UC San Diego

UC San Diego Previously Published Works

Title

Gyrokinetic theory of turbulent acceleration and momentum conservation in tokamak plasmas

Permalink

<https://escholarship.org/uc/item/2sh450qv>

Journal

Plasma Science and Technology, 20(7)

ISSN

1009-0630

Authors

WANG, Lu
PENG, Shuitao
DIAMOND, PH

Publication Date

2018-07-01

DOI

10.1088/2058-6272/aab5bc

Peer reviewed

Gyrokinetic theory of turbulent acceleration and momentum conservation in tokamak plasmas

Lu Wang^{*1}, Shuitao Peng¹, and P. H. Diamond²

¹International Joint Research Laboratory of Magnetic Confinement Fusion and Plasma Physics, State Key Laboratory of Advanced Electromagnetic Engineering and Technology, School of Electrical and Electronic Engineering, Huazhong University of Science and Technology, Wuhan, 430074, China

²Center for Momentum Transport and Flow Organization and Center for Astrophysics and Space Sciences, University of California at San Diego, La Jolla, CA 92093-0424, USA

*Author to whom any correspondence should be addressed, E-mail: luwang@hust.edu.cn

Abstract: Understanding the generation of intrinsic rotation in tokamak plasmas is crucial for future fusion reactors such as ITER. We proposed a new mechanism named turbulent acceleration for the origin of the intrinsic parallel rotation based on gyrokinetic theory. The turbulent acceleration acts as a local source or sink of parallel rotation, i.e., volume force, which is different from the divergence of residual stress, i.e., surface force. However, the order of magnitude of turbulent acceleration can be comparable to that of the divergence of residual stress for electrostatic ion temperature gradient (ITG) turbulence. A possible theoretical explanation for the experimental observation of electron cyclotron heating (ECH) induced decrease of co-current rotation was also proposed via comparison between the turbulent acceleration driven by ITG turbulence and that driven by collisionless trapped electron mode (CTEM) turbulence. We also extended this theory to electromagnetic ITG turbulence and investigated the electromagnetic effects on intrinsic parallel rotation drive. Finally, we demonstrated that the presence of turbulent acceleration does not conflict with momentum conservation.

Keywords: Turbulent acceleration, intrinsic rotation, momentum conservation.

1. Introduction

The intrinsic rotation can be generated by a self-organization process in turbulent atmosphere. This phenomenon is widely discovered in nature, such as the planetary atmosphere [1], solar tachocline [2], as well as in laboratory, such as the intrinsic rotation in tokamak plasmas [3]. The intrinsic rotation in tokamak plasmas has been extensively studied for decades since rotation is helpful for stabilizing magnetohydrodynamic (MHD) instabilities such as resistive wall modes (RWMs) [4, 5] and neoclassical tearing modes (NTMs) [6], and plays an important role in improving plasma confinement by suppressing micro-turbulence [7-9]. In addition, another idea to control tokamak plasma turbulence via

artificial intelligence techniques with using artificial neural networks was also proposed recently [10].

What the mechanisms account for the intrinsic rotation drive is still an open question. We proposed a new mechanism named turbulent acceleration for the intrinsic parallel rotation drive by electrostatic ion temperature gradient (ITG) turbulence [11]. The turbulent acceleration cannot be written as a divergence of stress term, which is different from the physics of residual stress, and so acts as a local source or sink. In other words, the turbulent acceleration is an effective volume-force, while the divergence of residual stress is a kind of surface-force. We also proposed a possible theoretical explanation for the experimental observation of electron cyclotron heating (ECH) induced decrease of co-current core toroidal rotation via the comparison between the turbulent acceleration driven by ITG turbulence and that driven by collisionless trapped electron mode (CTEM) turbulence [12]. Then, we extended our theory to electromagnetic ITG turbulence and found the importance of electromagnetic effects on intrinsic parallel rotation drive [13]. Finally, we demonstrated that the conserved quantity corresponding to axisymmetry is the total canonical momentum or total momentum carried by both particles and electromagnetic fields, and the presence of turbulent acceleration does not imply its confliction with momentum conservation [14].

