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## Extremely costly intensifiers are stronger than quite costly ones

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#### Abstract

We show how the wide range in strengths of intensifying degree adverbs (e.g. *very* and *extremely*) could be explained by pragmatic inference based on differing cost, rather than differing semantics. This predicts a linear relationship between the meaning of intensifiers and their length and log-frequency. We test this prediction in two studies, using two different dependent measures, finding that higher cost does predict stronger meanings. We discuss the implications for adverbial meaning and the more general question of how extensive non-arbitrary form-meaning association may be in language.

**Keywords:** intensifiers; degree adverbs; scalar adjectives; pragmatics; m-implicature

#### Introduction

How do different words get their meanings? For instance, why is an "extremely good paper" better than a "quite good paper"? The traditional answer (de Saussure, 1916) is that different meanings have been arbitrarily and conventionally assigned to the different word forms. This view has been challenged by a number of examples in which word meaning appears to be non-arbitrarily related to properties of the word. In some cases, the phonetic form of a word is systematically related to its meaning, for example rounded vowels and voiced consonants tend to refer to round objects (Köhler, 1947; Ramachandran & Hubbard, 2001; Holland & Wertheimer, 1964; Davis, 1961). In other cases, orthographic form is diagnostic of meaning, for example, speakers of Hebrew who have never seen Chinese characters are nonetheless above chance at matching them to their corresponding Hebrew words (Koriat & Levy, 1979). Similarly, the length of words predicts aspects of their meanings: across languages longer words refer to more complex meanings (Lewis, Sugarman, & Frank, 2014). In this paper, we explore adjectival intensifiers<sup>1</sup>, like extremely and quite, as a case study in which to empirically explore the relationship of meaning to factors like word form and distribution of usage. Intensifiers form a good case study both because they are amenable to simple quantitative measures of meaning (such as the numeric extent to which they shift the interpretation of a scalar adjective) and because theoretical considerations, which we lay out shortly, suggest a relationship between their meaning and their usage cost (e.g., due to frequency and length).

In the next section we start from the model presented by Lassiter and Goodman (2013) to explain the meaning of scalar adjectives, like tall and expensive. This probabilistic Rational Speech Acts (Frank & Goodman, 2012; Goodman & Stuhlmüller, 2013) model describes how a threshold on meaning (e.g. the minimum price that counts as an expensive watch) can be established by pragmatic inference that takes into account statistical background knowledge (such as the distribution of prices for watches). We explore the effect of having multiple versions of the adjective that have the same meaning but different costs, and find a M(arkedness)implicature (Levinson, 2000): more marked (costly to utter) versions will be interpreted as implicating higher values. This motivates the hypothesis that a major portion of the meaning of intensifiers comes from this process rather than from conventionally associated meanings. Concretely, this predicts that the meanings of intensifiers are influenced by their form (in length) and their distribution (frequency) of usage. The impact of word length is reminiscent of the results of Lewis et al. (2014), who studied noun categories. While word frequency is known to have major effects on sentence processing (Levy, 2008, e.g.), the prediction that frequency should affect meaning is more novel.

We confirm, in two experiments, that English intensifiers in adjective phrases are indeed interpreted as much higher degrees (e.g. in the case of *expensive*, higher prices) for both longer and less frequent intensifiers. This holds in quantitative judgments of meaning and in forced comparisons, and across a number of adjectival dimensions. We conclude with a discussion of different interpretations of these phenomena and future directions.

#### The semantics of intensifying degree adverbs

Our paper focuses on intensifying degree adverbs applied to scalar adjectives<sup>2</sup>. Scalar adjectives have been described as having a threshold semantics (Kennedy, 2007), where, for example, *expensive* means "having a price greater than  $\theta$ " and  $\theta$  is a semantic variable inferred from context (e.g., \$100). Above the threshold degree  $\theta$ , the adjective is true of an object, and below, the adjective is false. Lassiter and Goodman (2013) give a formal model of how this threshold might be inferred for a particular context, which we extend to intensifiers.

