

UC Berkeley

UC Berkeley Previously Published Works

Title

Effect of salt concentration profiles on protrusion growth in lithium-polymer-lithium cells

Permalink

<https://escholarship.org/uc/item/2w06f6z7>

Authors

Frenck, Louise
Veeraraghavan, Vijay D
Maslyn, Jacqueline A
et al.

Publication Date

2020-12-01

DOI

10.1016/j.ssi.2020.115517

Peer reviewed

1 **Effect of Salt Concentration Profiles on**
2 **Protrusion Growth in Lithium-polymer-lithium**
3 **Cells**

4 *Louise Frenck^{a,b}, Vijay D. Veeraraghavan^a, Jacqueline A. Maslyn^{a,b}, Alexander Müller^{c,d}, Alec S.*
5 *Ho^{a,b}, Whitney. S. Loo^a, Andrew M. Minor^{c,d}, Nitash P. Balsara^{a,b}*

6

7 ^aDepartment of Chemical and Biomolecular Engineering, University of California, Berkeley,
8 California 94720, United States

9 ^bMaterials Sciences Division, Lawrence Berkeley National Laboratory, Berkeley, California
10 94720, United States

11 ^cNational Center for Electron Microscopy, Molecular Foundry, Lawrence Berkeley National
12 Laboratory, Berkeley, California 94720, United States

13 ^dDepartment of Materials Science and Engineering, University of California, Berkeley,
14 California 94720, United States

15

16 **KEYWORDS:** “Lithium”, “Polymer Electrolyte”, “Salt Concentration”, “Rechargeable
17 Batteries”, “Salt Concentration Gradient”, “Concentrated Solution Theory”, “Electrochemical
18 Properties”.

19

20 **ABSTRACT**

21 The formation of dendrites and other protrusions on lithium metal anodes is a subject of
22 continued interest due to the potential to incorporate these anodes in next-generation
23 rechargeable batteries with increased energy densities. Solid polymer electrolytes show
24 improved stability against lithium metal compared to liquid carbonate electrolytes. We have
25 studied the effect of salt concentration on the formation of protrusions formed on
26 electrodeposited lithium through a rigid block copolymer electrolyte, polystyrene-*block*-
27 poly(ethylene oxide) (PS-*b*-PEO or SEO), in a lithium-lithium symmetric cell. The cell lifetime
28 decreases by a factor of 100 when salt concentration is increased by a factor of 5. Our main
29 objective is to understand the reason for this observation. We show that this decrease is not due
30 to a salt-induced change of the morphology of the block-copolymer electrolyte, nor is it due to a
31 salt-induced change of mechanical properties. We use an approach based on Newman's
32 concentrated solution theory to fully characterize ion transport in the block-copolymer
33 electrolyte, and report the conductivity, salt diffusion coefficient, cation transference number, and
34 thermodynamic factor. Neither cell lifetime nor protrusion density in failed cells correlate with
35 any of these electrochemical parameters. However, the electrochemical parameters can be used to
36 predict salt concentration profiles in our symmetric cells. We posit that an important parameter in
37 protrusion growth is the magnitude of the salt concentration gradient, Δ . We observe a direct
38 correlation between Δ and lithium protrusion growth.

39

40 INTRODUCTION

41 The formation of dendrites and other protrusions on lithium metal anodes[1–5] is a subject of
42 continued interest due to the potential to incorporate them in rechargeable batteries with high
43 energy densities.[6–10] Numerous theoretical and experimental studies aim to determine the
44 underpinnings of dendrite growth on lithium metal anodes.[11–16] Several studies on solid
45 polymer electrolytes show improved chemical stability and cycling reversibility against lithium
46 metal.[17–23] In practical batteries, electrolytes with higher salt concentrations are necessary to
47 maximize the flux of lithium ions.[24–26]

