Lawrence Berkeley National Laboratory
Recent Work

**Title**
Thermo-hydrologic processes in maar eruptions: The role of vapor transport and condensation

**Permalink**
https://escholarship.org/uc/item/2sx7s2kg

**Authors**
Anderson, ES
Ort, MH
Oldenburg, CM

**Publication Date**
2020-03-01

**DOI**
10.1016/j.jvolgeores.2020.106809

Peer reviewed
Thermo-Hydrologic Processes in Maar Eruptions:
The Role of Vapor Transport and Condensation

Emily S. Anderson¹, Michael H. Ort¹, Curtis M. Oldenburg²

¹ School of Earth and Sustainability, Box 4099, Northern Arizona University, Flagstaff, AZ 86011 USA

² Energy Geosciences Division, Lawrence Berkeley National Laboratory, 1 Cyclotron Rd., Berkeley, CA 94720 USA

Note this is a near-final manuscript form of the final paper published in Journal of Volcanology and Geothermal Research. Please read and cite the final paper:

Introduction

Phreatomagmatic eruptions occur when magma interacts directly with water or slurries, commonly from groundwater in the shallow crust, resulting in rapid conversion of thermal energy to mechanical energy in a set of processes known as molten fuel-coolant interaction (MFCI). The efficiency of MFCI is controlled by properties of the magma and coolant, contact surface geometry, and system conditions, such as pressure and temperature; phreatomagmatic behavior can range from passive thermal granulation to violent thermohydraulic explosions (Zimanowski et al., 2015). Maar-diatreme eruptions, characterized by repetitive phreatomagmatic explosions, can form in a wide range of near-surface environments, from soft-sediment substrate (e.g., Tecuitlapa, Mexico, Ort and Carrasco-Núñez, 2009; Hopi Buttes, AZ, Lefebvre et al., 2013) to hard, fractured country rock (e.g., West Eifel volcanic field, Germany and Massif Central, France, Lorenz, 2003). Country-rock structure, including faults and joints, rock type, and shallow crustal hydrologic properties, can influence an eruption’s behavior by controlling how much and at what rate water can be supplied to the magma (hydraulic flow rate), and determining the sediment: water ratio in the case of soft-sediment substrate eruptions. In a “soft” substrate environment, volcanic tremor can lead to liquefaction of saturated sediment, producing a slurry that may then interact with magma in unique ways (White, 1996; Auer, et al., 2006).

Studies of maars around the world have shown the importance of magma-water interaction, but have not answered some fundamental questions about how aqueous-phase water was present and available to interact with magma throughout an eruptive episode. We have carried out field investigations and numerical modeling directed at answering the following questions:
1. In areas with very deep water tables, how is the necessary quantity of liquid water supplied to the shallow subsurface to produce phreatomagmatic explosions?

2. How is liquid water continuously supplied to sustain a phreatomagmatic eruption without being depleted through explosions and vaporization?

In this paper, we describe a potential mechanism, the heat-pipe process (e.g., Schubert and Straus, 1979; Pruess, 1985), by which water in shallow crustal systems may be transported upward as vapor to levels higher in the subsurface where it condenses. By this mechanism, heat from shallow intrusions associated with the same eruption can potentially redistribute water to produce water-saturated domains at levels above the regional water table depth, and these domains, if rapidly intersected by magma, could lead to shallow (eruptible) phreatomagmatic explosions, provided other conditions are met. We demonstrate the mechanism of upward vapor transport and condensation by numerical simulations using TOUGH2 (Pruess et al., 2011) for an idealized shallow crustal system heated by magma. Our work suggests that knowledge of the hydraulic properties (e.g., permeability and fracture density) of bedrock is critical to understanding how water (both vapor and aqueous phases) may move through and interact with magma in the subsurface in the event of a magmatic intrusion.

1.1. Background and Prior Work

Maar-diatremes are formed by repeated magma-groundwater explosions. A maar is a broad crater cutting below the pre-eruptive surface enclosed by a <30-m-high tephra ring of repetitively bedded pyroclastic deposits (Fig. 1; Valentine and White, 2012; de Silva and Lindsay, 2015). Diatremes are debris-filled conduits beneath maars that form as explosions recycle wall rock and juvenile material. Early models of diatreme development attributed their...
formation to progressively deepening MFCI explosions as groundwater depleted and a “cone of depression” formed in the water table (Lorenz, 1986). In a current conceptual model (Fig. 1; Valentine and White, 2012), explosions may occur at any depth where groundwater is below the critical pressure of water ($P_{\text{crit}} = 22.5 \text{ MPa}$). As explosions progressively disrupt the shallow subsurface, broken-up material slumps into the diatreme/conduit, further widening the structure and producing a roughly conical diatreme that may extend to depths of 2 – 2.5 km, although shallower is more common (Valentine and White, 2012).

**Figure 1:** Modern conceptual model of maar-diatreme formation from Valentine and White (2012). Explosions may occur at any depth below the critical pressure of water, though shallow explosions are generally most efficient. The water table is probably maintained at a constant level throughout eruption, but debris jets and upward recycling within the diatreme may also assist in moving water through diatreme fill. MFCI = molten fuel-coolant interaction.

Valentine et al. (2014) estimated explosion energies in typical phreatomagmatic eruptions based on theoretical, field, and limited experimental data, and combined this information with
well-documented phenomenology of subsurface explosions that defines conditions under which explosions are contained in the subsurface versus ejecting large quantities of material onto crater rims. They concluded that explosions do occur over a range of depths throughout an eruption, but generally, because the strength of explosions tends to lie within a certain range, only those occurring above ~200 m, and mostly above ~100 m, are able to throw material out of the crater to form the tephra ring and excavate the crater. Deeper explosions rarely vent to the surface, instead transferring all of the energy into the host rock, brecciating country rock and recycling water and lithic and juvenile material within the diatreme (Graettinger et al., 2014; Valentine et al., 2014; Sonder et al., 2015).

In areas where the water table is deeper than ~200 m, the implication is that explosions may occur but few are large enough to eject material and begin to develop a crater. However, maars are observed in areas where the water table is deeper than 200 m. This necessitates a mechanism to make water available for MFCI at depths above the water table. One way is for subsurface jets of explosion debris to transport groundwater upward (White and McClintock, 2001; McClintock and White, 2006; Ross and White, 2006). In this paper, we explore another potentially important mechanism, which involves redistribution of water in the subsurface due to heat of magma intrusion. We demonstrate this using parameters relevant to two maars in the San Francisco Volcanic Field (Arizona, USA) that formed despite the deep (~350 m) water table at their locations.
2. **Approach and Methods**

2.1. **Numerical simulation of thermohydrologic processes**

We used the TOUGH2 numerical simulator (Pruess et al., 2011) to explore thermally-induced redistribution of groundwater in maar-diatreme systems. Our simulations are aimed at testing possible pre-eruptive and syneruptive thermohydrologic processes at maar-diatreme volcanoes. TOUGH2 does not model the MFCI itself, but it does simulate how water (as vapor and liquid) can ascend, driven by magmatic heat and a heat pipe mechanism, to set up the conditions for shallow explosive interaction. The heat-pipe process has been extensively studied for its ability to enhance heat transfer in geothermal systems (e.g., Schubert and Straus, 1979; Pruess, 1985; Udell, 1985; Hurst et al., 1991).

