

# Lawrence Berkeley National Laboratory

## Recent Work

### Title

GEOMETRY OF THE LiO<sub>2</sub> RADICAL

### Permalink

<https://escholarship.org/uc/item/26827708>

### Authors

O'Neil, Stephen V.  
Schaefer, Henry F.  
Bender, Charles F.

### Publication Date

1973-06-01

Submitted to Journal of Chemical Physics

LBL-1913  
Preprint c.d

GEOMETRY OF THE  $\text{LiO}_2$  RADICAL

Stephen V. O'Neil and Henry F. Schaefer III  
and Charles F. Bender

June 1973

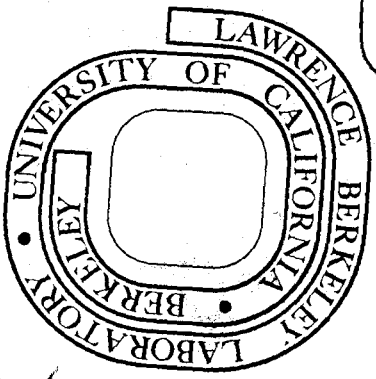
RECEIVED  
LAWRENCE  
RADIATION LABORATORY

JUN 6 1973

LIBRARY AND  
DOCUMENTS SECTION

Prepared for the U. S. Atomic Energy Commission  
under Contract W-7405-ENG-48

**TWO-WEEK LOAN COPY**  
  
This is a Library Circulating Copy  
which may be borrowed for two weeks.  
For a personal retention copy, call  
Tech. Info. Division, Ext. 5545



*34a*

LBL-1913  
c.d

## **DISCLAIMER**

This document was prepared as an account of work sponsored by the United States Government. While this document is believed to contain correct information, neither the United States Government nor any agency thereof, nor the Regents of the University of California, nor any of their employees, makes any warranty, express or implied, or assumes any legal responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by its trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof, or the Regents of the University of California. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof or the Regents of the University of California.

GEOMETRY OF THE  $\text{LiO}_2$  RADICAL\*Stephen V. O'Neil<sup>†</sup> and Henry F. Schaefer III<sup>††</sup>

Department of Chemistry and  
Lawrence Berkeley Laboratory  
University of California  
Berkeley, California 94720

and

Charles F. Bender<sup>‡</sup>

Lawrence Livermore Laboratory and  
Department of Applied Science at Davis  
University of California  
Livermore, California 94550

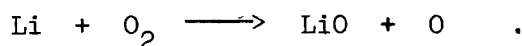
June 1973

## ABSTRACT

Ab initio quantum mechanical calculations have been carried out for the two lowest electronic doublet states of the lithium dioxide molecule. The results are pertinent to possible crossed molecular beam experiments and to matrix isolation spectroscopy. A qualitative discussion of the electronic structure changes accompanying the  $\text{Li} + \text{O}_2$  and  $\text{LiO} + \text{O}$  reactions is given. For the quantitative calculations, a contracted gaussian basis set was used, designated Li (9s 4p/4s 2p), O (9s 5p/4s 3p). For isosceles triangle configurations, the  ${}^2A_2$  state is the electronic ground state, with equilibrium geometry  $r(\text{LiO}) = 1.82 \text{ \AA}$  and  $\theta(\text{O-Li-O}) = 44.5^\circ$ . The  ${}^2B_2$  state is predicted to lie 14 kcal/mole higher with  $r(\text{LiO}) = 1.76 \text{ \AA}$ , and  $\theta(\text{O-Li-O}) = 46.5^\circ$ . For  $C_{\infty v}$  geometry the  ${}^2\Pi$  state bond distances were predicted,  $R(\text{Li-O}) = 1.62 \text{ \AA}$  and  $R(\text{O-O}) = 1.35 \text{ \AA}$ . There appears to be little or no barrier between the  $C_{2v}$  and  $C_{\infty v}$  forms.

