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An Active Region Model for Capturing Fractal Flow Patterns in Unsaturated Soils: **Model Development** H.H. Liu^a, R. Zhang^{b,c} and G. S. Bodvarsson^a ^a Earth Sciences Division, Lawrence Berkeley National Laboratory, Berkeley, California ^b Department of Renewable Resources, University of Wyoming, Laramie, Wyoming ^cSchool of Environmental Science and Engineering, Sun Yat-Sen (ZhongShan) Unversity, Guangzhou, China Submitted to Journal of Contaminated Hydrology * Corresponding author (email: hhliu@lbl.gov)

Abstract

- Preferential flow commonly observed in unsaturated soils allows rapid movement of solute from the soil surface or vadose zone to the groundwater, bypassing a significant volume of unsaturated soil and increasing the risk of groundwater contamination. A variety of evidence indicates that complex preferential patterns observed from fields are fractals. In this study, we developed a relatively simple active region model to incorporate the fractal flow pattern into the continuum approach. In the model, the flow domain is divided into active and inactive regions. Flow occurs preferentially in the active region (characterized by fractals), and inactive region is simply bypassed. A new constitutive relationship (the portion of the active region as a function of saturation) was derived. The validity of the proposed model is demonstrated by the consistency between field observations and the new constitutive relationship.
- 14 Key words: Preferential flow, Fractal, Constitutive relations, Vadose zone hydrology.

1. Introduction

3 It has been recognized that preferential flow is common for natural unsaturated soils. Preferential flow results in that liquid water propagates quickly to significant depths 4 5 while bypassing large portions of the involved soils, and solute travel times from the contamination source (located in soil surface or vadose zone) to groundwater are shorter 6 than a prior expected (e.g., Flury et al., 1994). Because of the important effects of this 7 8 flow process on groundwater contamination, preferential flow has been a major research 9 area in the vadose zone hydrology community for many years (Simunek et al., 2003). 10 Field-scale preferential flow is caused by a number of well-known mechanisms. First, 11 under flooding and/or high-infiltration-rate conditions, water can flow very quickly along macropores (such as cracks and fissures) in structured soils (Beven and Germann, 1982; 12 Bouma and Dekker, 1991; Flury et al., 1994; Öhrström et al., 2002). Second, because of 13 the high nonlinearity of the unsaturated flow process, an infiltrating water front can 14 become unstable and split into "fingers" even for relatively homogeneous, structureless 15 soils (Hillel, 1987; Glass et al., 1988; de Rooij 2000; Wang et al., 2003). Third, the 16 spatial variability of soil properties also causes highly non-uniform flow patterns 17 corresponding to preferential flow paths (e.g., Vogel et al., 2000). At the field scale, a 18 combination of these three mechanisms likely contributes to the observed preferential 19 flow processes, although one or two of them may be dominant mechanisms for a given 20 21 testing site. For example, Olsson et al. (2002) reported that dye-stained preferential pathways were not only restricted to macropores in the topsoil, but also to fingers 22 resulting from wetting front instability. 23

Because of its complexity, preferential flow and the associated transport are probably 1 2 the most frustrating processes in terms of hampering accurate predictions of contaminant 3 transport in the vadose zone (Simunek et al., 2003). Recently, though, significant effort has been made in developing a variety of approaches to deal with preferential flow and 4 5 transport. These approaches mainly fall into one of two categories: the continuum 6 approach and the discrete approach. An excellent review of the continuum-approach-7 based models was recently given by Simunek et al. (2003) for structured (macropore) 8 soils. In the continuum approach, connected macropores and soil matrix are viewed as 9 two or more overlapped interacting continua. In other words, at a "point," two or more continua are considered to co-exist. In this case, the continuum mechanics formulations 10 can be used to describe flow and transport in each continuum. Coupling of processes 11 12 between different continua is determined by their interaction mechanisms at a subgrid scale. The similar approaches have also been used in modeling water flow and transport 13 in fractured rock (e.g., Doughty, 1999). Because the continuum approach is relatively 14 15 simple and straightforward to implement, it is preferred for most applications encountered in practice. However, a major limitation of the currently available continuum 16 17 models is that they were mainly developed for dealing with the effects of macropores for 18 structured soils, and are unable to capture preferential flow paths resulting from fingering and the spatial variability of soil properties. 19 In contrast to the continuum models, a number of researchers have suggested using 20 21 discrete modeling approaches, such as the diffusion limited aggregation (DLA) and 22 percolation-based approaches (e.g., Ewing and Berkowitz. 2001; Glass 1993; Flury and 23 Flühler, 1995). Roughly speaking, these approaches treat soil water body as discrete