2.2. **TOUGH2 Model Setup**

TOUGH2 is a numerical simulator for non-isothermal, multiphase fluid flow in fractured and porous media (Pruess et al., 2011). The simulator solves mass and energy balance equations for fluid and heat flow in space- and time-discretized systems, with the assumption of local thermodynamic equilibrium of all phases. Capabilities of the software extend to numerous geological and hydrogeological applications through a variety of equation-of-state (EOS) modules, each of which is representative of specific fluid mixtures, or components, for which the modules provide the necessary thermophysical properties for mass and energy balance equations. The module used for this work is EOS3, which models non-isothermal water and air transport including boiling and condensation of water. We invoked TOUGH2/EOS3 from iTOUGH2 (Finsterle, 2007) which provides enhanced control features for TOUGH2 simulation runs.

Although TOUGH2/EOS3 does not include the capability to represent supercritical water ($P_{\text{crit}} > 22$ MPa, $T_{\text{crit}} > 374$ °C), it was used to investigate maar-related hydrologic processes with
the understanding that modeled temperatures are lower than would be realistically expected in volcanic eruptions, but that the processes of vaporization, upward vapor flow, condensation, and downward liquid water flow would be qualitatively analogous at higher temperatures. A second limitation to TOUGH2/EOS3 for modeling magmatic systems is that modeling full dry-out (transition from single-phase liquid or two-phase (aqueous and gas) conditions to single-phase gas) can cause convergence problems. Although we specify a non-zero liquid residual saturation ($S_{lr}$, Table 1), this value only affects flow processes, and vaporization and boiling can reduce aqueous phase saturation to values less than $S_{lr}$. Such dry-out conditions can lead to very small time-step sizes associated with poor convergence due to grid blocks oscillating back and forth within a time step between two-phase and single-phase conditions. When TOUGH2 converges on the first iteration twice in a row but fails when the time-step is automatically doubled on the next time step, the TOUGH2 simulation automatically stops, resulting in arbitrary end times for some simulations. This explains the different end times of the various simulations summarized in the Results section.

The TOUGH2 computational mesh representing the discretized physical system comprises grid blocks that are each assigned primary thermodynamic properties: pressure ($P$), temperature ($T$), and gas saturation ($S_g$) for EOS3, and material properties including permeability, porosity, and specific heat capacity. For the simulations carried out in this study, all mesh files are two-dimensional and 1 m thick in the $y$-direction (i.e., 2D Cartesian), which is appropriate for the case in which magma is intruded as a long dike trending perpendicular to the grid. The standard mesh design is a “zoomed in” view from the upper portion of the aquifer to the ground surface (Fig. 2). It is 300 m wide and 425 m deep, extending ~80 m below an approximately 345-m-deep water table. A second mesh extending 1200 m wide and 710 m deep
was also used to test the two base-case scenarios on a larger scale. We use a uniform mesh with fine resolution (grid-block size 20 m × 10 m) for all of the grid except for the upper 75 m of the standard models (Kaibab Formation, Table 2) and the lower 285 m (Supai Group) in the large models, in which grid blocks are 20 m × 15 m. The grid resolution was chosen to resolve the main heat and mass flow processes to demonstrate the mechanism of water re-distribution by heat pipe.

![Diagram](image)

**Figure 2:** Schematic diagrams showing the setups for models with rising heat injection (left) and those with a stationary heat source (right). The 1-m-thick magma dike at the base is approximately 360-m-wide, tapering up to 60-m-wide at the water table, and 20-m-wide within the fracture (up to 95 m depth) in the rising heat simulations. All orange blocks receive heat injection (5.50 × 10^7 J/s). In the rising heat simulations, heat is injected into rows of grid blocks, moving upward, at a rate corresponding to a magma ascent rate of 0.5 m/s. Boundary conditions labeled in the left diagram are the same in all models.

Initial model runs were performed to establish static steady-state gravity-capillary equilibrium water saturation profiles in the unsaturated (two-phase) subsurface prior to any heat input, and the final steady-state conditions from these simulations were then used as the starting conditions for simulations with heat injection representing magma intrusion. A 20-m-wide “fracture zone,” or a high-permeability, high-porosity feature, is located in the center of the model, intended to represent the combined effects of numerous smaller fractures or a single high-permeability zone of broken rock. For all heat injection simulations, the bottom boundary has
been assigned Dirichlet boundary conditions (i.e., constant $P$, $T$, and gas saturation), and the side and top boundaries are closed to heat (insulated) and mass flow.

Numerous forward models were carried out to understand how specific rock and thermodynamic parameters affect model outcomes. Ascending magma is modeled as heat injection into specified grid blocks, described only by a heating rate (J/s) (Anderson, 2017) (Appendix A). Total volume of liquid water moved above a depth of 205 m (the bottom depth of the row of grid blocks with center points at 200 m) at the final timestep has been calculated for some simulations, but we note these per-meter of dike volumes are strictly representative only of the two-dimensional, 1-m-thick domain or a 3D equivalent (arbitrary length perpendicular to the 2D plane of the domain) and are not strictly valid where 3D effects are present, e.g., at the ends of the dike (Anderson, 2017).

### 2.3. System properties and scenarios

The hydrologic and hydrostratigraphic properties of the modeled systems (Tables 2 and 3) are based on representative example cases, Colton Crater and Rattlesnake Crater. Our models are not meant to specifically model all the conditions of these particular eruptions. Rather, we use these extreme examples to help test whether heat pipes can provide a generally applicable mode to move water through diatremes. The water table is estimated to be at depths of ~340-380 m beneath Colton Crater and ~315-350 m beneath Rattlesnake Crater, placing it in the lower Coconino Sandstone or Upper Supai Group (Hoffman et al., 2006; Bills et al., 2000; ADWR). The nearest well to Rattlesnake Crater (~1.5 km to the SW) places the water table at ~315 m deep; the base-case groundwater depth of 345 m is therefore considered to be a lower limit for conditions during its eruption. The water table was probably close to these levels at the time of the eruptions in the Pleistocene (Moore and Wolfe, 1987); regional topography and elevation of
groundwater outflow into the Little Colorado River basin in the Pleistocene epoch are interpreted to have been similar to present day (Holm, 2001), which allows the inference that groundwater levels would have also been approximately the same. Permeability of the Coconino Sandstone and Upper Supai Group were estimated based on modeled hydraulic conductivity values for nearby wells (Hoffman et al., 2006). Initial parameters for gravity-capillary equilibrium runs are given in Table 1, and all estimated country-rock properties are given in Table 3.

