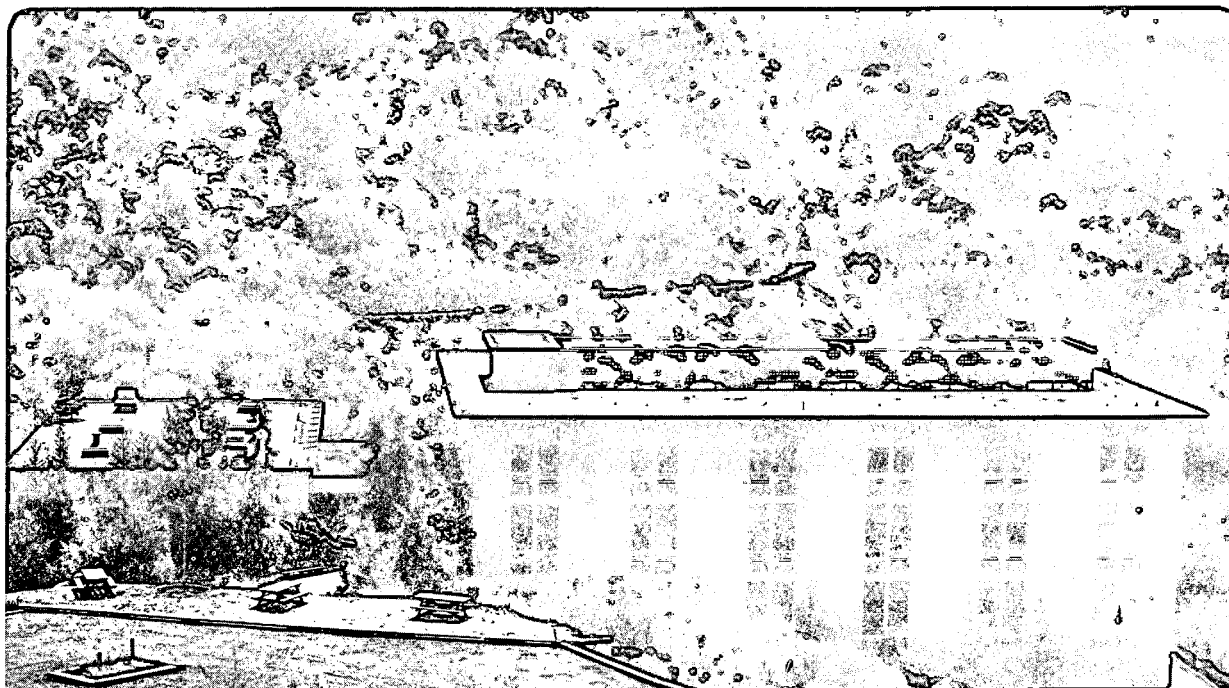
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Surface Diffusion Studies by Optical Diffraction Techniques

X.-D. Xiao
(Ph.D. Thesis)

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**SURFACE DIFFUSION STUDIES BY OPTICAL
DIFFRACTION TECHNIQUES**

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Ph.D. Thesis

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Abstract

Surface Diffusion Studies By Optical Diffraction Techniques

by

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Doctor of Philosophy in Physics

University of California at Berkeley

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Optical techniques have been proven to be powerful tools for surface studies. In this thesis, we have presented the newly developed techniques with either second harmonic (SH) diffraction or linear diffraction off a monolayer adsorbate grating for surface diffusion measurement. Their development will change the situation with surface diffusion field, which has been impeded by the lack of convenient and powerful measurement methods. The anisotropy of surface diffusion of CO on Ni(110) has been used as a demonstration for the second harmonic diffraction method. The linear diffraction method, which possesses a much higher sensitivity than the SH diffraction method, has been employed to study the effect of adsorbate-adsorbate interaction on CO diffusion on Ni(110) surface. The results unambiguously showed that only the short range direct CO-CO orbital overlapping interaction influences CO diffusion but not the long range dipole-dipole and CO-Ni-CO interactions. Effects of impurities and defects on surface diffusion have been further explored by using the linear diffraction method on the CO/Ni(110) system. It has been found that a few percent S impurity can alter the CO diffusion barrier height to a much higher value through changing the Ni(110) surface. The point defects of Ni(110)

surface seem to speed up CO diffusion significantly. A mechanism with long jumps over multiple lattice distance initiated by CO filled vacancy has been proposed to explain the observed defect effect.

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I never could have dreamed of receiving a Ph. D. degree if there had not been political changes in China in 1979. The cultural revolution once terminated my highest level of education at middle school. I cannot deny my gratitude for a life that put me at the right time, in the right place, and with the right people.

Most of the children in my village lost their opportunities for education before entering middle school. It was my parents, who themselves did not have higher education, who encouraged and supported me to be exposed to higher and higher education. They would never have believed that in ten years, their son would leave his village forever. I want to express my warmest gratitude and love to my parents and wish someday I could be with them to truly compensate for their emotional loss due to my years abroad.

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I. General Introduction

Surface science has been progressed enormously in the last two decades. A variety of surfaces have been investigated. In particular, many aspects of crystalline surfaces such as surface relaxation, surface reconstruction¹⁻⁸, kinetics of adsorption and desorption of foreign particles⁹⁻¹⁷, and chemical reactions on surfaces¹⁸⁻²³ have been intensively studied with a number of powerful techniques. Considerable activity in surface diffusion has also been undertaken in the last 10 years²⁴⁻²⁶. In contrast to the other subfields of surface science, however, surface diffusion is less explored and less understood.

Surface diffusion is a subject that studies stochastic motion of adparticles on surfaces. As is well known, surfaces have two dimensional periodic structures and a particle, atom or molecule, adsorbed on a surface sees a periodic potential. Most of the time the adparticle resides at a local minimum of the potential -- the adsorption site. Occasionally this adparticle jumps from one adsorption site to another in a random walk fashion through the interaction with the substrate phonons and electrons without leaving the surface. The adparticle's random motion is usually characterized by a quantity loosely called the surface diffusion coefficient.

There are two distinctive classes of surface diffusion. The first one is concerned with a single adparticle random motion and is described by tracer diffusion coefficient D^* . The second one is concerned with random motion of a macroscopic number of adparticles and is described by chemical diffusion coefficient D^{24} . The first one is the limit of the second at zero coverage. Much effort has been devoted to tracer diffusion by field ion microscopy (FIM) and

other techniques²⁶. Theoretical studies of tracer diffusion are coming into maturity as well. On the other hand, chemical diffusion study has just been started, especially in theory. The existing experimental techniques for chemical surface diffusion study are limited one way or another and a consistent picture of chemical surface diffusion has not been formed yet.

Apart from the fundamental interests of searching for surface diffusion mechanisms and measuring surface potential corrugations, surface diffusion is practically important for surface catalysis, crystal growth, and material fabrication. For example, the hydrogenation reaction of $\text{CO(a)} + \text{H(a)} \rightarrow \text{CH}_4\text{(g)} + \text{CO}_2\text{(g)}$ on catalysts such as Ni²⁷ relies on the mobilities of these two reactants and are likely controlled by their surface diffusions. Therefore, surface diffusion measurements for single species system as well as for mixed species system are of primary importance in understanding the reaction mechanism.

In this thesis we will first briefly review the status of the surface diffusion theory for both tracer diffusion and chemical diffusion. Despite some interesting features revealed by the theories, most of these theories are phenomenological in treating the interactions between the adparticle and the substrate as well as the interactions among the adparticles. There, we will see what still needs to be done in order to have a better understanding of surface diffusion. The experimental techniques of surface diffusion measurements will be summarized in the same chapter (chapter II) with a discussion on the limitations of each method. To overcome the limitations of these existing techniques, we have devoted our effort in developing new surface diffusion measurement techniques in the past few years and have successfully applied the new techniques to study anisotropy, coverage dependence, and impurity and defect effects of surface diffusion for CO of Ni(110).

The new techniques we have developed are based on the following

principles. First, an adsorbate grating is created by laser induced thermal desorption (LITD) with two laser beams interfering at an adsorbate-covered solid surface. With this initial coverage profile, diffraction (linear or nonlinear) off the grating of a probing laser beam is then used to monitor the time evolution of the coverage profile. The adsorbate grating is expected to get smeared out by surface diffusion and the diffraction signal to decay correspondingly. From the decay time constant of the diffraction signal the diffusion coefficient of the adsorbate can be deduced. The details of these techniques with both SH diffraction and linear diffraction probes will be described in chapter III. These methods bear a number of very attractive features. First, they involve a simple one-dimensional diffusion process for which the data analysis is relatively straightforward. Second, by properly orienting the grating, the diffusion coefficient along any direction on the surface can be directly measured. This makes the anisotropic diffusion measurement very easy. Third, as an optical method, the technique can be applied to a wide variety of adsorbates on any substrate. Fourth, with a tunable probe beam selectively probing particular species of adsorbates, surface diffusion of individual components of a mixed adsorbate system can be monitored. This allows the study of influence of surface diffusion on surface reactions such as catalysis. Fifth, the dynamic range can be extremely wide, ranging from 10^{-6} to 10^{-15} cm^2/sec for the diffusion coefficient. Finally, the technique can be used to study other forms of surface diffusion like diffusion of electronic or vibrational excitations.

Surface second harmonic generation (SHG) as a versatile tool for surface and interface studies has been reviewed by a number of authors^{28,29} and has been documented in detail in a number of thesis from the Shen group^{30,31}. The surface specificity of SH process allowed us to develop a

simple, straightforward diffraction scheme off an adsorbate monolayer grating for surface diffusion study^{31,32}. In chapter IV, the anisotropic surface diffusion of CO/Ni(110) will be presented and a number of related issues will be discussed.

Despite its initial success, the SH diffraction technique still has a few limitations. The intrinsic weak response of the SH process prevents us from studying coverage dependence in surface diffusion. The polarization modulated linear diffraction scheme we have developed has lifted these limitations and exploited the full advantages of the optical diffraction technique for surface diffusion study. The coverage dependent diffusion study for CO/Ni(110) will be presented in chapter V. It has been found that only the short range CO-CO direct interaction influences the diffusion of CO on Ni(110), while the long range dipole-dipole interaction and CO-Ni-CO interaction do not.

There exists the question how impurities and defects could affect surface diffusion. In many surface reactions it has been found that impurities and defects can play critical roles. Is this also true for surface diffusion? If so, what are the mechanisms? We have answered these questions to a certain extent by studying CO diffusion on S contaminated Ni(110) surfaces and Ar⁺ sputtered Ni(110) surfaces. The results will be presented in chapter VI. The S impurity has been found to be able to modify substantially the Ni(110) surface even at very low densities and thus alter the CO diffusion activation energy. The defects of Ni(110) surface introduced by Ar⁺ sputtering can also influence CO diffusion. However, the effect is quite different as the diffusion speed actually increases with increase of defects. Mechanism based on long jumps over multiple lattice distance assisted by CO filled vacancy has been proposed to interpret the the observation.

Future prospects will be discussed in Chapter VII. A few important issues

in surface diffusion will be addressed and some interesting experiments will be proposed.

References

- ¹ A. Thomy, X. Dual and J. Regnier, Surf. Sci. Rep. **1**, 1(1981).
- ² A. Kahn, Surf. Sci. Rep. **3**, 193(1983).
- ³ I. P. Ipatova and Yu. E. Kitaev, Prog. Surf. Sci. **18**, 189(1985).
- ⁴ H. Ohtani, C.-T. Kao, M. A. Hove and G. A. Somorjai, Prog. Surf. Sci. **23**, 155(1986).
- ⁵ R. Feidenhans'l, Surf. Sci. Rep. **10**, 105(1989).
- ⁶ S. Pick, Surf. Sci. Rep. **12**, 99(1991).
- ⁷ B. N. J. Person, Surf. Sci. Rep. **15**, 1(1992).
- ⁸ J. P. LaFemina, Surf. Sci. Rep. **16**, 133(1992).
- ⁹ J. Czarniecki and M. Jaroniec, Surf. Sci. Rep. **3**, 301(1983).
- ¹⁰ G. Comsa and R. David, Surf. Sci. Rep. **5**, 145(1985).
- ¹¹ E. Shustorovich, Surf. Sci. Rep. **6**, 1(1986).
- ¹² H. P. Bonzel, Surf. Sci. Rep. **8**, 43(1987).
- ¹³ T. Aruga and Y. Murata, Prog. Surf. Sci. **31**, 61(1989).
- ¹⁴ J. K. Norskov, Rep. Prog. Phys. **53**, 1253(1990).
- ¹⁵ V. P. Zhdanov, Surf. Sci. Rep. **12**, 183(1991).
- ¹⁶ R. D. Ramsier and J. T. Yates, Jr., Surf. Sci. Rep. **12**, 243(1991).
- ¹⁷ S. J. Lombardo and A. T. Bell, Surf. Sci. Rep. **13**, 1(1991).
- ¹⁸ M. P. Kiskinova, Surf. Sci. Rep. **8**, 359(1988).
- ¹⁹ L. K. Doraiswamy, Prog. Surf. Sci. **37**, 1(1991).
- ²⁰ H. F. Winters and J. W. Coburn, Surf. Sci. Rep. **14**, 161(1992).
- ²¹ J. Nishizawa and H. Sakuraba, Surf. Sci. Rep. **15**, 137(1992).
- ²² E. A. Colbourn, Surf. Sci. Rep. **15**, 281(1992).
- ²³ L. J. Richter and R. R. Cavanagh, Prog. Surf. Sci. **39**, 155(1992).

- ²⁴ Robert Gomer, *Rep. Prog. Phys.* **53**, 917(1990).
- ²⁵ A. Kapoor, R. T. Yang, and C. Wong, *Catal. Rev.-Sci. Eng.*, **31**, 129(1989);
A. G. Naumovets and Yu. S. Vedula, *Surf. Sci. Rep.* **4**, 365(1985);
Gert Ehrlich and Kaj Stolt, *Ann. Rev. Phys. Chem.* **31**, 603(1980).
- ²⁶ T. T. Tsong, *Surf. Sci. Rep.* **8**, 127(1988); *Prog. Surf. Sci.* **10**, 165(1980).
- ²⁷ G. A. Somorjai, *Chemistry in Two Dimensions: Surfaces*, (Cornell University Press, Ithaca New York, 1981).
- ²⁸ Y. R. Shen, *Annu. Rev. Phys. Chem.* **40**, 327(1989).
- ²⁹ G. L. Richmond, J. M. Robinson and V. L. Shannon, *Prog. Surf. Sci.* **28**, 1(1988).
- ³⁰ Tony F. Heinz, Ph. D. Thesis, Berkeley, 1984;
Harry K. Tom, Ph. D. Thesis, Berkeley, 1985;
Wei Chen, Ph. D. Thesis, Berkeley, 1990;
Marla B. Feller, Ph. D. thesis, Berkeley, 1991.
- ³¹ X. D. Zhu, Ph. D. Thesis, Berkeley, 1989.
- ³² X. D. Zhu, Th. Raising and Y. R. Shen, *Phys. Rev. Lett.* **61**, 2883(1988).

II. Overview on Recent Development of Surface Diffusion

A. Introduction

As pointed out in Chapter I, surface diffusion is of interest from both basic and technological view points. Theoretical studies of surface diffusion have undergone substantial progress in the past 10 years¹⁻⁴. Analytical and numerical tools have been developed for this purpose. The results obtained so far will be briefly reviewed in the next few sections. The surface diffusion theory can be classified into two categories: one deals with tracer diffusion of a single adparticle; the other deals with chemical diffusion of a large number of adparticles among which interactions may not be negligible.

Experimentally, quite a few techniques have been developed in the last two decades. Using these methods a large base of data on surface diffusion has been accumulated. However, all these techniques have limitations which have prohibited the building of a consistent picture for surface diffusion. Most of these techniques will be discussed in section F. Similar to the theoretical situation, the experimental studies fall into two classes as well. In the first class, tracer diffusion of single adsorbed particles is monitored. In the second class, chemical diffusion of a large number of adparticles is measured.

B. Single Particle Diffusion on Surfaces

An understanding of single particle diffusion on a surface from first principles was achieved early in this century^{5,6}. This was a first step towards

understanding more complicated diffusion. A microscopic picture of the motion of an adsorbed particle, atom or molecule, can be established in terms of interaction between the adparticle and the substrate atoms. The substrate applies not only a two-dimensional periodic static potential but also a random force to the adsorbed particle. It is this dynamic random force that initiates a jump of the adparticle and then damps the motion^{5,7}. The origin of the random force is the thermal vibration of the substrate atoms and the excitation of the substrate electrons⁷. Because of the randomness of the dynamic interaction between the adparticle and the substrate, the motion of the adparticle is essentially Brownian. To understand the nature of surface diffusion it is critical to first understand the nature of these interactions.

In order to describe the motion of the adparticle, models of the dynamic interaction with the substrate (or, the heat bath) must be employed. The very first systematic treatment was due to Kramers⁵, who described the random force from the surroundings (heat bath) by a fluctuating force $\xi(t)$ with a white noise spectrum and a linear damping force $-M\eta\dot{x}$, with η as the friction coefficient and \dot{x} as the velocity. The fluctuating force obeys the fluctuation-dissipation theorem

$$\langle \xi(t) \rangle = 0, \quad (1a)$$

$$\langle \xi(t) \xi(s) \rangle = 2 M\eta k_B T \delta(t-s), \quad (1b)$$

where M is the mass of the adparticle, k_B the Boltzmann constant, and T the absolute temperature. With the above mentioned forces, the equation of motion for the adsorbed particle is then given by the Langevin equation

$$M\ddot{x} = -\nabla U(x) - M\eta\dot{x} + \xi(t), \quad (2)$$

where $U(x)$ is the static potential. Unlike classical mechanics, the motion of the adparticle in this situation is not determined since the fluctuating force has only statistical meaning. Starting from the Langevin equation, Kramers was able to derive the Klein-Kramers equation^{5,6}

$$\frac{\partial \rho(x,v,t)}{\partial t} = \left[-\frac{\partial}{\partial x} v + \frac{\partial}{\partial v} \frac{U'(x) + M\eta v}{M} + \frac{\eta k T}{M} \frac{\partial^2}{\partial v^2} \right] \rho(x,v,t), \quad (3)$$

with $\rho(x,v,t)$ as the probability density for finding the adparticle at x with velocity v at time t , and $U'(x)$ the derivative of the static potential with respect to x . There is no general solution to this equation. To treat the jumping rate problem for a particle from one potential well to another, Kramers simplified this equation with further assumptions and then deduced the jump rate in terms of the vibrational frequency ω of the adparticle and the friction coefficient η . In the case of strong viscosity, the effect of the Brownian forces on the velocity of the particle is much larger than that of the static force $-\nabla U(x)$, and a Maxwell velocity distribution can be established in a time scale shorter than $1/\omega$. Thus, we have

$$\rho(x,v,t) = \sigma(x,t) \exp(-mv^2/2kT).$$

This probability density leads to a jump rate^{5,6}

$$k = \frac{\omega \omega^*}{2\pi\eta} \exp(-E_a/k_B T), \quad \text{for } \eta > \omega^* \quad (4a)$$

$$k = \frac{\omega}{2\pi} \exp(-E_a/k_B T), \quad \text{for } \omega k_B T / 2\pi E_a < \eta < \omega^* \quad (4b)$$

where $\omega = (U''/M)^{1/2}$ evaluated at the potential minimum is the angular

frequency of small oscillations of an adsorbed particle near the equilibrium position, $\omega^* = (-U''/M)^{1/2}$ evaluated at the saddle point is the angular frequency characterizing the potential barrier (U'' being the second order derivative), and E_a , the barrier height, is the energy difference between the saddle point and the bottom of the potential well. In the case of small viscosity, the Brownian forces cause only a small change of the energy during a period of oscillation of the particle in a potential well and thus the probability density can be written as a function of energy and time, $\rho(x,v,t) = \rho(E, t)$, and a jump rate

$$k = \eta \frac{E_a}{k_B T} \exp(-E_a/k_B T), \quad \text{for } \eta < \omega k_B T / 2\pi E_a \quad (4c)$$

can be deduced. In the moderate friction regime, the result Eq. (4b) is identical to that from absolute rate theory (or transition state theory, TST, see discussion below), in which the friction coefficient is irrelevant. However, in both weak and strong friction regimes, the diffusion rate is significantly different from that of the absolute rate theory. It is also clear that the Kramers theory only provides a way for calculating the jump rate rather than the diffusion coefficient. Further assumptions on jumping mechanisms are required in order to find the diffusion coefficient. For instance, in most surface diffusion cases, the elemental jumps of the adparticle are to the adjacent site. Therefore the diffusion coefficient is given by⁸

$$D = \frac{1}{4} k \langle l^2 \rangle, \quad (5)$$

where $\langle l^2 \rangle$ is the mean square jump length corresponding to the lattice distance.

Kramers theory deals with the jump rate of a structureless adparticle in one dimension. For surface diffusion, the adparticle can have many degrees of freedom of motion. How to couple these other degrees of freedom into the jump rate is a difficult problem. As a result, the extension of Kramers theory into multidimensions is very complicated⁶. Opposite to this, the transition state theory provides a simple, direct way to solve the problem to some extent.

The basic assumptions in the transition state theory (TST) are the following: (1) the adparticles are in equilibrium with the static substrate potential well at every point; (2) only adparticles with energy higher than the potential barrier will jump to the next site. Under these assumptions, finding the jump rate becomes a simple statistical problem. With Z_0 as the partition function of the adparticle at the bottom of the potential well and Z^\ddagger as the partition function at the saddle point, excluding the diffusion coordinate, the jump rate can be expressed as⁶

$$k_{\text{TST}} = \frac{k_B T}{h} \frac{Z^\ddagger}{Z_0} \exp(-E_a/k_B T). \quad (6)$$

For an adparticle without internal degrees of freedom and in one dimension, it is easy to verify that Eq. (6) gives result (4b).

The degrees of freedom other than the diffusion coordinate can affect the jump rate if the corresponding partition functions at the bottom of the well and at the saddle point are not the same. For example, for an adparticle diffusing on a surface, the second translational degree of freedom will come into the two partition functions differently. Furthermore, if the adparticle is a molecule, its bending modes can affect the jump rate through the two corresponding partition

functions as well.

Despite the success of the Kramers' theory, it is still an oversimplified model. The actual dynamic interaction between the adparticle and the substrate is far more complicated⁷. Furthermore, the phenomenological parameter η should be calculable from the microscopic origin of the interaction. Several authors have derived expressions for this parameter η by considering the dynamic interaction between the adparticle and the substrate due to both electronic excitations and lattice vibrations⁹. In general, since the electrons are much lighter than the adparticle and consequently their fluctuating motions are fast with respect to the motion of the adparticle. Treating the forces from the electrons as a Brownian-like force as in the Kramers model is a very good approximation. However, fluctuations of the substrate atoms are on a time scale comparable to or even longer than the motion of the adparticle, making the assumption of the Kramers model for the dynamic interaction very questionable.

Goran Wahnstrom⁷ and S. C. Ying¹⁰ independently developed theories to account for the above effect. In their theories, information about the dynamic interactions is contained in a so called memory function, from which the diffusion coefficient D can be deduced. The details of these theories must be referred to the original papers. The important result is that in most cases, a spatially dependent friction coefficient $\eta(r)$, in contrast to Kramers' constant friction coefficient, must be used in the Langevin equation in order to describe the diffusive motion of the adparticle well. In the case of light adparticles, even a position dependent friction coefficient is no longer appropriate to describe the adparticle's motion and a full account for the couplings between the adparticle and the substrate must be taken. This is because that the motion of the substrate atoms is slower than the motion of the adparticle, the forces applied to

the adparticle by the substrate atoms can no longer be described as Brownian force.

Aside from the analytical description of adparticle diffusion, molecular dynamics simulation has been extensively used and has proved to be a powerful tool to study surface diffusion of a single adsorbate on crystalline surfaces¹¹. The principles for applying molecular dynamics simulation in surface diffusion are the following. The diffusion coefficient D^* is defined in the random walk picture by¹¹

$$D^* = \lim_{t \rightarrow \infty} \frac{\langle \Delta R^2(t) \rangle}{4t}, \quad (7)$$

with $\langle \Delta R^2(t) \rangle$ as the mean square displacement of the adparticle. This formula can be rewritten in terms of the velocity correlation

$$D^* = \int_0^{\infty} dt \frac{1}{2} \langle \mathbf{v}(0) \cdot \mathbf{v}(t) \rangle. \quad (8)$$

With either Lennard-Jones or Morse potential describing the interaction between the adparticle and substrate atoms as well as between substrate atoms, the system can be thermalized at finite temperature and then the trajectories of the adparticle followed so that the mean square displacement, or the velocity correlation, can be calculated and the diffusion coefficient found. The diffusion activation energy and the pre-exponential factor can be subsequently determined from an Arrhenius fit.

The trajectory tracing procedure in the molecular dynamics simulation is very transparent and many interesting features of surface diffusion have been

found with this method. For instance, concerted motion with the adparticle exchanging position with a substrate atom¹², correlated successive hoppings^{12,13}, multiple-lattice distance hoppings^{12,13}, and recrossing of the saddle point have been observed. These provide essential information for understanding the diffusion mechanisms.

Unfortunately, molecular dynamics simulation is not adequate for diffusion studies at all temperatures for most given systems. Especially, at low temperatures, the adparticle resides at its local minimum energy site for such a long time that a jumping event is very rare. Directly simulating such a system for surface diffusion takes an unreasonably long time and it is impossible in practice. An alternative method to solve this problem is to incorporate a molecular dynamics simulation into the transition state theory (TST).

Formalisms for this purpose have been developed¹⁴. The key point in this approach is to factor the jump rate constant into two parts: (1) an equilibrium factor which is simply the transition state theory (TST) rate constant. The rare-event nature of the process is included in this factor; (2) a dynamic correction factor, $f_d(i \rightarrow j)$, which accounts for the fact that the flux crossing the dividing surface that separates the initial and final sites of a jump in (1) contains spurious crossings. The spurious crossings do not correspond to true site-change event. The jump rate from site i to site j thus can be expressed as

$$k_{i \rightarrow j} = k_{\text{TST}} f_d(i \rightarrow j). \quad (9)$$

The dynamic correction factor $f_d(i \rightarrow j)$ can be evaluated by following the trajectories of the adparticle in a short-time regime in the molecular dynamics simulation. To illustrate this point further, we look at two different time scales; τ_{corr} , which is the average time it takes an adparticle to thermalize with its

surroundings; and τ_{rxn} , which is the average time between two reactive successive crossings. Since the residence time for the adparticle in its equilibrium site is usually very long in the low temperature regime, it is generally true that $\tau_{corr} \ll \tau_{rxn}$. With the dynamic phenomena such as saddle point recrossing, multiple-lattice distance jumping, and correlated successive jumping all happening in the time scale τ_{corr} , it is easy to see that only the dynamic information on this time scale is needed for calculating the dynamic correction factors and this dynamic information can be obtained by setting the initial conditions properly in a simulation.

Once the rates $k_{i \rightarrow j}$ are known, the diffusion coefficient is then given by

$$D = \frac{1}{4} \sum_{j \neq i} k_{i \rightarrow j} l_{ij}^2 \quad (10)$$

where multiple-lattice distance jumping has been explicitly included. It is found in the low temperature regime that the TST theory is quite accurate. However, in the high temperature regime, multiple lattice distance jump rate $k_{i \rightarrow j}$ ($|i-j| > 1$) is appreciable and contributes to the diffusion coefficient significantly¹¹.

Recently, a molecular dynamics simulation was applied to the surface diffusion of CO on Ni(111)¹⁵. It was found that CO is subjected to a rather weak dissipative force on the Ni(111) surface, so that correlated jumps and multiple-lattice distance jumps are rather common (with a probability of 0.5). The internal degrees of freedom of the CO molecule is also important. In particular, the coupling between the diffusion coordinate and the bending mode is very strong. The potential seen by CO can be significantly modified when the molecule rocks uphill and downhill.

If only the static interaction is concerned, more advanced methods such as the *ab initio*, local density function (LDF) method can be used to calculate the diffusion activation energy and the lowest energy path. An example is Al/Al(100)¹⁶, in which concerted motion is found by the LDF method.

C. Chemical Surface Diffusion

In the tracer surface diffusion case, where only motion of noninteracting individual atom or molecule is involved, random walk models can be applied. The diffusion coefficient can be directly related to the microscopic quantities such as mean square displacement and jump rate. However, in the chemical surface diffusion case, where a macroscopic number of interacting atoms or molecules are involved, the diffusion can no longer be defined by simple microscopic quantities¹. The counterpart of the tracer diffusion coefficient D^* in the chemical diffusion case is the chemical surface diffusion coefficient D , defined by Fick's first law¹,

$$\mathbf{J} = -\overleftrightarrow{\mathbf{D}} \cdot \nabla C, \quad (11)$$

where \mathbf{J} is the adparticle flux and C the adparticle density. Here, we explicitly indicate the tensor characteristic of the surface diffusion coefficient by $\overleftrightarrow{\mathbf{D}}$.

In the isotropic case, the diffusion tensor reduces to a scalar and

$$\mathbf{J} = -D \nabla C. \quad (11a)$$

In a macroscopic system, equilibrating adatoms or molecules on a

surface is a response to the gradient in chemical potential μ rather than the gradient of the concentration. Therefore, a more appropriate way to express the flux is¹⁷

$$\begin{aligned} J &= -L_T \nabla \mu \\ &= -\frac{L_T}{N_S} \left(\frac{\partial \mu}{\partial \theta} \right)_T \nabla C, \end{aligned} \quad (12)$$

where L_T is a constant. The variable C in the chemical potential has been replaced by coverage θ through the relation $C=N_S \theta$, with N_S being the density of available adsorption sites on the surface. We have

$$\begin{aligned} D &= \frac{L_T}{N_S} \left(\frac{\partial \mu}{\partial \theta} \right)_T \\ &= \frac{1}{4} a^2 \Gamma(\theta) \left(\frac{\partial(\mu/k_B T)}{\partial \ln \theta} \right)_T. \end{aligned} \quad (13)$$

The second step here is to introduce a new parameter $\Gamma(\theta) = \frac{4}{a^2} \frac{k_B T}{\theta} \frac{L_T}{N_S}$, a quantity called effective jump frequency in analogy to the jump rate k in tracer diffusion case. The thermodynamic factor $\left(\frac{\partial(\mu/k_B T)}{\partial \ln \theta} \right)_T$, historically from Darken equation¹, is related to the mean value and the mean square fluctuation of the number of adparticles^{1,17}:

$$\left(\frac{\partial(\mu/kT)}{\partial \ln \theta} \right)_T = \frac{\langle N \rangle}{\langle \Delta N \rangle^2} \quad (14)$$

The effect of this thermodynamic factor on diffusion coefficient has been discussed rather in detail by Ref.[17] and can be calculated once the thermodynamic property is known. However, Eq. (13) only defines the effective jump frequency $\Gamma(\theta)$ phenomenologically and does not provide a way for calculating it.

Zhdanov has provided a better picture for the effective jump frequency $\Gamma(\theta)$ in the framework of lattice-gas model¹⁸. Consider a system with adsorbate interaction which affects the energy potential at adsorption site by ϵ_i and the saddle point by ϵ^*_i under a specific environment configuration (the arrangement of the rest adparticles) marked by i . Assuming a one dimensional coverage gradient exists, the flux of particles from row 1 to row 2 is then given by

$$J_{12} = N_s \frac{1}{4} \nu \exp(-E_a/k_B T) \sum_i P_{A0i} \exp(-(\epsilon^*_i - \epsilon_i)/k_B T), \quad (15)$$

where $N_s = 1/a$ is the number of sites on a unit length and ν the effective vibrational frequency of the adparticle at the bottom of the potential well at $\theta=0$. E_a is the diffusion activation energy at $\theta \rightarrow 0$. P_{A0i} is the probability that a site in the first row is occupied and the nearest site in the second row is empty, with the environment configuration marked by i . It can be further expressed as

$$P_{A0i} = P_{00i} \exp[(\mu_1 - \epsilon_i)/k_B T], \quad (16)$$

where μ_1 is the chemical potential in row 1 and P_{00i} is the probability that a pair of the nearest neighbor sites, one in row 1 and the other in row 2, are empty, with an environment configuration marked by i . Similarly the flux of particles from row 2 to row 1 can be found. With S defined as

$$S = \sum_i P_{00i} \exp(-\epsilon_i^*/k_B T), \quad (17)$$

the net flux from row 1 to row 2 is given by

$$\begin{aligned} J &= J_{12} - J_{21} \\ &= N_s \frac{1}{4} v \exp(-E_a/k_B T) S [\exp(\mu_1/k_B T) - \exp(\mu_2/k_B T)] \\ &= -\frac{1}{4} v a^2 \exp(-E_a/k_B T) S \exp(\mu(\theta)/k_B T) \frac{1}{\theta} \left(\frac{\partial(\mu/k_B T)}{\partial \ln \theta} \right) \Gamma \nabla C, \quad (18) \end{aligned}$$

where the difference in the square bracket has been replaced by an appropriate derivative. Up to this point, the effective jump frequency $\Gamma(\theta)$ has been related to fundamental quantities through S and chemical potential μ as

$$\Gamma(\theta) = v \exp(-E_a/k_B T) S \exp(\mu(\theta)/k_B T) / \theta. \quad (19)$$

and can be calculated once those quantities are known. The diffusion coefficient D as a function of coverage is given by

$$D(\theta) = \frac{1}{4} v a^2 \exp(-E_a/k_B T) S \exp(\mu(\theta)/k_B T) \frac{1}{\theta} \left(\frac{\partial(\mu/k_B T)}{\partial \ln \theta} \right) \Gamma \quad (20)$$

As an example, we consider the mean field approximation with a square lattice in the lattice gas frame and restrict ourselves to the nearest-neighbor interaction. We write down^{19,19a}

$$\exp(\mu(\theta)/kT) = \frac{\theta}{1-\theta} \exp(4\varepsilon\theta/kT), \quad (21a)$$

$$S = (1-\theta)^2 \exp(-6\varepsilon\theta/kT). \quad (21b)$$

The detail derivation of Eq. (21a) can be found in Ref. [19a]. To derive Eq. (21b) one simply has used the fact that the probability of finding an empty site is $(1 - \theta)$. The coverage dependent diffusion coefficient is thus obtained as

$$\begin{aligned} D(\theta) = & \frac{1}{4} a^2 \nu \exp(-E_a/kT) \\ & \times (1-\theta) \exp(4\varepsilon\theta/kT) \exp(-6\varepsilon\theta/kT) \\ & \times \left\{ \frac{1}{1-\theta} + 4\varepsilon\theta/kT \right\}. \end{aligned} \quad (22)$$

The physical meaning of this formula is worth exploring. The first line is the diffusion coefficient for a single adparticle. The factor $(1-\theta)$ is the site blocking effect in a random distribution configuration of adsorbates. The two exponential factors are the effect on the effective jump frequency from the lateral interactions of the adsorbates. The last factor is the thermodynamic factor.

For repulsive nearest-neighbor interaction, ε is positive. If there is no effect on the saddle point ($\varepsilon^*=0$), the repulsive interaction not only lowers the jumping barrier so as to increase the effective jumping frequency, but also increases the thermodynamic factor. Therefore, the diffusion coefficient

increases with coverage until a very high coverage where the blocking effect ($1 - \theta$) dominates, and then it decreases. If the nearest-neighbor interaction is attractive, the diffusion coefficient will monotonically decrease to 0. Certainly the interactions between the adsorbates can affect the saddle point as well. As a further complication, the lateral interaction can be long range (e.g., dipole interactions) so that one adparticle can interact with many other adparticles which are far away. Many body effects such as adsorbate-substrate-adsorbate interaction can be important as well. It is this interaction that provides attraction between adsorbates in most cases²⁰. None of these have been fully explored and they still comprise the most challenging problems in surface diffusion.

More sophisticated models, such as the quasi-chemical approximation (QCA), have been used to calculate the effective jump frequency $\Gamma(\theta)$ to investigate the effect of adsorbate interactions on surface diffusion. Nearest-neighbor interactions^{17,18,21}, next nearest-neighbor interactions and interactions at saddle points¹⁸ have all been considered. The qualitative behavior of the diffusion coefficient as a function of coverage is similar to that in the mean field approximation. In the same frame, surface diffusion in the case with adsorbate-induced surface reconstruction²² and coadsorbate surface diffusion²³ have also been studied.

As we discussed in the previous section, the dynamic interaction of adparticles with the substrate is the driving force for surface diffusion. It is also true that other adparticles can exert dynamic fluctuating forces on the adparticle under consideration. How this dynamic interaction affects surface diffusion and depends on coverage are not included in the lattice gas model and has never been studied. It is certain that the other adparticles on the surface can also

serve as a heat bath for the specific adparticle in a similar way as the substrate. Therefore, including only the static interaction from other adsorbates as in the lattice gas model is insufficient. The importance of such effects may require a first principle calculation to reveal.

The blocking effect can be more complicated in the case with ordered domain formation. If attractive interactions exist so that the molecules like to form two dimensional islands, the blocking effect is apparently larger than what the $(1-\theta)$ factor can account for. This factor $(1-\theta)$ can only describe a random adsorbates distribution case. Therefore, correct description of the site blocking effect is not a simple matter.

In principle, molecular dynamics simulation can be used in chemical diffusion study as well. Unfortunately, the large number of molecules involved in the problem makes it too time consuming and practically impossible. Instead, Monte Carlo simulations have been applied in many cases^{17,24,25} including ordered surface layers²⁵. The lateral interactions used in these Monte Carlo simulations are basically the lattice gas type. Mostly, only the first nearest-neighbor and second nearest-neighbor interactions have been considered. The results are qualitatively the same as those from the analytical study with the lattice gas model.

D. Anisotropic Surface Diffusion

For surfaces with crystallographic unequivalent directions, surface diffusions along them are expected to be different. In the extreme case, adparticles on such surfaces can preferentially hop in one direction, leading to

one-dimensional diffusion. In most cases, diffusion on such surfaces can be a competition between the two directions. In understanding the details of diffusion mechanisms, measurement of the anisotropic surface diffusion is important. One natural question is how many measurements are needed in order to describe a two dimensional diffusion completely.

As we know, surface diffusion is mathematically described by a second-rank tensor $\overleftrightarrow{\mathbf{D}}$, which has four elements. In general, the diffusion tensor can be diagonalized so that there are only two independent elements that should be determined²⁶. To see this diagonalization, let's break the diffusion tensor into a symmetric and an antisymmetric part as

$$\overleftrightarrow{\mathbf{D}} = \begin{pmatrix} D_{11} & D_{12} \\ D_{21} & D_{22} \end{pmatrix} = \mathbf{D}^+ + \mathbf{D}^- . \quad (23)$$

Substituting this into Fick's second law of diffusion

$$\frac{\partial C}{\partial t} = \nabla \cdot (\mathbf{D} \cdot \nabla C), \quad (24)$$

we obtain

$$\frac{\partial C}{\partial t} = \nabla \cdot (\mathbf{D}^+ \cdot \nabla C) + \nabla \cdot (\mathbf{D}^- \cdot \nabla C) . \quad (24a)$$

For a diffusion coefficient which can be approximated by a constant in the specific coverage range, the second term is given by

$$\nabla \cdot \bar{\mathbf{D}} \cdot \nabla C = \bar{D}_{12} \frac{\partial^2 C}{\partial x_1 \partial x_2} + \bar{D}_{21} \frac{\partial^2 C}{\partial x_2 \partial x_1}, \quad (25)$$

which vanishes since $\bar{D}_{12} = -\bar{D}_{21}$. Therefore, the antisymmetric part of the diffusion coefficient has no physical importance in the real diffusion measurement and the surface diffusion can be fully characterized by a symmetric diffusion tensor, which can always be diagonalized. To further prove $\bar{D}_{12} = -\bar{D}_{21} = 0$, general Onsager reciprocity relations must be applied^{26a}.