1 "particles" or "packages" whose movement is controlled by some simple rules to generate growth patterns with rich structures (fractals). These approaches have been 2 3 successfully used to represent relatively small-scale observations. However, use of these 4 discrete approaches is quite limited for large-scale applications (Liu et al., 2003). 5 Furthermore, completely satisfactory theories underlying these approaches are still 6 missing, and some critical steps in these approaches are somewhat arbitrary (Meakin and 7 Tolman, 1989; Ewing and Berkowitz, 2001). Obviously, an ideal approach to deal with preferential flow should be able to combine 8 9 the advantages of the continuum and discrete approaches. The objective of this study is to develop an active region model that represents an effort toward developing an approach 10 of this kind by incorporating fractal flow patterns (often observed in the field and 11 simulated by discrete approaches) into the continuum approach. In the next section, we 12 13 will discuss field evidence of fractal flow patterns in unsaturated soils. Section 3 will 14 present details of the active region model and its relation to a fractal flow pattern. Section 15 4 will demonstrate the consistency between the active region model and the relevant field

2. Fractal flow patterns and preferential flow process

observations.

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Fractals have been shown to provide a common language for describing many different natural and social phenomena (Mandelbrot, 1982). While a vast literature exists on the validity of the fractal concept for a great number of fields, fractals have been found to be useful for representing many spatial distributions in subsurface hydrology, including soil particle size distribution, roughness of fracture surface, distribution of permeability in heterogeneous formations, and large-scale solute dispersion processes

- 1 (e.g., Tyler and Wheatcraft, 1990; Rieu and Sposito, 1991a, b; Perfect et al., 1996;
- 2 Neuman, 1990, 1994; Molz and Boman, 1993; Molz et al., 1997).
- 3 Recent studies have also suggested that complex preferential flow patterns in unsaturated systems can be characterized by fractals. Hatano and Booltink (1992) may be 4 5 the first authors to report in the vadose zone hydrology community that the geometry of dyed flow patterns in two-dimensional images of soil profiles could be characterized by 6 fractals. Flury and Flühler (1995) indicated that solute leaching patterns, observed from 7 three field plots consisting of an unsaturated loamy soil, could be well represented by a 8 9 diffusion-limited aggregation (DLA) model (Witten and Sander, 1981), although the 10 relation between DLA parameters and soil hydraulic properties is still an unresolved 11 issue. The DLA model is a conceptual model describing the process where solid particles irreversibly attach to each other and form aggregates and the process is limited by 12 13 diffusion. It has been documented that DLA generates fractal patterns (e.g., Feder, 1988; Flury and Flühler, 1995). The observation of Flury and Flühler (1995) is further 14 15 supported by Persson et al. (2001), who used dye-infiltration data to investigate field pathways of water and solutes under unsaturated conditions. Persson et al. (2001) showed 16 that field observations are well described by the DLA model. Furthermore, they 17 18 demonstrated that observed mean power spectrum for dye penetration of a field plot displays a typical power-law relationship, another important indication of fractal flow 19 behavior. Öhrström et al. (2002; 2004) also noticed that the dye penetrations for two test 20 21 sites (corresponding to a clayey and a sandy soil) are characterized by power-law mean 22 power spectrum. Olsson et al. (2002) reported that a field observation of dyed flow 23 pattern in an unsaturated test site is characterized by multi-fractals. This finding is