Simulations were created using one of two primary model setups: rising heat injection or stationary heat injection (Fig. 2). Both models use the same calculated heating rate of $5.50 \times 10^5$ J/s for all heat injection. In the rising heat models, heat is injected row by row at timed intervals, moving upward from the bottom boundary of the model toward the surface, imitating the ascent of magma (Appendix A). The timing of heat injection was determined based on a magma ascent rate correlating with a volumetric injection rate of 0.5 m$^3$/s, considered to be an approximate minimum magma ascent rate for basaltic eruptions (Walker, 1973). Heat is injected up to 95 m depth; once magma and water reach this depth, they are shallow enough for MFCI to eject overlying material and the locus of explosion can then, theoretically, become the new surface. The stalled heat injection models are set up with a dome-shaped heat source, or magma injection that reaches from the base of the model to the water table. The region of heat injection for the standard 425-m-deep model is 360 m wide at the bottom boundary and tapers to 60 m at the water table (Fig. 2). The heat source does not move and the heating rate ($5.50 \times 10^5$ J/s) is continuous throughout the duration of each simulation. Note that the bottom of the simulation domain is held at the initial temperature of 20 ºC, but overall simulation times are short (on the order of days), so the high temperatures in the domain caused by heat injection are not altered appreciably by heat loss from the bottom. In other words, over the time of magma intrusion and
heat-pipe processes that we simulated, and with insulated boundary conditions along the top and sides and minimal effects arising from the bottom constant-temperature boundary condition, heat loss out the bottom is minor.

Several input parameter variations were applied to the models to test the dependency of model results on each parameter. These variations include: increased and decreased permeability of rock units, increased permeability and porosity of the fracture zone/conduit, anisotropic permeability of rock units, increased and decreased porosity, increased and decreased heat rate, raised and lowered water table depth, and doubled fracture zone width (Anderson, 2017).

Selected test simulations are described in Results.

These two setups are not necessarily separate processes; a stationary-heating scenario may occur prior to the first magma reaching the surface, or concurrent with magmatic eruption, with sill and dike intrusion in the shallow subsurface. Le Corvec et al. (2018) modeled intrusions into diatremes and show that the brecciation of the diatreme affects local stress states, inhibiting magma ascent and driving its lateral diversion, which would enhance heat transfer in a heat pipe, as in our slow-ascent simulations. While a narrow dike travels through a fracture or conduit to the surface, the larger rising or stationary magma body at depth can continue transferring heat to the surrounding country rock and groundwater. At any time in an eruption, dikes may branch from the main conduit through pre-existing or newly opened fractures (e.g. Re et al., 2015; Muirhead et al., 2016), where magma may then come into contact with transported groundwater and induce MFCI.

To demonstrate the heat pipe process in a growing diatreme, we have created a series of simplified simulations based on the formation of the Rattlesnake Crater diatreme to a depth of 710 m, using a growing region of high permeability to demarcate the diatreme shape (Fig. 3).
This is not representative of the entire diatreme beneath Rattlesnake Crater, as geophysical analysis indicates that it extends to at least 800 m and possibly as deep as ~3 km (Marshall et al., 2015). Case 3A begins at equilibrium, and heat ($5.50 \times 10^5$ J/s) is injected in a dome-shaped region from the base of the model to 345 m depth. The subsequent simulation (Case 3B) includes a zone of high permeability in the center of the model up to the new saturation limit, representing a region of brecciated country rock where first explosions might have occurred, and heat injection reaches 95 m depth. In the last step of the series (Case 3C), a large, high-permeability diatreme structure is added and the region of heat injection expands into the diatreme.
3. Results

3.1. Rising Heat Injection

3.1.1. Case 1

Case 1 models timed heat injection into a mesh with a fracture zone extending from the ground surface to 425 m depth within the saturated upper Supai Group. Heat is injected up to 95 m depth over 660 seconds (eleven minutes). The simulation ran for ~3.1 days (Fig. 4) until convergence problems occurred related to dry-out (see Section 2.2). The highest pressure zones (up to $2.2 \times 10^6$ Pa) form around either side of the fracture-zone pathway within the liquid-saturated base of the model, while the fracture-zone pathway itself has a significantly lower pressure. Maximum temperatures reach ~500°C within the middle to upper fracture zone, but do
not exceed ~220°C within the aquifer. The gas saturation plot shows how the water has moved as a result of the injected heat. Around the heat injection in the saturated base and up into the fracture zone, pore space contains 90-100% heated vapor by volume (i.e., grid block gas saturation equals 90-100%) with the remainder liquid water (10-0%). In the center of the model, the original water table is now raised, with grid blocks of 90-100% liquid saturation (10-0% water vapor) now reaching upward to a depth of ~300 m. Grid blocks containing up to ~60% liquid saturation are now present on either side of the fracture zone, nearly reaching the ground surface. Vectors show strong upward vapor flow through the fracture zone, while smaller magnitude vapor flows are seen on either side of the fracture pointing outward.

![Diagram](image)

**Figure 4:** Pressure, temperature, and gas saturation at t ~ 3.1 days for a simulation with rising heat injection up to 95 m depth. A fracture zone extends from the ground surface to 425 m depth. Gas flow vectors, scaled relative to magnitude, overlain on $S_z$ plot. Largest gas flow rate vector in fracture zones: $V_z = 0.29$ kg/s, $V_x = 6.00 \times 10^6$ kg/s. Dashed gray lines in the pressure diagram separate the geologic units, and the dashed white line shows the original water table.

3.1.2. **Case 1A**

In the large model of this scenario (Case 1A, supplementary files), heat is injected at the same rate, corresponding to 0.5 m$^3$/s of magma. A 600-m-wide zone in the bottom 45 m of the model is heated at a constant rate throughout the run, and step-wise heat injection begins at 665 m depth at 30 seconds. The injection zone tapers to a width of 60 m at the water table. Results of this simulation at 2.4 days show maximum pressure at the base of the aquifer, gradually
decreasing upward in the zone of heat injection. High temperatures and increased vapor saturation develop in the upper aquifer, outside the cooler fracture zone. Just above, several blocks of increased liquid saturation (>~70% aqueous phase, ~30% vapor) reach as high as 285 m depth. Zones of increased liquid saturation extend up to 40 m laterally away from the fracture zone within the unsaturated Coconino Sandstone, and near the Kaibab boundary, liquid saturation reaches ~50%.