From the above argument, it is clear that anisotropic surface diffusion in general needs only two independent measurements in order to fully specify the diffusion properties.

Anisotropic surface diffusion has been rarely investigated theoretically. For single adparticle diffusion, can the diffusion along a principal axis be treated as a one dimensional diffusion or not? Is there a coupling between diffusion along the two principal directions? These questions have not yet been answered.

In the case of chemical surface diffusion, if the adsorbate-adsorbate interaction is anisotropic, how can this anisotropy be incorporated into the lattice gas model or other theories? This needs to be addressed before we can fully understand the diffusion anisotropy.

E. Effects of Defects on Surface Diffusion

An important question in surface diffusion is how the surface defects

influence the adparticle diffusion. In tracer surface diffusion, the measurement techniques are microscopic and the defect problem has been simply avoided. It is however possible that a defect can cause some modification in the vicinity of the defect site, thus affecting diffusion of the adparticle in that vicinity. Such problems unfortunately have remained unexplored. On a different note, diffusion of single adparticles in a disordered lattice system has been extensively studied by random walk models with pre-specified distributions of the jump rate²⁷.

In the chemical surface diffusion cases, a large crystal surface is usually used and the effect of surface defects could be important. With some density of point defects, the dynamic interaction of the adparticle with the substrate, or the friction force, may be strongly altered but the static potential may remain approximately unchanged. As a result, the diffusion measurement of such a system may provide an intrinsic activation energy but not a reliable preexponential factor. How to evaluate this statement remains as an unsolved interesting problem. On the other hand, theoretical studies of chemical diffusion on an inhomogeneous surface in the framework of lattice gas model have appeared recently²⁸.

The effect of steps on surface diffusion is easier to analyze. In the case of low step densities, we can assume that surface diffusion consists of two independent parts, one on terraces and the other on steps. No interactions between steps or between steps and terraces have to be introduced in the first order approximation. Consider a case with unidirectional steps. For diffusion parallel to steps, the diffusion coefficient is simply the sum of two diffusion coefficients with the proper weighting:

$$D = \eta_s D_s + \eta_t D_t , \quad (26)$$

where D_s and D_t are diffusion coefficients for diffusion on terraces and on steps, respectively, and η_s , η_t are the area percentages of steps and terraces on the surface. For diffusion perpendicular to the steps, the diffusion coefficient can be obtained by summing up the diffusion time for adparticles to cross a terrace and to traverse an adjacent step. With D_s' denoting the diffusion coefficient when the duration time of the adparticle on terraces is negligible and D_t' denoting the diffusion coefficient when the duration time of the adparticle on steps is negligible respectively, the diffusion coefficient in general is given by

$$\frac{1}{D} = \frac{1}{D_s'} + \frac{1}{D_t'} . \quad (27)$$

We have used the relation that the diffusion coefficient is inversely proportional to the diffusion time to obtain Eq.(27). Equations (26) and (27) indicate that the diffusion coefficients in the case with unidirectional steps can be constructed as either in series or in parallel, analogous to the case in electric circuits.

Recently, it was pointed out that the steps can dominate surface diffusion even if the step density is low^{19,29}. The important issue here is the difference between the terrace diffusion activation energy and the step diffusion activation energy. If the time a molecule is trapped in the potential well associated with a step is long compared to the time it spends to cross a terrace, the surface diffusion perpendicular to the steps will be controlled by the steps. The condition for this to occur is the following:

$$\gamma = N^2 \exp [(E_{diff}^{(terrace)} - E_{diff}^{(step)})/k_B T] \ll 1, \quad (28)$$

where N is the number of rows of atoms in a terrace. For obtaining Eq. (28), we have assumed that the pre-exponential factors for the elementary jumping processes of an atom or molecule from one site to another on a terrace and across a step are the same. It is clear that the maximum N for step dominated diffusion is closely related to the difference between the terrace diffusion activation energy and the step diffusion activation energy. If the assumption on the pre-exponential factors is lifted, a modification on the step density will result in the step controlled diffusion condition.

In addition to controlling surface diffusion, steps can change the anisotropy of surface diffusion. In general, steps make an angle with respect to the principal axes, e.g., a surface miscut is in some arbitrary direction with respect to the principal axes. Although microscopically steps are developed to be parallel to either of the two principal axes, we assume that these step-kink-like small segments of steps can be considered to form macroscopic steps at an angle with respect to the surface principal axes and a unique diffusion activation energy across these macroscopic steps exists. Bearing this assumption in mind, we are going to construct the diffusion tensor on a surface with such unidirectional steps.

The intrinsic surface diffusion tensor for a surface without steps is given by

$$\hat{\mathbf{D}} = \begin{pmatrix} D_1 & 0 \\ 0 & D_2 \end{pmatrix}, \quad (29)$$

with the diagonal elements along the principal axes of the surface. Denoting the

angle between the steps and the first principal axis as ϕ_0 , and using the coordinate frame with the two axes along or perpendicular to the steps, the intrinsic diffusion tensor is transformed to

$$\underline{\underline{D}}' = \begin{pmatrix} D_1 \cos^2 \phi + D_2 \sin^2 \phi & (D_1 - D_2) \sin \phi \cos \phi \\ (D_1 - D_2) \sin \phi \cos \phi & D_1 \sin^2 \phi + D_2 \cos^2 \phi \end{pmatrix}. \quad (30)$$

The effect of steps on the diffusion tensor now only shows up in the diagonal elements but not in the off-diagonal elements. The diffusion tensor element in the direction perpendicular to the steps should be replaced by D_1' with (see Eq. (27))

$$\frac{1}{D_1'} = \frac{1}{D_1 \cos^2 \phi + D_2 \sin^2 \phi} + \frac{1}{D_s}, \quad (31)$$

where D_s' is the diffusion coefficient across steps. The diffusion tensor element in the direction parallel to the step is replaced by (see Eq. (23))

$$D_2' = \eta_t (D_1 \sin^2 \phi + D_2 \cos^2 \phi) + \eta_s D_s. \quad (32)$$

With the two off-diagonal elements remaining the same as in Eq. (30), the new diffusion tensor is also symmetric. Generally, it can not be diagonalized in any of the two coordinate frames mentioned above. However, the general property of a symmetric tensor allows it to be diagonalization in some other coordinate frame.

F. Review of Surface Diffusion Techniques

The techniques that are available for surface diffusion measurements have been reviewed¹. Generally, these techniques are divided into two different categories: those that measure the tracer diffusion and those that measure the chemical diffusion. Detail description of these techniques can be found in Gomer's review article. In the following I will briefly describe these techniques and point out their limitations.

The techniques to measure tracer diffusion are the field ion microscopy (FIM) and scanning tunneling microscopy (STM). In the FIM technique the adatom and the atoms in the first layer of the substrate can be imaged by imaging gases, usually He or Ne, so that the random motion of the adatom can be directly observed³⁰. The very high electric field ($\sim 1V/\text{\AA}$) near the tip surface (substrate) involved in the image process and the field-induced stress can alter the surface potential in some cases so that the diffusion is not purely intrinsic. Also, the tip materials are usually restricted to refractory metals and the adparticles in most cases are limited to metal atoms.

In comparison, the recently developed scanning tunneling microscope, or STM, has several advantages in measuring surface diffusion³¹. There, a tip with nominally one or a few atoms at the end is used to image the surface structure. The principle of operation is the following. When the tip is close enough to the surface (a few \AA), the electrons can tunnel through the vacuum gap between the tip and the surface with an applied bias voltage. As the tip moves around at a constant height the local electron density of the substrate can be mapped. An adatom on the surface can change the local electron density enough for the recognition of the existence of the adatom. This image

process clearly allows direct observation of the adatom diffusion. Other mode of operation exist as well. The electric field required for STM is at least an order of magnitude weaker than that for FIM. Furthermore, the only requirement on the substrate surface is a large enough conductance. Therefore, adatom diffusion on semiconductors can also be studied. On the other hand, for some metal substrates with electrons highly delocalized, the atomic resolution might be lost and diffusion of adparticles on such surfaces are not observable. As a whole, STM is a more versatile technique for tracer surface diffusion study. Because STM is able to image a large area ($1\mu\times 1\mu$), diffusion of a large number of adparticles (submonolayer) has been investigated with this method as well³¹.

Most of the diffusion measurement techniques were developed to measure chemical surface diffusion. All but one (FEM, see below) require an initial coverage gradient profile. The technique that has been employed to measure surface diffusion for many systems is the fluctuation-correlation field emission microscopy (FEM)³². The principle of this method is that the number of electrons emitted from a tip to a screen under a high electric field depends on the adsorbate coverage on the tip because the work function of the tip depends on the adsorbate coverage. With the numbers of atoms or molecules fluctuating in a restricted area, the emitted electron current fluctuates. This fluctuation can then be related to the surface diffusion coefficient through the current fluctuation-correlation function. Since no initial coverage gradient profile is required in this method, it is basically an equilibrium method and very suitable for study of coverage dependence in surface diffusion. The drawbacks are mainly from the restriction on the tip material, similar to those mentioned for FIM. Therefore, the systems commonly studied with this method are molecules or atoms on various tungsten and nickel surfaces¹.

Another technique that has gained popularity in recent years is the so called "hole burning" LITD method³³, in which a laser pulse is first used to desorb adsorbed molecules or atoms from the surface to create a hole in the adsorbate layer, and then a second laser pulse is subsequently applied to probe the hole with a mass spectrometer to measure the amount of molecules that backfilled the hole from the surroundings via surface diffusion. This second laser pulse can be applied at different delayed times so that a refilling curve can be measured, and subsequently the diffusion coefficient can be deduced. The advantage of this method is its simplicity and its applicability to a large family of adsorbates and substrates. The difficulties are as follows. First, with lateral adsorbate-adsorbate interactions the diffusion coefficient is not simply related to the refilling rate. A theoretical expression of the refilling that takes these lateral interactions into account does not exist³⁴. Second, the application of multiple laser pulses can damage the substrate surface³⁵. Third, the coverage dependence is difficult to measure in a well characterized manner. Lastly, the information on diffusion anisotropy is difficult to obtain. Recently, a modified scheme of LITD has been proposed by King's group³⁶ where a step-like initial coverage profile is formed with laser desorption and the time evolved profile is also detected by laser desorption. By applying Boltzmann-Matano analysis, the coverage dependence of surface diffusion of H, D/Rh(111) has been investigated. The disadvantage of this method is the experimental complexity and the low spatial resolution (~250 μ m). Only relatively fast diffusion can be measured, which can be a problem if the desorption rate competes with the diffusion rate.

Many other methods have been developed to measure surface diffusion. Usually, these methods monitor a time-dependent change of a coverage profile with a certain spatial resolution. These methods include the work function

change method, the field emission shadowing method, and the electron beam scanning method¹. The work function change method has a low spatial resolution, typically in the $\sim 100\mu\text{m}$ regime. The energy resolution ($\sim 0.1\text{eV}$) associated with this method limits the systems it can measure. Typically, a work function change of $\sim 1\text{eV}$ upon adsorption is required for good measurements. The field emission shadowing method has the same limitations of FIM and FEM. The Auger electron scanning method has high spatial resolution ($\sim 500\text{\AA}$), but is limited to species it can detect (for example, hydrogen is not observable) and to substrates with high enough electric conductance in order to avoid the surface charging effect. All these methods share a common disadvantage, which is the difficulty in creating a well characterized initial coverage profile. Therefore, they have not been very popular and only limited systems have been studied.

Methods based on FTIR and NMR have been used to study surface diffusion in some systems. The FTIR method³⁷ relies on the spectral difference for adparticles on different sites, and therefore it can not be used to study diffusion on a homogeneous surface with single type sites. The NMR method³⁸ uses the property that an adparticle has different resonant frequencies in different environments. A spectral density analysis of the NMR spectra then allows the deduction of the diffusion coefficient. This method is very limited because of its complicated data analysis and low signal-to-noise ratio.

Helium scattering has been applied to study surface diffusion as well³⁹. The diffusion coefficient is related to the scattering peak width. The analysis is very model dependent and therefore the results are only qualitatively meaningful.

One important aspect of surface diffusion is the directional dependence

of the diffusion coefficient on a crystalline surface. Only some of the above methods can be used to study surface diffusion anisotropy. The difficulties lie mostly in preparing the initial coverage profile. In this thesis I will describe optical diffraction methods for surface diffusion studies. The newly developed methods can overcome many of the shortcomings mentioned above. In short, the methods allow one to study surface diffusion of any adsorbate on any substrate with coverage dependence and anisotropy of surface diffusion measured in simple manner.

References:

- ¹ Robert Gomer, Rep. Prog. Phys. **53**, 917(1990).
- ² A. Kapoor, R. T. Yang, and C. Wong, Catal. Rev.-Sci. Eng., **31**, 129(1989).
- ³ A. G. Naumovets and Yu. S. Vedula, Surf. Sci. Rep. **4**, 365(1985).
- ⁴ Gert Ehrlich and Kaj Stolt, Ann. Rev. Phys. Chem. **31**, 603(1980).
- ⁵ H. A. Kramers, Physica **7**, 284(1940); S. Chandrasekher, Rev. Modern Phys. **15**, 1(1943).
- ⁶ Peter Hanggi, Peter Talkneer, and Michal Borkovec, Rev. Modern Phys. **62**, 251(1990); V. P. Zhdanov, Surf. Sci. Rep. **12**, 183(1991).
- ⁷ Goran Wahnstrom, Surf. Sci. **159**, 311(1985); Surf. Sci. **164**, 449(1985); J. Chem. Phys. **84**,5931(1986); Phys. Rev. B **33**, 1020(1985).
- ⁸ V.P Zhdanov, Surf. Sci. **214**, 289(1989)
- ⁹ W. L. Schaich, J. Chem. Phys.**60**, 1087(1974); A. Blandin, A. Nourtier and D. W. Hone, J. Physique **37**, 369(1976); C. Caroli, B. Roulet and D. Sain-James, Phys. Rev. B **18**, 545(1978); B. Hellsing and M. Persson, Phys. Scripta **29**, 360(1984); P. Minnhagen, J. Phys C **15**, 2293(1982).
- ¹⁰ S. C. Ying, Phys. Rev.B **41**, 7068(1990).
- ¹¹ J. D. Doll and A. F. Voter, Ann, Rev. Phys. Chem. **38**, 413(1987).
- ¹² G. De Lorenzi and G. Jacucci, Surf. Sci. **116**, 391(1982).
- ¹³ M. R. Mruzik and G. M. Pound, J. Phys. F: Metal Phys. **11**, 1403(1981); J. D. Doll and H. K. McDowell, J. Chem. Phys. **77**, 479(1982); John C. Tully, George H. Gilmer and Mary Shrgard, J. Chem. Phys. **71**, 1630(1979).
- ¹⁴ J. C. Keck, Discuss. Faraday Soc. **33**, 173(1962); D. Chandler, J. Chem. Phys. **68**, 2959(1978); J. A. Montgomery, Jr., D. Chandler, and B. J. Berne, J. Chem. Phys. **70**, 4056(1979); J. L. Skinner and P. G. Wolynes, J. Chem.

- Phys. **69**, 2143(1978); **72**, 4913(1980); Arthur F. Voter and Jimmie D. Doll, J. Chem. Phys. **82**, 80(1984).
- ¹⁵ D. J. Doren, APS meeting Bulletin 37, 527(1992); K. D. Dobbs and D. J. Doren, preprint (submitted to J. Chem. Phys.).
- ¹⁶ P. J. Feibelman, Phys. Rev. Lett. **65**, 729(1990).
- ¹⁷ David A. Reed and Gert Ehrlich, Surf. Sci. **102**, 588(1981); **105**, 603(1981).
- ¹⁸ V. P. Zhdanov, Surf. Sci. Lett. **149**, L13(1985).
- ¹⁹ V. P. Zhdanov, Phys. Lett. A **137**, 409(1989).
- ^{19a} Follower, *Statistical Thermodynamics*, (Cambridge Univ. Press, 1939).
- ²⁰ Yu. K. Tovbin, Prog. in Surf. Sci. **34**, 1(1991).
- ²¹ V. P. Zhdanov, Surf. Sci. **257**, 63(1991).
- ²² V. P. Zhdanov, Langmuir **5**, 1044(1989).
- ²³ V. P. Zhdanov, Phys. Lett. A **137**, 225(1989); Surf. Sci. **194**, 1(1988); V. Pereyra, G. Zgrablich, and V. P. Zhdanov, Langmuir **6**, 691(1990).
- ²⁴ Michael Bowker and David A. King, Surf. Sci. **71**, 583(1978); **72**, 208(1978).
- ²⁵ G. E. Murch, Philos. mag. A **43** 871(1981); Xue-Pei Jiang and Horia Metiu, J. Chem. Phys. **88**, 1891(1988).
- ²⁶ W. Jost, *Diffusion in Solids, Liquids, Gases*, (Academic Press, New York, 1960).
- ^{26a} L. Onsager, Phys. Rev. **37**, 405(1931); **38**, 2265(1931).
- ²⁷ J. W. Haus and K. W. Kehr, Phys. Rep. **150**, 264(1987).
- ²⁸ C. H. Mak, H. C. Anderson, S. M. George, J. Chem. Phys. **88**, 4052(1988); V. Pereyra, G. Zgrablich, and V. P. Zhdanov, Langmuir **6**, 691(1990); F. Bulnes, J. L. Riccardo, G. Zgrablich and V. Pereyra, Surf. Sci. **260**, 304(1992).
- ²⁹ Xu-dong Xiao, X. D. Zhu, W. Daum and Y. R. Shen, accepted for publication by Phys. Rev. B.
- ³⁰ G. Ehrlich and F. G. Hudda, J. Chem. Phys. **44**, 1039(1966); G. Ehrlich, J.

- Chem. Phys. **44**, 1050(1966); G. Ehrlich, Surf. Sci. **63**,422(1977); G. L. Kellogg, T. T. Tsong, and P. Cowan, Surf. Sci. **70**, 485(1978); T. Tsong, Rep. Prog. Phys. **51**, 759(1988); G. L. Kellogg and P. J. Feibelman, Phys. Rev. Lett. **64**, 3143(1990); G. L. Kellogg, Phys. Rev. Lett. **67**, 216(1991); T. T. Tsong and C. Chen, Phys. Rev. B **43**, 2007(1991).
- ³¹ G. Binnig, H. Fuchs, and E. Stoll, Surf. Sci. **169**, L295(1986); R. C. Jaklevic and L. Elie, Phys. Rev. Lett. **60**, 120(1988); M. G. Lagally, Y.-W. Mo, R. Kariotis, B. S. Swartzentruber, and M. B. Webb, in Kinetics of Ordering and Growth at surfaces, edited by M. G. Lagally (Plenum, New York, 1990), p.145; H. B. Elswijk, A. Hoeven, E. J. van Loenen, and Dijkamp, J. Vac. Sci. Technol. B **9**, 451(1991); Y.-W. Mo, J. Kleiner, M. B. Webb, and M. G. Lagally, Phys. Rev. Lett. **66** 1998(1991); R. M. Feenstra, A. J. Slavin, G. A. Held, and M. A. Lutz, Phys. Rev. Lett. **66**, 3257(1991); Eric Ganz, Silva K. Theiss, Ing-Shouh Hwang, and Jene Golovchenko, Phys. Rev. Lett. **68**, 1567(1992).
- ³² R. Gomer, Surf. Sci. **38**, 373(1973); J. R. Chen, and R. Gomer, Surf. Sci. **81**, 589(1979); R. Gomer, Vacuum **33**, 537(1983).
- ³³ R. Viswanathan, D. R. Burgess, Jr., P. C. Stair, and E. Weitz, J. Vac. Sci. Technol. **20**, 605(1982); R. B. Hall, and A. M. DeSantolo, Surf. Sci. **137**, 421(1984); S. M. George, A. M. DeSantolo, and R. B. Hall, Surf. Sci. **159**, L425(1985); E. G. Seebauer and L. D. Schmidt, Chem. Phys. Lett. **123**, 129(1986); C. H. Mak, J. L. Brand, A. A. Deckert, and S. M. George, J. Chem. Phys. **85**, 1676(1986); C. H. Mak, J. L. Brand, B. G. Koehler, and S. M. George, Surf. Sci. **191**, 108(1987); D. R. Mullins, B. Roop, S. A. Costello, and J. M. White, Surf. Sci. **186**, 67(1987); C. H. Mak, and S. M. George, Surf. Sci. **172**, 509(1986).
- ³⁴ M. C. Tringides, Surf. Sci. **204**, 345(1988).
- ³⁵ J. N. Rusell, Jr., R. B. Hall, Surf. Sci. **203**, L642(1988).

- ³⁶ S. S. Mann, T. Seto, C. J. Barnes, and D. A. King, *Surf. Sci.* **261**, 155(1992).
- ³⁷ J. E. Reutt-Robey, D. J. Dore, Y. J. Chabal, and S. B. Christman, *Phys. Rev. Lett.* **61**, 2778(1988); S. S. Iyer, T. F. Heinz, and M. M. T. Loy, *J. Vac. Sci. & Technol. B* **5**, 709(1987).
- ³⁸ Po-Kang Wang, Jean-Phillipe Ansermet, C. P. Slichter, and J. H. Sinfelt, *Phys. Rev. Lett.* **55**, 2731(1985); Po-Kang Wang, Jean-Phillipe Ansermet, S. L. Rudaz, Z. Wang, S. E. Shore, C. P. Slichter, and J. H. Sinfelt, *Science* **234**, 35(1986); S. E. Shore, Jean-Phillipe Ansermet, C. P. Slichter, and J. H. Sinfelt, *Phys. Rev. Lett.* **58**, 953(1987); Mamfred Riehl-Chudoba, U. Memmert, and D. Fick, *Surf. Sci.* **245**, 180(1991).
- ³⁹ J. W. M. Frenken, B. J. Hinch, and J. P. Toennies, *Surf. Sci.* **211/212**, 21(1989); C.-H. Hsu, B. E. Larson, M. El-Batanouny, and C. R. Willis, *Phys. Rev. Lett.* **66**, 3164(1991).

III. Nonlinear And Linear Optical Diffraction Methods For Surface Diffusion Study

A. General Principles of Surface Diffusion Measurement With Optical Diffraction Methods

As mentioned in chapter II, there exist several techniques for surface diffusion measurement. The techniques that measure the tracer diffusion coefficient rely on the random walk model to obtain the quantity D^*

$$D^* = \lim_{t \rightarrow \infty} \frac{\langle \Delta R^2(t) \rangle}{4t} \quad (1)$$

For those techniques that measure the chemical diffusion coefficient D , the fundamental equation is Fick's second law (except the Fluctuation Correlation FEM method):

$$\frac{\partial C}{\partial t} = \nabla \cdot (\mathbf{D} \cdot \nabla C) \quad (2)$$

To utilize this equation, two questions immediately arise: First, there must be an adsorbate density gradient in space; how is this density gradient created? Second, the time evolution of the density distribution must be known in order to extract the quantity D ; how is this time evolution of the density distribution measured?

In the techniques that I am going to describe for surface diffusion measurements, the gradient of adsorbate surface density (coverage) is generated by laser induced thermal desorption. By using a one-dimensional spatially modulated laser intensity, the desorption yields a one-dimensional monolayer grating. To probe surface diffusion of adsorbates in such a case, one monitors optical diffraction from the grating. Before diffusion, there is a finite diffraction signal from the grating. As diffusion proceeds, the adsorbate grating gets smeared out. This results in a decay of the diffraction signal, from which one can deduce the surface diffusion coefficient.

B. Methods To Determine Laser-Induced-Thermal-Desorption Yield

The key step in preparing for a diffusion measurement is to create a monolayer grating that will yield a strong enough diffraction signal. This can be achieved by laser-induced thermal desorption (LITD) with a spatial intensity modulation formed by interfering two laser beams. In order to create a prescribed adsorbate grating profile, the desorption yield versus desorbing laser energy has to be known. In this section I will describe the methods we use to measure this relation.

a) Reflection Second Harmonic Generation (SHG) Method

Reflected second harmonic generation (SHG) can be used to probe laser desorption. Because of the surface specificity, SHG is sensitive to the presence of adsorbates on a surface¹. The SHG signal usually has a one-to-one

correspondence with the adsorbate coverage and thus can be used to measure of the adsorbate coverage. In light of this, we can first measure the reflected SHG as a function of gas exposure (pressure x time) to the surface. The absolute adsorbate coverage from exposure can be calibrated by from thermal desorption spectroscopy (TDS)². Combining the results of SHG and TDS, the relation between reflected SHG and adsorbate coverage can be determined. To eliminate contribution from the bare surface, a nonlinear interference method can be used to directly measure the adsorbate induced SHG change, namely $|\Delta\chi_{\text{eff}}^{(2)}(\theta)|^2$, as a function of coverage θ . The details of this method can be found in Ref. [3]. A p-in(fundamental)/p-out(SH) polarization geometry is usually chosen for SHG measurements since this SHG signal is normally the strongest among all the different polarization combinations, which is due to the fact that $\chi_{\text{zzz}}^{(2)}(\theta)$ is the dominating component in the nonlinear susceptibility tensor.

If an intense enough laser pulse is applied to the adsorbate-covered sample surface, it can thermally desorption of the adsorbed atoms or molecules. The number of adsorbates that remain on the surface can then be measured by reflection SHG. Consequently, the desorption yield can be determined. By varying the energy of the laser pulse the relation of the desorption yield versus desorbing laser energy can be determined.

The set-up for the LITD experiment is shown in Fig.1, where the desorbing laser beam is aligned collinearly with the probing laser (for SHG). The probing beam radius is one tenth that of the desorbing beam and probes only the central uniform part of the desorbed area. As an example, the measured result of $|\Delta\chi_{\text{eff}}^{(2)}(\theta)|^2$ is shown in Fig.2 for CO/ Ni(110). The CO

desorption yield from Ni(110) as a function of laser energy is depicted in Fig.3(a)⁴.

b) Linear Reflectance Method

A second method for measuring the desorption yield of laser induced thermal desorption is linear optical reflectance. As we showed in Ref. [5] the linear reflectance can be used to monitor the adsorption and desorption processes *in situ*.

The experimental setup is shown in Fig.4. Since the adsorbate-induced signal is low, a lock-in technique is used. A chopped He-Ne beam first passes through a polarizer and then a Babinet phase compensator. The polarizer is adjusted to transmit equal intensities from the bare surface reflected p- and s-polarized light. The phase compensator is adjusted to compensate the phase shift introduced by the metal surface between the p and s components. In this way, an analyzer set at 45° with respect to the plane of incidence can cross out reflected light from the bare metal surface. Because of scattering from various optical components, this polarization cross-out can be achieved only to 10⁻⁵ of the total reflected light intensity from the surface. A lock-in amplifier can detect this background with a noise level of 1%. Therefore, a change of 10⁻⁷ or larger in reflection due to adsorption of atoms or molecules on the metal surface can be detected.

With the above set-up, the following quantity

$$S(\theta) \propto |r_p(\theta) E_p - r_s(\theta) E_s e^{i\Delta\phi}|^2 + \Delta'$$

$$\propto \left| \frac{r_p(\theta)}{r_p(0)} - \frac{r_s(\theta)}{r_s(0)} \right|^2 + \Delta$$

$$\propto |\Delta r(\theta)|^2 + \Delta, \quad (3)$$

is measured with Δ being the scattered background, and $r_p(\theta)$ ($r_s(\theta)$) and E_p (E_s) the field reflectivity at coverage θ and the field amplitude for the p (s) polarization, respectively. The quantity $\Delta\phi = \phi_p - \phi_s$ is the phase shift between the p and s polarizations introduced by the Babinet phase compensator. The relation $\frac{E_s}{E_p} e^{i\Delta\phi} = \frac{r_p(0)}{r_s(0)}$ set in the experiment has been used to obtain the second equation. The last equation defines $\Delta r(\theta) = \frac{r_p(\theta)}{r_p(0)} - \frac{r_s(\theta)}{r_s(0)}$.

The principle underlying this method is simple. It is well known that atoms or molecules adsorbed on a metal surface respond to p-polarized light much more strongly than to s-polarized light. For s-polarized light, the reflectance from metal surface is almost unity and the phases between the incident and the reflected light are opposite, so that the field immediately outside the metal is nearly zero. With a molecule adsorbed at such positions, the response must be very weak. For p-polarized light, the situation is completely different. The boundary conditions at the metal surface do not require the field at the surface to be zero. This component induces a polarization on the adsorbed molecules and causes $r_p(\theta)$ to differ appreciably from $r_p(0)$. Therefore, the quantity $\Delta r(\theta)$ is finite.

Although the principle is described for a metal substrate, it is valid for any material with a high index of refraction such as semiconductors.

In practice, the condition $\frac{E_s}{E_p} e^{i\Delta\phi} = \frac{r_p(0)}{r_s(0)}$ can never be met exactly due to mis-adjustment. If we introduce two parameters, δ_{am} and δ_{ph} , to represent the mis-adjustment for the amplitude and the phase, respectively:

$\frac{E_s}{E_p} e^{i\Delta\phi} = \frac{r_p(0)}{r_s(0)} (1 + \delta_{am}) e^{i\delta_{ph}}$, then the final form of the measured signal is:

$$S(\theta) \propto \left\{ \left| \frac{r_p(\theta)}{r_p(0)} - \frac{r_s(\theta)}{r_s(0)} (1 + \delta_{am}) e^{i\delta_{ph}} \right|^2 \right\} + \Delta$$

$$\propto \left\{ |\Delta r(\theta) - \delta_{am} - i\delta_{ph}|^2 \right\} + \Delta. \quad (4)$$

Unlike the background Δ , which is incoherent with respect to $\Delta r(\theta)$, the misadjustment terms δ_{am} and δ_{ph} are coherent with respect to $\Delta r(\theta)$. They can be exploited in a heterodyne technique to improve the sensitivity of measuring $\Delta r(\theta)$ by about one order of magnitude⁵.

To reach the highest sensitivity of measuring $\Delta r(\theta)$, in principle, δ_{am} and δ_{ph} should be chosen as large as possible so that the signal is dominated by the interfering term $2\text{Re}\{(\delta_{am} + i\delta_{ph})\Delta r(\theta)\}$. Unfortunately, along with the enhancement in signal, δ_{am} and δ_{ph} also contribute to the noise significantly through the term $|\delta_{am} - i\delta_{ph}|^2$. Therefore the compromised values of $|\delta_{am}|^2$ and $|\delta_{ph}|^2$ should be on the order of 1×10^{-5} of the reflected light intensity.

As mentioned earlier, the minimum reflectance change $S(\theta)$ we are able to measure is 10^{-7} of the reflected light intensity. Although it is two orders of magnitude better than other schemes for measuring $\Delta R(\theta)/R$ ^{6,7}, the sensitivity of measuring $\Delta r(\theta)$ is only comparable to those schemes, in which the effective δ_{am} and δ_{ph} have been chosen nearly unity and therefore the strength of the signal $2\text{Re}\{(\delta_{am} + i\delta_{ph})\Delta r(\theta)\}$ is correspondingly about two orders of magnitude larger. As a result, our scheme has not improved the sensitivity for $\Delta r(\theta)$. The advantage here is the simplicity of the set-up.

With this linear reflectance technique, we measured the adsorption and the laser induced thermal desorption for CO/Ni(110). In Fig. 5 we plot the differential reflectance signal $S(\theta(t))$ as a function of time. The signal increases as we dose CO onto the Ni(110) surface until saturation, which corresponds to a full CO monolayer. At time $t \sim 350$ sec a strong laser pulse with 1.1J/cm^2 is applied to desorb CO from the surface. Immediately the signal drops to a low level which corresponds to a low CO coverage. At time $t = 410$ sec the signal recovers as more CO molecules are adsorbed on to the surface until saturation is reached again. A second laser pulse with 0.9J/cm^2 is applied some time later and the signal drop is less, corresponding to a reduced CO desorption.

With a calibrated relation between coverage and exposure time as obtained by TDS², the differential reflectance signal $S(\theta(t))$ can be related to CO coverage. In Fig. 6, the desorption yield is shown as a function of desorption laser energy for three different initial coverages. The accuracy in determining the desorption yield is better than 0.05 monolayer, which is much better than reflection SHG. In principle a sensitivity of 0.01 monolayer can be achieved. We are basically limited by the long term instability from mechanical drifts of the optics and sample in our set-up.

c) Laser Heating Model and Laser Induced Thermal Desorption

The reason that a laser pulse can desorb adsorbed atoms or molecules from the surface is that the laser heats up the surface in a very short time. Models have been developed for this process⁸. In all the models, the absorbed laser energy is instantaneously converted into heat, which results in an increase in the surface temperature. The equations that govern this temperature change are the heat-conduction equation and the Fourier's law:

$$\nabla \cdot \mathbf{J}(\mathbf{r},t) + \rho C_p \frac{\partial T(\mathbf{r},t)}{\partial t} = A(\mathbf{r},t), \quad (5)$$

$$\mathbf{J}(\mathbf{r},t) = -K \nabla T(\mathbf{r},t), \quad (6)$$

where ρ , C_p , K are the density, heat capacity and heat conductance of the substrate, respectively and \mathbf{J} is the heat flux. The laser heating effect is represented by the source term $A(\mathbf{r},t)$, or by boundary conditions, depending on the model. The two equations above can be combined into a diffusion equation

$$\nabla^2 T(\mathbf{r},t) - \frac{1}{\kappa} \frac{\partial T(\mathbf{r},t)}{\partial t} = -\frac{A(\mathbf{r},t)}{K}, \quad (7)$$

with $\kappa = K/\rho C_p$, the heat diffusion constant. In our situation the laser spot is usually very large compared with the heat diffusion length $\xi \sim (\kappa \tau_p)^{1/2} \sim 1 \mu$. Therefore the lateral heat diffusion on the time scale of laser pulse duration τ_p can be neglected and the lateral temperature dependence can be treated quasi-statically. This reduces the heat diffusion equation to a one dimension.

There are two common ways to treat the laser heating effect: one is called surface heating, the other, volume heating. In the surface heating model, the source term is assumed to be a delta function and can be effectively represented by a boundary condition

$$K \frac{dT(r,t)}{dz} \Big|_{z=0} = -(1-R)I(r,t) \Big|_{z=0}, \quad (8)$$

where R is the reflectance, and $I(r,t)$ is the laser intensity at the surface. Using the fact that the temperature far into the bulk of the substrate is constant, the surface temperature rise is given by

$$\Delta T(t) = \frac{\Delta E(r)}{\Delta A} (1-R) \cos \theta_{inc} \frac{1}{\sqrt{\pi \tau_p}} \int_{-\infty}^t \frac{dt'}{\sqrt{\pi \rho C_p K}} \frac{\exp(-t'^2/\tau_p^2)}{\sqrt{t-t'}}, \quad (9)$$

where $\Delta E / \Delta A$ is the laser energy impinging on the surface, and θ_{inc} is the incident angle. For the surface heating model to be valid, the heat diffusion length ξ must be much longer than the laser absorption depth. This condition can be met by metals, which have a very high thermal conductivity and a large absorption coefficient for light. However, for materials such as semiconductors, which have reasonable thermal conductivity but a low light absorption coefficient, the surface heating model may fail. A better way to treat the problem is the volume heating model, which takes

$$A(r,t) = I_m (1-R) \alpha \exp(-\alpha z) f(r) q(t) \quad \text{and}$$

$$\frac{dT(r,t)}{dz} \Big|_{z=0} = 0, \quad (10)$$

where functions $f(r)$, $q(t)$ describe the spatial and temporal shape of the laser pulse in the medium, I_m is the peak intensity at the surface, and α the absorption coefficient. The solution for the surface temperature rise is now given by

$$\Delta T(t) = \frac{I_m(1-R)\alpha\kappa}{2\sqrt{\pi}K} f(r) \int_{-\infty}^t dt' \exp(-t'^2/\tau_p^2) \exp[\kappa\alpha^2(t-t')] \operatorname{erfc}[\alpha[\kappa(t-t')]^{1/2}], \quad (11)$$

where the complementary error function is defined by

$$\operatorname{erfc}(t) = \frac{2}{\sqrt{\pi}} \int_t^{\infty} \exp(-x^2) dx .$$

In the limit $\alpha \rightarrow \infty$, the result of volume heating model reduces to that of the surface heating model.

For the laser induced thermal desorption experiments on CO/Ni(110), the reflectance of Ni at the incident angle $\theta_{inc} \sim 0^\circ$ is $R=0.728$, the laser pulse width is $\tau_p = 10\text{nsec}$, and the density, heat capacity and heat conductance of Ni are $\rho = 8.902\text{g/cm}^3$, $C_p = 6.23\text{cal/mol.K}$ and $K = 91\text{W/m.K}$, respectively⁹. With the desorption rate of CO from Ni(110) given by a first order process

$$\frac{d\theta}{dt} = -v\theta e^{-E_{des}/k_B T(t)}, \quad (12)$$

v the desorption pre-exponential factor, E_{des} the desorption energy, and k_B the Boltzmann constant, the thermal desorption yield is

$$\Delta\theta(t) = \theta_s \left\{ 1 - \exp\left(- \int_{-\infty}^t \nu e^{-E_d/k_B T(t')} dt' \right) \right\}. \quad (13)$$

In Fig. 7, we have shown the laser-induced surface temperature rise $\Delta T(t)$ and the desorption yield $\Delta\theta(t)$ from such a calculation. The desorption yield data from both methods now can be fit by the surface heating model. The solid lines in Fig.3(a) and Fig. 6 are fits of the data using Eqs. (9) and (13). The fitting parameters for the desorption data with reflection SHG method are $\nu = 1 \times 10^{14}$ and $E_{des} = 28 \text{ kcal/mol}$. For the data with the linear reflectance method, $\nu = 1 \times 10^{14}$ and $E_{des} = 30 \text{ kcal/mol}$ for initial coverage $\theta_0 = 1.0$ and $\nu = 2 \times 10^{14}$ and $E_{des} = 32 \text{ kcal/mol}$ for $\theta_0 = 0.50$ and $\theta_0 = 0.25$. These results are in good agreement with previous measurements by other techniques¹⁰.

C. Adsorbate gratings

As pointed out in the introduction, the creation of a monolayer grating is crucial for diffusion measurements with optical diffraction methods. To make a monolayer adsorbate grating, we interfered two laser beams at the sample surface to produce a spatially modulated light intensity pattern

$$I(x) = I_0 \left[1 + r \cos\left(\frac{2\pi x}{s}\right) \right], \quad (14)$$

where I_0 is the average intensity, s the grating spacing, r the contrast of the interference pattern, and x the coordinate on the surface. With this intensity profile and the relation of desorption yield versus laser intensity from the

measurements described in section 2, the adsorbate grating, namely the coverage as a function of x can be mapped out. This is shown in Fig. 3.

The diffraction signal from this adsorbate grating can be estimated. In the SH diffraction case, the adsorbate induced second order nonlinear susceptibility $\Delta\chi_{\text{eff}}^{(2)}(\theta)$ is modulated by the adsorbate grating $\theta(x)$ with a periodicity s , therefore the diffraction signal of the n -th order is given by

$$S_n \sim |A_n|^2,$$

$$A_n = \lim_{L \rightarrow \infty} \frac{2}{L} \int_{-L/2}^{L/2} \chi_{\text{eff}}^{(2)}(\theta(x)) \exp(i\frac{2n\pi x}{s}) dx, \quad (15)$$

where L is the dimension of the grating. Assuming a simple case with $\chi_{\text{eff}}^{(2)}(\theta(x)) = A+B\theta$. The ratio

$$\frac{S_n}{S_0} \sim \frac{1}{n^2 \pi^2} \left| \frac{B\theta_n}{A+B\theta_0} \right|^2 \quad (16)$$

can be estimated with known A , B , θ_0 and θ_n , where θ_n is the n -th Fourier component of the adsorbate grating. Since S_0 can be easily measured for any system without a grating on the surface, the diffraction signals can then be estimated by Eq. (16).