48 The work presented here builds on previous studies in which we investigated the effect of
49 temperature[27], current density,[28] and salt concentration[29] on the electrodeposition of
50 lithium through block copolymer electrolytes. In a previous study[29], we uncovered the effect
51 of salt concentration on the formation of protrusions formed on electrodeposited lithium through
52 a rigid block copolymer electrolyte, polystyrene-*block*-poly(ethylene oxide) (PS-*b*-PEO or SEO)
53 mixed with LiTFSI (lithium bis(trifluoromethanesulfonyl) imide). Li/SEO/Li symmetric cells
54 were cycled at a fixed current density and the cycle life was found to decrease rapidly with
55 increasing salt concentration. The purpose of this work is to determine the reason for this
56 decrease in cycle life. In particular, we show that this decrease is not due to a salt-induced change
57 of the morphology of the block-copolymer electrolyte, nor is it due to a salt-induced change of
58 mechanical properties. We use the Newman approach[30] to characterize the block-copolymer
59 electrolyte, and report the conductivity, salt diffusion coefficient, cation transference number and
60 thermodynamic factor. These parameters are used to predict salt concentration profiles in our

61 symmetric cells.[31] We find a strong correlation between the nature of these concentration
62 profiles and cell lifetime.

63

64

65

66 METHODS

67 **Materials.** In this study, we used a polystyrene-*block*-poly(ethylene oxide) copolymer
68 electrolyte (SEO), which was synthesized by anionic polymerization, as described in previous
69 work.[32–34] The molar masses of the PS and PEO blocks were 235 and 222 kg mol⁻¹,
70 respectively, with a PEO volume fraction of 0.475 without salt and an overall polydispersity
71 index of 1.05. Methods for electrolyte preparation and electrochemical cycling mimicked those
72 previously reported by Maslyn *et al.*[28,35–37] All electrolyte preparation and lithium cell
73 assembly steps were performed in an argon filled glovebox with less than 1 ppm of water and
74 less than 1 ppm of oxygen to avoid any contamination.

75 **Electrolyte preparation.** Methods for electrolyte preparation and electrochemical cell
76 fabrication closely mimicked those previously reported.[29] The salt used in this study was
77 lithium bis(trifluoromethanesulfonyl) imide (LiTFSI). The average salt concentration, r_{av} ,
78 defined as the molar ratio of lithium cations to the ether oxygen, varied from 0.04 to 0.20. For
79 simplicity, we in the following refer to the set of electrolytes as SEO electrolyte.

80 **Ionic conductivity.** Ionic conductivity measurements were performed using both
81 aluminum/SEO/aluminum symmetric cells and Li/SEO/Li symmetric cells. Cells were assembled

82 using punched SEO electrolyte membranes with a diameter of 3/8 inch and two aluminum
83 blocking electrodes or lithium metal non-blocking electrodes (FMC), backed with nickel foil, of
84 5/16 inch diameter. The obtained aluminum sandwiches were pressed in a hand-press at 90 °C
85 for 10 s, while the obtained lithium sandwiches were pressed in a hand-press at room
86 temperature for 10 s. Then, aluminum tabs were added and assembled cells were vacuum sealed
87 inside a laminated aluminum pouch material (Showa-Denko) in order to carry out experiments
88 outside of the glovebox. Cells were placed in a custom heating stage. First, cells were annealed
89 at 120 °C for 4 h in order to ensure good contact and erase the electrolyte's temperature history.
90 Next, the cells were decreased to room temperature and then heated up to 90 °C and equilibrated
91 for 1 h prior to the electrochemical measurements. Ionic conductivity measurements were
92 measured by ac impedance spectroscopy using a BioLogic VMP3 potentiostat. Complex
93 electrochemical impedance spectra were acquired for a frequency range from 1 MHz to 1 Hz at
94 an amplitude of 10 mV. The data were analyzed in the form of a Nyquist plot and an electrical
95 equivalent circuit was used to fit the data and obtain the bulk resistance to calculate the ionic
96 conductivity.

