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### **Authors**

Gyulassy, M.  
Plumer, M.

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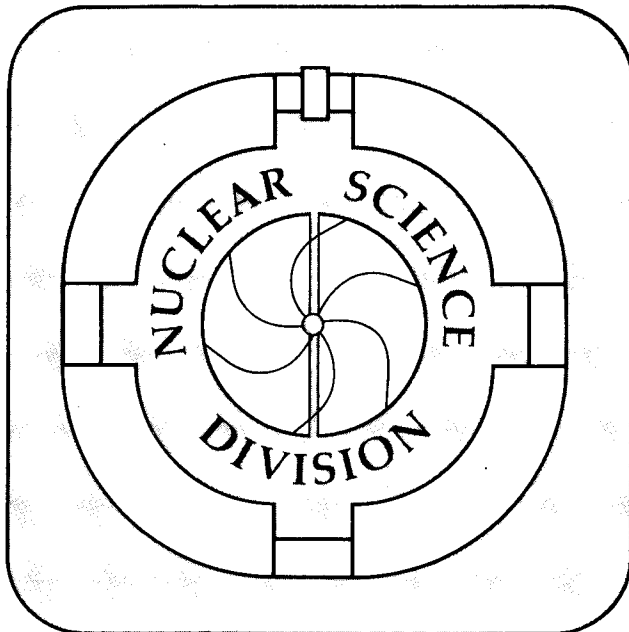
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## Testing String Dynamics in Lepton Nucleus Reactions

M. Gyulassy and M. Plümer

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## Testing String Dynamics in Lepton Nucleus Reactions\*

Miklos Gyulassy<sup>1</sup> and Michael Plümer<sup>2</sup>  
 Nuclear Science Division  
 Lawrence Berkeley Laboratory  
 Berkeley, CA 94720 USA

## Abstract:

The sensitivity of nuclear attenuation in 10-100 GeV lepton nucleus ( $\ell A$ ) reactions to space-time aspects of hadronization is investigated within the context of the Lund string model. We consider two mechanisms for attenuation in a nucleus: (1) final state cascading and (2) string flip excitations. Implications for the evolution of the energy density in nuclear collisions are discussed.

## 1 The Formation Length in String Models

A successful string phenomenology of hadronic multiparticle production in  $e^+e^-$ ,  $pp$ ,  $pA$  and  $AA$  collisions has been developed by the Lund[1,2] and Saclay[3] groups. The relativistic space-time picture of hadronization implied by such models however has not yet been adequately tested. Deep inelastic lepton nucleus ( $\ell A$ ) reactions provide an ideal testing ground for string dynamics because the initial string configuration is under direct experimental control and only one string is excited. We therefore apply the basic concepts of these models (concerning string excitation, scattering and fragmentation) as well as the available Monte Carlo routines [4,5] as the input for our analysis of nuclear effects on distributions of secondaries in such reactions. This report is condensed from ref. [6], where more details and discussion can be found.

A string is specified by its light cone momenta  $E^\pm = E \pm P_z$ , its transverse momentum  $\mathbf{P}_\perp$  and the quark flavors at the ends. We neglect here possible kinks corresponding to gluon jets. While the string models used in phenomenological applications do not contain any configuration space description of either string

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motion or string fragmentation, a natural space-time picture follows[1] if a string is interpreted as a system of two relativistic point particles in 1+1 dimensions bound by a linear (confining) potential  $V = \kappa r$ , where  $\kappa$  is the string tension. The corresponding equations of motion describe relativistic “yoyos”, and momentum space diagrams (such as Fig. 1) can be mapped onto coordinate space simply by rescaling momenta with a factor  $1/\kappa$ . In particular, the length scale characteristic of the yoyo motion of a string of energy  $E$  is then given by  $L = E/\kappa$ . In this paper we study the consequences of only this particular extension of the string models into phase space.

Thus, we assume that Fig. 1 describes the formation and fragmentation of a  $(\bar{q}q)$ -string in an inelastic electron hadron collision both in momentum and coordinate space. The fragmentation of a string with end point flavors  $\bar{q}_0 q_0$  in Fig. 1 proceeds by creating pairs,  $q_i \bar{q}_i$ , at light cone coordinates,

$$C_i = [z_i^+, z_i^-] \equiv [t_i + z_i, t_i - z_i].$$

The  $i$ th rank hadron is formed out of  $\bar{q}_{i+1}$  and  $q_i$  whose trajectories cross at points  $Y_i = [z_i^+, z_{i+1}^-]$ . The classical string equations then imply that the light cone momenta of the  $i$ th rank hadron are

$$p_i^\pm = \pm \kappa (z_i^\pm - z_{i+1}^\pm) . \quad (1)$$

Fig. 1 clearly reveals the ambiguity inherent in the definition of hadronic formation lengths emphasized in ref.[7]. One simple possibility is to assume that the rank  $i$  hadron can rescatter only beyond its “yoyo-point”  $Y_i$  where the trajectories of  $\bar{q}_{i+1}$  and  $q_i$  intersect for the first time, at a longitudinal distance

$$\ell_y(i) = \frac{1}{2}(z_i^+ - z_{i+1}^-) - \frac{1}{2}(z_0^+ - z_0^-) ,$$

from the point  $[z_0^+, z_0^-]$ , where the initial quark,  $q_0$ , was knocked out. Alternatively, it could be that its constituent antiquark  $\bar{q}_{i+1}$  with its associated color string can begin to interact with the nuclear medium immediately after it is created at  $C_{i+1}$ . This would correspond to a smaller effective formation length

$$\ell_c(i) = \frac{1}{2}(z_{i+1}^+ - z_{i+1}^-) - \frac{1}{2}(z_0^+ - z_0^-) .$$

We refer to  $\ell_y$  and  $\ell_c$  as the yoyo formation length and the constituent formation length, respectively, as in ref.[7].

For the Lund string, one finds that the mean values of  $\ell$  as a function of  $x$  qualitatively behave like  $\ell_y(x) \sim xL$  and  $\ell_c(x) \sim x(1-x)L$  (a detailed discussion as well as analytic expressions for  $\ell(x)$  for certain simple fragmentation models may be found in [7]). Clearly, the ambiguity is maximal in the limit  $x \rightarrow 1$ , where  $\ell_c \rightarrow 0$  while  $\ell_y \rightarrow L$ .

In applying the Lund model to  $\ell A$ , we assume first that fragmentation is independent of the nuclear medium and proceeds as in free space as shown in Fig. 1. For

a given exclusive fragmentation event specifying the final momenta and flavors of the produced hadrons, the coordinate space points  $C_i$  are computed by inverting (1). In this way we compute the yoyo and constituent formation lengths for all produced hadrons in an event. Given a choice of the effective formation length specifying the point beyond which intranuclear cascade is turned on, our next main dynamical assumption is that the Lund/Fritiof algorithm provides the basic mechanism for subsequent hadron excitations via intranuclear cascading. The final assumption is that the fragmentation of all excited strings produced during cascading can be treated independent of the nuclear medium.

In the Fritiof algorithm [2] two interacting strings specified by light cone momenta  $E_i^\pm$  interact by sharing their light cone momenta and ending up with  $(x^+ E^+, (1-x^-)E^-)$  and  $((1-x^+)E^+, x^- E^-)$ , respectively. The light cone fractions  $x^\pm$  are assumed to be distributed according to the scaling distribution,  $dx^\pm/x^\pm$ , and the fragmentations of the newly excited strings all proceed independently. That model successfully describes many features of the data on  $pA$  and  $AA$  at energies  $\gtrsim 20 A$  GeV to the 20% level. However, it should be kept in mind that in our application, the secondary cascading processes generally involve only intermediate energies  $\lesssim 10$  GeV due to the finite size of nuclei. This represents a considerable extrapolation down from the well tested domain and is one of the sources of theoretical uncertainty. For example, at these energies production of discrete hadron resonances may be important, while in this model only a continuous distribution of excited string configurations is considered. It will be important to compare this model of cascading with future  $pA$ - and  $\pi A$ -data at intermediate energies to assess the magnitude of uncertainties resulting from this dynamical approximation.

Ultimately, the questions of whether attenuation due to hadronic cascading in the nuclear medium starts at  $\ell_y$  or at  $\ell_c$ , or at some different point, and what is the proper dynamical framework for final state cascading can only be answered by the experiment. As we show next, the resolution of those questions has significant impact for the ongoing discussion about the possibility of creating a quark-gluon-plasma in the relativistic nucleus nucleus collision experiments at CERN and at BNL.