In the linear diffraction case, the estimate is very similar. We only have to replace $\chi_{\text{eff}}^{(2)}(\theta)$ by the field reflectivity $r(\theta)$. That is

$$\frac{S_n}{S_0} \sim \left| \frac{r_n}{r_0} \right|^2$$

$$\sim \frac{1}{n^2 \pi^2} \left| \frac{r(\theta) - r(0)}{r(0)} \right|^2, \quad (17)$$

with r_n defined as

$$r_n = \lim_{L \rightarrow \infty} \frac{2}{L} \int_{-L/2}^{L/2} r(\theta(x,t)) \exp(i \frac{2n\pi x}{s}) dx, \quad n=0,1,2,\dots$$

If the absolute change in the reflectivity is known, the absolute strength of the diffraction signal can be estimated. Typically, $r(\theta) - r(0)$ is about $10^{-4} - 10^{-3}$ so the first order diffraction signal will be $10^{-9} - 10^{-7}$ of the reflection.

The periodicity s of the grating is determined by the angle between the two interfering laser beams. With the half angle denoted by ϕ , the grating spacing is given by

$$s = \frac{\lambda}{2 \sin \phi}. \quad (18)$$

The choice of this spacing depends on the diffusion rate. As we will see in the next section, the diffusion coefficient D is related to the decay time constant τ of the n th-order diffraction by $\tau = s^2 / 8\pi^2 n^2 D$. The maximum decay time constant we can measure is limited by the long term stability of the system and the rate of contamination of the sample surface. This time is typically one hour. The minimum decay time constant is limited by the data acquisition time. In the SH diffraction case it is about half an hour, but in the linear diffraction case it can be less than a second. It is then seen that properly adjusting the grating spacing, the dynamic range of the diffusion coefficient we can measure can extend from 10^{-6} to 10^{-15} cm^2/sec .

The depth of the adsorbate grating should be chosen according to the signal-to-noise ratio of the diffraction signal and can be controlled by the intensities of the two interfering laser beams. Typically, an initial signal-to-noise ratio of 10 is required for diffusion measurement with 20% accuracy in determining the diffusion coefficient. For large response systems the adsorbate grating can be made shallow, i.e., with a small coverage modulation. For small response systems the adsorbate grating should have a large coverage modulation. A control of this coverage modulation relies on the control of the two laser beams' intensities. As we will see, the linear diffraction method has the capability for detecting shallow gratings, while the SH diffraction method may require a deep grating.

D. Optical Diffraction as a Probe of Surface Diffusion

a) Second Harmonic Diffraction Probe

In the second harmonic diffraction case, the surface specificity of the signal eliminates the background from the bulk metal so that no modulation scheme is necessary. This can be seen as follows. Since the scattered light intensity in the diffraction direction is roughly 10^{-6} of the reflected intensity and the diffraction signal is on the order of 1/10 of the adsorbate-induced SH reflection signal, the signal-to-background ratio is then 10^5 due to the fact that the change in SHG signal due to adsorption is comparable to the bare surface signal. The optical arrangement for the diffusion experiment is shown in Fig.8. A single-mode Q-switched Nd:YAG laser with a pulse width of 10ns at $1.06\mu\text{m}$ was used for both the creation of the adsorbate grating and the SH diffraction

measurement. The detection of the diffraction signal relies on the knowledge of the diffraction spot position. One can calculate this diffraction spot position from the relation

$$k_{x n}(2\omega) = 2 k_x(\omega) + \frac{2\pi n}{s}, \quad (19)$$

where $k_{x n}(2\omega)$ and $k_x(\omega)$ are the tangential components of the wavevectors for the n -th order diffraction second harmonic beam and the incident fundamental beam respectively. In practice, the alignment of the detection system then is performed using the calculated angle between the reflection direction and the diffraction direction.

The diffusion of atoms or molecules on a surface can be related to the diffraction signal in a simple way. The solution of the one dimensional diffusion equation

$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial x} \left(D \frac{\partial \theta}{\partial x} \right), \quad (20)$$

with a periodic initial condition can be expressed in terms of a Fourier series expansion:

$$\theta(x,t) = \theta_0 + \sum_{n=1}^{\infty} \theta_n(t) \cos(2n\pi x/s). \quad (21)$$

If D is assumed to be independent of the coverage θ , we further obtain

$$\theta(x,t) = \theta_0 + \sum_{n=1}^{\infty} \theta_n^0 \cos(2n\pi x/s) \exp(-4n^2\pi^2Dt/s^2). \quad (22)$$

From Eq. (15) we find the n-th order diffraction signal to be

$$\begin{aligned} S_n(t) &\propto |\theta_n|^2 \\ &= S_{0n} \exp(-8\pi^2n^2Dt/s^2), \end{aligned} \quad (23)$$

with the diffusion coefficient only related to the decay time $\tau = s^2/8\pi^2n^2D$ but not to the signal strength if the optical response $\chi_{\text{eff}}^{(2)}(\theta(x))$ is linear with the coverage θ . With this important result the diffusion coefficient measurement can be achieved simply by measuring the diffraction signal decay.

b) Linear Diffraction Probe

The disadvantage of SH diffraction is that the nonlinear optical process is usually very weak so the signal strength can be very small. However, linear optical processes can have tremendously stronger response than SHG. The difficulty in applying linear diffraction for probing surface diffusion is that the signal from a monolayer grating of adsorbates is buried in a much stronger scattered background, which is typically 10^{-6} of the reflected intensity. This renders a direct measurement of diffraction signal difficult.

To overcome this difficulty, we have to use a method in which the diffracted signal is modulated differently from the scattered background. One way to achieve this is polarization modulation. If we realize that the scattered background light is arising from the roughness of the surface and the defects in

the bulk, then the intensity is not strongly dependent on the incident light polarization. In contrast, the diffraction signal from a monolayer grating is a response to the electric field at the surface and therefore is strongly polarization dependent. For s-polarization the electric field at the surface is almost zero, for p-polarization the electric field at the surface is nonzero. Therefore, modulating the polarization of the incident light suppresses the scattered background. The suppress can be achieved to as much as a factor of 10^5 . With a signal strength comparable with the background the signal-to-background ratio is about 10^5 . In this way, the sensitivity of detecting a monolayer grating with optical linear diffraction is greatly enhanced compared to the SH diffraction case.

The linear diffraction set-up is shown in Fig. 9. A polarized He-Ne beam (5mW) first passes through a photoelastic modulator which modulates the polarization sinusodally at 50kHz. Then the beam is enlarged by about a factor of 3 with a telescope. This beam is slightly focused by a 2m lens onto the sample surface. A PMT detector is aligned in the first order diffraction direction by using the relation

$$s(\sin\theta_n - \sin\theta_0) = n\lambda, \quad (24)$$

where θ_n is the n-th order diffraction angle, θ_0 is the incident angle, and $n = \pm 1$ for the first order diffraction. Experimentally, this direction can also be determined if a permanent grating is created with the two interfering beams. The diffusion coefficient is deduced in the same way as in the SH diffraction case. The diffraction signal detected by the set-up in Fig. 8 is expressed as

$$S_n = |r_{np}|^2 I_p - |r_{ns}|^2 I_s, \quad (25)$$

with
$$r_{n\kappa} = \lim_{L \rightarrow \infty} \frac{2}{L} \int_{-L/2}^{L/2} r_{\kappa}(\theta(x)) \exp(i \frac{2n\pi x}{s}) dx, \quad \text{for } \kappa = s, p.$$

With the incident light being polarization modulated to give intensities

$$\begin{aligned} I_p &\sim |E_p|^2 \cos^2(\psi \sin \omega t + \phi_0), \\ I_s &\sim |E_s|^2 \sin^2(\psi \sin \omega t + \phi_0), \end{aligned} \quad (26)$$

with ψ the phase modulation amplitude, ω the modulation frequency, and ϕ_0 the residual phase in the modulator, the lock-in amplifier then detects a signal of

$$S_n = \frac{V_p + V_s}{2} + \frac{V_p - V_s}{2} \cos(\psi \sin \omega t + \phi_0), \quad (27)$$

with V_p and V_s the diffraction signal strength for p and s polarizations respectively. The cosine function in Eq. (27) can be expanded into Fourier series and the coefficients of the Fourier series are given by different orders of Bessel functions. With $\phi_0 = 0$, only even harmonics have nonvanishing coefficient and with $\phi_0 = \pi/2$ only odd harmonics have nonvanishing coefficient. If we desire to measure a signal with the fundamental frequency, the phase $\phi_0 = \pi/2$ has to be introduced with a quarter wave plate.

The optical diffraction methods off an adsorbate grating for surface diffusion measurement have a number of very attractive features. First, it involves a simple one-dimensional diffusion process for which the data analysis is relatively straightforward. Second, by properly orienting the grating, the

diffusion coefficient along any direction on the surface can be directly measured. Third, as an optical method, the technique can be applied to a wide variety of adsorbate-substrate systems. Fourth, with a tunable probe beam selectively probing particular species of adsorbates, surface diffusion of individual components of a mixed adsorbate layer can be monitored. This allows the study of influence of surface diffusion on surface reactions. Finally, the technique can be used to study other forms of surface diffusion such as diffusion of electronic or vibrational excitations.

E. Measuring Coverage Dependence of Diffusion

In order to study the coverage dependence of diffusion, two schemes are considered. The first scheme is simple and easily implemented. The second one involves some careful considerations and at present still is difficult to implement.

In the first scheme, we make an adsorbate grating with shallow depth $\Delta\theta$. Upon establishing a uniform coverage of adsorbates through dosing, we use two laser beams with prescribed intensities to interfere at the surface. The intensities of the two beams are chosen so that only a little desorption takes place to create an adsorbate grating with a small modulation depth $\Delta\theta$. The choice of this depth is limited by the strength of the diffraction signal for the specific system under study. In the CO/Ni(110) case, the depth is chosen to be 0.05 ML. With such a shallow grating the diffusion coefficient can be very well approximated as a constant and can be described by Eq. (23). With varying

initial coverages the dependence of the diffusion coefficient with coverage can be determined.

The second scheme for coverage dependent diffusion study is principally the same as the Boltzmann-Matano method¹², where a step coverage was initially created. With laser desorption by a spatially modulated intensity, a single step coverage profile is difficult to achieve and even if it is achieved, the diffraction signal would be very weak. Naturally, a series of step-like coverage profiles with a periodicity defined by the interfering beams can be easily realized by choosing a large enough intensity modulation. If we can detect not only the first order diffraction signal but also all the higher orders, in principle, the evolution of the coverage profile can be determined. With this known coverage profile as a function of time, it is possible for us to solve the diffusion equation numerically and find the coverage dependent diffusion coefficient.

To examine this clearly, let us start with the Fourier expansions of the coverage and the diffusion coefficient

$$\theta(x,t) = \theta_0 + \sum_{n=1}^{\infty} \theta_n(t) \cos(2n\pi x/s), \quad (28)$$

$$D(\theta(x,t)) = D_0 + \sum_{n=1}^{\infty} D_n(t) \cos(2n\pi x/s). \quad (29)$$

Assuming the Fourier components as functions of time in the expansion of coverage are known from the multiple diffraction measurements, then substituting them into the diffusion equation,

$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial x} \left(D \frac{\partial \theta}{\partial x} \right),$$

we obtain

$$\begin{aligned} & \sum_{n=0}^{\infty} \frac{\partial \theta_n(t)}{\partial t} \cos(2n\pi x/s) \\ &= \frac{\partial}{\partial x} \left(\sum_{n=0}^{\infty} D_n(t) \cos(2n\pi x/s) \frac{\partial}{\partial x} \sum_{n=0}^{\infty} \theta_n(t) \cos(2n\pi x/s) \right). \end{aligned}$$

By carrying out the derivatives and collecting the terms with the same base function, we can show that

$$\begin{aligned} \frac{\partial \theta_0(t)}{\partial t} &= 0, \\ \frac{\partial \theta_1(t)}{\partial t} &= -\frac{\pi^2}{a^2} \left(D_0(t) - \frac{1}{2} D_2(t) + \frac{\sum_{n \neq 1} n [D_{n+1}(t)\theta_n(t) - D_{n-1}(t)\theta_n(t)]}{2\theta_1(t)} \right) \theta_1(t), \quad (30) \end{aligned}$$

and generally,

$$\frac{\partial \theta_m(t)}{\partial t} = -\frac{m^2 \pi^2}{a^2} \left(D_0(t) - \frac{1}{2} D_{m+1}(t) + \frac{\sum_{n \neq m} n [D_{n+1}(t)\theta_n(t) - D_{n-1}(t)\theta_n(t)]}{2\theta_m(t)} \right) \theta_m(t). \quad (31)$$

These are coupled equations for the $D_n(t)$'s. By solving them we should be able to obtain all the components of D_n . From them we can easily construct

$$D(\theta(x,t)) = D_0 + \sum_{n=1}^{\infty} D_n(t) \cos(2n\pi x/s)$$

There are two ways to determine D as a function of θ from the above equation. The first one is to sit at a fixed position x and watch the coverage change as a function of time. For any time t , there is a corresponding θ and a corresponding $D(\theta)$. A complete mapping for D from variable t to θ can be achieved if the change of coverage at the chosen position x covers the full range. The second way is to fix the time and examine the coverages at different positions within a period of the grating. $D(\theta)$ can then be mapped out through the variable x .

In order to complete the discussion, we still have to relate the Fourier components of the coverage to all different orders of diffraction signals. For such a purpose we need to know the coverage dependent reflectivity $r(\theta)$ first. This can be approximately measured by the method we discussed in section 2. For an adsorbate grating given by Eq. (25) we have

$$r(\theta(x,t)) = r_0 + \sum_{n=1}^{\infty} r_n(t) \cos(2n\pi x/s), \quad (32)$$

and the n -th order diffraction signal is directly proportional to the $|r_n(t)|^2$. To relate these measured quantities to the Fourier components of coverage $\theta_n(t)$, we utilize the inverse function $\theta(r)$ of $r(\theta)$ and then solve them in terms of $r_n(t)$.

To elaborate on this point further, let us expand $r(\theta)$ into a power series,

$$r(\theta) = \sum_{n=0}^{\infty} a_n (\theta - \theta_0)^n \quad (33)$$

around the average coverage θ_0 . Substituting the Fourier expansions for both the coverage and the reflectivity into the above equation, we can then relate the measured quantities $r_n(t)$ to $\theta_n(t)$. One important point is that the phases of the Fourier components of the reflectivity are not directly measurable since only the diffraction intensity was measured and not the diffraction field. In simple cases such as a real functional dependence, the phases reduce to plus or minus and it is possible to determine them by constructing a self consistent coverage evolution profile. In more complicated situations direct determination of phases is needed. This is yet to be solved in this multiple diffraction scheme.

Despite the difficulties in the second scheme, it is still very intriguing. With a slightly complicated set-up to measure all the orders of diffraction, coverage dependent diffusion coefficient measurement requires the creation of only one single grating. The data analysis is then supposed to give complete information on $D(\theta)$ with θ almost as a continuous variable. This is certainly in strong contrast with the first scheme, where the coverage dependence measurement is done by varying the initial coverage. Since it can save a tremendous amount of experimental time, the second scheme is attractive. The additional problem is that if the diffusion coefficient is not only dependent on the coverage but also the coverage gradient, then the measured $D(\theta)$ in the two schemes can be different. Even though theoretically it is possible, practically, that effect may be very small as compared to the coverage dependence itself.

References:

- ¹ For reviews of surface SHG see G. I. Richmond, J. M. Robinson, and V. L. Shannon, *Prog. Surf. Sci.* **28**, 1(1988); T. F. Heinz and G. A. Reider, *Trends Anal. Chem.* **8**, 235(1989); Y. R. Shen, *Nature* **337**, 519(1989).
- ² For example, R. J. Behm, G. Ertl, and V. Penka, *Surf. Sci.* **160**, 387(1985).
- ³ X. D. Zhu, Winfried Daum, Xu-dong Xiao, R. Chin and Y. R. Shen, *Phys. Rev. B* **43**, 11571(1991).
- ⁴ Xu-dong Xiao, X. D. Zhu, Winfried Daum, and Y. R. Shen, accepted for publication by *Phys. Rev. B*.
- ⁵ Xu-dong Xiao, Yuanlin Xie, and Y. R. Shen, to be published.
- ⁶ Graciela B. Blanchet, P. J. Estrup, and P. J. Stiles, *Phys. Rev. Lett.* **44**, 171(1980); *Phys. Rev. B.* **22**, 3655(1981).
- ⁷ D. E. Aspnes, *J. Vac. Sci. Technol. B* **3**, 1498(1985); 1138(1985); D. E. Aspnes, J. P. Harbison, A. A. Studna and L. T. Florez, *Appl. Phys. Lett.* **52**, 957(1988).
- ⁸ J. H. Bechtel, *J. Appl. Phys.* **46**, 1585(1975).
- ⁹ American Institute of Physics Handbook, 3rd ed., ed. by D. Gray (McGraw-Hill, New York, 1972), pp. 4-106, 4-154.
- ¹⁰ C. S. Feigerle, S. R. Desai, and S. H. Overbury, *J. Chem. Phys.* **93**,787(1990).
- ¹¹ X. D. Zhu, A. Lee, and A. Wong, *Appl. Phys. A.* **52**, 317(1991).
- ¹² For example, W. Jost, *Diffusion in Solids, Liquids, Gases*, (Academic Press, New York, 1960).

Figure Captions

Figure 1: Optical set-up for experiment using optical second harmonic generation to probe laser induced thermal desorption. F1 and F2 are color filters and Q is a quartz plate employed to cancel the SHG signal from the bare Ni(110) surface by interference.

Figure 2: $|\Delta\chi_{\text{eff}}^{(2)}(\theta)|^2$ versus coverage θ measured by SHG with the plane of incidence parallel to $[1\bar{1}0]$ and the p-in/p-out polarization combination.

Figure 3: (a) Desorption mass yield versus desorbing laser energy as measured by laser induced thermal desorption. The solid line is a theoretical calculation from Eq. (3) with $\nu=1 \times 10^{14}$ and $E_{\text{des}}=28 \text{ kcal/mol}$. The dashed line along the data points is for eyeguide; (b) Laser energy distribution at the surface from two interfering laser beams; (c) The resulting coverage grating created by the laser energy distribution in (b).

Figure 4: Sketch of the experimental set-up for differential reflectance measurement. P is the polarizer, A the analyzer, and C the phase compensator.

Figure 5: Differential reflectance signal $S(\theta(t))$ versus time for CO adsorption (at CO pressure 2.5×10^{-8} torr) and laser induced thermal desorption kinetics on Ni(110) surface.

Figure 6: Laser induced thermal desorption yield versus laser energy for CO/Ni(110) system at three different initial coverages: $\theta_0=0.25$, $\theta_0=0.5$, and $\theta_0=1.0$. The solid curves are fits from a simple thermal desorption model discussed in the text.

Figure 7: Surface temperature rise $\Delta T(t)$ and laser-induced desorption yield $\Delta\theta(t)$ as a function of time calculated from Eq.(9) and(13). The laser energy and the desorption parameters used for the calculation are $1.0\text{J}/\text{cm}^2$ and $\nu = 1 \times 10^{14}$ and $E_{\text{des}} = 30\text{kcal}/\text{mol}$ respectively. The surface temperature levels at a different value from its initial one due to the fact that no heat dissipation mechanism has been introduced in the model.

Figure 8: Experimental set-up for surface diffusion experiment with SH diffraction detection. A single laser shot at $1.06\mu\text{m}$ is always used to generate an adsorbate grating. The decay of the grating is monitored by the first-order SH diffraction using the $0.532\mu\text{m}$ probe beam.

Figure 9: Schematic of the experimental arrangement for detection of first-order linear diffraction from a monolayer grating on Ni(110). The He-Ne laser has been polarization-modulated by entering into the chamber. The diffraction angle with respect to reflection can be calculated.

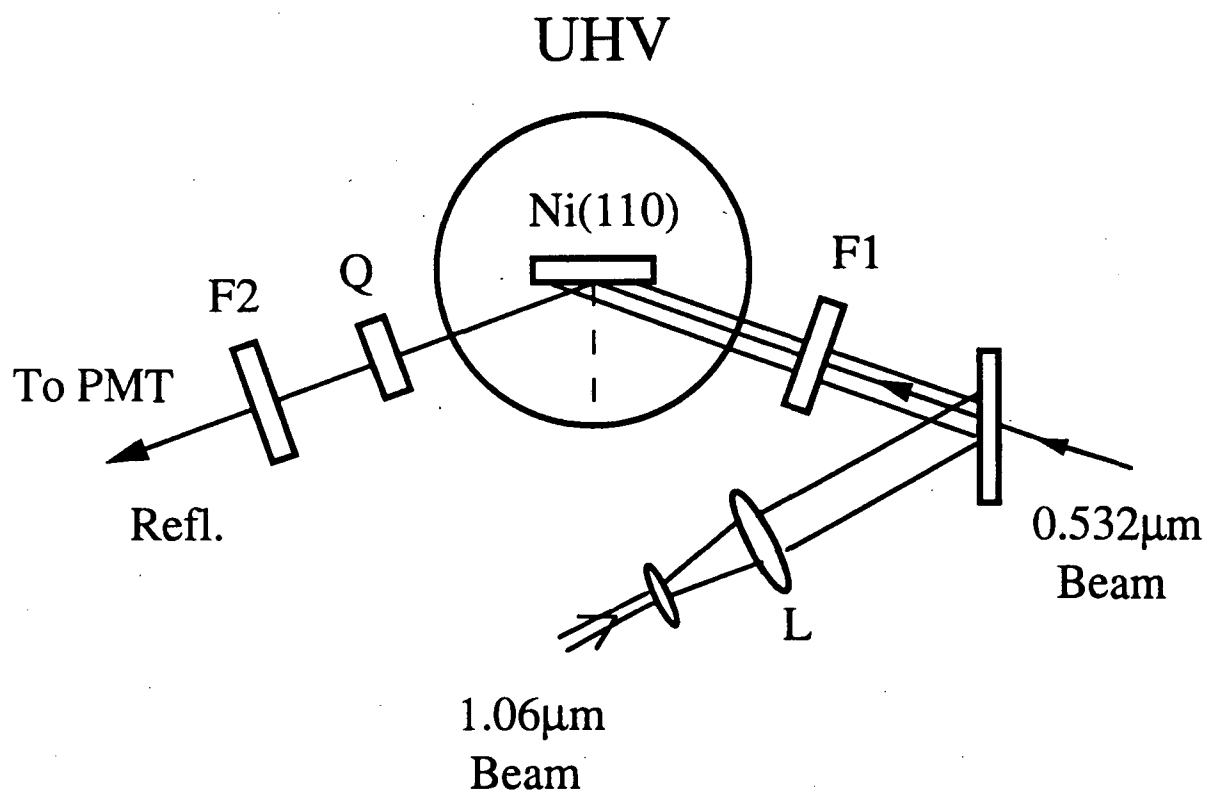


Figure 1

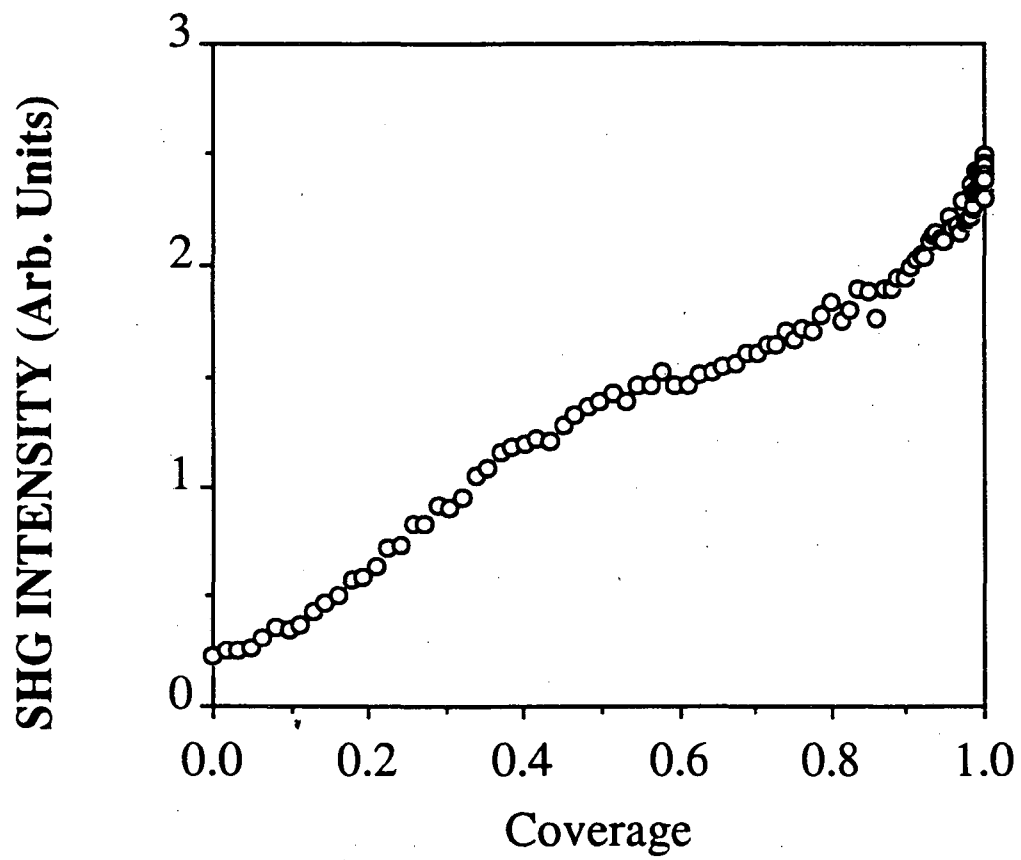


Figure 2

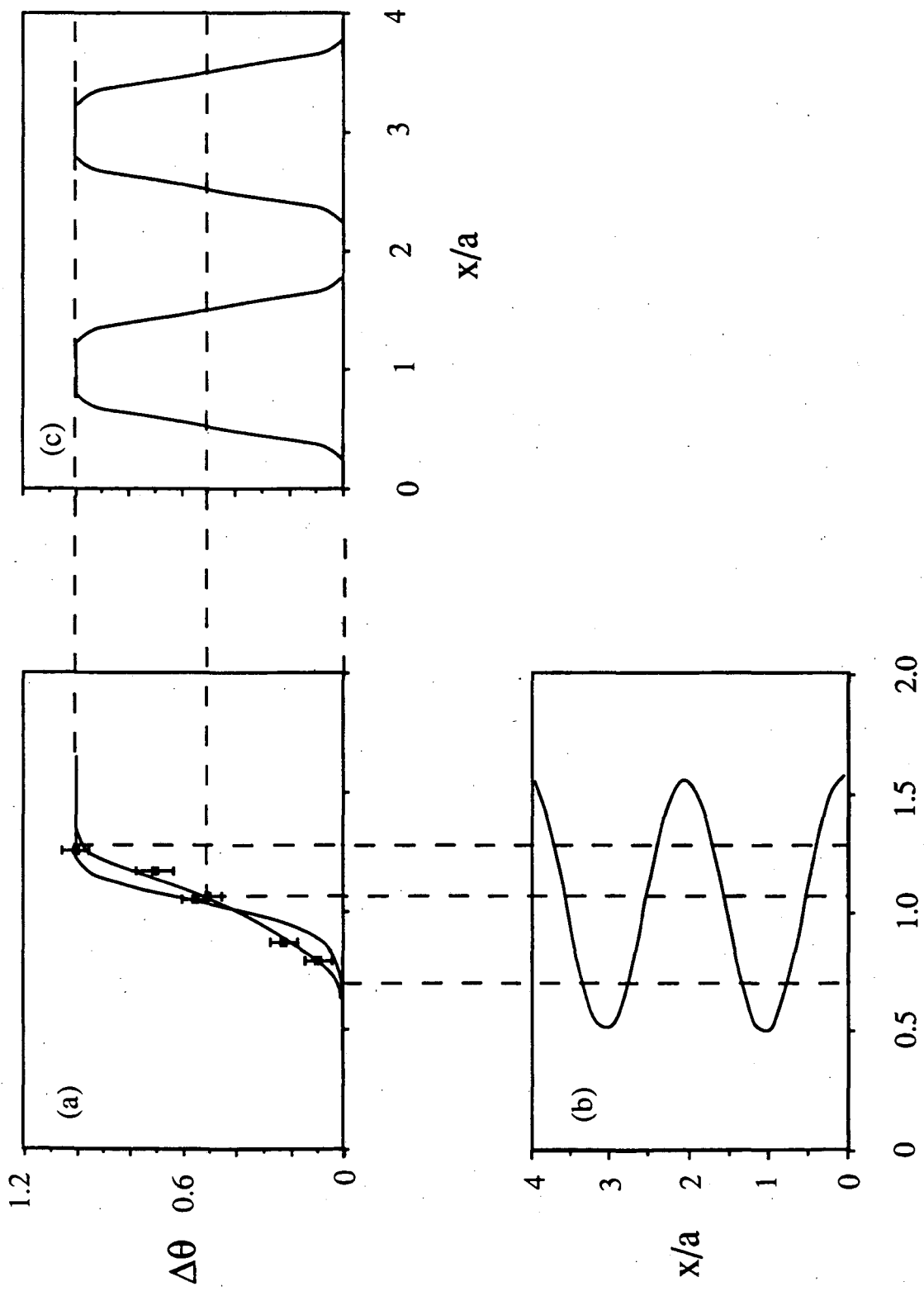


Figure 3

Energy(J/cm²)

