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1	Coastal stratocumulus dissipation dependence on initial conditions and
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# ABSTRACT

The impact of initial states and meteorological variables on stratocumulus 14 cloud dissipation time over coastal land is investigated using a Mixed-Layer 15 Model. A large set of realistic initial conditions and forcing parameters are de-16 rived from radiosonde observations and Numerical Weather Prediction model 17 outputs, including: total water mixing ratio and liquid water potential temper-18 ature profiles (within the boundary layer, across the capping inversion, and 19 at 3 km), inversion base height and cloud thickness, large-scale divergence, 20 wind speed, Bowen ratio, sea surface fluxes, sky effective radiative tempera-2 ture, shortwave irradiance above the cloud, and sea level pressure. We study 22 the sensitivity of predicted dissipation time using two analyses. In the first, 23 we simulate 195 cloudy days (all variables co-vary as observed in nature). 24 We caution that simulated predictions correlate only weakly to observations 25 of dissipation time, but the simulation approach is robust and facilitates co-26 variability testing. In the second, a single variable is varied around an ide-27 alized reference case. While both analyses agree in that initial conditions 28 influence dissipation time more than forcing parameters, some results with 29 co-variability differ greatly from the more traditional sensitivity analysis and 30 with previous studies: opposing trends are observed for boundary layer total 31 water mixing ratio and Bowen ratio, and co-variability diminishes the sensi-32 tivity to cloud thickness and inversion height by a factor of five. With co-33 variability, the most important features extending predicted cloud lifetime are 34 (i) initially thicker clouds, higher inversion height, and stronger temperature 35 inversion jumps, and (ii) boundary forcings of lower sky effective radiative 36 temperature. 37

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# 38 1. Introduction

Marine stratocumulus (Sc) clouds cover a large area of the planet at the eastern side of oceans 39 where upwelling keeps the sea colder and at latitudes where the subsiding branch of the Hadley 40 cell pushes the atmospheric boundary layer (ABL) down and caps it with warm air, creating an in-41 version layer that limits the vertical cloud extent. The main physical processes controlling the evo-42 lution of Sc clouds are radiation, turbulence, surface fluxes, entrainment, and precipitation (Wood 43 2012; Stevens 2004; Nieuwstadt and Duynkerke 1996). Sc clouds are maintained by convective 44 turbulent motions, driven mainly by cloud-top radiative cooling that generates sinking plumes and 45 cools the ABL (Lilly 1968). The turbulent motions allow water vapor from the surface to mix and 46 rise up to the condensation level to form a cloud. Near the top of the cloud, there is a complex 47 interface zone exposed to entrainment of air from the free troposphere (Mellado 2017). 48

Marine Sc clouds have a net cooling effect on the planet (Hartmann et al. 1992) and their im-49 pact under climate change conditions is still a matter of research (Zelinka et al. 2017; Bony and 50 Dufresne 2005; Duynkerke and Teixeira 2001). Coastal cities near Sc regions are affected by their 51 presence— not only in terms of climate, but also from the perspective of solar energy genera-52 tion. As solar heating overcomes cloud-top radiative cooling, clouds over land thin during the day, 53 warming the ABL and changing its turbulent structure (Fang et al. 2014). No solar radiation is 54 present during the night, resulting in more effective radiative cooling, which causes cloud growth. 55 During the day, solar electricity generation ramps up as Sc clouds dissipate in the morning hours 56 (Jamaly et al. 2013; Wellby and Engerer 2015) or an extended shortfall of solar generation occurs 57 when Sc clouds persist for the whole day. A better understanding of Sc cloud dissipation can help 58 improve solar energy forecasting in these regions. 59

Different physical processes and meteorological parameters affect the inland coverage of ma-60 rine Sc clouds and the dissipation time over coastal land. For marine clouds, some parameters 61 have been linked to decreased cloudiness: greater sea surface temperatures (SST) (Hanson 1990; 62 Seethala et al. 2015), weaker lower tropospheric stability (LTS) (Klein and Hartmann 1993; Wood 63 and Bretherton 2006; Klein et al. 1995), weaker horizontal cold-air advection, weaker surface wind 64 speed, a moister free-troposphere, and lower sea level pressure (SLP) (Klein et al. 1995; Seethala 65 et al. 2015). Research has been less extensive over coastal land, where earlier dissipation has been 66 linked to smaller Bowen ratio Bo (the ratio between sensible and latent heat fluxes over land) and 67 weaker sea-breeze advection using simple sensitivity analyses (Ghonima et al. 2016; Akyurek and 68 Kleissl 2017). 69

Most factors do not contribute independently to cloud dissipation because they are inter-related 70 with other variables and co-vary in nature. Some variables co-vary due to the nature of physical 71 processes, such as greater SST yielding larger surface heat fluxes. Other variables co-vary be-72 cause their definitions are linked, such as lower SST occurring with stronger LTS. Some variables 73 with opposing trends on cloud dissipation can be correlated themselves, causing the total cloud 74 response to be dominated by only one variable and masking the independent effect of the non-75 dominant variable. This is the case for stronger subsidence, which tends to thin Sc clouds, being 76 correlated with larger LTS, which tends to sustain a thicker cloud— their combined occurrence 77 is linked to larger cloudiness due to dominance by LTS (Myers and Norris 2013; Seethala et al. 78 2015). Such co-variability can arise from seasonal trends, such as decreasing LTS co-occurring 79 with increasing SST, which causes cloudiness to decrease from May/June to August/September in 80 Southern California (Clemesha et al. 2016; Klein and Hartmann 1993). 81

The research-to-date on coastal Sc dissipation presents several gaps: (i) Only a few parameters have been considered, specifically two in Ghonima et al. (2016), while 9 variables have been stud<sup>84</sup> ied for marine Sc in Seethala et al. (2015). (ii) The parameters do not resemble realistic conditions.
<sup>85</sup> Specifically, Ghonima et al. (2016) parameter values for Bowen ratio and sea-breeze advection
<sup>86</sup> were chosen ad-hoc and only for two idealized cases. (iii) As a result of (ii), co-variability effects
<sup>87</sup> have been ignored.

In this work, we conduct a comprehensive analysis of how coastal Sc cloud dissipation time 88 depends on initial conditions and boundary forcings, with consideration of co-variability. We use 89 a large set of 15 variables measured or derived from realistic meteorological conditions for South-90 ern California as input to a two-column Mixed-Layer Model (MLM) to predict dissipation time 91 (Section 2.a). The two columns represent ocean and land conditions and allow the modeling of 92 sea-breeze advection over coastal land. Realistic conditions for the MLM are obtained from ra-93 diosonde profiles, ground measurements, and NWP models for the 2014 to 2017 summer seasons 94 in Southern California (Section 2.b). In Section 3.a, we review the correlations of the variables 95 in the dataset. We perform two analyses in order to consider the impact of co-variability on the 96 predicted dissipation time (Section 3.b). In the first, coastal Sc evolution is simulated for 195 97 cloudy days in which the initial conditions and forcing parameters co-vary as in nature. In the sec-98 ond, simulations are performed in which a single forcing parameter is varied around an idealized, 99 composite reference simulation. Because the different parameters co-vary in nature, the sensitivity 100 to changes in a single parameter will differ between the two approaches: changes in one variable 101 are accompanied by changes in other variables sampled from their climatological co-variation. In 102 this paper, "co-variability" refers to the effects of these secondary correlations on changes in the 103 evolution of the cloud and, in particular, on the time of its breakup. In Section 3.c, we quantify 104 and compare the dissipation time trends obtained by the different approaches. Section 4 contains 105 the conclusions. For an easier reading, a nomenclature is included in Appendix A. 106

## 107 2. Methods

# <sup>108</sup> a. Mixed-Layer Model framework

The MLM used in this study follows the implementation of Ghonima et al. (2016) (refer to 109 Appendix B for further details). In the MLM, the state of the well-mixed ABL is described by 110 three prognostic equations and several parameterizations. The prognostic equations determine the 111 evolution of the thermodynamic state of the ABL, described by: the ABL thickness or inversion 112 base height  $z_i$ , the mean liquid water potential temperature in the ABL  $\theta_l^{BL}$ , and the mean total 113 water content in the ABL  $q_t^{\text{BL}}$ . Cloud thickness h depends on these three variables, where the 114 cloud top height is also  $z_i$  and the cloud base height depends on  $\theta_i^{\text{BL}}$  and  $q_t^{\text{BL}}$ . The growth of  $z_i$ 115 depends on the balance between the entrainment of upper air and large scale subsidence. Changes 116 in  $\theta_l^{\text{BL}}$  depend on the balance of radiation and turbulent fluxes, while the evolution of  $q_t^{\text{BL}}$  is only 117 determined by turbulent fluxes (precipitation is not considered). Consequently, changes in h are 118 affected by all these factors. Aside from the governing equations, parameterizations in the MLM 119 allow quantifying radiation, entrainment of upper air, large-scale subsidence, and turbulent fluxes 120 at the surface and top of the ABL. 121

Since we are interested in cloud dissipation over coastal land, a Eulerian framework is preferred, which introduces advection tendencies in the prognostic equations. To account for this effect, we model the evolution of two columns: one over the ocean and the other over land, as illustrated in Fig. 1. The dominant wind direction in this region is from the ocean to the land, day and night, as a consequence of the North Pacific subtropical high and the continental U.S. thermal low during the summer (Halliwell and Allen 1987). Therefore, advection is considered only for the land column, and the advection terms depend on both ocean and land conditions (Appendix B2).

For this study, we are specifically interested in the effect of different variables on cloud dis-129 sipation. We accordingly select relevant meteorological variables used by the equations and pa-130 rameterizations in the MLM. The variables determine the initial conditions and boundary forcings 131 during the simulation. Initial condition variables include the inversion base height  $z_i$ , as well as 132 the ABL values of liquid water potential temperature  $\theta_l^{BL}$  and total water mixing ratio  $q_t^{BL}$ , that 133 determine the initial cloud thickness h. Thermodynamic values above the ABL are also part of the 134 initial input, including values at 3 km ( $\theta_l^{3km}$  and  $q_t^{3km}$ ) and inversion jumps ( $\Delta_i \theta_l$  and  $\Delta_i q_t$ ), which 135 are assumed to occur over an infinitesimally thin layer (Lilly 1968). 136

The parameters used to determine forcings include large-scale, radiative, and turbulent pro-137 cesses. The large-scale parameters are the ABL large-scale divergence D that determines the 138 subsidence rate at the top of the ABL  $w_{sub}$  (Eq. B2), an average wind speed  $\overline{u}$  for the advec-139 tion tendencies (Appendix B2), and sea-level pressure (SLP). The radiation parameterization has 140 shortwave and longwave components (Appendix B4), where the solar irradiance above the cloud 141  $SW_i$  along with the cloud properties will determine the shortwave net radiation flux. For the long-142 wave component, the sky effective radiative temperature  $T_{sky}$  represents the longwave radiation 143 gain from the sky above the ABL. Lastly, turbulent fluxes exist both at the surface and the top of 144 the ABL (Appendix B5). Surface fluxes depend on the type of column: for the ocean, we prescribe 145 sensible and latent heat fluxes (SHF and LHF) as daily averages, and for the land, we prescribe 146 a Bowen ratio Bo that partitions the sensible and latent heat fluxes. At the top of the ABL, the 147 turbulent fluxes are determined by the inversion jumps  $\Delta_i \theta_l$  and  $\Delta_i q_t$  along with the entrainment 148 rate  $w_e$ . Lastly, entrainment mixes air from the free troposphere into the ABL through turbulence, 149 which results from a complex combination of radiative cooling, evaporative cooling, and wind 150 shear, among other processes (Mellado 2017). In the MLM, the entrainment parameterization de-151 pends on most of the other variables described (Appendix B3). Entrainment acts as a regulating 152

<sup>153</sup> mechanism in response to cloud thickness as it promotes thinning for thicker clouds (Zhu et al. <sup>154</sup> 2005). Entrainment also favors dissipation over land as larger surface fluxes increase  $w_e$  and both <sup>155</sup> surface fluxes and entrainment promote ABL heating, thinning the cloud.

A comment on the choice of the data / modeling tool for the analysis is in order. We use a MLM because it allows a comprehensive sensitivity analysis in an idealized geometry. Conversely, real observations would introduce unknowns, uncertainties, and errors. For example, real 3D topography affects dissipation time due to differential heating and differences in boundary layer height, while the MLM allows removing these effects. Another example is that boundary layer heights are only observed twice per day in reality while the MLM provides a detailed evolution. A detailed discussion of the benefits of the MLM framework is provided in Appendix D.