For a 200  $A$  GeV oxygen beam interacting with  $Au$  target nuclei, Fig. 2 shows the evolution of the energy density (as calculated with the ATTILA version of the Fritiof code [8] which incorporates the extension of the Lund model to coordinate space along the lines discussed here). The energy density in a central (zero impact parameter)  $O + Au$  collision at 200  $A$  GeV was calculated in a cylinder of radius 1 fm and length 1 fm in the center of mass system as a function of time. The space-time origins of  $\sim 70$  excited baryon strings was distributed with a Gaussian distribution of rms  $R_O \approx 2.7$  fm in the transverse direction and in an approximately rectangular region of light cone coordinates of width  $\Delta z^\pm \approx 2R_{Au}/\gamma, 2R_O/\gamma$  with  $\gamma = 10$ . Each string then was allowed to fragment independently and the formation points  $C_i$  or  $Y_i$  were computed for each event. A produced particle was added to the energy density at the formation time if its coordinates happened to fall into the

computational cylinder. After production the hadrons are assumed to propagate on straight line trajectories with their initial velocities.

The full curve shows the results assuming that the yoyo length is the relevant formation length for the case  $\kappa = 1$  GeV/fm. The dashed curve shows that the energy density could get  $\sim 50\%$  larger and the interesting period where  $\epsilon \gtrsim 1$  GeV/fm<sup>3</sup> could last much longer if the constituent length were the relevant scale. The dashed-dot curve shows that if the effective tension scale were 2 GeV/fm, then significantly higher energy densities could be achieved. The point that we wish to emphasize is the sensitivity of the initial energy density to assumptions of the formation length. The actual maximum energy densities and their temporal profiles will of course also depend on the assumed cascading dynamics, but Fig. 2 serves to indicate the order of magnitude of the differences between different formation length assumptions. The information gained from  $\ell A$  reactions is therefore essential to constraints of the space-time evolution of  $AA$  collisions.

## 2 Final State Cascading

### 2.1 Schematic Model

To get a qualitative understanding of the expected  $A$  dependence of particle production in  $\ell A$  collisions, consider the schematic model illustrated in Fig. 3, where the  $z$ -axis is chosen in the direction of the 3-momentum of the virtual photon,  $\Delta$  denotes the dimension of the nucleus in this direction, and  $z_0$  ( $0 \leq z_0 \leq \Delta$ ) denotes the position of the  $\gamma^* N$  vertex. We assume that a hadron formed initially with an energy fraction  $x_0$  can rescatter on target nucleons only beyond its formation point  $z_0 + \ell(x_0)$  and of course only if  $\Delta - z_0 - \ell(x_0) \geq 0$ .

As a measure of that rescattering, we study the distribution

$$D_{eA}(x) \equiv \frac{1}{\sigma_{eA}} \frac{d\sigma_{eA}}{dx} \quad (2)$$

In terms of a multiple collision expansion, this can be written as

$$D_{eA}(x) = \int_0^\Delta \frac{dz_0}{\Delta} \int_x^1 dx_0 D(x_0) \sum_{n \geq 0} P_n(x_0, z_0) K_n(x_0, x) \quad (3)$$

where  $D(x) \equiv D_{eN}(x)$  is the initial  $x$  distribution of secondaries resulting from the fragmentation process (Fig. 1).  $P_n(x_0, z_0)$  is the probability that a hadron, with energy fraction  $x_0$  and formed from a string originating at the point  $z_0$ , scatters  $n$  times in the target. The scattering kernel  $K_n(x_0, x)$  specifies the cascade dynamics and the probability that after  $n$  collisions the hadron retains a fraction  $x$  of the initial quark energy.

For a slab of uniform density  $\rho_0$  and thickness  $\Delta$ ,

$$P_n(x, z_0) = \Theta(z_0 + \ell(x) - \Delta) \delta_{n0} \quad (4) \\ + \Theta(\Delta - z_0 - \ell(x)) \frac{1}{n!} \left( \frac{\Delta - z_0 - \ell(x)}{\lambda} \right)^n \exp \left( - \frac{\Delta - z_0 - \ell(x)}{\lambda} \right)$$

where  $\lambda \equiv (\rho_0 \sigma)^{-1}$  is the hadron's mean free path in the target nucleus and  $\sigma$  is the hadron-nucleon inelastic cross section. The integration over the initial vertex position only affects the rescattering probability, and thus

$$D_{eA}(x) = \int_x^1 dx_0 D(x_0) \sum_{n \geq 0} P_n(x_0) K_n(x_0, x) \quad (5)$$

where

$$P_n(x) = \delta_{n0} \left[ \Theta(\ell(x) - \Delta) + \Theta(\Delta - \ell(x)) \frac{\ell(x)}{\Delta} \right] + \Theta(\Delta - \ell(x)) \frac{\lambda}{\Delta} \left[ 1 - \sum_{j=0}^n \frac{1}{j!} \left( \frac{\Delta - \ell(x)}{\lambda} \right)^j \exp \left( -\frac{\Delta - \ell(x)}{\lambda} \right) \right] \quad (6)$$

Data on the  $A$  dependence of distributions of secondary hadrons are usually presented in terms of the ratio

$$\mathcal{R}_A(x) \equiv \frac{1}{\sigma_{eA}} \frac{d\sigma_{eA}}{dx} \bigg/ \frac{1}{\sigma_{eN}} \frac{d\sigma_{eN}}{dx} \quad (7)$$

Note that  $\mathcal{R}_A(x) \equiv D_{eA}(x)/D_{eN}(x)$ , and that  $\mathcal{R}_A(x) \equiv 1$  in the absence of final state cascading. While the  $n = 0$  contribution to  $\mathcal{R}_A$  depends only on nuclear geometry and on the formation length  $\ell(x)$ , the contributions from hadrons that have been rescattered  $n \geq 1$  times depend on the dynamics of the rescattering process through the  $K_n(x_0, x)$  which in turn depend on the degree of inelasticity and nuclear stopping power. For the sake of illustration, consider the case of a fixed inelasticity  $(1 - \alpha)$  associated with every single collision, i.e.  $K_n(x_0, x) = \delta(x - \alpha^n x_0)$ . In this case

$$\mathcal{R}_A(x) = P_0(x) + \sum_{n \geq 1} P_n(x/\alpha^n) \frac{1}{\alpha^n} \frac{D(x/\alpha^n)}{D(x)} \Theta(1 - x/\alpha^n) \quad (8)$$

The resulting ratio  $\mathcal{R}_A(x)$  is sketched in Fig. 4 for the yoyo and for the constituent formation model, respectively. In the kinematic region where the extension of the string is comparable to the nuclear dimensions,  $E_{lab} \sim 10$  GeV, one finds that in the high and intermediate  $x$  region  $\mathcal{R}_A(x)$  will be dominated by the survival probability  $P_0(x)$ , while hadrons that suffer  $n \geq 1$  collisions will typically contribute in the region below  $x \sim \alpha^n$ . Here, we would like to emphasize that

- The  $n = 0$  contribution to  $\mathcal{R}_A(x)$  is simply  $P_0(x)$  and depends on the dimensionless ratios  $n_\Delta \equiv \Delta/\lambda$  and  $n_L \equiv L/\lambda = \nu/(\kappa\lambda)$  which can be varied experimentally by varying  $A$  and  $E_{lab}$ . It also depends on the model dependent functional form of  $\ell(x)/L$ .
- The  $n \geq 1$  contributions depend in addition on the inelasticity distribution (the parameter  $\alpha$  in our schematic model).



## 2.2 Monte Carlo Model

We now introduce a Monte Carlo model of hadronic cascading in lepton nucleus collisions that includes effects of multistring excitation, rescattering and fragmentation in a way consistent with the momentum space description of the Lund/Fritiof models [1,2]. We investigate the consequences of three different assumptions concerning which formation length is relevant for the onset of hadronic cascading: (a) the yoyo formation length, (b) the constituent formation length and (c) zero formation length ( $\ell(x) \equiv 0$ ). This model contains the following basic steps:

1. The initial ( $qq-q$ ) string configuration in an inelastic lepton nucleon scattering process is set up by calling the appropriate Lund routine, LEPTO4.3 [5], and the space coordinate of the target nucleon involved in the initial  $\ell N$  collision is randomly selected according to a three parameter Woods-Saxon distribution.

