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Effect of Salt Concentration Profiles on Protrusion Growth in Lithium-polymer-lithium Cells

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Batteries”, “Salt Concentration Gradient”, “Concentrated Solution Theory”, “Electrochemical
Properties”.

ABSTRACT

21 The formation of dendrites and other protrusions on lithium metal anodes is a subject of
22 continued interest due to the potential to incorporate these anodes in next-generation
23 rechargeable batteries with increased energy densities. Solid polymer electrolytes show
24 improved stability against lithium metal compared to liquid carbonate electrolytes. We have
25 studied the effect of salt concentration on the formation of protrusions formed on
26 electrodeposited lithium through a rigid block copolymer electrolyte, polystyrene-*block*-
27 poly(ethylene oxide) (PS-*b*-PEO or SEO), in a lithium-lithium symmetric cell. The cell lifetime
28 decreases by a factor of 100 when salt concentration is increased by a factor of 5. Our main
29 objective is to understand the reason for this observation. We show that this decrease is not due
30 to a salt-induced change of the morphology of the block-copolymer electrolyte, nor is it due to a
31 salt-induced change of mechanical properties. We use an approach based on Newman's
32 concentrated solution theory to fully characterize ion transport in the block-copolymer
33 electrolyte, and report the conductivity, salt diffusion coefficient, cation transference number, and
34 thermodynamic factor. Neither cell lifetime nor protrusion density in failed cells correlate with
35 any of these electrochemical parameters. However, the electrochemical parameters can be used to
36 predict salt concentration profiles in our symmetric cells. We posit that an important parameter in
37 protrusion growth is the magnitude of the salt concentration gradient, Δ . We observe a direct
38 correlation between Δ and lithium protrusion growth.

INTRODUCTION

The formation of dendrites and other protrusions on lithium metal anodes[1–5] is a subject of continued interest due to the potential to incorporate them in rechargeable batteries with high energy densities.[6–10] Numerous theoretical and experimental studies aim to determine the underpinnings of dendrite growth on lithium metal anodes.[11–16] Several studies on solid polymer electrolytes show improved chemical stability and cycling reversibility against lithium metal.[17–23] In practical batteries, electrolytes with higher salt concentrations are necessary to maximize the flux of lithium ions.[24–26]

The work presented here builds on previous studies in which we investigated the effect of temperature[27], current density,[28] and salt concentration[29] on the electrodeposition of lithium through block copolymer electrolytes. In a previous study[29], we uncovered the effect of salt concentration on the formation of protrusions formed on electrodeposited lithium through a rigid block copolymer electrolyte, polystyrene-*block*-poly(ethylene oxide) (PS-*b*-PEO or SEO) mixed with LiTFSI (lithium bis(trifluoromethanesulfonyl) imide). Li/SEO/Li symmetric cells were cycled at a fixed current density and the cycle life was found to decrease rapidly with increasing salt concentration. The purpose of this work is to determine the reason for this decrease in cycle life. In particular, we show that this decrease is not due to a salt-induced change of the morphology of the block-copolymer electrolyte, nor is it due to a salt-induced change of mechanical properties. We use the Newman approach[30] to characterize the block-copolymer electrolyte, and report the conductivity, salt diffusion coefficient, cation transference number and thermodynamic factor. These parameters are used to predict salt concentration profiles in our

symmetric cells.[31] We find a strong correlation between the nature of these concentration profiles and cell lifetime.

METHODS

Materials. In this study, we used a polystyrene-*block*-poly(ethylene oxide) copolymer electrolyte (SEO), which was synthesized by anionic polymerization, as described in previous work.[32–34] The molar masses of the PS and PEO blocks were 235 and 222 kg mol⁻¹, respectively, with a PEO volume fraction of 0.475 without salt and an overall polydispersity index of 1.05. Methods for electrolyte preparation and electrochemical cycling mimicked those previously reported by Maslyn *et al.*[28,35–37] All electrolyte preparation and lithium cell assembly steps were performed in an argon filled glovebox with less than 1 ppm of water and less than 1 ppm of oxygen to avoid any contamination.

Electrolyte preparation. Methods for electrolyte preparation and electrochemical cell fabrication closely mimicked those previously reported.[29] The salt used in this study was lithium bis(trifluoromethanesulfonyl) imide (LiTFSI). The average salt concentration, r_{av} , defined as the molar ratio of lithium cations to the ether oxygen, varied from 0.04 to 0.20. For simplicity, we in the following refer to the set of electrolytes as SEO electrolyte.