INTRODUCTION

Recent developments in the experimental study of chemical reactions using crossed molecular beams have produced an impressive amount of detailed information on the dynamics of an increasing number of interesting reactions.<sup>1</sup> An interesting reaction which has not been studied is



While  $\text{O}_2$  beams are relatively easy to prepare, only within the past several years have reactions involving Li been observed in crossed beams.<sup>2</sup> However, the real reason the  $\text{Li} + \text{O}_2$  reaction has not been studied is the endothermicity involved,  $\sim 37$  kcal/mole.<sup>3</sup> In principle, of course, this endothermicity could be overcome either by giving the reactants excess (relative to thermal energies) kinetic energies or by vibrationally exciting the  $\text{O}_2$  molecules, or by some combination of the two. In practice, however, either of these two routes appears rather difficult. In fact, the exothermic reverse reaction appears a more likely candidate for beam studies, even though both LiO and O would be difficult to prepare in beams. Furthermore, the reverse reaction might be more interesting since the  $v = 0$  through  $v = 12$  vibrational states of  $\text{O}_2$  are energetically accessible.<sup>4</sup>

The dynamics of the  $\text{Li} + \text{O}_2$  and  $\text{LiO} + \text{O}$  reactions will of course depend on the potential energy surfaces which correlate with the reactants. For  $\text{Li}(^2\text{S}_g) + \text{O}_2(^3\Sigma_g^-)$  and  $\text{C}_{\infty v}$  geometries,  $^4\Sigma^-$  and  $^2\Sigma^-$  states of LiOO are possible. For  $\text{C}_s$  geometries  $^4\text{A}''$  and  $^2\text{A}'$  states of  $\text{Li-O-O}$  can arise, and for  $\text{C}_{2v}$  geometries, the pertinent potential surfaces of  $\text{O}'\text{Li-O}$  are  $^4\text{B}_1$  and  $^2\text{B}_1$ . These are the three types of geometries at which a Li atom can approach an  $\text{O}_2$  molecule. For the  $\text{LiO}(^2\Pi) + \text{O}(^3\text{P}_g)$  reaction, a larger number of surfaces are accessible due to the spatial

degeneracy of the reactants. Specifically, for  $C_{\infty v}$  approaches the  ${}^4\Sigma^+$ ,  ${}^4\Sigma^-$ ,  ${}^4\Pi$ ,  ${}^4\Delta$ ,  ${}^2\Sigma^+$ ,  ${}^2\Sigma^-$ ,  ${}^2\Pi$ , and  ${}^2\Delta$  surfaces will be accessible. For general geometry ( $C_s$ ), the pertinent surfaces will be  ${}^4A'$  (3),  ${}^4A''$  (3),  ${}^2A'$  (3), and  ${}^2A''$  (3). As discussed by Herzberg,<sup>5</sup> there is not a unique symmetry-determined correlation between  ${}^2\Pi$  LiO +  ${}^3P$  O and the  $C_{2v}$  electronic state of LiO<sub>2</sub>. There will be 12 such  $C_{2v}$  potential surfaces, and they may be of any of the symmetries  ${}^4A_1$ ,  ${}^4A_2$ ,  ${}^4B_1$ ,  ${}^4B_2$ ,  ${}^2A_1$ ,  ${}^2A_2$ ,  ${}^2B_1$ , and  ${}^2B_2$ . Since these 12 surfaces must correlate with the  $C_s$  surfaces designated above, there will be no more than three  $C_{2v}$  surfaces of the same irreducible representation. The precise correlation between  $C_s$  and  $C_{2v}$  states can only be obtained by solving the electronic Schrödinger equation.

The above discussion shows that the Li + O<sub>2</sub> reaction proceeds on two potential energy surfaces, while the LiO + O reaction can occur on 12 different surfaces. It seems clear that a detailed a priori description of the two reactions would be difficult to obtain. Therefore, in the present work we have set for ourselves a much more modest goal: to learn something about only the lowest two potential surfaces of LiO<sub>2</sub> near their equilibrium geometrical configurations. Such information will of course be qualitatively pertinent to crossed molecular studies. If LiO<sub>2</sub> is significantly bound with respect to LiO + O, one may expect long-lived collision complexes to accompany the reactions. Otherwise the reactions may be expected to proceed in a "direct" fashion, resulting in little forward and backward peaking in the angular distribution.<sup>6</sup>