<sup>&</sup>lt;sup>1</sup>Intensifiers are adverbs that modify scalar adjectives to increase the degree. The word "intensifier" is often used to denote the full range of degree adverbs, be they "amplifiers", or "downtoners" (Quirk, Greenbaum, Leech, & Svartvik, 1985). The "intensifiers" we are looking at in this paper are, according to this typology, "amplifiers" because they increase (rather than decrease) the threshold associated with a gradable predicate. This typology also distinguishes between two different kinds of amplifiers: those that increase an adjective maximally (e.g. completely and utterly) and those that merely increase (e.g. greatly and terribly). We do not make this distinction. The word "intensifier" is sometimes used for a completely different linguistic phenomenon, where a reflexive is used for emphasis, e.g. "The king himself gave the command," which we do not analyze in this paper.

<sup>&</sup>lt;sup>2</sup>Some of these intensifiers can also apply to verbal and nominal predicates, and different restrictions apply for different intensifiers, e.g. *I truly like carrots* is an acceptable utterance, whereas *I very like carrots* is not. See Bolinger (1972) for a discussion.

#### **Background**

Previous researchers have proposed that adjective phrases modified by intensifiers have the same semantics as unmodified adjective phrases, except with new, higher thresholds (Kennedy & McNally, 2005; Klein, 1980; Wheeler, 1972). That is, some threshold, inferred from context, exists above which objects are expensive and below which they are not. and the intensifier very determines a new, higher threshold for very expensive. They suggest that the intensified thresholds are determined by first collecting the set of objects in the comparison class for which the bare adjective is true, and then using that as the comparison class to infer a new threshold, i.e. very expensive laptop means "expensive for an expensive laptop". This analysis results in the expected intensification of adjectives ("expensive for an expensive laptop" has a higher threshold for being true than simply "expensive for a laptop") and is appropriately sensitive to different domains (e.g. the absolute difference in price between thresholds for expensive and very expensive is much higher in the context of "That space station is very expensive," than in the context of "That coffee is very expensive."). However, this account does not, in and of itself, distinguish between the graded strengths of different intensifiers, for example, very expensive and phenomenally expensive.

Intuition suggests that different intensifiers do have different strengths (e.g. *outrageously* seems stronger than *quite*), and we provide further evidence of this in our experiments, where participants interperet and compare different intensifiers. It could be that the degree of strength of different intensifiers is conventionally specified by the lexicon. But the semantics must then specify how these entries affect the very flexible threshold of the relevant adjective. In addition, the multitude of intensifiers (Bolinger, 1972) and their apparent productivity<sup>3</sup> suggest a more parsimonious solution would be welcome. That is, having a lexically determined meaning for each different intensifier might overlook the similarity among words of this class.

We propose instead that each time a scalar adjective is used, in each phrase, it introduces a free threshold variable (that is, a new token threshold is inferred for every time the lexical entry of the adjective is accessed). Further we propose that intensifiers contribute *nothing* to the literal, compositional semantics<sup>4</sup>. This implies that different adjectival phrases (e.g. "very expensive watch" and "extremely expensive watch") have equivalent meanings, though with thresholds that will be separately assigned based on context. *However*, the intensifiers do affect the production cost of the corresponding sentences, and it is this cost difference that results in meaning differences.

We next outline and extend Lassiter and Goodman's model of scalar adjectives to include several copies of the relevant adjectival phrase, each with its own threshold variable. We show that simply having different thresholds for different adjective phrases—and being aware of alternative utterances and their relative communicative costs—is sufficient to communicate the wide range of degrees designated by intensifying degree adverbs.

#### Model

Lassiter and Goodman (2013)'s model belongs to the family of Rational Speech Act (RSA) models in which speaker and listener communicate by recursively reasoning about each other's goals and inferences. These models have been shown to account for many phenomena in pragmatics (Frank & Goodman, 2012; Goodman & Stuhlmüller, 2013). The adjective model accounts for uncertainty about the adjectival threshold by including a lifted semantic variable, which the pragmatic listener infers at the same time that she infers the speaker's intended meaning. We assume every adjective phrase has its own such variable  $\theta_i^5$ , together notated  $\vec{\theta}$ , but to otherwise mean the same thing, so that, for example, *expensive*, *very expensive* and *phenomenally expensive* all denote:  $\lambda x.price(x) > \theta_i$ .

