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Measurement of the branching fraction for inclusive semileptonic $B$ meson decays


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031101-2
Measurements of semileptonic $B$ meson decays are a good way to determine the Cabibbo-Kobayashi-Maskawa (CKM) matrix elements $|V_{cb}|$ and $|V_{ub}|$, two of the parameters of the standard model. For $|V_{cb}|$, analyses of exclusive and inclusive decay have resulted in comparable precision. While most measured values of $B(B \to Xe\nu)$ are below 11% [1], theoretical calculations including perturbative QCD contributions predict values of 12% or above [2].

The measurement presented here employs the method introduced by ARGUS [3] and later used by CLEO [4], in which $B\bar{B}$ events are tagged by the presence of a high momentum lepton. As a tag, we choose electrons with momentum $p^*$ in the interval 1.4 to 2.3 GeV/$c$, where $p^*$ is measured in the center-of-mass frame. A second electron in the event is taken as the signal lepton for which we require $p^* >$0.6 GeV/$c$, to avoid large backgrounds at lower momenta. Signal electrons are mostly from primary $B$ decays if they are accompanied by a tag electron of opposite charge (unlike sign). Those with a tag of the same charge (like sign) originate predominantly from secondary decays of charm particles produced in the decay of the other $B$ meson. Inversion of this charge correlation due to $B^0\bar{B}^0$ mixing is treated explicitly, and unlike-sign pairs with both electrons originating from the same $B$ meson are isolated kinematically. With a small model dependence on the estimated fraction of primary electrons below $p^* = 0.6$ GeV/$c$, we infer the semileptonic $B$ branching fraction from the background corrected ratio of unlike-sign electron pairs to tag electrons.

This measurement is based on data recorded in the year 2000 with the BABAR detector [5] at the PEP-II energy asymmetric $e^+e^-$ storage ring [6] at SLAC. The detector consists of a five-layer silicon vertex tracker, a 40-layer drift chamber (DCH), a detector of internally reflected Cherenkov...
light (DIRC), and an electromagnetic calorimeter (EMC) all embedded in a solenoidal magnetic field of 1.5 T and surrounded by an instrumented flux return. To ensure the high quality of the data, we have selected the largest contiguous block of events with identical and stable detector conditions in the year 2000, corresponding to an integrated luminosity of 4.13 fb\(^{-1}\) collected at the \(Y(4S)\) resonance, and 0.965 fb\(^{-1}\) recorded about 40 MeV below the \(Y(4S)\) peak (off resonance).

Multihadron events are selected by requiring a charged track multiplicity of \(N_{ch}>4\), or \(N_{ch}=4\) plus at least 2 neutral energy deposits above 80 MeV in the EMC. Track pairs from converted photons are not included in \(N_{ch}\), but count as one neutral particle. For further suppression of non-\(B\bar{B}\) events, we require \(R_{z}<0.6\), where \(R_{z}\) is the ratio of Fox-Wolfram moments \(H_{2}/H_{0}\) [7].

The electron momentum measurement and identification are critical for this analysis. For electron candidates we require hits in at least 12 DCH layers, and a polar angle \(\theta\) within the EMC acceptance, i.e. \(-0.72<\cos \theta<0.92\). To reduce the contamination from photon conversions and beam-gas background we require the track impact parameters in the plane perpendicular to the beams and along the detector axis to be less than 0.25 cm and 3.0 cm, respectively.

The track finding efficiency \(e_{trk}\) is determined from data as a function of charged multiplicity, transverse momentum, and polar and azimuthal angles. For signal electrons with \(p^{*}>0.6\) GeV/c, the average efficiency is \((97.1 \pm 1.1)\%\).

Electron identification is based on the ratio of the energy in the EMC and the track momentum, \(E_{EMC}/p\), the shower shape in the EMC, the specific energy loss \(dE/dx\) in the DCH, and the number of Cherenkov photons and the Cherenkov angle measured in the DIRC. Muons are eliminated on the basis of \(dE/dx\) and \(E_{EMC}/p\). Taking into account the correlations between deposited energy and shape in hadronic showers, we combine probability density functions derived from data samples for each discriminating variable to construct the likelihood function \(L(\xi), \xi \in \{e, \pi, K, p\}\). A track is identified as an electron if

\[
\frac{L(e)}{L(e)+5L(\pi)+L(K)+0.1L(p)}>0.95.
\]

The weights roughly reflect the relative abundances, their exact values not being crucial for electron identification.