Ionic conductivity. Ionic conductivity measurements were performed using both aluminum/SEO/aluminum symmetric cells and Li/SEO/Li symmetric cells. Cells were assembled

using punched SEO electrolyte membranes with a diameter of 3/8 inch and two aluminum blocking electrodes or lithium metal non-blocking electrodes (FMC), backed with nickel foil, of 5/16 inch diameter. The obtained aluminum sandwiches were pressed in a hand-press at 90 °C for 10 s, while the obtained lithium sandwiches were pressed in a hand-press at room temperature for 10 s. Then, aluminum tabs were added and assembled cells were vacuum sealed inside a laminated aluminum pouch material (Showa-Denko) in order to carry out experiments outside of the glovebox. Cells were placed in a custom heating stage. First, cells were annealed at 120 °C for 4 h in order to ensure good contact and erase the electrolyte's temperature history. Next, the cells were decreased to room temperature and then heated up to 90 °C and equilibrated for 1 h prior to the electrochemical measurements. Ionic conductivity measurements were measured by ac impedance spectroscopy using a BioLogic VMP3 potentiostat. Complex electrochemical impedance spectra were acquired for a frequency range from 1 MHz to 1 Hz at an amplitude of 10 mV. The data were analyzed in the form of a Nyquist plot and an electrical equivalent circuit was used to fit the data and obtain the bulk resistance to calculate the ionic conductivity.

Current fraction and restricted diffusion experiments. Steady-state current fraction and restricted diffusion measurements were performed using Li/SEO/Li symmetric cells (same assembly method as lithium metal ionic conductivity cells) and a BioLogic VMP3 potentiostat.

All measurements were performed at 90°C. To ensure stable interfacial layers at the lithium-polymer interfaces, 15 charge (positive current density applied)/discharge (negative current density applied) conditioning cycles at a low current density of 0.02 mA cm⁻² were performed prior to the measurements. Each conditioning cycle consisted of a 4 h charge followed by a 45

104 min rest and a 4 h discharge. Ac electrochemical impedance spectroscopy was performed before
 105 polarization. Impedance spectra were measured from 1 MHz to 1 Hz at an amplitude of 10 mV.
 106 The data were plotted in the form of Nyquist plots and analyzed using equivalent electrical
 107 circuits. The steady-state current fraction experiment consisted of applying a potential of $\Delta V =$
 108 10 mV and measuring the current at time intervals of 2 s for 2 h, a time long enough to reach
 109 steady-state current. Ac impedance spectra were measured every 20 min.

110 In the absence of a concentration gradient (i.e. prior to polarization), the calculated initial
 111 current, i_0 , is defined by the Ohm's law as given in Equation 1, where ΔV is the potential
 112 applied, and $R_{i,0}$ and $R_{b,0}$ the initial resistances measured for the interface and the bulk
 113 respectively.

$$114 \quad i_0 = \frac{\Delta V}{R_{i,0} + R_{b,0}} \quad \text{Equation 1}$$

115 The current fraction, $\rho_{i,ss}$, was calculated according to Equation 2, where $R_{i,ss}$ is the resistance of
 116 the interface at steady-state, and i_{ss} is the steady-state current.[38,39]

$$117 \quad \rho_{i,ss} = \frac{i_{ss}(\Delta V - i_0 R_{i,0})}{i_0(\Delta V - i_{ss} R_{i,ss})} \quad \text{Equation 2}$$

118 The restricted salt diffusion coefficients were measured using the polarization induced by the
 119 current fraction experiment. The potential applied was stopped and cells were allowed to relax
 120 for 4 h while the open-circuit voltage, U , was recorded at time interval of 1 s. The restricted salt
 121 diffusion coefficient, D , was calculated according to:

$$122 \quad \frac{-d \ln U}{dt} = \frac{\pi^2 D}{L^2}, \quad \text{Equation 3}$$

123 where L is the thickness of the electrolyte, and the left side of Equation 3 is the slope from the
124 least-squares fit of $-\ln U$ vs. time.

125 **Galvanostatic experiments.** Methods to prepare, condition and cycle Li/SEO/Li symmetric cells
126 can be found in previous work by Frenck *et al.*[29]

127 **Scanning Electron Microscopy.** Three samples were prepared for morphology analysis. The
128 SEO block-copolymer was dissolved in N-methylpyrrolidone, (NMP), and mixed with LiTFSI
129 salt such that r_{av} was equal to 0.04, 0.085 and 0.12. Then each solution was drop casted on a
130 silicon wafer. The solvent was evaporated at 60 °C on a casting plate, and then the samples were
131 dried at 90 °C under active vacuum for 3 days prior to the experiment. Samples were transferred
132 to the SEM facility using an air-tight desiccator. To prevent charging artefacts, a Gatan Sputter
133 Coater was used to coat all samples with an approximately 2 nm thick carbon layer. The
134 morphology of the samples was investigated using a FEI Helios G4 UX scanning electron
135 microscope operated at 2 kV. Secondary electron images were acquired using the through-lens
136 detector.