The rest of this paper is organized as follows. In Section 2, the new mechanism named turbulent acceleration for electrostatic ITG turbulence and the comparison of turbulent acceleration between ITG turbulence and CTEM turbulence are presented. Then, an extension to electromagnetic ITG turbulence and some discussions on relevant experiments are given in Section 3. The relationship between the turbulent acceleration and the momentum conservation law is clarified in Section 4. Finally, we make a summary and discuss our future work in Section 5.

2. Turbulent acceleration driven by electrostatic turbulence

2.1. Electrostatic ITG turbulence

Starting from the conservative form of the nonlinear electrostatic gyrokinetic equation in the continuity form [15]

$$\frac{\partial}{\partial t}(FB_{\parallel}^*) + \nabla \cdot \left(\frac{d\mathbf{R}}{dt} FB_{\parallel}^* \right) + \frac{\partial}{\partial v_{\parallel}} \left(\frac{dv_{\parallel}}{dt} FB_{\parallel}^* \right) = 0, \quad (1)$$

with gyrocenter equations of motion

$$\frac{d\mathbf{R}}{dt} = v_{\parallel} \hat{\mathbf{b}} + \frac{c}{eB_{\parallel}^*} \hat{\mathbf{b}} \times (e\nabla \langle \delta\phi_{gc} \rangle) + \mu \nabla B + m_i v_{\parallel}^2 \hat{\mathbf{b}} \cdot \nabla \hat{\mathbf{b}}, \quad (2)$$

and

$$\frac{dv_{\parallel}}{dt} = -\frac{\mathbf{B}^*}{m_i B_{\parallel}^*} \cdot (e\nabla \langle \delta\phi_{gc} \rangle + \mu \nabla B). \quad (3)$$

Here, $F = F(\mathbf{R}, \mu, v_{\parallel}, t)$ is the gyrocenter distribution function, μ is the gyrocenter magnetic moment and $v_{\parallel} = \mathbf{v} \cdot \hat{\mathbf{b}}$ is the parallel velocity of ions' gyrocenter, $B_{\parallel}^* \equiv \hat{\mathbf{b}} \cdot \mathbf{B}^*$ is the Jacobian of the transformation from particle phase space to the gyrocenter phase space with $\mathbf{B}^* = \mathbf{B} + \frac{m_i c}{e} v_{\parallel} \nabla \times \hat{\mathbf{b}}$, and $\mathbf{B}$ is the equilibrium magnetic field with $\hat{\mathbf{b}} = \frac{\mathbf{B}}{B}$. m_i is the ion mass, $\delta\phi_{gc}$ is the gyrocenter electric potential fluctuation, and $\langle \langle \dots \rangle \rangle$ denotes gyroaveraging. In the following, we denote $\langle \langle \delta\phi_{gc} \rangle \rangle = \delta\phi$ since a long wavelength approximation $k_{\perp}^2 \rho_i^2 \ll 1$ is used, where $k_{\perp}$ is the perpendicular wave number and $\rho_i = \frac{v_{thi}}{\Omega_i}$ is the ion Larmor radius with $v_{thi} = \sqrt{\frac{T_i}{m_i}}$ being the ion thermal velocity and $\Omega_i = \frac{eB}{m_i}$ being the ion cyclotron frequency. In this paper, the index $\parallel$ refers to the components parallel to the equilibrium magnetic field, and the index $\perp$ refers to the components perpendicular to the equilibrium magnetic field. Note that the usual experimentally measured quantity is the ion parallel flow velocity rather than the ion parallel momentum density, so we focus on the mean parallel flow velocity equation. By taking the zeroth order and the first order moments of Eq. (1), decoupling the density from momentum density equation and taking flux average of parallel flow equation, we can finally obtain the evolution equation of the mean parallel flow velocity [11]

$$\frac{\partial \langle U_{\parallel} \rangle}{\partial t} + \nabla \cdot \Pi_{r,\parallel} = a_{\parallel}. \quad (4)$$