#### 163 *b. Data*

To study how different variables influence Sc dissipation time, we created a comprehensive 164 dataset with realistic Sc conditions for the years 2014 to 2017 in Southern California. It is impor-165 tant to consider realistic conditions to understand if the influence of a variable is actually observ-166 able / relevant, as well as to understand which variables need to be measured / obtained to improve 167 cloud dissipation predictions. The dataset contains the variables needed in the MLM: inversion 168 height  $z_i$ , liquid water potential temperature  $\theta_l(z)$  and total water mixing ratio  $q_t(z)$  profiles, ABL 169 large-scale divergence D, average wind speed  $\overline{u}$ , Bowen ratio Bo, incoming solar irradiance above 170 the cloud SW<sub>i</sub>, sky effective radiative temperature  $T_{sky}$ , SLP, and ocean sensible and latent heat 171 fluxes (SHF and LHF). May through September months are selected as they constitute the Sc 172 cloud season, and also when the highest solar irradiance is available. The variables are obtained 173 from different sources including radiosondes, Numerical Weather Prediction (NWP) model out-174 puts, observations, and radiative models. Further details are provided in Appendix C. 175

ABL thickness  $z_i$  and profiles of liquid water potential temperature  $\theta_l(z)$  and total water mix-176 ing ratio  $q_t(z)$  are processed from radiosonde data to be compatible with the MLM framework 177 (Appendix C2). We analyze early morning radiosondes at the NKX Miramar Marine Corps Air 178 Station in San Diego, CA. First, the inversion base height  $z_i$  is detected as the starting point of the 179 largest temperature inversion. Next, we check if the state of the ABL could be decoupled using 180 the criterion  $|\theta_{vb} - \theta_{v0}| > 1$  K (Ghate et al. 2015), where  $\theta_{vb}$  and  $\theta_{v0}$  are the virtual potential tem-181 perature at the radiosonde cloud base (the point where the relative humidity (RH) exceeds 95%) 182 and at the surface, respectively. Decoupled cases are discarded because the MLM cannot describe 183 the ABL physics appropriately. For the remaining cloudy cases, the state of the ABL is averaged 184 to create a well-mixed profile described by  $\theta_l^{BL}$  and  $q_t^{BL}$ . Lastly, the free troposphere is included 185 by considering data above the inversion region up to 3 km. While moisture above the inversion is 186 assumed to be constant and represented by an average value of total water mixing ratio  $q_t^{3km}$  and 187 a sharp inversion jump of total water mixing ratio  $\Delta_i q_t$ , the liquid water potential temperature is 188 fitted into a linear profile and represented by the value of the fit at 3 km  $\theta_1^{3km}$  and by the sharp 189 inversion jump  $\Delta_i \theta_l$ . Fig. 2 shows an example of the processed well-mixed ABL structure. Since 190 the initial state is derived from the radiosonde launched at 0300 LST (11 UTC), we use that time 191 to initialize the simulations. Furthermore, we assume that this early state is representative of both 192 ocean and coastal land and thus, start the MLM with the same initial condition for both columns. 193 This assumption is justified as the region experiences a sea breeze day and night and night time 194 surface radiative cooling over land is small due to the Sc cloud cover. 195

The radiation model in the MLM depends on SW<sub>*i*</sub> for the shortwave and  $T_{sky}$  for the longwave radiation fluxes. For obtaining SW<sub>*i*</sub>, we assume that there are no other cloud layers overhead– typical for the summer season in Southern California (Christensen et al. 2013)– and calculate the daily maximum of global horizontal irradiance (GHI) from a clear sky model (Ineichen and Perez 2002). For obtaining  $T_{sky}$ , we solve for the longwave radiative fluxes across the whole atmosphere by inputting the temperature profiles from the radiosonde into the Streamer radiative transfer model (Key and Schweiger 1998) and calculating  $T_{sky}$  as the blackbody temperature from the longwave downwelling flux at the top of the cloud (Appendix C3).

We estimate  $\bar{u}$  and SLP from measurements at the NKX METAR weather station. We compute  $\bar{u}$  as the average of the westerly wind speeds between 0500 and 2100 LST and scale a 10-year average daily profile to recreate the diurnal cycle (see Fig. B1-b). This daily profile never reaches zero, so advection is continually present during the day (Appendix C5). We compute SLP as a daily average.

For the turbulent fluxes at the surface, we take different approaches for the ocean and land 209 columns. For the ocean column, the prescribed values of sensible and latent heat surface fluxes 210 (SHF and LHF) are computed with a bulk formula (Appendix C5) from observations of wind speed 211  $\overline{u}$  and daily averages of sea surface temperature (SST) at the Torrey Pines Outer station obtained 212 from the National Data Buoy Center (NDBC) (NOAA 2017). For the land column, we estimate 213 a daily Bowen ratio Bo at NKX by analyzing in-house operational runs of the Weather Research 214 and Forecasting (WRF) model. Bo is computed as the ratio between SHF and LHF at the nearest 215 grid point to the NKX station, averaged between 0800 and 1500 LST (Appendix C4). 216

Lastly, we estimate large-scale divergence *D* from the North American Mesoscale Forecasting System (NAM) as the partial derivative of pressure vertical velocity  $\omega$  with respect to pressure in the ABL (Appendix C4).

# 220 c. Steady thickness initialization (STI)

The MLM is initialized at 0300 LST prior to sunrise, when we expect a stable Sc behavior. Nevertheless, we occasionally observed large changes in modeled cloud thickness in the first few hours after initialization but still prior to sunrise, indicating possible inconsistencies in the initial state. For reference, Duynkerke et al. (2004, Fig. 4) observed  $\Delta LWP/\Delta t$  tendencies of 2.8 g m<sup>-2</sup> h<sup>-1</sup> and 7.6 g m<sup>-2</sup> h<sup>-1</sup> at 0300-0400 LST. In contrast, the first-hour average of  $\Delta LWP/\Delta t$  for our preliminary MLM runs ranged between -42 g m<sup>-2</sup> h<sup>-1</sup> and 12 g m<sup>-2</sup> h<sup>-1</sup>.

The reasons for large model tendencies following initialization are multifold: (i) The well-mixed 227 approach fits the radiosonde data to a slightly different state (Fig. 2); (ii) radiosonde measurement 228 errors, especially in the humidity measurement; (iii) LWP is not measured and has to be derived 229 using a crude model (LWP =  $\int_0^{z_i} \rho(z) q_l(z) dz$ , where  $\rho(z)$  is the density of air); (iv) the MLM does 230 not adequately describe all ABL physics; and (v) uncertainties in the estimated large-scale diver-231 gence. Since the variable inter-dependencies will be studied as a function of the initial conditions, 232 it is important that the initial conditions are representative of the first few hours of the simulations. 233 While initial variables should reflect real conditions as much as possible, our main objective is to 234 understand the sensitivities of Sc evolution. Therefore, a stable, self-consistent MLM initialization 235 is the priority and slight deviation from measured conditions when needed is tolerated. The steady 236 thickness initialization (STI) method was developed to create a stable initial condition from the 237 measured profiles. 238

<sup>239</sup> We seek a more stable state by keeping  $z_i$  constant and varying the set of thermodynamic vari-<sup>240</sup> ables  $\mathbf{s} \equiv (\theta_l^{\text{BL}}, \Delta_i \theta_l, q_l^{\text{BL}}, \Delta_i q_l)$ . For mathematical consistency, the tropospheric mixing ratio  $q_l^{3\text{km}}$ <sup>241</sup> will also be modified (since it is the sum of ABL and inversion jump quantities). We do not seek a <sup>242</sup> state with zero tendency because (i) we want to avoid deviating too much from the original state, <sup>243</sup> (ii) there is no unique value of  $\mathbf{s}$  that satisfies the steady thickness condition (van der Dussen et al. <sup>244</sup> 2013, Fig. 3), and (iii) it has been observed that the  $z_i$  tendencies at dawn are small but not zero. <sup>245</sup> Instead, we seek for a close, more stable state  $\mathbf{s}$  by thresholding the rate of change of thickness <sup>246</sup> (Eq. 1).

$$\left|\frac{\partial h}{\partial t}\right| = \left|\frac{\partial z_i}{\partial t} - \frac{\partial z_b}{\partial t}\right| < 5 \cdot 10^{-3} \,[\mathrm{m \, s}^{-1}] \tag{1}$$

<sup>247</sup> Using an iterative gradient descent method the 4 variables change at the same time (Eq. 2), in <sup>248</sup> an amount proportional to the local gradient of the thickness tendency.

$$\mathbf{s}_{n+1} = \mathbf{s}_n - \operatorname{sgn}\left(\frac{\partial h}{\partial t}(\mathbf{s}_n)\right) \xi \nabla \frac{\partial h}{\partial t}(\mathbf{s}_n), \tag{2}$$

<sup>249</sup> where  $\xi$  is the proportionality constant used to follow the gradient;  $\xi = 0.1$  yielded satisfactory <sup>250</sup> results for most days. We compute the gradient with second order central finite differences using <sup>251</sup> a step of 0.1 K or 0.1 g kg<sup>-1</sup> in each component of **s** and iterate until the thinning or thickening <sup>262</sup> is less than 5 mm s<sup>-1</sup> (Eq. 1). An example of the effect of the STI is shown in Fig. 3. The strong <sup>263</sup> thinning experienced in the first hour of simulation with the original initial conditions is greatly <sup>264</sup> reduced, and the STI initial conditions yield -6.4 g m<sup>-2</sup> h<sup>-1</sup> <  $\Delta$ LWP/ $\Delta$ t < 12 g m<sup>-2</sup> h<sup>-1</sup>, in <sup>265</sup> better agreement with observations in Duynkerke et al. (2004, Fig. 4).

<sup>256</sup> Finally, we remove STI states that lie far from the original using a squared distance threshold

$$d^{2} = \sum_{i=1}^{4} \left( \frac{s_{i}^{\text{STI}} - s_{i}}{s_{i}} \right)^{2} = 0.005,$$

where  $s_i$  and  $s_i^{\text{STI}}$  are the components of **s** prior and after the STI method is applied, respectively. Twelve cases are removed in this way. For the final set of 195 cases used in the analysis, 115 cases were not modified by the STI, as the original state was already steadier than 5 mm s<sup>-1</sup>, and for the 80 cases that were modified, the average  $d^2$  was 0.0007.

# 261 d. Model runs

The STI-adjusted dataset becomes the new input to the MLM. The initial conditions are the STI thermodynamic profiles derived from the radiosonde. The other variables are related to forcings at the boundaries of the ABL, such as air mass advection and fluxes at the surface and inversion levels. The MLM predicts the evolution of the cloud and yields the cloud dissipation time over
land. Simulations are terminated when clouds dissipate because the increase in solar heating of
the ABL prevents cloud reformation until evening and because several model assumptions (e.g.
the entrainment calculation) are no longer valid.

#### *e. Data subsetting*

Some of the original 278 cloudy and not decoupled days produced results inconsistent with the MLM assumptions: (i) STI leading to a cloudless state; (ii) negative entrainment values that may be related to decoupling (Appendix B3); (iii) clouds whose base reached the surface during the simulation (the longwave radiation scheme in the MLM may not represent fog conditions accurately); (iv) otherwise extremely thick clouds that could precipitate (precipitation is not modeled in the MLM), using a threshold of LWP = 250 g m<sup>-2</sup>; and (v) days with precipitation at the METAR station. After filtering these cases out, we were left with a dataset of 195 days.

# 277 f. Sensitivity analyses

# 278 1) All variables co-vary on 195 real days

<sup>279</sup> We analyze the results of the MLM runs for the diverse conditions of 195 days that span a broad <sup>280</sup> range of the parameter space and display co-variability. We investigate the trends in dissipation <sup>281</sup> time over land,  $t_{diss}$ , in relationship to each one of the variables of interest.