137 **Linear Rheology experiments.** All sample preparation was performed inside an argon filled
138 glove box. Three samples were prepared: one neat polymer sample, and two SEO electrolytes
139 with $r_{av} = 0.085$ and $r_{av} = 0.20$, respectively. The neat SEO sample was prepared by adding
140 polymer into a 1 mm thick polycarbonate spacer with a 9 mm diameter hole, and pressing it
141 between two Teflon sheets in a hand press heated to 120 °C. The sample was pressed at this
142 temperature for 4 h and then removed from the spacer using a metal punch. The two salt-
143 containing samples were prepared by first casting polymer electrolyte membranes (see
144 electrolyte preparation). Then the membrane was punched to obtain 9 mm disks, which were hot

pressed together inside a hand press at 110 °C until a 1 mm thick disk was obtained. After preparation, the final samples were transferred in a desiccator to a Rheometric Scientific ARES Rheostat. Prior to the experiment, the rheometer plattens were cleaned and heated up to 90 °C under a flow of dry nitrogen. In addition, the gap between the plattens was zeroed. The samples were then placed between the plattens; samples were in contact with air for less than 30 s before the nitrogen-purged oven was closed.

Samples were first annealed at 120 °C for 1 h. Then, the temperature was decreased to 90 °C, the temperature used for measurements. Samples were left to equilibrate for 1 h at 90 °C prior to the measurement. First, a dynamic strain sweep test was performed at a frequency of 1 rad s⁻¹ to ensure measurement in the linear regime between stress and strain. Then a frequency sweep test was performed from 1 to 100 rad s⁻¹ at the chosen strain. In order to ensure good adhesion between the plattens and the sample, a normal force between 10 and 40 gm was applied during measurement. One sample of each polymer type was made due to limited material; however, measurements were repeated 3 times and averaged.

RESULTS AND DISCUSSION

Figure 1 summarizes results of cell cycling experiments on Li/SEO/Li symmetric cells as a function of average salt concentration in the SEO electrolyte. These results are taken from reference [29]. In each cycle, a steady current density of 0.175 mA cm⁻² was applied for 4 hours in one direction followed by 45 minutes of rest and another 4 hours of the same steady current in the opposite direction followed by 45 minutes of rest. The average number of cycles to failure is plotted as a function of r_{av} in Figure 1. The right ordinate converts cycles to charge density passed before failure, including charge passed during the conditioning cycles (8.64 C cm⁻²). Cells

fail due to short circuit when a growing protrusion from one electrode touches the opposite electrode. The cell lifetime decreases rapidly with average salt concentration between $r_{av} = 0.04$ and $r_{av} = 0.15$. The cell lifetime at $r_{av} = 0.04$ is a factor of 10 larger than that at $r_{av} = 0.15$. Between $r_{av} = 0.15$ and $r_{av} = 0.20$ the cell lifetime remains low but increases slightly. Our main objective is to understand the reason for the large decrease in cell lifetime presented in Figure 1. We present our understanding based on three sets of characterization results: electron microscopy, rheology and electrochemical characterization.

Figure 1. Average number of cycles to failure (cell lifetime) at 90 °C (left y axis) as a function of salt concentration in the SEO electrolyte, r_{av} . The cycles shown do not include the conditioning cycles. Charge density passed just before failure, C_d , is shown on the right y axis, where charge density passed during conditioning is included ($8.64\ C\ cm^{-2}$). Error bars represent the standard deviation from 3 to 6 cells. Data taken from reference [29].

180 The morphologies of three electrolytes at $r_{av} = 0.04$, $r_{av} = 0.085$, and $r_{av} = 0.12$ are shown in
181 Figure 2. All electron micrographs show lamellae, with bright PEO lamellae alternating with
182 dark PS lamellae. This morphology is consistent with the volume fraction of the PEO-rich
183 microphase in our electrolytes.[40,41] The micrographs in Figure 2 were obtained at room
184 temperature and do not necessarily represent the grain structures in the symmetric cells at 90 °C.
185 We suspect that the formation of spherulites (defined as radial centrosymmetric organization of
186 crystals often seen in semi-crystalline polymers) at $r_{av} = 0.04$ is due to effects related to the
187 crystallization of the PEO block. Differential scanning calorimetry experiments (DSC) indicate
188 that the sample at $r_{av} = 0.04$ is crystalline at room temperature with a melting point at 57 °C and
189 a crystallinity percentage of 45%, while $r_{av} = 0.085$ presents a melting temperature at 43 °C with
190 a low crystallinity percentage of 2%, and $r_{av} = 0.12$ is completely amorphous at room
191 temperature (see DSC data and methods in supplemental information Figure S1). Our cycling
192 and electrochemical data were obtained at 90 °C, where all of the electrolytes are amorphous.
193 We expect the morphology of the $r_{av} = 0.04$ electrolyte at 90 °C to be similar to that shown in
194 Figures 2(b) and (c). The glass transition temperature, T_g , of the PS phase is roughly 108 °C for
195 the whole range of salt concentrations (see Figure S2 in SI). The domain spacing of the lamellae
196 phases (center to center distance between adjacent PS lamellae) is not a strong function of salt
197 concentration and is, on average, 165 nm, in the micrographs in Figure 2. This value is consistent
198 with previous reports.[42] The SEM data in Figure 2 show that the decrease in cell lifetime by a
199 factor of 5 when r_{av} increases from 0.04 to 0.12 cannot be attributed to a change in electrolyte
200 morphology.