Here, $U_{\parallel}$ is the ion parallel flow velocity and $\langle \dots \rangle$ denotes flux average. $\Pi_{r,\parallel} = \langle \delta \mathbf{v}_{E \times B, r} \delta U_{\parallel} \rangle$ is the usual parallel Reynolds stress with $\delta \mathbf{v}_{E \times B} = \frac{c \hat{\mathbf{b}} \times \nabla \delta \phi}{B}$ being the fluctuating $\mathbf{E} \times \mathbf{B}$ drift velocity and $\delta U_{\parallel}$ being the parallel flow fluctuation, which consists of three terms including diffusion, convection, and residual stress $\Pi_{r,\parallel}^{\text{res}}$. The parallel Reynolds stress has been intensively investigated [16, 17], $a_{\parallel} = \frac{1}{m_i n_0} \langle \delta \hat{n} \hat{\mathbf{b}} \cdot \nabla \delta P_{\parallel i} \rangle$ is the *turbulent acceleration* with $\delta \hat{n} = \frac{\delta n}{n_0}$ being the normalized density fluctuation and $\delta P_{\parallel i}$ being the ion pressure fluctuation with $P_{\parallel i} = 2\pi \int dv_{\parallel} d\mu B_{\parallel}^* F v_{\parallel}^2 = n_i T_i$. The turbulent acceleration cannot be written as a divergence of the parallel Reynolds stress, and plays a role of local source/sink of parallel rotation. Its existence does not depend on the magnetic geometry and it is independent of the mean parallel velocity or the gradient of mean parallel velocity. Therefore, it is a *new* candidate mechanism for the origin of intrinsic rotation.

For electrostatic ITG turbulence, an adiabatic electron response is assumed, i.e., $\delta \hat{n} =$

$\delta\hat{\phi}_k$ with $\delta\hat{\phi}_k = \frac{e\delta\phi_k}{T_e}$. By linearizing the ion pressure equation we can obtain the ion pressure fluctuation

$$\delta P_{\parallel i} = P_{\parallel i} \frac{\omega_{*e}}{\omega_r} \left(1 - i \frac{|\gamma_k|}{\omega_r}\right) \delta\hat{\phi}_k, \quad (5)$$

where ω_r and γ_k are real frequency and linear growth rate, respectively. Then, a quasilinear expression for the turbulent acceleration can be written as [10]

$$a_{\parallel} = \frac{1}{m_i n_0} \langle \delta \hat{n} \hat{\mathbf{b}} \cdot \nabla \delta P_{\parallel i} \rangle \approx \tau (1 + \eta_i) \frac{1}{L_n} \sum_k \Pi_{ES,k}, \quad (6)$$

where $\tau = \frac{T_i}{T_e}$, $\eta_i = \frac{L_n}{L_{Ti}}$ with L_n being the density gradient scale length and L_{Ti} being the ion temperature gradient scale length. $\Pi_{r,\parallel}^{\text{res}} = \sum_k \Pi_{ES,k} = \sum_k \rho_s c_s^3 \frac{|\gamma_k|}{\omega_r^2} k_{\theta} k_{\parallel} |\delta\hat{\phi}_k|^2$ is electrostatic residual stress which is consistent with previous result [16], $c_s = \sqrt{\frac{T_e}{m_i}}$ is the ion acoustic velocity and $\rho_s = \frac{c_s}{\Omega_i}$. By taking the parallel symmetry breaking induced by intensity gradient [17], i.e., $I_k(x) = |\delta\hat{\phi}_k|^2(x) = I_k(0) + x \left(\frac{\partial I_k}{\partial x} \right)$ and $k_{\parallel} = \frac{k_{\theta} x \hat{s}}{q R_0}$, where $\hat{s}$ is the magnetic shear, q is the safety factor, R_0 is the major radius, $x = r_{m,n} - r$, with $r_{m,n}$ being the radial location of the resonant surface, we can obtain the turbulent acceleration

$$a_{\parallel} \approx \tau (1 + \eta_i) \frac{1}{L_n} \frac{\hat{s}}{q R_0} \sum_k \rho_s c_s^3 \frac{|\gamma_k|}{\omega_r^2} k_{\theta}^2 x^2 \frac{\partial I_k}{\partial x}. \quad (7)$$