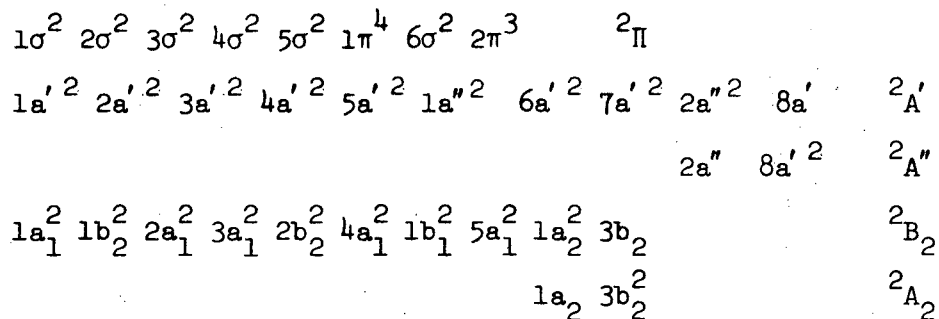
The LiO<sub>2</sub> radical has been observed experimentally by Andrews and coworkers<sup>7</sup> in low temperature oxygen and noble gas matrices. They have concluded that the bonding is ionic, Li<sup>+</sup> O<sub>2</sub><sup>-</sup>, and hence that the proper name for the molecule should be lithium superoxide. In addition Andrews was able to classify the equilibrium

geometry of  $\text{LiO}_2$  as an isosceles triangle, point group  $C_{2v}$ . Finally, they estimated the Li-O bond distance to be 1.77 Å and the  $\begin{array}{c} \text{Li} \\ \diagdown \quad \diagup \\ \text{O} \quad \text{O} \end{array}$  bond angle to be  $44^\circ$ .

The only previous theoretical work on  $\text{LiO}_2$  appears to be that of Billingsley and Trindle.<sup>8</sup> They used a "mixed basis set", with simple integrals being evaluated over Slater functions, and the more difficult integrals by gaussian expansions of the Slater functions. Constraining the molecule to be of  $C_{2v}$  symmetry, Billingsley and Trindle<sup>8</sup> obtained good agreement with the experimentally estimated geometry.<sup>7</sup> However, they predicted the equilibrium geometry not to be a  $C_{2v}$  but rather a  $C_s$  structure with  $\begin{array}{c} \text{Li} \\ \diagdown \quad \diagup \\ \text{O} \quad \text{O} \end{array}$  bond angle of about  $135^\circ$ . This type of geometry is qualitatively similar to that predicted earlier for the  $\text{HO}_2$  radical.<sup>9</sup> For  $\text{LiO}_2$ , however, this disagreement between calculation and experiment is disturbing. Billingsley and Trindle suggest several reasons why the matrix-isolation identification of the molecule as  $C_{2v}$  at equilibrium might be incorrect.

### LOW-LYING ELECTRONIC STATES OF LiO<sub>2</sub>

If one assumes the electronic ground state of the lithium superoxide molecule to have the structure Li<sup>+</sup>O<sub>2</sub><sup>-</sup>, then the C<sub>∞v</sub> symmetry will be <sup>2</sup>Π, the C<sub>s</sub> symmetry either <sup>2</sup>A' or <sup>2</sup>A'', and the C<sub>2v</sub> symmetry either <sup>2</sup>A<sub>2</sub> or <sup>2</sup>B<sub>2</sub>. The corresponding electron configurations will be



It is interesting to note that for C<sub>∞v</sub> and C<sub>2v</sub> approaches, Li(<sup>2</sup>S<sub>g</sub>) + O<sub>2</sub>(<sup>3</sup>Σ<sub>g</sub><sup>-</sup>) does not correlate with the assumed electronic ground state of LiO<sub>2</sub>. This is because, as discussed in the introduction, the ground state reactants correlate with the <sup>4</sup>Σ<sup>-</sup> and <sup>2</sup>Σ<sup>-</sup> states of linear LiO<sub>2</sub> and the <sup>4</sup>B<sub>1</sub> and <sup>2</sup>B<sub>1</sub> states of the isosceles molecule. However, it is clear that essentially all Li + O<sub>2</sub> collisions will occur for C<sub>s</sub> geometries, and Li(<sup>2</sup>S<sub>g</sub>) + O<sub>2</sub>(<sup>3</sup>Σ<sub>g</sub><sup>-</sup>) does correlate with the <sup>2</sup>A'' state, which should be either the ground or first excited state in the ionic picture. For the reverse reaction LiO + O, the large number of accessible surfaces makes possible the correlation with either of the two lowest states of LiO<sub>2</sub> for all three point groups.