Vacuum Chamber

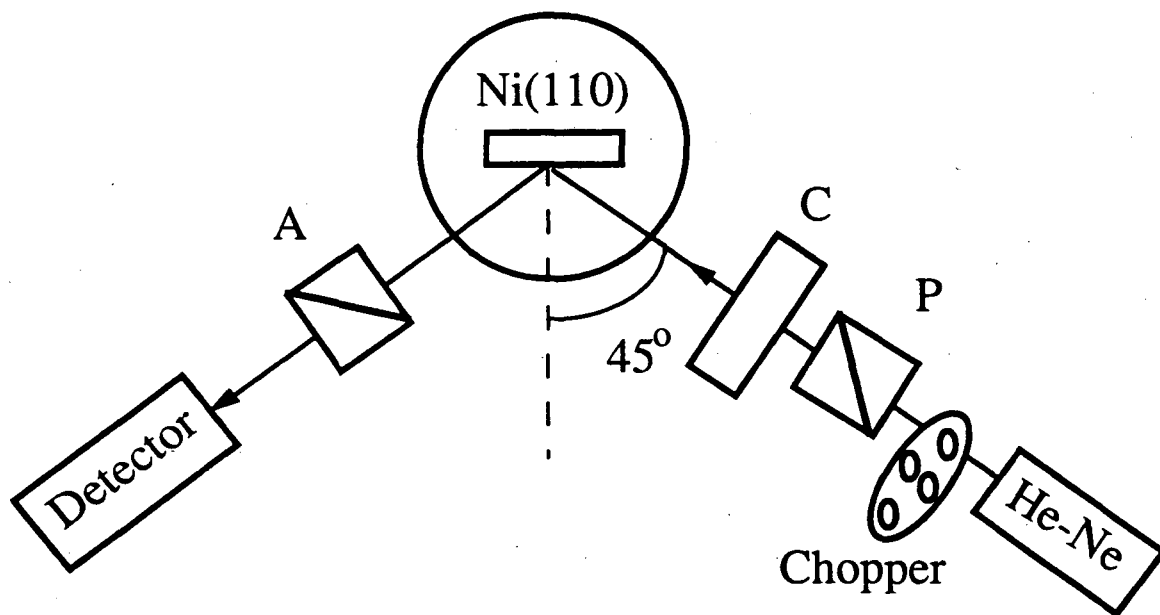


Figure 4

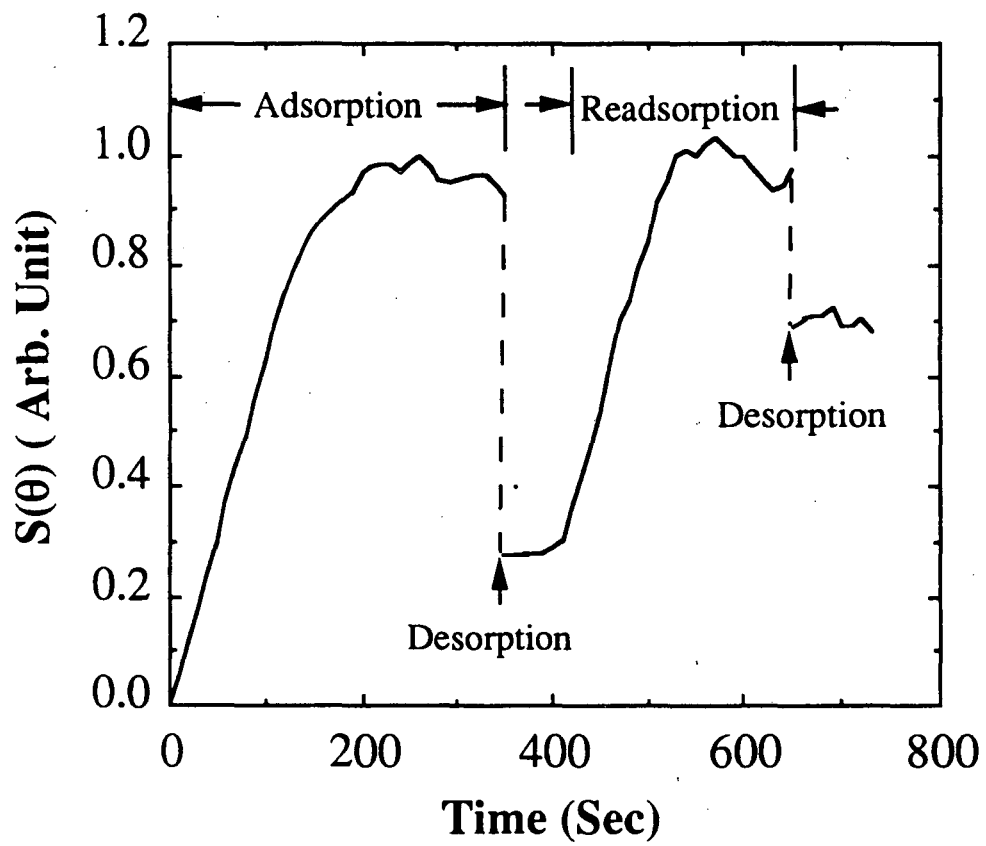


Figure 5

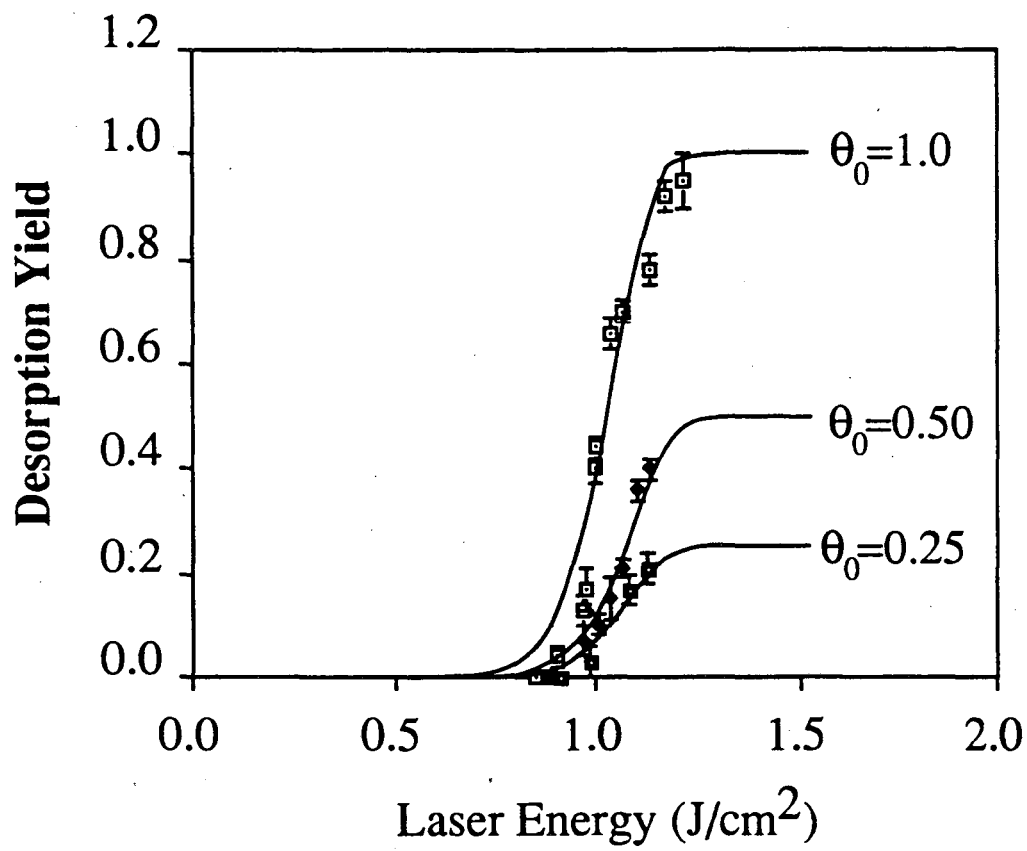


Figure 6

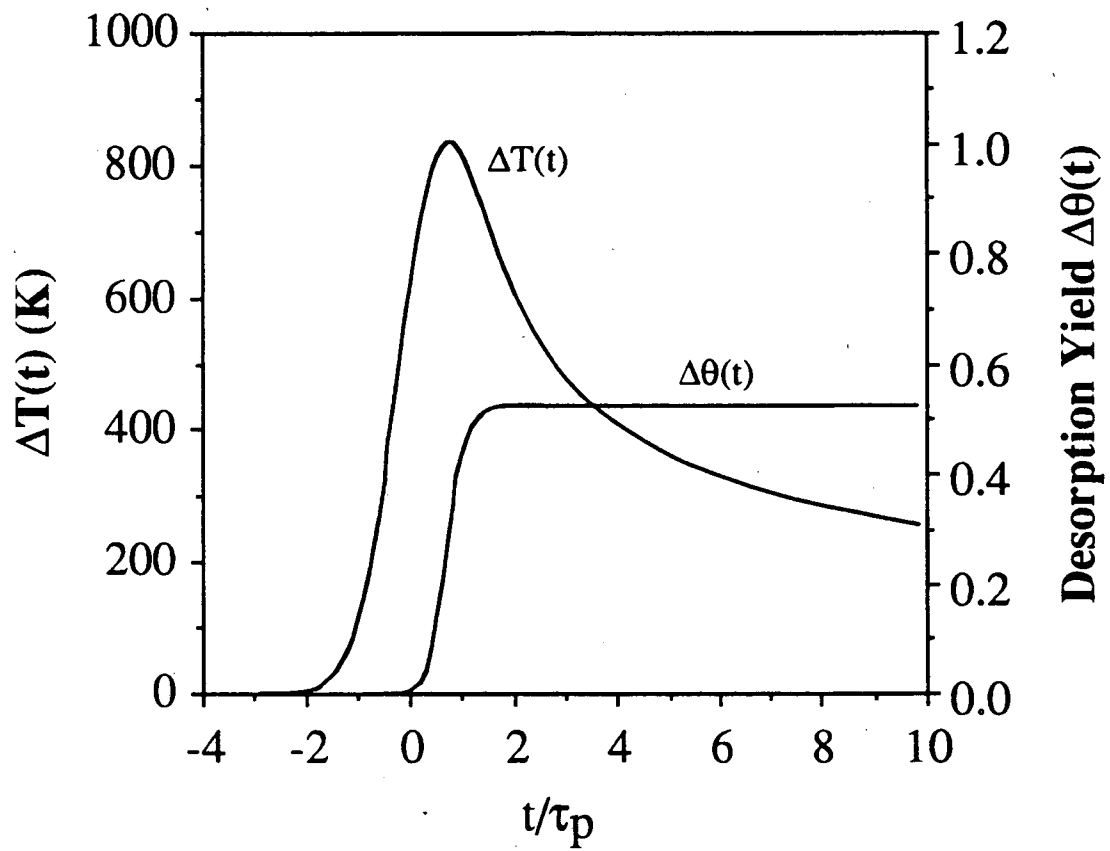


Figure 7

Vacuum Chamber

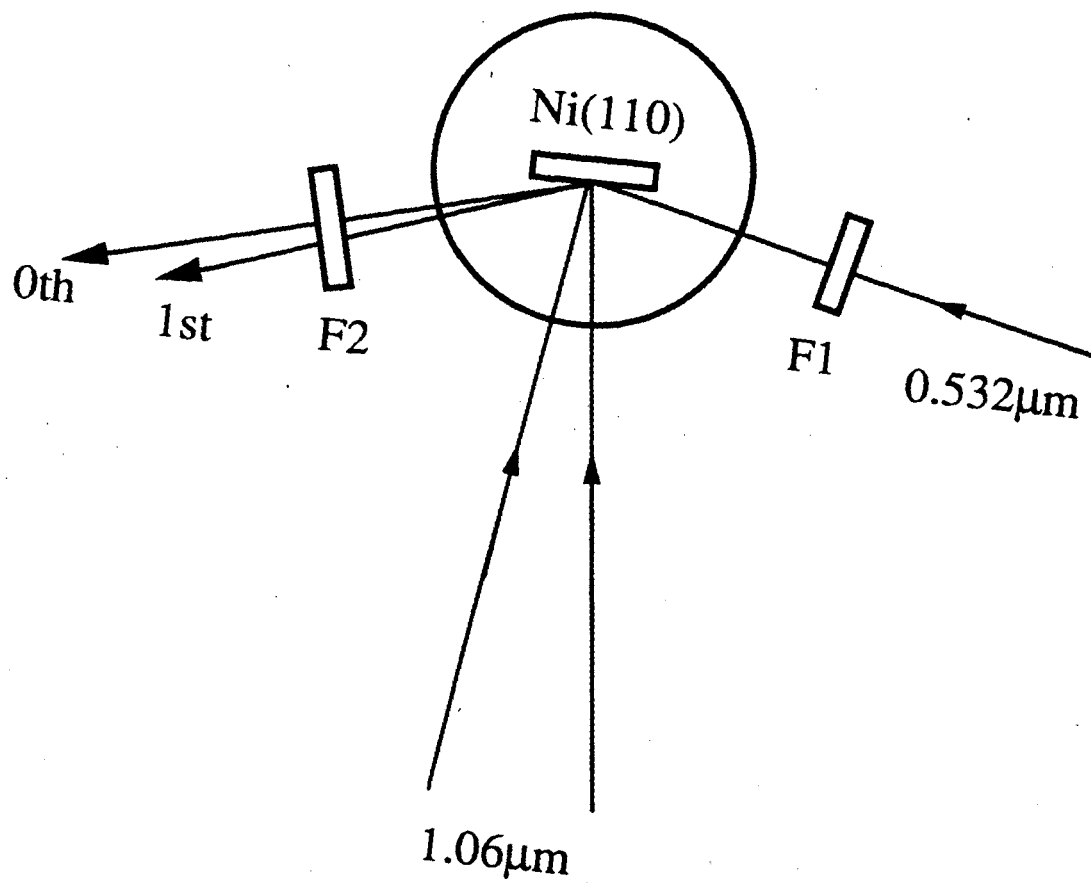


Figure 8

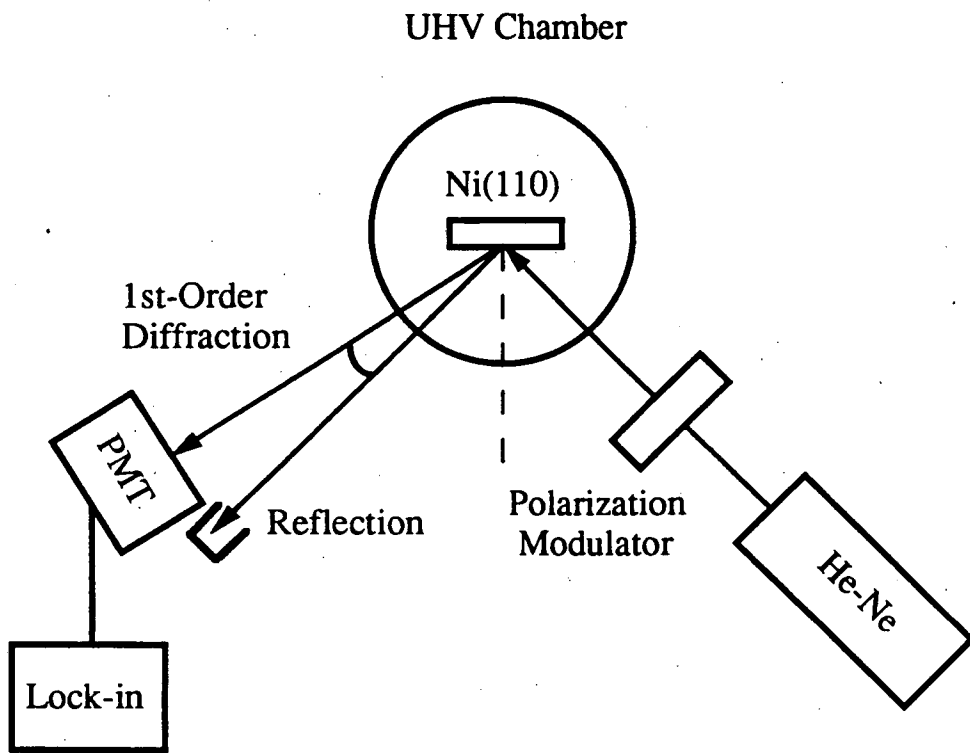


Figure 9

IV. Optical Second Harmonic Diffraction Study of Anisotropic Surface Diffusion: CO on Ni(110)

A. Introduction

The study of heterogeneous surface diffusion is a fundamental step towards understanding the mechanism of many surface processes, ranging from associative desorption of adsorbates, epitaxial crystal growth, to catalysis.^{1,2,3} It can also provide useful information about the effective surface potential and diffusion pathways experienced by adsorbates. On crystalline surfaces, the structural anisotropy is expected to effect anisotropy in surface diffusion. Anisotropic surface diffusion can cause preferential development of surface reactions in certain forms and is therefore important in the practical consideration of controlling surface reactions. Surprisingly, despite its importance, research effort on anisotropic surface diffusion so far has been rather limited. This is presumably due to limitation in the existing experimental techniques.

In this chapter I will present an anisotropic surface diffusion study using the SH diffraction off a monolayer grating technique. As discussed in chapter III, this method is particularly suitable for surface diffusion anisotropy study. The system chosen to demonstrate the technique is CO/Ni(110).⁴ The Ni(110) surface has a row structure with atoms closely packed in the $[1\bar{1}0]$ direction (see Fig. 1). The CO molecules can adsorb with almost equal probabilities on both top and short-bridge sites up to a coverage of $\theta=0.85$.⁵ For $\theta>0.85$, the CO molecules are pushed to the short-bridge site to form zig-zag chains along the $[1\bar{1}0]$ rows with adjacent CO molecules displaced in the $[001]$ and $[00\bar{1}]$

directions respectively⁶. At a full coverage, the tilt angle of CO molecular axis with respect to the surface normal is $\sim 20^\circ$ and the adsorbate structure appears as 2×1 .⁶ Obviously, surface diffusion of CO on Ni(110) at all coverages must be anisotropic. At an average CO coverage of $\theta_0 \sim 0.5$ we can expect diffusion along $[1\bar{1}0]$ as jumping from top or short-bridge sites to short-bridge or top sites; and along $[001]$ as jumping from top sites to top sites and from short-bridge sites to short-bridge sites. Thus one would anticipate the existence of two independent diffusion channels, one along $[1\bar{1}0]$ and the other along $[001]$. They were indeed identified in our experiment. The diffusion energies and the pre-exponential factors for the two channels were deduced. Both of them show strong anisotropy, namely, the diffusion energy is significantly larger along $[001]$ than along $[1\bar{1}0]$, accompanied by a larger pre-exponential factor also along $[001]$. Our results are however approximate since the coverage dependence of the diffusion coefficients has not been taken into account in the analysis. The coverage dependence of surface diffusion for CO/Ni(110) will be the topic of next chapter.

B. Experiment

a) Sample Preparation

The experiment was performed in an ultrahigh vacuum (UHV) chamber with a base pressure of 1.0×10^{-10} torr. The single crystal Ni(110) sample was cut and mechanically polished to within 0.3° from the (110) plane with the miscut along the $[001]$ direction, and mounted vertically on a rotatable sample holder capable of more than 90° of rotation about $[110]$. Before any

measurement, the surface of the sample was first Ar^+ sputtered (at 1.0×10^{-4} torr with a 500V beam voltage for approximately 30 minutes) at room temperature until no impurity contamination could be detected by the Auger electron spectrometer within its detection limit ($<0.3\%$ for carbon, and $<0.5\%$ for sulfur). The sample was then annealed at 1070K for a few seconds followed by a slow cooling down to the measurement temperature. Right before each dosing of CO the sample was flash heated to 570K to remove residual adsorbed molecules from the ambient, mostly hydrogen and CO. The adsorption of CO on Ni(110) surface was carried out at approximately 100K by introducing CO into the chamber through a leak valve. A sharp 1×1 LEED pattern was observed for a clean Ni(110) surface and a 2×1 pattern for a full CO monolayer on Ni(110). In order to avoid possible alternation of the surface and the adsorbate monolayer by the electron beam in the LEED measurement, separately prepared monolayers were used for the diffusion experiment. A Chromel-Alumel thermal couple welded to the sample was used to monitor the sample temperature. The diffusion experiment was conducted in a temperature range of 100K to 170K and was controlled to within 2K. The average CO coverage for all the diffusion experiments at different temperatures and in different directions was $\theta_0 \sim 0.5$, with $\theta=1$ defined as full CO coverage with one CO molecule per Ni atom on the surface .

b) Diffusion Measurement

The optical arrangement for diffusion experiment has been shown in Fig.8 of chapter III. A single-mode Q-switched Nd:YAG laser with a pulse width of 10ns at 1.06mm was used for both the monolayer grating creation and the

SH diffraction measurement. To create a CO monolayer grating on Ni(110), the 1.06mm beam was split into two and then recombined at incident angles of $\phi = \pm 1.50^\circ$ with an overlapping area of $\sim 2\text{mm}$ in diameter on the Ni(110) surface fully covered by CO. The grating period was $s = \lambda / 2 \sin \phi \sim 20\mu\text{m}$. The two beams' intensities were chosen so that the average intensity I_0 corresponded to a desorption yield of 0.5ML, and the contrast of $r = 0.53$ was enough to modulate the adsorbate from full coverage to zero coverage, making a square-wave-like pattern. This kind of grating could yield the highest SH diffraction signal. To probe the diffusion, a frequency-doubled laser beam at $0.532\mu\text{m}$ from the Nd:YAG laser was used. Its intensity was $\sim 1/10$ that of the desorbing beam. The beam was incident at 70° with respect to the surface normal and the first-order second harmonic (SH) diffraction from the CO grating was detected as a function of time in order to probe the decay of the CO grating via CO diffusion. The probe beam was not strong enough to desorb CO from Ni, as could be checked by monitoring SHG in the specularly reflected direction. Alternatively, this was made sure by creating a CO adsorbate grating in the [001] direction at $\sim 100\text{K}$ and monitoring the change in the first-order SH diffraction. No change was found for several hours, indicating that diffusion, desorption, and adsorption of CO are all negligible in that circumstance. The diffusion coefficient could be deduced from the decay of the diffracted SH signal.

In comparison with CO/Ni(111) diffusion, the CO-induced SHG from Ni(110) is 4~5 times smaller than that from Ni(111)^{7,8,9}. The desorption energy range is also very narrow for CO on Ni(110) as opposed to CO on Ni(111)¹⁰. In the present case, the desorption laser energy has to be controlled to within 2~3% of $1.24\text{J}/\text{cm}^2$ in order to create a good grating that can yield a reasonable SH diffraction level ($\sim 80\text{counts}/5\text{min}$, with $S/N \sim 10$ in our measurement). These reasons make the surface diffusion experiment of CO/Ni(110) rather difficult.

Moreover, for gratings along different crystalline orientations, the SH diffraction signal may differ by about 10% because the p-in/p-out SH response with the plane of incidence parallel to different crystalline directions involve different components of the second-order nonlinear susceptibility tensor $\chi^{(2)}(\theta)$. For instance, $\chi_{\text{eff}}^{(2)}$ is a linear combination of $\chi_{\text{zzz}}^{(2)}$, $\chi_{\text{xzx}}^{(2)}$, and $\chi_{\text{zxx}}^{(2)}$ if the plane of incidence is parallel to $[1\bar{1}0]$ and a linear combination of $\chi_{\text{zzz}}^{(2)}$, $\chi_{\text{zyz}}^{(2)}$, and $\chi_{\text{zyy}}^{(2)}$ if the plane of incidence is parallel to $[001]$. Nevertheless, this magnitude difference would not affect the diffusion coefficient measurement since it affected the signal strength but not the decay time constant, which is directly related to the diffusion coefficient as has been seen in Chapter III.

The diffusion anisotropy was measured in the following way. For measurement of CO diffusion along a selected direction on Ni(110), the sample was rotated to have that direction in the plane of incidence of the desorbing laser beams. The CO monolayer grating on the surface could then be created by the method described in Chapter III. The diffusion measurement along such a chosen direction was subsequently carried out at a few temperatures in order to find the temperature dependence of the diffusion coefficient $D(T)$. Measurements were performed for CO diffusion not only along the principal axes of Ni(110) but also along other directions of interest.

C. Relations Between Diffusion Coefficient and the SH Diffraction Signal

Surface diffusion is generally characterized by a rank-2 diffusion coefficient tensor \vec{D} which is related to the particle flux \mathbf{J} and the surface

concentration C by

$$\mathbf{J} = -\vec{\mathbf{D}} \cdot \nabla C. \quad (1)$$

The tensor can be diagonalized along symmetry axes in the surface. For the case of Ni(110) the axes for diagonalization are $[\bar{1}\bar{1}0]$ and $[001]$, so that we have

$$\vec{\mathbf{D}} = \begin{pmatrix} D_{[\bar{1}\bar{1}0]} & 0 \\ 0 & D_{[001]} \end{pmatrix}. \quad (2)$$

Thus for surface diffusion along a direction at an angle ϕ away from $[\bar{1}\bar{1}0]$, the diffusion coefficient is given by

$$D(\phi) = D_{[\bar{1}\bar{1}0]} \cos^2 \phi + D_{[001]} \sin^2 \phi. \quad (3)$$

As discussed in the Chapter III, we are interested in observing surface diffusion from the time-dependent smearing of a monolayer grating of adsorbates. In this case, surface diffusion is governed by the one-dimensional diffusion equation

$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial x} \left(D \frac{\partial \theta}{\partial x} \right), \quad (4)$$

with a periodic initial condition. In the case of coverage independent D the solution is

$$\begin{aligned}
\theta(x,t) &= \theta_0 + \sum_{n=1}^{\infty} \theta_n(t) \cos(2n\pi x/s) \\
&= \theta_0 + \sum_{n=1}^{\infty} \theta_n^0 \cos(2n\pi x/s) \exp(-4n^2\pi^2 D t/s^2), \quad (5)
\end{aligned}$$

where θ_n^0 are constants. More generally, D depends on θ and the solution becomes more complicated. This will be discussed later in the discussion section.

The nonlinear susceptibility $\chi_{\text{eff}}^{(2)}(\theta)$ responsible for SHG from a CO covered Ni(110) surface can be separated into two parts, one from the bare metal substrate, and the other from the adsorbate-induced contribution which depends on coverage:

$$\chi_{\text{eff}}^{(2)}(\theta) = \chi_{\text{eff}}^{(2)}(0) + \Delta\chi_{\text{eff}}^{(2)}(\theta), \quad (6)$$

If $\theta(x)$ is periodic in x , then $\chi_{\text{eff}}^{(2)}(\theta)$ is also periodic in x , and can be written as

$$\chi_{\text{eff}}^{(2)}(\theta(x)) = \chi_{\text{eff}}^{(2)}(0) + \sum_{n=0}^{\infty} A_n(t) \cos(2n\pi x/s) \quad (7)$$

with

$$A_n = \lim_{L \rightarrow \infty} \frac{2}{L} \int_{-L/2}^{L/2} \chi_{\text{eff}}^{(2)}(\theta(x)) \exp(i \frac{2n\pi x}{s}) dx. \quad (8)$$

SHG from such a susceptibility grating appears both in specular reflection and in diffraction. The specularly reflected SH signal is proportional to $|\chi_{\text{eff}}^{(2)}(0) + A_0|^2$ and the n th-order diffracted SH signal is proportional to $|A_n|^2$.

Consider the simple case that $\Delta\chi_{\text{eff}}^{(2)}(\theta)$ is linearly proportional to the coverage θ . Then $A_n \propto \theta_n$ and the n th-order SH diffraction is given by

$$\begin{aligned} S_n(t) &\propto |\theta_n|^2 \\ &= S_{0n} \exp(-8\pi^2 n^2 D t / s^2), \end{aligned} \quad (9)$$

From the time constant of the exponential decay of the diffracted SH signal, the diffusion coefficient D can be deduced. Note that the decay time constant is independent of the grating pattern except the grating spacing s . If $\Delta\chi_{\text{eff}}^{(2)}(\theta)$ is not linearly proportional to θ , the situation again becomes more complicated as $S_n(t)$ is no longer proportional to $|\theta_n(t)|^2$. The decay of $S_n(t)$ would appear as multi-exponential. This will be discussed in the discussion section.

D. Experimental Results

The measured data of the first-order SH diffraction signal versus time from CO monolayer gratings on Ni(110) along three different directions, $[1\bar{1}0]$ ($\phi=0^\circ$), $[001]$ ($\phi=90^\circ$), and $\phi=45^\circ$, are presented in Fig. 2(a), 2(b), and 2(c), respectively. Assuming that Eq. (9) is valid, we fit the data at each temperature by a single exponential, as shown by the solid curves in Fig. 2. From the fit and using Eq. (9) with $n=1$, we can deduce the decay time constant and hence the

diffusion coefficient $D(T)$ (with $s=20\mu\text{m}$). The fluctuation of the data points was mainly due to the poor signal-to-noise ratio. The uncertainty in determining the diffusion coefficient D is around $\pm 40\%$.

The deduced diffusion coefficient D versus $1/T$ is plotted in Fig. 3 for CO diffusion along the three specific directions on Ni(110). The results for diffusion along the orthogonal directions, $[1\bar{1}0]$ and $[001]$, are well described by the Arrhenius form,

$$D = D_0 \exp(-E_{\text{diff}}/k_B T). \quad (10)$$

This indicates that CO diffusion on Ni(110) has two distinct channels, one along $[1\bar{1}0]$ and the other along $[001]$. The fit of Eq. (10) to the data points in Fig. 3 yields

$$\text{along } [1\bar{1}0]: E_{\text{diff}}([1\bar{1}0]) = 1.1 \pm 0.2 \text{ kcal/mol, (0.048eV)}$$

$$D_0([1\bar{1}0]) = (3.8 \pm 2.0) \times 10^{-9} \text{ cm}^2/\text{sec};$$

$$\text{along } [001]: E_{\text{diff}}([001]) = 3.1 \pm 0.4 \text{ kcal/mol, (0.134eV)}$$

$$D_0([001]) = (4.8 \pm 4.4) \times 10^{-6} \text{ cm}^2/\text{sec}.$$

That surface diffusion of CO on Ni(110) is anisotropic is obvious from the above results. For diffusion along the direction $\phi=45^\circ$, we expect from Eq. (3)

$$D(\phi=45^\circ) = \frac{1}{2} (D_{[1\bar{1}0]} + D_{[001]}) \quad (11)$$

Plotted in Fig. 3, Eq. (11) fits the experimental data very well. Note that two combined exponential functions of $1/T$ are needed to describe $D(\phi=45^\circ)$. This further supports the picture of two orthogonal independent diffusion channels of CO on Ni(110).

Figure 4 depicts the measured D as a function of the diffusion direction specified by ϕ at fixed temperature $T \sim 110\text{K}$. The solid curve calculated from Eq. (3) is also in good agreement with the data. The diffusion anisotropy at $T = 110\text{K}$ is obviously very significant.

E. Discussion

In deducing the diffusion coefficient D from our experiment, we have made a number of simplifying assumptions (see Sec. C). In this section, we shall first consider the effects of those assumptions and other possible experimental complications before we discuss the implication of the experimental results.

a) Heating Effect From the Probing Beam

One may wonder if the laser beam used to probe the monolayer grating would heat up the sample surface and significantly affect the surface diffusion of the adsorbates. In our measurements, the fluence of the probe laser pulse was $\sim 0.1 \text{ J/cm}^2$. Using Eq. (9) in Chapter III, we estimate a maximum temperature rise of 65K for the Ni surface at $t \sim 10\text{nsec}$ due to laser heating. This temperature rise decays away to $\Delta T < 10\text{K}$ at $t \sim 40 \text{ nsec}$. From Eq. (10), we find $D(T+\Delta T)/D(T)$

= 10 to 500 for a temperature range of $T \sim 100$ to 170K with $\Delta T = 65\text{K}$ if $E_{\text{diff}} = 3.1$ kcal/mol. The excess mean square displacement resulting from $D(T+\Delta T)$ during the heating period of $\delta t \sim 40\text{nsec}$ is given by $\Delta\langle x^2 \rangle = \int_0^{\delta t} 2\{D(T+\Delta T) - D(T)\} dt \sim 2D(T+\Delta T)\delta t$. This is negligible compared to the mean square displacement $2D(T)\Delta t$ of CO molecules during the period $\Delta t = 0.1\text{sec}$ between two successive laser pulses. For smaller E_{diff} , the effect is even smaller. Thus we can conclude that the probe laser heating effect is insignificant in our surface diffusion measurements.

b) Coverage Dependence of Nonlinear Susceptibility

In the data analysis, we assumed $\Delta\chi_{\text{eff}}^{(2)}(\theta)$ is linear in θ . This is not true in general and is a poor approximation for CO on Ni(110) as seen in Fig. 2 of Chapter III. As mentioned briefly in Sec. C, the nonlinear relation between $\Delta\chi_{\text{eff}}^{(2)}(\theta)$ and θ may cause the first-order SH diffraction to decay multi-exponentially or non-exponentially. This can be seen by expanding $\Delta\chi_{\text{eff}}^{(2)}(\theta)$ into power series of $(\theta - \theta_0)$, where θ_0 is the average surface coverage of the monolayer grating.

$$\Delta\chi_{\text{eff}}^{(2)}(\theta) = \Delta\chi_{\text{eff}}^{(2)}(\theta_0) + \left(\frac{d\Delta\chi_{\text{eff}}^{(2)}}{d\theta} \right)_{\theta_0} (\theta - \theta_0) + \frac{1}{2} \left(\frac{d^2\Delta\chi_{\text{eff}}^{(2)}}{d\theta^2} \right)_{\theta_0} (\theta - \theta_0)^2 + \dots$$

$$+ \frac{1}{6} \left(\frac{d^3 \Delta \chi_{\text{eff}}^{(2)}}{d\theta^3} \right)_{\theta_0} (\theta - \theta_0)^3 + \dots \quad (12)$$

From Eq. (8), the first-order SH diffraction amplitude takes the form

$$\begin{aligned} A_1(t) = & \left(\frac{d\Delta\chi_{\text{eff}}^{(2)}}{d\theta} \right)_{\theta_0} \theta_1^0 \exp(-t/2\tau) + \\ & + \frac{1}{2} \left(\frac{d^2\Delta\chi_{\text{eff}}^{(2)}}{d\theta^2} \right)_{\theta_0} \sum_{m=1} \theta_m^0 \theta_{m+1}^0 \exp(-[m^2+(m+1)^2]t/2\tau) \\ & + \frac{1}{8} \left(\frac{d^3\Delta\chi_{\text{eff}}^{(2)}}{d\theta^3} \right)_{\theta_0} \left\{ \sum_{(m,n)=1} \theta_m^0 \theta_n^0 \theta_{m+n+1}^0 \exp(-[m^2+n^2+(m+n+1)^2]t/2\tau) \right. \\ & \left. + \sum_{(m,n)=1} \theta_m^0 \theta_n^0 \theta_{m+n-1}^0 \exp(-[m^2+n^2+(m+n-1)^2]t/2\tau) \right\} \\ & + \dots \quad (13) \end{aligned}$$

where $\tau = s^2/8\pi^2D$ and D is assumed constant. Since generally, $\theta_{m+1}^0 < \theta_m^0$

$< 1/2$ for $m > 1$, we expect that the higher-order terms can be appreciably smaller

than the first term in Eq. (13). The two leading correction terms are

$$\frac{1}{2} \left(\frac{d^2\Delta\chi_{\text{eff}}^{(2)}}{d\theta^2} \right)_{\theta_0} \theta_1^0 \theta_2^0 \exp(-5t/2\tau), \quad \text{and} \quad \frac{1}{8} \left(\frac{d^3\Delta\chi_{\text{eff}}^{(2)}}{d\theta^3} \right)_{\theta_0} (\theta_1^0)^3$$

$\times \exp(-3t/2\tau)$. For $t > \tau/2$, they are further reduced by factors larger than

$e^{-5/4}$ and $e^{-3/4}$, respectively. Thus we can conclude that if $\Delta\chi_{\text{eff}}^{(2)}(\theta)$ can be

approximated by a power series expansion of Eq. (12) and if the data analysis puts more emphasis on the diffraction data at later times, then a single-exponential decay of the diffraction with $\Delta\chi_{\text{eff}}^{(2)}(\theta) = \Delta\chi_{\text{eff}}^{(2)}(\theta_0) + \left(\frac{d\Delta\chi_{\text{eff}}^{(2)}}{d\theta} \right)_{\theta_0} x(\theta - \theta_0)$ is a fair approximation. In principle, one can make grating groove sufficiently shallow to render $\Delta\chi_{\text{eff}}^{(2)}(\theta) \propto (\theta - \theta_0)$ so that the decay would certainly be single exponential. Unfortunately, limited by the diffraction signal strength which is proportional to $|\Delta\chi_{\text{eff}}^{(2)}(\theta)|^2$, this may not always be possible.

For the case of CO on Ni(110), the experimental data of $\Delta\chi_{\text{eff}}^{(2)}(\theta)$ can be approximated by (see Fig. 2 of Chapter III)

$$\Delta\chi_{\text{eff}}^{(2)}(\theta) \approx 0.707 + 0.707(\theta - \theta_0) - 0.354(\theta - \theta_0)^2 + 0.354(\theta - \theta_0)^3 + \dots, \quad (14)$$

with $\theta_0 = 0.5$. If we assume an initial CO monolayer grating of the rectangular periodic form

$$\theta(x) = 0.5 + \sum_{n=1}^{\infty} \frac{2}{n\pi} \sin\left(\frac{n\pi}{2}\right) \cos(2n\pi x/s), \quad (15)$$

Then we can show from Eq. (13) that by keeping only the first term in Eq. (13), the decays calculated from $|A_1(t)|^2$ with $t \geq 0$, $t \geq \tau/2$, and $t \geq \tau$ are 22%, 4%, and 1% slower than the real case.

In deducing D from fitting our experimental data with $|A_1(t)|^2$, we recognized the poor signal-to-noise ratio at large t. We therefore fit the data with a single exponential starting from t=0, knowing that the deduced value of D could be larger than the real value by about 22%. This is especially true for the

lower temperature cases, where less data with $t > \tau/2$ are available because of larger τ . These systematic errors make our deduced diffusion activation energies and pre-exponential factors somewhat smaller than their real values.

c) Coverage Dependence of Diffusion Coefficient

The diffusion coefficient generally also depends on the surface coverage of adsorbates which we have neglected in our data analysis. If the dependence of D on θ is strong and the grating groove depth is deep, then even with $\Delta\chi_{\text{eff}}^{(2)}(\theta)$ linear in θ , the first-order SH diffraction will not have a single exponential decay. This is seen as follows.

Assume $D(\theta)$ can be described by a power series

$$D(\theta) = D(\theta_0) [1 + d_1(\theta - \theta_0) + d_2(\theta - \theta_0)^2 + \dots] \quad (16)$$

From Eqs. (4) and (5), we find,

$$\frac{\partial \theta_1}{\partial t} = - \frac{\pi^2}{a^2} D(\theta_0) \left[\theta_1 + \frac{1}{2} d_1 \theta_1 \theta_2 + \frac{1}{4} d_2 \theta_1^3 + \dots \right] \quad (17)$$

$$\frac{\partial \theta_2}{\partial t} = - \frac{4\pi^2}{a^2} D(\theta_0) \left[\theta_2 + \frac{1}{4} d_1 \theta_1^2 - \frac{11}{8} d_1 \theta_1 \theta_3 \dots \right].$$

.....

It is obvious that the solution of Eq. (17) will give a $\theta_1(t)$ with a non-exponential or multi-exponential decay. Thus even if $\Delta\chi_{\text{eff}}^{(2)}(\theta) \propto (\theta - \theta_0)$ so that $A_1(t) =$

$(d\Delta\chi_{\text{eff}}^{(2)}/d\theta)_{\theta_0} \theta_1(t)$ from Eq. (13), the first-order SH diffraction may decay non-exponentially. However, if $d_1\theta_1\theta_2$ and the higher-order terms in Eq. (17) are much smaller than θ_1 , we still have

$$\frac{\partial\theta_1}{\partial t} \cong -\frac{\pi^2}{a^2} D(\theta_0) \theta_1$$

and hence $\theta_1(t) \propto \exp(-t/2\tau)$, from which $D(\theta_0)$ can be deduced. This can be achieved with a sufficiently small θ_2 either from a shallow monolayer grating with a small initial θ_2^0 or by waiting long enough for θ_2 to decay to a small value.

In our experiment, the CO monolayer grating was square-wave-like with a modulation ranging from zero to full coverage. We estimated $\theta_2^0 \sim 0.1$. The fact that the decay of SH diffraction can be roughly fit by single exponentials suggests $d_1 \ll 20$ and $d_2 \ll 4$. The values of $D(\theta_0)$ deduced from the experiment are accurate to within a factor of 5 judging from the above discussion.

As we will see in Chapter V, the diffusion coefficient has a strong coverage dependence and therefore with a deep modulation on the coverage grating our data analysis can only provide some kind of effective diffusion coefficient D . What is the meaning of this D ? Is it the diffusion coefficient at the average coverage? To answer these questions, let us use a coverage dependent $D(\theta)$ given by

$$D(\theta) = D(0), \quad \text{for } \theta < c$$

$$= D(0)\exp\left(d(T) \frac{\theta-c}{1-c}\right), \quad \text{for } \theta > c \quad (18)$$

where $d(T)$ is a temperature dependent constant and decreases as temperature increases. As we will see in Chapter V, this coverage dependent diffusion coefficient $D(\theta)$ can describe CO diffusion on Ni(110) with $c = 0.67$ quite well. With this $D(\theta)$, we have solved the diffusion equation (Eq. (4)) numerically for an initial square-wave coverage profile. The evolution of the coverage is shown in Fig. 5(a) for $d=2.5$. It is clear from this graph that the high coverage region smears out significantly faster than the low coverage region, especially in the early time period ($t < s^2/8\pi^2 D(\theta=0.9)$). The calculated SH diffraction signal for $d=2.5$ (Eq.(8)) by taking Eq. (14) for $\Delta\chi_{\text{eff}}^{(2)}(\theta)$ is depicted in Fig. 5(b). The diffusion coefficient obtained is $\sim 3.5D(0)$ if we limit the approximate data fitting to decay to only 70% of the initial signal and is $\sim 1.25D(0)$ if we fit the data approximately down to 5% of the initial signal. The physical picture here is that in the early time period, diffusion occurs mostly in the high coverage region and therefore the diffusion coefficient deduced from the SH signal corresponds to high coverage values. As time goes on, the weighting of the lower coverage ($\theta < 0.7$) diffusion becomes larger and larger and brings the deduced diffusion coefficient close to low coverage values. This result clearly demonstrates that D deduced from our measurement, in general, is neither the diffusion coefficient at the average coverage (which should be $D(0)$ in the above case) nor that of a unique effective coverage. Depending on the length of the relative time t/τ ($\tau = s^2/8\pi^2 D(0)$) in which the data has been collected, the deduced D may correspond to the value at a very high coverage (if $t/\tau \ll 1$) or to that at a somewhat lower coverage (if $t/\tau \gg 1$). In particular, the deduced diffusion coefficient in our experiment at low temperatures appears to correspond to the

value at high coverages (~0.90ML) since only data during the initial decay period $t \ll \tau$ were collected, while at high temperatures it should correspond to a value at relatively low coverages (~0.7ML) since data with $t \gg \tau$ were measured.

Guided with this general argument and using the coverage dependent diffusion coefficients for diffusion along $[1\bar{1}0]$ from Chapter V, we have obtained the effective D as a function of reciprocal temperature and the results are shown in Fig. 6(a). It is seen that the diffusion activation energy deduced from such a set of data can appear lower than the real activation energy at full coverage. This is indeed the case for $E_{\text{diff}} [1\bar{1}0]$ observed in our SHG experiment, which is 1.1kcal/mol as compared to 2.0kcal/mol at full coverage. Therefore, the diffusion parameters E_{diff} and D_0 determined from the experiment are not quantitatively meaningful.

However, unlike the case of diffusion along $[1\bar{1}0]$, the activation energy for CO diffusion along $[001]$ deduced from the present set of data is still comparable to the value at full coverage (Chapter V), with the former being 3.1kcal/mol and the latter being 2.8kcal/mol. This can be understood if we notice that the measured SH signal $|\chi_{\text{eff}}^{(2)}(\theta)|^2 = |\chi_{\text{eff}}^{(2)}(0) + \Delta\chi_{\text{eff}}^{(2)}(\theta)|^2$ along $[001]$ direction is insensitive to CO coverage above 0.80ML (Fig. 7). Using a $\Delta\chi_{\text{eff}}^{(2)}(\theta)$ given by Eq. (14) below 0.8ML and by a constant above 0.80ML, simulation of CO diffusion with an initial square-wave coverage profile yields approximate diffusion coefficients at low temperatures corresponding to $\theta < 0.8\text{ML}$ (Fig. 6(b)). Because the SH diffraction is insensitive to diffusion of high coverages, the measured $E_{\text{diff}} [001]$ appears to be somewhat larger than the activation energy at full coverage.

In principle, we should be able to quantitatively simulate the SH diffraction results by the experimentally measured $D(\theta)$ from Chapter V. Unfortunately, we have not succeeded in doing so. A number of reasons could be responsible for it. First, the accuracy of $D(\theta)$ was not sufficient for such a quantitative simulation and the functional form of $D(\theta)$ given by Eq. (18) was only meant as an approximation. Second, the initial coverage of each grating prepared for SH diffraction experiment was not necessarily the same and their detail shapes could have affected the decay constants of SH diffraction differently at different temperatures. Third, by no means the form of $\chi_{\text{eff}}^{(2)}(\theta)$ used in the simulation was accurate enough. Fourth, and the most importantly, the present measurements were carried out on a different Ni(110) surface from those presented in Chapter V. With significantly stronger laser intensities used to create the adsorbate gratings in the present measurements, the Ni(110) surface could be disturbed to a higher degree. As we will see in Chapter V and VI, laser-induced defects may have significant effect on diffusion.

d) Effects of Surface Defect

Before we discuss the results of our surface diffusion measurements, we need to know whether they are intrinsic to the Ni(110) surface or dominated by defects on the surface. First, consider the effect of point defects. Their density is presumably around 10^{-3} to 10^{-4} of a full monolayer if it is properly annealed.¹¹ These defect sites are often first covered by adsorbates because of the stronger binding energy. In our experiment with an average coverage of $\theta_0 \sim 0.5$, the effect of such point defects may be negligible. The same argument can apply to

short line defects (ineffective in blocking diffusion paths) with lengths much shorter than the size of the grating. (However, I will present experimental evidence in Chapter VI that renders above statements).

Special attention has to be paid to line defects which run across the sample and are parallel to the adsorbate grating. They can be steps arising from a miscut of the sample. For diffusion perpendicular to the steps, we have to consider the durations that the adsorbate molecules spend on the terraces and in traversing the steps. Let the average trapping times of an adsorbate molecule on a terrace and at a step site be τ_T and τ_S , respectively. The total time for the molecule to diffuse across a terrace and a step is simply the sum

$$\tau_{\text{tot}} = \tau_T + \tau_S \quad (19)$$

If Na is the average width of a terrace, a the lattice constant and also the width of the steps, and N the average number of rows of atoms in a terrace, then from $\langle x^2 \rangle = 2Dt$, we have $(N+1)^2 a^2 = 2 D \tau_{\text{tot}}$. With D_T and D_S denoting the diffusion coefficients of adsorbates diffusing on a terrace and across a step, respectively, we also have $N^2 a^2 = 2 D_T \tau_T$ and $a^2 = 2 D_S \tau_S$. We then find

$$\frac{1}{D} = \frac{2\tau_{\text{tot}}}{(N+1)^2 a^2} = \frac{N^2}{(N+1)^2} \frac{1}{D_T} + \frac{1}{(N+1)^2} \frac{1}{D_S}, \quad (20)$$

For the steps to dominate in the surface diffusion, we must have $D_S \ll D_T/N^2$.

In our case, the Ni(110) surface had a 0.3° miscut along the [001] direction. This leads to an average terrace width of $N \sim 70$. If we assume that the trial frequencies (pre-exponential factors in D) for crossing a step and jumping over a barrier on a terrace are roughly the same, then $D_S \ll D_T/N^2$ leads to

$$\begin{aligned} \gamma &\equiv N^2 D_s / D_T \\ &= 70^2 \exp [(E_{\text{diff}}(\text{terrace}) - E_{\text{diff}}(\text{step}))/k_B T] \ll 1 \end{aligned} \quad (21)$$

where $E_{\text{diff}}(\text{terrace})$ and $E_{\text{diff}}(\text{step})$ are the diffusion activation energies on a terrace and across a step, respectively. If what we measured in our experiment were a step-dominated diffusion process ($\gamma \ll 1$) with $E_{\text{diff}}(\text{step}) = 3.1 \text{ kcal/mol}$ as obtained by fitting $D = D_0 \exp(-E_{\text{diff}}/k_B T)$ to the diffusion data along [001], then Eq.(21) dictates $E_{\text{diff}}(\text{terrace})$ should be smaller than $[E_{\text{diff}}(\text{step}) - 8.5kT]$, which at $T=150\text{K}$ is 0.56 kcal/mol . This small value of $E_{\text{diff}}(\text{terrace})$ is only twice as much as the thermal energy (0.3 kcal/mol) and would make the stable adsorption of CO on top and short-bridge sites of Ni(110) unlikely, contrary to the experimental observation. Therefore, we believe that the measured diffusion is intrinsic for CO on Ni(110) with $\gamma \gg 1$, and the effect of line defects is not significant. If we assume $\gamma=10$ we estimate from Eq. (21) that $E_{\text{diff}}(\text{step}) \sim 6 \text{ kcal/mol}$.

e) Diffusion Results

Despite the various systematical errors discussed above in the measurement, the diffusion results are very suggestive. First, under similar conditions for measurements along $[\bar{1}\bar{1}0]$ and [001], for which similar systematical errors must exist, the anisotropy of the surface diffusion of CO on Ni(110) has been beautifully shown. Two independent diffusion barriers, one along $[\bar{1}\bar{1}0]$ the other along [001], have been identified. To our best knowledge,

this is the first direct observation of anisotropic heterogeneous molecular diffusion with two independent channels.