Given an utterance  $u_i$  (e.g. an *expensive laptop* or a *very expensive laptop*) and a set of thresholds, a literal listener  $L_0$  will use Bayesian inference to update his prior beliefs P(d) about the degree d (e.g. the laptop's price) given that the degree is greater than the threshold for that utterance.

$$P_{L_0}(d|u_i,\theta_i) \propto P(d) \cdot \delta_{d>\theta_i}$$

A speaker with the goal of communicating some actual degree d assigns a utility  $\mathbb{U}(u_i|d)$  to each utterance such that he prefers utterances which will inform the literal listener, but avoids utterance cost,  $C(u_i)$ :

$$\mathbb{U}(u_i|d,\vec{\theta}) = \ln\left(P_{L_0}(d|u_i,\theta_i)\right) - C(u_i)$$

Given a set of alternative utterances (e.g. the speaker might be choosing between saying *very expensive* as opposed to *expensive* or *extremely expensive*, or saying nothing at all), the speaker  $S_1$  will choose utterances according to a softmax decision rule (Sutton & Barto, 1998) with optimality parameter  $\lambda$ , so that:

$$P_{S_1}(u_i|d,\vec{\theta}) \propto e^{\lambda \mathbb{U}(u_i|d,\vec{\theta})}$$

A pragmatic listener  $L_1$  uses the prior probability, P(d), of different degrees, along with knowledge of the cost of each

<sup>&</sup>lt;sup>3</sup>For example, *altitidinously expensive* is not in common usage, but one can easily interpret *altitidinously* as a novel intensifier.

<sup>&</sup>lt;sup>4</sup>We take this strong view for rhetorical purposes. It is highly likely that some intensifiers have other aspects of meaning.

<sup>&</sup>lt;sup>5</sup>Other versions of this model could easily be imagined in which the threshold for an adjective phrase is determined by the basic threshold for the adjective and some transformation on that threshold (e.g. multiplication, addition, etc.) caused by the intensifier. If the transformation is mostly regular, with a single parameter needing to be inferred for each intensifier, and if the values of these parameters are inferred for each adjective phrase, then such a model would be functionally equivalent to the one we describe here.

utterance, in order to guess both the thresholds for each utterance and which degree the speaker intended to communicate<sup>6</sup>:

$$P_{L_1}(d, \vec{\Theta}|u_i) \propto P(d) \cdot P_{S_1}(u_i|d, \vec{\Theta})$$

As an initial exploration, we simulated such a model with three alternative adjective phrases (i.e. three intensifiers) with costs of 1, 5, and 10. We also included a null utterance, with trivial meaning (always true) and cost of 0. The prior distribution of degrees along this adjective's scale (which we will discuss as "prices" for concreteness and consistency with our Experiment 1) was a gaussian peaked at 0. We used an optimality parameter of  $\lambda = 5$  in our simulation.

Though the literal semantics are identical (except that they have different threshold parameters), the different phrases received different interpretations: the more costly intensifiers corresponded to less probable, more extreme prices (Figure 1). This can be seen as an M-implicature: more costly intensifiers are assigned strong, less probable, meanings. The model therefore predicts an association between intensifier meaning and utterance cost.

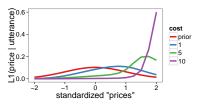


Figure 1: Modeling intensifiers as M-implicature: more costly intensifiers correspond to more extreme meanings.

### **Factors affecting utterance cost**

We have identified the intensifier's cost,  $C(u_i)$ , as a potentially critical factor of its interpreted meaning. The quantitative form predicted by the model of the relationship between cost and meaning is a approximately linear (Figure 2).<sup>7</sup>.

To connect this linear prediction to empirical facts, we still must specify (at least a subset of) the factors we expect to impact cost. The most natural notion of cost is the effort a speaker incurs to produce an utterance. This could include cognitive effort to access lexical items from memory, articulatory effort to produce the sound forms, and other such direct costs. Speakers might also seek to minimize comprehension cost for their listeners, resulting in other contributions to cost. For the purposes of this paper, we restrict to the most straightforward contributors to production cost and use proxies that are straightforward to quantify: length (longer utter-

ances are more costly) <sup>8</sup> and frequency (rarer intensifiers are harder to access and therefore more costly). In a number of different tasks, lexical frequency affects difficulty in an approximately logarithmic way. For instance word recognition time (McCusker, 1977) and reading time in context (Smith & Levy, 2013) are both logarithmic in frequency. We thus use the log-frequency (whose negative is also called *surprisal*) as the quantitative contribution to cost.