# 282 2) SINGLE VARIABLE CHANGES FROM A REFERENCE CASE

The results of the cases with co-variability can be difficult to analyze, as different impacts can be enhanced or diminished by the combination of different variables. To aid the understanding of the co-variability analysis, we first identify the individual influence of each variable on dissipation

time through a traditional sensitivity analysis. We vary one variable at a time from an idealized 286 reference case composed of the medians of all the MLM input variables:  $z_i$ ,  $q_t^{\text{BL}}$ ,  $\Delta_i q_t$ ,  $q_t^{\text{3km}}$ ,  $\theta_l^{\text{BL}}$ , 287  $\Delta_i \theta_l, \theta_l^{3\text{km}}, \overline{u}, SW_i, D, Bo, SLP, T_{sky}, SHF, and LHF.$  The purpose of using this idealized reference 288 case is to be able to change most variables in their observed ranges. A set of 5 equidistant points 289 between the percentiles  $p_{25}$  and  $p_{75}$  of the observed distribution for that input variable is simulated. 290 The other 14 variables are held constant with the following exceptions: (i)  $\Delta_i q_t$  and the tropo-291 spheric mixing ratio are varied together for self-consistency (Eq. C3); (ii)  $z_i$  is varied following 292 two approaches: (ii-a) variations of  $z_i$  alone, which yields different cloud thicknesses, and (ii-b) 293 variations of  $z_i$  with constant cloud thickness obtained by adjusting  $q_t^{\text{BL}}$ ; (iii) variations of cloud 294 thickness h with constant  $z_i$  and  $\theta_l^{BL}$  obtained by adjusting  $q_t^{BL}$ . 295

The motivation for (ii-b) is to assess the changes of  $z_i$  without the feedbacks related to the abrupt change in cloud thickness. We refer to (ii-b) as varying  $z_i|_h$ , and we calculate the adjusted  $q_t^{\text{BL}}(z_i|_h)$ using  $\partial z_b / \partial q_t^{\text{BL}}$  (Ghonima et al. 2015, Eq. 15) (Eq. 3).

$$(q_t^{BL})_{new} = (q_t^{BL})_{old} + \Delta z_i \frac{\partial q_t}{\partial z_b} = (q_t^{BL})_{old} \left(1 + \frac{g}{R_d T_b} \left(1 - \frac{L_{lv} R_d}{C_p R_v T_b}\right) \Delta z_b\right),\tag{3}$$

where  $(q_t^{\text{BL}})_{new}$  is the value of moisture needed for the updated height  $(z_i)_{new}$  with respect to the original  $(q_t^{\text{BL}})_{old}$ . For varying  $z_i|_h$ , *h* is constant and  $\Delta z_b = \Delta z_i = (z_i)_{new} - (z_i)_{old}$  is the change in cloud thickness from the reference case, with  $(z_i)_{old}$  the reference case inversion base height.  $T_b$ is the temperature at the original cloud-base height.

Similarly, the motivation for (iii) is to assess the changes of *h* without the effects of varying  $z_i$ . We refer to this case as varying  $h|_{z_i}$ , and the adjusted  $q_t^{\text{BL}}(h|_{z_i})$  is obtained with Eq. 3, taking  $\Delta z_b = -\Delta h = (h)_{old} - (h)_{new}$  because  $z_i$  is constant. Here,  $(h)_{old}$  is the cloud thickness for the reference case and  $(h)_{new}$  is the updated cloud thickness.

## **307 3. Results and discussion**

## *a. Data statistics and correlations*

We present a description of the most important inter-correlations within the dataset, which is 309 crucial for understanding the results of the impacts when all variables co-vary. Table 1 shows 310 the main statistics, including diagnostic variables from the MLM (cloud-base height  $z_b$ , cloud 311 thickness h, inversion jump of virtual potential temperature  $\Delta_i \theta_v$ , and liquid water path LWP) and 312 for the well-mixed profiles before and after STI. In the remainder of this section, we describe the 313 main correlations (Fig. 4), distinguished by the nature of their relationship (seasonal trends, initial 314 conditions, and boundary forcings). We emphasize that initial conditions are prior to sunrise and 315 represent both coastal land and ocean conditions. 316

Given the large number of variables, Principal Component Analysis (PCA) would seem to be a relevant tool. We do not report PCA results for this dataset because the reduction of dimensions is limited (it takes 10 variables to explain 90% of the variance) and the resulting parameter space is non-physical.

#### 321 1) VARIABLES AFFECTED BY SEASONAL TRENDS

<sup>322</sup> Our dataset includes measurements taken between May and September, a time span that is long <sup>323</sup> enough to show seasonal patterns that influence the correlation between some variables (no de-<sup>324</sup> trending is performed in this dataset). While solar irradiance above the cloud SW<sub>i</sub> varies during <sup>325</sup> the year, peaking on June 21, the set of temperature variables SST,  $\theta_l^{BL}$ , and  $T_{sky}$  peak in early <sup>326</sup> August. The time lag between SW<sub>i</sub> and the temperature variables is influenced by the seasonal <sup>327</sup> pattern of SST, which in turn is affected by the oceanic upwelling that is stronger during June and <sup>328</sup> July for Southern California (Clemesha et al. 2016) as well as the thermal inertia of the ocean. The time lag is long enough to cause a negative correlation between temperatures and SW<sub>i</sub> as shown in Fig. 4-a.

The strong correlation between SST and  $\theta_l^{\text{BL}}$  results from the strong influence of ocean SST on the early morning coastal air temperature through horizontal advection.

## 2) VARIABLES THAT DETERMINE INITIAL CONDITIONS

The initial state, prior to sunrise, comprises  $z_i$ ,  $q_t(z)$ , and  $\theta_l(z)$ , which together determine *h*. By definition, a warmer ABL that is cloudy is at (in-cloud) or near (below-cloud) saturation and can contain more water due to the Clausius-Clapeyron relationship; this makes  $\theta_l^{BL}$  and  $q_t^{BL}$  highly correlated. Conversely, conditions that are warm and dry (causing a negative correlation) are less likely to sustain a cloud and are therefore under-represented in the dataset.

Inversion base height  $z_i$  is strongly anticorrelated with  $q_t^{\text{BL}}$ ; a deeper ABL is associated with 339 lower temperature at the inversion base, requiring less water content to be present to saturate and 340 form a cloud. Entrainment also supports this relationship, as prolonged or stronger entrainment 341 can result in deeper ABLs and a lower  $q_t^{\text{BL}}$ . Interestingly, the relationship between the primary 3 342 ABL variables  $q_t^{\text{BL}}, z_i, \theta_l^{\text{BL}}$  is observed to be linear (R<sup>2</sup> of linear fit is 0.945, Fig. 7-a) and closely 343 follows saturation conditions (see Appendix E). Although a linear relationship exists, only two of 344 the three pairs are correlated, as  $z_i$  and  $\theta_l^{BL}$  do not correlate; therefore,  $q_t^{BL}$  acts like a dependent 345 variable. 346

<sup>347</sup> Cloud thickness *h* is defined as the difference between cloud-top  $z_i$  and cloud-base  $z_b$  heights. <sup>348</sup> One might expect lower cloud base to mean greater cloud thickness, but instead variations in cloud <sup>349</sup> thickness are dominated by variations in ABL top height (deeper ABLs have more room for thick <sup>350</sup> clouds). The correlation between  $z_i$  and  $q_t^{BL}$  causes thicker clouds to be strongly associated with <sup>351</sup> smaller  $q_t^{BL}$ . Cloud thickness is also strongly correlated with  $\Delta_i \theta_l$  because a stronger temperature

inversion limits the entrainment of drier and warmer air into the ABL, which thins the cloud. 352 Fig.4-b shows that both  $z_i$  and  $\Delta_i \theta_l$  influence h. Although the linear correlation coefficient is only 353 0.61, both variables combined explain nearly all the variance in h: ABLs with lower (higher) tops 354 and weaker (stronger) capping inversions are related to thinner (thicker) clouds. Note that  $\Delta_i \theta_l$  and 355  $z_i$  are not correlated in our dataset (Fig. 4). While this may seem counter-intuitive as strong LTS 356 has been linked to shallower ABLs (Klein and Hartmann 1993), LTS not only depends on  $\Delta_i \theta_l$  but 357 also on  $z_i$ . Following Wood and Bretherton (2006), the correlation coefficients of  $z_i$  and  $\Delta_i \theta_l$  with 358 LTS are -0.48 and 0.84, respectively. 359

For the tropospheric quantities,  $q_t^{3\text{km}}$  correlates with  $q_t^{\text{BL}}$ : a smaller  $q_t$  in the ABL is related to a smaller  $q_t$  above. The same logic explains the correlation between  $\theta_l^{3\text{km}}$  and  $\theta_l^{\text{BL}}$ .

#### 362 3) VARIABLES THAT DETERMINE BOUNDARY FORCINGS

Here, correlations between parameters that specify the boundary forcing of the ABL from above 363 and below are described. Large-scale subsidence, represented by the horizontal divergence D, 364 is weakly correlated with  $z_i$  even though subsidence pushes the ABL top down. At -0.08, the 365 correlation coefficient is small, which could be related to errors in estimating divergence, or to the 366 different values of entrainment that also affect  $z_i$ , or due to time lags / phase shifts between when 367 changes in D affect  $z_i$ , thus weakening the correlation between the two variables. From Myers and 368 Norris (2013), we would expect subsidence to also influence  $\Delta_i \theta_l$ , but the correlation between D 369 and  $\Delta_i \theta_l$  is weak. This disagreement may be explained also by the variables being out of phase 370 and by the exclusive use of well-mixed Sc-capped ABLs in our dataset (versus all ABLs in Myers 371 and Norris (2013)), since other ABL types tend to be associated with smaller D and smaller  $\Delta_i \theta_i$ . 372 Surface fluxes affect both temperature and moisture in the ABL. Over the ocean, LHF and SHF 373 correlate with  $\overline{u}$  by definition (Eqs. C8, C9). LHF is correlated with  $z_i$  while SHF is not. A larger 374

LHF was also related to a larger  $z_i$  in (Bretherton and Wyant 1997) probably because a larger LHF is related to a smaller  $q_t^{\text{BL}}$  (by definition), which in turn correlates to a larger  $z_i$ . In contrast, SHF depends on  $\theta_l^{\text{BL}}$ , which is not correlated to  $z_i$ .

Over land, Bo is negatively correlated to  $q_t^{\text{BL}}$  as an ABL with stronger surface latent heat fluxes causes both a larger  $q_t^{\text{BL}}$  and a smaller Bo. Secondary variable correlations ( $q_t^{\text{BL}}$  to  $\theta_l^{\text{BL}}$  and  $z_i$ ) explain the correlation of Bo to  $\theta_l^{\text{BL}}$  and  $z_i$ .

The last set of forcings are the radiative fluxes. For the shortwave portion, the yearly variations of solar irradiance causes SW<sub>i</sub> to be anti-correlated with temperature metrics (Section 3.a.1). For the longwave portion,  $T_{sky}$  is correlated with  $q_t^{3km}$  due to the longwave absorption and emission by water molecules above the cloud (Fig. B1-a). Secondary variable correlations ( $q_t^{3km}$  to  $q_t^{BL}$  and  $z_i$ ) explain the correlation of  $T_{sky}$  with  $q_t^{BL}$  and  $z_i$ .

# *b. Dissipation time dependence*

<sup>387</sup> We now review the results of the sensitivity analyses of modeled dissipation time, defined as <sup>388</sup> the time when cloud thickness *h* becomes zero. The main focus of this section is to compare the <sup>389</sup> co-variability results of the 195 simulated days to the single variable changes as well as previous <sup>390</sup> studies. The discussion is subdivided into initial conditions and forcing parameters.

The co-variability results for the 195 MLM simulations are shown in Fig. 5. The  $t_{diss}$  histogram (Fig. 5-a) shows that clouds either dissipate before 1300 LST or persist for the whole day. We refer to these two categories as dissipating and persisting cases, respectively, so  $t_{diss}$  is defined for dissipating clouds only. Some of the variables influence  $t_{diss}$ , while others differ markedly between dissipating and persisting cases, and some show unclear trends or non-monotonic tendencies. Figs. 5-b-r show the top 17 trends with linear fits for  $t_{diss}$  with R<sup>2</sup> > 0.02 or with a noticeable difference <sup>397</sup> between persisting and dissipating cases. Dissipation time is strongly related to h,  $z_i$ , LWP,  $q_t^{\text{BL}}$ , <sup>398</sup>  $\Delta_i \theta_l$ ,  $T_{sky}$ , and oceanic SHF; while  $\overline{u}$ , Bo, and D show weaker trends.

The results for the single variable changes from an idealized reference case while holding all other variables constant are shown in Fig. 6, where simulated dissipation time for the land column is plotted against the variables' Z-score (subtracting observed mean and dividing by the standard deviation) for ease of comparison. The idealized reference case corresponds to a coastal cloud that dissipates around 0800 LST (continuous line in Fig. F1).

# 404 1) INITIAL ABL STATE

The initial state of the ABL affects the dissipation time more than the forcing parameters. The components of the initial state are  $z_i$ ,  $q_t^{\text{BL}}$ , and  $\theta_l^{\text{BL}}$ , which have an intricate relationship (Section 3.a.2), and together determine *h*. Although *h* is not an explicit input variable to the MLM, we include it in the analysis because of its strong trend, the fact that it is readily observable, and its importance for entrainment and radiation.