Figure 2. Electron micrographs of SEO electrolytes at room temperature. (a) $r_{av} = 0.04$, (b) $r_{av} = 0.085$ and (c) $r_{av} = 0.12$. The morphology of the $r_{av} = 0.04$ sample is distorted due to crystallization of the PEO block. All of the ion transport experiments were conducted in the amorphous state pictured in (b) and (c). We expect the morphology of the $r_{av} = 0.04$ sample in the amorphous state to be similar to Figures (b) and (c).

The relationship between mechanical properties of the electrolyte and cycle life of Li/SEO/Li symmetric cells has been discussed extensively in the literature,[27,37,43] starting with pioneering work by Monroe and Newman.[24,44,45]

Figure 3 shows the frequency dependency of storage (G') and loss (G'') shear moduli of SEO, measured at 90 °C, as a function of increasing average salt concentration (from neat to r_{av}

212 = 0.20). All three samples are viscoelastic solids where G' is significantly larger than G'' . In
 213 theory, the growth of protrusion through electrolytes is a slow process governed by the low
 214 frequency shear modulus. The data in Figure 3 indicate no deterioration in the low frequency
 215 shear modulus in SEO electrolytes as a function of increasing average salt concentration. Thus, it
 216 is evident that the rapid decrease in cycle life seen in Figure 1 is not related to mechanical
 217 properties.

219 **Figure 3.** Frequency (ω) dependence of (a) storage (G') and (b) loss (G'') moduli measured at 90
 220 °C for the neat SEO electrolyte, and salt-containing SEO electrolytes at $r_{av} = 0.085$ and $r_{av} =$
 221 0.20. Error bars from the 3 repeated measurements for each sample are too small to be visible.

222 The results of electrochemical characterization experiments on this SEO electrolyte as a
 223 function of average salt concentration are shown in Figure 4. All electrochemical
 224 characterization was conducted at 90 °C, the temperature used throughout the protrusion growth
 225 study.

Figure 4(a) presents the ionic conductivity from ac impedance spectroscopy of symmetric cells with blocking electrodes, κ_b , and with non-blocking electrodes, κ_{nb} , as a function of the average salt concentration. Both κ_b and κ_{nb} follow the same trend. The ionic conductivity increases with r_{av} until a maximum is reached in the vicinity of $r_{av} = 0.085$. This is followed by a decrease at higher r_{av} values. This behavior is similar to many previous reports on the ionic conductivity of SEO electrolytes.[20,46–51] The solid curve represents a polynomial fit through the κ_b data; the polynomial is given in Figure 4(a). In order to reduce the influence of experimental noise on our analysis, fits of experimental data will be used.

235

236

237 **Figure 4.** Electrochemical properties of SEO electrolytes at 90 °C as a function of salt
 238 concentration, r_{av} . (a) Ionic conductivity, κ , from ac impedance spectroscopy of symmetric cells
 239 with blocking electrodes, κ_b , and with non-blocking electrodes, κ_{nb} . (b) Salt diffusion coefficient,
 240 D , obtained by restricted diffusion in a Li/SEO/Li symmetric cell (diamonds represent the
 241 average measured diffusion coefficient). The solid line represents the average diffusion
 242 coefficient. The two dotted lines represent the upper and lower bounds of the experimental data
 243 including error bars. (c) Current fraction, ρ_+ , obtained using the steady-state current technique in
 244 a Li/SEO/Li symmetric cell. Error bars in (a), (b), and (c) represent the standard deviation from 3
 245 measurements. (d) Product of ionic conductivity, κ_{nb} , (Figure 4(a)) and steady-state current
 246 fraction, ρ_+ (Figure 4(c)). The error bars represent the standard errors calculated from the
 247 standard deviations of the measured κ_{nb} and ρ_+ .