The two diffusion activation energies along $[1\bar{1}0]$ and $[001]$ are clearly different, with the barrier along $[001]$ higher than that along $[1\bar{1}0]$. Qualitatively, this is understandable since the Ni atoms form closely packed rows along $[1\bar{1}0]$ and the resulting surface potential seen by a CO which is adsorbed on the Ni rows is then expected to be less corrugated. A theoretical calculation by Doyen and Ertl indeed predicted a surface potential variation of ~ 1.25 kcal/mol along $[1\bar{1}0]$ and ~ 2.25 kcal/mol along the $[001]$ direction¹². The experimental observation of streak-like $c(4 \times 2)$ and $c(8 \times 2)$ LEED patterns by Behm *et al*, which was interpreted as a consequence of CO occupation at intermediate positions other than the high symmetry sites (on-top and short-bridge sites) along $[1\bar{1}0]$ direction, further indicated that the potential corrugation along $[1\bar{1}0]$ is smoother than that along $[001]$ ¹³.

The deduced diffusion preexponential factors along the two directions are also anisotropic, however, the systematical errors may have contributed to it to some larger extent than to the diffusion activation energy. Therefore, any quantitative discussion on them is not very meaningful. The detail discussion of the implication of CO surface diffusion on Ni(110) should be postponed until better quality data are available (see Chapter V).

In comparison with adatom diffusion of metal atoms on the (110) plane of fcc crystals such as Ni/Ni(110), Pt/Pt(110), Ir/Pt(110), Ir/Ir(110) and W/Ir(110), in which two distinct channels with adatoms hopping along the atomic rows of the substrate or exchanging with substrate atoms (concerted motion) to go across the rows³, we can conclude that the diffusion paths for CO/Ni(110) are as follows: along the $[1\bar{1}0]$ direction, a CO molecule hops successively from a

short-bridge (or on-top) site to a neighboring on-top (or short-bridge) site, then to a neighboring short-bridge (on-top) site, and so on; along the [001] direction, CO hops either from a short bridge site through a hollow site to another short-bridge site and so on or from a on-top site through a long-bridge site to another on-top site and so on (see Fig. 1).

F. Conclusion

The new technique using SH diffraction from a monolayer grating to measure surface diffusion is applicable to measure surface diffusion for all surfaces and is ideal for studying diffusion on crystalline surfaces with strong anisotropy. The anisotropic surface diffusion of CO/Ni(110) is used here as a demonstration. The results indicate unequivocally the existence of two independent diffusion channels along [001] and $[1\bar{1}0]$ with strong anisotropy. The smaller activation energy for diffusion along $[1\bar{1}0]$ is directly associated with the close-packed rows of Ni atoms along $[1\bar{1}0]$. The various effects that may influence the data analysis have been discussed.

As seen from the work described here, the monolayer grating technique has clearly the advantage of involving a simple and straightforward data analysis in the case with the optical field response linear to coverage and the diffusion coefficient independent of coverage. This eliminates the need of developing a theory just for the data analysis as with some other techniques. However, the present method using SH diffraction to probe the monolayer grating often suffers from a poor signal-to-noise ratio. This makes the study of , for example, coverage dependence of surface diffusion difficult. It is possible to greatly enhance the sensitivity by using linear optical diffraction instead to probe the monolayer grating. The coverage dependence of surface diffusion of

CO/Ni(110) which we have neglected in the present work can then be measured. This is the topic of next chapter.

References

- ¹ An excellent review of the field has been provided recently by R. Gomer, *Rep. Prog. Phys.* **53**, 917(1990).
- ² A. G. Naumovets and Yu.S. Vedula, *Surf. Sci. Reports* **4**, 365(1985).
- ³ G. Ehlich and Kaj Stolt, *Ann. Rev. Phys. Chem.* **31**, 603(1980).
- ⁴ Xu-dong Xiao, X. D. Zhu, W. Daum and Y. R. Shen, *Phys. Rev. Lett.* **66**, 2352(1991).
- ⁵ J. Bauhofer, M. Hock and J. Koppers, *Surf. Sci.* **191**, 395(1987).
- ⁶ D. J. Hannaman and M.A. Passler, *Surf. Sci.* **203**, 449(1988); S. Haq, J.G. Love and D.A. King, *Surf. Sci.* **275**, 170(1992); B. Voigtlander, S. Lehwald and H. Ibach, *Surf. Sci.* **225**, 151(1990).
- ⁷ X. D. Zhu, Winfried Daum, Xu-dong Xiao, R. Chin and Y. R. Shen, *Phys. Rev. B* **43**, 11571(1991).
- ⁸ X. D. Zhu, and Y. R. Shen, *Opt. Lett.* **14**, 503(1989).
- ⁹ J. C. Hamilton, R. J. M. Anderson, and L. R. Williams, *J. Vac. Sci. Technol. B* **7**, 1203(1989).
- ¹⁰ X.D. Zhu, Ph.D. thesis, Berkeley, unpublished.
- ¹¹ J. E. Reutt-Robey, D. J. Doren, Y. J. Chabal, and S. B. Christman, *Phys. Rev. Lett.* **61**, 2778(1988).
- ¹² G. Doyen and G. Ertl, *Surf. Sci.* **43**, 197(1974).
- ¹³ R. J. Behm, G. Ertl, and V. Penka, *Surf. Sci.* **160**, 387(1985).

Figure Captions

Figure 1: Ni(110) surface with (a) c(4x2) and (b) p2gm 2x1 CO superstructures on it. The sizes of Ni atoms and CO molecules are not shown in proportion.

Figure 2: Normalized first-order SH diffraction signal versus time at different temperatures for CO diffusion along (a) $[1\bar{1}0]$, (b) $[001]$ and (c) the direction bisecting $[1\bar{1}0]$ and $[001]$ on the Ni(110) surface. The solid lines are the exponential fits with Eq.(9).

Figure 3: Diffusion coefficient D versus reciprocal temperature $1/T$ in an Arrhenius plot for CO diffusion on Ni(110) along $[1\bar{1}0]$, $[001]$, and the direction bisecting the two ($\phi = 45^\circ$). The solid lines are least square fits by Eq.(10) and Eq. (11) with $E_{\text{diff}}[1\bar{1}0] = 1.1$ kcal/mol, $D_0[1\bar{1}0] = 3.8 \times 10^{-9}$ cm²/sec, and $E_{\text{diff}}[001] = 3.1$ kcal/mol, $D_0[001] = 4.8 \times 10^{-6}$ cm²/sec.

Figure 4: Diffusion coefficient D for CO/Ni(110) as a function of azimuthal angle ϕ away from $[1\bar{1}0]$ at $T \sim 110$ K. The solid line is calculated from Eq.(3) using the diffusion parameters deduced from Fig.3.

Figure 5: (a) Coverage profile evolutions simulated with a coverage dependent diffusion coefficient given by Eq.(18) with $d=2.5$. The labeled time are in unit of $\tau = s^2/8\pi^2 D(0)$, with $D(0)$ defined in Eq. (18). (b) The simulated SH diffraction signal decay with $D(\theta)$ given by Eq. (18) and $\Delta\chi_{\text{eff}}^{(2)}(\theta)$ given by Eq. (14). The exponential decay curve $\exp(-t/\tau)$ is shown for comparison.

Figure 6: (a) Simulated diffusion coefficient as a function of reciprocal temperature along $[1\bar{1}0]$. The two lines are from the results that will be presented in Chapter V. Starting from the low temperature end, the first point is resulted from fit to the simulated SH diffraction signal from $t=0$ to the time with 80% of the initial signal left ($d=5$), the second point to 50% ($d=4$), the third point to 40% ($d=3$), the fourth point to 20% ($d=2.5$), the fifth point to 1% ($d=1.5$). (b) Same as (a) for D along $[001]$ direction with the first point fit to 85%, second point to 60%, third point to 40%, fourth point to 20%, and the fifth point to 1%.

Figure 7: Reflection SH signal $|x_{\text{eff}}^{(2)}(\theta)|^2$ as a function of CO coverage for a polarization combination $p(\text{in})/p(\text{out})$ with (a) the plane of incidence parallel to $[1\bar{1}0]$, (b) the plane of incidence parallel to $[001]$.

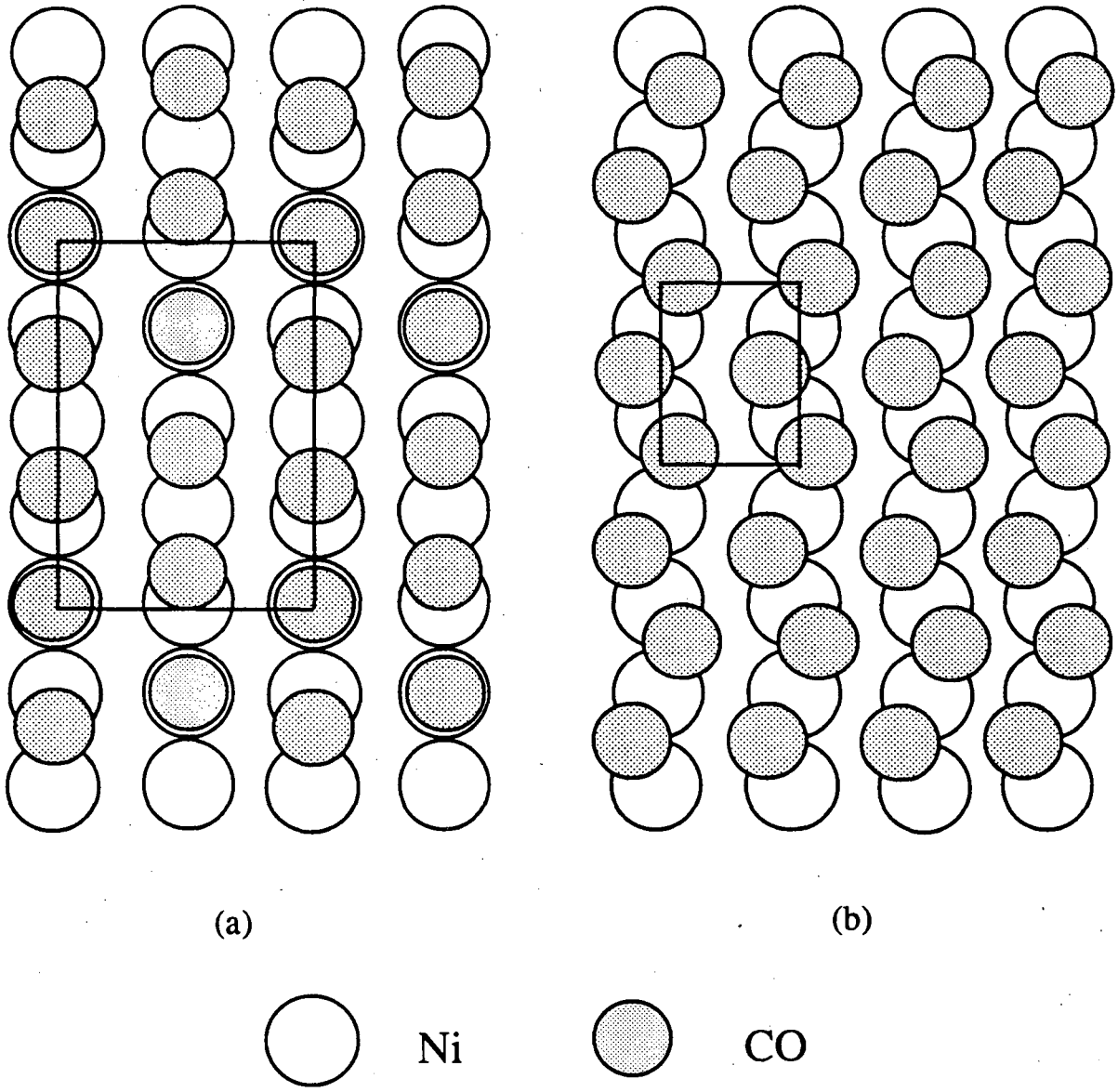


Figure 1

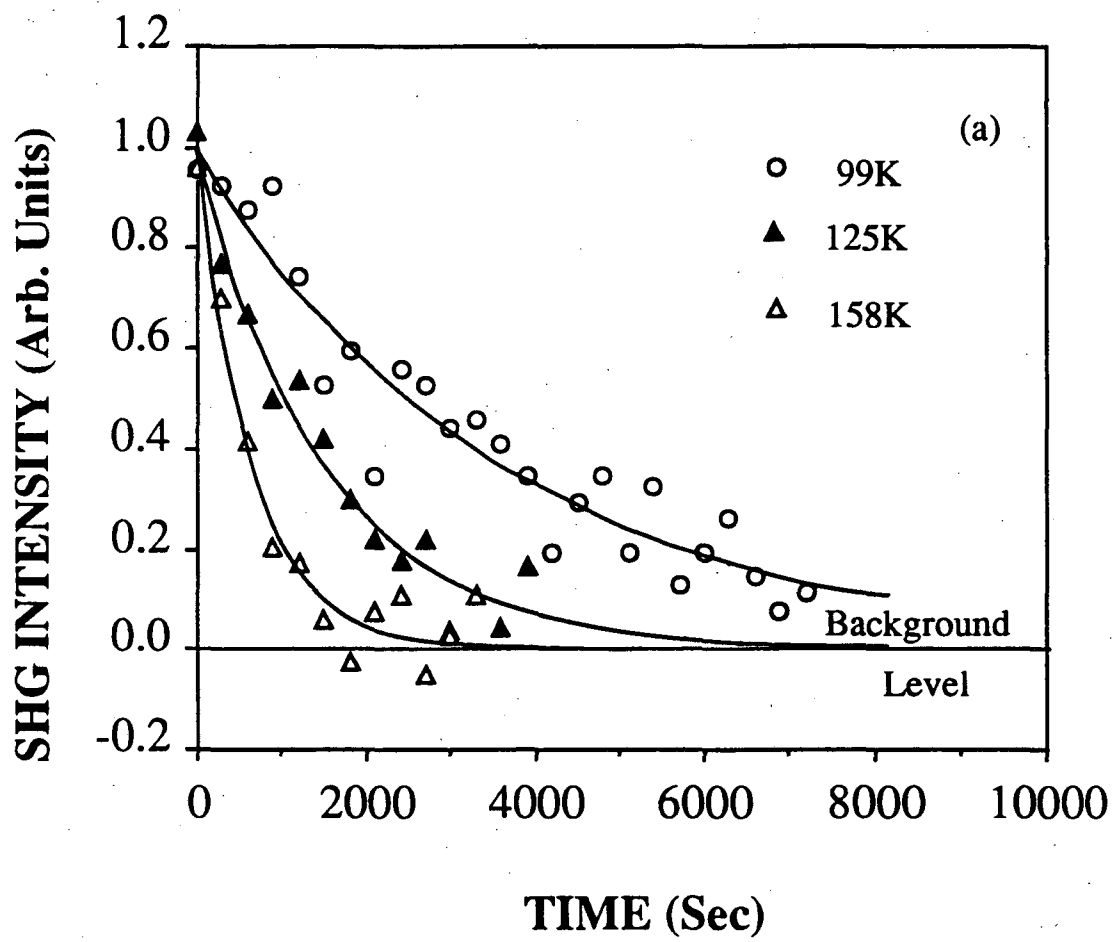


Figure 2(a)

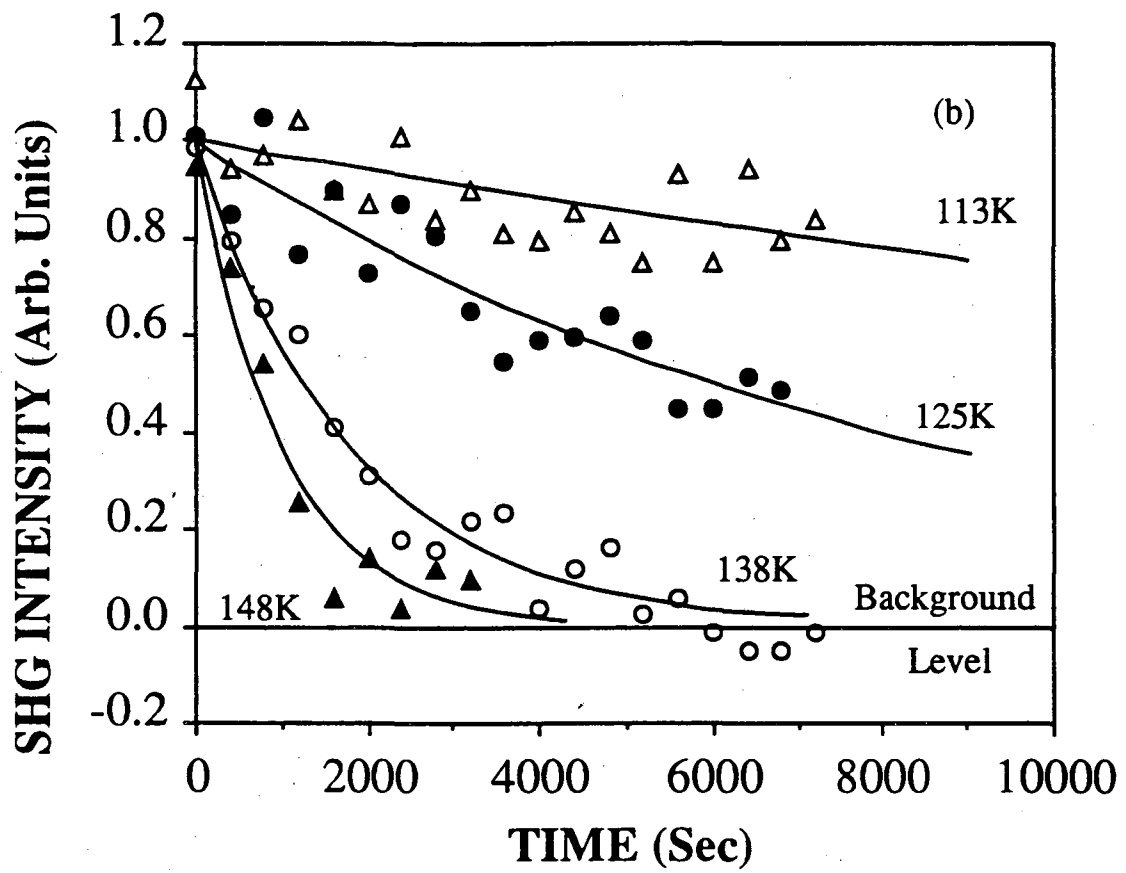


Figure 2(b)

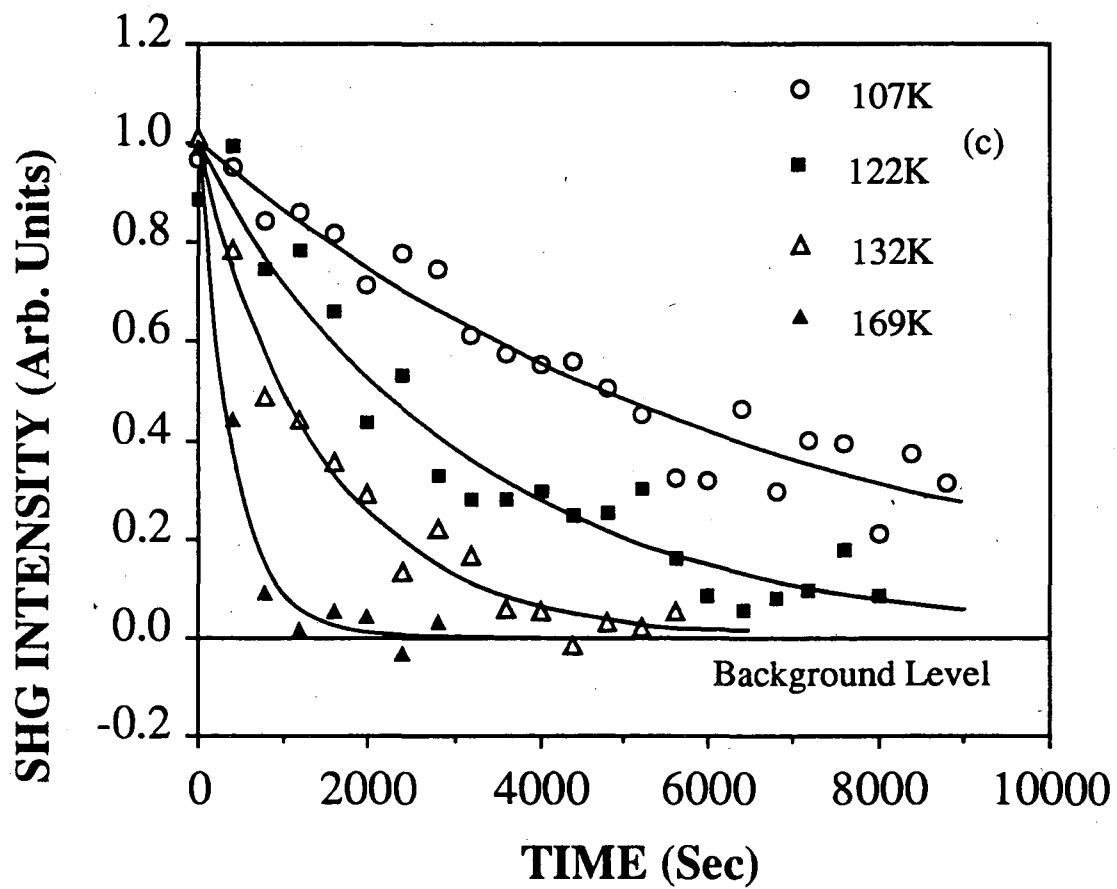


Figure 2(c)

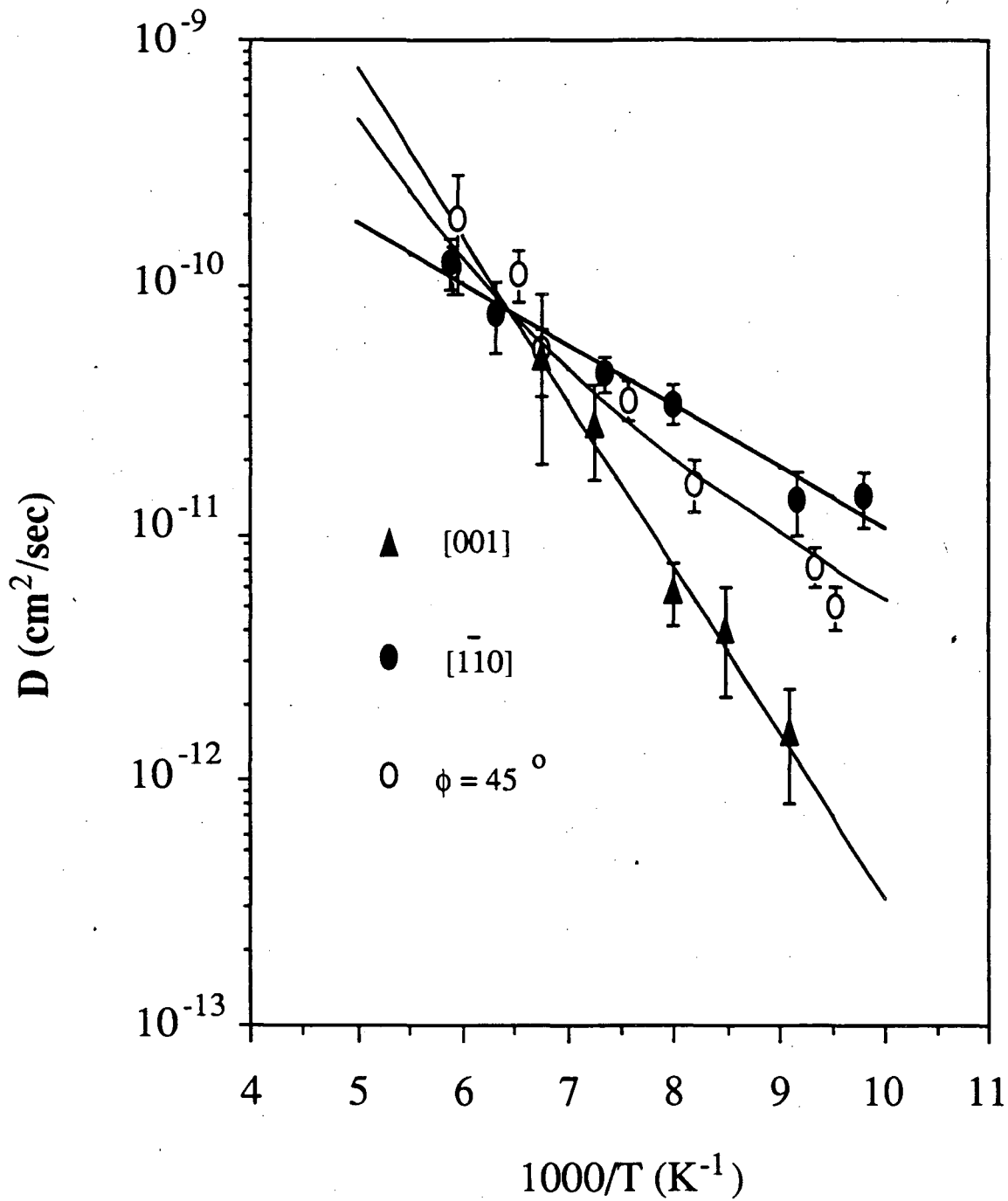


Figure 3

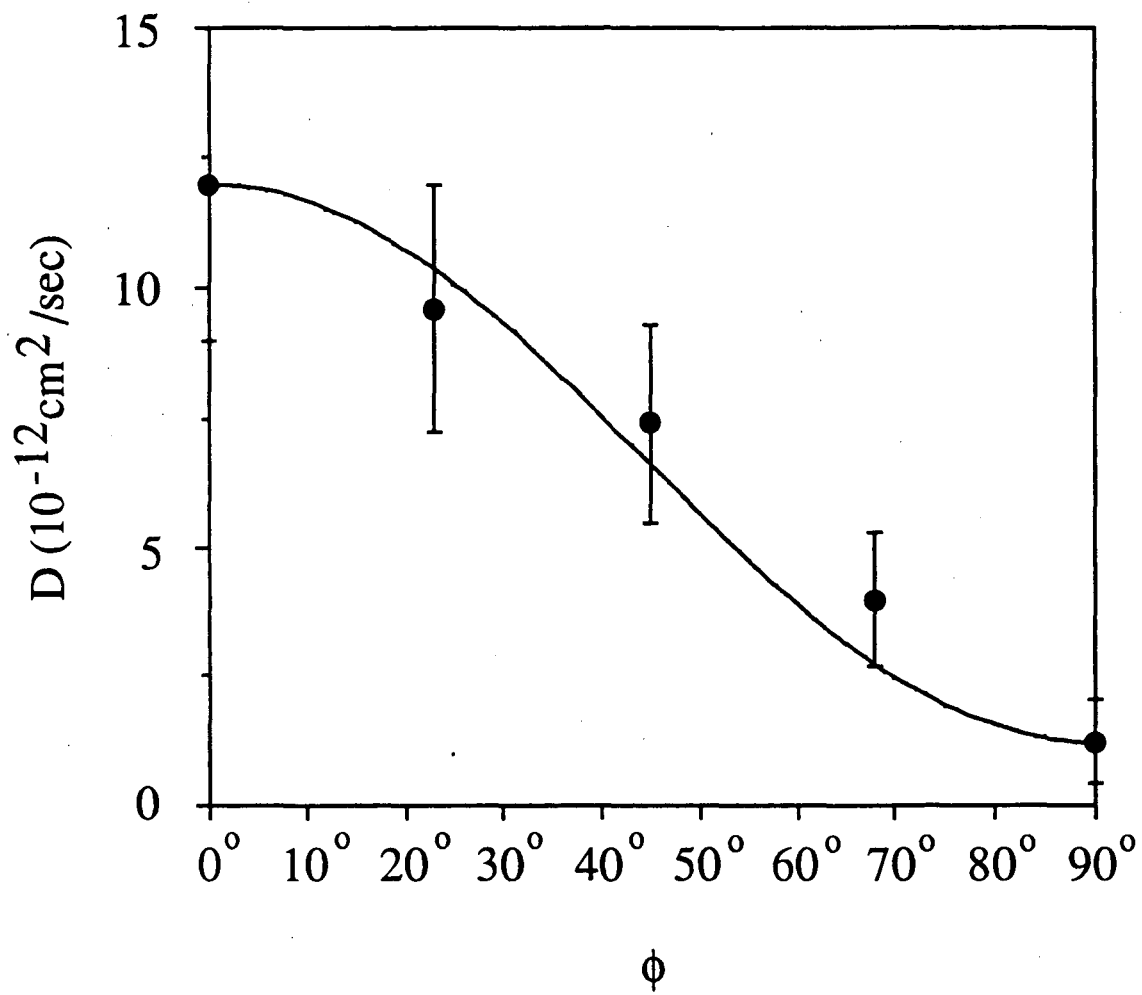


Figure 4

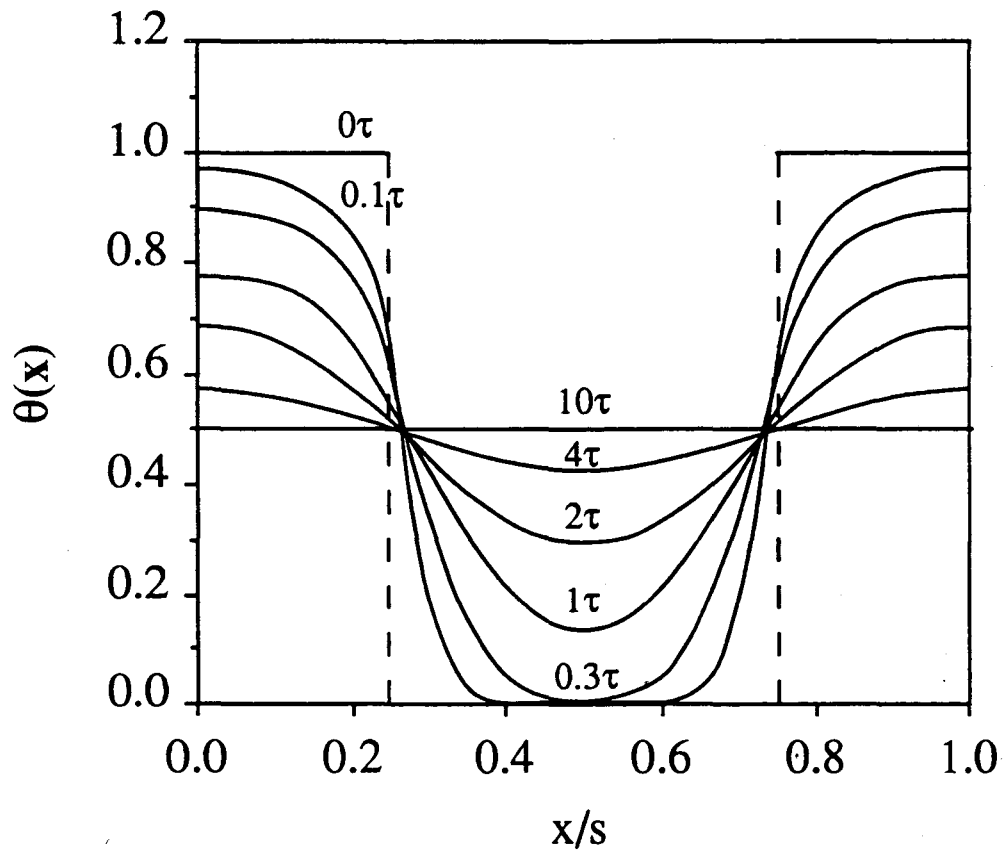


Figure 5(a)

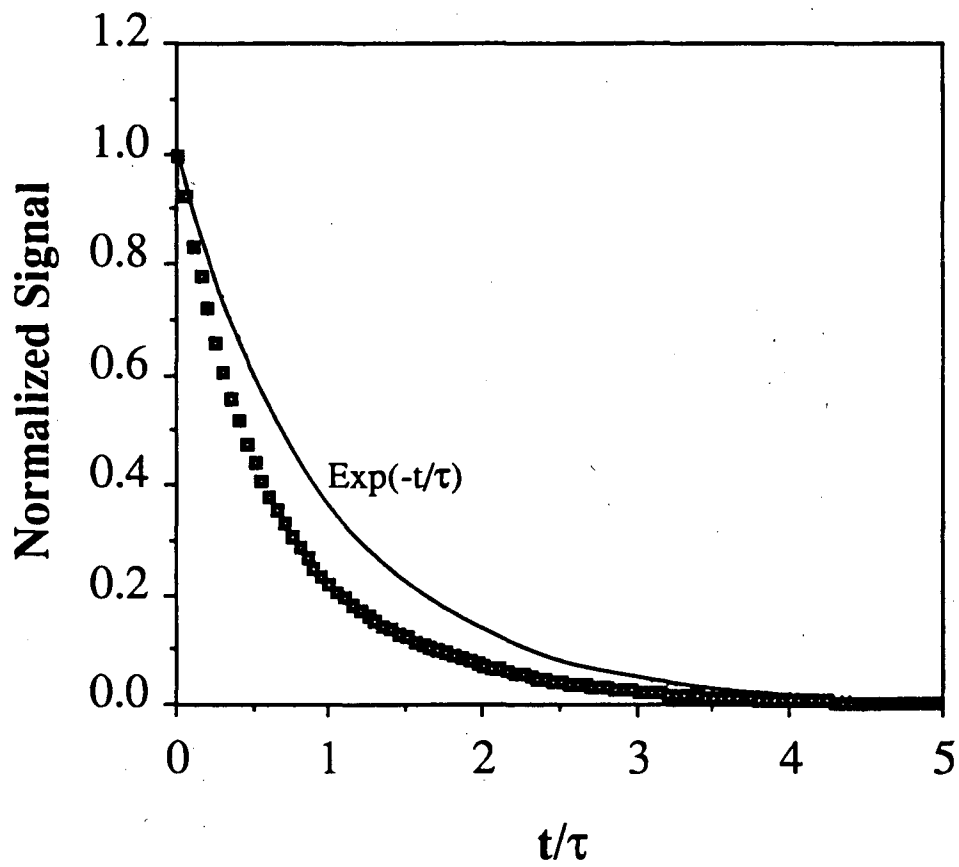


Figure 5(b)

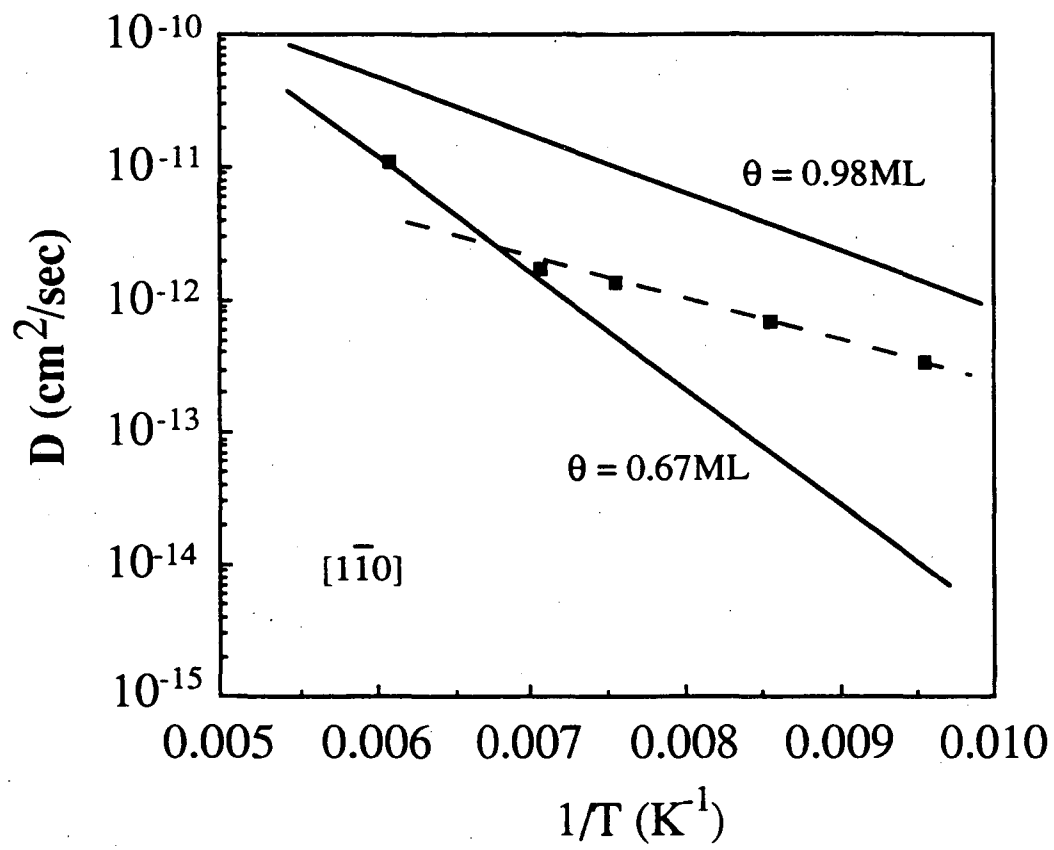


Figure 6(a)

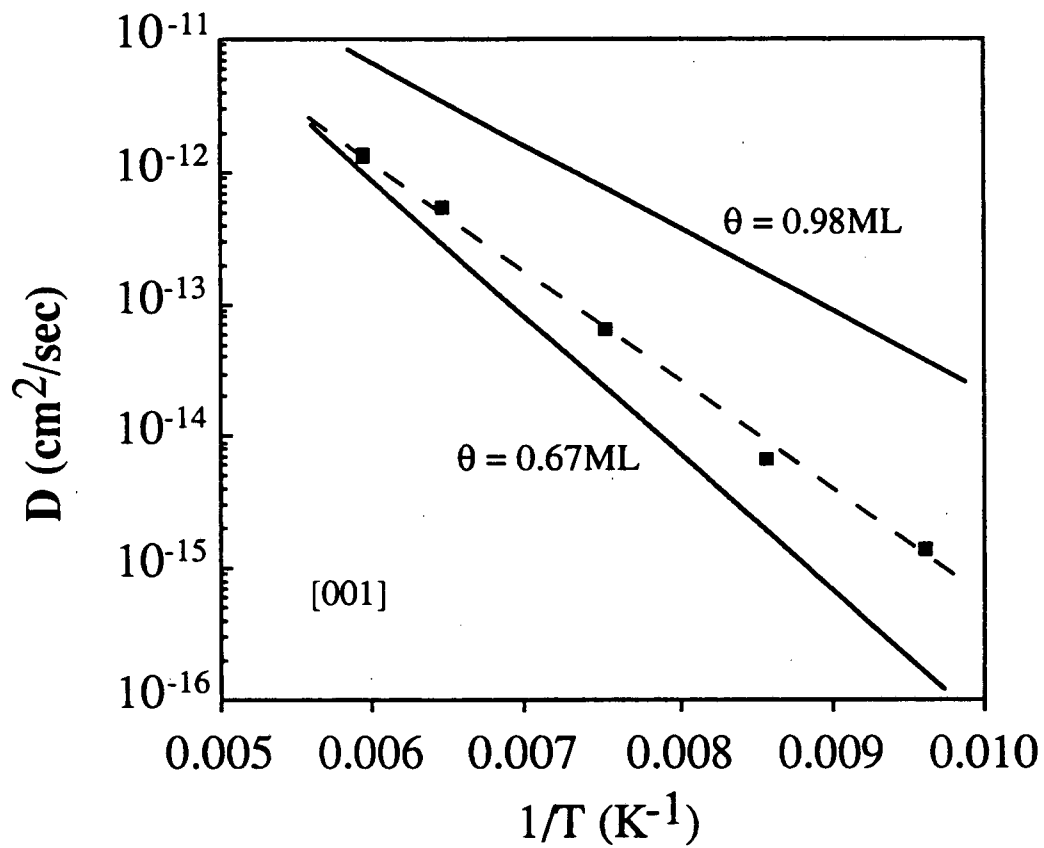


Figure 6(b)

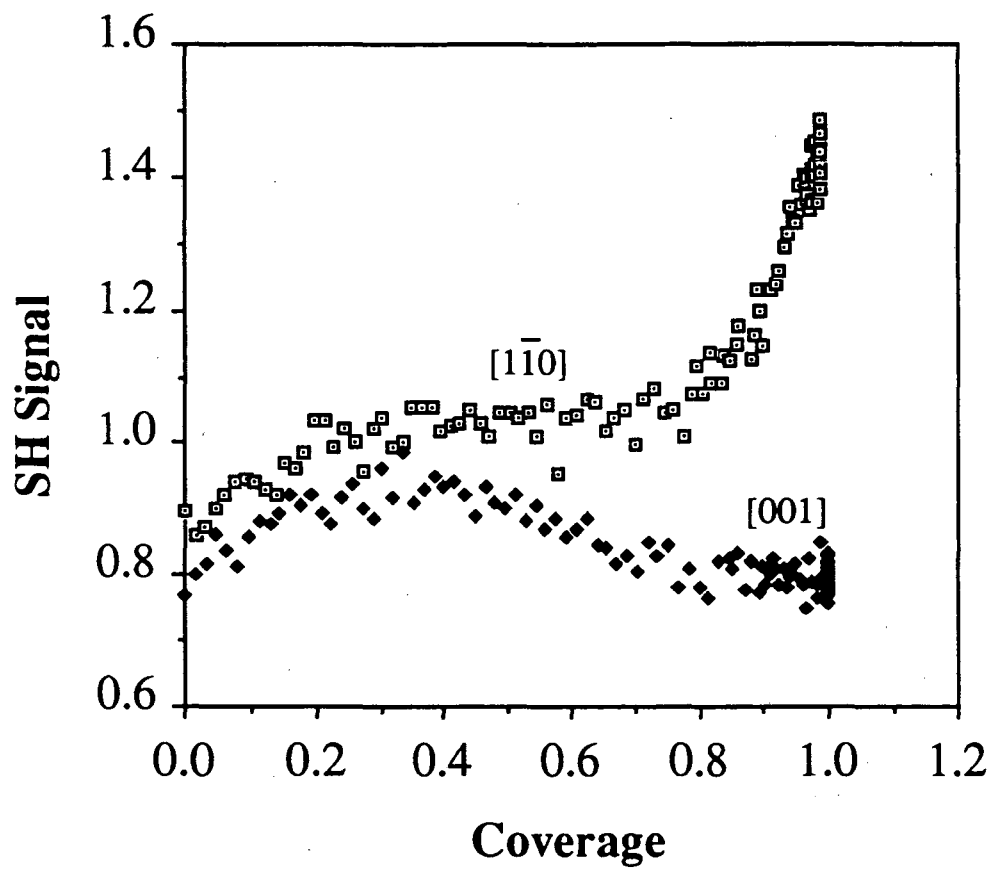


Figure 7

V. Surface Diffusion with Adsorbate-Adsorbate Interaction: CO/Ni(110)

A. Introduction

Surface diffusion is of great importance to many processes in surface science and have received increasing attention in the past decade¹. For example, a full understanding chemical reactions on surfaces, surface catalysis and crystal growth, all require detailed information about surface diffusion. Tracer surface diffusion which concerns with a single adparticle motion can provide valuable knowledge about adsorbate-substrate interaction. However, it can not account for the more complicated diffusion processes, in which a large number of adsorbed atoms or molecules are involved. The latter case, known as chemical surface diffusion, connects more closely with the real surface problems. The adsorbate-adsorbate interactions can significantly affect chemical diffusion and need to be carefully investigated².