We thus predict a linear contribution of longer and higher surprisal intensifiers to the meaning. This leaves open the the relative importance of length and surprisal, and potential interactions (as well as other factors that might enter into cost), which can be explored via regression models.

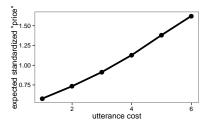


Figure 2: Model prediction of expected price as cost of intensifier increases, based on intensifiers evenly spaced in cost. The relationship is approximately linear.

## **Experiment 1**

The proposal detailed above predicts an association between measures of cost and strength of interpretations. In Experiment 1, we test this qualitative prediction by eliciting free response price estimates from people and determining whether these prices are correlated with our independent measures of utterance cost.

#### Method<sup>9</sup>

30 participants with US IP addresses were recruited through Amazon's Mechanical Turk and paid \$0.40 for their participation, of whom 1 was excluded for saying they did not follow the directions in a post-experiment survey.

We asked participants to estimate the prices of different objects based on descriptions of those objects. The descriptions included intensifiers paired with the adjective *expensive* (Figure 3). There were three categories of objects (*laptop*, *watch*, and *coffee maker*) and 40 intensifiers (see Table 1). We chose intensifiers that have a wide range of frequencies and excluded intensifiers that are either more commonly used to signal affect than to signal degree (e.g. "depressingly expensive" might indicate a degree, but it mainly indicates affect)

<sup>&</sup>lt;sup>6</sup>We assume a uniform prior on thresholds  $\theta_i$ .

<sup>&</sup>lt;sup>7</sup>This second simulation was identical as the first, except run on a more discretized scale for 6 different utterance costs (or "intensifiers").

<sup>&</sup>lt;sup>8</sup>We measure length in number of syllables, although length in characters (which might be a relevant source of utterance cost in a written format, as our experiments were in) has similar predictive power to syllable length in all of our analyses.

<sup>&</sup>lt;sup>9</sup>The full experiment can be found at http://cocolab.stanford.edu/cogsci2015/intensifiers/Experiment1

Table 1: Intensifiers from Experiment 1, number of occurences in G	oogle Web 1T 5grams corpus, and number of syllables.
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ngram	frequency	syllables	ngram	frequency	syllables	ngram	frequency	syllables
	11156	4		11167	4	terrifically	62292	4
surpassingly		4	colossally		4	J		4
frightfully	65389	3	astoundingly	73041	4	phenomenally	120769	5
uncommonly	135747	4	outrageously	240010	4	fantastically	250989	4
mightily	252135	3	supremely	296134	3	insanely	359644	3
strikingly	480417	3	acutely	493931	3	awfully	651519	3
decidedly	817806	4	excessively	877280	4	extraordinarily	900456	6
exceedingly	977435	4	intensely	1084765	3	markedly	1213704	3
amazingly	1384225	4	radically	1414254	3	unusually	1583939	4
remarkably	1902493	4	terribly	1906059	3	exceptionally	2054231	5
desperately	2139968	3	utterly	2507480	3	notably	3141835	3
incredibly	4416030	4	seriously	12570333	4	truly	19778608	2
significantly	19939125	5	totally	20950052	3	extremely	21862963	3
particularly	41066217	5	quite	55269390	1	especially	55397873	4
verv	292897993	2	_					

or are ambiguous between other parts of speech (e.g. "super" can be used as an intensifier, as in "super expensive", but it can also be used as an adjective, as in "super hero"). Each participant gave price judgments for every intensifier-category pairing in a randomized order (different for different participants). We chose the domain of price and used only the adjective *expensive* because price constitutes a quantitative scale with standard units (dollars for our US participants) on which to measure the different intensifers.



Figure 3: Screenshot from Experiment 1 target question.

**Corpus Methods** Table 1 shows word frequency and length in syllables for the intensifiers used in the experiment. The frequencies were collected from the Google Web 1T 5-grams database (Brants & Franz, 2006)<sup>10</sup> In the analysis below we use word length and word surprisal (negative log-frequency) as proxies for a word's cost, as motivated above. The syllable lengths of our intensifiers and the surprisals were clearly correlated, but not strongly so (r = 0.27, t = 16, p < 5e - 16).