We measure the electron identification efficiency as a function of \(p^{*}\) and center-of-mass polar angle \(\theta^{*}\) using radiative Bhabha events. For momenta \(p^{*}>0.6\) GeV/c, the average efficiency is \(92\%\) (see Fig. 1a). However, Monte Carlo simulations indicate that relative to radiative Bhabha events, the identification efficiency in \(B\bar{B}\) events is reduced between \((4 \pm 2)\%\) at low momenta \((p^{*}<1\) GeV/c) and \((2 \pm 1)\%\) above \(p^{*}=1.6\) GeV/c. We correct the measured efficiency for this momentum-dependent difference.

The misidentification rates for pions, kaons, and protons is taken from a \(B\bar{B}\) Monte Carlo simulation. The DCH and DIRC contribute significantly at low momenta, while the performance of the EMC increases with \(p^{*}\). This leads to a minimum of 0.05% for \(\eta_{p}\) at \(p^{*}<1.3\) GeV/c. The relative systematic error is estimated to be \(15\%\) from the purities of the control samples and the uncertainties in the relative abundances.

The branching fraction analysis makes use of three samples: (1) the tag electrons, (2) unlike-sign and (3) like-sign pairs of a tag and a signal electron candidate. Misidentified hadrons and electrons from non-\(B\bar{B}\) (continuum) events, photon conversions, \(\pi^{0}\to\gamma e^{+} e^{-}\) (“Dalitz”) and \(J/\psi, \phi(2S)\to e^{+} e^{-}\) decays contribute to the background in all three samples. The unlike-sign sample also contains pairs of primary and secondary electrons from the same \(B\) meson decay. Further contaminations to the like- and unlike-sign samples arise from decays of \(\tau\) leptons and charm mesons produced in \(b\to c\bar{c}s\) decays. Apart from the correction for unlike-sign electron pairs from the same \(B\), which is performed in bins of \(p^{*}\) only, all background corrections are performed in bins of \(p^{*}\) and polar angle \(\theta^{*}\).

The continuum background is subtracted from all three samples by scaling the off-resonance yields by the ratio of on-and off-resonance integrated luminosities, corrected for the energy dependence of the continuum cross sections, \(4.25\pm 0.02\). The relative systematic error in this ratio is estimated from the variation of the efficiency of di-muon events used to measure the relative luminosity. The continuum momenta are scaled by \(\sqrt{s_{t}}\), to compensate for the 0.4% lower center-of-mass energy. After the continuum subtraction, the yields for \(p^{*}>2.6\) GeV/c are compatible with zero for all samples.

Electrons from photon conversions and Dalitz decays are identified by pairing them with any oppositely charged track with transverse momentum \(p_{t}>0.1\) GeV/c. We distinguish the two sources of pairs by the distance \(R_{\text{pair}}\) of the pair vertex from the detector axis. Photon conversions are identified by requiring \(R_{\text{pair}}>1.6\) cm, a pair invariant mass \(M_{ee}\)
<10 MeV/c^2, and the transverse and longitudinal distances between the two tracks at the point of closest approach \( \Delta s < 0.3 \) cm and \( \Delta t < 1 \) cm. For Dalitz pairs, we require \( R_{\text{pair}} < 1.6 \) cm, \( M_{e^-} < 20 \) MeV/c^2, \( \Delta s < 0.2 \) cm and \( \Delta t < 1 \) cm. The momentum- and polar-angle-dependent pair finding efficiency, which is obtained from a full detector simulation, is low since, in most cases, the momentum of the second track is too small to produce a track in the DCH. It varies between 30% and 40% for photon conversions and between 20% and 30% for Dalitz pairs. From a detailed comparison between data and simulation, including the energy spectra of the pairs, the relative systematic uncertainties are estimated to be 13% and 19% for the conversion and Dalitz background rates, respectively.