97 **Current fraction and restricted diffusion experiments.** Steady-state current fraction and
98 restricted diffusion measurements were performed using Li/SEO/Li symmetric cells (same
99 assembly method as lithium metal ionic conductivity cells) and a BioLogic VMP3 potentiostat.
100 All measurements were performed at 90°C. To ensure stable interfacial layers at the lithium-
101 polymer interfaces, 15 charge (positive current density applied)/discharge (negative current
102 density applied) conditioning cycles at a low current density of 0.02 mA cm⁻² were performed
103 prior to the measurements. Each conditioning cycle consisted of a 4 h charge followed by a 45

104 min rest and a 4 h discharge. Ac electrochemical impedance spectroscopy was performed before
 105 polarization. Impedance spectra were measured from 1 MHz to 1 Hz at an amplitude of 10 mV.
 106 The data were plotted in the form of Nyquist plots and analyzed using equivalent electrical
 107 circuits. The steady-state current fraction experiment consisted of applying a potential of $\Delta V =$
 108 10 mV and measuring the current at time intervals of 2 s for 2 h, a time long enough to reach
 109 steady-state current. Ac impedance spectra were measured every 20 min.

110 In the absence of a concentration gradient (i.e. prior to polarization), the calculated initial
 111 current, i_{Ω} , is defined by the Ohm's law as given in Equation 1, where ΔV is the potential
 112 applied, and $R_{i,0}$ and $R_{b,0}$ the initial resistances measured for the interface and the bulk
 113 respectively.

$$114 \quad i_{\Omega} = \frac{\Delta V}{R_{i,0} + R_{b,0}} \quad \text{Equation 1}$$

115 The current fraction, ρ_{+i} , was calculated according to Equation 2, where $R_{i,ss}$ is the resistance of
 116 the interface at steady-state, and i_{ss} is the steady-state current.[38,39]

$$117 \quad \rho_{+i} = \frac{i_{ss}(\Delta V - i_{\Omega} R_{i,0})}{i_{\Omega}(\Delta V - i_{ss} R_{i,ss})} \quad \text{Equation 2}$$

118 The restricted salt diffusion coefficients were measured using the polarization induced by the
 119 current fraction experiment. The potential applied was stopped and cells were allowed to relax
 120 for 4 h while the open-circuit voltage, U , was recorded at time interval of 1 s. The restricted salt
 121 diffusion coefficient, D , was calculated according to:

$$122 \quad \frac{-d \ln U}{dt} = \frac{\pi^2 D}{L}, \quad \text{Equation 3}$$

123 where L is the thickness of the electrolyte, and the left side of Equation 3 is the slope from the
124 least-squares fit of $-\ln U$ vs. time.

125 **Galvanostatic experiments.** Methods to prepare, condition and cycle Li/SEO/Li symmetric cells
126 can be found in previous work by Frenck *et al.*[29]

127 **Scanning Electron Microscopy.** Three samples were prepared for morphology analysis. The
128 SEO block-copolymer was dissolved in N-methylpyrrolidone, (NMP), and mixed with LiTFSI
129 salt such that r_{av} was equal to 0.04, 0.085 and 0.12. Then each solution was drop casted on a
130 silicon wafer. The solvent was evaporated at 60 °C on a casting plate, and then the samples were
131 dried at 90 °C under active vacuum for 3 days prior to the experiment. Samples were transferred
132 to the SEM facility using an air-tight desiccator. To prevent charging artefacts, a Gatan Sputter
133 Coater was used to coat all samples with an approximately 2 nm thick carbon layer. The
134 morphology of the samples was investigated using a FEI Helios G4 UX scanning electron
135 microscope operated at 2 kV. Secondary electron images were acquired using the through-lens
136 detector.