For all the approaches considered, h has the most robust relationship with  $t_{diss}$ , followed by  $z_i$ . 410 Thicker clouds or deeper ABLs either dissipate later or persist for the whole day. Similarly to 411 marine Sc (Burleyson and Yuter 2015), clouds that are thicker at dawn can withstand more solar 412 heating and delay dissipation. For both h and  $z_i$ , co-variability weakens the single variable changes 413 trends on  $t_{diss}$  (Figs. 5-e,b and 6-a) because the independent effects are diminished by the effects 414 of the variables that co-vary with them, such as  $q_t^{\text{BL}}$ . For  $z_i$ , the co-variability trend is more similar 415 to the experiment where cloud thickness is held constant by varying  $z_i|_h$  together with  $q_t^{\text{BL}}$  (Fig. 416 6-b). This means that even when we control for the strong effects of h, other variables with weaker 417 independent trends also impact the final trend for  $z_i$ . The trends for h and  $z_i$  imply a strong trend 418 for LWP as well (Fig. 5-q). Since  $z_i$  and h are correlated, we analyze the trend of  $t_{diss}$  with respect 419

to both variables. Fig. 8-b shows that dissipation time varies with both *h* and  $z_i$ , but it is more strongly correlated with cloud thickness.

<sup>422</sup> While colder ABLs are related to later dissipation, as expected, moister ABLs dissipate earlier <sup>423</sup> with co-variability. For  $\theta_l^{BL}$ , the trend with co-variability (Fig. 5-c) is weaker than for the single <sup>424</sup> variable changes (Fig. 6-a), and for  $q_t^{BL}$ , the trend with co-variability (Fig. 5-d) is completely <sup>425</sup> opposite to the single variable changes (Fig. 6-a). This seeming contradiction is actually in agree-<sup>426</sup> ment with the strong correlations observed between larger  $q_t^{BL}$  and both lower *h* and  $z_i$  and larger <sup>427</sup>  $\theta_l^{BL}$ , which shorten cloud lifetime.

The fact that  $q_t^{\text{BL}}$  does not dominate the trend with co-variability also agrees with the linear 428 dependence of  $q_t^{\text{BL}}$  on  $z_i$  and  $\theta_l^{\text{BL}}$  (Section 3.a.2), and with the cloud thickness regulation feedback. 429 Cloud thickness is regulated towards an equilibrium state in that thicker clouds enhance cloud 430 radiative cooling and entrainment, which in turn thin the cloud and regulate h (Zhu et al. 2005). 431 At nighttime, thinner clouds will experience weaker entrainment due to the regulating feedback, 432 keeping the ABL moister and shallower and supporting the negative correlation between  $z_i$  and 433  $q_t^{\text{BL}}$ , and between h and  $q_t^{\text{BL}}$ . For these initially thin clouds experiencing reduced entrainment, we 434 expect a shorter cloud lifetime, which agrees with the trend of weaker first hour initial entrainment 435 rates  $\overline{w_{e,1h}}$  and earlier  $t_{diss}$  (Fig. 5-p). Lastly, Fig. 8-a visually shows the lack of dominance of  $q_t^{\text{BL}}$ 436 on  $t_{diss}$  when compared to  $z_i$ : the gradient of dissipation time, as well as the region of persisting 437 clouds, are more strongly correlated with  $z_i$  than  $q_t^{\text{BL}}$ , meaning that the trend between  $q_t^{\text{BL}}$  and  $t_{diss}$ 438 in Fig. 5-d is a consequence of the anti-correlation between  $z_i$  and  $q_t^{\text{BL}}$ . 439

# 440 2) INVERSION JUMPS AND FREE-TROPOSPHERIC CONDITIONS

While the inversion jumps and free-tropospheric state are part of the initial conditions, we analyze them separately because they represent the interaction between the ABL and free troposphere, rather than the ABL state. Stronger temperature inversion jumps  $\Delta_i \theta_l$  and weaker moisture inversion jumps  $\Delta_i q_l$  (moister tropospheres) delay dissipation time (Figs. 5-f,g), in agreement with most previous studies.

The effect of stronger temperature inversion jumps  $\Delta_i \theta_l$  agrees with the result for the single 446 variable changes (Fig. 6-a) for our reference case. Ma et al. (2018) obtained a  $\Delta_i \theta_l$  trend that 447 opposed ours and that of Xu and Xue (2015), and argued that the impacts of the temperature 448 inversion jump might depend on the reference case selected. There are competing effects of  $\Delta_i \theta_i$ : 449 while a stronger temperature inversion jump reduces the entrainment rate, it also means that the 450 entrained air is warmer. Mathematically, the net warming heat flux is the product of a reduced 451 entrainment rate and a stronger inversion jump, and the direction of the effect for the product 452 could vary for different conditions (Eq. B15). For our reference case, the diminished entrainment 453 rate dominates the over the warmer entrained air, delaying the dissipation by maintaining the ABL 454 moister and colder over land and ocean (Fig. F1-a). Our results with co-variability support the 455 trend of Xu and Xue (2015) and van der Dussen et al. (2015), as well as the trend of increased 456 cloudiness with stronger  $\Delta_i \theta_l$  in previous climate studies (Seethala et al. 2015; Klein and Hartmann 457 1993; Klein et al. 1995; Wood and Bretherton 2006). Nonetheless, we note that persisting clouds 458 do not predominantly exhibit stronger inversion jumps. 459

As was the case with *h*, the influence of  $\Delta_i \theta_l$  on  $t_{diss}$  is not dominated by  $z_i$ . This is evident in the two-dimensional space of  $z_i$  jointly with  $\Delta_i \theta_l$ . Fig. 8-c shows that earlier dissipation (persisting clouds) occurs for shallow (deeper) ABLs under a weak (strong) inversion, which also corresponds to the conditions for thinner clouds shown in Fig. 4-b.

For moisture, weaker inversion jumps  $\Delta_i q_t$  (relatively moister free tropospheres) are linked to persisting clouds, although dissipation time (as a continuous variable) is not strongly correlated to  $\Delta_i q_t$  (Fig. 5-g). The trend is consistent with the single variations due to reduced entrainment drying (Fig. 6-a), in agreement with the LWP responses reported by van der Dussen et al. (2015); Xu and Xue (2015); Ma et al. (2018).

At first glance, the co-variability trends of  $\Delta_i q_t$  and  $q_t^{3km}$  seem contradicting: weaker  $\Delta_i q_t$  (rel-469 atively moister free tropospheres) and also lower  $q_t^{3km}$  (drier free tropospheres) lead to persisting 470 clouds (Figs. 5-g,h). However, a weaker  $\Delta_i q_t$  is only a free troposphere that is similar in moisture 471 to the ABL, and not necessarily a moister free troposphere. Thus, a very dry free troposphere 472 can have a weak inversion jump if the ABL is also dry. Nevertheless, the trend of a dry tropo-473 sphere extending dissipation time is still unexpected since it opposes the single variable changes 474 (Fig. 6-a). The strong correlations between drier  $q_t^{3km}$  to higher  $z_i$  and lower  $T_{sky}$ , both of which 475 extend cloud lifetime, explain the trend. Previous studies have related moister free tropospheres 476 to reduced cloudiness (Dal Gesso et al. 2014; Seethala et al. 2015), where the latter (correctly) 477 speculated that correlations rather than physical processes are responsible for the trend. 478

<sup>479</sup> The combined effects of moisture and temperature inversion jumps have been studied for the <sup>480</sup> CTEI (Cloud Top Entrainment Instability), a process that can trigger cloud dissipation (Deardorff <sup>481</sup> 1980; Kuo and Schubert 1988; van der Dussen et al. 2013; Xu and Xue 2015). Even though <sup>482</sup> the stability parameter criterion  $\kappa \ge 0.23$  van der Dussen et al. (2013, Eq. 1) was found to be <sup>483</sup> insufficient to predict the CTEI, Fig. 5-r shows a trend between larger  $\kappa$  and earlier dissipation, <sup>484</sup> suggesting that CTEI could be contributing to cloud dissipation for larger  $\kappa$ . Nevertheless, the <sup>485</sup> great dispersion precludes us from stating this conclusively ( $\mathbb{R}^2 = 0.03$ ).

Similarly to  $q_l^{3\text{km}}$ ,  $\theta_l^{3\text{km}}$  has a stronger effect with co-variability than in the single variable changes (Figs. 5-i and 6-a). The enhanced effect of  $\theta_l^{3\text{km}}$  can be explained by the strong correlation to  $\theta_l^{\text{BL}}$ .

#### 489 3) SEABREEZE ADVECTION

Since seabreeze advection is crucial in extending the lifetime of coastal Sc (Ghonima et al. 490 2016), a robust trend between  $\overline{u}$  and  $t_{diss}$  is expected, as shown by the single variable changes (Fig. 491 6-c). In actuality, the trends with co-variability show  $\overline{u}$  exhibiting a nonlinear behavior where 492 larger wind speeds are associated with both persisting clouds and early dissipation time (Fig. 5-j). 493 The nonlinear trend of  $\overline{u}$  is not related to the physics, but it is caused by a sampling issue. In 494 order to explain this misleading trend, we look at the influence of initial cloud thickness on the 495 relationship between  $\overline{u}$  and  $t_{diss}$ . Fig. 8-d shows first that h dominates the dependence of dissipation 496 time in the  $\overline{u}$  and h space. Second, separating analyses for thick (h > 150 m) and thin clouds is 497 enlightening. Thicker clouds persist with larger  $\overline{u}$ , as expected, and the critical wind speed for 498 clouds to persist decreases with greater initial cloud thickness. For thinner clouds, the dissipation 499 time is not affected by  $\overline{u}$ . Since the persisting clouds are not part of the trend lines in Fig. 7, a 500 misleading anti-correlation of wind speed and dissipation time is observed. This analysis suggests 501 that advection is irrelevant for thin clouds as they already dissipate before the onset of advection 502 around 0700 LST. Advection does play an important role for thicker clouds that survive through 503 the weak advection period, which then benefit from the cooling associated with stronger advection. 504 This effect was not observed by Ghonima et al. (2016) as they only analyzed two reference cases 505 with the presence or absence of seabreeze. 506

Another aspect that could cause our results to deviate from real observations is the wind speed input for the MLM. For ease of comparison, we have assumed that the wind speed for all 195 days has the same diurnal variation (i.e., the onset of seabreeze is fixed, but the magnitude changes). However, we speculate that the timing of the sea-breeze onset may be as or more important than the wind speed magnitude. By 0800 LST, when the wind speed increases in our simulation (Fig. C1-

24

<sup>512</sup> b), 116 days are already clear or have clouds that are already so thin that the heat input from solar
<sup>513</sup> radiation dominates over cooling from horizontal advection. For these early morning dissipation
<sup>514</sup> cases, the wind speed is irrelevant. This timing dependence was also mentioned by Burleyson and
<sup>515</sup> Yuter (2015) for marine Sc, as cloud breakup rates strengthen near noon.

#### 516 4) SURFACE FLUXES

For coastal Sc clouds, both the surface fluxes over the ocean and over land can affect the cloud 517 evolution. A larger SHF over the ocean is linked to earlier dissipation time, agreeing with previous 518 studies for marine Sc (McMichael et al. 2019; Chlond and Wolkau 2000). The effect of SHF under 519 co-variability is greater than for the single variable changes (Figs. 5-k and 6-c). In contrast, the 520 influence of LHF on t<sub>diss</sub> is weak with co-variability, despite the existence of persistent clouds for 521 larger LHF (Fig. 5-1) supporting the trend of the single variable changes (Figs. 6-c). This differ-522 ence between the effect of SHF and LHF suggests that the importance of the ocean fluxes, which 523 influences coastal clouds through advection, may be greater for temperature than for moisture, 524 agreeing with Ghonima et al. (2016). 525

<sup>526</sup> Over land, the influence of Bo on dissipation time does not show a strong trend when co-<sup>527</sup> variability is considered, but persistent cases are related to higher Bo (Fig. 5-m), contradicting <sup>528</sup> Ghonima et al. (2016) and the trends of single variable changes. This unexpected effect is a con-<sup>529</sup> sequence of the correlation between Bo and  $q_t^{\text{BL}}$ .

# 530 5) LARGE-SCALE FORCINGS

<sup>531</sup> Subsidence is known to be of great importance for the evolution of Sc clouds. Stronger *D* <sup>532</sup> reduces cloud lifetime by thinning the cloud from the top, and the clouds that persist have lower <sup>533</sup> *D* (Fig. 5-n), agreeing with the single variable changes (Fig. 6-d), as well as the response in LWP in previous sensitivity studies (McMichael et al. 2019; Ma et al. 2018; van der Dussen et al. 2016;
Noda et al. 2014; Blossey et al. 2013) and the response in cloudiness for independent changes of
subsidence (Myers and Norris 2013).

Aside from subsidence, SLP is an indicator of the synoptic conditions over the coast of California. Although there is not a robust impact of SLP on  $t_{diss}$  with co-variability (not shown), we note that the physical impact of a smaller SLP yields later  $t_{diss}$  because –for constant  $\theta_l^{BL}$ – a colder temperature profile is needed to balance the change in pressure, resulting in a thicker cloud.