In the unlike-sign sample, electrons from primary and charm decays of the same \( B \) tend to be produced in opposite directions. Defining \( \hat{p}_e \) as the center of the signal electron momentum bin, this background is reduced by a factor of 24 by imposing the condition

\[
\cos \alpha > 1 - \frac{\hat{p}_e^2}{(\text{GeV}/c)} \quad \text{and} \quad \cos \alpha > -0.2 \tag{1}
\]
on the opening angle \( \alpha \) of \( e^+e^- \) pairs, measured in the \( Y(4S) \) frame. Since \( B \) mesons are nearly at rest in this frame, there is no angular correlation between two electrons from different \( B \) mesons, and the loss in signal efficiency can be calculated on the basis of geometrical acceptance.

This selection also rejects \( e^+e^- \) pairs from \( J/\psi \) and \( \psi(2S) \) decays in the unlike-sign sample. The background from \( J/\psi \) and \( \psi(2S) \) decays with only one contributing \( e \) is estimated by Monte Carlo simulation, using \( B(B \to J/\psi \to e^-e^-) = (6.82 \pm 0.38) \times 10^{-4} \), \( B(B \to J/\psi(2S) \to e^-e^-) = (3.1 \pm 0.6) \times 10^{-5} \) [1] and the observed inclusive \( J/\psi \) and \( \psi(2S) \) momentum spectra.

For each tag candidate, we ensure that the invariant mass \( M_{e^-} \) formed with any oppositely charged electron satisfying \( \cos \alpha < -0.2 \) is incompatible with the \( J/\psi \) hypothesis, 2.9 \( < M_{e^-} < 3.15 \) GeV/c^2. This veto also rejects true tags; the loss rate is corrected using the background below the \( J/\psi \) peak in the observed \( M_{e^-} \) distribution.

The contribution of unlike-sign pairs from the same \( B \) decay satisfying Eq. (1) is approximately 2%. After subtraction of background contributions from continuum, photon conversions and Dalitz decays, the observed opening angle distribution (without the requirement) contains a flat contribution from electron pairs from different \( B \) mesons and a contribution from electron pairs from the same \( B \), which peaks at \( \cos \alpha = -1 \). The shape of the non-flat background is taken from Monte Carlo simulation and the relative normalization of the two contributions is determined by a fit to the data, which is performed separately for each 100 MeV/c-wide momentum bin below 1.2 GeV/c. The integral over the fitted non-flat contribution between the minimal allowed value of \( \cos \alpha \) and 1 is taken as the residual background. As can be seen in Fig. 2, the shape of the \( \cos \alpha \) distribution is well described by the Monte Carlo simulation. The very small background above 1.2 GeV/c (0.8% of the total contribution) is determined from Monte Carlo simulation with a relative uncertainty of 50%.

The study of systematic uncertainties in the predicted opening angle distributions is based on a parameterization of heavy quark effective theory (HQET) derived form factors [8] to model the decay \( B \to J/\psi e^- e^- \), the Isgur-Grinstein-Wise model 2 (ISGW2) [9] for \( B \) decays to \( D^* e^- e^- \) and charmless mesons, and the work of Goity and Roberts [10] for non-resonant \( B \to D^{(*)} e^- e^- \) decays. Varying the branching fractions by one standard deviation around current average values [1] and repeating the fitting procedure from above leads to a relative systematic error of 5% for this background estimate.

Figure 3 shows the observed momentum spectra and the individual background contributions discussed so far, corrected for tracking efficiency; a summary of yields is given in Table I. Following this initial set of background correc-

FIG. 2. Distribution of the cosine of the opening angle of unlike-sign pairs for \( 0.7 < p^* < 0.8 \) GeV/c. The points represent the data and the histogram is the result of a fit. The shaded area represents the estimated contribution of background electrons, and the vertical dashed line indicates the requirement on the opening angle.

FIG. 3. Total measured spectrum (points) and estimated backgrounds (histograms) for signal electron candidates in (a) the \( e^+e^- \) sample, and (b) the \( e^+e^+ \) sample.
TABLE I. Electron yield for the three samples and corrections with statistical and systematic errors.