#### **Results and Discussion**

If the meaning of an intensifier is stronger for higher cost intensifiers, we would expect to find that as surprisal increases and length in syllables increases, the prices participants give will also increase. We find that this is the case.

We ran a linear mixed effects regression with centered fixed effects of syllables, surprisal, and their interaction, and random intercepts and slopes for syllables and surprisal for both participant and object. We used the logarithm of participants' price estimates as the dependent variable, because of evidence that people's representation of numbers, including prices, is logarithmic (Dehaene, 2003, e.g.)<sup>11</sup>.

Our results are shown in Figure 4. Both measures of cost play a role in predicting participants' price estimates. We found a significant main effect of surprisal ( $\beta$  = 0.0536, SE = 0.00902, t(3) = 5.94, p < 0.05) such that less frequent words tend to be associated with higher price estimates. We also found a significant main effect of syllable length ( $\beta = 0.0900, SE = 0.0189, t(4) = 4.76, p < 0.05$ ), above and beyond surprisal, such that longer words predict stronger meanings. We also found a significant interaction  $(\beta = 0.0196, SE = 0.00520, t(3.5) = 3.77, p < 0.0005)$  between surprisal and syllable length, wich may indicate that the relationship between the two predictors of cost is not simply additive, and that having multiple sources of communicative cost (i.e. length and surprisal) might increase the implicature even more. Although these effects are significant, the marginal and conditional  $R^2$  values (Barton, 2015) were 0.015 and 0.72 respectively, indicating that much of the variance in estimated prices is captured by the random effects rather than the fixed effects of surprisal and syllable length.

Overall, intensifiers that are less frequent and longer (and therefore are more costly to utter) also tend to be interpreted as having stronger meanings, at least when used to modify *expensive*. Furthermore, the relationship appears to be linear in surprisal and length (though with an interaction), as predicted. This is consistent with the M-implicature model introduced above.

#### **Experiment 2**

The M-implicature account described above implies that there is no semantic interaction between the intensifier and the adjective it is applied to. Instead an intensifier should contribute similar cost, and therefore meaning, to the different adjectival phrases in which it occurs<sup>12</sup>. To explore this issue,

We also ran the same analyses on frequency information collected from the Google Books American Ngrams Corpus (Michel et al., 2011) and found similar results.

<sup>&</sup>lt;sup>11</sup>I.e. the perceptual distance between two prices the same dollar amount apart is more for small numbers (e.g. \$3 and \$6) and less for large numbers (e.g. \$1,543 and \$1,546).

<sup>&</sup>lt;sup>12</sup>If the bigram frequency of the modified adjective ("very expensive") deviated from that expected based on independent word fre-

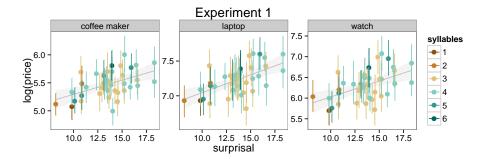


Figure 4: Results of Experiment 1. As surprisal and length in syllables increase, participants' free response prices increased.

we would like to extend our results to additional adjectival scales. However, most scales are not so easily quantifiable as price; we require a different dependent measure in order to probe them. For Experiment 2 we used a forced-ranking dependent measure, which allows us to consider additional adjectival scales. This dependent measure has the added benefit of providing a more sensitive measure of the differences in degrees between similar adjectival phrases.

## Method<sup>13</sup>

30 participants with US IP addresses were recruited through Amazon's Mechanical Turk and paid \$0.40 for participation. 3 said they did not follow the directions in a post-experiment survey and were excluded from the analysis.

We asked participants to order (by clicking and dragging) various adjective phrases with the same adjective but different intensifiers according to strength of meaning. Because arranging these phrases required participants to be aware of the full set of adjective phrases and access all of them on the same computer screen, not all of our 40 intensifiers could effectively be presented at once. We divided the 40 intensifiers from Experiment 1 into four lists of 10 intensifiers. Each list was randomly paired with one of four adjectives (old, expensive, beautiful, and tall). For each adjective-list pairing, participants were shown every combination of the 10 intensifiers with one adjective. Participants were asked to move the adjective phrases across the screen, reordering the phrases from the "lowest" to the "highest" degree (Figure 5). Each participant completed four trials, seeing all four lists and all four adjectives. The list-adjective pairings were randomized between participants. The division of the intensifiers into lists of 10 was constant, so that the same 10 intensifiers were always shown together.