One would like to be able to predict the geometry of LiO<sub>2</sub> on the basis of Walsh-like arguments.<sup>10</sup> Although it might appear that a Walsh diagram for AB<sub>2</sub> triatomics would be useful for this purpose, the usefulness is limited. The diagram can be used to predict that for C<sub>2v</sub> geometries the <sup>2</sup>B<sub>2</sub> state should lie slightly below the <sup>2</sup>A<sub>2</sub> state. This is done by noting that, of the a<sub>2</sub> and b<sub>2</sub> components of the 1π<sub>g</sub> orbital (which is triply occupied in O<sub>2</sub><sup>-</sup>), the a<sub>2</sub> lies



lower for  $C_{2v}$  geometries. However, the absence of a doubly occupied 2s orbital in the Li atom makes Walsh's diagram otherwise inapplicable. That is, it appears that  $BO_2$  is the simplest dioxide molecule for which Walsh's diagram is applicable. Taken literally, the  $AB_2$  diagram predicts  $LiO_2$  (13 valence electrons) to be linear, of  $D_{\infty h}$  symmetry. A perhaps more reasonable possibility is to use the HAB Walsh diagram, neglecting the core 1s orbital of lithium. In this case  $LiO_2$  is predicted to have the same geometry as  $HO_2$ ,<sup>9</sup> about  $105^\circ$ . As is the case for  $HO_2$ , Walsh's diagram predicts the  ${}^2A''$  state of  $LiO_2$  lie below the  ${}^2A'$  state. In this regard it should be noted that Gole and Hayes<sup>11</sup> have predicted the  ${}^2A'$  state of  $HO_2$  to lie only 17 kcal above the  ${}^2A''$  ground state.

### DETAILS OF THE CALCULATIONS

A basis set of contracted gaussian functions was employed in the present work. For lithium, the (9s 4p) primitive gaussian basis of Huzinaga<sup>12</sup> and Williams<sup>13</sup> was contracted to (4s 2p) in the spirit of Dunning's work.<sup>14</sup> For oxygen atom, the basis used was the Huzinaga-Dunning (9s 5p/4s 3p) set. Although we frequently use the less flexible 2p contraction of oxygen p functions, in the present work the 3p set was used to provide a better description of possible ionic  $\text{Li}^+ \text{O}_2^-$  bonding. In summary, then 69 primitive gaussian functions were contracted to 36 functions.

Open-shell self-consistent-field calculations<sup>15</sup> were carried out for the lowest  ${}^2A'$  and  ${}^2A''$  states of  $\text{LiO}_2$ . In employing only a single plane of symmetry in constructing molecular orbitals from the chosen basis functions, we have exploited only that element of symmetry which is common to the three point groups  $C_{\infty v}$ ,  $C_s$ , and  $C_{2v}$ . Within the single configuration SCF framework,<sup>16</sup> this is the only way to avoid discontinuities in the calculated potential energy surface. Recall that for  $C_{\infty v}$  geometries the  ${}^2A'$  and  ${}^2A''$  states are the degenerate components of the  ${}^2\Pi$  state, while for  $C_{2v}$  geometries  ${}^2A'$  becomes  ${}^2B_2$  and  ${}^2A''$  becomes  ${}^2A_2$ . However, when the individual molecular orbitals are forced to have full  $C_{2v}$  symmetry, the  ${}^2B_2$  energy is calculated to lie  $\sim 0.003$  hartrees = 2 kcal/mole above the energy obtained imposing only  $C_s$  symmetry. This perhaps somewhat surprising result is due to the fact that, for the type of wave function chosen, the spatial symmetry of the electronic state being described represents a (slight) constraint on the wave function. Removal of this constraint yields a slightly lower restricted Hartree-Fock energy.