3.1.3. **Case 1B**

Case 1B tests increased country-rock permeability relative to the base case. The Coconino Sandstone permeability is increased to $8.97 \times 10^{-11} \text{ m}^2$, and the same permeability and density are given to the upper Supai Group. Boundary blocks have also been given the same density as the Coconino Sandstone and aquifer of 2,450 kg/m$^3$, and a porosity of 15%. Results of this simulation at 2.1 days (when dry-out caused poor convergence) are shown in Fig. 5 alongside those for the base case (Case 1.1) at the same time in the experiment. The high-permeability model shows a wider area of impact around the heat injection, but total pressure and temperature are generally lower. Vapor and associated condensation reach outward 40 m laterally from the fracture zone up to nearly 100 m depth.
Figure 5: Pressure, temperature, and gas saturation at ~2.1 days for rising heat injection simulations with increased country rock permeability (Case 1B, top) and base-case conditions (Case 1.1, bottom). Color scale ranges spanning the max/min P and T are not uniform between models, as this results in significant loss of detail for some simulations. Gas flow vectors overlain on $S_g$ plot are scaled relative to magnitude. Largest gas flow rate vector in fracture zone: $V_z = 0.34$ kg/s, $V_x = -7.53 \times 10^{-6}$ kg/s (Case 1B). Dashed gray lines in the pressure diagram separate geologic units, and the dashed white line shows the original water table.

3.2. Stationary Heat Source

3.2.1. Case 2.1

Case 2.1 models stationary heat injection into a system with a fracture zone extending from the ground surface to 425 m depth (Fig. 6). The model runs for ~4.4 days and, as in the rising-heat-injection models, the highest pressure zones are focused around either side of the fracture zone within the aquifer. The center of the direct heat injection zone is primarily ~350-450°C, with one block within the fracture zone at the depth of the original water table reaching ~500°C. Gas saturations show a zone of heated vapor in the center of the injection, with liquid...
water, some of which is barely heated above equilibrium temperature, being driven upward. On either side of the fracture zone at a depth of 290 m, grid blocks previously at residual saturation reach a liquid saturation of ~65%, and condensed water is present as far as 40 m away from the fracture zone. Vectors show strong vapor flow toward the surface through the fracture zone. In just over 4 days, an additional ~270 m³ of liquid water is emplaced above a depth of 205 m in this two-dimensional scenario.
Figure 6: Pressure, temperature, and gas saturation at ~4.4 days for stationary heat injection simulations under base-case conditions (Case 2.1), with increased country-rock permeability (Case 2B), and with doubled fracture zone width (Case 2N). Color scale ranges for $P$ and $T$ are not uniform between models, as this results in significant loss of detail for some simulations. Gas flow vectors overlain on $S_g$ plots are scaled relative to magnitude. Largest gas flow rate vectors in fracture zone: $V_Z = 0.15$ kg/s, $V_X = 4.45 \times 10^{-6}$ kg/s (Case 2.1). Dashed gray lines in the pressure diagram separate geologic units, and the dashed white line shows the original water table.

3.2.2. Case 2A

The large model of stationary heat injection at standard conditions (Case 2A, supplementary file) is set up with constant heat injection in a dome-like shape. The base of the
injection is 600 m wide at 710 m depth, tapering upward to 200 m at 530 m depth. The model runs to ~8.1 days before TOUGH2 stops due to dry-out. Highest pressure is focused within the central and lower heated region, surrounded by a gradual pressure gradient up to the top of the saturated zone. The water table has shifted upward from 345 m depth; grid blocks with as much as 50% liquid water reach 275 m depth, decreasing to <30% liquid by 245 m. The heat injection region itself is entirely vapor at ~8.1 days, surrounded by a thin rim of two-phase liquid and vapor.

3.2.3. Case 2B

We tested the sensitivity of simulation results to the assigned permeability values for the geologic units. As in the rising heat injection models, permeability was increased for the Coconino Sandstone and saturated upper Supai Group to 8.97 × 10⁻¹¹ m² (Case 2B). Conditions at the end of the simulation at 4.4 days are shown in Fig. 6 compared to the base case (Case 2.1) at the same time. A large tear-drop-shaped zone of vapor and associated condensed water is present within the sandstone, affecting grid blocks as high as ~95 m below the surface. Just above the water table, the zone extends ~420-460 m wide. Most of the affected grid blocks contain less than ~75% vapor saturation, or greater than 25% liquid water saturation, and most of the model remains below 200°C.

3.2.4. Cases 2C & 2D

Lower permeabilities were tested in Cases 2C and 2D. Permeabilities of the Coconino Sandstone and upper Supai Group are lowest in Case 2C. The simulation runs to just under 4 days (Fig. 7). Heat and fluid flow are largely restricted to the fracture zone, but vapor does form...
within the aquifer, and a small area of rising saturation is seen around the fracture zone just above the water table. Water begins condensing around the fracture zone, but blocks do not exceed 50% liquid saturation above ~100 m depth. The highest pressures are more than an order of magnitude greater than under base-case conditions. In Case 2D, permeabilities for Coconino Sandstone and the upper Supai Group are an average of the base-case and 2C permeabilities. Results of this simulation at ~4 days vary little from the base case (supplementary figures).

Figure 7: Pressure, temperature, and gas saturation at ~3.9 days for stationary heat injection simulations with low (Case 2C) and base-case permeabilities. Gas flow vectors overlain on $S_g$ plots are scaled relative to magnitude. Largest gas flow rate vector in fracture zone: $V_z = 0.25$ kg/s, $V_y = 0$ kg/s (Case 2C). Dashed gray lines in the pressure diagram separate the geologic units, and the dashed white line shows the original water table.
3.2.5. **Case 2N**

Fracture-zone width is doubled to 40 m in Case 2N, and parameters for this model at ~4.4 days are shown in Fig. 6. Increased fracture zone size has little effect on general pressure and temperature conditions, but \( T_{\text{max}} \) is dropped to below 400°C. In ~4.4 days, a column of two-phase fluid 120 m wide (including the fracture zone) reaches the Kaibab-Coconino boundary at 75 m, and a narrowing column continues into the Kaibab limestone up to ~15 m depth. A total of 1,560 m³ of liquid water is brought up above 205 m depth (in the two-dimensional space). Allowing the simulation to continue to ~5.3 days shows a total of 1,780 m³ of liquid water brought to this depth, or an additional 220 m³ in less than a day.