- 1 consistent with that in many cases spatial distributions of hydraulic conductivity are
- 2 multi-fractals (Liu and Molz, 1997).
- Related to preferential flow in unsaturated soils, fractal flow patterns have often been
- 4 observed in other unsaturated and multi-phase flow systems. Glass (1993) first showed
- 5 that unsaturated flow in a single vertical fracture is characterized by gravity-driven
- 6 fingers, and the resulting flow patterns could be modeled by an invasion-percolation
- 7 approach (Wilkinson and Wilemsen, 1983). Again, percolation-based models generate
- 8 fractal clustering patterns (Stauffer and Aharony, 2001). Viscous fingering in porous
- 9 media has been experimentally shown to be fractal (Feder, 1988). (The problem of
- viscous fingering in porous media is of central importance in oil recovery.) Smith and
- 11 Zhang (2001) also reported that DNAPL fingering in water saturated porous media.
- observed from sandbox experiments, is fractal. Liu et al. (2003) demonstrated that a
- spatial distribution of fractures with mineral coatings is also fractal, while fracture
- coating is roughly a signature of water flow paths.

3. An active region model

- As discussed in Section 2, highly non-uniform (preferential) flow patterns in
- unsaturated soil (and other unsaturated and multi-phase flow systems) are fractal. The
- success of discrete approaches in modeling preferential flow largely relies on their
- 19 capabilities for generating fractal patterns. Therefore, it is critical to incorporate fractal
- 20 flow patterns within a continuum model for it to capture preferential flow behavior. To
- do so, we develop, in this sudy, an active region model. The main idea behind the active
- 22 region model is that flow domain can be divided into active and inactive regions. Flow

1 occurs preferentially in the active region (characterized by fractals) and inactive

2 (immobile) region is simply bypassed.

3.1 Fractal dimension

The key parameter for a fractal pattern is fractal dimension. Fractal dimension, d_f , is generally a noninteger and less than the corresponding Euclidean (topological) dimension of a space, D. Different kinds of definitions for fractal dimension exist (e.g., similarity dimension, Hausdorff dimension, and box dimension), although they provide very close fractal dimension values for practical applications (Feder, 1988). The most straightforward definition is the so-called box dimension, based on a simple "box-counting" procedure. This dimension is determined from Equation (1) (below) by counting the number (N) of "boxes" (e.g., line segments, squares and cubes for one-, two-, and three-dimensional problems, respectively) needed to cover a spatial pattern, as a function of box size (I) (e.g., Feder, 1988):

$$N(l) = \left(\frac{L}{l}\right)^{d} f \tag{1}$$

where L refers to the size of the entire spatial domain under consideration. Fig. 1 shows a box-counting procedure for a spatial pattern with $d_f = 1.6$, in a two-dimensional domain with size L (Yamamoto et al., 1993).

Obviously, if a spatial pattern is uniformly distributed in space, the fractal dimension will be identical to the corresponding Euclidean dimension. In this case, the number of boxes that cover the pattern, N^* , and the box size l have the following relation

$$N*(l) = \left(\frac{L}{l}\right)^D \tag{2}$$

- A fractal pattern exhibits similarity at different scales. When $d_f < D$, the corresponding
- 4 pattern does not fill the whole space, but only part of it (Fig. 1).

5 3.2 Characterization of fractal flow patterns

- To incorporate the effects of fractal flow patterns, we need to develop a simple scheme
- 7 to characterize these patterns in terms of parameters relevant to water flow processes.
- 8 Consider Fig. 1(a) to be a gridblock containing an active flow region and the
- 9 corresponding flow pattern to be fractal. In this case, only a portion of the medium within
- a gridblock contributes to water flow (Fig. 1). This is conceptually consistent with the
- preferential flow process. Note that in Fig. 1, a box is shadowed if it covers the active
- 12 flow region.
- 13 Combining Equations (1) and (2) yields

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$$[N(l)]^{1/df} = [N*(l)]^{1/D}$$
 (3)

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- 17 The average active water saturation (Se*) for the whole gridblock (Fig. 1a) is determined
- 18 to be

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$$20 S_e^* = \frac{V}{l^D \phi N^*(l)} (4)$$

21 where V is the total water volume (excluding residual water) in the active region for the