<table>
<thead>
<tr>
<th>Sample</th>
<th>(1) Tag sample</th>
<th>(2) $e^+e^-$ sample, cut on $\alpha$</th>
<th>(3) $e^0e^-$ sample, all $\alpha$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$1.4&lt;p^*&lt;2.3$ GeV/c</td>
<td>$0.6&lt;p^*&lt;2.5$ GeV/c</td>
<td>$0.6&lt;p^*&lt;2.5$ GeV/c</td>
</tr>
<tr>
<td>On Y(4S)</td>
<td>395791 ± 630</td>
<td>14692 ± 120</td>
<td>10838 ± 110</td>
</tr>
<tr>
<td>Continuum</td>
<td>82073 ± 590 ± 410</td>
<td>1301 ± 76 ± 7</td>
<td>939 ± 64 ± 5</td>
</tr>
<tr>
<td>$\gamma\rightarrow e^+e^-$</td>
<td>561 ± 23 ± 140</td>
<td>283 ± 40 ± 37</td>
<td>856 ± 82 ± 110</td>
</tr>
<tr>
<td>$\eta, \eta^0 \rightarrow \gamma e^+e^-$</td>
<td>92 ± 9 ± 23</td>
<td>51 ± 22 ± 10</td>
<td>80 ± 82 ± 15</td>
</tr>
<tr>
<td>Faked $e$</td>
<td>1445 ± 140 ± 360</td>
<td>136 ± 16 ± 20</td>
<td>348 ± 48 ± 52</td>
</tr>
<tr>
<td>$e$ from same $B$</td>
<td></td>
<td>317 ± 7 ± 16</td>
<td></td>
</tr>
<tr>
<td>Yield before and</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>after correction</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>for electron</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>efficiency</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$B \rightarrow \tau \rightarrow e$</td>
<td></td>
<td>353 ± 17 ± 42</td>
<td>93 ± 9 ± 11</td>
</tr>
<tr>
<td>$B \rightarrow D_s \rightarrow e$</td>
<td></td>
<td>293 ± 19 ± 110</td>
<td>72 ± 9 ± 28</td>
</tr>
<tr>
<td>$B \rightarrow D \rightarrow e$</td>
<td></td>
<td>226 ± 16 ± 57</td>
<td>65 ± 8 ± 16</td>
</tr>
<tr>
<td>Secondary tags</td>
<td>8073 ± 91 ± 2,000</td>
<td>296 ± 17 ± 74</td>
<td>886 ± 29 ± 220</td>
</tr>
<tr>
<td>$e$ from $J/\psi$ or $\phi(2S)$</td>
<td>1925 ± 42 ± 122</td>
<td>77 ± 8 ± 6</td>
<td>119 ± 10 ± 7</td>
</tr>
<tr>
<td>$e$ removed by $J/\psi$ veto</td>
<td>(2435 ± 50 ± 220)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Net $e$ yield</td>
<td>304048 ± 880 ± 2,100</td>
<td>12890 ± 180 ± 230</td>
<td>8500 ± 200 ± 300</td>
</tr>
</tbody>
</table>

Background contributions from $B \rightarrow D(s)\tau X, D(s)\rightarrow e\nu\tau Y$ decays and $B \rightarrow \tau \rightarrow e$ decays are estimated by Monte Carlo simulation, using the ISGW2 model [9] to describe semileptonic $D$ and $D_s$ decays, together with currently known branching fractions: Combining $B(D_s \rightarrow X e \nu)$ = $(8.12 \pm 0.68)$%, which is computed from the average $D$ branching fraction $B(D^{0,+,s} \rightarrow X e \nu)$ [1] and the lifetime ratios $\tau_{D^{0,+}}/\tau_{D_s}$, with $B(B \rightarrow D_s \tau X) = (9.8 \pm 3.7)$% [11] yields $B(B \rightarrow D \tau X) = (0.80 \pm 0.31)$%. We take the inclusive branching fraction $B(B \rightarrow D D^* X)$ to be $(8.2 \pm 1.3)$% [11]. Assuming equal production rates of $D$ and $D^*$, but allowing for any ratio in the systematic error, we arrive at $B(B \rightarrow D \rightarrow e) = (0.84 \pm 0.21)$%. To estimate the contribution of electrons from $\tau$ decays, we use $B(B \rightarrow X \tau\nu) = (2.6 \pm 0.2)$%, $B(D_s \rightarrow \tau \nu) = (5.79 \pm 2.00)$% [12] and $B(\tau \rightarrow e \nu \bar{\nu}) = (17.83 \pm 0.06)$% [1]. This leads to $B(B \rightarrow \tau \rightarrow e) = (0.565 \pm 0.063)$%, where the $\tau$ lepton originates either directly from a $B$ decay or from a $B \rightarrow D_s \rightarrow \tau$ cascade.