137 **Linear Rheology experiments.** All sample preparation was performed inside an argon filled
138 glove box. Three samples were prepared: one neat polymer sample, and two SEO electrolytes
139 with $r_{av} = 0.085$ and $r_{av} = 0.20$, respectively. The neat SEO sample was prepared by adding
140 polymer into a 1 mm thick polycarbonate spacer with a 9 mm diameter hole, and pressing it
141 between two Teflon sheets in a hand press heated to 120 °C. The sample was pressed at this
142 temperature for 4 h and then removed from the spacer using a metal punch. The two salt-
143 containing samples were prepared by first casting polymer electrolyte membranes (see
144 electrolyte preparation). Then the membrane was punched to obtain 9 mm disks, which were hot

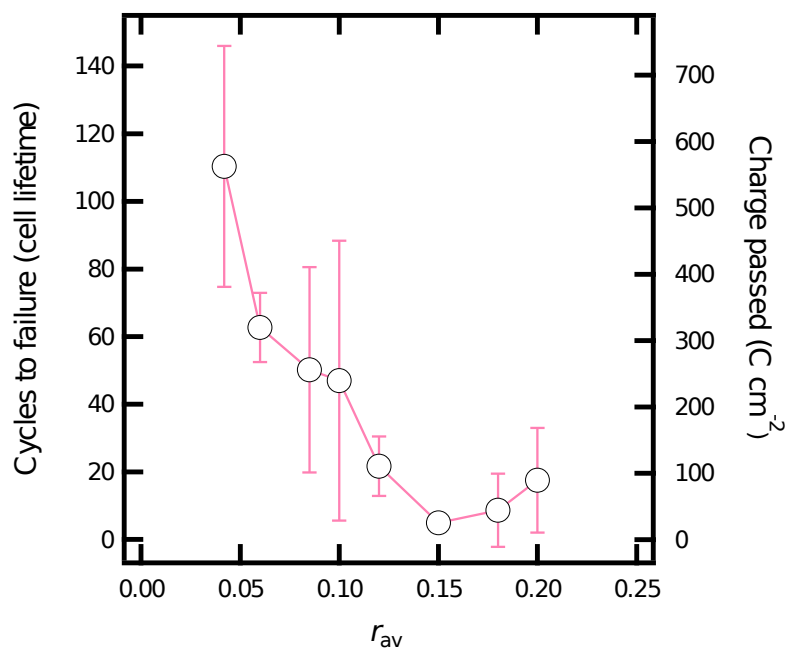
145 pressed together inside a hand press at 110 °C until a 1 mm thick disk was obtained. After
146 preparation, the final samples were transferred in a desiccator to a Rheometric Scientific ARES
147 Rheostat. Prior to the experiment, the rheometer plattens were cleaned and heated up to 90 °C
148 under a flow of dry nitrogen. In addition, the gap between the plattens was zeroed. The samples
149 were then placed between the plattens; samples were in contact with air for less than 30 s before
150 the nitrogen-purged oven was closed.

151 Samples were first annealed at 120 °C for 1 h. Then, the temperature was decreased to 90 °C,
152 the temperature used for measurements. Samples were left to equilibrate for 1 h at 90 °C prior to
153 the measurement. First, a dynamic strain sweep test was performed at a frequency of 1 rad s⁻¹ to
154 ensure measurement in the linear regime between stress and strain. Then a frequency sweep test
155 was performed from 1 to 100 rad s⁻¹ at the chosen strain. In order to ensure good adhesion
156 between the plattens and the sample, a normal force between 10 and 40 gm was applied during
157 measurement. One sample of each polymer type was made due to limited material; however,
158 measurements were repeated 3 times and averaged.