Theoretical studies on chemical diffusion with different adsorbate-adsorbate interactions have been reported in the literature^{2,3}. In these studies, the adsorbate-adsorbate interactions are treated in the framework of the lattice gas model, and often only nearest-neighbor and the next nearest neighbor interactions are included. Interactions of an adsorbate at the saddle point (activated complex) with its surrounding adsorbates are sometimes considered as well. However, the origin of the adsorbate-adsorbate interactions has been seldom discussed and the difference of their effect on molecules at adsorption sites and at saddle points has never been systematically examined. Intuitively, the induced potential change by a long range adsorbate-adsorbate interaction

such as dipole-dipole interaction on an adsorption site and a saddle point may only have slight difference and therefore will not alter the diffusion barrier height much. In strong contrast to this, a short range adsorbate-adsorbate interaction can affect the potential at the adsorption site and the saddle point by significantly different amount and consequently alter the barrier height of diffusion. Experimentally, no direct confirmation of this assertion has been made yet.

In this chapter we will present a coverage dependent study for anisotropic surface diffusion of CO on Ni(110) using a newly developed technique, namely, the polarization-modulated linear optical diffraction off a monolayer adsorbate grating⁴. The CO/Ni(110) system is interesting because the short range adsorbate-adsorbate interaction occurs only at high coverages⁵. Therefore, the effects of different types of adsorbate-adsorbate interactions on surface diffusion can be studied by varying the CO coverage. Moreover, the Ni(110) surface is anisotropic and one may wonder if an anisotropy in the coverage dependence of surface diffusion also exists. Our results have unambiguously shown that the diffusion activation energies are influenced by the CO-CO short-range interaction but not by the long-range dipole-dipole and CO-Ni-CO interactions. The anisotropy of the adsorbate-substrate interaction affecting surface diffusion is present, but the short-range CO-CO interaction does not seem to have appreciable effect on the anisotropy of surface diffusion.

B. Experimental Details

The experiment was performed in an ultrahigh vacuum (UHV) chamber

with a base pressure of 2.0×10^{-10} torr. The single crystal Ni(110) sample was cut and mechanically polished to within 0.2° from the (110) plane, and mounted vertically on a rotatable sample holder capable of more than 90° of rotation about [110]. Before any measurement, the sample was treated by many sputtering and annealing cycles for few days to reduce impurities such as S, O, and C in the bulk. A normal cleaning procedure was adopted subsequently to clean the sample surface: it was first Ar^+ sputtered at 1.0×10^{-4} torr Ar pressure with a 500V beam voltage for approximately 30 minutes at room temperature and then annealed at 1120K for 10 min followed by slow cooling at a rate of $\sim 0.5\text{K/sec}$ to 820K and a rate of $\sim 2\text{K/sec}$ to room temperature. Auger spectra showed no detectable surface impurities ($< 0.3\%$ S, O and C) after this procedure. A sharp 1×1 LEED pattern from a clean Ni(110) surface and a clear 2×1 LEED pattern from a full CO monolayer on Ni(110) could be observed. They ensured that the surface was well ordered. Liquid nitrogen cooling and electron beam heating were used in the experiment to control the sample temperature. A Chromel-Alumel thermal couple welded to the sample was used to monitor the sample temperature. The temperature could be controlled to within $\pm 1\text{K}$.

The diffusion experiment was conducted in the temperature ranges of 140K to 220K for the $[1\bar{1}0]$ direction and 180K to 240K for the [001] direction for coverages up to 0.8ML. For higher coverages in the [001] direction somewhat lower temperatures were chosen in order to avoid possible CO adlayer phase transitions⁶. Immediately before each measurement, the sample was flash-heated to 600K to remove residual adsorbed molecules from the ambient, mostly hydrogen and CO, or previously adsorbed CO monolayer. The adsorption of CO on the Ni(110) surface was carried out at approximately 180K by introducing CO into the chamber through a leak valve. The CO coverage on

Ni(110) at this temperature was calibrated by thermal desorption spectroscopy (TDS). The accuracy in determining the CO coverage was about 0.03ML. We used a polarization-modulated linear optical diffraction technique which has been described in Ref. [4] and Chapter III to measure CO diffusion. The CO adsorbate grating was created by laser-induced thermal desorption with two interfering pulsed laser beams from a single-mode Q-switched Nd:YAG laser (pulse width of 10ns at 1.06 μ m)⁷. The grating period was $s \sim 3\mu$ m. The depth of the adsorbate grating was controlled by adjusting the beam intensities properly. We chose to have a coverage modulation of ~ 0.03 ML on top of an average coverage varying from 0.07ML to 0.97ML. With such a small coverage modulation, the diffusion coefficient can be very well approximated by a coverage independent constant and the coverage dependence of the diffusion should only come from the average coverage. To probe the adsorbate grating by linear optical diffraction, a 5-mW He-Ne laser was used. The probe beam was polarization-modulated, which was achieved by passing the beam through a photoelastic modulator. First-order diffraction from the grating was selected by an aperture and detected by a lock-in amplifier. The starting signal-to-noise ratio was on the order of 10.

The detail derivation of the relation between the diffraction signal and the diffusion coefficient is referred to Ref. [4] and Chapter III. Here, we only mention that upon diffusion the first order diffraction signal decays exponentially with time and is given by

$$S_1 = S_{01} \exp(-8\pi^2 D t / s^2), \quad (1)$$

where the exponent is directly proportional to the diffusion coefficient D. In determining D, only the decay time constant and the grating spacing s need to

be known accurately. The detail shape of the grating is of no consequence. To deduce the diffusion activation energy and the preexponential factor from D following the Arrhenius law, measurements at five temperatures or more were made for each coverage. Surface diffusion along different directions were measured by setting the adsorbate grating in the appropriate directions.

C. Results and Discussion

a) Measurement Accuracy

Representative diffraction decay curves are shown in Fig. 1(a) and (b) for average coverage $\theta=0.98$ for diffusion along $[1\bar{1}0]$ and $[001]$ directions, respectively. The decay time constant deduced from such curves can be usually determined to within $\pm 15\%$, however, the accuracy of determining the diffusion coefficients in our experiment is rendered to $\pm 50\%$ by the irreproducibility of the measurements. Two sources for this irreproducibility could exist, one being the intrinsic property to the sample, the other being the laser effect of the desorbing laser beams.

Experimentally, we have explicitly showed the existence of the laser effect by shining a second laser pulse (single beam) onto an adsorbate grating at certain time after its creation. Some typical data are shown in Fig. 2 for initial CO coverage $\theta=0.5\text{ML}$ at $T=210\text{K}$. The decay time constants of the diffraction signal before and after this laser pulse are all indicated along the curves. The accuracy of the deduced time constants is $\sim \pm 5\%$. It is clear that the decay time constant has been altered by this second laser pulse and becomes longer or shorter in a random fashion. Since the coverage effect has been properly

avoided by working with initial coverage $\theta=0.5$, where $D(\theta)$ is coverage independent (see subsection b)), the change in the decay time constant should solely come from the laser effect on the substrate surface. The background level change induced by the second laser pulse in curve (a) and (c) further indicated the existence of such effects. However, the nature of this laser effect is not apparent. If the laser pulse only causes surface damage the decay time constant should change in only one direction. Only if the laser can also anneal the surface, the decay time constant can change randomly in both directions.

The above experiment cannot rule out the possibility that the observed irreproducibility could be an intrinsic property of the surface. Methods that do not perturb a surface between diffusion measurements should be applied to address this issue. The Fluctuation-correlation field emission microscopy(FEM) method, which has an accuracy of $\pm 15\%$ to deduced diffusion coefficient from a single run, seems to be ideal for this purpose. The fact that even with FEM an irreproducibility of ~ 2 has been observed indicates that the irreproducibility could be the intrinsic nature of metal surfaces⁸.

b) Coverage Dependent Diffusion Results

Diffusion coefficients versus reciprocal temperature $1/T$ for coverage $\theta=0.98$ and 0.48 in both $[1\bar{1}0]$ and $[001]$ directions are plotted in Fig. 3 as examples. The solid lines are best fits by the Arrhenius law,

$$D = D_0 \exp\left(-\frac{E_{\text{diff}}}{k_B T}\right), \quad (2)$$

with D_0 as the preexponential factor, E_{diff} as the diffusion activation energy, and k_B as the Boltzmann constant. The deduced diffusion activation energies and the preexponential factors for CO diffusion on Ni(110) surface both along $[1\bar{1}0]$ and $[001]$ directions are shown in Fig.4 (a) and (b). In Fig. 5 the diffusion coefficients as a function of coverage are depicted for three temperatures for CO diffusion in $[001]$ direction.

The coverage dependence of diffusion are similar in both directions as shown by Fig. 4. The diffusion activation energies are almost constants up to a coverage of 0.7ML and then drop by ~ 2 kcal/mol at full coverage. The preexponential factors follow similar trends. The anisotropy of diffusion can be seen from both Fig. 3 and Fig. 4. The activation energies in the low coverage regime are 4.7kcal/mol along $[001]$ and 4.0kcal/mol along $[1\bar{1}0]$. The preexponential factors have a difference around a factor of 3, with the one along $[1\bar{1}0]$ larger. In the high coverage range the diffusion activation energies in both directions drop by about the same amount to reduce the activation energy in the $[001]$ direction to 2.8kcal/mol and in the $[1\bar{1}0]$ direction to 2.0kcal/mol. This result indicates that the adsorbate-adsorbate interaction has little effect on the anisotropy of the diffusion activation energy.

c) Discussion on Coverage Dependence

Adsorption sites of CO on Ni(110) have been studied with dynamical LEED⁹, electron energy loss spectroscopy (EELS)¹⁰ and reflection-adsorption

infrared spectroscopy (RAIRS)¹¹. Below 0.7ML(theoretically, it should be 0.67ML), CO adsorbs on both short-bridge and top sites along the Ni atomic rows with a coverage independent occupation ratio^{11,12}. The separation between the CO molecules is at least 3.74Å in the $[1\bar{1}0]$ direction. Certain superstructures such as $c(8 \times 2)$, $c(4 \times 2)$ have been observed by some authors^{6,9,13} and these structures indicate that the site registry is not ideal¹³. Above this coverage the CO molecules are pushed to short-bridge sites^{9,13} (EELS results prefer top sites¹⁰) and tilt in the $[001]$ and $[00\bar{1}]$ directions with a tilt angle of 19° with respect to the surface normal^{5,6}. At the full coverage a $p2mg(2 \times 1)$ structure is formed^{5,6}. The adsorbate-adsorbate interactions have been investigated by TDS¹⁴, EELS¹⁰, angular resolved photoemission spectroscopy (ARUPS)¹⁵ and other techniques. While ARUPS concerns more about the electronic states, TDS and EELS do provide binding energy information. It has been found by TDS that an α_2 desorption state with a low desorption energy appears at coverage above 0.7ML, with some dispute in the exact uptake coverage^{13,14,16}. The coverage dependent desorption energy¹⁴ is depicted in Fig. 4(a) along with the diffusion activation energies. The correlation between them is excellent; both the diffusion activation energies and the desorption energy show a decrease above coverage 0.7ML. The drop in the desorption energy is about 4kcal/mol and in the diffusion activation energies is about 2kcal/mol. Up to this point, we can conclude that the long range dipole-dipole interaction and CO-Ni-CO indirect interaction, which are present at all coverages, do not influence the diffusion activation energy and the desorption energy. This is because first they are of long range. The potential at the saddle points may have been affected by the same amount as that at the adsorption site. Second, the dipole-dipole interaction is repulsive and the CO-Ni-CO interaction is attractive¹⁷. Their effects on the surface potential may get

canceled to certain extent. Above 0.7ML coverage, since the CO molecule has a diameter of 2.8\AA ⁶, and the Ni atom has a diameter of 2.49\AA , the CO-CO molecules start to have significant orbital overlapping in the $[1\bar{1}0]$ direction (The nearest-neighbor CO's in the $[001]$ direction do not have this interaction because the distance between two Ni rows is 3.52\AA , larger than the diameter of CO molecules. The displacement of the CO molecules makes the situation somewhat more complicated but will not change this result, see Fig. 6). The orbital overlapping is significantly reduced once a CO molecule jumps to a saddle point, which is at least $\sim 3.10\text{\AA}$ in the $[1\bar{1}0]$ direction and $\sim 2.72\text{\AA}$ in the $[001]$ direction away from the nearest-neighbor CO molecules⁹. Because of this repulsive CO-CO interaction, a net reduction of diffusion activation energy can result. The same reason should be responsible for the drop in the desorption energy.

d) Comparison with Other Nickel Surfaces

A comparison with CO diffusion on the other two low Miller index planes of nickel, namely Ni(111) and (100), is worthwhile. CO diffusion on Ni(111) has been studied in detail by FEM method and no coverage dependence for the activation energy (6.8kcal/mol) has been found¹⁸. Even at the saturation coverage of 0.57ML for a $(\sqrt{7}/2 \times \sqrt{7}/2)R19.1^0$ superstructure¹⁹ for CO/Ni(111), the shortest distance between CO-CO is about 3.30\AA , which is still much larger than the CO diameter. Therefore, no CO-CO direct interaction is expected on this surface. The diffusion results of CO/Ni(111) then confirm our findings from CO/Ni(110) that the long range interactions do not affect the diffusion activation energy. However, this agreement is contrasted by a strong coverage dependent desorption energy of CO/Ni(111), which is 30kcal/mol up to 0.35ML

and drops monotonically to 14.5kcal/mol to the saturation coverage²⁰. The difference in the coverage dependences between the desorption energy and the diffusion activation energy can only be explained by assuming that the long range interactions affect them in different ways. The situation for CO/Ni(100) is different. CO diffusion has been measured for only a few coverages by the LID method²¹ and a coverage dependent activation energy has been found with $E_{diff}=6.4\text{kcal/mol}$ at $\theta=0.25\text{ML}$, and $E_{diff}=4.6\text{kcal/mol}$ at $\theta=0.4$ and 0.64ML (saturation coverage). While it is clear that the CO-CO overlapping interaction is not responsible for this drop since the CO-CO separation at saturation is at least 5.0\AA ²², the coverage dependence has been interpreted as due to the CO superstructures $c(2\times 2)$ and $c(2\sqrt{2}\times 2)R45^\circ$ at the two high coverages²¹. No reliable desorption energy data exists for this system. However, qualitatively, the desorption energy has been estimated to also have a coverage dependence, namely 26kcal/mol at low coverage and 10kcal/mol at high coverage²³.

From the data discussed above, we obtain the ratios of diffusion-activation-energy/desorption-activation-energy as: ≥ 0.23 for CO/Ni(111), ≥ 0.24 for CO/Ni(100), and ≤ 0.15 for CO/Ni(110). From these ratios and the absolute diffusion activation energies, Ni(110) is seen to be the smoothest for CO diffusion. The fundamental reason for this may have to do with the relaxation of the clean Ni surfaces. It has been found that the first atomic layers of these three surfaces contract by different amount: about 1% for Ni(111)²⁴ and Ni(100)²⁵, and 9% for Ni(110)²⁶. The significantly large contraction in Ni(110) can result into a much smoother electronic charge density and thus a smoother surface potential corrugation²⁷.

e) Discussion on Anisotropic Activation Energy

Diffusion activation energies along $[1\bar{1}0]$ and $[001]$ directions of Ni(110) are expected to be different. Due to the relatively smooth electronic charge density along $[1\bar{1}0]$ direction, the potential seen by a CO molecule along that direction should be less corrugated than that along $[001]$ direction. A theoretical calculation by Doyen and Ertl indeed predicted a surface potential variation of ~ 1.25 kcal/mol along $[1\bar{1}0]$ and ~ 2.25 kcal/mol along the $[001]$ direction²⁸. The experimental observation of streak-like $c(4 \times 2)$ and $c(8 \times 2)$ LEED patterns by Behm *et al*, which was interpreted as a consequence of CO occupation at intermediate positions other than the high symmetry sites (on-top and short-bridge sites) along the $[1\bar{1}0]$ direction, further indicated that the potential corrugation along $[1\bar{1}0]$ is smoother than that along $[001]$ ¹³. The measured diffusion activation energies of CO on Ni(110) for all coverages unequivocally showed this predicted anisotropy. However, our observed $\sim 20\%$ anisotropy of the CO-Ni interaction appearing in the diffusion activation energies is somewhat insignificant. This weak anisotropy is in good agreement with the EELS measurement¹⁰, in which the vibrational frequencies of the two CO frustrated translational modes (corresponding to the two diffusion coordinates here) also showed very little anisotropy. In the case of adatom diffusion of Ni/Ni(110), the anisotropy of diffusion activation energies measured by FIM is $\sim 40\%$, again a relatively small value.

We can further seek for a quantitative agreement between the diffusion results and the EELS results. The CO frustrated vibrational frequencies spectra of a full CO monolayer can be estimated from the measured diffusion activation energies with a simple chain model. Considering the force on CO at a Ni site

to be $-M\omega_0^2 x$ and the force from a nearest CO to be proportional to the difference of their displacements, the equation of motion for the s-th CO molecule is then

$$M \frac{d^2 x_s}{dt^2} = -M\omega_0^2 x_s - C(x_{s+1} + x_{s-1} - 2x_s), \quad (3)$$

where x_s is the displacement of the s-th CO molecules, M the mass of CO molecule, and C the force constant between CO molecules(repulsive). Using the standard procedure in textbooks²⁹, we can obtain a dispersion relation for the phonon spectrum as

$$\omega^2 = \omega_0^2 - \frac{2C}{M} (1 - \cos Ka). \quad (4)$$

where K is the wave-vector and a the lattice constant. Approximating the force constant by $M\omega_0^2 = E_a / a^2$ and $C = \epsilon / a^2$, with E_a as the diffusion barrier height at zero coverage and ϵ as the CO-CO interaction energy, we have obtained downward dispersion relations of phonon spectra of 105cm^{-1} to 74cm^{-1} from the $\bar{\Gamma}$ point ($K=0$) to the zone boundary ($K=\pi/2a$) in the $[1\bar{1}0]$ direction and 80cm^{-1} to 62cm^{-1} in the $[001]$ direction. Despite the crudeness of the calculation, quantitatively these results are in good agreement with the EELS measurement¹⁰.

Opposite to what we might expect, the CO-CO adsorbate-adsorbate interaction does not show any anisotropic effect in the diffusion activation energies. The reductions of these diffusion activation energies due to the short range CO-CO direct interaction in both $[1\bar{1}0]$ and $[001]$ directions are about the

same, 2.0kcal/mol. Although we cannot rule out the possibility that the CO-CO direct interaction is isotropic, the model we will construct next seems to be more reasonable to explain this absence of anisotropy.

In Fig. 6 (a) and (b), we have shown the adsorbates configurations near the saturation coverage (only one site is not occupied) for CO diffusion along $[1\bar{1}0]$ and $[001]$, respectively. Since only neighboring CO molecules on the same Ni row interact with each other (see subsection c)), a diffusing CO molecule jumping from its adsorption site to neighboring empty site along $[1\bar{1}0]$ can interact with only one nearest neighbor CO. On the other hand, a diffusing CO along $[001]$ can interact with two nearest CO molecules. This would lead to anisotropy due to adsorbate-adsorbate interaction on diffusion activation energy if the effect from adsorbate-adsorbate interaction on the saddle points did not cancel it. However, a CO molecule at the saddle point C along $[1\bar{1}0]$ is at least 3.10\AA away from all the other CO molecules and thus should not be affected by the direct CO-CO interaction. The situation for CO at the saddle point C' along $[001]$ is very different. The distance of CO at C' from the two nearest neighbor CO molecules is $\sim 2.72\text{\AA}$ without considering possible displacement of the activated complex along the surface normal direction. Therefore, the adsorbate-adsorbate interaction cannot be neglected. It could have compensated the effects on CO at the adsorption site and resulted in apparently weak anisotropy in the change of diffusion activation energy due to CO-CO interaction.

f) Discussion on the Anisotropy of Preexponential Factor

From Fig. 4(b), the anisotropy in the diffusion preexponential factors are obvious. However, the usual compensation law is not obeyed. With the diffusion

activation energies along [001] being larger than those along $[1\bar{1}0]$, the associated preexponential factors in the [001] direction are smaller by a factor of 3 than those in the $[1\bar{1}0]$ direction. Due to the small difference in the activation energies, this violation of the compensation law may not be very severe.

Transition state theory (TST) can be applied to calculate anisotropy of the preexponential factor once a surface potential is known. Because of the coverage independence of the diffusion coefficient in the low coverage region, we can simplify the calculation by applying the TST in the $\theta \rightarrow 0$ limit (tracer diffusion). The expression for the tracer diffusion coefficient is¹

$$D = \frac{1}{4} \langle l^2 \rangle \nu = 1/4 \langle l^2 \rangle \nu_0 \exp(-E_a/k_B T), \quad (5)$$

where l is the hopping length, ν the hopping frequency, ν_0 the trial frequency and E_a the diffusion activation energy. The pre-exponential factor is defined in terms of hopping length l and trial frequency ν_0 by

$$D_0 = 1/4 \langle l^2 \rangle \nu_0. \quad (6)$$

In the transition state theory, the trial frequency is given by³⁰

$$\nu_0 = \frac{kT}{h} \frac{Z_C^\ddagger}{Z_A}, \quad (7)$$

where Z_C^\ddagger is the partition function of the adsorbate (excluding the diffusion coordinate) at the saddle point C and Z_A is the total partition function of the

adsorbate in the well A (see Fig.7). In order to calculate the partition functions, we use a surface potential

$$V(x,y) = E_{\text{diff}}[1\bar{1}0](1 - \cos \frac{2\pi x}{a}) + E_{\text{diff}}[001] (1 - \cos \frac{\sqrt{2}\pi y}{a}) , \quad (8)$$

where $E_{\text{diff}}[1\bar{1}0]$ and $E_{\text{diff}}[001]$ are the measured diffusion activation energies in the two principal directions respectively. The periodicity of the surface potential has been chosen to be the same as that of the substrate, namely a along $[1\bar{1}0]$ (\hat{x} direction) and $\sqrt{2}a$ along $[001]$ (\hat{y} direction). This potential can give correct barrier heights for CO diffusion. Since the well site A is common, the partition function Z_A is the same for both $[1\bar{1}0]$ and $[001]$ directions. The anisotropy in the trial frequencies comes solely from the partition functions at the two different saddle points along the two corresponding directions. The relevant partition functions at the saddle points C and C' in $[1\bar{1}0]$ and $[001]$ directions (see Fig. 7) can be written approximately as

$$Z_C^\ddagger[1\bar{1}0] = Z_{C,y\text{vib}} \cdot Z_{C,\text{bending}} \cdot Z_{C,z\text{vib}} \cdot Z_{C,\text{in}} \cdot Z_{C,\text{el}} , \quad (9)$$

$$Z_{C'}^\ddagger[001] = Z_{C',x\text{vib}} \cdot Z_{C',\text{bending}} \cdot Z_{C',z\text{vib}} \cdot Z_{C',\text{in}} \cdot Z_{C',\text{el}} , \quad (10)$$

if the coordinates involved can be separated. Here, \hat{z} is the $[110]$ (surface normal) direction. The electronic, CO internal vibrational, and the z-direction vibrational partition functions $Z_{C,\text{el}}$ ($Z_{C',\text{el}}$), $Z_{C,\text{in}}$ ($Z_{C',\text{in}}$), and $Z_{C,z\text{vib}}$ ($Z_{C',z\text{vib}}$) at the two saddle points certainly would not differ very much because the corresponding potentials seen by the electrons of the molecule or by the molecule as a whole do not have large differences³¹. The anisotropy in the trial

frequencies should be dominated by the difference in the frustrated translational partition functions $Z_{C,yvib.}$ and $Z_{C',xvib.}$ and the bending (frustrated rotational) partition functions $Z_{C,bending}$ and $Z_{C',bending}$.

The frustrated translational partition functions can be readily calculated by using the surface potential of Eq. (8). Including contribution from the continuum states to the partition functions, we obtain

$$\begin{aligned}
 Z_{C,yvib.} &= \sum_{n=0}^{23} \exp\left(-\frac{n\hbar\omega_y}{k_B T}\right) + \sum_k \exp\left(-\frac{\hbar^2 k^2}{2Mk_B T}\right) \exp\left(-\frac{E_{diff}^{[001]}}{k_B T}\right) \\
 &= \sum_{n=0}^{23} \exp\left(-\frac{n\hbar\omega_y}{k_B T}\right) + \frac{\sqrt{2}a}{\hbar} \sqrt{\frac{Mk_B T}{2\pi}} \exp\left(-\frac{E_{diff}^{[001]}}{k_B T}\right), \quad (11)
 \end{aligned}$$

$$\begin{aligned}
 Z_{C',xvib.} &= \sum_{n=0}^{15} \exp\left(-\frac{n\hbar\omega_x}{k_B T}\right) + \sum_k \exp\left(-\frac{\hbar k^2}{2Mk_B T}\right) \exp\left(-\frac{E_{diff}^{[1\bar{1}0]}}{k_B T}\right) \\
 &= \sum_{n=0}^{15} \exp\left(-\frac{n\hbar\omega_x}{k_B T}\right) + \frac{a}{\hbar} \sqrt{\frac{Mk_B T}{2\pi}} \exp\left(-\frac{E_{diff}^{[1\bar{1}0]}}{k_B T}\right), \quad (12)
 \end{aligned}$$

where the vibrational frequencies can be calculated from small vibration formulas: $\omega_x = (2\pi/a) [E_{diff}^{[1\bar{1}0]}/M]^{1/2} \sim 2\pi \times 105 \text{cm}^{-1}$ for vibration in \hat{x} and $\omega_y = (2\pi/\sqrt{2}a) [E_{diff}^{[001]}/M]^{1/2} \sim 2\pi \times 80 \text{cm}^{-1}$ for vibration in \hat{y} . The number of discrete states in the summation are truncated by the maximum potential and no anharmonic effect has been included. It turns out that the contribution from the continuum are negligible. The results of the two partition functions are $Z_{C,yvib.} \sim 2.45$ and $Z_{C',xvib.} \sim 2.00$ respectively. From the above discussion, the

ratio of the two preexponential factors is given by

$$\frac{D_0[1\bar{1}0]}{D_0[001]} = \frac{Z_C^\ddagger[1\bar{1}0]}{Z_{C'}^\ddagger[001]} \frac{a^2}{(\sqrt{2}a)^2} \sim 0.6 \frac{Z_{C \text{ bending}}}{Z_{C' \text{ bending}}} \quad (13)$$

The bending partition functions are somewhat difficult to calculate because the corresponding potentials are not known. Assuming they are not very different at the two saddle points, we then obtain comparable preexponential factors for the two directions. This can be compared with the experimental value of 3. Considering the approximations made in this estimate, the agreement with the experiment is reasonable.

e) Theoretical Fittings of $D(\theta)$

The adsorbate-adsorbate interaction effect on surface diffusion has been investigated on a number of other systems. Some systems such as H or D/Ni(100)³², H/Ru(001)³³, H or D/Rh(111)^{34,35}, CO/Rh(111)³⁵, and CO/Pt(111)³⁶ do not show much coverage dependence, other systems such as H or D/Ni(111)³², D/Pt(111)³⁵ and CO/Ru(100)³⁷ show strong coverage dependence. Most of these studies except CO/Ru(100) did not address the nature of the adsorbate-adsorbate interaction. For CO/Ru(100) system the nature of adsorbate-adsorbate interaction was identified as CO-CO direct interaction. However, the use of a lattice gas model for this system with nonequivalent sites diminishes the value of theoretical attempts^{3,37}. Without identifying the range of the nearest neighbor interaction, two separate

calculations, one including CO-CO interaction at saddle points³ and the other not³⁷, yielded very different interaction parameters.

In this section we will try to use a simple model to fit the coverage dependent diffusion results. The simplest theory is the lattice gas model with a mean field approximation as discussed in Chapter II. For CO/Ni(110), the assumptions of the lattice gas model are not strictly met since the adsorption site in CO/Ni(110) system changes from a mixture of top and short-bridge sites below a 0.7ML coverage to pure short-bridge sites above 0.7ML coverage. The CO-CO direct interaction comes in as a result of the change on adsorption sites. To account for this effect, we modify Eq. (22) of Chapter II by replacing the adsorbate-adsorbate interaction $4\epsilon\theta$ and $6\epsilon*\theta$ with $2\epsilon\theta_{\text{eff}}$ and $2\epsilon*\theta_{\text{eff}}$ respectively, where θ_{eff} is defined by

$$\begin{aligned} \theta_{\text{eff}} &= 0, & \text{for } \theta < \theta_0 \\ &= \frac{\theta - \theta_0}{1 - \theta_0} & \text{for } \theta > \theta_0 \end{aligned} \quad (14)$$

The 4->2, and 6->2 change in the interaction is due to change in the number of nearest-neighbor sites. In our case, the number of nearest-neighbor site of CO-CO direct interaction for CO/Ni(110) is 2 when the CO is at an adsorption site and 4 when CO is at the saddle point. This modification correctly gives us the CO-CO interaction below θ_0 and at $\theta=1$. The θ_0 is the coverage at which the adsorption site starts to change. We will take it as the hypothetical value $\theta_0=0.67$ for our calculation. The coverage dependent diffusion coefficient is then given by³⁸

$$D(\theta) = D_0 \exp(-E_a/k_B T) (1-\theta) \exp(2\epsilon\theta_{\text{eff}}/k_B T) \exp(-2\epsilon*\theta_{\text{eff}}/k_B T)$$

$$\times \left\{ \frac{1}{1-\theta} + 2\varepsilon\theta_{\text{eff}}/k_{\text{B}}T \right\}. \quad (15)$$

The diffusion activation energy and the preexponential factor can be derived from this expression as

$$E_{\text{diff}}(\theta) = E_{\text{a}} - 2\varepsilon\theta_{\text{eff}} + 2\varepsilon^*\theta_{\text{eff}} - \frac{2\varepsilon\theta_{\text{eff}}(1-\theta)}{1 + 2\varepsilon\theta_{\text{eff}}(1-\theta)/k_{\text{B}}T} \quad (16)$$

$$D_0(\theta) = D_0 \left\{ 1 + 2\varepsilon\theta_{\text{eff}}(1-\theta)/k_{\text{B}}T \right\} \exp\left(- \frac{2\varepsilon\theta_{\text{eff}}(1-\theta)/k_{\text{B}}T}{1 + 2\varepsilon\theta_{\text{eff}}(1-\theta)/k_{\text{B}}T} \right) \quad (17)$$

Assuming $\varepsilon^* = 0$, we fit the diffusion activation energies by Eq. (16). The solid curves in Fig. 4(a) are fittings with parameter $2\varepsilon = 1.8\text{kcal/mol}$ in both $[1\bar{1}0]$ and $[001]$ directions. The agreement between the experimental data and the calculation is very reasonable and the resulting interaction energy from the fittings are comparable with the reduction of the activation energies, namely 2kcal/mol . However, the same parameter will not fit $D_0(\theta)$. This is because the theory has not considered the effect of the adsorbates on the preexponential factor correctly. Without properly evaluating the entropy change from adsorption sites to saddle points caused by the adsorbate-adsorbate interactions, the model cannot predict a correct preexponential factor. For example, the preexponential factor from Eq. (17) at $\theta=1.0$ is D_0 , which is unreasonable as it is the same as that of tracer diffusion. The compensation effect between the activation energy and the preexponential factor is missing from Eq. (16) and (17), in contradictory with our experimental observation (see Fig. 4). Because of

this, any attempt to fit $D(\theta)$ as a function of coverage at a constant temperature by Eq. (15) will not result in a correct adsorbate-adsorbate interaction energy. An attempt to fit $D(\theta)$ by Eq. (15), shown by Fig. 5 , leads to an interaction energy ϵ about a factor of 3 smaller than the correct one.

D. Summary

In summary, we have studied a coverage dependent diffusion for a system with intrinsic anisotropy. Only CO-CO direct interaction is found to affect surface diffusion. The adsorbate-substrate interaction and its anisotropy are clearly identified. The CO-CO direct interaction is deduced to be about 2kcal/mol and its effect on the anisotropy of the diffusion activation energy appears negligible. The latter has been explained as a result of different adsorbate-adsorbate interactions on the two saddle points. Comparisons with other experimental results have been made and in most cases good agreements have been reached. Theoretical fitting of the coverage dependent diffusion results has been attempted. The crudeness of the model has prohibited us to obtain a complete agreement with the experiment.

References

- ¹ For a recent review, see R. Gomer, Rep. Prog. Phys. **53**, 917(1990).
- ² M. Bowker and D.A King, Surf. Sci. **71**, 583(1978); **72**, 208(1978); D.A.Reed and G. Ehrlich, Surf. Sci. **102**, 588(1981); **105**, 603(1981); A. Natori and H. Ohstubo, Surf. Sci. **171**, 13(1986); R. DiFoggio and R. Gomer, Phys. Rev. B **25**, 3490(1982).
- ³ V.P. Zhdanov, Surf. Sci. **257**, 63(1991), and references therein.
- ⁴ Xu-dong Xiao, Yuanlin Xie and Y. R. Shen, Surf. Sci. **271**, 295(1992).
- ⁵ M. D. Aley, M. J. Yates, Jr., Surface Sci. **165**, 447(1986); D.A.Wesner, F.P.Coenen and H.P.Bonzel, Phys. Rev. Lett. **60**, 1045(1988).
- ⁶ W. Riedl and D. Menzel, Surface Sci. **163**, 39(1985).
- ⁷ For details, see Xu-dong Xiao, X.D. Zhu, W. Daum and Y.R. Shen, Phys. Rev. B, (1992).
- ⁸ R. Gomer, private communication.
- ⁹ D. J. Hannaman and M.A.Passler, Surf. Sci. **203**, 449(1988).
- ¹⁰ B. Voigtlander, D. Bruchmann, S. Lehwald and H. Ibach, Surf. Sci. **225**, 151(1990).
- ¹¹ S.Haq, J.G.Love and D.A.King, Surf. Sci. **275**, 170(1992).
- ¹² J. Bauhofer, M. Hock, and J. Koppers, Surf. Sci. **191**,395(1987).
- ¹³ R. J. Behm, G. Ertl and V. Penka, Surf. Sci. **160**, 387(1985).
- ¹⁴ C.S.Feigerle, S.R.Desai and S.H.Overbury, J.Chem.Phys. **93**,787(1990).
- ¹⁵ H.Kuhlenbeck, M.Neumann and H.-J. Freund, Surf. Sci. **173**, 194(1986).
- ¹⁶ J. Lee, J.Arias, C. Hanrahan, R.Martin, H. Metiu, C. Klauber, M.D.Alvey and J.T.Yates, Jr., Surf. Sci. **159**, L460(1985); J.T.Yates,Jr., C. Klauber, M.D. Alvey, H. Metiu, J. Lee, R.M. Martin, J. Arias and C. Hanraman, in: *Desorption*

- Induced by Electronic Transitions*, Proc. DIET II Conf., Eds. W. Brenig and D. Menzel (Springer, Berlin, 1985)p.123; B. A. Gurney and W. Ho, *J. Vacuum Sci. Technol.* **A3**, 1541(1985).
- ¹⁷ Yu.K. Tovbin, *Prog. Surf. Sci.* **34**,1(1991).
- ¹⁸ T.S. Lin, H.-J. Lu and R. Gomer, *Surf. Sci.* **234**, 251(1990).
- ¹⁹ M. Trenary, K.J.Uram and J. T. Yates,Jr., *Surf. Sci.* **157**, 512(1985).
- ²⁰ H. Froitzheim and U. Kohler, *Surf. Sci.* **188**,70(1987); J.B.Miller, H.R.Siddiqui, S.M.Gates, J.N.Russell,Jr., J.T. Yates,Jr., J.C.Tully, and M.J.Cardillo, *J.Chem.Phys.* **87**, 6725(1987).
- ²¹ B. Roop, A. Costello, D. R. Mullins, and J. M. White, *J. Chem. Phys.* **86**, 3003(1987).
- ²² H. C. Peebles, D. E. Peebles and J. M. White, *Surface Sci. Lett.* **125**, L87(1983).
- ²³ J.T.Yates,Jr., and D. W.Goodman, *J. Chem.Physics*, **73**, 5371(1980).
- ²⁴ T. Narusawa, W. M. Gibson, and E. Tornqvist, *Phys. Rev. Lett.* **47**, 417(1981); *Surf. Sci.* **114**, 331(11982).
- ²⁵ W. Oed, U. Starke, K. Heinz, K. Muller, and J. B. Pendry, *Surf. Sci.* **251/252**, 488(1991).
- ²⁶ M. L. Xu, and S. Y. Tong, *Phys. Rev. B* **31**, 6332((1985); S. M. Yalisove, W. R. Graham, E. D. Adams, M. Copel, and T. Gustafsson, *Surf. Sci.* **171**, 400(1986).
- ²⁷ M. W. Finnis, and V. Heine, *J. Phys. F* **4**, L37(1974).
- ²⁸ G. Doyen and G. Ertl, *Surf. Sci.* **43**, 197(1974).
- ²⁹ For example, C. Kittel, *Introduction to Solid State Physics*, (John Wiley & Son, Inc. New York, 1986).
- ³⁰ Peter Hanggi, Peter Talkneer, and Michal Borkovec, *Rev. Modern Phys.* **62**, 251(1990).