248 Figure 4(b) presents the salt diffusion coefficient, D , obtained by the restricted diffusion
 249 method, in Li/SEO/Li symmetric cells at 90 °C. The data are scattered around an average value

250 of $2.69 \times 10^{-8} \text{ cm}^2 \text{ s}^{-1}$, represented by the solid red line in Figure 4(b). These data are consistent
 251 with previous studies of SEO electrolytes.[48] For simplicity, we assume that D is independent
 252 of salt concentration. The dotted lines in Figure 4(b) represent the upper and lower bounds of the
 253 experimental data including error bars.

254 Figure 4(c) shows the current fraction, ρ_{+Li} , measured at 90 °C, determined by the steady-
 255 state approach proposed by Bruce and Vincent.[38] This method gives the cation transference
 256 number for a thermodynamically ideal dilute electrolyte. The current fraction follows a parabolic
 257 trend with a minimum at $r_{av} = 0.15$, consistent with previous studies.[48,52] The solid turquoise
 258 curve in Figure 4(c) represents a quadratic fit.

259 The current obtained in a Li/SEO/Li symmetric cell in the limit of small applied fields is
 260 proportional to the product $\kappa_{nb} \rho_{+Li}$. [39,53–55] (For comparison, we show this product for both
 261 conductivity measured with blocking and non-blocking electrodes in Figure S3 in the SI.) This
 262 product is thus a measure of the efficacy of the electrolyte in the limit of infinitesimal current. In
 263 Figure 4(d) we plot $\kappa_{nb} \rho_{+Li}$ versus r_{av} . The dependence of $\kappa_{nb} \rho_{+Li}$ on r_{av} is non-monotonic with a
 264 sharp maximum on $r_{av} = 0.085$ and a relatively shallow maximum at $r_{av} = 0.20$.

265 Since we have already shown that the dependence of morphology and mechanical properties
 266 of our SEO electrolyte on average salt concentration cannot explain the cell cycling results in
 267 Figure 1, we are left with the conclusion that the electrochemical properties of the electrolyte
 268 must play a role. The data in Figure 4(b) indicate that cell lifetime is not affected by the salt
 269 diffusion coefficient alone, as the former is a strong function of average salt concentration and
 270 the latter is independent of average salt concentration. Similarly, the dependence of the efficacy

271 of SEO electrolytes, in the limit of small applied fields, on average salt concentration is very
 272 different from the dependence of cell lifetime on average salt concentration (Figure 4(d)). We
 273 thus examine other electrochemical characteristics of our SEO electrolytes.

274 Complete electrochemical characterization of an electrolyte requires knowledge of the
 275 transference number with respect to the solvent velocity, $t_{+,\vec{c},\vec{c}}$, [48,56,57] and the thermodynamic
 276 factor, T_f . We use the method described in reference [57] to determine $t_{+,\vec{c},\vec{c}}$ and T_f from the data
 277 presented in Figure 4. This method requires knowledge of the open circuit potential of the
 278 electrolyte in concentration cells. In reference [52], it was shown that the open circuit potential
 279 of many different SEO electrolytes was within experimental error (see Figure S3 in SI). We use
 280 this result to calculate $t_{+,\vec{c},\vec{c}}$ and T_f of our SEO electrolyte as a function of r_{av} , and these results are
 281 given in Figure 5.

Figure 5. (a) Cation transference number with respect to the solvent velocity, t_{+}^{0} and (b) thermodynamic factor $T_f = 1 + \frac{d \ln \gamma_{\pm}}{d \ln m}$. Fitted values from Figures 4(a), (b) and (c) are used to evaluate t_{+}^{0} and T_f . Markers are the calculated data, error bars represent the standard errors calculated from the standard deviations of the measured properties, and dotted lines are polynomial fits.

Equations 4 and 5 were used to determine t_{+}^{0} and T_f from experimental measurements.

$$t_{+}^{0} = 1 + \frac{d \ln \gamma_{+}}{d \ln m} \quad \text{Equation 4}$$

$$T_f = \left(1 + \frac{d \ln \gamma_{\pm}}{d \ln m} \right) = - \frac{z_{+} F}{RT} \quad \text{Equation 5}$$

where F is the Faraday constant (C mol), R is the gas constant (J mol⁻¹ K⁻¹), c is the salt concentration (mol.cm⁻³), ϕ_c is the volume fraction of the conducting phase, m is the molality (mol kg⁻¹), $\frac{dU}{d \ln m}$ is the change in the open circuit potential, z_{+} is the charge number, ν_{+} is the number of cations, both z_{+} and ν_{+} are 1 for LiTFSI, and $\nu = \nu_{+} + \nu_{-}$.