- 1 gridblock (Fig. 1a), and φ is the effective porosity (corresponding to saturated water
- 2 content excluding residual water content). Similarly, the average active water saturation
- 3 (S_b^*) for shadowed boxes with size of l is

$$5 S_b^* = \frac{V}{l^D \phi N(l)} (5)$$

From Fig. 1, it is obvious that there exists a box size $l_1 < L$ satisfying:

$$7 \qquad \frac{V}{l_1^D \phi} = 1 \tag{6}$$

- Based on Equations (3)–(6), the average saturation for shadowed boxes with size l_1 , S_{b1} *,
- 9 can be expressed by

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$$S_{b1}^* = (S_e^*)^{\frac{d_f}{D}}$$
 (7)

- Because a fractal is similar at different scales, the procedure to derive Equation (7)
- from a gridblock with size L can be applied to shadowed boxes with the smaller size of l_1 .
- In this case, for a given box size smaller than l_1 , the number of shadowed boxes will be
- 14 counted as an average number for those within the (previously shadowed) boxes with a
- size of l_1 . Again, we can find a box size $l_2 < l_1$ to obtain a saturation relation:

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$$S_{b2}^* = (S_{b1}^*)^{\frac{d_f}{D}} = (S_e^*)^{\frac{d_f}{D}^2}$$
 (8)

- 18 The procedure to obtain Equation (8) can be continued until it reaches an iteration level,
- n^* , at which all the shadowed boxes with a size of l_n cover the active region only. The
- 20 resultant average saturation for these shadowed boxes is

$$S_{bn}^* = (S_e^*)^{\left(\frac{d_f}{D}\right)^{n^*}} \tag{9}$$

- By definition, S_{bn} should be equivalent to the effective water saturation (S_a) within
- the active region. Using f to denote the fraction of the active region within the gridblock
- 4 and based on Equation (9), we have

$$5 f = \frac{S_e^*}{S_a} = (S_e^*)^{\gamma} (10)$$

6 with

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$$\gamma = 1 - \left(\frac{d_f}{D}\right)^{n^*} \tag{11}$$

Parameter y is defined between zero and one. It is a key parameter for the active 8 9 region model. If flow pattern is uniform and does not contain preferential flow, y will be 10 equal to zero (corresponding to $d_f = D$ or f = 1). Otherwise, γ will be larger than zero and 11 result in an f value less than one. In this case, only a portion of the flow domain 12 corresponding to preferential flow paths actually conducts liquid water. The y may be a 13 complex function of soil properties, flow conditions, and scale. In this study, we assume it to be a constant for a given test site. (As will be discussed later in this paper, this 14 15 approximation seems to suffice for practical applications.) Liu et al. (2003) also demonstrated that this approximation is valid for fingering flow in homogeneous porous 16 media. 17

3.3 Governing equations for water flow

As previously indicated, the active region model divides the flow domain into active and inactive regions. Flow occurs preferentially in the active region (characterized by

- fractals), with the inactive (immobile) region simply bypassed. The governing equation
- 2 for water flow can be expressed as (in the one-dimensional form):

$$3 \qquad \frac{\partial \theta}{\partial t} = \frac{\partial}{\partial z} \left[K \left(\frac{\partial h}{\partial z} + 1 \right) \right] - S \tag{12}$$

- 4 where z is the vertical coordinate (positive upwards), t is time, S is the sink term, h is the
- 5 pressure head, θ is the total water content (including water contents from both active and
- 6 inactive regions), and K is the unsaturated hydraulic conductivity.
- While the governing equation (12) is almost identical to the traditional continuum
- 8 approaches, the major difference between the active region model and the other models is
- 9 constitutive relations among saturation, capillary pressure, and unsaturated hydraulic
- 10 conductivity. To demonstrate this difference, consider the simplest case without
- preferential flow and macropores. In such a case, the water capillary pressure head may
- be described by the well-known van Genuchten relation (van Genuchten, 1980):

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$$h(S_e) = \frac{1}{\alpha} [S_e^{-1/m} - 1]^{1/n}$$
 (13)

where α , (Pa^{-1}) , n, (-) and m=1-1/n are van Genuchten parameters. The effective

saturation is defined as

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$$S_e = \frac{\theta - \theta_r}{\theta_s - \theta_r} \tag{14}$$

where θ_s and θ_r are saturated and residual water contents, respectively.