2. The first generation (=primary) hadrons produced in the fragmentation of the initial string are allowed to rescatter within the nucleus. For each primary hadron of momentum  $\mathbf{p}$  the formation point  $\mathbf{r}_p$  is computed depending on the model for  $\ell(x)$ . The mean number of inelastic collisions  $\langle n \rangle$  is calculated assuming straight line propagation,

$$\langle n \rangle = \sigma \int_0^\infty ds \rho(\mathbf{r}_p + s \hat{\mathbf{p}}) \quad (9)$$

where  $\sigma$  is the inelastic cross section (taken to be 20 mb for mesons, and 30 mb for baryons) and  $\hat{\mathbf{p}}$  is the unit vector in the direction of the hadron's 3-momentum. The actual number of inelastic collisions that hadron suffered is then chosen from a Poisson distribution,

$$P(n) = \frac{\langle n \rangle^n}{n!} \exp(-\langle n \rangle) \quad (10)$$

The  $n$  subsequent collisions are processed according to the Fritiof string-string scattering algorithm [2], where each of the colliding hadrons (=strings) can be excited to a higher mass  $M$  according to a  $M^{-1}$  law.

3) Finally the fragmentation of all excited strings in the final state is executed according to the Lund JETSET6.3 routine [4].

Below, we show results obtained for 14.5 GeV/c electrons scattering on noble gas targets up to xenon. All distributions and observables relate to the rest frame of the target nucleus. For the kinematic variables, the cuts

$$4 \text{ GeV} \leq \nu \leq 11 \text{ GeV}$$

$$4 \text{ GeV}^2 \leq Q^2$$

$$0.25 \leq x_{Bj} \leq 1$$

$$3 \text{ GeV} \leq W \leq 4 \text{ GeV}$$

were applied. Unless explicitly stated otherwise, calculations were done for the canonical parameter value of the string tension,  $\kappa = 1 \text{ GeV/fm}$ . The limit of large

string tension corresponds to the case of vanishing formation length. Thus, the curves labeled  $\kappa = 10$  GeV/fm refer to that limit,  $\ell \approx 0$ .

For  $e + Xe \rightarrow \pi^+$  distribution in the variable  $x = E/\nu$  is plotted in Fig. 5 for various formation models. Clearly, on an absolute scale the differences between the constituent case and the yoyo case (the latter is approximately the same as the case of  $eN$ ) are modest and high precision data are essential for comparison. The differences however can be amplified considerably by triggering on high multiplicities. In Fig. 6 the contributions from different multiple collision components of the ratio  $\mathcal{R}_{Xe}(x)$  are shown for the case of the constituent formation length.

### 2.3 Comparison with Data

Next, we compare results of our Monte Carlo model to data on the nuclear attenuation of hadron production in the forward region in inelastic lepton nucleus reactions. The low energy data, at  $\langle \nu \rangle = 10$  GeV, are taken from an early SLAC experiment [9] that used a 20 GeV/c electron beam. The more recent high energy data were obtained by the EMC [10,11] with 200 GeV/c incident muons. Here, we shall concentrate on the heaviest target nuclei available in both experiments,  $Cu$  and  $Sn$ , where the observed effects of intranuclear cascading are strongest.

In Fig. 7, EMC- and SLAC-data on the ratio of integrated particle yields,

$$\bar{\mathcal{R}}_A \equiv \int_{x_{min}}^1 dx \frac{1}{\sigma_{eA}} \frac{d\sigma_{eA}}{dx} \bigg/ \int_{x_{min}}^1 dx \frac{1}{\sigma_{eN}} \frac{d\sigma_{eN}}{dx} \quad (11)$$

are plotted as a function of  $\nu$  for  $Cu$  target nuclei, and compared to Monte Carlo results for the three formation models. The data correspond to cutoff values  $x_{min} = 0.2$  (EMC) and  $x_{min} = 0.4$  (SLAC), all theoretical calculations correspond to  $x_{min} = 0.2$ .

For the constituent formation model (histograms labeled  $C$ ), we have included both the total ratio (solid curve) and the separate contribution of the zero scattering component (dashed curve). The difference between the two curves for  $\nu \lesssim 40$  GeV is due to the fact that the  $n \geq 1$  contribution of rescattered secondaries begins to contribute significantly in the region  $x \lesssim 0.3 - 0.4$  as can be seen in Fig. 6. For  $\nu \gtrsim 50$  GeV, the difference between the histograms becomes comparable to the statistical fluctuations in the Monte Carlo run ( $\Delta \bar{\mathcal{R}}_A \sim 0.03 - 0.04$ ). We note that our results for the  $n = 0$  component are consistent with those obtained from a semi-analytical calculation in ref.[12]. The only significant discrepancy between theory and experimental data concerns the data point at  $\nu = 10$  GeV from the SLAC experiment. We have checked that this is *not* a consequence of the higher cutoff in  $x$  for these data. The  $n = 0$  contribution of  $\mathcal{R}_A(x)$  (i.e.,  $P_0(x)$ ) is rather weakly dependent on  $x$  (cf. Fig. 6).

On the other hand, both the yoyo formation model and the Glauber limit,  $\ell \equiv 0$ , (histograms labeled  $Y$  and  $G$ , respectively) appear to be ruled out by the data, as they fail to reproduce the experimentally observed  $\nu$  dependence over a wide range

of energies (we note that for the  $\ell \equiv 0$  case the decrease of  $\bar{\mathcal{R}}_A$  with increasing  $\nu$  in the low  $\nu$  regime results from finite energy effects, since the variable  $x = E/\nu$ , unlike  $x^+$ , is not invariant).

Thus, at this point we may conclude (in agreement with refs.[10,12]) that the  $\nu$  dependence of the nuclear attenuation effect clearly favors the constituent formation model over both the yoyo formation model and the Glauber limit.

However, the discrepancy with the  $\nu = 10$  GeV data becomes much more pronounced if one considers the  $x$  dependence of the effect, as can be seen in Fig. 8 (note that here the SLAC-data are plotted against the Feynman variable in the hadronic CM frame  $x_F$ , the EMC-data against  $x \equiv E/\nu$ ). We compare our results to data obtained with  $Sn$  targets, at  $\langle \nu \rangle = 10$  GeV [9] and at  $\langle \nu \rangle = 62$  GeV [10]. As in Fig. 7, the solid curves labeled  $C$ ,  $Y$  and  $G$  correspond to the constituent formation length, the yoyo formation length and the Glauber limit  $\ell \equiv 0$ , respectively. For  $\langle \nu \rangle = 62$  GeV, the yoyo curve is equal to unity (within the statistical errors of the Monte Carlo run) and has been omitted from Fig. 8. As before, the constituent formation model gives reasonable agreement with the EMC-data but fails to fit the low energy SLAC-data. In the region of intermediate  $x_F$ , the SLAC-data are not well described by any of the curves that correspond to a finite formation length, but are consistent with  $\ell \approx 0$ . In the low  $x_F$  region dominated by the contribution from secondary cascading, they disagree with all three model calculations. In fact, the weak  $x_F$  dependence exhibited by the data would seem to suggest that only the zero rescattering component contributes significantly to particle production in the forward region (see also Fig. 6). At this point one might be tempted to speculate that the assumption of zero formation length together with higher inelasticities could indeed offer a consistent explanation of the data. However, as can be seen both from Fig. 7 and from the  $\langle \nu \rangle = 62$  GeV plot, a vanishing formation length completely fails to describe the observed  $\nu$  dependence.

Thus, none of the formation zone scenarios is able to fit the combined  $\nu$ ,  $x$  and  $A$  dependence of the observed nuclear attenuation effect. Previous studies that managed to fit the  $x$  dependence of the SLAC-data did so at the cost of either neglecting the secondary cascading ( $n \geq 1$ ) contribution [10,13] or of adopting scenarios [14,15] that do not yield the recently observed energy dependence. Thus, the model of ref.[15] describes a simple inside-outside cascade scenario (cf. eq.(1)), with an extreme  $\kappa_{eff} \approx 7$  GeV/fm, and ref.[14] corresponds to a Glauber model ( $\ell = 0$ ) for intranuclear scattering of the leading quark of the initial ( $qq-q$ ) string configuration, with an energy independent ansatz for the inelasticity distribution.

Unfortunately, the results of the SLAC experiment are the only data presently available in the (interesting) low energy regime. Clearly, at this point it is highly desirable to get new and more sensitive experimental data at  $\nu \sim 10$  GeV. If the earlier observations were confirmed, one would have to conclude that the effects of final state cascading alone cannot account for the observed nuclear attenuation of particle production in the forward region. Since the formation model calculations discussed above all assume the absence of interactions before the onset of

secondary cascading, it may be important to explore whether the discrepancies can be reduced by allowing strong interaction with the nuclear medium prior to the fragmentation of the original  $qq$ - $q$  string configuration into final state hadrons. One possible mechanism is studied in the next section.