The tag electron sample is first corrected for continuum background and hadron misidentification. The remaining background is from secondary decays of charm particles, $\psi(2S)$ and unvetoes J/$\psi$, $e^+e^-$ decays. All these contributions are estimated by Monte Carlo simulation, leading to the background-subtracted number of tag electrons $N_{tag} = 304048 \pm 880$(stat) $\pm 2100$(syst) (Table I).

Due to $B^0\bar{B}^0$ flavor oscillations, electrons from primary $B$ decays and $B \rightarrow D X, D \rightarrow e^- \nu \tau Y$ cascades contribute to both unlike- and like-sign spectra. Denoting the efficiency of the opening angle cut as $\epsilon_{d}(p^*)$, their $p^*$ distributions can be written as

\[
\frac{dN^{e+}}{dp^*} = \frac{dN_{B \rightarrow X e \nu}}{dp^*}(1 - \chi + \frac{dN_{B \rightarrow D \rightarrow X e \nu}}{dp^*} \chi),
\]

\[
\frac{dN^{e-}}{dp^*} = \frac{dN_{B \rightarrow X e \nu}}{dp^*} \chi + \frac{dN_{B \rightarrow D \rightarrow X e \nu}}{dp^*}(1 - \chi),
\]

where $\chi$ is the product of the $B^0\bar{B}^0$ mixing parameter $\chi_0 = 0.174 \pm 0.009$ [1] and $f_{0} = B(Y(4S) \rightarrow B^0\bar{B}^0)$. Since the measured ratio of charged to neutral Y(4S) decays is consistent with unity [13], we assume $f_0 = 0.500 \pm 0.025$, where the error is taken from [13]. We use these linear equations to determine the primary electron spectrum from $B$ decays, $dn_{B \rightarrow X e \nu}/dp^*$. Integration of this spectrum between 0.6 and 2.5 GeV/c yields $N_{B \rightarrow X e \nu} = 25070 \pm 410$(stat). Using Monte Carlo simulation, the electron yield is corrected for electron identification efficiency.

TABLE II. Impact of systematic uncertainties on $B_{SL}$.

<table>
<thead>
<tr>
<th>Source</th>
<th>$\Delta B_{SL}$ (%)</th>
<th>Source</th>
<th>$\Delta B_{SL}$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\gamma \rightarrow e^+e^-$</td>
<td>0.042</td>
<td>$B \rightarrow D_{s} \rightarrow e$</td>
<td>0.130</td>
</tr>
<tr>
<td>Faked $e$</td>
<td>0.024</td>
<td>$B \rightarrow D \rightarrow e$</td>
<td>0.067</td>
</tr>
<tr>
<td>$e$ from same $B$</td>
<td>0.022</td>
<td>Mistagged $e$</td>
<td>0.061</td>
</tr>
<tr>
<td>$\pi^0 \rightarrow \gamma e^+e^-$</td>
<td>0.014</td>
<td>$B \rightarrow \tau \rightarrow e$</td>
<td>0.044</td>
</tr>
<tr>
<td>Continuum</td>
<td>0.008</td>
<td>$J/\psi, \phi(2S) \rightarrow e^+e^-$</td>
<td>0.003</td>
</tr>
<tr>
<td>$e$ efficiency</td>
<td>0.144</td>
<td>Extrapolation</td>
<td>0.092</td>
</tr>
<tr>
<td>$\epsilon_{r_{k}}$</td>
<td>0.120</td>
<td>$N_{tag}$</td>
<td>0.075</td>
</tr>
<tr>
<td>$\epsilon_{int}$</td>
<td>0.054</td>
<td>$f_0\chi_0$</td>
<td>0.059</td>
</tr>
<tr>
<td>$\epsilon_{br_{em}}$</td>
<td>0.039</td>
<td>$\Delta B_{SL}$ (%)</td>
<td>0.296</td>
</tr>
</tbody>
</table>

Total $\Delta B_{SL} = 0.296$.
MEASUREMENT OF THE BRANCHING FRACTION FOR ... PHYSICAL REVIEW D 67, 031101(R) (2003)

TABLE III. Determination of $\kappa$, $B_{SL}$, and the contributions to the systematic error for different signal electron momentum cutoffs. All numbers are stated in percent.