We used fitted functions for the concentration dependent parameters on the right-hand side of Equations 4 and 5 to obtain t_{+}^{0} and T_f : the solid curves in Figures 4(a) and (c) and the horizontal line in Figure 4(b).

The cation transference number is negative over the entire range of average salt concentration, varying from -0.31 to -2.14 (Figure 5(a)). It is a non-monotonic function of average salt concentration with a maximum at $r_{av} = 0.06$ and a minimum at $r_{av} = 0.20$. The thermodynamic factor, shown in Figure 5(b), varies between 0.34 and 0.8. If the electrolyte were

thermodynamically ideal, T_f would be unity at all average salt concentrations. Even at very low average salt concentrations, our electrolytes are far from ideal.[46,48,57]

It is instructive to examine the salt concentration gradients that emerge in our electrolyte at $i = 0.175 \text{ mA cm}^{-2}$. These gradients depend on all of the transport and thermodynamic parameters discussed in Figures 4 and 5. The importance of salt concentration gradients has been recognized by several researchers.[14,58] We used the methodology developed by Pesko *et al.*[31] to calculate $r(x)$, the salt concentration profile at steady state which is given by

$$\int_{r(x=0)}^{r(x)} \frac{D(r)c(r)}{r t_{-i^0 i}} dr = \int_{r(x=0)}^{r(x)} J(r) dr = \frac{-iL}{F} \left(\frac{x}{L} \right) i, \quad \text{Equation 6}$$

where $c(r)$ is the molar salt concentration, and the anion transference number, $t_{-i^0 i}$, is defined as $1 - t_{+i^0 i}$.

Furthermore, substituting $t_{-i^0 i}$ by its equivalent using Equation 4 in $J(r)$, we can rewrite Equation 6 as:

$$J(r) = \frac{\kappa}{i i} \quad \text{Equation 7}$$

The integrand on the left side of equation 6 contains two parameters $D(r)$ and $t_{-i^0 i}$. It is important to recognize that $t_{-i^0 i}$ (or equivalently $t_{+i^0 i}$) is not measured directly but requires

combining measurements of $\rho_{+i i}$ with κ , D and $\frac{dU}{d \ln m}$ (see Equation 4). The experimental

uncertainty of $t_{-i^0 i}$ is thus compounded by the experimental uncertainty of 4 independently

measured parameters. In contrast, the 3 parameters given in Equation 7, $\rho_{+i i}$, κ and $\frac{dU}{d \ln m}$ are all

measured directly. Equation 7 also makes it clear that the current, i , is not dependent on D , and

321 this arises because t_{-i}^0 is proportional to D . Equation 6 and 7 are based on the framework
 322 presented in [30]. For the case of thermodynamically ideal dilute electrolytes, these equations
 323 reduce to the familiar result of Bruce and Vincent in the limit of small salt concentration.[38]

324
 325 **Figure 6.** Dependence of $J(r)$ on salt concentration, r_{av} , at 90 °C. The dashed curve shows the
 326 least-squares polynomial fit. Error bars show the standard error calculated from the standard
 327 deviations of the measured electrochemical parameters.

328 The integrand, $J(r)$, is a known function of salt concentration r_{av} . We plot this function in
 329 Figure 6. A polynomial fit was used to calculate the required integral. The dashed curve shows a
 330 polynomial fit of Equation 7:

$$331 \quad J(r) = ar_{av}^6 + br_{av}^5 + cr_{av}^4 + dr_{av}^3 + er_{av}^2 + fr_{av} + g, \quad \text{Equation 8}$$

332 with fitting parameters $a = -4 \times 10^{-4}$, $b = 4 \times 10^{-4}$, $c = -1 \times 10^{-4}$, $d = 3 \times 10^{-5}$, $e = -3 \times 10^{-6}$, $f = 2 \times$
 333 10^{-7} , and $g = -3 \times 10^{-9}$. Our goal is to establish $r(x)$ for a given value of r_{av} and i . This is achieved

334 by first assuming $r(x = 0)$ and solving for $r(x)$ using Equation 7 for all x from 0^+ to L by
335 numerical integration.

336 Figure 7(a) presents the salt concentration profile at steady state for all salt concentrations at
337 a current density of 0.02 mA cm^{-2} , the current density used during the conditioning cycles. Figure
338 7(b) presents the salt concentration profile at steady state for all salt concentrations at a current
339 density of 0.175 mA cm^{-2} , the current density used during in our study of protrusion growth. For
340 both sets of calculations, the electrolyte thickness was assumed to be 0.005 cm . As expected,
341 increasing current density results in steeper concentration gradients. The magnitude of the
342 gradients also increases with average salt concentration. This is seen more clearly in Figure 7(b).