### 3 A String Flip Scenario

We now consider the possibility that the hadronization mechanism is strongly influenced by the presence of the nuclear medium.

Specifically, we adopt a color string flip model as illustrated in Fig. 9 (where for simplicity  $\bar{q}q$  rather than  $qq$ - $q$  strings are presented). Our model is based on the observation that on its passage through the nucleus, the leading quark  $q_0$  of the initial jet ( $\bar{q}_0q_0$ ) can interact by exchanging color with partons  $q_i$  ( $i = 1, \dots, n$ ) of other target nucleons. The initial string can thus be successively “reconnected” to different color sources  $\bar{q}_i$  along its path, possibly forming a number of different string configurations

$$\gamma^*A \rightarrow (\bar{q}_0q_1) + (\bar{q}_1q_2) + \dots + (\bar{q}_{n-1}q_n) + (\bar{q}_nq_0) + (A - n - 1)$$

Eventually, the  $n + 1$  color singlet strings fragment into secondary hadrons which in turn may rescatter on target nucleons. Thus, the hadron cascading scenario described above corresponds to the limit of a mean free path  $\lambda$  for string flip that is large compared to the nuclear dimensions. For small  $\lambda \ll R$  note that  $q_0$  will be connected to  $\bar{q}_n$  near the nuclear surface and thus, hadronic cascading of secondaries from the fragmentation of the leading  $\bar{q}_nq_0$ -jet will be negligible. On the other hand, strings attached to quarks other than  $q_0$  will end up with rather low masses  $M \approx \sqrt{2\kappa m_N \lambda} \sim 2 \text{ GeV}$ , where  $m_N$  is the nucleon mass. Therefore the cascading of the fragments from intermediate strings ( $\bar{q}_i q_{i+1}$ ) will only contribute very low momentum particles. In this scenario the  $x > 0.1$  region is mainly affected by the reconnection of  $q_0$  from  $\bar{q}_0$  to  $\bar{q}_n$ .

#### 3.1 Schematic Model

As before, it is instructive to consider a schematic model before introducing the complete Monte Carlo description. Initially, the leading quark carries a light cone momentum  $E^+ = m_N + \nu + \sqrt{\nu^2 + Q^2}$ . That means that after traveling a distance  $L \equiv E^+/(2\kappa)$  it has converted its kinetic energy into potential energy and turns around. It can however interact through color exchange at points  $z$  with  $z_0 \leq z \leq \tilde{\Delta}$ , where  $\Delta$  and  $z_0$  are defined as before, and  $\tilde{\Delta} \equiv \min(\Delta, z_0 + L)$ . The probability for  $n \geq 1$  string flips, with the final one occurring at  $z = z_f$ , is

$$P(z_f; z_0) = \frac{1}{\lambda} \exp\left(-\frac{\tilde{\Delta} - z_f}{\lambda}\right) \theta(z_f - z_0) \theta(\tilde{\Delta} - z_f) \quad (12)$$

where  $\lambda \equiv (\rho_0 \sigma_q)^{-1}$  is the string flip mean free path and  $\sigma_q$  the string flip cross section.

After the final interaction, the leading quark remains only with a light cone momentum fraction

$$x^+ = \frac{E^+ - 2\kappa(z_f - z_0)}{E^+} \quad (13)$$

Note that  $x^+ \rightarrow 1$  in the high energy limit  $\nu \gg \kappa\Delta$ .

The fluctuations in  $x^+$  are described by the distribution  $P_0\delta(1 - x^+) + w(x^+)$ , where now

$$P_0 = 1 - \int_0^\Delta \frac{dz_0}{\Delta} \int_{z_0}^\Delta dz_f P(z_f; z_0) \quad (14)$$

and

$$w(x^+) = \int_0^\Delta \frac{dz_0}{\Delta} \int_{z_0}^\Delta dz_f P(z_f; z_0) \delta(x^+ - \frac{z_f - z_0}{L}) \Theta(\tilde{\Delta} - z_f) \quad (15)$$

As before, the results of the schematic model calculations depend on two dimensionless ratios: the number of mean free paths covered by the dimensions of the string and of the nucleus,  $n_L \equiv L/\lambda \approx \nu/(\kappa\lambda)$  and  $n_\Delta \equiv \Delta/\lambda$ , respectively. For the case  $L < \Delta$ , one obtains

$$w(x^+) = \frac{n_L}{n_\Delta} + \left[ \left(1 - \frac{n_L}{n_\Delta}\right) n_L - \frac{n_L}{n_\Delta} \right] \exp(-n_L x^+) \quad (16)$$

$$P_0 = \frac{1}{n_\Delta} + \left[ \left(1 - \frac{n_L}{n_\Delta}\right) - \frac{1}{n_\Delta} \right] \exp(-n_L) \quad (17)$$

and for  $L \geq \Delta$ ,

$$w(x^+) = \frac{n_L}{n_\Delta} [1 - \exp(-n_L(x^+ - x_0^+))] \quad (18)$$

$$P_0 = \frac{1}{n_\Delta} [1 - \exp(-n_\Delta)] \quad (19)$$

where  $x_0^+ \equiv 1 - (n_\Delta/n_L)$  is a lower cutoff in  $x^+$  that results from the assumption of sharp nuclear surfaces ( $z_f - z_0 \leq \Delta$  implies  $x^+ \geq x_0^+$  in the case  $L \geq \Delta$ ).

The ratio  $\mathcal{R}_A(x)$  is then given by

$$\mathcal{R}_A(x) = P_0 + \int_{\max(x_0^+, x)}^1 dx^+ w(x^+) \frac{\frac{x}{x^+} D(\frac{x}{x^+})}{x D(x)} \quad (20)$$

To illustrate the behavior of the ratio  $\mathcal{R}_A$  as a function of  $x$ ,  $\nu$  and  $A$ , let us consider the simple ansatz for the fragmentation function,  $D(x) = \frac{1}{x}$ , corresponding to a uniform rapidity distribution. In the kinematic regime of interest,  $L > \Delta$ , and one finds that

$$\mathcal{R}_A(x) = 1 - \Theta(x - x_0^+) \left[ \frac{\nu}{\kappa\Delta} (x - x_0^+) - \frac{\lambda}{\Delta} \left( 1 - \exp \left\{ \frac{\nu}{\kappa\lambda} (x - x_0^+) \right\} \right) \right]$$

where  $x_0^+ \equiv 1 - (\nu/\kappa\Delta)$ . There is no attenuation (i.e.,  $\mathcal{R}_A(x) = 1$ ) in the interval  $0 \leq x \leq 1 - x_0^+$  (see Fig.10). In the region  $1 - x_0^+ \leq x \leq 1$ ,  $\mathcal{R}_A$  decreases with  $x$ , and the value at  $x = 1$  is given by the zero interaction probability of the leading quark,

$$P_0 = \frac{\lambda}{\Delta} \left[ 1 - \exp\left(-\frac{\Delta}{\lambda}\right) \right].$$

For a given nuclear target,  $P_0$  is independent of the energy transfer  $\nu$  (if we neglect possible effects of an energy dependence of the string flip cross section). Hence, with increasing  $\nu$  the width of the region where attenuation occurs,  $\kappa\Delta/\nu$ , decreases like  $1/\nu$  while the magnitude of the slope at  $x = 1$ ,  $\nu P_0/(\kappa\lambda)$ , increases proportionally to the energy transfer (cf. Fig.10).

For more realistic parametrizations of the fragmentation function, such as  $D(x) = \frac{1}{x}(1-x)^c$  with  $c > 0$ , some attenuation will occur in the region  $x \leq x_0^+$  as well, but qualitatively the behavior of the ratio  $\mathcal{R}_A$  remains the same as for the simple case considered above. That is to say, the attenuation effect disappears in the high energy limit for all  $x < 1$ , and the width of the region below  $x = 1$  where strong attenuation can be observed is of the order  $\sim 1.5 \kappa R/\nu$ . At  $x = 1$ , the ratio  $\mathcal{R}_A$  is simply the zero scattering probability  $P_0$  of the leading quark, i.e., it is determined by nuclear geometry and the string flip interaction cross section.