## GEOMETRIES

Assuming the molecule to have an isosceles triangle structure, the SCF energy of the  ${}^2B_2$  and  ${}^2A_2$  states was first minimized with respect to the bond distance  $R(\text{Li-O})$  and bond angle  $\theta$  ( $\text{O-Li-O}$ ). Next a  $C_{\infty v}$  geometry was assumed and the energy minimized with respect to  $R(\text{Li-O})$  and  $R(\text{O-O})$ . As mentioned earlier, the lowest  ${}^2A'$  and  ${}^2A''$  states are degenerate components of the  ${}^2\Pi$  state for  $C_{\infty v}$  geometries. All these results are summarized in Table I. Also included in Table I are the calculations of Billingsley and Trindle<sup>8</sup> and the experimental estimates of Andrews.<sup>7</sup>

The present ab initio self-consistent-field calculations predict the  ${}^2A_2$  state to lie 14 kcal/mole below the  ${}^2B_2$  state. The two states have very similar equilibrium geometries. Both of the above facts are quite analogous to the ab initio predictions of Gole and Hayes<sup>11</sup> for  $\text{HO}_2$ . In fact, the high degree of similarity is surprising since one intuitively suspects that  $\text{LiO}_2$  should be much more ionic than  $\text{HO}_2$  and therefore somewhat different in electronic structure. Billingsley and Trindle<sup>8</sup> have predicted the  ${}^2B_2$  state to lie below the  ${}^2A_2$  state, in apparent disagreement with our more complete calculations. We note that we have adopted the spectroscopic notation of Herzberg,<sup>5</sup> and that our  ${}^2A_2$  ground state wave function correlates with a  ${}^2A''$  wave function, which is anti-symmetric with respect to the plane of the molecule. Our predicted  ${}^2A_2$  ground state geometry is in good qualitative agreement with that estimated from experimental data by Andrews.<sup>7</sup>

The  ${}^2\Pi$  state, constrained to be of  $C_{\infty v}$  geometry is predicted to lie only 1.2 kcal/mole above the  ${}^2A_2$  state. The very small size of this energy difference suggests that the true equilibrium geometry of  $\text{LiO}_2$  may be qualitatively  $\begin{array}{c} \text{Li} \\ \backslash \quad / \\ \text{O-O} \end{array}$ ,

in analogy<sup>9</sup> with  $\text{HO}_2$ . This is in fact the prediction of Billingsley and Trindle.<sup>8</sup> However, Andrews and coworkers have insisted that only an isosceles triangle geometry is consistent with their experimental results. Therefore we carried out the  $C_s$  calculations summarized in Table II. Perhaps the most important result seen in Table II is that the energy of the  $^2A''$  state becomes slightly higher in going from the isosceles triangle to the adjacent  $C_s$  geometry. This seems to establish the  $C_{2v}$  geometry as the true equilibrium. The analogous calculation by Billingsley and Trindle yielded the opposite result. However the miniscule nature of the energy differences involved warns us to be cautious in our interpretation. The proper procedure would be to compute the entire minimum energy path connecting the  $C_{2v}$  and  $C_{\infty v}$  minima.

From the standpoint of the dynamics of the  $\text{Li} + \text{O}_2$  reaction, the most important result found here is that the lowest potential energy surface,  $^2A''$  is rather isotropic. That is, for any Li-O-O angle, the surface is attractive by about the same degree. This result is quite different than that found recently<sup>17</sup> for another attractive surface,  $\text{F} + \text{Li}_2$ . There the  $\text{F} - \text{Li} - \text{Li}$  structure lies 30 kcal/mole higher in energy than  $\text{Li} \begin{array}{c} \text{F} \\ \diagup \quad \diagdown \\ \text{Li} \end{array}$ . However, our  $\text{LiO}_2$  result is analogous to that found by Clementi, Kistenmacher, and Popkie<sup>18</sup> for the  $\text{LiNC} \rightarrow \text{LiCN}$  system. they have used the term "polytopic" to describe the Li - CN bond, in order to stress its equality in energy for substantially different Li - CN orientations.

#### ACKNOWLEDGEMENTS

We thank Professor R. R. Herm for helpful discussions and Dr. J. E. Williams for the use of his  $\text{Li}(^2P)$  basis set.

FOOTNOTES AND REFERENCES

\* Work performed under the auspices of the U. S. Atomic Energy Commission.

† Neshan Zovick Fellow.

†† Alfred P. Sloan Fellow.

‡ M. H. Fellow.