### 3.3. Diatreme Formation

A simplified demonstration of the heat pipe process in a growing diatreme is modeled in Cases 3A-3C (Fig. 8). In Case 3A, heat is injected from the base of the model up to 345 m depth. After ~4.4 days, a zone of grid blocks containing >70% liquid saturated reaches ~235 m depth. A zone of high permeability is added in the new saturated region and heat is injected up to 95 m depth in Case 3B. After ~11 minutes, gas vectors show strong flow into and outward from this region. A large, high-permeability diatreme structure is opened in the last step (Case 3C), and heat injection expands into this region. After just over 20 minutes in the final simulation, vapor and liquid water have begun to spread out to the walls of the diatreme and to the surface. It is important to emphasize the change in time scale from days to minutes once the brecciation of the diatreme occurs.
Figure 8: Pressure, temperature, and gas saturation for the simplified progressive diatreme growth simulation. Case 3A (top) shows magma injection up to 345 m depth after ~4.4 days. Case 3B (middle) is a continuation of Case 3A, with an additional zone of high permeability (as shown in 8A) and heat injection up to 95 m depth, and Case 3C (bottom) is a continuation of Case 3B with a high-permeability diatreme structure (as shown in 8A) and an expanded zone of heat injection into the high-permeability area. Color scale ranges for $P$ and $T$ are not uniform between models, as this results in significant loss of detail for some simulations.

4. Discussion

All of the models show that liquid water, driven upward as heated vapor, can condense around the outside of a permeable fracture zone, magma conduit, or diatreme prior to and during
an eruption under a range of conditions. The rising-heat-injection scenarios show how water and vapor may move around a super-heated fracture zone or conduit during the earliest stages of an eruption, while stationary-heat-injection models demonstrate thermohydrologic processes that may occur near the water table with the presence of a hot magmatic body in an aquifer. Base-case models show a zone of condensation reaching 40-60 m outside the conduit after only ~3-4 days, and a halo of increased saturation reaching ~50 m above the equilibrium water table. As eruptive episodes often last days to weeks, or even years, injecting dikes and sills below the volcano, it is likely that these processes would continue at a similar rate to transport even greater quantities of water upward, where it can then condense and be temporarily held by capillary forces or within fractures and voids. When magma then rises quickly toward the surface and erupts, a potentially large volume of liquid water may be available at shallow enough depth to produce sustained, ejecta-producing explosions. Shallow intrusions, such as sills and dikes, are common under maars (e.g. Re et al., 2015; Muirhead et al., 2016). Our modeled setup, with a shallow, dome-shaped heat source, provides an indication of how these shallow dike/sill complexes may affect water movement.

Models show water redistribution can occur under a range of subsurface conditions, with efficiency largely dependent on permeability, fracturing, and time (Anderson, 2017). The lateral and vertical extent of the ascending vapor halo increases with permeability and porosity, while the amount of time it takes to be driven upward is inversely related to these parameters. The calculated Coconino Sandstone permeability is high compared to other published sandstone permeabilities (Bear, 1988), largely because of its significant fracturing in the study area. The tested low-end permeability values (Cases 1D and 2D) are most comparable to moderately fractured or non-fractured sandstone, while the tested higher-permeability values (Cases 1B and
are most similar to a very fine, unconsolidated sand (Bear, 1988), similar to the lower Bidahochi Formation, the country rock for the maars of the Hopi Buttes volcanic field (e.g., Lefebvre et al., 2013). In lower-permeability rocks, a fracture zone or otherwise high-permeability feature appears necessary to allow vapor and water to be driven toward the surface. Simulations doubling the width of the fracture zone/conduit from 20 to 40 m showed more than three times the amount of water brought above 205 m than in the base case, with vapor reaching as high as 15 m from the surface (Fig. 6). In natural conditions with three dimensions, we can expect similar increases in water transport as dike length increases. Regardless of initial country-rock permeability, the first explosions in a maar eruption will substantially change permeability and porosity conditions as surrounding country rock is brecciated and overall permeability increases; these processes should be modeled in future studies.

The heat rate (J/s) is dependent on estimated or averaged variables, and therefore includes significant uncertainty. It is reasonable for these simplified models, but considering that magma injection is only described by this rate, and heat rate should vary during eruption and between different rock types, this parameter is open to variation. Increasing and decreasing heat rate by nearly half an order of magnitude produces similar results to the base case, but at much different rates (Anderson, 2017). A lower heat rate may take ~2 weeks or more to produce a result similar to what is seen in ~3-4 days in the base case, and increasing it by the same magnitude produces similar or nearly identical results in ~40% less time (1.8 – 2.3 days). The models with a higher heat rate are probably most similar to actual direct heat from magma at very shallow depth immediately prior to eruption, while lower heat rates are probably most comparable to a magma body intruded well below the water table.
4.1. Colton & Rattlesnake Crater Eruptions

The eruption of Colton Crater was dominated by Strombolian activity, producing a large scoria cone (Cummings, 1972), until late in the eruption when magma interacted with liquid water and the resulting large explosions ejected much of the core of the existing scoria cone (Van Kooten and Buseck, 1978), redepositing it on the outer flanks of the cone as a ~20-30-m-thick massive bed of scoria and broken lava clasts. After a few small surge-producing events, the eruption then quickly dried out again, producing a small scoria/spatter cone inside the crater before the eruption ceased.

The conditions that caused or allowed water to come into contact with the magma remain uncertain, but the limited phreatomagmatic tephra sequence at Colton Crater suggests this period of activity did not last long. Evidence of northward vent migration is preserved in the scoria-cone deposits (Leudemann et al., 2013), so perhaps the vent intersected a water-filled fracture in the Kaibab or Coconino Formations. The phreatomagmatism was also near the end of the eruption, so it is possible that magma flux had begun to wane and allowed water in the country rock to flow toward the vent rather than driving it away as vapor. In either case, the modeled thermohydrologic processes provide one possible mechanism for supplying shallow liquid water for the Colton Crater eruption (Fig. 9). Abundant fractures present throughout the Coconino and Kaibab Formations could have allowed for transport of even greater quantities of water than observed in the idealized models, especially over the course of weeks or months that Colton Crater erupted prior to magma-water interaction. Other factors that contributed to changes in behavior are beyond the scope of this research.
The Rattlesnake Crater eruption appears to have started with a brief period of Strombolian activity, but little of the initial scoria cone remains, buried beneath phreatomagmatic tuff (Schwoerer, 2014). Most of the eruption consisted of repeated phreatomagmatic explosions over a period possibly lasting weeks to months, followed by another stage that built a small scoria cone on the southeastern crater rim. The crater and scoria cone vents trend northwest, consistent with regional faulting. With an initially dry eruption, Rattlesnake Crater’s behavior was probably most similar to the rising heat injection model, with magma rising quickly to the surface and driving away water as steam, rather than interacting with it. The presence of magma below the water table during and potentially before the onset of eruption would have vaporized aquifer water, which moved toward the surface to condense at shallow depths around the conduit, similar to the stationary heat model. When the eruption transitioned to phreatomagmatic activity after a short time, a significant quantity of water would have been available in the shallow subsurface for sustained, efficient MFCI (Fig. 9).