## 3.2 Monte Carlo Model

The full Monte Carlo version of the string flip model may be considered an extension of the code described in [6] and in section 3.2 above. As before, for each event the original string configuration is determined via the Lund routine LEPTO4.3, and the position of the  $\gamma^*N$  vertex,  $\mathbf{r}_0$ , is chosen according to a three parameter Woods-Saxon distribution  $\rho(\mathbf{r})$ . If  $\hat{\mathbf{p}}_q$  is the unit vector in the direction of the three momentum of the leading quark (or antiquark), the probability that its final color exchange interaction occurs at a distance  $z_f$  from the point  $\mathbf{r}_0$  where it has been created is

$$dP(z_f, \mathbf{r}_0) = \sigma_q \rho(\mathbf{r}_0 + z_f \hat{\mathbf{p}}_q) dz_f \exp\left[-\sigma_q \int_{z_f}^L ds \rho(\mathbf{r}_0 + s \hat{\mathbf{p}}_q)\right] \quad (21)$$

and consequently, the probability for no such interaction to occur is taken to be

$$P_0(\mathbf{r}_0) = \exp\left[-\sigma_q \int_0^L ds \rho(\mathbf{r}_0 + s \hat{\mathbf{p}}_q)\right] \quad (22)$$

If a string flip has occurred, the light cone momenta of the leading string are  $\tilde{E}^+ = x^+ E^+$  and  $\tilde{E}^- = (1 - x^-) E^-$ , where  $E^\pm$  are the light cone momenta of the original  $(\bar{q}_0 q_0)$  string configuration,  $x^+$  is given by eq(16) and  $x^-$  is chosen randomly according to a  $1/x^-$  distribution. Fragmentation of the leading string (or of the initial string, if no string flip has occurred) is processed via the Lund routine JETSET6.3 [4]. We emphasize that in this scenario final state cascading is completely neglected for reasons discussed above. All effects are due to the rewiring of string end points.

### 3.3 Comparison with Data

In Figs.7 and 8, we have included the results for  $\mathcal{R}_A$  obtained for the extreme value of the spin flip cross section,  $\sigma_q = 30$  mb. We note that the  $x$  dependence of the ratio  $\mathcal{R}_A$  exhibits the qualitative features discussed earlier for the case of the schematic model: at  $x = 1$  the ratio is equal to the zero interaction probability of the leading quark, and a significant attenuation effect is found in a region of width  $\sim 1.5 \kappa R/\nu$  below  $x = 1$ . Quantitative differences are due to the more realistic parametrizations of nuclear density distributions and fragmentation functions. In particular, the absence of the constraint  $x^+ > x_0^+$  (which resulted from the assumption of sharp nuclear surfaces), and the fact that the LUND fragmentation function falls almost exponentially as a function of  $x$ ; combine to produce the slower variation of  $\mathcal{R}_A$  with  $x$  in Fig. 7, as compared to Fig.10.

The fit to the EMC-data is better than for the constituent formation model, but there remains a considerable discrepancy with the low energy SLAC-data. Clearly, in the low energy case the model predicts a weaker  $x_F$  dependence of particle attenuation in the forward region than any of the final state cascading scenarios (except for the Glauber limit, which, as we have shown, is ruled out because of the observed  $\nu$  dependence). This trend goes into the right direction, but fails to actually fit the data, which would require an even flatter curve. In contrast, the  $x$  dependence of the  $\langle \nu \rangle = 62$  GeV data is consistent with the string flip approach.

While in Fig. 8 we show only the results for  $\kappa = 1$  GeV/fm and  $\sigma_q = 30$  mb, we have checked that the fit to the low energy data cannot be greatly improved by considering smaller values for the cross section, or different values of the string tension parameter  $\kappa$ . Furthermore, taking into account the effects of final state cascading of secondaries produced in the fragmentation of the leading string does not help much either, as at  $\nu \sim 10$  GeV the yoyo formation scenario gives rise to very small corrections only, and the constituent formation ansatz would reduce the quality of the fit by increasing the slope of the curve for  $\mathcal{R}_A(x_F)$ .

Thus, it appears that if the low energy data were confirmed by new high precision experiments along the lines of [16], they would imply that even the combined effects of string flip color exchange and final state cascading could not account for the observed attenuation of particle production in the forward region at  $\langle \nu \rangle = 10$  GeV.

## 4 Conclusions and Outlook

We have investigated the sensitivity of particle spectra in lepton nucleus reactions on space-time aspects of the hadronization process. The necessary theoretical input for a realistic model of final state cascading consists of

- the momentum space dynamics, specified by the inelastic hadron nucleon cross sections,  $\sigma_{in}(hN)$ , as well as a scattering kernel  $K_n(x_0, x)$  to describe nuclear stopping power, and

- additional model assumptions concerning the mapping of momentum space information onto coordinate space, as specified by the overall length scale  $L \sim \nu/\kappa$  (in terms of the effective string tension parameter  $\kappa$ ) and by the  $x$  dependence of the formation length (the function  $\ell(x)/L$ )

Here, we used the parametrization of phase space distributions provided by the Fritiof/Lund string models [1,2,4,5] as an input. In a Monte Carlo model, we studied the cases where (1) the yoyo formation length or (2) the constituent formation length are taken to determine the onset of intranuclear cascading. As a limiting case, we also considered (3) the Glauber limit, i.e. the case of zero formation length.

We compared our results for the  $\nu$ ,  $x$  and  $A$  dependence of the attenuation effect to data obtained at SLAC [9] and by the EMC [10,11]. The SLAC-data correspond to  $\langle \nu \rangle = 10$  GeV, while the EMC-data cover the range  $15 \text{ GeV} \lesssim \nu \lesssim 200$  GeV. We find that the yoyo formation model and the assumption of zero formation length are both inconsistent with the observed energy dependence of the effect. The constituent formation model is consistent with the  $\nu$  and  $x$  dependence of the EMC-data, but considerably underestimates the attenuation observed in the low energy SLAC-data. In fact, these data cannot be accounted for even in the limit of vanishing formation length.

In order to test for the possibility of strong interactions within the nuclear medium prior to the onset of secondary cascading, we considered a string flip mechanism where the leading quark can interact through color exchange during its passage through the nucleus. We find that such an approach yields a weaker  $x$  dependence than the formation zone models of hadronic cascading, and slightly improves the quality of the fits to the EMC-data, but still fails to fit the low energy SLAC-data which exhibit an even weaker  $x$  dependence in the low  $x$  region.

Again, we would like to emphasize that previous studies which succeeded in fitting the SLAC-data either have done so by ignoring the secondary cascade component or else fail to describe the experimentally observed  $\nu$  dependence.

Unfortunately, in the interesting kinematic region where the attenuation effect becomes prominent, only one set of data are available. Given the difficulty of understanding those data, it would be desirable to confirm and extend the data base through a systematic study of the  $\nu$ ,  $x$  and  $A$  dependence of the attenuation effects. If future high precision experiments (along the lines of the proposal [16]) should indeed confirm the observed strong suppression of hadron production in the forward region, this may point to a basic flaw in present models of the space-time evolution of hadronization. That may in turn have other important implications, e.g., for estimates of the energy densities produced in high energy heavy ion collisions.



## Figure Captions

- Fig. 1** String excitation and fragmentation in the Lund model for an inelastic electron hadron collision.  $C_i$  and  $Y_i$  are the constituent formation point and the yoyo formation point of the hadron of rank  $i$ , respectively.
- Fig. 2** Time evolution of the central energy density in 200 A GeV  $O+Au$  collisions, for various formation zone models.
- Fig. 3** Schematic picture of hadronic cascading in  $eA$ . The figure illustrates the notation employed in section 2.
- Fig. 4** Qualitative behavior of the ratio  $\mathcal{R}_A(x)$  for the constituent and for the yoyo formation model, in the kinematic regime  $\nu \sim \kappa R$ . For the constituent case, the separate contributions due to hadrons that suffered a specific number  $n$  of inelastic collisions are shown.
- Fig. 5** Distribution of positively charged pions per inelastic event in the variable  $x = E/\nu$ .
- Fig. 6** The ratio  $\mathcal{R}_A(x)$  for the constituent formation zone models. with the separate contributions due to hadrons that suffered a specific number  $n$  of inelastic collisions.
- Fig. 7** The  $\nu$  dependence of the ratio  $\bar{\mathcal{R}}_A$  of hadrons produced in the forward region. The histograms labeled  $Y$ ,  $C$ ,  $G$  and  $S$  correspond to the yoyo formation model, the constituent formation model, the Glauber limit ( $\ell \equiv 0$ ) and to the string flip model, respectively. For the constituent formation model, the zero scattering component has been included (dashed histogram). The data were taken from refs[9,10].
- Fig. 8** The ratio  $\mathcal{R}_A(x)$  for  $Sn$  targets, at  $\langle \nu \rangle = 10$  GeV and  $\langle \nu \rangle = 62$  GeV. The curves are labeled as in Fig.7. The data are from refs. [9,10].
- Fig. 9** Color exchange interactions of the leading quark ( $q_0$ ) in the string flip model.
- Fig.10** The ratio  $\mathcal{R}_A(x)$  for the fragmentation function  $D(x) = \frac{1}{x}$  in the string flip model, as obtained in the schematic model of section 3.1. The slope at  $x = 1$  is given by  $-\nu P_0/(\kappa\lambda)$ .