1. For a recent review see J. L. Kinsey, MPT International Review of Science, edited by J. C. Polanyi (Butterworth's, London, 1972), Physical Chemistry Series One, Vol. 9, Chap. 6.
2. D. D. Parrish and R. R. Herm, J. Chem. Phys. 49, 5544 (1968); 51, 5467 (1969); 54, 2518 (1971).
3. A. G. Gaydon, Dissociation Energies and Spectra of Diatomic Molecules (Chapman and Hall, London, 1968).
4. J. T. Vanderslice, E. A. Mason, and W. G. Maisch, J. Chem. Phys. 32, 515 (1960).
5. See page 293 of G. Herzberg, Electronic Spectra of Polyatomic Molecules (Van Nostrand Reinhold, New York, 1966).
6. D. R. Herschbach, in Proceedings of the Conference on Potential Energy Surfaces in Chemistry, W. A. Lester, editor (IBM Research, San Jose, 1971).
7. L. Andrews, J. Chem. Phys. 50, 4288 (1969); D. A. Hatzenbuehler and L. Andrews, J. Chem. Phys. 56, 3398 (1972); L. Andrews and R. R. Smardzewski, J. Chem. Phys. 58, 2258 (1973).
8. F. P. Billingsley II and C. Trindle, J. Phys. Chem. 76, 2995 (1972).
9. D. H. Liskow, H. F. Schaefer, and C. F. Bender, J. Am. Chem. Soc. 93, 6734 (1971). For a verification of this ab initio prediction, see M. E. Jacox and D. E. Milligan, J. Mol. Spectry. 42, 495 (1972).

10. A. D. Walsh, J. Chem. Soc. 1953, 2260, and following five papers.
11. J. L. Gole and E. F. Hayes, J. Chem. Phys. 57, 360 (1972).
12. S. Huzinaga, J. Chem. Phys. 42, 1293 (1965).
13. J. E. Williams, unpublished gaussian basis set for the  $^2P$  state of Li.
14. T. H. Dunning, J. Chem. Phys. 53, 2823 (1970).
15. W. J. Hunt, T. H. Dunning, and W. A. Goddard, Chem. Phys. Letters 3, 606 (1969);  
4, 231 (1969).
16. C. C. J. Roothaan and P. S. Bagus, Methods in Computational Physics 2, 47 (1963).
17. P. K. Pearson, W. J. Hunt, C. F. Bender, and H. F. Schaefer, J. Chem. Phys.  
58, 0000 (1973).
18. E. Clementi, H. Kistenmacher, and H. Popkie, J. Chem. Phys. 58, 2460 (1973).

Table I. Predicted Geometries and Energies of the Lowest Two States  
of  $\text{LiO}_2$ .

State	Total Energy (hartrees)	Relative Energy (kcal/mole)	R(Li-O) (Å)	$\theta$ (O-Li-O) (degrees)	R(O-O) (Å)
$^2B_2$	-157.061 18	14	1.76	46.5	1.39
$^2A_2$	-157.083 51	0.0	1.82	44.5	1.38
$^2\Pi$ (degenerate pair)	-157.081 59	1.2	1.62	-	1.35
Billingsley and Trindle <sup>a</sup>	-156.547	-	1.72	44.4	1.30
Experimental Estimate <sup>b</sup>	-	-	1.77	44.1	1.33

<sup>a</sup>Ref. 8.

<sup>b</sup>Ref. 7.

Table II. Calculations on the  $2A'$  State of  $LiO_2$ . Bond Distances are  
 Tabulated in Bohr Radii (1 Bohr = 0.5292 Å).

Beginning Near the $C_{2v}$ Equilibrium Geometry			
$R(Li-O)$	$R(O-O)$	$\theta(Li-O-O)$	E(hartrees)
3.454	2.600	67.9°	-157.083 489
		75°	-157.083 468
		90°	-157.078 435
		105°	-157.075 214
		120°	-157.074 165
		135°	-157.073 586
		150°	-157.072 849
		180°	-157.071 888
Beginning Near the $C_{\infty v}$ Equilibrium Geometry			
3.05	2.56	180°	-157.081 587
		150°	-157.079 251
		135°	-157.076 691
		120°	-157.074 147
		105°	-157.073 418
		90°	-157.076 309
		75°	-157.07



LEGAL NOTICE

*This report was prepared as an account of work sponsored by the United States Government. Neither the United States nor the United States Atomic Energy Commission, nor any of their employees, nor any of their contractors, subcontractors, or their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness or usefulness of any information, apparatus, product or process disclosed, or represents that its use would not infringe privately owned rights.*

TECHNICAL INFORMATION DIVISION  
LAWRENCE BERKELEY LABORATORY  
UNIVERSITY OF CALIFORNIA  
BERKELEY, CALIFORNIA 94720