As first explosions occurred in these eruptions, country rock would have been brecciated and mixed with juvenile material and condensed water, creating a rapidly evolving setting for
these vapor transport processes. Feeder dikes probably deviated many times within the permeable diatreme fill, resulting in continued heating, water redistribution, and explosions from many locations within the diatreme, as demonstrated in Case 3 (Fig. 8). The important feature of this model is that, once a diatreme starts to form, it appears to provide a very efficient pathway for heat pipes to transport water vapor and liquid. Thus, once a maar-diatreme forms, it may help provide its own water to itself for MFCI activity.

4.2. Continuous Water Supply

The observed results of these modeled scenarios may help to explain different behaviors that have been recorded in eruptions around the world. As described, the process of vaporization and related upward transport and condensation could provide shallow water to phreatomagmatic eruptions in locations similar to the SFVF, where the water table is deep and well below the estimated ideal depth for tephra-producing explosions.

A possibly more significant implication of this work is that these processes are probably also important in locations where the water table is not deep; in these situations, they help perpetuate eruptions that would otherwise “dry out” quickly. The cone of depression scenario of Lorenz (1986) may occur in locations where very low country-rock permeability prevents groundwater recharge to the diatreme on the time scale of the eruption. However, the TOUGH2 models show that movement of vapor and liquid water within and around the permeable, dike-rich diatreme (Le Corvec et al., 2018), driven by the heat itself, could provide water to potential explosion loci throughout the diatreme (Fig. 10). With dikes forming a complex network within a diatreme breccia with broadly distributed water, the consequent explosions can happen anywhere within a diatreme, both deep and shallow, where magma is intruded. Some dikes will be
emplaced non-explosively, as described by Lefebvre et al. (2013), but others will cause
explosions through rapid ascent and interaction with this intra-diatreme water.

Upward movement of water within the diatreme has often been attributed to debris jets
and recycling of material with explosions, processes that certainly occur and provide some
shallow water for explosions. The processes modeled here are capable of liquid and vapor
transport during and prior to eruption at a larger scale than would be expected by these
processes, especially in situations where magma may reside at a shallow depth for days to weeks.

The models may also explain phenomena like what occurred in 1759 in the first few
weeks of the El Jorullo eruption in central Mexico, where hot mud poured out of springs and
hillsides as phreatic and phreatomagmatic explosions occurred at the vent (Gadow, 1930).
Similar expulsions of hot water occurred at Mont Pelée (Martinique) in 1902, and meter-scale
increases in water levels in wells occurred at Mayon (Philippines) in 1993 and Usu (Japan) in
fluid migration into a shallow aquifer due to magma intrusion at Cotopaxi in 2015. In models
with highly permeable subsurface material, the wide halo of vapor and water reaches shallow depths in just a few days even with a deep water table. If groundwater depth is ~100-200 m deep, this time could be reduced to less than a day—especially if water and vapor follow fractures and springs. The occurrence of this type of phenomena could also provide clues about the size of the shallow magma source in an eruption.

5. Conclusions

Pre-eruptive and early eruption simulations created using TOUGH2/EOS3 provide possible explanations for the occurrence of sustained phreatomagmatic activity in areas with unusually deep groundwater, as well as a possible mechanism for providing a continuous, shallow liquid water supply to an eruption. Simulations show that magmatic heat prior to and during an eruption can drive a significant quantity of water toward the ground surface as heated vapor, which then condenses to liquid water upon reaching cooler temperatures at shallower depths. Once explosions brecciate and mix diatreme fill, increased permeability allows these processes to increase in rate and efficiency. With liquid water placed in the shallow subsurface or throughout a diatreme, rapidly ascending magma at the onset of eruption or interaction with branching intra-diatreme dikes can initiate explosive MFCI to drive and sustain a phreatomagmatic eruption. Rapid, large-scale vapor transport and condensation can also explain the voluminous outpouring of hot, muddy water that occurs with eruptions at some volcanoes. Future investigation of these processes could be bolstered by experiments, geophysical analysis of subsurface fracturing and structure, and/or detailed larger-scale modeling including geomechanical processes and potentially eruption processes.
ACKNOWLEDGMENTS

This research was completed with funding from Pioneer Natural Resources, the Tom and Rose Bedwell Trust, and the NAU Friday Lunch Clubbe. Additional support was provided by Lawrence Berkeley National Laboratory under Department of Energy Contract No. DE-AC02-05CH11231 and by National Science Foundation grant EAR1322081. We are grateful to Walnut Canyon National Monument for permitting us to conduct research in the canyon, and to Paul Whitefield for guiding us. We would also like to thank Stefan Finsterle, Yingqi Zhang, and Christine Doughty for their invaluable instruction in using TOUGH2 and iTOUGH2, and Ryan Porter for his assistance with producing figures for our models. Critiques by Greg Valentine and an anonymous reviewer greatly improved the manuscript.

Data Availability: Datasets related to this article can be found at http://dx.doi.org/10.17632/fhvsfjx7j6.1, an open-source online data repository hosted at Mendeley Data
REFERENCES


1171.

pipes in fractured porous rock.

LBNL-43134 (revised). Lawrence Berkeley National Laboratory, Berkeley, CA.

emplacement of the Jagged Rocks Complex, Hopi Buttes Volcanic Field, Navajo Nation,
USA. Journal of Volcanology and Geothermal Research 295, 65-79, DOI:
10.1016/j.jvolgeores.2015.01.009.

34. Ross, P.-S., White, J.D.L., 2006. Debris jets in continental phreatomagmatic volcanoes:
A field study of their subterranean deposits in the Coombs Hills vent complex,

Geophysical Research: Solid Earth 84 (B4), 1621-1628.