#### 541 6) RADIATIVE FORCINGS

<sup>542</sup> We have two radiation parameters of importance for dissipation of coastal clouds representing <sup>543</sup> radiative cooling and solar heating. Stronger radiative cooling, represented by a lower  $T_{sky}$ , delays <sup>544</sup> dissipation with the most robust trend of all the forcing parameters (Fig. 5-o). This effect agrees <sup>545</sup> with the single variable changes (Fig. 6-d) and previous studies (Kopec et al. 2016; Chlond and <sup>546</sup> Wolkau 2000).

For the solar heating,  $SW_i$  shows no clear trend with  $t_{diss}$  under co-variability (not shown). Meanwhile, the effect observed for single variable changes is that increased heating shortens cloud lifetime (Fig. 6-d), as the additional heating of the cloud and the land surface accelerates dissipation. Although  $SW_i$  was found to strongly influence the rate of cloud breakup for marine clouds (Burleyson and Yuter 2015), that effect may be reduced by the dominance of other factors such as ABL depth and cloud thickness.

# <sup>553</sup> c. Summary, quantification, and discussion of dissipation trends

<sup>554</sup> Most of the impacts of different variables on cloud dissipation time over land were either di-<sup>555</sup> minished or increased when considering co-variability, while others were unexpected due to the <sup>556</sup> correlations among parameters related to forcings and initial conditions. In this section, we sum-<sup>557</sup> marize and quantify the most robust trends when all variables co-vary and compare them to the <sup>558</sup> trends resulting from changes in a single variable when all others are held constant.

The trends are expressed as  $\delta \psi / \delta t_{diss}$ , quantifying how much change in a variable  $\psi$  is needed 559 to delay  $t_{diss}$  by one hour. Thus, the greater the number, the less sensitive  $t_{diss}$  is for that variable. 560 For the analysis of changes with all variables co-varying, we obtain one-dimensional linear fits for 561 all dissipating cases. For the analysis of changes in a single variable from a reference case with all 562 other variables held constant, we calculate the slope  $\delta \psi / \delta t_{diss}$  also for all dissipating cases. We 563 also compute trends for the two-dimensional space spanned by strongly correlated variables  $z_i$  and 564  $q_t^{\text{BL}}$  as a two-dimensional linear fit of all the points to estimate the relationship between  $t_{diss}$  and 565 the two variables  $(z_i, q_t^{BL})$  as 566

$$\Delta t_{diss} \approx \frac{\delta t_{diss}}{\delta z_i} \Delta z_i + \frac{\delta t_{diss}}{\delta q_t^{\rm BL}} \Delta q_t^{\rm BL}.$$
(4)

The results of the different methods are shown in Table 2. We acknowledge that for the single variable changes the linear trend results depend on the reference case and only a single reference case is considered here. For the dissipation time trends when all variables co-vary, the different linear fits are also an approximation since the behavior is likely to be nonlinear based on the non-linearities in the entrainment and radiation parameterizations. The estimated trends should be interpreted with caution, as they are marginal views of the behavior in the multi-dimensional space and other variables will naturally vary and contribute to the overall impact.

The most consistent trend is the  $\delta \psi / \delta t_{diss}$  response to changes in  $z_i$ . A greater change of  $z_i$  is needed to influence  $t_{diss}$  when all variables co-vary (163.9 m h<sup>-1</sup>) compared to when only  $z_i$  varies and other variables are held constant (50.40 m h<sup>-1</sup>). The  $\delta \psi / \delta t_{diss}$  response is least sensitive for changes in inversion base height with cloud thickness held constant ( $z_i|_h$ , 320.9 m h<sup>-1</sup>) probably <sup>578</sup> because the  $z_i$  change is not reinforced by changes in initial *h*. For *h*, we find a similar effect <sup>579</sup> of co-variability, requiring greater changes (319.6 m h<sup>-1</sup>) compared to when only  $h|_{z_i}$  was varied <sup>580</sup> (78.74 m h<sup>-1</sup>).

The impact of  $q_t^{\text{BL}}$  on  $t_{diss}$  is strong, but the different approaches yield contradictory trends, as discussed in Section 3.b.1. While the single variable changes yielded a positive  $\delta \psi / \delta t_{diss}$  response (0.359 g kg<sup>-1</sup> h<sup>-1</sup>), the fit for  $q_t^{\text{BL}}$  when all variables co-vary (-2.826 g kg<sup>-1</sup> h<sup>-1</sup>) and the fit in the 2D ( $q_t^{\text{BL}}, z_i$ ) space (-21.11 g kg<sup>-1</sup> h<sup>-1</sup>) are both negative. Meanwhile, the constant cloud thickness analysis varying  $z_i|_h$  yields a similar value to the trend with co-variability (-1.891 g kg<sup>-1</sup> h<sup>-1</sup>).

The comparison of the sensitivity of dissipation time when a single variable changes to sen-587 sitivity when all variables co-vary highlights the difficulty in finding universal cloud response 588 trends because of the multi-dimensionality and inter-correlations in the dataset. Changing a sin-589 gle variable ignores its correlations with other variables and may create unrealistic meteorological 590 conditions. Simplified co-variability, such as variations of  $z_i|_h$  together with  $q_t^{\text{BL}}$  to minimize feed-591 backs related to strong changes of cloud thickness, can yield more realistic trends. However, we 592 are not able to isolate the unique influence of one variable on dissipation time when all variables 593 co-vary, and the net effects are composed of all the correlated variable contributions. However, 594 the trends in cloud dissipation time when all variables co-vary can quantify the marginal impact 595 of a variable in the most realistic way, in the sense that it is what we would observe in nature if 596 we were to measure a limited number of variables. Still, co-variability effects are found to be too 597 important to ignore, and thus, they should be considered in sensitivity analyses in order to improve 598 prediction models. 599

The timing of dissipation may also affect the importance of some variables, as noted by Burleyson and Yuter (2015) in explaining why breakup rates of marine Sc are stronger in the late

morning. Over coastal land, when  $t_{diss}$  is closer to noon, wind speed and solar irradiance are 602 greater than in the early morning and the same relative change in these variables would cause a 603 larger absolute change in advective cooling and solar heating. This dependence on dissipation 604 timing could apply to all variables with diurnal cycles, such as  $\overline{u}$ , Bo (as it is applied to surface 605 fluxes over land), and SW<sub>i</sub>. In fact, Figs. 5-j-o show that most cases resulting in early dissipation 606 times are caused by a larger range of forcing variables than later dissipation times. Because of this 607 spread in the early morning cases, the dissipation trends can be affected. Elucidating the extent 608 of this impact is left for future work and it can indeed help to move forward to more realistic 609 predictions. 610

While the physical processes described are consistent with the statistical results in this paper, 611 simplifications may affect real dissipation trends: (1) The wind speed timeseries was simplified to 612 allow a more standardized comparison. (2) Uncertainties exist in the estimation of D and Bo. (3) 613 The ABL is assumed to be well-mixed. (4) Decoupling is not considered in the MLM, which might 614 influence the real trends related to  $z_i$  and dissipation time even though cases that were initially 615 decoupled were removed from the analysis. Even though this means that the prediction skill of the 616 model is currently not sufficient to predict real dissipation times (as discussed in Appendix D), it 617 also means that the complex results obtained are a pure consequence of the co-variability within 618 the dataset. If co-variability has such a great influence on the results of a simple model such as the 619 MLM, it will probably have it to a greater extent in more complex models and in nature. 620

# 621 4. Conclusions

We have studied the effects of several variables on the predicted dissipation time of Sc clouds over a coastal region using a realistic dataset and a two column Mixed-Layer Model. The dataset <sup>624</sup> included 195 Sc days in the summers of 2014 to 2017 in Southern California, with 15 variables <sup>625</sup> acting as initial and forcing parameters in the MLM.

<sup>626</sup> The main findings are summarized as follows:

• This work confirmed the importance of initial ABL height and cloud thickness in coastal Sc dissipation, in agreement with the trends of cloudiness for marine Sc. If these two variables could be measured more accurately and time-resolved in coastal areas using lidar, solar forecasts in the area could be improved.

Co-variability results, in which perturbations to one variable are accompanied by correlated variations in other variables related to initial conditions and forcings from a sample of 195
 cloudy days, differ greatly from a traditional, single-variable sensitivity analysis. In most cases, co-variability only strengthened or diminished the trend of a variable (albeit sometimes substantially), while in other cases the trend was the complete opposite.

• For example, lower ABL total water mixing ratio and larger Bowen ratio delay cloud dissipation with co-variability while they accelerate dissipation time as single variables or in previous studies (Ghonima et al. 2016).

• Co-variability also provides a different perspective on how sea-breeze advection can affect dissipation time compared to previous Sc studies over coastal land (Ghonima et al. 2016), affecting initially thinner clouds more than thicker ones.

• Co-variability effects are uniquely observable in our analysis and could not have been observed with a traditional sensitivity analysis. The use of a model instead of observed data ensures that the trends observed are solely a consequence of the co-variability in the dataset and not of unknown or unobservable effects stemming from real-world complexities. Given

- the importance of co-variability, modeling studies with sensitivity analyses should include co-variability in the scenario generation.
- Dissipation times predicted by the MLM correlate only weakly to observed dissipation times, likely due to the simplicity of the model.

<sup>650</sup> Future work should examine correlations in other coastal Sc regions in order to study the extent <sup>651</sup> of regional influence on the variables. Another topic of interest is the influence of realistic wind <sup>652</sup> conditions on coastal dissipation time.

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APPENDIX A
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# Nomenclature

# 660 Roman symbols

AIn-cloud entrainment efficiency $A_{CBL}$ Convective ABL entrainment efficiency $A_{1}, A_{2}$ Constants for the shortwave radiative flux $c_{1}, c_{2}$ Constants for the longwave radiative flux $C_{f}$ Bulk transfer coefficient for surface fluxes $C_{p}$ Mean heat capacity of dry air in the ABL

$d^2$	Squared distance for the STI method
D	ABL large-scale horizontal divergence
$f_w$	Filter for westerly wind
F	Total net radiative flux
F <sub>LW</sub>	Net longwave radiation flux
F <sub>SW</sub>	Net shortwave radiation flux
g	Gravitational acceleration
h	Cloud thickness
k	Constant for the shortwave radiative flux
$L_{lv}$	Mean latent heat of vaporization in the ABL
$LW \mathop{\downarrow_i}$	Downwelling longwave flux at $z_i$
$n_b^{\rm RH}$	Points below $z_b^{\text{RH}}$ in the radiosonde
р	Pressure
$p_{00}$	Reference pressure (1000 hPa)
q	Constant for the shortwave radiative flux
$q_l$	Liquid water mixing ratio
$q_{\rm sat}$	Water saturation mixing ratio
$q_t$	Total water mixing ratio
$q_v$	Water vapor mixing ratio
$R_d$	Specific gas constant for dry air
$R_{v}$	Specific gas constant for water vapor
Ri	Bulk Richardson number
S	Auxiliary variable for the STI method

$SW_i$	Shortwave irradiance above the cloud
t <sub>diss</sub>	Predicted dissipation time
$T_b$	Temperature at cloud base
$T_{cld}$	Mean cloud temperature
$T_{sc}$	Mean temperature below cloud
T <sub>sky</sub>	Effective sky temperature
и	Wind speed for large scale advection
$\mathbf{u}(t)$	Wind velocity vector
ū	16 h average wind speed
$\overline{w' \theta_l'}$	Vertical turbulent flux of $\theta_l$
$\overline{w' \theta_v'}$	Buoyancy flux
$\overline{w'q'_t}$	Vertical turbulent flux of $q_t$
$W_*$	Convective vertical velocity scale
We	Entrainment rate
Wsub	Subsidence rate
Z.	Height
z <sub>b</sub>	Cloud-base height
$z_b^{\rm RH}$	Radiosonde cloud-base height
$z_i _h$	Changes of $z_i$ maintaining constant $h$
Zi	Inversion base height
$z_i^+$	Just above inversion base height
Zit	Inversion top height

# 661 Greek symbols

α	Constant for the longwave radiative flux
$\pmb{lpha}_{\scriptscriptstyle W}(t)$	Wind direction
β	Constant for the shortwave radiative flux
γ	Constant for the longwave radiative flux
$\delta \psi / \delta t_{diss}$	Change in $\psi$ to delay $t_{diss}$ by 1 h
$\Delta x$	Distance between ocean and land columns
$\Delta T$	Temperature inversion strength
θ	Potential temperature
$ heta_l$	Liquid water potential temperature
$oldsymbol{ heta}_{v}$	Virtual potential temperature
$\mu_0$	Cosine of the solar zenith angle
ξ	Tuning parameter for the STI method
П	Exner function
ρ	Air density in the ABL
σ	Stefan-Boltzmann constant
$\tau_{\rm SW}(z)$	Cloud optical depth for shortwave radiation (zero at cloud top)
$\tau_{\rm LW}(z)$	Cloud optical depth for longwave radiation (zero at cloud top)
$ au_{LW,b}$	Cloud optical depth at cloud base for longwave radiation
$\phi$	Conversion efficiency for land surface fluxes
ω	Pressure vertical velocity
$ abla_h$	Horizontal gradient operator