- In the active region model, however, the van Genuchten capillary-pressure relation is
- 2 considered to be relevant for the active region, rather than for the whole flow domain.
- 3 The capillary pressure for the active region is determined by replacing Se in Equation
- 4 (14) with S_a . From Equation (10), we obtain

$$S_a = (S_e *)^{1-\gamma}$$
 (15)

$$h(S_e) = \frac{1}{\alpha} [(S_a)^{-1/m} - 1]^{1/n} = \frac{1}{\alpha} [(S_e^*)^{(\gamma - 1)/m} - 1]^{1/n}$$
(16)

The saturation S_e^* can be related to total water saturation S_e by

$$S_e = fS_a + (1 - f)S_i = S_e * + (1 - (S_e^*)^{\gamma})S_i$$
(17)

- where S_i is the water saturation within the inactive (immobile) region. It can be zero or a
- value corresponding to water flow that can be ignored compared to preferential flow
- 11 (Larsson et al., 1999).
- Equation (16) rather than (13) should be used to simulate water flow in soils with
- preferential flow. For a given effective water saturation, a larger γ value corresponds to a
- larger effective water saturation (S_a) within the active region, and therefore to a lower
- absolute value for capillary pressure (Liu et al., 1998).
- 16 The unsaturated hydraulic conductivity for the active region, Ka, is directly
- determined by the effective water saturation of the active region. However, because only
- a portion of the soil are active, the unsaturated hydraulic conductivity of the entire flow
- 19 region (including both active and inactive regions), K, should be the K_a multiplied by f,
- 20 or

$$K = fK_a = (S_e^*)^{\gamma} K_a$$
 (18)

where K_a can be given by the following van Genuchten permeability relation:

$$3 K_a = K_s S_a^{1/2} [1 - \{1 - S_a^{1/m}\}^m]^2 = K_s (S_e^*)^{(1-\gamma)/2} [1 - \{1 - (S_e^*)^{(1-\gamma)/m}\}^m]^2$$
 (19)

- where Ks is the saturated hydraulic conductivity.
- 5 Combining Equations (18) and (19) yields

$$K = K_s (S_e^*)^{(1+\gamma)/2} [1 - \{1 - (S_e^*)^{(1-\gamma)/m}\}^m]^2$$
(20)

- In general, K is affected by γ in a complex manner for a given S_e . A larger γ value,
- 8 resulting in a higher effective water saturation within the active region (Sa), gives rise to a
- larger value of K_a . On the other hand, a larger γ value corresponds to a smaller value of f.
- 10 Because the former effect is dominant, a larger γ value gives a larger K for a given
- effective water saturation S_e (Liu et al., 1998).
- Note that the above discussion concerns water flow in a soil without macropores.
- 13 Therefore, a single set of van Genuchten parameters is used, but the active region model
- is not limited to this special case. Two schemes can be used to include the effects of
- macropores. One approach is to treat mcropore and soil matrix within the active region as
- 16 two coupled continua. Standard dual-continuum formulations can be borrowed here
- 17 (Simunek et al., 2003). The disadvantage of this approach is that additional parameters to
- describe the coupling are needed. The other approach is to assume the local equilibrium
- 19 within the active region, considering that the high water saturation (and hydraulic
- 20 conductivity) generally existing within the active region could result in equilibrium
- quickly. In this case, the composite constitutive relationships as described in Simunek et

- al. (2003) can be used to replace the van Genuchten relations in the above equations.
- 2 However, the reasonableness of this local equilibrium approximation needs to be further
- 3 evaluated.
- 4 It is instructive to compare the active region model with two models in the literature. One of them is the active fracture model developed for simulating unsaturated flow and 5 6 transport in fractured rock (Liu et al., 1998, 2003). (We refer the readers to Liu et al. 7 (1998, 2003) regarding the details of the active fracture model and its validation results.) Because both the active region model and active fracture model are based on the notion 8 9 that flow patterns in unsaturated systems are fractal, constitutive relationships for the two models are almost identical. Therefore, the active region model can be considered a direct 10 extension of the active fracture model. However, it is useful to highlight the differences 11 between the two models. First, because flow mechanisms are not exactly the same for 12 unsaturated fractures and porous media (e.g., Liu and Bodvarsson, 2001), the two models 13 are conceptually different. It is not appropriate to assume that a model valid for modeling 14 flow in fractured rock will be equivalently valid for porous media. Furthermore, the 15 active fracture model was developed to describe water flow and solute transport in 16 fractures only, whereas our active region includes both soil matrix and macropores, as 17 previously discussed. Also note that in the active fracture model, all the inactive 18 19 fractures are assumed to have residual water saturation, whereas in the active region model, the immobile water saturation is not necessarily the same as the residual 20 saturation. The similar treatment has been used in mobile/immobile models to be 21 22 discussed later. As a result, the relationship between different water saturations in the active region model (Eq. 17) is more general than that in the active fracture model. 23