## References

- [1] B. Andersson et al, Phys.Rep. 97 (1983) 31
- [2] B. Andersson, G. Gustafson and B. Nilsson-Almqvist, Nucl.Phys. B281 (1987) 289
- [3] A. Cappelletti et al, Z. Phys. C3 (1980) 68; C33 (1987) 541; J. Ranft, Phys. Lett. B188 (1987) 379.
- [4] T. Sjöstrand, JETSET manual, Lund preprints LU-TP-85-10, LU-TP-86-22
- [5] G. Ingelman, "LEPTO version 4.3", CERN library long writeup THE LUND MONTE CARLO PROGRAMS (April 1987)
- [6] M. Gyulassy, M. Plümer, LBL-27605 (1989), submitted to Nucl. Phys. B
- [7] A. Bialas and M. Gyulassy, Nucl.Phys. B291 (1987) 793
- [8] M. Gyulassy, CERN preprint CERN-TH-4794 (1987)
- [9] L.S. Osborne et al., Phys.Rev.Lett. 40 (1978) 1624
- [10] P.B. Renton et al., Nucl. Physics Lab., Oxford, Preprint Ref. 55/88
- [11] European Muon Collaboration, A. Arvidson, et al., Nucl.Phys. B246 (1984) 381; Report at the High Energy Physics Conference, Munich 1988
- [12] A. Bialas and M. Czyzewski, Phys.Lett. 222B (1989) 132
- [13] A. Dar and F. Takagi, Phys.Rev.Lett. 44 (1980) 768
- [14] G. Nilsson, B. Andersson and G. Gustafson, Phys.Lett. 83B (1979) 379
- [15] N.N. Nikolaev, Z.Physik C5 (1980) 291
- [16] R. Arnold et al., PEGASYS Letter of Intent, SLAC, December 1987