# 662 Abbreviations

Bo	Bowen ratio
GHI	Global Horizontal Irradiance
LHF	Latent heat flux at the ocean surface
LTS	Lower Tropospheric Stability
MLM	Mixed-Layer Model
Sc	Stratocumulus
SHF	Sensible heat flux at the ocean surface
STI	Steady Thickness Initialization
SZA	Solar zenith angle

# 663 Subscripts and superscripts

$\psi^{ m BL}$	Well-mixed value of $\psi$ in the ABL		
$\psi^{3km}$	Value of $\psi$ at $z = 3$ km		
$\psi_0$	Value of $\psi$ at the surface		
$\psi_b$	Value of $\psi$ at the cloud base		
$\psi_{cld}$	Value of $\psi$ evaluated in the cloud region		
$\psi_i$	Value of $\psi$ at the inversion base		
$(\psi)_{new}$	New value of $\psi$ to maintain constant $h$		
$(\psi)_{old}$	Original value of the variable $\psi$		
$\Delta_i \psi$	Inversion jump of $\psi$		

#### APPENDIX B

# **Mixed-Layer Model**

# **B1. Governing equations**

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The state of the well-mixed ABL is described by inversion base height  $z_i$ , total water mixing ratio  $q_t = q_v + q_l$ , and liquid water potential temperature  $\theta_l \approx \theta - \frac{L_l v q_l}{C_p \Pi}$ , where  $q_v$  is the water vapor mixing ratio,  $q_l$  is the liquid water mixing ratio,  $\Pi = (p/p_{00})^{R_d/C_p}$  is the Exner function,  $L_{lv}$ is the latent heat of vaporization,  $C_p$  is the heat capacity of dry air, p is pressure,  $p_{00} = 1000$  hPa, and  $R_d$  is the specific gas constant for dry air.

The governing equations of the MLM are the air mass, energy, and moisture balances (Eqs. B1, B3, B4), which describe the average state of the ABL through the well-mixed variables  $q_t^{\text{BL}}$  and  $\theta_l^{\text{BL}}$ . In the air mass balance (Eq. B1), entrainment, subsidence velocity, and large-scale advection determine the evolution of the ABL depth  $z_i$ .

$$\frac{\partial z_i}{\partial t} = w_e + w_{sub} - u\nabla_h z_i,\tag{B1}$$

where  $w_e$  is the entrainment rate,  $w_{sub}$  is the subsidence rate, u is horizontal wind speed, and  $\nabla_h$ is the large-scale horizontal gradient operator. The subsidence rate at the top of the ABL,  $w_{sub}$ , is parameterized by constant horizontal divergence D within the ABL:

$$w_{sub} = -D \cdot z_i. \tag{B2}$$

<sup>679</sup> In the heat balance (Eq. B3), turbulent fluxes, radiation, and large-scale advection drive the <sup>680</sup> evolution of the temperature in the ABL:

$$\frac{\partial \theta_l^{\text{BL}}}{\partial t} = -\frac{\partial}{\partial z} \left( \overline{w' \theta_l'}(z) + \frac{F(z)}{\rho C_p} \right) - u \nabla_h \theta_l^{\text{BL}}, \tag{B3}$$

where  $\overline{w'\theta_l'}(z)$  is the turbulent flux of liquid potential temperature and F(z) is the vertical profile of radiative flux.

In the total water content balance (Eq. B4), we do not consider precipitation fluxes and subsequently, only turbulent fluxes and large-scale advection are present:

$$\frac{\partial q_t^{\rm BL}}{\partial t} = -\frac{\partial}{\partial z} \overline{w' q_t'}(z) - u \nabla_h q_t^{\rm BL}, \tag{B4}$$

where  $\overline{w'q'_t}(z)$  is the turbulent flux of total water mixing ratio.

# **B2.** Horizontal advection

To describe ocean-land interaction, we model the evolution of two columns: one over the ocean and the other over land (Fig. 1). Due to the dominant wind direction from the ocean to the land, the ocean column model does not contain any advection terms, i.e. the last terms in (Eqs. B1, B3, B4) are removed. For the land column, the advection terms depend on both ocean and land conditions.

$$u\nabla_h \theta_l^{\rm BL} = \frac{u}{\Delta x} (\theta_{l,\text{land}}^{\rm BL} - \theta_{l,\text{ocean}}^{\rm BL})$$
(B5)

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$$u\nabla_h q_t^{\rm BL} = \frac{u}{\Delta x} (q_{t,\text{land}}^{\rm BL} - q_{t,\text{ocean}}^{\rm BL}), \tag{B6}$$

where *u* is the wind speed and  $\Delta x = 30$  km is the distance between the two columns. The associated coupling timescales  $\Delta x/u$  range between 1.3 h and 3.6 h min at noon, when the wind speed is maximum, and between 3.1 h and 8.4 h at night.

# **B3.** Entrainment parameterization

The entrainment rate is parameterized through buoyancy flux contributions (Ghonima et al. 2016, Section 4b). The total entrainment rate is the sum of contributions from surface and cloud regions, where each amount is proportional to a convective velocity scale,  $w_*$ , and inversely pro<sup>700</sup> portional to a bulk Richardson number, Ri.

$$w_e = w_{e,0} + w_{e,cld} = A_{\text{CBL}} \frac{w_{*0}}{\text{Ri}_0} + A \frac{w_{*cld}}{\text{Ri}_{cld}} = 1.25 \frac{A_{\text{CBL}}}{\Delta_i \theta_v} \overline{w' \theta_v'}|_0 + 2.5 \frac{A}{h \Delta_i \theta_v} \int_{z_b}^{z_i} \overline{w' \theta_v'}(z) dz, \quad (B7)$$

where, at the surface, the constant  $A_{CBL} = 0.2$  (Deardorff 1976) is a clear convective boundary 701 layer (CBL) entrainment efficiency,  $w_{*0}$  is the surface convective velocity scale, and Ri<sub>0</sub> is the 702 surface bulk Richardson number. For the cloud region, A is an entrainment efficiency coefficient 703 (Grenier and Bretherton 2001) that includes evaporative enhancement effects,  $w_{*cld}$  is a cloud 704 convective velocity scale, and Ricld is the bulk Richardson number in the cloud region. Lastly, 705  $\Delta_i \theta_v$  is the inversion jump of virtual potential temperature, and  $\overline{w' \theta'_v}(z)$  is the buoyancy flux with 706  $\overline{w'\theta_{\nu}'}|_0$  as its surface value. The buoyancy flux uses a vertical profile of dry and moist coefficients 707 that were updated at each iteration and were calculated differently for the subcloud and cloud 708 regions, following Cuijpers and Duynkerke (1993, Appendix A). 709

Some cases resulted in negative entrainment when using this paramterization, and were discarded from the analysis. When analyzing the entrainment rate, algebraic manipulation yields an explicit equation:

$$w_{e} = \frac{w_{e,0} + \frac{2.5A}{h\Delta_{i}\theta_{v}}\int_{z_{b}}^{z_{i}}\left(C_{1}\left[\left(1 - \frac{z}{z_{i}}\right)\left(\overline{w'\theta_{l}'}|_{0} + \frac{F_{0}}{\rho C_{p}}\right) + \frac{z}{z_{i}}\frac{F_{i}}{\rho C_{p}} - \frac{F(z)}{\rho C_{p}}\right] + C_{2}\left[\left(1 - \frac{z}{z_{i}}\right)\overline{w'q_{l}'}|_{0}\right]\right)dz}{1 + \frac{2.5A}{h\Delta_{i}\theta_{v}}\int_{z_{b}}^{z_{i}}\frac{z}{z_{i}}(C_{1}\Delta_{i}\theta_{l} + C_{2}\Delta_{i}q_{t})dz}$$
(B8)

where  $C_1$  and  $C_2$  are the moist coefficients. The denominator can be negative depending on the value of the integral. Assuming  $C_1$  and  $C_2$  are constants (which is a reasonable assumption), the criterion for negative entrainment becomes

$$\frac{h}{2z_i}(C_1\Delta_i\theta_l + C_2\Delta_iq_t) < -\frac{\Delta_i\theta_v}{2.5A},\tag{B9}$$

which depends on many parameters and cannot be analyzed in a simple way. If we explore the condition for r.h.s.= 0, with referential moist coefficients  $C_1 = 0.5$  and  $C_2 = 970$  K (Ghonima et al. 2016, Section 4b), we obtain:  $\Delta_i \theta_l < C_2/C_1 |\Delta_i q_t| \approx 1.94 |\Delta_i q_t|$ . The CTEI criterion also relates the inversion jumps (van der Dussen et al. 2013, Eq. (1)) and can be rewritten as  $\Delta_i \theta_l <$ 0.77  $L_{l\nu}/C_p |\Delta_i q_t| \approx 1.915 |\Delta_i q_t|$ . Both conditions are very similar, suggesting that the cases close to the critical CTEI criterion can yield negative entrainment rates when using this parameterization. Our physical interpretation is that for cases where negative subcloud fluxes should develop, the integrated buoyancy flux in the ABL cannot be described by the positive in-cloud buoyancy flux alone, resulting in an artificial negative entrainment velocity.

# 725 **B4. Radiative model**

The net upward radiative flux includes longwave and shortwave contributions:  $F = F_{LW} - F_{SW}$ .

$$F_{\rm SW}(z) = \frac{4}{3} SW_{\rm i}(qA_1 e^{-k\tau_{\rm SW}(z)} - qA_2 e^{k\tau_{\rm SW}(z)} -\beta e^{-\tau_{\rm SW}(z)/\mu_0}) + \mu_0 SW_{\rm i} e^{-\tau_{\rm SW}(z)/\mu_0},$$
(B10)

where SZA is the solar zenith angle,  $\mu_0 = \cos(SZA)$ ,  $\tau_{SW}(z)$  is the cloud optical depth (zero at cloud top) (Duynkerke et al. 2004, Eqs. 6 and 7) calculated with an effective radius of 10  $\mu$ m,  $A_1$  and  $A_2$  come from boundary conditions of the radiative transfer equation, and k, q and  $\beta$ are constants that depend on  $\mu_0$  and optical properties of cloud droplets (Duynkerke et al. 2004, Appendix).

The longwave contribution  $F_{LW}$  depends on three temperatures:  $T_{sc}$  taken as the mean temperature of the subcloud region;  $T_{cld}$  taken as the mean temperature in the cloud region, and  $T_{sky}$  taken as an effective radiative temperature of the sky.

$$F_{\rm LW}(z) = \gamma \sigma [(T_{cld}^4 - T_{sky}^4)c_1 e^{-\alpha \tau_{\rm LW,b}} + (T_{sc}^4 - T_{cld}^4)c_2] e^{\alpha \tau_{\rm LW}(z)} + [(T_{cld}^4 - T_{sky}^4)c_2 e^{\alpha \tau_{\rm LW,b}} + (T_{sc}^4 - T_{cld}^4)c_1] e^{-\alpha \tau_{\rm LW}(z)},$$
(B11)

<sup>735</sup> where  $\sigma$  is the Stefan-Boltzmann constant,  $\tau_{LW}(z)$  is the cloud optical depth (Larson et al. 2007, <sup>736</sup> Eqs. 6 and 7), and  $\tau_{LW,b}$  is the maximum optical depth (at cloud base). The parameters  $\alpha$ ,  $c_1$ ,  $c_2$ , <sup>737</sup> and  $\gamma$  are terms derived from the radiation transfer equation (Ghonima et al. 2016, Appendix B).

#### 738 **B5.** Surface and cloud-top fluxes

The surface fluxes of moisture  $\overline{w'q'_t}|_0$  and temperature  $\overline{w'\theta'_t}|_0$  depend on the type of the surface. For the ocean column, the SHF and LHF are fixed during the day. For the land column, the surface fluxes depend on the Bowen ratio Bo. A part of the net radiation flux at the surface  $F_0$  is converted into a moisture and a heat flux released to the ABL (Eqs. B12, B13).

$$\overline{w'q_t'}|_{0,\text{land}} = \phi \frac{1}{1 + \text{Bo}} \frac{F_0}{\rho C_p} \tag{B12}$$

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$$\overline{w'\theta_l'}|_{0,\text{land}} = \phi \frac{\text{Bo}}{1+\text{Bo}} \frac{F_0}{\rho C_p},\tag{B13}$$

where  $\phi = 0.88$  is the efficiency at which net radiation is converted into surface fluxes (Ghonima et al. 2016).