<table>
<thead>
<tr>
<th>$p_{\text{min}}^*$ (GeV/c)</th>
<th>0.5</th>
<th>0.6</th>
<th>0.7</th>
<th>0.8</th>
<th>0.9</th>
<th>1.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\kappa$</td>
<td>3.8</td>
<td>6.1</td>
<td>9.3</td>
<td>13.6</td>
<td>19.2</td>
<td>27.2</td>
</tr>
<tr>
<td>$B_{SL}$</td>
<td>10.79</td>
<td>10.87</td>
<td>10.87</td>
<td>10.82</td>
<td>10.80</td>
<td>10.93</td>
</tr>
<tr>
<td>$\Delta B_{SL}(\gamma, \pi^0)$</td>
<td>0.07</td>
<td>0.04</td>
<td>0.03</td>
<td>0.02</td>
<td>0.02</td>
<td>0.01</td>
</tr>
<tr>
<td>$\Delta B_{SL}(\epsilon_{\text{eff}})$</td>
<td>0.12</td>
<td>0.12</td>
<td>0.12</td>
<td>0.12</td>
<td>0.12</td>
<td>0.12</td>
</tr>
<tr>
<td>$\Delta B_{SL}(B \rightarrow D_s)$</td>
<td>0.17</td>
<td>0.13</td>
<td>0.09</td>
<td>0.06</td>
<td>0.05</td>
<td>0.04</td>
</tr>
<tr>
<td>$\Delta B_{SL}(B \rightarrow \tau)$</td>
<td>0.10</td>
<td>0.07</td>
<td>0.05</td>
<td>0.03</td>
<td>0.02</td>
<td>0.01</td>
</tr>
<tr>
<td>$\Delta B_{SL}(B \rightarrow D)$</td>
<td>0.05</td>
<td>0.04</td>
<td>0.04</td>
<td>0.03</td>
<td>0.03</td>
<td>0.02</td>
</tr>
<tr>
<td>$\Delta B_{SL}(\text{extrapolation})$</td>
<td>0.06</td>
<td>0.09</td>
<td>0.13</td>
<td>0.19</td>
<td>0.25</td>
<td>0.33</td>
</tr>
<tr>
<td>$\Delta B_{SL}(\text{other})$</td>
<td>0.15</td>
<td>0.14</td>
<td>0.14</td>
<td>0.15</td>
<td>0.15</td>
<td>0.17</td>
</tr>
<tr>
<td>$\Delta B_{SL}(\text{syst})$</td>
<td>0.33</td>
<td>0.30</td>
<td>0.29</td>
<td>0.30</td>
<td>0.34</td>
<td>0.41</td>
</tr>
<tr>
<td>$\Delta B_{SL}(\text{stat})$</td>
<td>0.21</td>
<td>0.18</td>
<td>0.16</td>
<td>0.16</td>
<td>0.15</td>
<td>0.15</td>
</tr>
</tbody>
</table>

Based on the work by Hoang et al. [15], we relate decay rate and modulus of the CKM matrix element $V_{cb}$ by

$$|V_{cb}| = (41.9 \pm 0.8_{\text{pert}}, 0.7_{(\text{stat})} \pm 0.5_{(m_b)} ) \times 10^{-3} \\
\times \sqrt{B(B \rightarrow X_e \nu)}/1.05 \sqrt{1.6 \text{ ps}/\tau_B}.$$

Using $\tau_B = (1.601 \pm 0.021) \text{ ps}$ and $B(B \rightarrow X_e \nu) = (1.7 \pm 0.6) \times 10^{-3}$ [1], we obtain $|V_{cb}| = 0.0423 \pm 0.0007 (\text{expt}) \pm 0.0020 (\text{theory})$, where the individual theoretical errors have been added linearly.

In conclusion, we have used electrons in $Y(4S)$ decays tagged by a high momentum electron to measure $B(B \rightarrow X_e \nu) = (10.87 \pm 0.18 (\text{stat}) \pm 0.30 (\text{syst}))%$. This measurement is largely model independent. The result is in agreement with previous measurements [4,16], but the systematic uncertainties are reduced. However, the poorly known branching fractions in $B$ and $D_s$ decays lead to significant systematic uncertainties in the background subtraction. The resulting measurement of $|V_{cb}|$ remains dominated by theoretical uncertainties.

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