Appendix A

Model Software

The TOUGH (“Transport Of Unsaturated Groundwater and Heat”) suite of software codes are multi-dimensional numerical models for simulating the coupled transport of water, vapor, non-condensible gas, and heat in porous and fractured media. Developed at the Lawrence Berkeley National Laboratory (LBNL) in the early 1980s primarily for geothermal reservoir engineering, the suite of simulators is now widely used at universities, government organizations, and private industry for applications to nuclear waste disposal, environmental remediation problems, energy production from geothermal, oil and gas reservoirs as well as gas hydrate deposits, geological carbon sequestration, vadose zone hydrology, and other uses that involve coupled thermal, hydrological, geochemical, and mechanical processes in permeable media. The TOUGH suite of simulators is continually updated, with new equation-of-state (EOS) modules being developed, and refined process descriptions implemented into the TOUGH framework (see the overview of the TOUGH development history). Notably, EOS property modules for mixtures of water, NaCl, and CO₂ has been developed and is widely used for the analysis of geologic carbon sequestration processes. TOUGH and its application have been the subject of more than 500 peer-reviewed journal articles, conference proceedings, and project reports. TOUGH and its various modules are documented in a series of manuals. An example software validation report of TOUGH2 is provided in Pruess et al.

https://escholarship.org/content/qt0gq2w0r5/qt0gq2w0r5.pdf
Appendix A


More information about the TOUGH codes can be found here:

https://tough.lbl.gov/

For the simulations of water vapor transport and condensation related to maar volcanoes reported on in this paper, we used TOUGH2/EOS3, the equation of state module for water and air. In this module, water properties are calculated using the steam table equations from the International Formulation Committee, and air is approximated as an ideal gas (Pruess et al., 2011). The primary variables for EOS3 in two-phase conditions are pressure (P), temperature (T), and gas saturation (Sg). The number of mass and energy balance equations to be solved for each grid block of the computational mesh corresponds to the number of primary thermodynamic variables. With execution of the code, sets of coupled nonlinear equations for all grid blocks are solved simultaneously using Newton-Raphson iteration (Pruess et al., 2011).
Heat Flow Calculation

\[ q = -K(\Delta T/\Delta z) \]
\[ q = \text{heat rate (J/s)} \]
\[ K = \text{thermal conductivity} \quad 2.1 \text{ W/m K} \]
\[ \Delta T = T_{\text{rock}} - T_{\text{magma}} \quad 1000^\circ \text{C} \]
\[ \Delta z = z_{\text{rock}} - z_{\text{magma}} = S_{\text{TBL}} \]

\[ S_{\text{TBL}} = \sqrt{\kappa \tau} \]
\[ \kappa = K/(\rho C_p) \]
\[ \kappa = \text{thermal diffusivity (m}^2/\text{s)} \]
\[ \rho = \text{density of sandstone} \quad 2500 \text{ kg/m}^3 \]
\[ C_p = \text{heat capacity of wet sandstone} \quad 920 \text{ J/kg K} \]
\[ \tau = \text{time scale} \quad 3600-14400 \text{ s (1-4 hrs)**} \]

1. \[ \kappa = K/(\rho C_p) \]
   \[ = 2.1/(2500 \times 920) \]
   \[ = 9.13 \times 10^{-7} \text{ m}^2/\text{s} \]

2. \[ S_{\text{TBL}} = \sqrt{\kappa \tau} \]
   \[ = \sqrt{(9.13 \times 10^{-7})(3600)} \quad (2a) \]
   \[ = 5.70 \times 10^{-2} \text{ m} \]
   \[ = \sqrt{(9.13 \times 10^{-7})(14400)} \quad (2b) \]
   \[ = 1.15 \times 10^{-1} \text{ m} \]

3. \[ q = -K(\Delta T/\Delta z) \]
   \[ = -2.1(-1000/(5.70 \times 10^{-2})) \quad (3a) \]
   \[ = 3.66 \times 10^4 \text{ J/s m}^2 \]
   \[ = -2.1(-1000/(1.15 \times 10^{-1})) \quad (3b) \]
   \[ = 1.83 \times 10^4 \text{ J/s m}^2 \]

4. Across whole 20 m\(^2\) of interface (i): \[ q \times i = (3.66 \times 10^4) \times 20 \quad (4a) \]
   \[ = 7.33 \times 10^5 \text{ J/s} \]
   \[ = (1.83 \times 10^4) \times 20 \quad (4b) \]
   \[ = 3.66 \times 10^5 \text{ J/s} \]

Average heat rate = **5.50 \times 10^5 \text{ J/s}**

** Parameter was tested over a range of values; “final” or base-case heat rate is an average of these values.
Appendix A

Table A1: Schedules of heat injection with depth over time for the small models (left) and large models (right). After each injection start time, heat rate is continuous \((5.50 \times 10^5 \text{ J/s})\) for the remainder of the simulation.