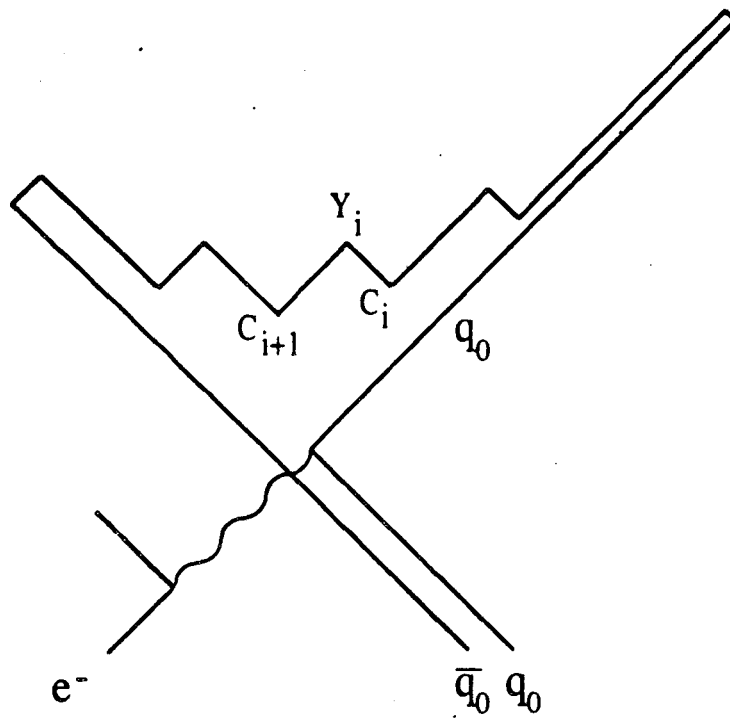


Fig. 1

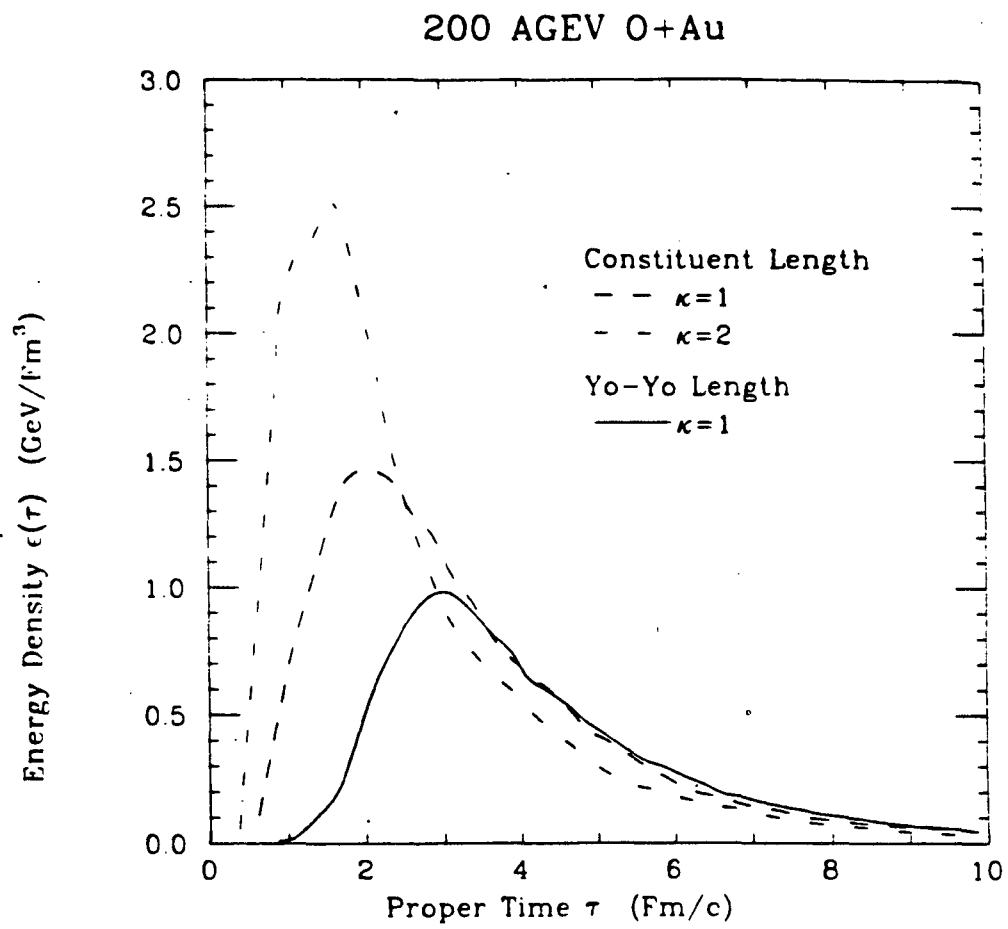


Fig. 2

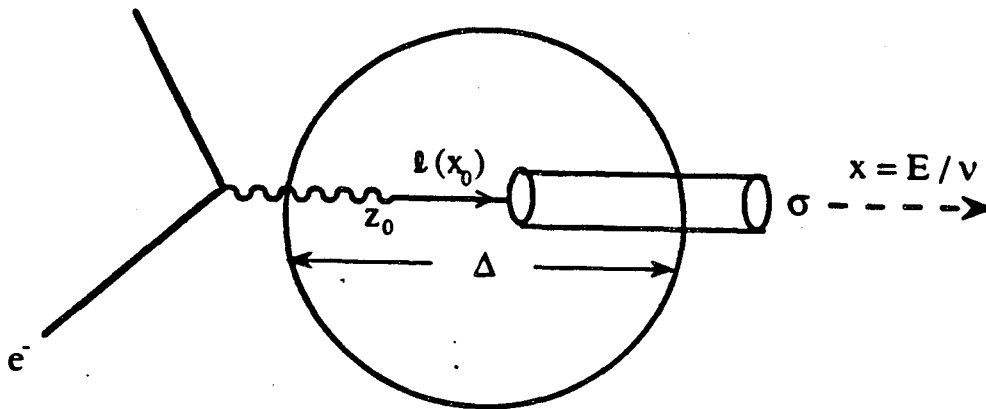


Fig. 3

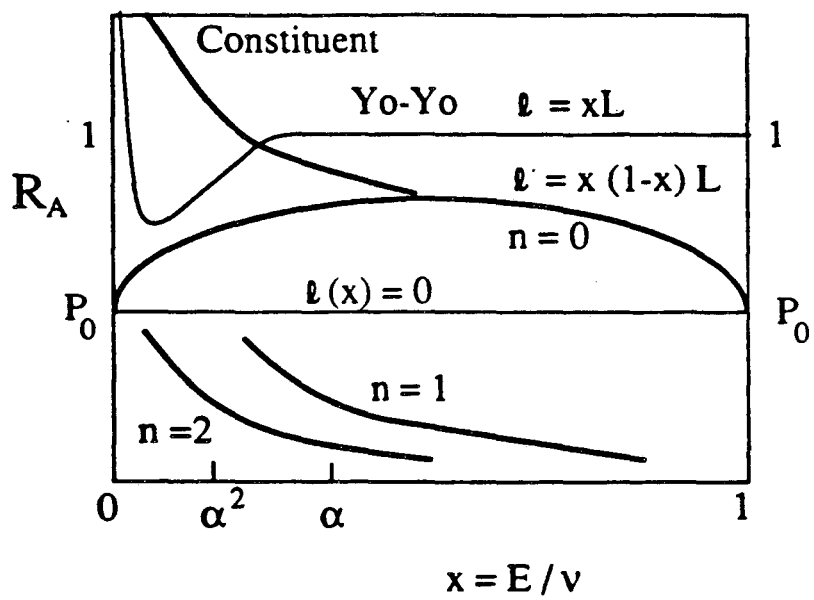


Fig. 4

$e + \chi e \rightarrow \pi^+$

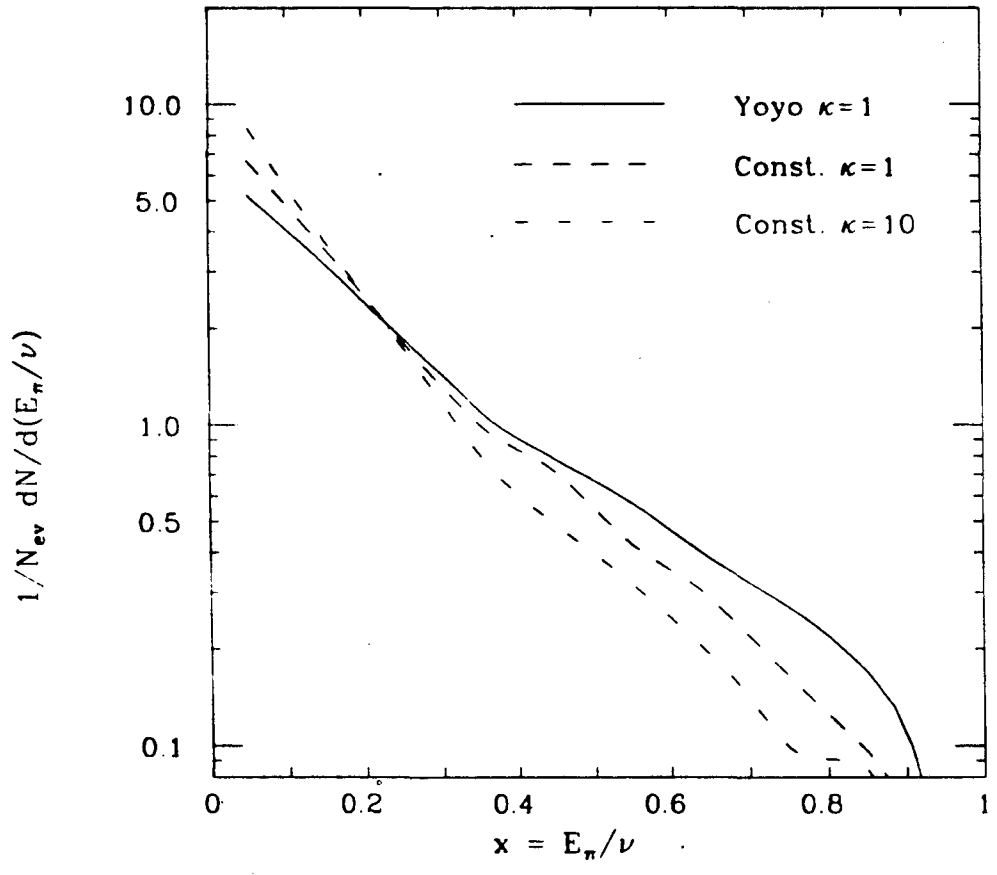


Fig. 5

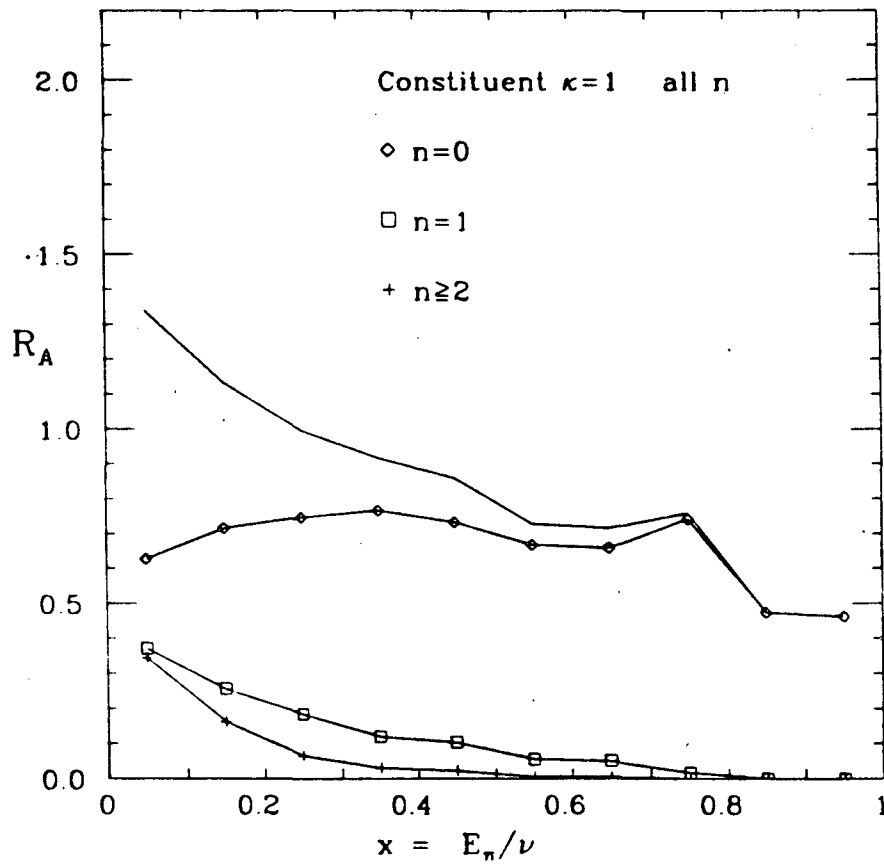
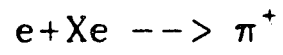


Fig. 6

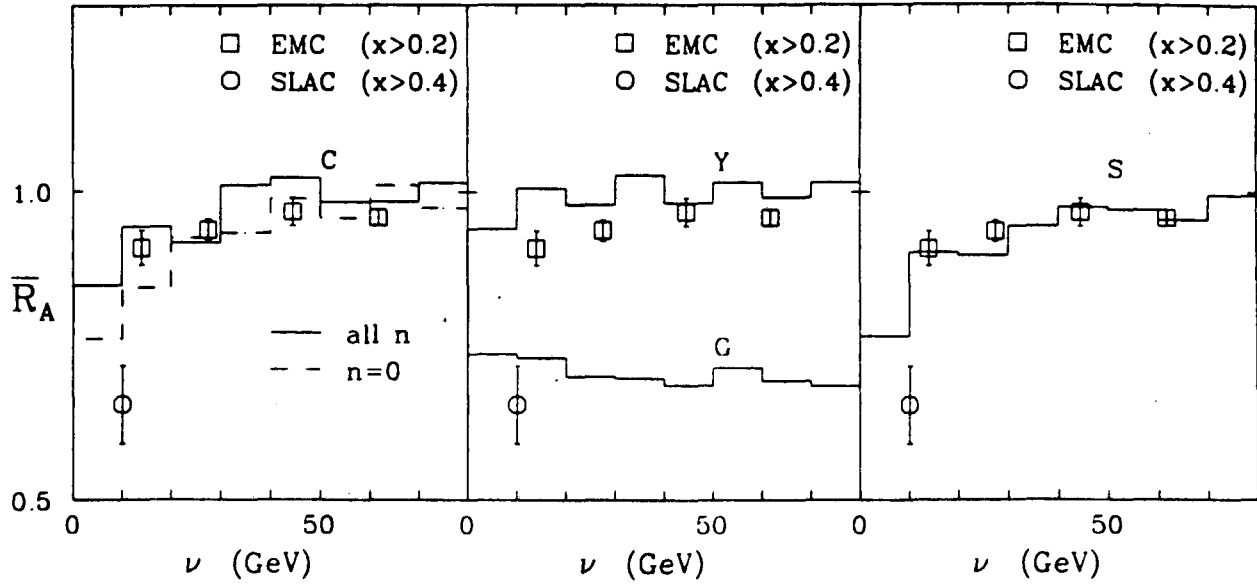
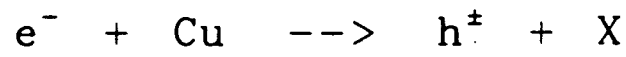