159 RESULTS AND DISCUSSION

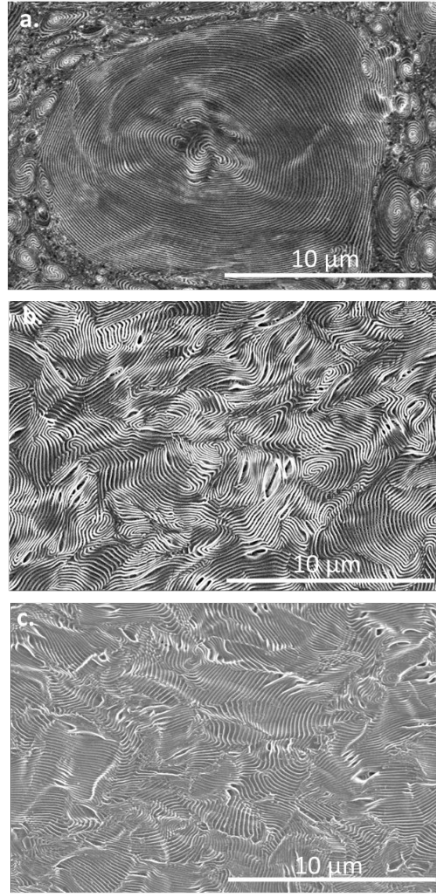
160 Figure 1 summarizes results of cell cycling experiments on Li/SEO/Li symmetric cells as a
161 function of average salt concentration in the SEO electrolyte. These results are taken from
162 reference [29]. In each cycle, a steady current density of 0.175 mA cm⁻² was applied for 4 hours
163 in one direction followed by 45 minutes of rest and another 4 hours of the same steady current in
164 the opposite direction followed by 45 minutes of rest. The average number of cycles to failure is
165 plotted as a function of r_{av} in Figure 1. The right ordinate converts cycles to charge density
166 passed before failure, including charge passed during the conditioning cycles (8.64 C cm⁻²). Cells

167 fail due to short circuit when a growing protrusion from one electrode touches the opposite
168 electrode. The cell lifetime decreases rapidly with average salt concentration between $r_{av} = 0.04$
169 and $r_{av} = 0.15$. The cell lifetime at $r_{av} = 0.04$ is a factor of 10 larger than that at $r_{av} = 0.15$.
170 Between $r_{av} = 0.15$ and $r_{av} = 0.20$ the cell lifetime remains low but increases slightly. Our main
171 objective is to understand the reason for the large decrease in cell lifetime presented in Figure 1.
172 We present our understanding based on three sets of characterization results: electron
173 microscopy, rheology and electrochemical characterization.



174
175 **Figure 1.** Average number of cycles to failure (cell lifetime) at 90 °C (left y axis) as a function
176 of salt concentration in the SEO electrolyte, r_{av} . The cycles shown do not include the
177 conditioning cycles. Charge density passed just before failure, C_d , is shown on the right y axis,
178 where charge density passed during conditioning is included ($8.64\ C\ cm^{-2}$). Error bars represent
179 the standard deviation from 3 to 6 cells. Data taken from reference [29].

180 The morphologies of three electrolytes at $r_{av} = 0.04$, $r_{av} = 0.085$, and $r_{av} = 0.12$ are shown in
181 Figure 2. All electron micrographs show lamellae, with bright PEO lamellae alternating with
182 dark PS lamellae. This morphology is consistent with the volume fraction of the PEO-rich
183 microphase in our electrolytes.[40,41] The micrographs in Figure 2 were obtained at room
184 temperature and do not necessarily represent the grain structures in the symmetric cells at 90 °C.
185 We suspect that the formation of spherulites (defined as radial centrosymmetric organization of
186 crystals often seen in semi-crystalline polymers) at $r_{av} = 0.04$ is due to effects related to the
187 crystallization of the PEO block. Differential scanning calorimetry experiments (DSC) indicate
188 that the sample at $r_{av} = 0.04$ is crystalline at room temperature with a melting point at 57 °C and
189 a crystallinity percentage of 45%, while $r_{av} = 0.085$ presents a melting temperature at 43 °C with
190 a low crystallinity percentage of 2%, and $r_{av} = 0.12$ is completely amorphous at room
191 temperature (see DSC data and methods in supplemental information Figure S1). Our cycling
192 and electrochemical data were obtained at 90 °C, where all of the electrolytes are amorphous.
193 We expect the morphology of the $r_{av} = 0.04$ electrolyte at 90 °C to be similar to that shown in
194 Figures 2(b) and (c). The glass transition temperature, T_g , of the PS phase is roughly 108 °C for
195 the whole range of salt concentrations (see Figure S2 in SI). The domain spacing of the lamellae
196 phases (center to center distance between adjacent PS lamellae) is not a strong function of salt
197 concentration and is, on average, 165 nm, in the micrographs in Figure 2. This value is consistent
198 with previous reports.[42] The SEM data in Figure 2 show that the decrease in cell lifetime by a
199 factor of 5 when r_{av} increases from 0.04 to 0.12 cannot be attributed to a change in electrolyte
200 morphology.