<table>
<thead>
<tr>
<th>Injection depth (grid block top, m)</th>
<th>Injection width (m)</th>
<th>Vertical distance of magma travel (m)</th>
<th>Injection start time (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>95</td>
<td>20</td>
<td>10</td>
<td>660</td>
</tr>
<tr>
<td>105</td>
<td>20</td>
<td>10</td>
<td>640</td>
</tr>
<tr>
<td>115</td>
<td>20</td>
<td>10</td>
<td>620</td>
</tr>
<tr>
<td>125</td>
<td>20</td>
<td>10</td>
<td>600</td>
</tr>
<tr>
<td>135</td>
<td>20</td>
<td>10</td>
<td>580</td>
</tr>
<tr>
<td>145</td>
<td>20</td>
<td>10</td>
<td>560</td>
</tr>
<tr>
<td>155</td>
<td>20</td>
<td>10</td>
<td>540</td>
</tr>
<tr>
<td>165</td>
<td>20</td>
<td>10</td>
<td>520</td>
</tr>
<tr>
<td>175</td>
<td>20</td>
<td>10</td>
<td>500</td>
</tr>
<tr>
<td>185</td>
<td>20</td>
<td>10</td>
<td>480</td>
</tr>
<tr>
<td>195</td>
<td>20</td>
<td>10</td>
<td>460</td>
</tr>
<tr>
<td>205</td>
<td>20</td>
<td>10</td>
<td>440</td>
</tr>
<tr>
<td>215</td>
<td>20</td>
<td>10</td>
<td>420</td>
</tr>
<tr>
<td>225</td>
<td>20</td>
<td>10</td>
<td>400</td>
</tr>
<tr>
<td>235</td>
<td>20</td>
<td>10</td>
<td>380</td>
</tr>
<tr>
<td>245</td>
<td>20</td>
<td>10</td>
<td>360</td>
</tr>
<tr>
<td>255</td>
<td>20</td>
<td>10</td>
<td>340</td>
</tr>
<tr>
<td>265</td>
<td>20</td>
<td>10</td>
<td>320</td>
</tr>
<tr>
<td>275</td>
<td>20</td>
<td>10</td>
<td>300</td>
</tr>
<tr>
<td>285</td>
<td>20</td>
<td>10</td>
<td>280</td>
</tr>
<tr>
<td>295</td>
<td>20</td>
<td>10</td>
<td>260</td>
</tr>
<tr>
<td>305</td>
<td>20</td>
<td>10</td>
<td>240</td>
</tr>
<tr>
<td>315</td>
<td>20</td>
<td>10</td>
<td>220</td>
</tr>
<tr>
<td>325</td>
<td>20</td>
<td>10</td>
<td>200</td>
</tr>
<tr>
<td>335</td>
<td>20</td>
<td>10</td>
<td>180</td>
</tr>
<tr>
<td>345</td>
<td>60</td>
<td>10</td>
<td>160</td>
</tr>
<tr>
<td>355</td>
<td>100</td>
<td>10</td>
<td>140</td>
</tr>
<tr>
<td>365</td>
<td>140</td>
<td>10</td>
<td>120</td>
</tr>
<tr>
<td>375</td>
<td>180</td>
<td>10</td>
<td>100</td>
</tr>
<tr>
<td>385</td>
<td>220</td>
<td>10</td>
<td>80</td>
</tr>
<tr>
<td>395</td>
<td>260</td>
<td>10</td>
<td>60</td>
</tr>
<tr>
<td>405</td>
<td>300</td>
<td>10</td>
<td>40</td>
</tr>
<tr>
<td>415</td>
<td>380</td>
<td>10</td>
<td>0</td>
</tr>
<tr>
<td>425</td>
<td>380</td>
<td>5</td>
<td>0</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Injection depth (grid block top, m)</th>
<th>Injection width (m)</th>
<th>Vertical distance of magma travel (m)</th>
<th>Injection start time (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>95</td>
<td>20</td>
<td>10</td>
<td>1140</td>
</tr>
<tr>
<td>105</td>
<td>20</td>
<td>10</td>
<td>1120</td>
</tr>
<tr>
<td>115</td>
<td>20</td>
<td>10</td>
<td>1100</td>
</tr>
<tr>
<td>125</td>
<td>20</td>
<td>10</td>
<td>1080</td>
</tr>
<tr>
<td>135</td>
<td>20</td>
<td>10</td>
<td>1060</td>
</tr>
<tr>
<td>145</td>
<td>20</td>
<td>10</td>
<td>1040</td>
</tr>
<tr>
<td>155</td>
<td>20</td>
<td>10</td>
<td>1020</td>
</tr>
<tr>
<td>165</td>
<td>20</td>
<td>10</td>
<td>1000</td>
</tr>
<tr>
<td>175</td>
<td>20</td>
<td>10</td>
<td>980</td>
</tr>
<tr>
<td>185</td>
<td>20</td>
<td>10</td>
<td>960</td>
</tr>
<tr>
<td>195</td>
<td>20</td>
<td>10</td>
<td>940</td>
</tr>
<tr>
<td>205</td>
<td>20</td>
<td>10</td>
<td>920</td>
</tr>
<tr>
<td>215</td>
<td>20</td>
<td>10</td>
<td>900</td>
</tr>
<tr>
<td>225</td>
<td>20</td>
<td>10</td>
<td>880</td>
</tr>
<tr>
<td>235</td>
<td>20</td>
<td>10</td>
<td>860</td>
</tr>
<tr>
<td>245</td>
<td>20</td>
<td>10</td>
<td>840</td>
</tr>
<tr>
<td>255</td>
<td>20</td>
<td>10</td>
<td>820</td>
</tr>
<tr>
<td>265</td>
<td>20</td>
<td>10</td>
<td>800</td>
</tr>
<tr>
<td>275</td>
<td>20</td>
<td>10</td>
<td>780</td>
</tr>
<tr>
<td>285</td>
<td>20</td>
<td>10</td>
<td>760</td>
</tr>
<tr>
<td>295</td>
<td>20</td>
<td>10</td>
<td>740</td>
</tr>
<tr>
<td>305</td>
<td>20</td>
<td>10</td>
<td>720</td>
</tr>
<tr>
<td>315</td>
<td>20</td>
<td>10</td>
<td>700</td>
</tr>
<tr>
<td>325</td>
<td>20</td>
<td>10</td>
<td>680</td>
</tr>
<tr>
<td>335</td>
<td>20</td>
<td>10</td>
<td>660</td>
</tr>
<tr>
<td>345</td>
<td>60</td>
<td>10</td>
<td>640</td>
</tr>
<tr>
<td>355</td>
<td>100</td>
<td>10</td>
<td>620</td>
</tr>
<tr>
<td>365</td>
<td>140</td>
<td>10</td>
<td>600</td>
</tr>
<tr>
<td>375</td>
<td>180</td>
<td>10</td>
<td>580</td>
</tr>
<tr>
<td>385</td>
<td>220</td>
<td>10</td>
<td>560</td>
</tr>
<tr>
<td>395</td>
<td>260</td>
<td>10</td>
<td>540</td>
</tr>
<tr>
<td>405</td>
<td>300</td>
<td>10</td>
<td>520</td>
</tr>
<tr>
<td>415</td>
<td>380</td>
<td>10</td>
<td>500</td>
</tr>
<tr>
<td>425</td>
<td>380</td>
<td>5</td>
<td>480</td>
</tr>
<tr>
<td>440</td>
<td>380</td>
<td>15</td>
<td>450</td>
</tr>
<tr>
<td>455</td>
<td>420</td>
<td>15</td>
<td>420</td>
</tr>
<tr>
<td>470</td>
<td>420</td>
<td>15</td>
<td>390</td>
</tr>
<tr>
<td>485</td>
<td>420</td>
<td>15</td>
<td>360</td>
</tr>
<tr>
<td>500</td>
<td>460</td>
<td>15</td>
<td>330</td>
</tr>
<tr>
<td>515</td>
<td>460</td>
<td>15</td>
<td>300</td>
</tr>
<tr>
<td>530</td>
<td>460</td>
<td>15</td>
<td>270</td>
</tr>
<tr>
<td>545</td>
<td>500</td>
<td>15</td>
<td>240</td>
</tr>
<tr>
<td>560</td>
<td>500</td>
<td>15</td>
<td>210</td>
</tr>
<tr>
<td>575</td>
<td>540</td>
<td>15</td>
<td>180</td>
</tr>
<tr>
<td>590</td>
<td>540</td>
<td>15</td>
<td>150</td>
</tr>
<tr>
<td>605</td>
<td>580</td>
<td>15</td>
<td>120</td>
</tr>
<tr>
<td>620</td>
<td>580</td>
<td>15</td>
<td>90</td>
</tr>
<tr>
<td>635</td>
<td>580</td>
<td>15</td>
<td>60</td>
</tr>
<tr>
<td>650</td>
<td>620</td>
<td>15</td>
<td>30</td>
</tr>
<tr>
<td>665</td>
<td>620</td>
<td>15</td>
<td>0</td>
</tr>
<tr>
<td>680</td>
<td>620</td>
<td>15</td>
<td>0</td>
</tr>
<tr>
<td>695</td>
<td>620</td>
<td>15</td>
<td>0</td>
</tr>
<tr>
<td>710</td>
<td>620</td>
<td>7.5</td>
<td>0</td>
</tr>
</tbody>
</table>