Figure 7. Concentration profiles in SEO electrolytes predicted by concentrated solution theory at steady-state at 90 °C. (a) Concentration profiles for $i = 0.02 \text{ mA cm}^{-2}$, the current density used during conditioning cycles. (b) Concentration profiles for $i = 0.175 \text{ mA cm}^{-2}$, the current density used in our study of protrusion growth during cell cycling. The anode is at $x/L = 0$ and the cathode is at $x/L = 1$.

In order to quantify differences in salt concentration profiles (Figure 7), we define an average salt concentration gradient, Δ , to be the difference of salt concentration between the anode and cathode electrodes, divided by the thickness of the cell. Figure 8 presents the calculated salt

352 concentration gradients as a function of average salt concentration for the two current densities
 353 of interest. During the conditioning cycles (blue squares), salt concentration gradients are small,
 354 varying from 0.4 cm^{-1} for $r_{av} = 0.06$ to 1.3 cm^{-1} for $r_{av} = 0.20$. However, for the higher current
 355 density (turquoise circles), the gradients are large and about 10 times higher than that during the
 356 conditioning cycles. One may use the magnitude of Δ as a measure of the efficacy of an
 357 electrolyte at the current density of interest. The magnitude of the salt concentration gradient to
 358 maintain a current density of $i = 0.175 \text{ mA cm}^{-2}$ increases monotonically with salt concentration.
 359 Many theories[59,60] suggest that lithium dendrite growth is affected by the magnitude of salt
 360 concentration gradients. It is therefore instructive to examine the cycling behavior of our cells as
 361 a function of Δ .

362 **Figure 8.** A plot of average salt concentration gradient at 90°C , Δ , defined as the salt
 363 concentration difference between the cathode and the anode normalized by electrolyte thickness,
 364 as a function of the average salt concentration, r_{av} , for current density used in the conditioning
 365

cycles at $i = 0.02 \text{ mA cm}^{-2}$ (turquoise circles) and for current density used in our study of protrusion growth during cell cycling at $i = 0.175 \text{ mA cm}^{-2}$ (blue squares).

In Figure 9(a) we plot cell lifetime as a function of Δ . We see a direct correlation between the two parameters. Cell lifetime decreases precipitously as Δ increases from 2.8 cm^{-1} to 9.5 cm^{-1} . The average salt concentrations used to obtain each of the data points is indicated using the color scheme shown on the right. Cell lifetimes obtained at the two highest values of Δ are slightly higher than that at 9.5 cm^{-1} , an observation that requires further investigation. Nevertheless, the data in Figure 9(a) indicate that Δ must be significantly less than 9 cm^{-1} for stable cycling of lithium-lithium symmetric cells. We note in passing that Δ for the conditioning cycles ranges from 0.4 to 1.3 cm^{-1} . This range is well outside the range of gradients where rapid cell failure is expected. Planar and stable deposition might be expected in this range as seen by Maslyn *et al.* [28]

Figure 9. (a) Cell lifetime (cycles to failure) and (b) average number of defects per cycle, P_c , as a function of salt concentration gradient, Δ at 90 °C. Data points are color-coded according to salt concentration, r_{av} , using the color scale presented on the right. Dashed lines are guides for the eye.

An important characteristic of failed cells is the areal density of defects on the electrodes at the point of failure. Since different cells exhibited different lifetimes, it makes sense to examine the average number of defects per cycle P_c , in all of the failed cells. The procedure for quantifying P_c is presented in ref.[29] In Figure 9(b), we plot P_c versus Δ . To a good approximation, P_c is independent of Δ when Δ increases from 2.8 cm⁻¹ to 9.5 cm⁻¹, suggesting that areal defect density in this regime is related to an intrinsic property of lithium metal rather than the applied current. Note that cell lifetime decreases rapidly over the same range of Δ values. In the regime $\Delta > 9.5$ cm⁻¹, P_c increases substantially with Δ , suggesting that defects density in this regime is affected by the applied current. Many of the defects seen at high salt concentration do not protrude significantly into the electrolyte (see Figure S5 in the SI). Since cell-failure requires a protrusion to span the thickness of the electrolyte, our experiments do not shed light on the effect of these defects on cell-failure.