It is obvious that the turbulent acceleration can provide a co-current intrinsic rotation drive for positive magnetic shear ($\hat{s} > 0$) and positive intensity gradient ($\frac{\partial I_k}{\partial x} > 0$). For convenience of comparison, the divergence of the residual stress obtained in Ref. [16] is written as

$$\nabla \cdot \Pi_{r,\parallel}^{\text{res}} \approx \pm \frac{1}{L} \frac{\hat{s}}{q R_0} \sum_k \rho_s c_s^3 \frac{|\gamma_k|}{\omega_r^2} k_{\theta}^2 x^2 \frac{\partial I_k}{\partial x}. \quad (8)$$

Here, L is the scale length of the radial variation of the residual stress. Thus, the ratio of the turbulent acceleration to the divergence of the residual stress is $\tau (1 + \eta_i) \frac{L}{L_n}$, which means the turbulent acceleration can be comparable to the divergence of the residual stress, depending upon $\tau (1 + \eta_i)$ and $\frac{L}{L_n}$. Hence, the new mechanism of turbulent acceleration is qualitatively different from the usual Reynolds stress, but it is quantitatively comparable to

the divergence of residual stress.

2.2. Electrostatic CTEM turbulence

For CTEM turbulence, by using quasi-neutrality condition, the ion gyrocenter density fluctuation can be approximated by the electron density fluctuation without considering finite Larmor radius effects, which is consist of adiabatic response and non-adiabatic response, i.e., $\delta \hat{n} \simeq \left(1 - i \frac{|\gamma_k|}{\omega_r}\right) \delta \hat{\phi}_k$ [12]. There is no phase shift between the density fluctuation and the ion pressure fluctuation (Eq. (5)), so the turbulent acceleration vanishes [12], i.e., $a_{\parallel} = \frac{1}{m_i n_0} \langle \delta \hat{n} \hat{\mathbf{b}} \cdot \nabla \delta P_{\parallel i} \rangle \approx 0$. This is different from the ITG case as mentioned above where the turbulent acceleration can provide co-current intrinsic rotation drive, and its order of magnitude can be comparable to that of the divergence of residual stress. We also note that the residual stress driven by CTEM turbulence is an outward flux of co-current rotation for positive magnetic shear ($\hat{s} > 0$) and positive intensity gradient ($\frac{\partial I_k}{\partial x} > 0$), leading to flattening of co-current rotation or an increment of counter-current rotation [12]. Therefore, the turbulence mode transition from ITG to CTEM may result in a reduction of co-current rotation. This is because the co-current turbulent acceleration for ITG turbulence vanishes for CTEM turbulence, and the divergence residual stress for CTEM turbulence provides counter-current rotation drive. This may offer a theoretical explanation for the experimental observation of co-current core toroidal rotation reduction in co-current neutral beam injection (NBI) heated L-mode [18] and H-mode plasmas [19, 20] with ECH turning on.

Conversely, the turbulence mode transition from CTEM to ITG can lead to increase of co-current rotation. This is qualitatively consistent with the experimental observation in TCV tokamak where the toroidal rotation inverts its sign spontaneously from the counter-current to co-current direction after electron density exceeding a well-defined threshold [21]. The turbulence mode transition from trapped electron mode (TEM) to ITG occurs at the transition from linear Ohmic confinement (LOC) to saturated Ohmic confinement (SOC) during the density ramp up. The phenomena of rotation reversal were also observed in Alcator C-Mod tokamak [22, 23], but the direction of rotation reversal is from co-current to counter-current. The difference between the experimental observation from TCV and that from Alcator C-Mod may result from the different boundary condition with limiter configuration in TCV and divertor configuration in Alcator C-Mod, which has not been well understood yet.

3. Intrinsic rotation drive by electromagnetic ITG turbulence

For electromagnetic turbulence, the shear component of magnetic perturbation, i.e., $\delta A_{\parallel}$, is considered [13]. Starting from the nonlinear electromagnetic gyrokinetic equation with

gyrocenter equations of motion in the symplectic formulation (i.e., $v_{\parallel}$ representation)

$$\frac{d\mathbf{R}}{dt} = v_{\parallel} \hat{\mathbf{b}}^* + \frac{c}{eB} \hat{\mathbf{b}} \times e \nabla \langle \delta \phi \rangle \quad (9)$$

and

$$\frac{dv_{\parallel}}{dt} = -\frac{e}{m_i} \left(\hat{\mathbf{b}}^* \cdot \nabla \langle \delta \phi \rangle + \frac{1}{c} \frac{\partial \langle \delta A_{\parallel} \rangle}{\partial t} \right). \quad (10)$$