- ³¹ C. H. Mak and S. M. George, Chem. Phys. Lett. **135**, 381(1987).
- ³² T.-S. Lin and R. Gomer, Surf. Sci. **255**, 41(1991).
- ³³ C.H.Mak, J. L. Brand, B.G.Koehler, and S.M.George, Surface Sci. **191**,108(1987).
- ³⁴ S.S.Mann, T.Seto, C.J.Barnes and D.A.King, Surface Sci. **261**, 155(1992).
- ³⁵ E. G. Seebauer, A.C.F. Kong and L.D.Schmidt, J. Chem. Phys. **88**, 6597(1988).
- ³⁶ V.J.Kwasniewski and L.D. Schmidt, Surf. Sci. **274**, 329(1992).
- ³⁷ A.A.Deckert, J. L. Brand, M. V. Arena and S. M. George, Surface Sci. **208**,441(1989); V.P.Zhdanov, Surface Sci. **257**, 63(1991).
- ³⁸ V. P. Zhdanov, Phys. Lett. A **137**, 409(1989).

Figure captions:

Figure 1: Linear diffraction signals versus time for coverage $\theta=0.98$ at three temperatures for diffusion (a) along $[1\bar{1}0]$, and (b) along $[001]$. The solid lines are single exponential fits.

Figure 2: Diffraction signals versus time with a second laser pulse applied at the times indicated by the arrows. The experiment have been carried out along $[001]$ at $T=210\text{K}$ for initial coverage $\theta_0=0.5$. The starting S/N is ~ 40 , and the second laser pulse intensities are: (a) $1.08\text{J}/\text{cm}^2$, (b) $0.98\text{J}/\text{cm}^2$, and (c) $1.11\text{J}/\text{cm}^2$. The time constants indicated along the decay signals are from single exponential fits.

Figure 3: Arrhenius plot for diffusion of CO on Ni(110) with coverage 0.48ML and 0.98ML along the two principal directions: $[1\bar{1}0]$ and $[001]$.

Figure 4: (a) Diffusion activation energy and (b) preexponential factor as a function of coverage for CO diffusing along $[1\bar{1}0]$ and $[001]$ directions. The solid lines in (a) are theoretical fits by Eq. (16), and the solid lines in (b) are for eyeguide. The desorption energy as a function of coverage has also been depicted in (a) for comparison.

Figure 5: Diffusion coefficient as a function of coverage at constant temperatures. The solid lines are theoretical fits by Eq.(15) with $2\varepsilon=0.55\text{kcal/mol}$ for 218K, 0.61kcal/mol for 200K, and 0.63kcal/mol for 182K respectively.

Figure 6: Geometries of CO on Ni(110) surface with one Ni site unoccupied. The positions of diffusion saddle points along $[1\bar{1}0]$ and along $[001]$ has been indicated in (a) and (b) with the relevant distances labeled. The Ni and CO are not drawn in proportion.

Figure 7: Surface potential corrugations given by Eq. (8). The scales of the barrier height in $[1\bar{1}0]$ and $[001]$ are not in proportion for the purpose of showing anisotropy.

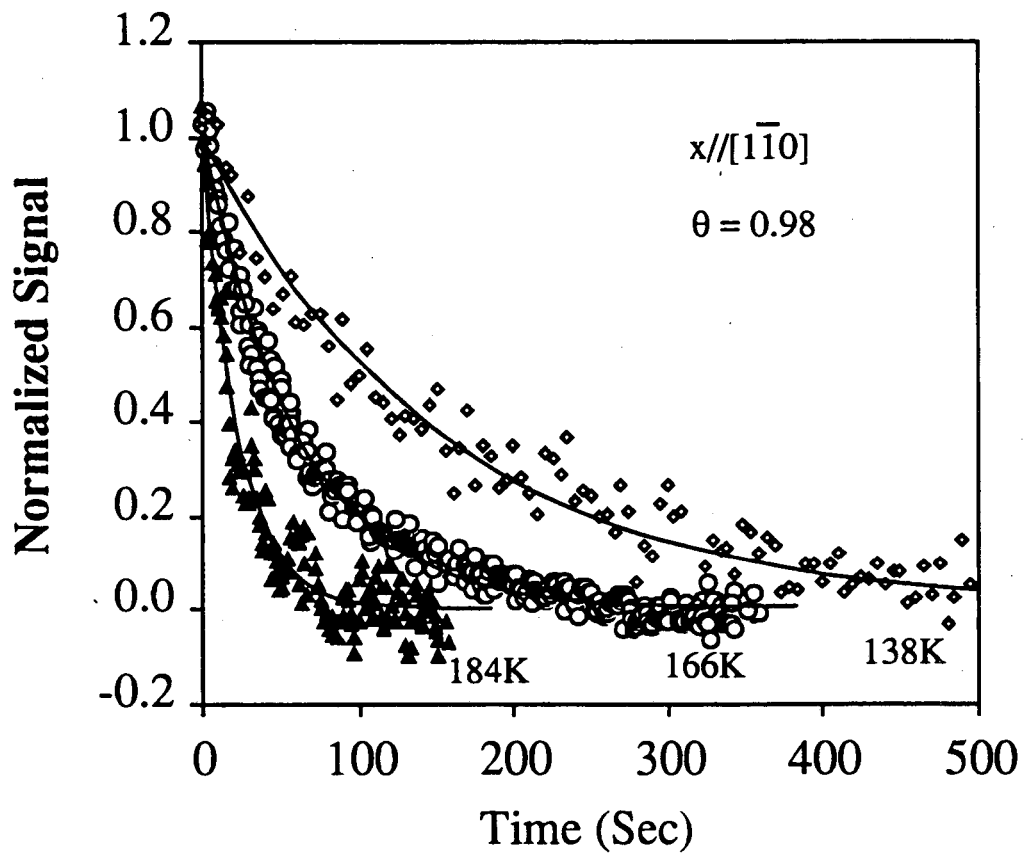


Figure 1(a)

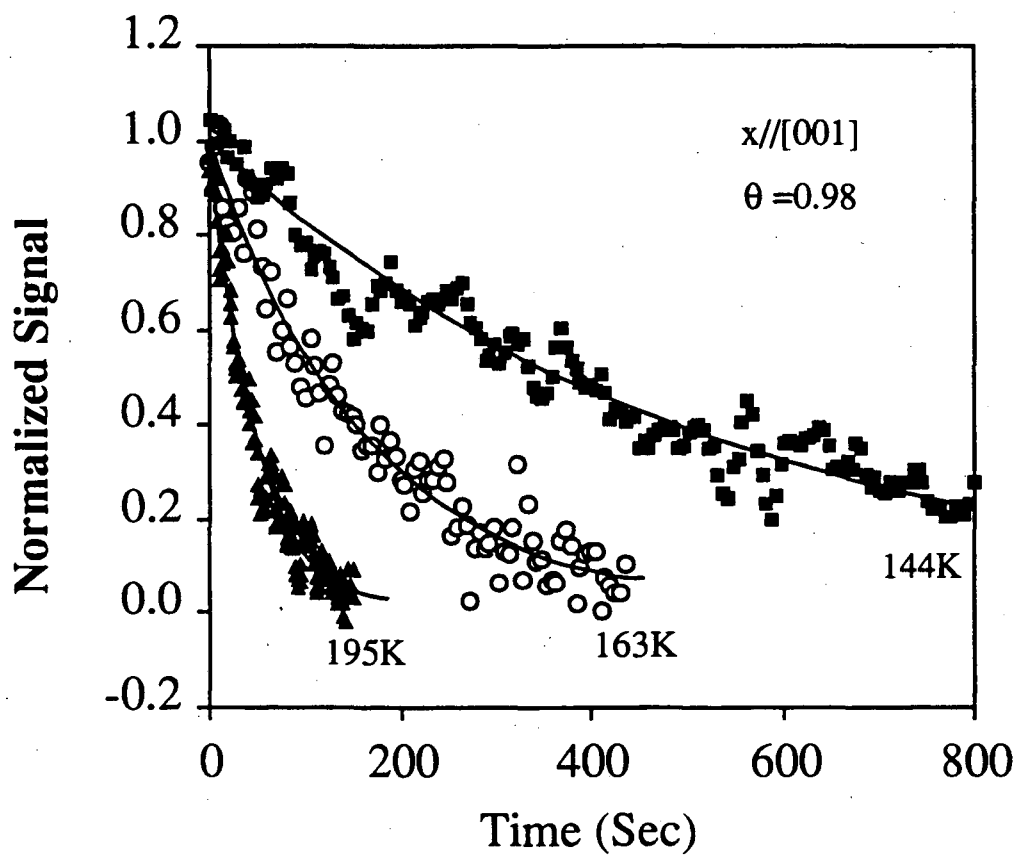


Figure 1(b)

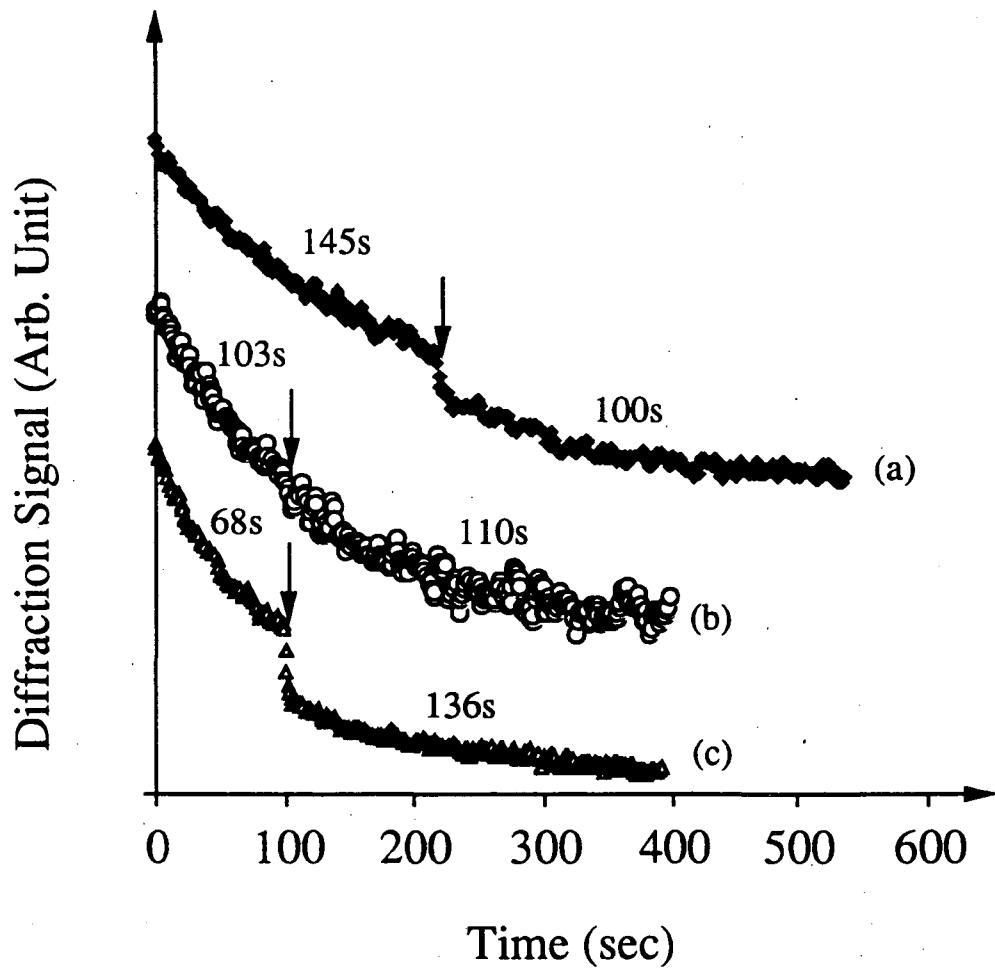


Figure 2

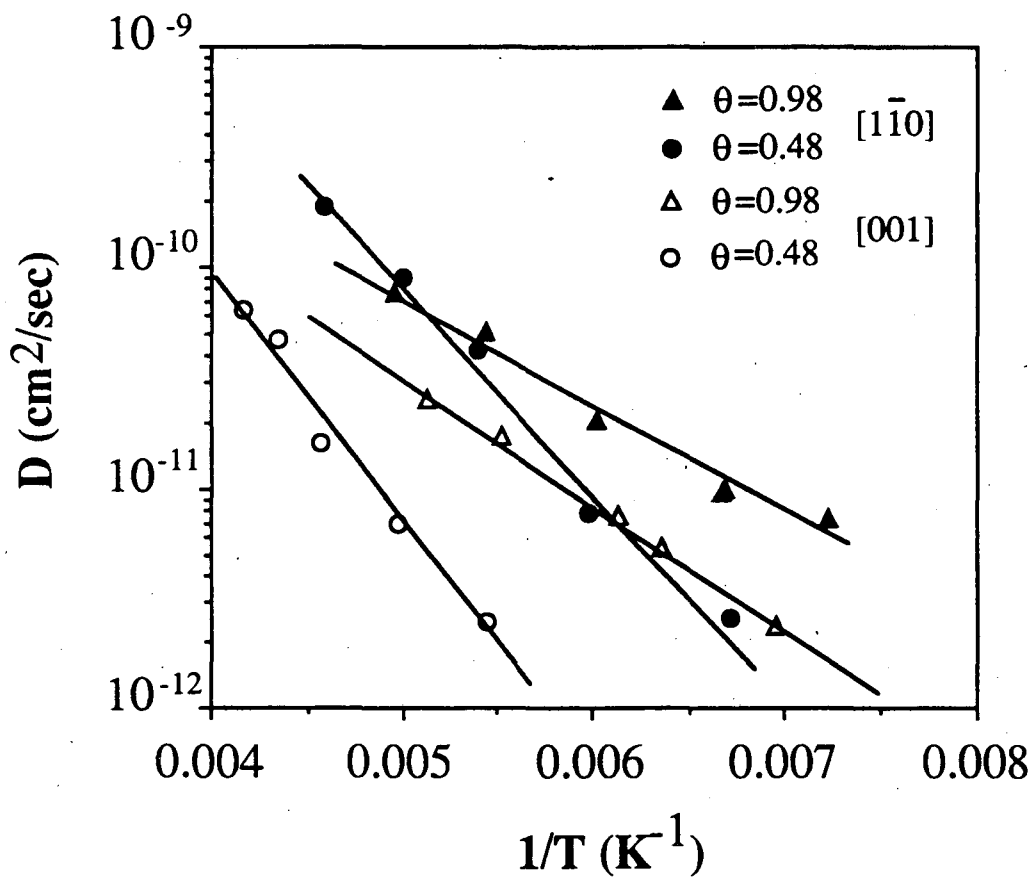


Figure 3

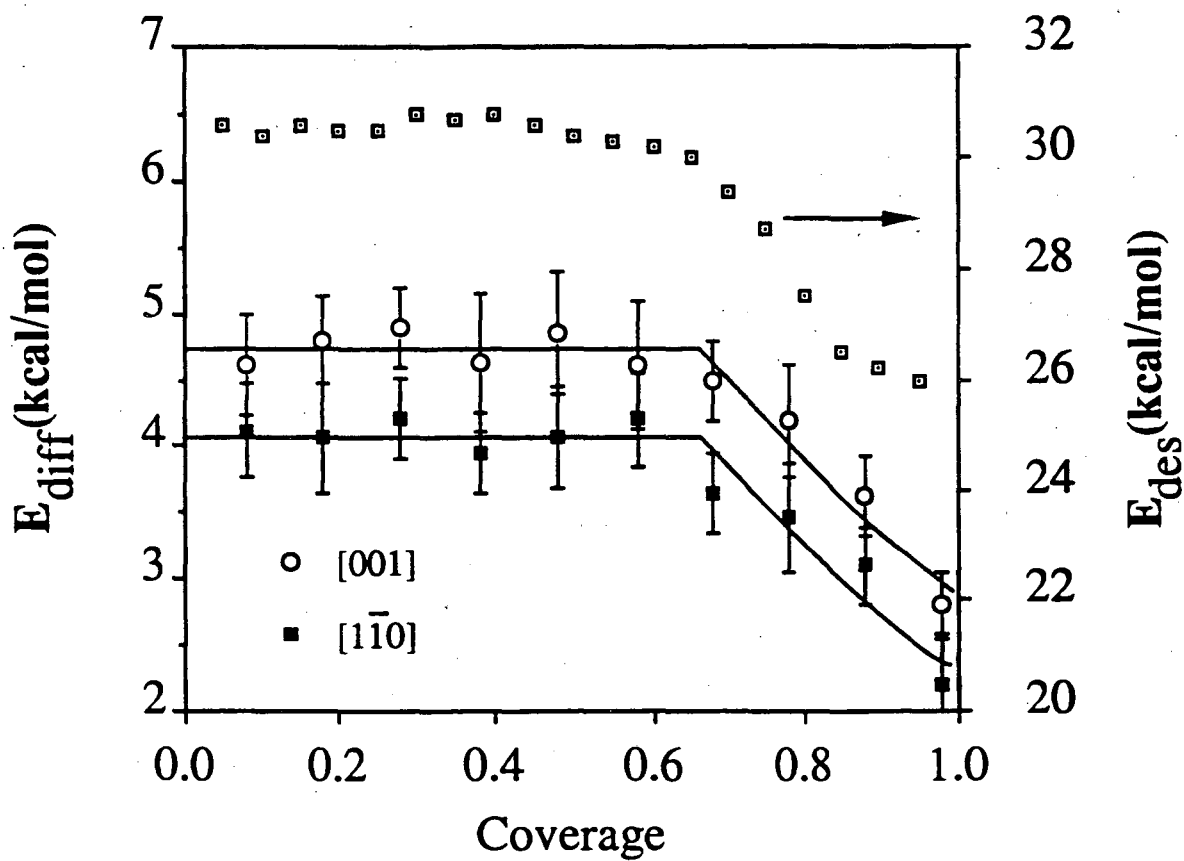


Figure 4(a)

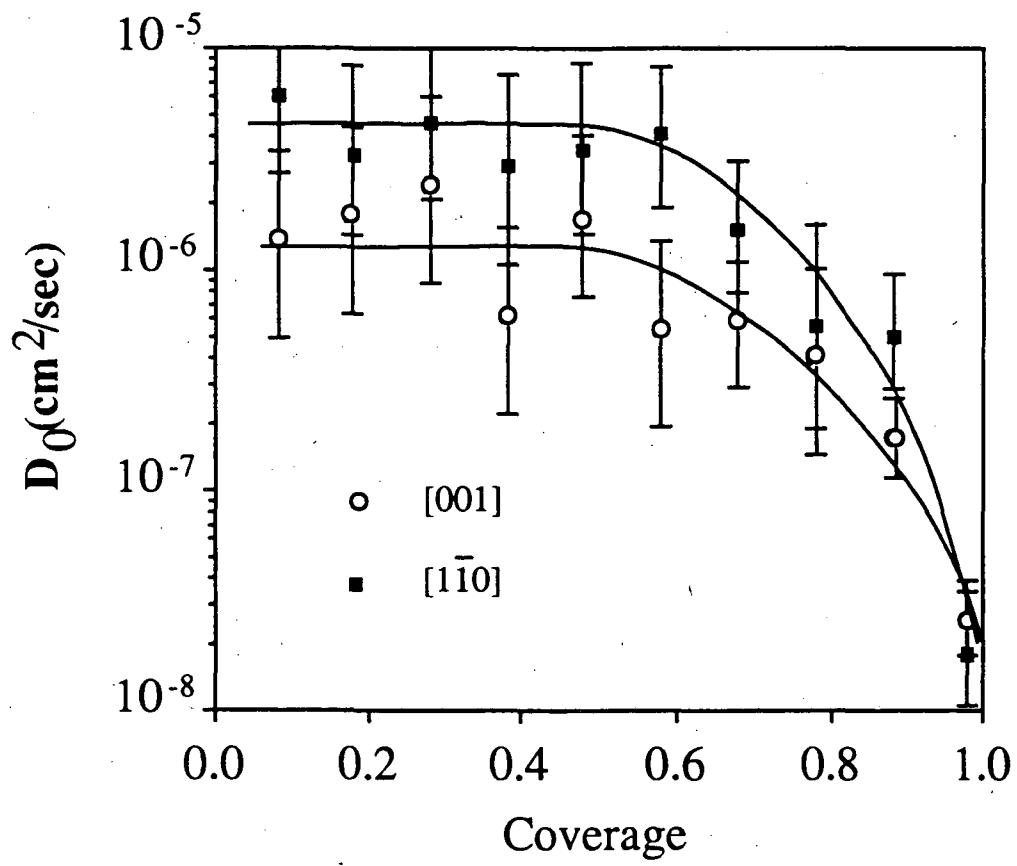


Figure 4(b)

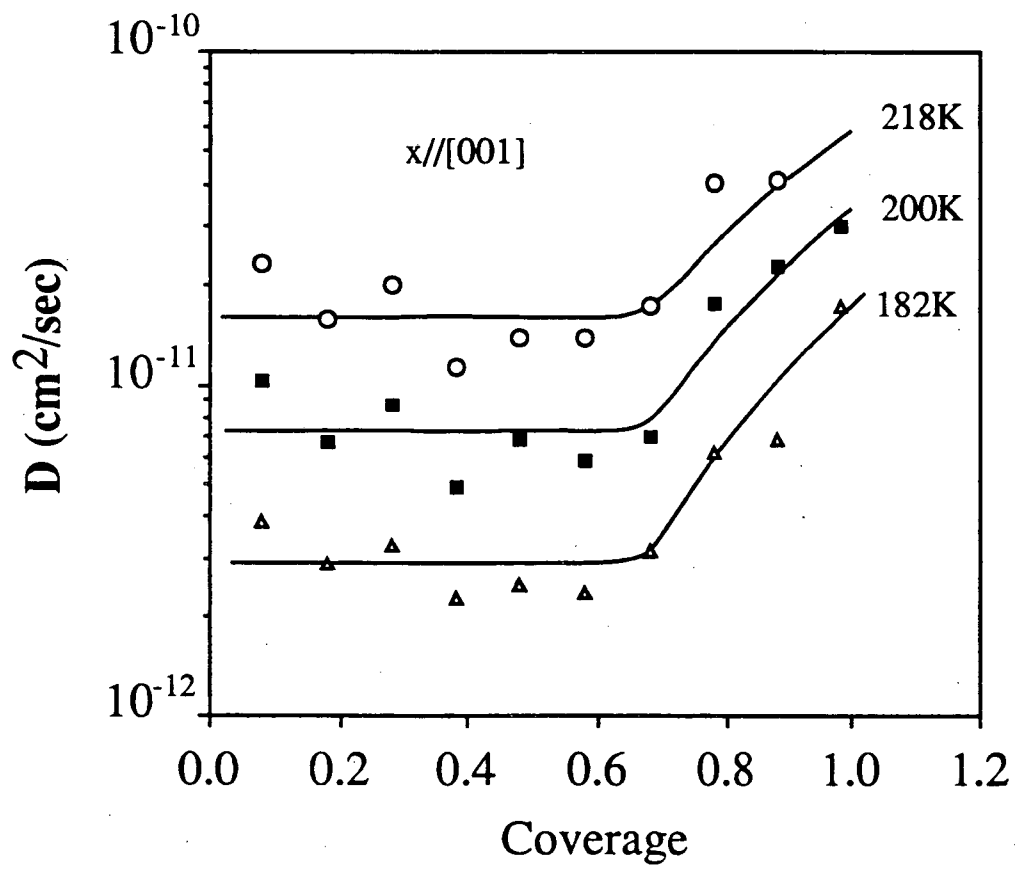


Figure 5

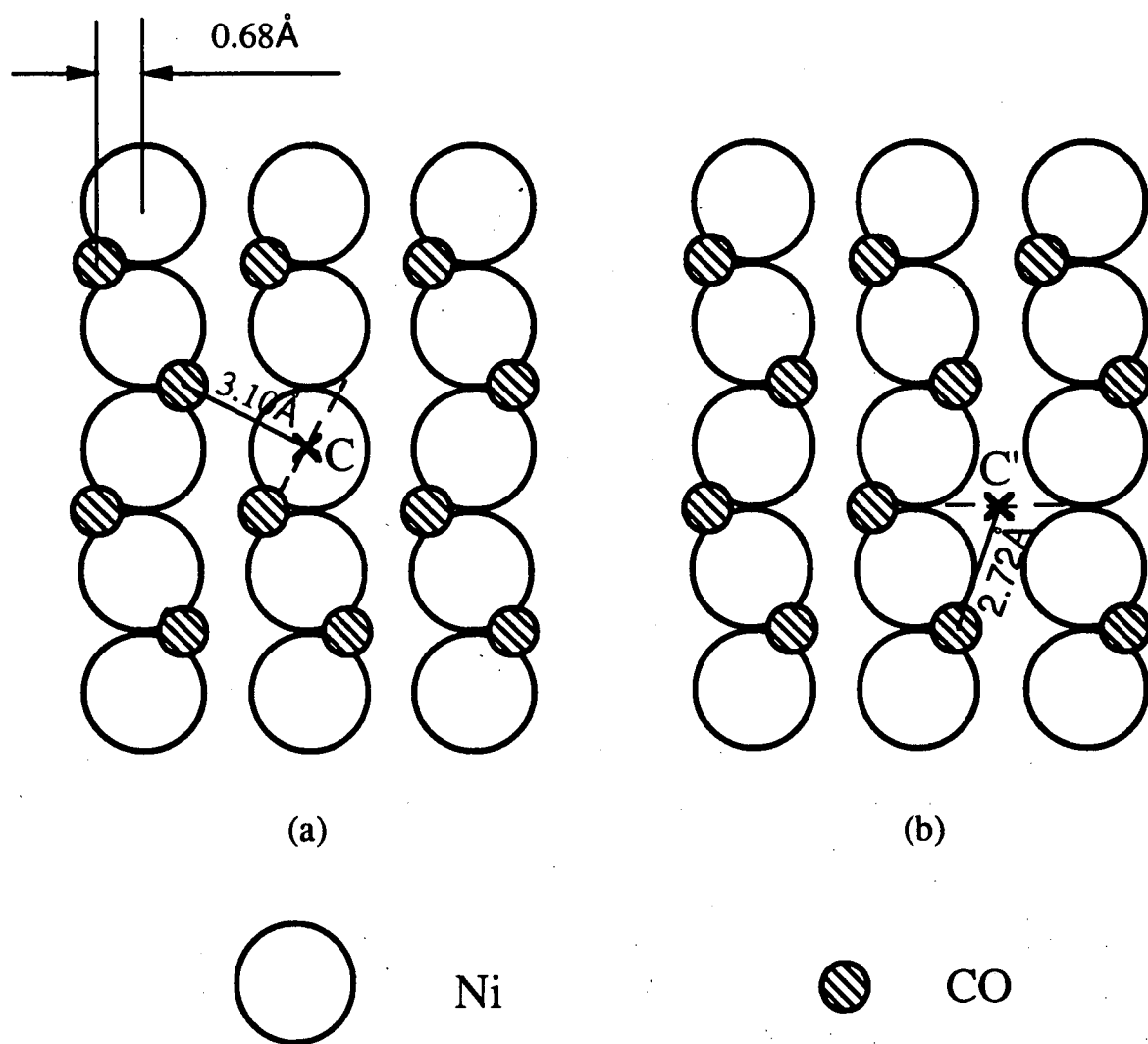


Figure 6

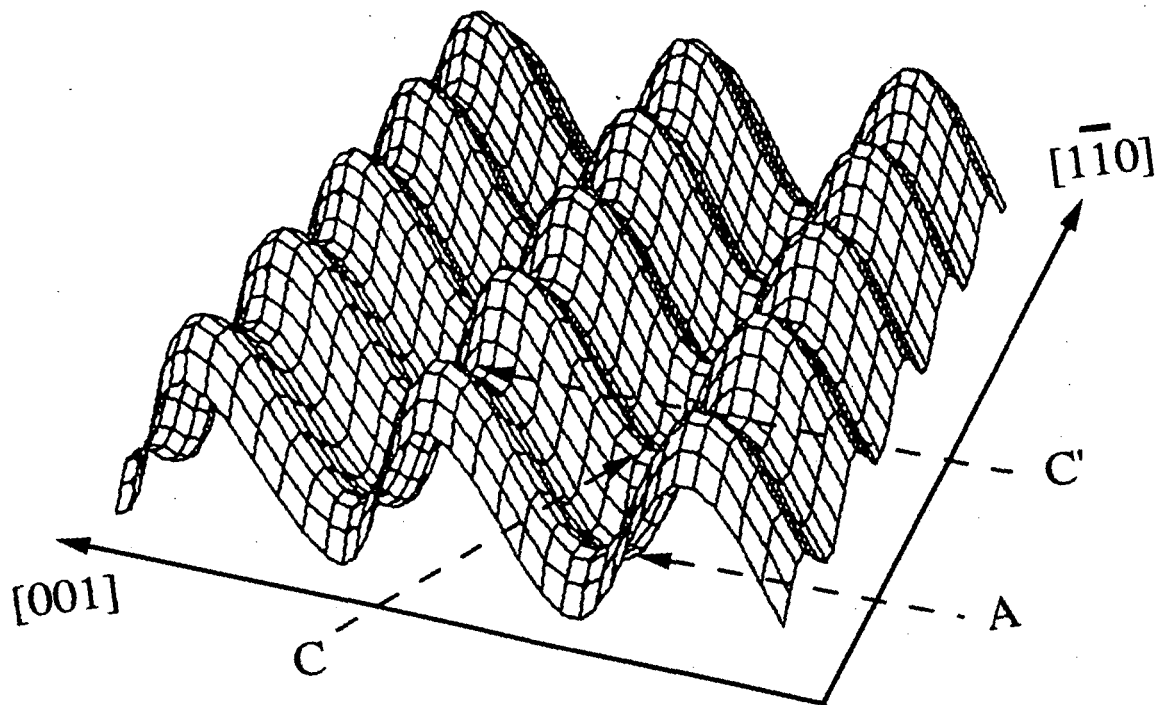


Figure 7

VI. Impurities, Defects, and Surface Diffusion: CO/Ni(110)

A. Introduction

As an important surface process surface diffusion has been studied extensively with a variety of techniques in the past¹. Considerable data base was established for different systems. However, questions such as how impurities and defects affect surface diffusion were seldom explored experimentally. Theoretical calculations on these questions do exist. They predict little effect from small amount of impurities or defects (few percent)^{2,3}.

It has been noted that surface diffusion measurements carried out presumably on the same systems with different techniques by different authors often yield rather different activation energies and preexponential factors^{1,4}. The discrepancy was often attributed to difference in temperatures¹ or techniques⁵ used in the measurements. Whether this discrepancy can also be due to different samples and different sample treatments, or more specifically, due to surface impurities, defects, or strains, no one has yet provided any answer.

Recently we have worked on CO diffusion on Ni(110) surface using different samples and different sample preparation procedures. The results showed unambiguously that the sample treatment could significantly affect surface diffusion. In this chapter we will report effects from S impurities and surface defects on CO diffusion on Ni(110). The investigation on the effect of S impurities was performed for a few low S coverages and it was found that as low as 3% S monolayer could change appreciably the diffusion speed and its activation energy of CO on Ni(110). The effect of surface point defects was examined in a qualitative way, namely by additional Ar⁺ ion sputtering on a

well annealed surface or by annealing an Ar^+ sputtered sample for different length of times. The step effect on CO diffusion was carried out with a miscut Ni(110) surface. The effect of point defects was found to be profound in altering the preexponential factor, but insignificant to the diffusion activation energy. The steps have been found to dominate surface diffusion with an increasing surface diffusion barrier. Qualitative explanations are given for the observations.

B. Experiment

The experiment was performed in an ultrahigh vacuum (UHV) chamber with a base pressure of 2.0×10^{-10} torr. The major set of the data was collected from a single crystal Ni(110) sample, cut and mechanically polished to within 0.2° from the (110) plane. The data on the step effect were obtained from a Ni(110) sample miscut by $\sim 1.5^\circ$ along the $[1\bar{1}0]$ direction. Before any measurement, the sample was treated by many sputtering and annealing cycles to get rid of impurities such as S, O, and C. Subsequently, normal cleaning procedure was adopted to prepare a clean surface, i.e., the surface of the sample was first Ar^+ sputtered at 1.0×10^{-4} torr Ar pressure with a 500V beam voltage for approximately 30 minutes at room temperature and then annealed at 1120K for 10 min followed by a slow cooling down at a rate of $\sim 0.5\text{K}/\text{sec}$ to 800K and a rate of $2\text{K}/\text{sec}$ to room temperature. In the later sections, surfaces prepared by this procedure will be referred as normally prepared surface. Auger spectra showed no detectable impurities ($< 0.3\%$ S and C). Sharp 1×1 LEED pattern from a clean Ni(110) surface and clear 2×1 LEED pattern from a full CO monolayer on Ni(110) were observed to ensure that the surface was well ordered. Liquid nitrogen was used to cool the sample afterwards to the measurement temperatures. A Chromel-Alumel thermal couple welded to the

sample was used to monitor the sample temperature. The temperature could be controlled to within $\pm 1\text{K}$.

For experiment on the S impurity effect, the S surface impurities were introduced through bulk-to-surface segregation by heating a normally prepared sample for an extended period at 1120K, typically, about one hour to yield 1% S. The concentration of S was measured by AES with a calibrated ratio of S(152eV)/Ni(848eV)⁶. The S atoms are known to desorb only at very high temperatures (above 1200K)⁷ and are presumably uniformly distributed on the Ni(110) surface due to the S-S repulsive interactions. Therefore briefly flashing sample to 600K to get rid of either the adsorbed ambient gas molecules or the previously adsorbed CO before each diffusion measurement should not alter the amount of S. The experiment on the effect of point defects was performed in two different ways. The first one was by annealing the sample at 1120K for different lengths of time, from less than 1 minute to 10 minutes, after it is sputtered by Ar^+ for 30 minutes. The second one was by sputtering a normally prepared Ni(110) surface by a 500eV Ar^+ beam with a current density of $5\mu\text{A}/\text{cm}^2$ at room temperature for 5 min without no further annealing.

With the Ni(110) sample prepared in the above ways, we then dosed CO to a saturation coverage. LEED structures were still found to be 2x1 for all the surfaces except for the 15% S surface, where a 2x1 structure was barely visible with a large diffused background. CO diffusion along $[\bar{1}\bar{1}0]$ was chosen to be investigated and was measured at least at four different temperatures in the range of 140K-220K on each prepared surface. The measurement technique was described in Chapter III and we give only a briefly review here. First, two $1.06\mu\text{m}$ laser beams were used to interfere at the CO covered Ni surface to create an adsorbate grating with a coverage modulation of $\sim 3\%$ and a grating spacing of $\sim 3\mu\text{m}$. Then a polarization modulated He-Ne laser beam was used

to probe the adsorbate grating with an incident angle of 45° and the first order diffraction signal was monitored as a function of time by a lock-in detection scheme. The decay of the first order diffraction signal is related to the surface diffusion coefficient D by

$$S_1 = S_{01} \exp(-8\pi^2 D t / s^2)$$

where s is the grating spacing and S_{01} is the initial diffraction signal strength. It should be noticed that the decay time constant here depends only on the grating spacing but not on its shape.

C. Results and Discussion

a) S Impurity Effect

In Fig.1 we show the measured CO diffusion coefficients along $[1\bar{1}0]$ as a function of reciprocal temperature in an Arrhenius plot for a number of differently prepared surfaces with a CO average coverage of $\theta \sim 0.98$. Data (a) is from a normally prepared surface as described in the previous section. Data (b), (c), (d), and (e) are from surfaces with different amount of S impurities. The Arrhenius fitting parameters for these cases are summarized in Table 1. It is seen that the CO diffusion activation energy on Ni(110) with $\leq 1\%$ S impurity remain unchanged (2kcal/mol) within the experimental error. However, the CO diffusion activation energies on surfaces with 3% or higher S coverage are clearly much higher: about 6kcal/mol for surfaces with 3% and 5% S coverages and 8kcal/mol for surface with 15% S. Although the preexponential factors are

significantly larger with impurities than that for a clean surface, the CO diffusion speeds are much slower than that on a clean surface in the temperature range of our measurement. Especially in the low temperature region (~160K) the CO diffusion on surfaces with 5% S impurity are 2~3 orders of magnitude slower.

The above results are surprising in many folds. First, with only a few percent of S impurity on the Ni surface the CO diffusion has been dramatically impeded in the low temperature regime. The barrier for CO diffusion has also been significantly altered. Second, the change of CO diffusion activation energy seems to have a sudden jump as the S impurity on Ni(110) surface increases. A careful investigation of this may provide information about the nature of the S contaminated Ni(110) surface.