CONCLUSION

We have studied both the failure of cycled Li/SEO/Li symmetric cells due to the defective electrodeposition of lithium and the formation of lithium protrusions as a function of salt concentration in the SEO electrolyte (r_{av}) at a fixed current density. The SEO electrolyte presents a lamellar morphology at all salt concentrations. We find that the cell lifetime decreases by a factor of 100 when salt concentration in the SEO electrolyte is increased from $r_{av}=0.04$ to 0.15,

401 and it remains low at the highest salt concentrations tested. The average number of defective
402 deposits on the electrodes is also considerably higher at high salt concentrations. We know that
403 the defective electrodeposition of lithium is controlled by electrochemical and mechanical
404 properties of the electrolyte. Since these properties depend on the morphology of the electrolyte,
405 we first studied the effect of salt on electrolyte morphology. We found no qualitative differences
406 in the morphology as a function of salt concentration. We also found no significant difference in
407 the mechanical properties as a function of r_{av} . The electrochemical properties were quantified by
408 measuring the ionic conductivity, salt diffusion coefficient, transference number, and
409 thermodynamic factor. None of these properties deteriorated rapidly with increasing salt
410 concentration. We used these properties to compute salt concentration profiles in the symmetric
411 cells using Newman's concentrated solution theory. We posit that Δ , the average salt
412 concentration gradient across the electrolyte, governs protrusion growth from a lithium metal
413 cathode through an electrolyte. We show that cell lifetime decreases linearly with Δ .

414 Since the early work by Monroe and Newman,[24,44,45] it has been clear that the growth of
415 lithium protrusions is related to the electrochemical and mechanical properties of the electrolyte.
416 Which of these properties is directly relevant for the observed protrusions has not yet been
417 established. It is common to report parameters such as modulus, conductivity, and transference
418 number. These parameters characterize the linear response of the electrolyte as they are relevant
419 when the electrolyte is slightly perturbed away from equilibrium. The shear modulus describes
420 stress-strain behavior in the limit of infinitesimal strain, conductivity describes the voltage-
421 current relationship in the limit of infinitesimal current densities, and the transference number
422 describes the migration of ions at uniform concentration. In this work, we have shown that cell

lifetime and protrusion density are not dependent on these parameters. Instead, we find that cell lifetime and protrusion density appear to be correlated with the concentration gradient, Δ , a parameter that reflects the nonlinear response of the electrolyte to the applied current density used in the cycling experiments. It would be interesting to see if the relationship between lithium protrusion growth and electrochemical properties in different classes of electrolytes can be understood in term of Δ .

ASSOCIATED CONTENT

The following file is available free of charge.

Supplementary Information (PDF)

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Author Contributions

J.A.M. and W.S.L. synthesized SEO block copolymer. L.F., J.A.M., and V.V. fabricated samples and performed the experiments. A. M. acquired scanning electron micrographs. A.S.H. contributed to calculations. L.F. and N.P.B. prepared figures and composed the manuscript. N.P.B. directed the work.

451 **Notes**

452 The authors declare no competing financial interest.

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467

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469 **LIST OF SYMBOLS**

470 C_d , Charge density passed (C.cm⁻²); Δ , salt concentration gradient; d , Domain spacing (nm); D ,
471 restricted salt diffusion coefficient; $\frac{dU}{d\ln m}$, change in the open circuit potential; ΔV , potential
472 applied (V); F , Faraday constant (G' , Storage shear modulus; G'' , loss shear modulus; i ,

473 Applied current density (mA cm^{-2}); i_0 , measured initial current (A); i_Ω , calculated initial current
 474 (A); κ_b , ionic conductivity from measurements with blocking electrodes (S.cm^{-1}); κ_{nb} , ionic
 475 conductivity from measurements with non-blocking electrodes (S cm^{-1}); L , electrolyte thickness;
 476 Li , Lithium; $Li\text{-ion}$, Lithium-ion battery; $LiTFSI$, Lithium bis (trifluoromethanesulfonyl) imide;
 477 m , molality (mol kg^{-1}); NMP , N-methylpyrrolidone; ρ_+ , steady-state current fraction; ϕ_c ,
 478 volume fraction of the conducting phase; P_c , average number of defects per cycle; PEO ,
 479 Poly(ethylene oxide); PS , Polystyrene; R , gas constant ($\text{J mol}^{-1} \text{K}^{-1}$); r_{av} , Average salt
 480 concentration; $R_{b,0}$, initial bulk resistance (Ω); $R_{i,0}$, initial interfacial resistance (Ω); $R_{i,ss}$,
 481 interfacial resistance at steady state (Ω); SEI , Solid Electrolyte Interphase; SEO , Polystyrene-*b*-
 482 poly(ethylene) oxide; T , temperature; $t_{+\text{Li}^+}$, cation transference number; $t_{-\text{PF}_6^-}$, anion transference
 483 number; T_f , thermodynamic factor; U , open-circuit voltage (V); $v_{+\text{Li}^+}$, number of cations for
 484 $LiTFSI$; $z_{+\text{Li}^+}$, the charge number for $LiTFSI$.

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