The other model is the mobile/immobile model for simulating preferential flow in non-structured soils (van Dam et al., 1990, 1996; Larsson et al., 1999). In this model, flow domain is divided into mobile and immoble regions, corresponding to active and inactive regions, respectively. van Dam et al. (1990, 1996) and Sexena et al. (1994) found that use of the two-region model can significantly improve the comparisons between simulated and observed results. However, in the mobile/immobile model, the fraction of the mobile region (corresponding to our f in Equation (10)) was treated as constant. Both van Dam et al. (1996) and Larsson et al. (1999) noticed that the fraction is not in reality a constant, especially under the transient flow conditions. Van Dam et al. (1996) also called for better practical concepts and models for simulating field-scale water flow and transport (involving preferential flow) under transient conditions. Our active region can be considered a generalization of the mobile/immobile model.

4. A comparison with field observations

The key element of the active region model is Equation (10). While the comprehensive evaluation of the active region model will be performed in our future research, we present our preliminary evaluation of Equation (10) in this study, based on data available in the literature.

Van Dam et al. (1990) used mobile/immobile model to analyze field tests involving application of a bromide solution to a field soil, subsequently leached by natural rainfall. The tests were carried out in two adjacent fields, one with a water-repellent top layer and one with a wettable top layer. Both soils are sandy soils. Using model calibration, van Dam et al. (1990) were able to estimate the fraction of mobile water (corresponding to f in Equation (10) here) at three depth intervals for each of the two soils. Because, for a

given depth, the water content did not change significantly during the tests, the assumption of the constant fraction of mobile water for a given depth interval, used in van Dam et al. (1990), is reasonable and not inconsistent with our Equation (10). As shown in Fig 2, although the number of data points is limited for a given soil, the results of van Dam et al. (1990) are fairly well represented by Equation (10) with different y values for the two different soils. The soil with the water-repellent top layer has a larger y value (0.8) and therefore a larger degree of preferential flow, which is consistent with findings in the literature (van Dam et al., 1990). Larsson et al. (1999) used the similar mobile/immobile model to analyze test results for a sandy soil. Again, water content for a given depth did not change significantly during tests. Fig. 2 also shows that the results of Larsson et al. (1999) are consistent with Equation (10) with $\gamma = 0.4$. Note that in the studies of van Dam et al. (1990) and Larsson et al. (1999), macropores did not come to play in the observed flow process. Recently, a number of studies of dye-stained preferential pathways have been published in the literature. Unfortunately, most of these studies did not include measurements of water content (or saturation) within the pathways, and therefore, cannot be used to directly evaluate Equation (10). One exception is the study reported by Öhrström et al. (2002). The tests were performed for six plots located in a clayey-soil site containing a considerable amount of macropores in the top layers. Soil samples were collected from an auger before and after tests for each plot. To compare the test results with Equation (10), we use the portion of dye coverage for a given depth as the portion of the active region. The observed water content is considered the content for the active region because it is higher than the initial water content observed before the tests started.