Here, uniform equilibrium magnetic field $\mathbf{B}$ is assumed. $\mathbf{B}^* = \mathbf{B} + \delta \mathbf{B}_{\perp}$, $\delta \mathbf{B}_{\perp} = -\hat{\mathbf{b}} \times \nabla \delta A_{\parallel}$. $\hat{\mathbf{b}}^* = \hat{\mathbf{b}} + \delta \hat{\mathbf{B}}_{\perp}$ with $\delta \hat{\mathbf{B}}_{\perp} = \frac{\delta \mathbf{B}_{\perp}}{B}$. By taking the process similar to electrostatic case, we can obtain the mean field equation of the parallel flow velocity

$$\begin{aligned} \frac{\partial \langle U_{\parallel} \rangle}{\partial t} + \nabla \cdot \langle \delta \mathbf{v}_{E \times B, r} \delta U_{\parallel} \rangle + \frac{1}{m_i n_0} \nabla \cdot \langle \delta \hat{\mathbf{B}}_r \delta P_{\parallel i} \rangle + \frac{e}{m_i} \nabla \cdot \langle \delta \hat{\mathbf{B}}_r \delta \phi \rangle \\ = \frac{1}{m_i n_0} \left[\langle \delta \hat{n} \hat{\mathbf{b}} \cdot \nabla \delta P_{\parallel i} \rangle + \langle \delta \hat{n} \delta \hat{\mathbf{B}}_r \rangle \cdot \nabla P_{\parallel i} \right]. \end{aligned} \quad (11)$$

Here, $\langle \delta \hat{\mathbf{B}}_r \delta P_{\parallel i} \rangle$ is known as the kinetic stress [24, 25] and it is somewhat analogous to the kinetic dynamo physics which is a transport process of electron parallel momentum (current) [25, 26]. The kinetic stress was experimentally identified to drive the intrinsic parallel plasma flow in MST [24]. $\langle \delta \hat{\mathbf{B}}_r \delta \phi \rangle$ is the cross Maxwell stress, which was also presented in Ref. [27]. Both kinetic stress and cross Maxwell stress are surface force since they enter the parallel flow equation via their divergence. This is similar to the usual Reynolds stress $\langle \delta \mathbf{v}_{E \times B, r} \delta U_{\parallel} \rangle$. While, the turbulent acceleration on the right hand side (RHS) of Eq. (11) is an effective volume-force, because it cannot be recast into the divergence of stress term. $\frac{1}{m_i n_0} \langle \delta \hat{n} \hat{\mathbf{b}} \cdot \nabla \delta P_{\parallel i} \rangle$ is the turbulent acceleration driven by parallel gradient of ion pressure fluctuation, which has been investigated for electrostatic turbulence as mentioned above. $\frac{1}{m_i n_0} \langle \delta \hat{n} \delta \hat{\mathbf{B}}_r \rangle \cdot \nabla P_{\parallel i}$ is a new turbulent acceleration related to the correlation between density and magnetic fluctuations and the equilibrium ion pressure gradient as well. Combining these two terms, the total electromagnetic turbulent acceleration can be rewritten as $\frac{1}{m_i n_0} \langle \delta \hat{n} \delta (\hat{\mathbf{b}}^* \cdot \nabla P_{\parallel i}) \rangle$, which represents the correlation between density fluctuation and perturbed pressure gradient along the total magnetic field.

Quasilinear estimates of all the intrinsic rotation drive can be calculated for the typical parameters of the pedestal top region on DIII-D where the dominant instability is electromagnetic ITG turbulence [28]. The total stress force can be written as

$$\Lambda_{\text{tot}} = \mp \frac{1}{L'} \sum_k \Pi_{ES, k} (1 - 23 \hat{\beta}_e), \quad (12)$$

and the total turbulent acceleration is

$$a_{\text{tot}} = \frac{1}{L_n} \sum_k \Pi_{ES,k} 16 \left(1 + \frac{17}{4} \hat{\beta}_e \right). \quad (13)$$