If sulfur is only considered as a usual coadsorbate of CO, the existing theory cannot predict such a dramatic change in the CO diffusion coefficient with any realistic S-CO interactions². What is responsible for the change, in our opinion, must be associated with the Ni substrate. It is known that S acts as a poison on Ni for catalytic methanation reaction^{9,10}. The surface science studies of S/Ni(110) has revealed that S atoms adsorb at the rectangular hollow sites of the Ni(110) surface and form a p(2x2) superstructure at 0.25ML coverage, and a c(2x2) superstructure at 0.5 ML¹¹. Sulfur has a strong interaction with Ni surfaces and this interaction generally leads to an expansion of the Ni surface. With a saturation S coverage (0.5ML, c(2x2)), the originally contracted Ni(110) surface ($\Delta d_{12}/d_{12B} \sim -9\%$, d_{12B} is the bulk distance between two layers in the surface normal direction) is expanded by more than 10% as compared to the bulk atomic distance¹¹. For a clean metal surface, contractive relaxation presumably results from smoothing of surface electronic charge density¹². Expansion of ~20% of the first Ni layer at an S saturation coverage could significantly increase the electronic charge density corrugation and thus

the surface potential corrugation. Although no measurement exists on how this first Ni layer of Ni(110) expands as S coverage increases, experiment on S/Ni(100) system seems to indicate that the substrate expands linearly as a function of the S coverage¹³. In the case of Ni(110), we suspect that considerable first Ni layer expansion can occur at low S coverages so that a large number of CO adsorption sites are affected. Despite some controversy¹⁴, it was suggested that for a S/Ni(100) surface each S atom may have effectively poisoned 10Ni atoms^{10,15}. Theoretical calculation on S/Rh(100) also indicated that the effect of S-Ni interaction can be extended to the next nearest neighbors of the S adsorption site (hollow site) through the local density of electronic state at the Fermi energy¹⁶. For S/Ni(110), if we assume that the local Ni expansion induced by S is independent of coverage, then this distortion has to be relaxed by the nearby Ni atoms. Consequently, it is possible that one adsorbed S atom can affect its nearest four and the next nearest neighbor eight Ni atoms. With this picture in mind, a 3% S coverage could have affected more than 30% of the Ni(110) surface. With CO diffusing on such a modified, more corrugated Ni(110) surface, the CO diffusion energy barrier can be effectively higher, as indicated by our measurement.

The sudden jump in the diffusion activation energy with coverage of S could be due to the fact that a critical coverage of S can effectively induce a surface corrugation change over the entire surface. Whether this is true or not can be checked by a dynamic LEED analysis as a function of S coverage.

b) Defects Effect

The data (f) and (g) in Fig. 1 were taken on surfaces with different defect densities for CO coverage $\theta=0.98$. In the case of (f), a Ni(110) surface was

flash-annealed at 1120K for < 1min followed by a cooling down procedure described in section B. In the case of (g), a normally prepared Ni(110) surface, which was annealed at 1120K for 10 min, was Ar⁺ sputtered for 5min.

Comparing to the normally prepared surface (a), CO diffusions in cases (f) and (g) are significantly faster. However, the diffusion activation energies remain the same as that of a normal surface within the experimental error (Table 1).

In order to explain the CO diffusion data with defects on the Ni(110) surface, we need to know the defects density on the surfaces. Although experiment showed that a saturation density of defects created by Ar⁺ sputtering exists¹⁷, no absolute knowledge of this value is known since the techniques that have been employed in measuring this quantity can only provide relative information. In principle, the annealing process should remove the surface defects and lead to a microscopic smooth and flat surface as long as the annealing temperature is lower than the surface roughening temperature and the annealing time is long enough¹⁸. However, the healing speed and its temperature dependence are seldom known. In the literature, annealing temperatures in the range of 1000-1300K for preparing a Ni(110) surface have been often reported without providing the annealing time¹⁹, not to speak about the residual defect density. For Pt(110), which has a surface roughening temperature of 1080K²⁰, it has been found that as much as 40min annealing at 1000K is required to remove the defects and create a smooth flat surface (judging by the X-ray diffraction pattern to have an average step spacing of 500Å)²¹. In the case of Ni(110), the surface roughening has been studied by high resolution LEED and a roughening transition temperature of 1300K is found²². Annealing Ni(110) at 1120K should eventually lead to a microscopically smooth surface. The annealing time at this temperature can be estimated by the power law of the terrace growth kinetics²³,

$$L = A(T)t^n,$$

where L is the dimension of terrace, $A(T)$ is a temperature dependent rate coefficient, and the exponent n is found to be $\sim \frac{1}{2}$ by at high temperatures²¹.

Knowing that $A(T)$ is proportional to the self-diffusion coefficient $D(T)$ and $D(T \sim 1120\text{K}) \sim 3 \times 10^{-6} \text{ cm}^2/\text{sec}$ for Ni(110)²⁴, and $D(T \sim 1000\text{K}) \sim 5 \times 10^{-7} \text{ cm}^2/\text{sec}$ for Pt(110)²⁵, the annealing time for getting a smooth Ni(110) surface is then in the order of minutes at 1120K. From the above argument, we conclude that the defect densities increases as we go from (a) to (f) and to (g).

Although in the surface treatment of (a) and (f), two processes could happen simultaneously during surface annealing, one being the healing of defects, the other being the segregation of S atoms to the surface with time, we could safely exclude the possible S impurity effect since it has an extremely low surface density (<0.3%). Knowing that there were increasing surface defect densities for surfaces (a), (f), and (g), our experimental results show unambiguously that CO diffusion along $[1\bar{1}0]$ on Ni(110) becomes faster with a larger defect density. Similar behavior were also observed for low CO coverages and for CO diffusion along $[001]$. These results are very astonishing and puzzling. Intuitively, one would expect CO diffusion to become slower as the defect density increases since CO molecules adsorbed on the defect sites have a larger binding energy than those on normal sites and may diffuse slower on one hand and block diffusion of the others on the other hand. Theoretical calculations based on lattice gas models for adsorbate diffusion on an inhomogeneous surface also predict that the diffusion coefficient decreases with increasing inhomogeneity³. However, both the intuition and the theory have

assumed that the defect sites has changed only the diffusion activation energy but not the preexponential factor. The probable existence of a compensation effect between the activation energy and the preexponential factor, namely the larger the activation energy the larger the preexponential factor, may lead to faster diffusion on defect sites. However, this does not explain our observation either because the relative low defect density compared to normal site density indicates that the CO diffusion on surfaces with low density of defects should correspond to normal-site diffusion. The observed invariance of the CO diffusion activation energy is a further support to this assertion.

No similar study has been carried out on any other systems and a general conclusion is very difficult to reach at this moment. It can be shown (Appendix) that in the usual lattice gas models, even assuming that the interactions between CO molecules depends on whether they are adsorbed on normal sites or defect sites, an appreciable change in the diffusion coefficient is not possible. Therefore, new mechanism has to be responsible for our observation.

One possible mechanism is long jumps over multiple lattice distance initiated by CO filled vacancies. As an experimental fact, it is known that a second layer CO molecule cannot be formed on top of the chemical adsorbed first CO layer. Therefore, it is very possible that a CO adsorbed in a vacancy can smooth the potential at that site for other CO. Unlike CO adsorbed on normal site, a CO molecule adsorbed in a vacancy even geometrically may be less effective in blocking motion of other CO molecules due to the lowered latitude. As a result, a CO molecule adsorbed on a normal site near the vacancy can jump across this vacancy and land at the next normal site. Such long jumps can increase the diffusion coefficient through its quadratic dependence on the average jumping length but will not change the diffusion

activation energy. As long as enough CO molecules are there on the surface to fill the vacancies, no coverage dependence should be expected for CO diffusion on surfaces with defects. Therefore, all our results have been consistently explained. The details for this model to work certainly depend on the exact surface morphology. There are experimental evidence that both Ni adatoms and vacancies can exist on a sputtered Ni(110) surface. Furthermore, a vacancy clustering model has been proposed to interpret the low temperature (~340K) thermal annealing results¹⁷. With this larger vacancy structure, the average distance of long jumps can be much longer. Then, to explain our observation, only a low density of vacancies is needed.

c) CO Diffusion on Stepped Surface

Study of CO diffusion has also been carried out on a stepped Ni(110) surface. The sample we used has a step density of ~1 step/40 terrace atoms and a step direction parallel to the [001] direction. In Fig. 2, we have plotted the CO diffusion coefficient along $[1\bar{1}0]$ as a function of reciprocal temperature for the stepped surface (a) and the good surface (b) at $\theta=0.98$. It is seen that the CO diffusion activation energy on the stepped surface is much higher than that on the good surface (5kcal/mol vs. 2kcal/mol). This is a clear evidence that diffusion along $[1\bar{1}0]$ has been affected by steps. However, detailed understanding is not straight forward. From the discussion in Chapter II, with the interaction between the steps and the terrace neglected the diffusion coefficient on a surface with steps is given by

$$\frac{1}{D} = \frac{1}{D_s'} + \frac{1}{D_t'}$$

with D_s' denoting the diffusion coefficient when the duration time of the adparticle on terraces is negligible and D_t' denoting the diffusion coefficient when the duration time of the adparticle on steps is negligible respectively. The overall diffusion coefficient D is expected from the above relation to be smaller than the terrace diffusion coefficient D_t' (By definition, $D_s' < D_t'$). Opposite to this anticipation, the diffusion data shown in Fig. 2 showed diffusion on stepped surface is faster than that on good surface in the high temperature region. Without knowing the true morphology of such a stepped surface we cannot pin down the reason for the observed phenomenon. However, the results can be easily understood if we assume that a significant large number of point defects also exist on the terrace region of the stepped surface.

The coverage dependent CO diffusion activation energies and the preexponential factors on the stepped surface are shown in Fig. 3. The activation energy of CO diffusion along [001] direction (parallel to the steps) is not affected by the steps as compared with that on a good surface (Fig. 4 in Chapter V). However, the preexponential factors are larger than that on a good surface. In the $[1\bar{1}0]$ direction (perpendicular to the steps), both the CO diffusion activation energy and the preexponential factor are affected by the steps significantly. From the discussion in Chapter II, the invariance of CO diffusion activation energy along [001] on the stepped Ni(110) is a consequence of the relatively low step density and the preexponential factor change is a consequence of possible presence of point defects associated on the stepped surface. For diffusion perpendicular to the steps, i.e., along $[1\bar{1}0]$, the

difference in the activation energies associated with terrace sites and step sites is very important. Using Eq. (28) of Chapter II,

$$\gamma = N^2 \exp [(E_{\text{diff}}(\text{terrace}) - E_{\text{diff}}(\text{step}))/k_B T] \ll 1,$$

as the condition for steps to dominate diffusion, we find that $N \leq 70$ if the energy difference $E_{\text{diff}}(\text{terrace}) - E_{\text{diff}}(\text{step})$ is taken as ~ 3 kcal/mol. That $N \sim 40$

on the stepped surface we used is in agreement with the step dominated diffusion picture.

In summary, we have reported a CO diffusion study on Ni(110) to observe the effects of impurities and defects. The results on S impurities can be understood through surface modification induced by adsorption of S. The defect effect on CO diffusion is more difficult to understand: first, we do not have a good description of defects and defect densities on Ni(110); and second, an intuitive thinking leads to results opposite to observations. We propose a vacancy-filled model that lead to long jumps in diffusion to explain the observations. Results on the effect of steps on CO/Ni(110) show that steps can dominate diffusion if they are perpendicular to the diffusion direction.

Appendix

In order to show that the observed defect effect on CO diffusion on Ni(110) cannot be a thermodynamic result, we use the expression for coverage-dependent diffusion coefficient from Chapter II

$$D(\theta) = \nu a^2 S(\theta) \exp(-E_a/k_B T) \exp(\mu(\theta)/k_B T) \frac{1}{\theta} \left(\frac{\partial(\mu/k_B T)}{\partial \ln \theta} \right)_T,$$

where ν is the trial frequency, a the lattice constant, E_a the activation energy at zero coverage. The quantity $S(\theta)$ and chemical potential $\mu(\theta)$ will be discussed in this appendix. Now we have two kind of sites, normal sites and defect sites (ignoring the differences among adatom sites, vacancy site, and double vacancy sites, and so on) on the Ni(110) surface. The adsorption of CO on these two kinds of sites resulted in different binding energies, E_D on defect sites and E_N on normal sites. Using

$$a = \exp(E_N/k_B T),$$

and

$$b = \exp(E_D/k_B T),$$

we can write down the free energy for a noninteracting CO adlayer

$$\exp(-\beta F) = Z = \sum_{n=0}^{N_d} \frac{N_d!}{n!(N_d-n)!} \frac{N_t!}{(N-n)!(N_t-N+n)!} a^{N-n} b^n,$$

where N_t is the number of normal sites, N_d the number of defect sites, N the total number of CO molecules adsorbed on the surface, and n the number of CO molecules adsorbed on the defect sites. There is no exact way to carry out this summation. However, we can simply take the most probable configuration of n without introducing too much error. Let the first order derivative of the quantity within the summation symbol with respect to n be zero, we obtain an equation for the most probable n ,

$$\frac{(N_d - n)(N - n)}{n(N_t - N + n)} = \frac{a}{b}$$

If the interaction between the CO molecules comes only from nearest neighbors and can be treated as perturbation and the mean field approximation is employed, the free energy for an interacting system can be expressed as

$$\exp(-\beta F) = Z = \frac{N_d!}{n!(N_d - n)!} \frac{N_t!}{(N - n)!(N_t - N + n)!} a^{N - n} b^n \\ * \exp(-N_{tt} \epsilon_{tt} / k_B T) \exp(-N_{dt} \epsilon_{dt} / k_B T)$$

where N_{tt} is the number of pairs of nearest neighbor CO's on the good sites, ϵ_{tt} the corresponding CO-CO interaction; N_{dt} is the number of pairs of nearest neighbor CO's with one CO on good site and other on defect site, ϵ_{dt} the corresponding CO-CO interaction. In the mean field approximation (see Ref. 19a in Chapter II),

$$N_{tt} = (N - n)^2 / N_t$$

$$N_{dt} = (N - n)n / N_t$$

The chemical potential will be given by

$$\begin{aligned} \mu/kT &= \frac{\partial \beta F}{\partial N} \\ &= \left(1 - \frac{\partial n}{\partial N}\right) \ln \frac{N-n}{N_t - N + n} - \ln a + \frac{1}{N_t} \left[(N-n) \frac{2\varepsilon_{tt}}{k_B T} + n \frac{\varepsilon_{dt}}{k_B T} \right] \\ &\quad + \frac{1}{N_t} \left[(N-2n) \frac{\varepsilon_{dt}}{k_B T} - (N-n) \frac{2\varepsilon_{tt}}{k_B T} \right] \frac{\partial n}{\partial N} \end{aligned}$$

Expressing this in terms of coverages, we have

$$\begin{aligned} \mu/kT &= \left(1 + \frac{\partial \theta_d}{\partial \theta}\right) \ln \frac{\theta - \theta_d}{\Theta_t - \theta - \theta_d} - \ln a + \\ &\quad + \frac{1}{\Theta_t} \left[(\theta - \theta_d) \frac{2\varepsilon_{tt}}{k_B T} + \theta_d \frac{\varepsilon_{dt}}{k_B T} \right] \\ &\quad + \frac{1}{\Theta_t} \left[(\theta - 2\theta_d) \frac{\varepsilon_{dt}}{k_B T} - (\theta - \theta_d) \frac{2\varepsilon_{tt}}{k_B T} \right] \frac{\partial \theta_d}{\partial \theta} \end{aligned}$$

where Θ_t is the percentage of the normal sites on the surface, θ the CO coverage and θ_d the CO coverage on defect sites. The

thermodynamic factor $\left(\frac{\partial(\mu/k_B T)}{\partial \ln \theta}\right)_T$ can then be found from the above

expression and is involved with first and second derivatives of θ_d with respect

to θ . The defect associated contribution to the diffusion coefficient is related to θ_d and its derivatives. However, with a reasonable difference in the binding

energy for CO on defect and normal sites, a ratio of 10-1000 can be expected

for b/a . In this range, n is almost equal to the defect sites. Therefore, the

derivatives of θ_d are very small and their contribution to the diffusion coefficient

negligible. Numerical calculations show that 10% increase in D could be

expected from 5% defect on the surface. This is too small to explain our experimental results.

References

- ¹ See a recent review by R. Gomer, Rep. Prog. Phys. **53**, 917(1990).
- ² V. P. Zhdanov, Surf. Sci. **194**, 1(1988); Phys. Lett. A **137**, 225(1989).
- ³ C. H. Mak, H. C. Anderson, S. M. George, J. Chem. Phys. **88**, 4052(1988); V. Pereyra, G. Zgrablich and V. P. Zhdanov, Langmuir **6**, 691(1990); F. Bulnes, J. L. Riccardo, G. Zgrablich and V. Pereyra, Surf. Sci. **260**, 304(1992).
- ⁴ For example, inconsistent results have been obtained by different authors on the following systems: CO/Ni(111), X. D. Zhu, Th. Rasing, and Y. R. Shen, Phys. Rev. Lett. **61**, 2883(1988); T. S. Lin, H.-J. Lu, and R. Gomer, Surf. Sci. **234**, 251(1990). H/Ni(100), S. M. George, A. M. Desantolo, and R. B. Hall, Surf. Sci. **159**, L425(1985); D. A. Mullins, B. Roop, and J. M. White, Chem. Phys. Lett. **129**, 511(1986); T.-S. Lin and R. Gomer, Surf. Sci. **255**, 41(1991); X. D. Zhu, A. Lee, and A. Wong, Phys. Rev. Lett. **68**, 1862(1992). CO/Pt(111), B. Poelsema, L. K. Verherij, and G. Comsa, Phys. Rev. Lett. **49**, 1731(1982); J. E. Reutt-Robey, D. J. Doren, Y. J. Chabal, and S. B. Christman, Phys. Rev. Lett. **61**, 2778(1988); V. J. Kwasniewski, and L. D. Schmidt, Surf. Sci. **274**, 329(1992).
- ⁵ M. C. Tringides, J. Chem. Phys. **92**, 2077(1990); M. C. Tringides and R. Gomer, Surf. Sci. **265**, 283(1992).
- ⁶ W. Daum, Surf. Sci. **182**, 521(1987).
- ⁷ M. Blaszcyszyn, R. Blaszcyszyn, R. Meclowski, A. J. Melmed and T. E. Madey, Surf. Sci. **131**, 433(1983).
- ⁸ Xu-dong Xiao, Yuanlin Xie and Y. R. Shen, Surf. Sci. **271**, 295(1992).
- ⁹ R. A. Dalla Betta, A. G. Piken and M. Shelef, J. Catalysis **40**, 173(1975); C. H. Bartholomew, G. D. Weatherbee and G. A. Jarvi, J. Catalysis **60**, 257(1979);

- M. A. Vannice, *Catalysis Rev. Sci. Eng.* **14**, 153(1976); R. D. Kelley and D. W. Goodman, in: *Chemical Physics of Solid Surfaces and Heterogeneous Catalysis*, Vol. 4, Eds. D. A. King and D. P. Woodruff (Elsevier, Amsterdam, 1982)p427.
- ¹⁰ M. P. Kiskinova, *Surf. Sci. Rep.* **8**, 359(1988).
- ¹¹ D. R. Warburton, G. Thornton, D. Norman, C. H. Richardson and R. Mcgrath, *Surf. Sci.* **189/190**, 495(1987); R. Baudoing, E. Blanc, C. Gaubert and Y. Gauthier, *Surf. Sci.* **128**, 22(1983).
- ¹² M. W. Finnis, and V. Heine, *J. Phys. F4*, L37(1974).
- ¹³ W. Oed, U. Starke, K. Heinz, K. Muller and J. B. Pendry, *Surf. Sci.* **251/252**, 488(1991).
- ¹⁴ R. J. Madix, Michael Thornburg and S.-B. Lee, *Surf. Sci.* **133**, L447(1983).
- ¹⁵ Maya Kiskinova and D. Wayne Goodman, *Surf. Sci.* **108**, 64(1981).
- ¹⁶ P. J. Feibelman, *Annu. Rev. Phys. Chem.* **40**, 261(1989); P. J. Feibelman and D. R. Hamann, *Phys. rev. Lett.* **52**, 61(1984); *Surf. Sci.* **149**, 48(1985).
- ¹⁷ L. K. Verheij, J. A. Van Den Berg and D. G. Armour, *Surf. Sci.* **122**, 216(1982).
- ¹⁸ J. D. Weeks and G. H. Gilmer, *Adv. Chem. Phys.* **40**, 157(1979).
- ¹⁹ For examples, S. M. Yalisove, W. R. Graham, E. D. Adams, M. Copel and T. Gustafsson, *Surf. Sci.* **171**, 400(1986); B. Voigtander, D. Bruchmann, S. Lehwald and H. Ibach, *Surf. Sci.* **225**, 151(1990); D. R. Huntley, *Surf. Sci.* **240**, 13(1990).
- ²⁰ I. K. Robinson, E. Vlieg, and K. Kern, *Phys. Rev. Lett.* **63**, 2578(1989).
- ²¹ Klaus Kern, Ian K. Robinson and Elias Vlieg, *Surf. Sci.* **261**, 118(1992).
- ²² E. H. Conrad, *Prog. Surf. Sci.* **39**, 65(1992); Y. Cao, and E. H. Conrad, *Phys. Rev. Lett.* **64**, 447(1990).

- ²³ I. M. Lifshitz, Sov. Phys. JETP **15**, 939(1962); S. M. Allen and J. W. Cahn, Acta Metall. **27**, 1085(1979).
- ²⁴ H. P. Bonzel and E. E. Latta, Surf. Sci. **76**, 275(1978).
- ²⁵ D. W. Basset and P. R. Webber, Surf. Sci. **70**, 520(1978).

Table 1. CO Diffusion parameters of the Arrhenius fits from a number of differently treated Ni(110) surfaces.

Labels	Sample Conditions	Activation energy E_d (kcal/mol)	Preexponential Factor D_0 (cm ² /sec)
(a)	Clean, Annealed for 10 min at 1120K	2.2 ± 0.4	$10^{-7.7 \pm 0.5}$
(b)	1% S	1.9 ± 0.4	$10^{-8.6 \pm 0.5}$
(c)	3% S	5.9 ± 0.4	$10^{-4.1 \pm 0.5}$
(d)	5% S	6.2 ± 0.3	$10^{-4.0 \pm 0.4}$
(e)	15% S	7.8 ± 0.7	$10^{-2.9 \pm 0.7}$
(f)	Clean, Annealed for <1 min at 1120K	1.9 ± 0.2	$10^{-7.8 \pm 0.3}$
(g)	Clean, Annealed for 10 min at 1120K then Ar ⁺ Sputtered for 5 min	2.4 ± 0.3	$10^{-6.5 \pm 0.5}$

Figure Captions

Figure 1: CO Diffusion coefficient along $[1\bar{1}0]$ as a function of reciprocal temperature for a number of differently treated Ni(110) surfaces at coverage $\theta=0.98$: (a) normally prepared, (b) 1% S, (c) 3% S, (d) 5% S, (e) 15% S contaminated, (f) flash-annealed, (g) normally prepared followed by 5min Ar^+ sputtering.

Figure 2: CO diffusion coefficient along $[1\bar{1}0]$ as a function of reciprocal temperature at coverage $\theta=0.98$ on (a) good surface and (b) stepped surface. Both surfaces have been flash-annealed after 30 minutes Ar^+ sputtering. The stepped surface has a step density of 1step/40 terrace atoms and a direction perpendicular to $[1\bar{1}0]$.

Figure 3: Diffusion activation energies and preexponential factors as a function of coverage along (a) $[1\bar{1}0]$ and (b) $[001]$ for CO on the stepped Ni(110) surface.

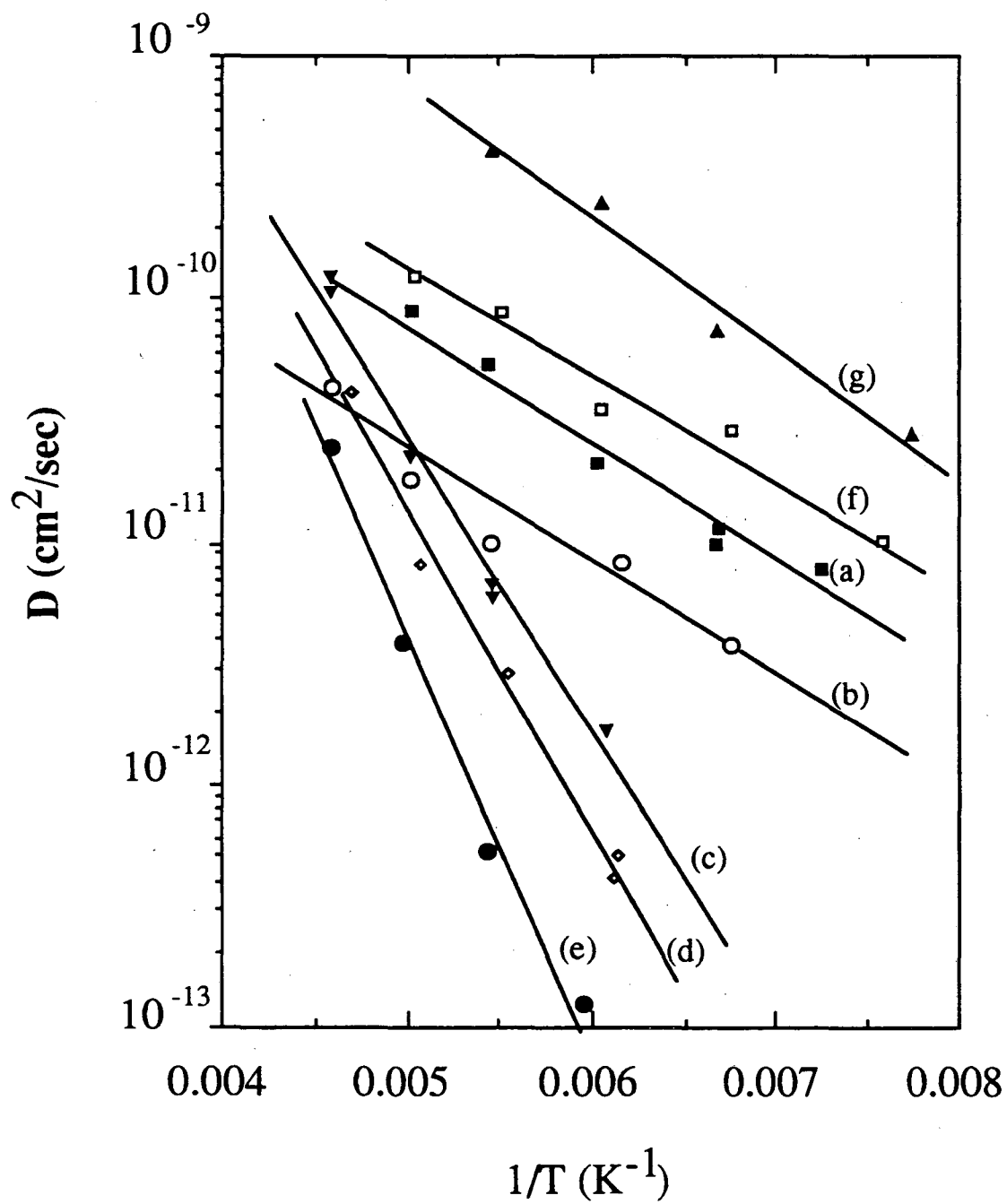


Figure 1

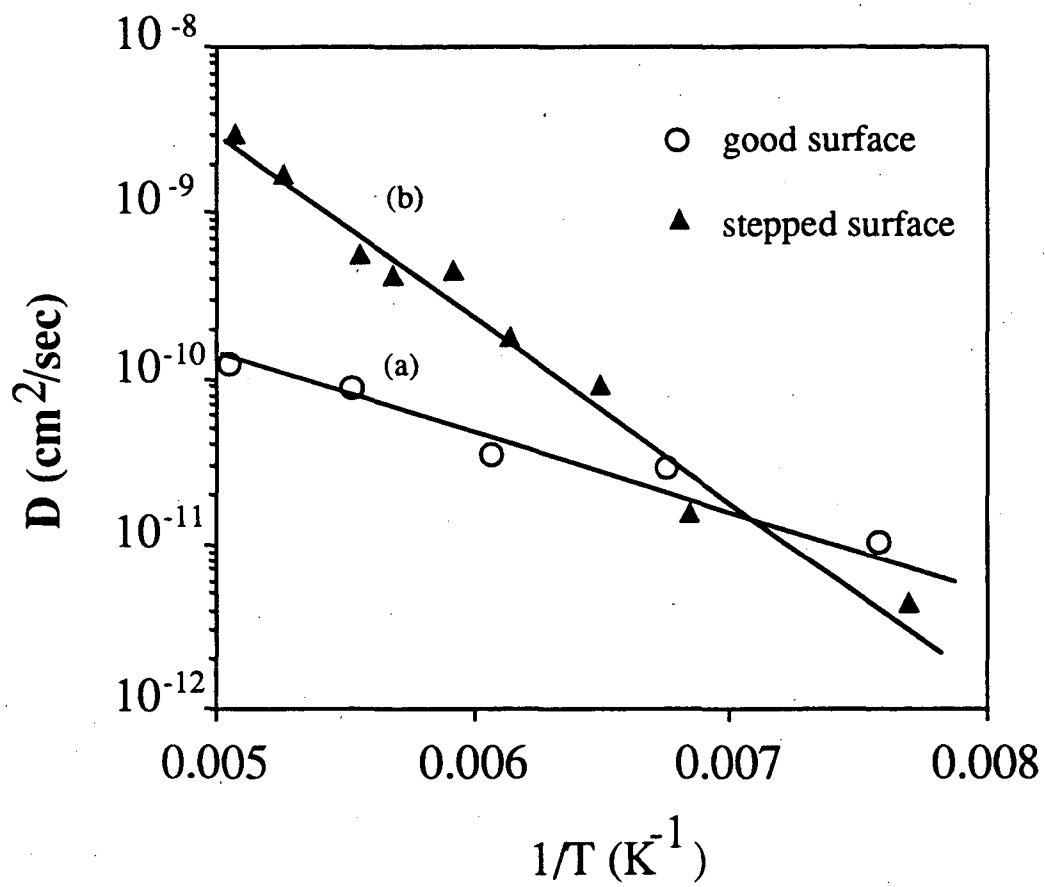


Figure 2

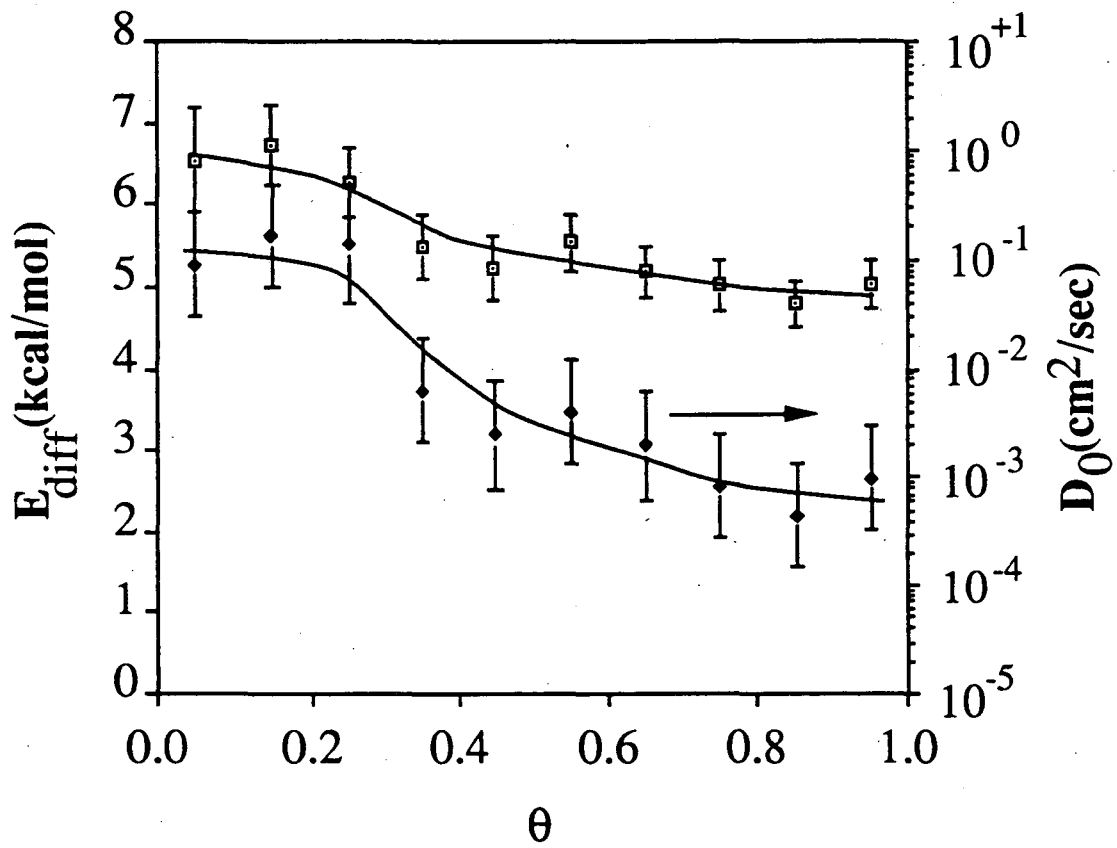


Figure 3(a)

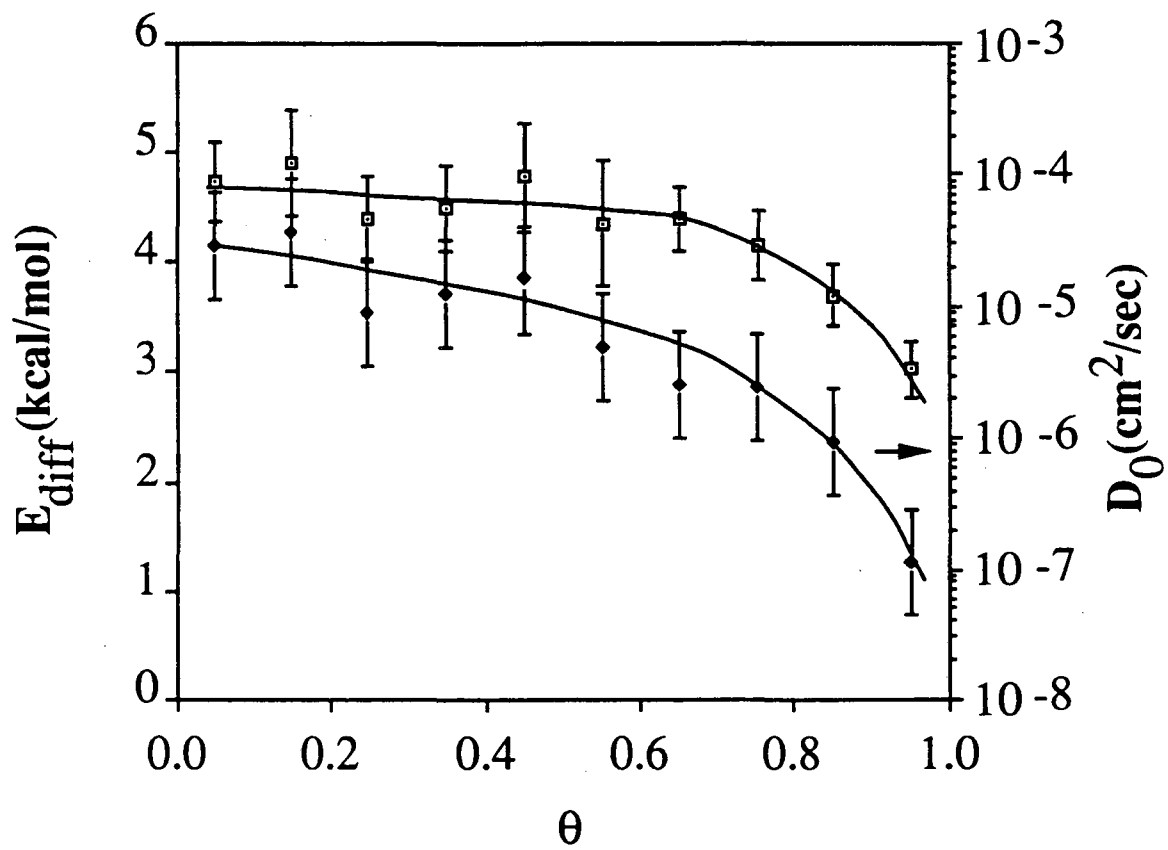


Figure 3(b)

VII. Future Prospects

In the previous chapters many aspects of surface diffusion have been discussed. However, surface diffusion is not yet a mature field and there are still many problems to solve. The important issues in surface diffusion studies are: First, the existing data measured by different methods often do not overlap due to their limited dynamic ranges and are often contradictory. The optical diffraction method presented in this thesis with its extremely large dynamic range should contribute in resolving this problem to a great extent. Second, the systems that have been measured are often limited to adsorbate diffusion on refractory metal surfaces. Diffusion on soft metal surfaces and semiconductor surfaces should be explored complementarily. Third, theoretical studies of surface diffusion are very limited, especially for chemical diffusion. Models that can account for the adsorbate-adsorbate interaction in more sophisticated manner than the lattice gas model must be developed. The role of the thermodynamic factor $\left(\frac{\partial(\mu/k_B T)}{\partial \ln \theta}\right)_T$ in surface diffusion in connection with adlayer properties has to be further investigated. Only with substantial advance in theory, can a variety of experimental results be understood.

Related with the first issue, the study of effects of defects and impurities presented in Chapter VI has revealed the importance of surface characterization. Since diffusion is very sensitive to the fine conditions of a surface, caution has to be taken when one compares diffusion data for the nominally same surfaces. This may have contributed to the divergence of the existing data in a large degree.

With the S impurity effect on CO diffusion interpreted in terms of S induced surface structure change in Chapter VI, one may wonder whether impurities of oxygen, and hydrogen can have similar effect. Experiment to

reveal the answer for it is currently undergoing in Shen's group. Oxygen has a strong interaction with Ni(110) and presumably will change the structure of Ni(110) to certain extent. On the other hand, hydrogen interacts with Ni(110) less stronger and probably will not affect CO diffusion much.

The observed effect of defects for CO diffusion on Ni(110) is counter-intuitive and can be explained in terms of multiple lattice distance jump assisted by CO filled vacancies. Is this picture general? Experiment on other systems, for example, CO/Pt(110) which resembles CO/Ni(110) in many aspects, can be used to test our proposed model. Along this direction, significant effort in both experiment and theory has to be invested.

Coverage dependence measurements of CO diffusion on low Miller index Ni surfaces have not reached a consistent picture yet. A measurement for CO/Ni(100) with the optical diffraction technique would be helpful in order to eliminate the possible artifacts due to "hole burning" LITD measurement scheme, which is ill defined for coverage dependence studies. Hopefully the new results will support the conclusion from the other two surfaces, namely long range CO-CO interaction does not change the diffusion activation energy. Whether it is generally true that long range interaction does not affect diffusion, systems with other adsorbate and other surfaces should be also investigated. Only with an accumulation of experimental data, can a consistent picture then be built.

Diffusion of adsorbates on semiconductor surfaces are very interesting due to the intrinsic bonding difference between semiconductor surface and metal surface. The covalent bonding in the case of semiconductor presumably provides a much higher potential barrier for adsorbate to overcome in the path of jumping from one well to another. Diffusion of H and K on GaAs(110) is being investigated with the optical diffraction technique. Since the surface

potentials of these two systems have been calculated, direct comparison with experimental results will be possible. In particular, diffusion of K could be very interesting because K might form chains along $[1\bar{1}0]$ on the GaAs(110) surface. Whether K diffuses as a chain or an atom should be an important issue to address. Even if the diffusion occurs via single atom motion, how the K atom detach from one chain and jump over some distance to attach to another chain should enrich our understandings on crystal growth. The anisotropy of the systems again provides us one more degree of freedom.

The last, the optical technique for coverage dependence measurement could be improved with a scheme of simultaneous detection of multi-order diffractions as described in Chapter III. A success in implementing such a scheme could save tremendous time and improve the measurement accuracy.

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