#### **Results and Discussion**

Our results for Experiment 2 are shown in Figure 6. We ran an ordinal mixed effects regression with centered sur-

quencies our frequency-based cost account would predict an interactive effect on meaning. This would be a relatively small effect, and the relevant bigrams were too sparse in our corpora to pursue.

<sup>13</sup>The full experiment can be found at http://cocolab.stanford.edu/cogsci2015/intensifiers/Experiment2

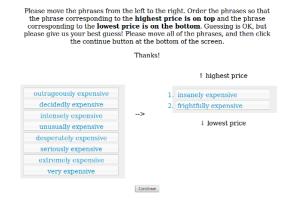


Figure 5: Screenshot from Experiment 2 target question.

prisal and syllable lengths and their interaction as fixed effects, and random intercepts and slopes for syllables and surprisal for both participant and adjective. As in Experiment 1, we found strong main effects of surprisal ( $\beta = 0.432, SE = 0.0934, t = 4.63, p < 0.05$ ) and syllable length ( $\beta = 0.671, SE = 0.122, t = 5.50, p < 0.005$ ), and a significant interaction ( $\beta = 0.0725, t = 2.01, p < 0.05$ ). In this experiment, a much higher proportion of our explained variance was due to our fixed effects (marginal  $R^2 = 0.18$ , and conditional  $R^2 = 0.22$ ). In other words, we again found that participants assign stronger interpretations to intensifiers with higher surprisals and/or higher syllable lengths, extending now across four different adjectival scales.

#### **General Discussion**

Motivated by a recent probabilistic model of scalar adjectives (Lassiter & Goodman, 2013), we showed how adjectival intensifiers could potentially get their meaning through a pragmatic M-implicature, despite having vacuous literal meaning to add to an adjective. Our model predicted a linear relationship between the intensity of an intensifier and its cost, measured here in terms of length and log-frequency. In two experiments we provided evidence that intensifier meanings do depend systematically on the length and frequency of distribution of those word forms. While it is unlikely that this ac-

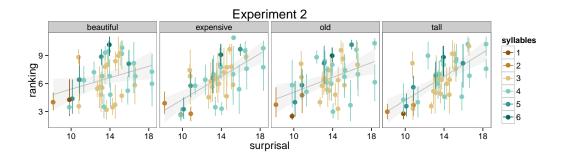


Figure 6: Results of Experiment 2. As surprisal and length in syllables increase, participants' rankings increased.

counts for all intensifier meaning, it does suggest that a major portion of meaning comes not from arbitrary, conventional association of signal to sign (de Saussure, 1916), but from features of the word's form and distribution.

It should be noted that, since this is a correlational study, such a relationship does not confirm that an intensifier's cost causes it to have a given meaning. This correlation is predicted by the model sketched above, but it might be predicted by other analyses of intensifiers and their meanings. Rarity in particular might be correlated with strength of meaning merely because more extreme meanings refer to less probable things in the world, are therefore talked about less, and therefore the words with those meanings will necessarily be rarer. Although it seems reasonable to suspect that word frequencies reflect the probabilities of the real-world concepts they describe, it might also be the case that improbable things are more likely to be commented on, and so the frequencies of words that describe rare concepts might be inflated. In addition, this confound on causal direction exists only for word frequency (and its effect on syllable length) and not for syllable length directly. Although the length of a word certainly depends on frequency of use, it seems unlikely that it also depends directly on the real-word prevalence of the concept it refers to.

A number of issues remain to future work, including the causality of the relationship we have described and the other aspects of intensifier meaning (such as polarity or affective color). However we believe that the preliminary results presented in this paper already have interesting implications. For the semantics of adverbial modifiers, we have shown how pragmatic mechanisms could be central in establishing flexible contributions to sentence meaning. For the broader question of form-meaning mapping, we have suggested a source of non-arbitrary association based on both properties of the word form and of its distribution.

#### Acknowledgments

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