Here, L' is the scale length of the radial variation of the stresses and $\sum_k \Pi_{ES,k}$ is the electrostatic residual stress mentioned in section 2.1. $\hat{\beta}_e = \beta_e \frac{q^2 R_0^2}{L_n^2} \approx 0.144$ for the typical parameters of the pedestal top region on DIII-D with $\beta_e = \frac{8\pi n_0 T_e}{B^2} \approx 0.4\%$, and the terms related to $\hat{\beta}_e$ come from electromagnetic effects. From Eqs. (12) and (13), we can see that the electromagnetic effects can reduce the electrostatic stress force and even reverse it, but enhance the turbulent acceleration, and the total turbulent acceleration is comparable to the total stress force. Therefore, taking into account the electromagnetic effects and the turbulent acceleration is important for more accurate understanding and prediction of intrinsic rotation in pedestal region.

Now, we discuss some possible relevant experimental observations. In the MST, the kinetic stress related to density fluctuations $\langle \delta \hat{n} \delta \hat{\mathbf{B}}_r \rangle$ was directly measured [24], so the turbulent acceleration related to the kinetic stress (i.e., $\frac{1}{m_i n_0} \langle \delta \hat{n} \delta \hat{\mathbf{B}}_r \rangle \cdot \nabla P_{\parallel i}$) can be also easily obtained there. This turbulent acceleration $\frac{1}{m_i n_0} \langle \delta \hat{n} \delta \hat{\mathbf{B}}_r \rangle \cdot \nabla P_{\parallel i}$ can provide counter-current rotation drive for normal ion pressure profile ($\nabla P_{\parallel i} < 0$) and positive kinetic stress. Taking this turbulent acceleration into account in the intrinsic flow drive of MST will lead to the reversal point of flow drive closer to that of the plasma parallel flow [24], which may result in better agreement between the intrinsic flow drive and the observed parallel flow profile.

4. Turbulent acceleration and momentum conservation

As mentioned above, turbulent acceleration is obtained by decoupling density from the gyrocenter parallel momentum density equation and then taking flux average of flow velocity, i.e.,

$$\frac{\partial \langle U_{\parallel} \rangle}{\partial t} = \left\langle \frac{1}{n} \left[\frac{\partial (n U_{\parallel})}{\partial t} - U_{\parallel} \frac{\partial n}{\partial t} \right] \right\rangle. \quad (14)$$

Besides, there is an alternative method to derive the mean parallel flow velocity equation by taking flux average of the gyrocenter parallel momentum density first, and then decoupling flow velocity and density as follows

$$\frac{\partial \langle U_{\parallel} \rangle}{\partial t} = \frac{1}{n_0} \left[\frac{\partial \langle n U_{\parallel} \rangle}{\partial t} - \langle U_{\parallel} \rangle \frac{\partial n_0}{\partial t} - \langle \delta U_{\parallel} \frac{\partial}{\partial t} \delta n \rangle - \langle \delta n \frac{\partial}{\partial t} \delta U_{\parallel} \rangle \right]. \quad (15)$$

Through Eqs. (14) and (15), we can obtain the same mean field equation of the parallel flow velocity (i.e., Eq. (11)) regardless of the sequence of taking flux average and decoupling the

parallel flow from parallel momentum density [14]. Therefore, the presence of the turbulent acceleration does not result from regrouping terms as one may wonder.

By taking summation of gyrocenter momentum density equation over both species and using quasi-neutrality condition for electron density n_e and ion gyrocenter density $\bar{n}_i$, i.e., $n_e - \bar{n}_i = n_{\text{pol}}$ with $n_{\text{pol}} = \nabla_{\perp} \cdot \left(\frac{c^2 m_i n_0}{e B^2} \nabla_{\perp} \delta \phi \right)$ being ion polarization density, we can obtain the gyrocenter momentum conservation equation after some algebra [14]

$$\frac{\partial}{\partial t} \sum_s \langle \bar{p}_{\parallel s} \rangle + \nabla_r \cdot \langle \delta v_{E \times B, r} \delta (m_i \bar{n}_i \bar{U}_{\parallel i}) + \delta \hat{\mathbf{B}}_r \delta \bar{P} \rangle - \nabla_r \cdot \langle \frac{c^2 m_i n_0}{B^2} \nabla_r \delta \phi \hat{\mathbf{b}} \cdot \nabla \delta \phi \rangle = 0, \quad (16)$$