At the top of the ABL, the turbulent fluxes of moisture  $\overline{w'q'_t}|_i$  and temperature  $\overline{w'\theta'_t}|_i$  depend on the entrainment rate  $w_e$  and the sharp inversion jumps of moisture (Eq. B14) and temperature (Eq. B15), respectively (Lilly 1968):

$$\overline{w'q'_t}|_i = -w_e \Delta_i q_t, \tag{B14}$$

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$$\overline{w'\theta_l'}|_i = -w_e \Delta_l \theta_l. \tag{B15}$$

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# APPENDIX C

#### Data

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## 752 C1. Variables

The parameterizations and equations included in the MLM determine our variables of interest. We gather data from different sources for the years 2014 to 2017, May to September. In the following, variables are grouped by their data source.

# <sup>756</sup> C2. Radiosondes: $z_i$ , $\theta_l(z)$ , $q_t(z)$

<sup>757</sup> We obtain 1200 UTC radiosonde data (reported at 0400 LST, launched at 0300 LST) from the <sup>758</sup> NKX Miramar Marine Corps Air Station in Southern California (32.85° N, 117.2°W). The station <sup>759</sup> is located 10 km away from the coast, where the shoreline is aligned meridionally.

Radiosonde profiles are post-processed into well-mixed layers to make them compatible with 760 the MLM. First, temperature inversions in the lowest 3 km are detected. The largest temperature 761 inversion is assumed to cap the mixed layer if it is sufficiently strong ( $\Delta T > 3$  K), yielding inversion 762 base and top heights,  $z_i$  and  $z_{it}$  respectively. Clouds are assumed to exist where relative humidity 763 (RH) exceeds 95% below  $z_i$ , with the radiosonde cloud base  $z_b^{\rm RH}$  defined as the lowest point that 764 meets that condition. Decoupled days cannot be represented in an MLM, and thus, we discard 765 these days using the criterion  $|\theta_{vb} - \theta_{v0}| > 1 K$  (Ghate et al. 2015), where  $\theta_{vb}$  and  $\theta_{v0}$  are the 766 virtual potential temperature at the radiosonde cloud base and at the surface, respectively. 767

The well-mixed  $q_t$  (Eq. C1) is an ABL average of the radiosonde measurements. Since  $q_l$  is not measured by radiosondes,  $q_t$  will be underestimated, but in view of the limited resolution of the data and that  $q_t \gg q_l$ , this approach is reasonable. Above the inversion, we consider  $q_t$  to be constant, and also compute it as an average up to 3 km.

$$q_{t}(z) = \begin{cases} q_{t}^{\mathrm{BL}} = \frac{1}{z_{i}} \int_{0}^{z_{i}} q_{v}(z) dz & \text{if } z < z_{i} \\ q_{t}^{3\mathrm{km}} = \frac{1}{3 \mathrm{km} - z_{it}} \int_{z_{it}}^{3 \mathrm{km}} q_{v}(z) dz & \text{if } z \ge z_{i}. \end{cases}$$
(C1)

For  $\theta_l(z)$ , we follow a similar averaging approach (Eq. C2). If there are more than 5 data points below  $z_b^{\text{RH}}$ , the average is computed in the subcloud region to avoid phase-change heating effects on  $\theta(z)$ ; otherwise, all points in the ABL are averaged (including all the points is not a major concern for  $q_t$  since  $q_t \gg q_l$ ). Above the ABL, we obtain a linear fit for  $\theta(z_{it} < z < 3 \text{ km})$ .

$$\theta_{l}(z) = \begin{cases} \theta_{l}^{\mathrm{BL}} = \frac{1}{z_{i}} \int_{0}^{z_{i}} \theta(z) dz & \text{if } z < z_{i} \text{ and } n_{b}^{\mathrm{RH}} \leq 5 \\ \theta_{l}^{\mathrm{BL}} = \frac{1}{z_{b}^{\mathrm{RH}}} \int_{0}^{z_{b}^{\mathrm{RH}}} \theta(z) dz & \text{if } z < z_{i} \text{ and } n_{b}^{\mathrm{RH}} > 5 \\ a \cdot z + b & \text{if } z \geq z_{i} \text{ with } a, b \text{ from linear fit for } \theta(z_{it} < z < 3 \text{ km}), \end{cases}$$
(C2)

where  $n_b^{\text{RH}}$  is the number of points below  $z_b^{\text{RH}}$ .

We assume that the inversion occurs over an infinitesimally thin layer, defining the inversion jumps of total water mixing ratio and liquid water potential temperature:

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$$\Delta_i q_t = q_t^{3\mathrm{km}} - q_t^{\mathrm{BL}},\tag{C3}$$

$$\Delta_i \theta_l = \theta_l (z = z_i^+) - \theta_l^{\mathrm{BL}}, \tag{C4}$$

where  $z_i^+$  is just above the inversion height.

# <sup>781</sup> C3. Radiative and clear sky models: $T_{sky}$ and SW<sub>i</sub>

We obtain the effective sky temperature  $T_{sky}$  for the longwave radiative model using the Streamer radiative transfer model (Key and Schweiger 1998). Inputs are the temperature and relative humidity soundings, which are extended to 100 km with a *U.S. Standard Atmosphere, 1976*. We compute  $T_{sky}$  as the blackbody temperature from the longwave downwelling flux at the top of the cloud as LW  $\downarrow_i = \sigma T_{sky}^4$ . Fig. B1-a shows that skies with more water content experience a smaller net radiative cooling at the cloud top.

For the shortwave radiation model,  $SW_i$  is the solar irradiance incident on the top of the Sc cloud. We estimate  $SW_i$  as the global horizontal irradiance (GHI) from a clear sky model (Ineichen and Perez 2002). Monthly climatological Linke turbidities for that location are input to the clear sky
 model.

# 792 C4. NWP models: Bo, D

<sup>793</sup> We estimate the Bowen ratio Bo at NKX by analyzing in-house operational runs of the Weather <sup>794</sup> Research and Forecasting (WRF) model using the Noah land surface model (Skamarock et al. <sup>795</sup> 2008). Bo is the ratio between SHF and LHF at the surface at the nearest grid point to the NKX <sup>796</sup> station. Hourly output is averaged between 0800 and 1500 LST to yield a (constant) daily Bo <sup>797</sup> that is input to the MLM simulations. Land surface models in WRF are known to differ from <sup>798</sup> measurements (Wharton et al. 2016); land surface models tend to produce Bo  $\approx$  1 with small <sup>799</sup> temporal deviations.

<sup>800</sup> We estimate large-scale divergence *D* from the NAM Forecasting System as the partial derivative <sup>801</sup> of pressure vertical velocity  $\omega$  with respect to pressure in the ABL. The differences are computed <sup>802</sup> between 975 hPa and 850 hPa (Eq. C5). We average *D* spatially over an area of 21 grid points <sup>803</sup> over the ocean around (38.15°N, 117.5°W) and then temporally with a 3-day moving average:

$$D = -\frac{\partial \omega}{\partial p} \approx -\frac{\omega(975 \text{ hPa}) - \omega(850 \text{ hPa})}{975 \text{ hPa} - 850 \text{ hPa}}.$$
 (C5)

#### **C5. METAR and NDBC:** $\overline{u}$ , SLP, SHF, LHF

For coastal regions in Southern California, the sea breeze acts during the day with a strong westerly component, usually beginning around 0800 LST and peaking around 1200 LST. A 16 h average (between 0500 and 2100 LST) wind speed  $\bar{u}$  is computed from the METAR weather station at NKX. All westerly winds (with direction between 180° and 360°) are scalar-averaged (Eq. C6).

$$\overline{u} = \frac{1}{16 \text{ h}} \int_{t=0500 \text{ LST}}^{t=2100 \text{ LST}} f_w(\mathbf{u}(t)) dt, \qquad (C6)$$

where  $\mathbf{u}(t)$  is the wind velocity with magnitude u(t) and direction  $\alpha_w(t)$  and  $f_w(\mathbf{u}(t))$  is the filter for considering westerly directions only:

$$f_w(\mathbf{u}) = \begin{cases} u(t) & \text{if } \alpha_w(t) \in (180^\circ, 360^\circ) \\ 0 & \text{else.} \end{cases}$$
(C7)

A 10-year average daily wind profile is shown in Fig. B1-b. The daily profile is normalized by its 16 h average wind speed and then re-scaled with the daily  $\overline{u}$ .

<sup>813</sup> We estimate SLP as the daily average SLP at the METAR weather station at NKX.

<sup>814</sup> Surface turbulent fluxes in the ocean column, which are fixed in the MLM, are computed from <sup>815</sup> wind and sea surface temperature data. Daily averages of SST are obtained at the Torrey Pines <sup>816</sup> Outer station from the National Data Buoy Center (NDBC) (NOAA 2017). Surface fluxes are <sup>817</sup> computed using a bulk transfer coefficient  $C_f = 1.2 \times 10^{-3}$  (Blossey et al. 2013), the average SST <sup>818</sup> and wind speed, and assuming that the temperature and moisture above the surface is the same as <sup>819</sup> that of the initial state of the ABL (Eqs. C8, C9):

 $SHF = \rho C_p \overline{u} C_f (SST - \theta_l^{BL}), \qquad (C8)$ 

$$LHF = \rho L_{lv} \overline{u} C_f(q_{sat}(SST) - q_t^{BL}), \qquad (C9)$$

where  $q_{sat}$  is the saturation mixing ratio.

# APPENDIX D

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# **Dissipation time comparison**

We estimate dissipation time over NKX  $t_{diss}^{SAT}$  using a satellite derived low cloudiness product (Clemesha et al. 2016; Wu et al. 2018). This dataset has a 4 km spatial resolution and 30-minute time resolution. We obtain  $t_{diss}^{SAT}$  at the closest pixel to NKX as the time when skies are clear for at least 1 hour afterwards. We neglect  $t_{diss}^{SAT}$  before 0500 LST since they are unlikely to caused by Sc, which would thicken during the night.

<sup>829</sup> We also estimate dissipation time  $t_{diss}^{\text{GHI}}$  from 1 s global horizontal irradiance data measurements <sup>830</sup> at the UC San Diego campus, 5 km west of NKX (Zamora Zapata et al. 2019). Only Sc to clear <sup>831</sup> transitions are included; a Sc cloud is assumed to exist if the early sounding is well-mixed and <sup>832</sup> has a cloud presence (RH>95%), while also checking sky imagery at the time of the breakup to <sup>833</sup> discard other cloud types or the presence of upper lever clouds. A  $t_{diss}^{\text{GHI}}$  event is recorded when the <sup>834</sup> clear sky index is close to 1 for the following 5 minutes.

There is a strong correlation between  $t_{diss}^{\text{SAT}}$  and  $t_{diss}^{\text{GHI}}$  (0.79,  $R^2 = 0.6$ ), while the correlation between MLM modeled dissipation time and  $t_{diss}^{\text{SAT}}$  and  $t_{diss}^{\text{GHI}}$  is 0.26 and 0.28 with  $R^2$  of 0.06 and 0.07, respectively.

Ideally the MLM dissipation times would be more correlated to the observed dissipation times. 838 But given the MLM assumptions, parameter uncertainties, adjustment of initial conditions, and 839 neglect of some physical processes, the relatively small correlation is not surprising. We maintain 840 that the MLM based analysis of parameter correlations is valuable and superior to the alterna-841 tives. Strengths of the MLM application in this analysis include: (i) The MLM represents most 842 of the physical processes. (ii) The MLM has been validated by Ghonima et al. (2016) against 843 LES, demonstrating that the MLM is capable of correctly predicting the evolution of an ideal-844 ized coastal Sc cloud. (iii) Initial conditions are approximated through elaborate sourcing from 845 best available models and measurement sources. (iv) The simple geometric domain of the MLM 846 prevents real-world complexities such as varying topography and 3D effects from affecting the 847 results. (v) Simulation days are limited to conditions that are represented in the model, e.g. days 848 with decoupling are removed. However, as evidenced by the need for adjustment of initial con-849 ditions, there are inconsistencies in the initial conditions and/or shortcomings in the model. As a 850

result the MLM results live in a virtual / model world. But we maintain that to analyze variability and co-variability between variables an internally consistent albeit somewhat idealistic modeling approach is preferable over sparse measurements and 3D models such as WRF that also perform poorly and introduce additional complexities. This paper is the first to attempt a comprehensive evaluation of variability and co-variability of atmospheric parameters for Sc dissipation over land. It is our hope that in the future models are improved and models can be better coupled to measurements to narrow the gap between model results and observations.