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Saturation within the active region is estimated from the observed water content. Because 1 2 residual water content is not available, it is assumed to be zero. For a given depth, the average active water saturation (S_e*) is estimated by the water saturation in the active 3 region multiplied by the observed portion of dye coverage at that depth. Fig. 3 shows the 4 data points at depths of 15, 50 and 75 cm for the six plots. As indicated in Öhrström et al. 5 (2002), because water content values were observed from a single auger for a plot and 6 water content may be highly variable, the observed water content data may only be 7 8 indicative of actual soil water contents. Nevertheless, Fig 3 shows that the data points can be very well represented by our Equation (10) with $\gamma = 0.8$. 9 The consistency between Equation (10) and the data points from different test sites 10 supports the usefulness of the active region model. Considering the relative simplicity of 11 the model and its capability for capturing fractal flow patterns, we believe that the active 12 13 region model can be used as a practical tool to deal with often-observed preferential flow and transport. As expected, the y parameter is site specific (Figures 2 and 3). The 14 relationship of this parameter to other soil hydraulic parameters is important for practical 15 applications, but not clear at this stage. This issue needs to be investigated in future 16

5. Conclusions

research.

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Preferential flow and transport are common processes in unsaturated soils.

Development of theoretically rigorous and practically useful models is a current challenge. Existing field evidence indicates that complex preferential flow patterns are fractals. The success of the developed discrete models in describing preferential flow at small scales is based on their ability to generate fractal patterns. In this study, we

developed a relatively simple active region model to incorporate the fractal flow pattern into the continuum approach. In the model, the flow domain is divided into active and inactive regions. Flow occurs preferentially in the active region (characterized by fractals) and inactive region is simply bypassed. Consistency between field observations and the proposed model supports the usefulness of the model. However, further studies are needed for more comprehensive evaluation of the active region model and for developing relations between the γ parameter (defined in Equation (10)) and the other soil hydraulic parameters.

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1 Figures

- Fig. 1. Demonstration of the "box" counting procedure for several box sizes
- 4 Fig. 2 Comparison between Equation (10) and data from van Dam et al. (1990)
- 5 and Larsson et al. (1999). Note that Gamma here represents the factor γ in Equation (10).
- 6 Fig. 3 A comparison between Equation (10) and data from Ohrstrom et al. (2002). Note
- 7 that Gamma here represents the factor γ in Equation (10).



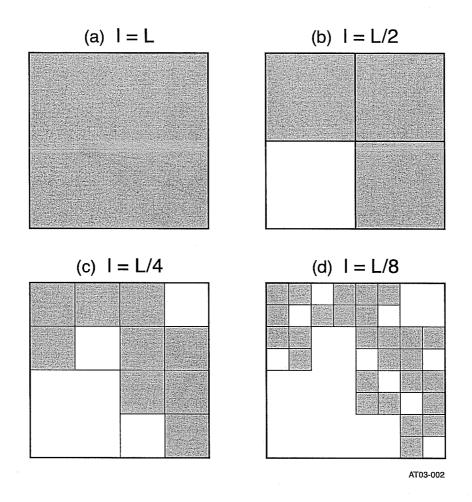


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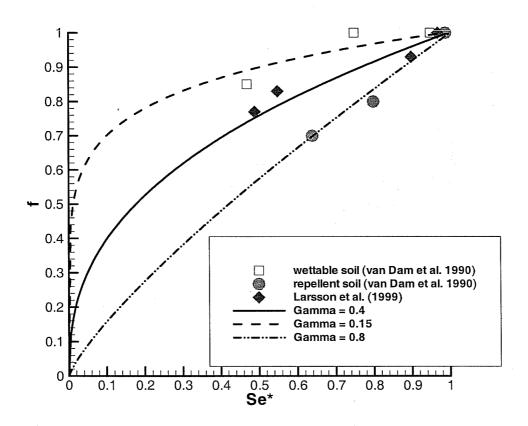


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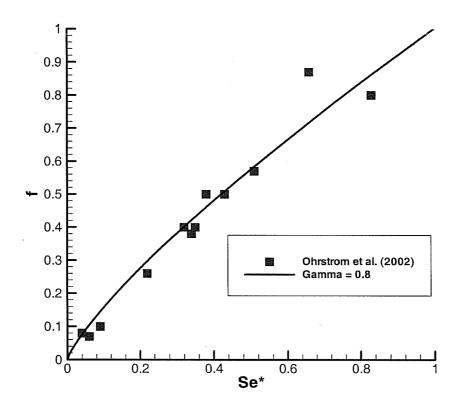


Fig. 3 A comparison between Equation (10) and data from Ohrstrom et al. (2002)