where s includes ions and electrons, $\sum_s \langle \bar{p}_{\parallel s} \rangle = \langle m_i \bar{n}_i \bar{U}_{\parallel i} - n_{\text{pol}} \frac{e}{c} \delta A_{\parallel} \rangle$ with $\bar{p}_{\parallel s} = m_s \bar{n}_s \bar{U}_{\parallel s} + \bar{n}_s \frac{e_s}{c} \delta A_{\parallel}$ being the gyrocenter canonical parallel momentum of one species including the ordinary gyrocenter kinematic momentum and the gyrocenter magnetic vector momentum. The ordinary kinematic momentum carried by electrons was neglected because of small electron mass as compared to ion mass ($m_e \ll m_i$). $-n_{\text{pol}} \frac{e}{c} \delta A_{\parallel}$ is the total gyrocenter magnetic vector momentum resulting from the ion polarization density n_{pol} . Then, we obtain the conservation equation of the total gyrocenter canonical parallel momentum carried by ions and electrons. The terms under the divergence are radial flux of the ion gyrocenter parallel kinematic momentum, total kinetic stress and electric Maxwell stress, respectively. By using the relationship between total gyrocenter magnetic vector momentum and the electromagnetic fields momentum

$$\frac{\partial \langle -n_{\text{pol}} \frac{e}{c} \delta A_{\parallel} \rangle}{\partial t} = \frac{\partial \langle m_i n_0 \frac{c^2}{B^2} (\delta \mathbf{E} \times \delta \mathbf{B})_{\parallel} \rangle}{\partial t} - \nabla \cdot \langle \frac{c^2 m_i n_0}{B^2} \nabla_r \delta \phi \frac{1}{c} \frac{\partial \delta A_{\parallel}}{\partial t} \rangle, \quad (17)$$

Eq. (16) can be rewritten as

$$\begin{aligned} \frac{\partial}{\partial t} \langle m_i \bar{n}_i \bar{U}_{\parallel i} + m_i n_0 \frac{c^2}{B^2} (\delta \mathbf{E} \times \delta \mathbf{B})_{\parallel} \rangle + \nabla_r \cdot \langle \delta v_{E \times B, r} \delta (m_i \bar{n}_i \bar{U}_{\parallel i}) + \delta \hat{\mathbf{B}}_r \delta \bar{P} \rangle \\ - \nabla_r \cdot \langle \frac{c^2 m_i n_0}{B^2} \nabla_r \delta \phi \left(\hat{\mathbf{b}} \cdot \nabla \delta \phi + \frac{1}{c} \frac{\partial \delta A_{\parallel}}{\partial t} \right) \rangle = 0. \end{aligned} \quad (18)$$

This is another conservative format of momentum which is the total gyrocenter parallel momentum density including the ion gyrocenter kinematic momentum and electromagnetic fields momentum. The pieces under the divergence are radial flux of the ion gyrocenter kinematic momentum, total kinetic stress, and electric Maxwell stress including both parallel electrostatic field and inductive electric field.

These two gyrocenter momentum conservation equations mentioned above (i.e., Eqs. (16) and (18)) are equivalent. We can see that the conserved quantity can be either the total gyrocenter parallel canonical momentum carried by both species or the total gyrocenter parallel momentum including the ion gyrocenter kinematic momentum and the electromagnetic fields momentum, but not the ion parallel kinematic momentum or the ion

parallel flow velocity. Hence, the turbulent acceleration-the local source or sink of the mean ion parallel flow *does not* imply that the momentum conservations is broken [14].

5. Summary and discussions

A new mechanism for the origin of intrinsic rotation named turbulent acceleration has been discovered. It cannot be written as a divergence of stress term and acts as the local source or sink of parallel rotation. The order of magnitude of turbulent acceleration is comparable to that of the divergence of residual stress which is also thought to be the origin of intrinsic rotation in previous works. Therefore, the turbulent acceleration is significant for intrinsic rotation. The co-current acceleration driven by electrostatic ITG turbulence vanishes after mode transition to CTEM turbulence, which qualitatively agrees with experimental observations. An extension to electromagnetic ITG turbulence has also been investigated, showing that the electromagnetic effects are important for both stress force and turbulent acceleration. We have derived two equivalent equations of momentum conservation and discussed the conserved quantity corresponding to the axisymmetry of tokamak plasmas. We clarified that the turbulent acceleration does not contradict with momentum conservation law.