858

# APPENDIX E

859

# Linear approximation to $q_t^{\text{BL}}(z_i, \theta_l^{\text{BL}})$

For a cloud to form given ABL height  $z_i$  and well-mixed liquid water potential temperature  $\theta_l^{\text{BL}}$ , the total water content at ABL top must surpass saturation by a small amount, which is condensed into a cloud:  $q_t^{\text{BL}} = q_{sat}(z_i, \theta_l^{\text{BL}}) + q_l(z_i)$ . Since  $q_l(z_i) << q_t^{\text{BL}}$ , we investigate the behavior of  $q_{sat}(z, \theta_l)$ :

$$q_{sat} = \frac{\varepsilon}{p(z)/e_s(z,\theta_l) - 1},\tag{E1}$$

where  $\varepsilon = 0.622$  and pressure follows the hydrostatic assumption  $p(z) \approx p_0 - \rho gz$ . The water saturation pressure  $e_s$  is given by the August-Roche-Magnus approximation:

$$e_s = \kappa_1 \exp\left(\frac{\kappa_2 T_c}{\kappa_3 + T_c}\right),\tag{E2}$$

where  $\kappa_1 = 610.94$  Pa,  $\kappa_2 = 17.625$ ,  $\kappa_3 = 243.04$ , and  $T_c$  is temperature in Celsius. To estimate temperature near the cloud top, we will assume that we are just surpassing saturation with an infinitesimally thin cloud and use the dry adiabatic lapse rate.

$$T_c = T_0 - \Gamma_d z - 273.15 \text{ K},$$
 (E3)

where  $\Gamma_d = g/C_p$  is the dry adiabatic lapse rate and  $T_0$  is surface temperature, which is related to the well-mixed  $\theta_l$  and surface pressure  $p_0$ :

$$T_0 = \theta_l \left(\frac{p_0}{p_{00}}\right)^{R_d/C_p}.$$
(E4)

With these assumptions, we can estimate  $\frac{\partial q_{sat}}{\partial z}$  and  $\frac{\partial q_{sat}}{\partial \theta_l}$  and evaluate them at the observed means of  $z_i$ ,  $\theta_l$ , and  $p_0$  (Table 1), obtaining

$$\frac{\partial q_{sat}}{\partial \theta_l} = \frac{\varepsilon p}{(\frac{p}{e_s} - 1)^2} \frac{p \kappa_2 \kappa_3}{e_s (\kappa_3 + T_c)^2} \approx 0.6964 \text{ g kg}^{-1} \text{K}^{-1}, \tag{E5}$$

873

$$\frac{\partial q_{sat}}{\partial z} = \frac{-\varepsilon}{\left(\frac{p}{e_s} - 1\right)^2} \frac{\frac{p\kappa_2 \Gamma_d \kappa_3 e_s}{(\kappa_3 + T_c)^2} - \rho g e_s}{e_s^2} \approx -0.0055 \text{g kg}^{-1} \text{m}^{-1}, \tag{E6}$$

which yields results similar to the linear fit coefficients in Fig. 7-a. This indicates that even with the assumptions made here, the linear relationship between  $z_i$ ,  $\theta_l^{\text{BL}}$ , and  $q_t^{\text{BL}}$  closely follows the saturation condition.

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# APPENDIX F

Fig. F1 here

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# 1027 LIST OF TABLES

1028 1029 1030	Table 1.	Statistics for the variables considered in the MLM initialization and comple- mentary variables for describing the cloudy states, corresponding to the 195 available days. Original and STI derived states are included
1031 1032	Table 2.	Comparison of dissipation time trends for different variables; single variable changes from a reference case, and when all variables co-vary. Only the most
1033		robust trends are included

TABLE 1. Statistics for the variables considered in the MLM initialization and complementary variables for describing the cloudy states, corresponding to the 195 available days. Original and STI derived states are included.

		Orig	inal value	s		
Variable	Units	Min	Max	Median	Mean	SD
$q_t^{\mathrm{BL}}$	$\rm g \ kg^{-1}$	7.557	16.38	11.51	11.52	1.494
$\Delta_i q_t$	$\rm g \ kg^{-1}$	-10.89	-2.513	-7.246	-7.091	1.758
$q_t^{3\mathrm{km}}$	${\rm g}~{\rm kg}^{-1}$	0.5531	12.59	4.217	4.424	2.278
$\theta_l^{\mathrm{BL}}$	К	287.9	298	291.8	291.7	1.697
$\Delta_i \theta_l$	K	5.679	19.53	11.04	11.3	2.538
		STI mo	odified val	ues		
Variable	Units	Min	Max	Median	Mean	SD
$q_t^{\mathrm{BL}}$	${\rm g~kg^{-1}}$	7.557	16.38	11.38	11.43	1.532
$\Delta_i q_t$	$\rm g \ kg^{-1}$	-10.82	-2.513	-7.243	-7.073	1.749
$q_t^{3\mathrm{km}}$	$\rm g \ kg^{-1}$	0.2555	12.59	4.077	4.358	2.321
$\theta_l^{\mathrm{BL}}$	К	288.1	298	291.8	291.7	1.692
$\Delta_i \theta_l$	К	5.679	19.53	11.04	11.32	2.531
		Uncha	anged valu	ies		
Variable	Units	Min	Max	Median	Mean	SD
zi	m	181	1493	587	597.8	190.8
Zit	m	322	1602	805	843.6	191.7
$\theta_l^{3km}$	K	304.8	324.4	317	316.8	3.391
$\overline{u}$	${\rm m}~{\rm s}^{-1}$	1.543	4.148	2.458	2.531	0.4971
SLP	hPa	1008	1017	1012	1013	1.716
D	$10^{-6} \ {\rm s}^{-1}$	-3.167	14.11	3.442	3.696	2.865
Во	-	0.2293	1.563	1.053	1.047	0.1778
$SW_i$	${\rm W}~{\rm m}^{-2}$	827.4	989.5	977.5	961.5	33.75
LHF	${\rm W}~{\rm m}^{-2}$	8.385	75.18	31.82	32.54	11.44
SHF	${\rm W}~{\rm m}^{-2}$	1.222	19.24	8.661	8.829	3.312
SST	К	290.6	298.7	295	294.7	1.891
$T_{sky}$	K	255.7	291	272.4	272.2	6.608
		Deri	ved value	s		
Variable	Units	Min	Max	Median	Mean	SD
z <sub>b</sub>	m	159	1139	448	458.9	142.3
h	m	4	423	125	138.9	81.53
$\Delta_i \theta_v$	К	4.607	18.48	9.281	9.525	2.41

	1D Trend	Units Single variations		Co-variability trends	
			(95% CI)		
	$\delta z_i / \delta t_{diss}$	${\rm m}{\rm h}^{-1}$	50.40	163.9 (130.6,219.8)	
	$\delta q_t^{ m BL}/\delta t_{diss}$	$\mathrm{g}\mathrm{kg}^{-1}\mathrm{h}^{-1}$	0.359	-2.826 (-5.465,-1.905)	
	$\delta \Delta_i  heta_l / \delta t_{diss}$	${\rm K}~{\rm h}^{-1}$	3.398	5.627 (3.571,13.27)	
	$\delta$ SHF $/\delta t_{diss}$	$\mathrm{W} \ \mathrm{m}^{-2} \ \mathrm{h}^{-1}$	-26.35	-9.974 (-48.24,-5.562)	
$\delta T_{sky}/\delta t_{diss}$ K h $^{-1}$		${\rm K}~{\rm h}^{-1}$	-8.556	-15.92 (-42.75,-9.781)	
1D Trend Units		Units	Cloud thickness	Co-variability trends	
			variations $(h _{z_i})$	(95% CI)	
	$\delta h/\delta t_{diss}$	${\rm m}~{\rm h}^{-1}$	78.74	319.6 (190.6,989.7)	
2D Trend Units		Units	Constant thickness	Co-variability trends	
			variations $(z_i _h)$	(95% CI)	
	$\delta z_i / \delta t_{diss}$	$m h^{-1}$	320.9	171.1 (130.1,249.7)	
	$\delta q_t^{ m BL}/\delta t_{diss}$	$\mathrm{g}\mathrm{kg}^{-1}\mathrm{h}^{-1}$	-1.891	-21.11 (7.486,-4.380)	

TABLE 2. Comparison of dissipation time trends for different variables; single variable changes from a refer ence case, and when all variables co-vary. Only the most robust trends are included.

# 1039 LIST OF FIGURES

1040 1041 1042 1043 1044 1045 1046 1047 1048 1049	Fig. 1.	Two columns are simulated to account for sea-breeze advection. Ocean and land column states are described by their height $z_i$ , moisture $q_l(z)$ , and temperature $\theta_l(z)$ ; from which the liquid water profile $q_l(z)$ and cloud-base height $z_b$ can be derived. Ocean and land have different surface flux conditions, with the ocean having prescribed fluxes of LHF and SHF, while over land the net surface radiative flux $F_0$ is partitioned using a Bowen ratio Bo. At the cloud top, both columns are affected by the net radiative flux $F_i$ and entrainment fluxes that depend on the inversion jumps. Entrainment mixes air into the columns at a rate $w_e$ , while subsidence reduces column height at a rate $w_{sub}$ . The properties of the ocean column are advected onto the land column with a wind speed $u$ and considering a distance $\Delta x$ (see Eq. B5).	 60
1050 1051 1052	Fig. 2.	Mixed-layer idealization for 21 July 2014. We detect the inversion region from radiosonde data (gray), and compute a well-mixed profile (black) by averaging properties in the ABL and tropospheric regions. The well-mixed profile is compatible with the MLM.	 61
1053 1054 1055 1056	Fig. 3.	Effect of the steady thickness initialization (STI) for 21 July 2014. The changes to the original sounding (dashed lines) for (a) $\theta_l(z)$ and (b) $q_t(z)$ are shown in solid lines. MLM simulated cloud boundaries $z_i$ and $z_b$ for the (c) ocean and (d) land column for the original properties and the modified STI.	62
1057 1058 1059 1060	Fig. 4.	Correlation coefficient matrix for variables spanning the 195 selected days grouped by their relationship: (a) seasonal trends, (b) initial conditions, (c-d) boundary forcings divided into two figures for easier presentation: (c) wind and surface fluxes variables and (d) large scale and radiation parameters. The sign is representative of each correlation coefficient.	 63
1061 1062 1063 1064 1065 1066	Fig. 5.	(a) shows the distribution of dissipation time $t_{diss}$ over coastal land. (b-r) show the effects of all variables on $t_{diss}$ for all 195 days. Raw data (grey dots) and a linear fit (dashed black) are shown for the dissipating cases. Distributions (gray box plots) are shown for the persisting cases (marked as P in the $t_{diss}$ axis), with boxes marking the 25 and 75 percentiles, circle marking the median, and lines extending between minimum and maximum (excluding outliers).	 64
1067 1068 1069 1070 1071 1072 1073 1074	Fig. 6.	Effect on dissipation time over land of the change of a single variable for the idealized reference case of observed medians. Variables are shown in terms of their Z-score, computed by subtracting the observed mean and dividing by the observed standard deviation. (a) Changes of initial condition variables one at a time, (b) changes of $z_i _h$ to maintain constant cloud thickness and the corresponding values of $q_t^{BL}(z_i _h)$ , and changes of $h _{z_i}$ maintaining constant $z_i$ and the corresponding changes of $q_t^{BL}(h _{z_i})$ , (c) changes in advection and land surface forcing variables, (d) changes in radiative, subsidence and SLP variables. Some trends include less than five points as clouds were not present for some configurations.	 65
1075 1076 1077	Fig. 7.	Relationships between triads of variables: (a) $q_t^{\text{BL}}$ in the plane described by $z_i$ and $\theta_l^{\text{BL}}$ , and (b) $h$ in the plane described by $z_i$ and $\Delta_i \theta_l$ . Gray dots are data points and contours are the best linear fit per the fit equation shown on top.	66
1078 1079 1080	Fig. 8.	Two-dimensional variable spaces for (a) $z_i$ and $q_t^{\text{BL}}$ , (b) $z_i$ and $h$ , (c) $z_i$ and $\Delta_i \theta_l$ , and (d) $\overline{u}$ and $h$ . Data are classified by: cases that persist for the whole day (black asterisks, 38 cases), and cases that dissipate during the day (dots colored by dissipation time, 157 cases).	 67
1081 1082	Fig. B1.	(a) Sky effective radiative temperatures for the 209 cloudy days dataset as a function of water content above the cloud and below 3 km. The sky effective radiative temperatures	

1083 1084 1085	were obtained with Streamer (Key and Schweiger 1998). (b) Climatological daily wind profile for the NKX station (10-year average), showing the original wind speed profile and the wind speed normalized by its 16 h average.	58
<ul> <li>1086 Fig. F1</li> <li>1087</li> <li>1088</li> </ul>	• Cloud evolution properties for the ocean (upper row) and land (lower row) columns, for single variable changes of (a) $\Delta_i \theta_l$ , (b) SHF, and (c) $T_{sky}$ over the idealized reference case. From left to right, they show: cloud boundaries, entrainment rate, $q_t^{\text{BL}}$ , $\Delta_i q_t$ , $\theta_l^{\text{BL}}$ , and $\Delta_i \theta_l$ .	59



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