Fig. 7

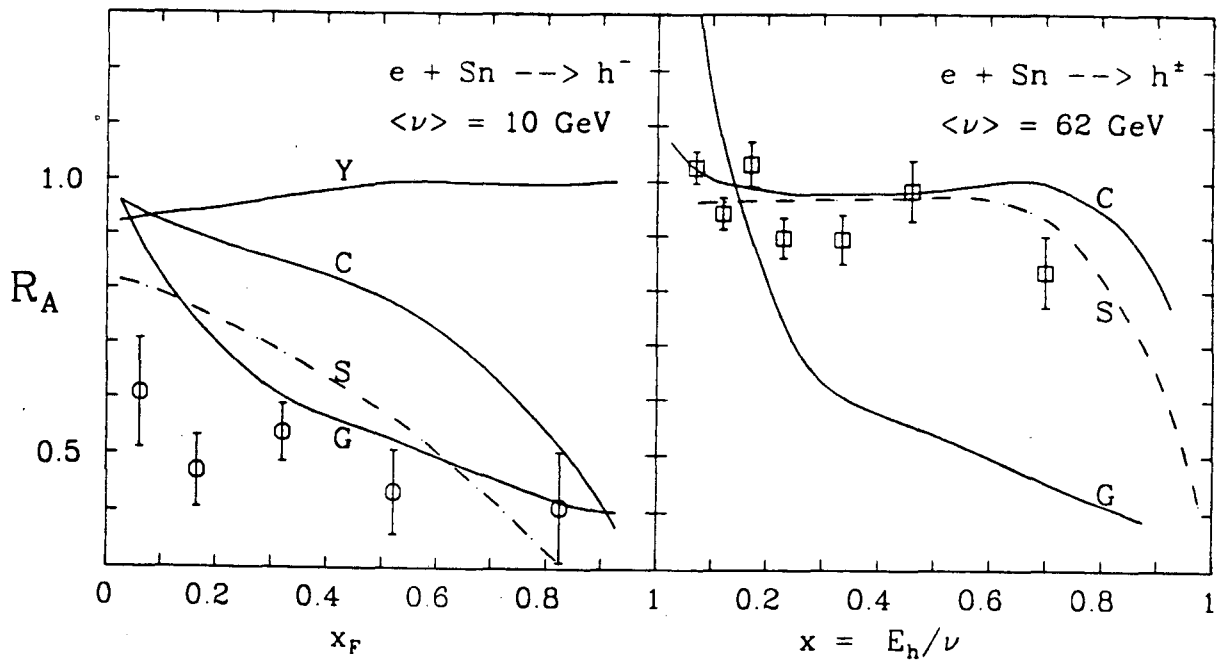


Fig. 8



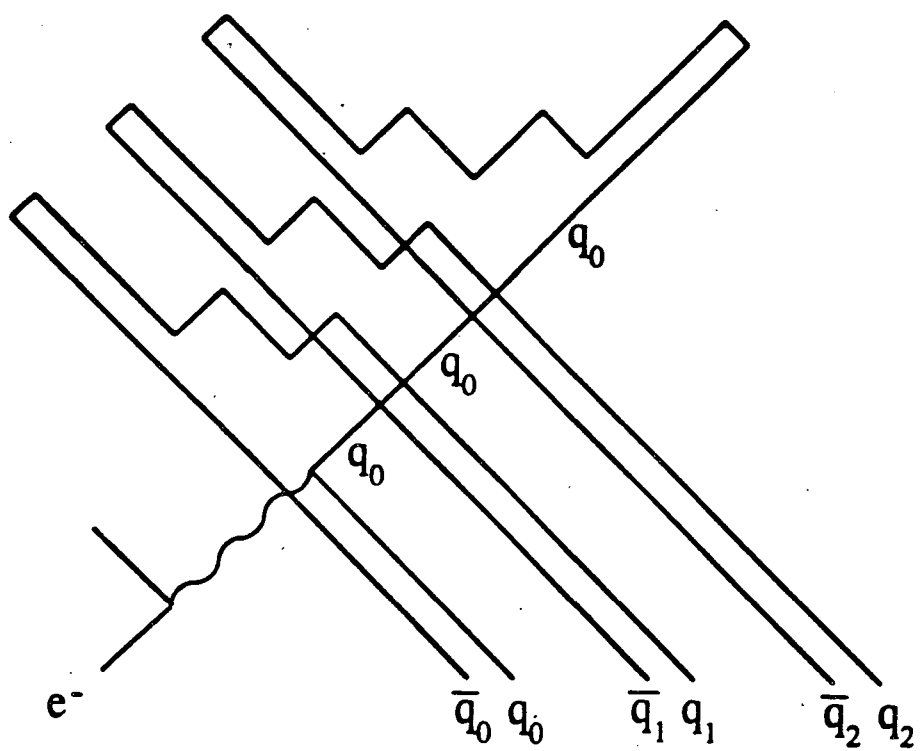


Fig. 9

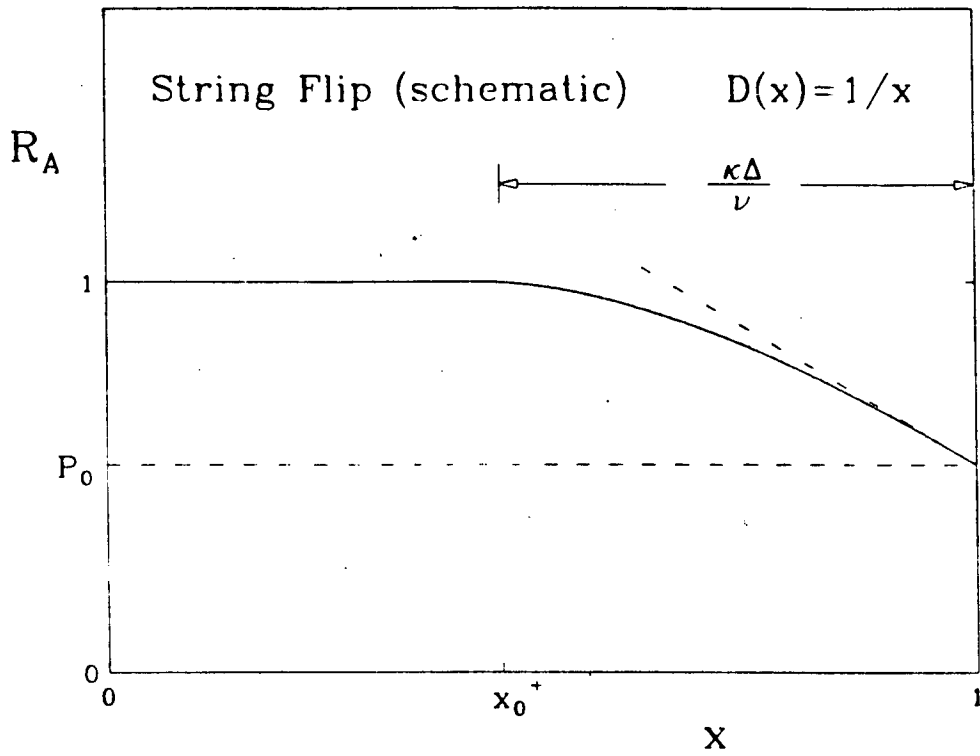


Fig.10

LAWRENCE BERKELEY LABORATORY  
TECHNICAL INFORMATION DEPARTMENT  
1 CYCLOTRON ROAD  
BERKELEY, CALIFORNIA 94720