Our ongoing work is extending to toroidal geometry, such as considering kinetic ballooning mode, which is the dominant electromagnetic mode in the peaked gradient region of DIII-D pedestal plasmas [28]. Moreover, inspired by the investigation of intrinsic rotation (which is mainly carried by ions) driven by turbulence, we are also working on the intrinsic non-inductive current (which is mainly carried by electrons) driven by turbulence. This could be also important for tokamak performance, since the modification of current profile may affect the confinement and a variety of MHD instabilities.

Acknowledgments

These works are supported by the NSFC Nos. 11675059 and 11305071, and the Ministry of Science and Technology of China under Contract No. 2013GB112002.

References

- [1] Baldwin M P, Rhines P B, Huang H-P, *et al* 2007 *Science* **315** 467
- [2] Hughes D W *et al* 2007 *The Solar Tachocline (Cambridge: Cambridge University Press)*
- [3] Rice J E, Ince-Cushman A, deGrassie J S, *et al* 2007 *Nucl. Fusion* **47** 1618
- [4] Bondeson A and Ward J D 1994 *Phys.Rev. Lett.* **72** 2709
- [5] Betti R and Freidberg J P 1995 *Phys. Rev. Lett.* **74** 2949
- [6] Politzer P A, Petty C C, Jayakumar R J, *et al* 2008 *Nucl. Fusion* **48** 075001
- [7] Biglari H, Diamond P H and Terry P W 1990 *Phys. Fluids B* **2** 1
- [8] Hahm T S and Burrell K H 1995 *Phys. Plasmas* **2** 1648

- [9] Terry P W 2000 *Rev. Mod. Phys.* **72** 109
- [10] Rastovic D 2007 *J. Fusion Energy* **26** 337; Rastovic D 2012 *Journal of Modern Physics* **3** 1858;
Rastovic D 2015 *J. Fusion Energy* **34** 207
- [11] Wang L and Diamond P H 2013 *Phys. Rev. Lett.* **110** 265006
- [12] Wang L, Peng S and Diamond P H 2016 *Phys. Plasmas* **23** 042309
- [13] Peng S, Wang L and Pan Y 2017 *Nucl. Fusion* **57** 036003
- [14] Peng S, Wang L 2017 *Phys. Plasmas* **24** 012304
- [15] Hahm T S 1988 *Phys. Fluids* **31** 2670
- [16] Diamond P H, Kosuga Y, Gürçan Ö D, *et al* 2013 *Nucl. Fusion* **53** 104019
- [17] Gürçan Ö D, Diamond P H, Hennequin P, *et al* 2010 *Phys. Plasmas* **17** 112309
- [18] Shi Y J, Ko S H, Kwon J M, *et al* 2016 *Nucl. Fusion* **56** 016014
- [19] Shi Y J, Ko W H, Kwon J M, *et al* 2013 *Nucl. Fusion* **53** 113031
- [20] McDermott R M, Angioni C, Dux R, *et al* 2011 *Plasma Phys. Control. Fusion* **53** 124013
- [21] Bortolon A, Duval B P, Pochelon A, *et al* 2006 *Phys. Rev. Lett.* **97** 235003
- [22] Rice J E, Duval B P, Reinke M L, *et al* 2011 *Nucl. Fusion* **51** 083005
- [23] Reinke M L, Rice J E, White A E, *et al* 2013 *Plasma Phys. Control. Fusion* **55** 012001
- [24] Ding W X, Lin L, Brower D L, *et al* 2013 *Phys. Rev. Lett.* **110** 065008
- [25] Prager S C 1999 *Plasma Phys. Control. Fusion* **41** A129
- [26] Lee G S, Diamond P H and An Z G 1989 *Phys. Fluids B* **1** 99
- [27] Kaang H H, Jhang H, Singh R, *et al* 2016 *Phys. Plasmas* **23** 052501
- [28] Holod I, Fulton D and Lin Z 2015 *Nucl. Fusion* **55** 093020