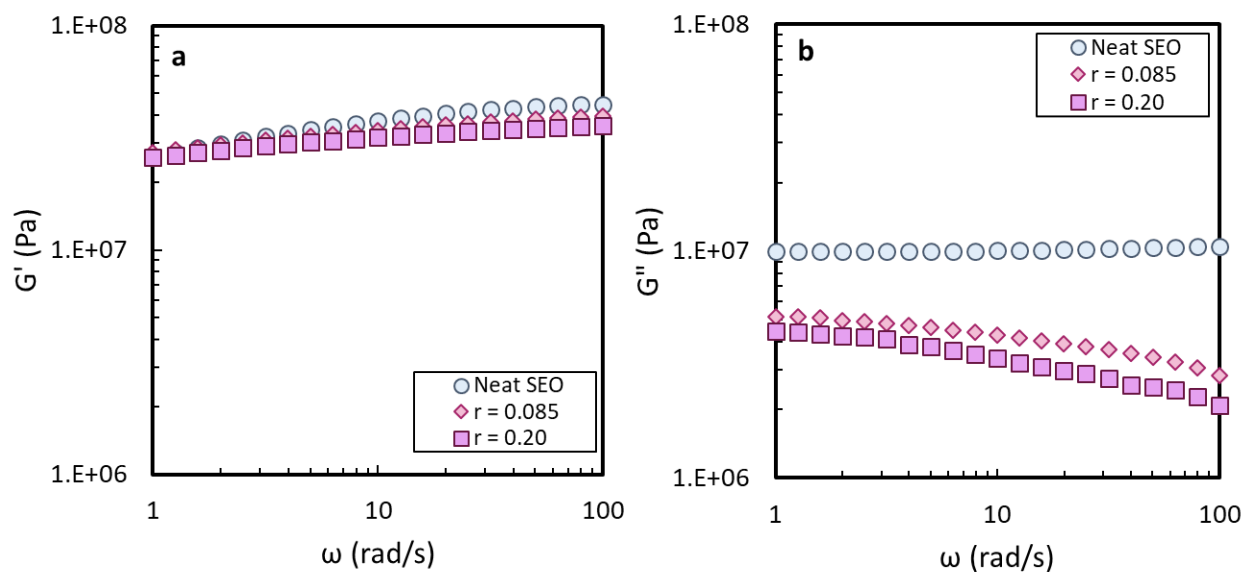
201

202 **Figure 2.** Electron micrographs of SEO electrolytes at room temperature. (a) $r_{av} = 0.04$, (b) $r_{av} =$
203 0.085 and (c) $r_{av} = 0.12$. The morphology of the $r_{av} = 0.04$ sample is distorted due to
204 crystallization of the PEO block. All of the ion transport experiments were conducted in the
205 amorphous state pictured in (b) and (c). We expect the morphology of the $r_{av} = 0.04$ sample in
206 the amorphous state to be similar to Figures (b) and (c).

207 The relationship between mechanical properties of the electrolyte and cycle life of Li/SEO/Li
208 symmetric cells has been discussed extensively in the literature,[27,37,43] starting with
209 pioneering work by Monroe and Newman.[24,44,45]

210 Figure 3 shows the frequency dependency of storage (G') and loss (G'') shear moduli of
211 SEO, measured at 90 °C, as a function of increasing average salt concentration (from neat to r_{av}

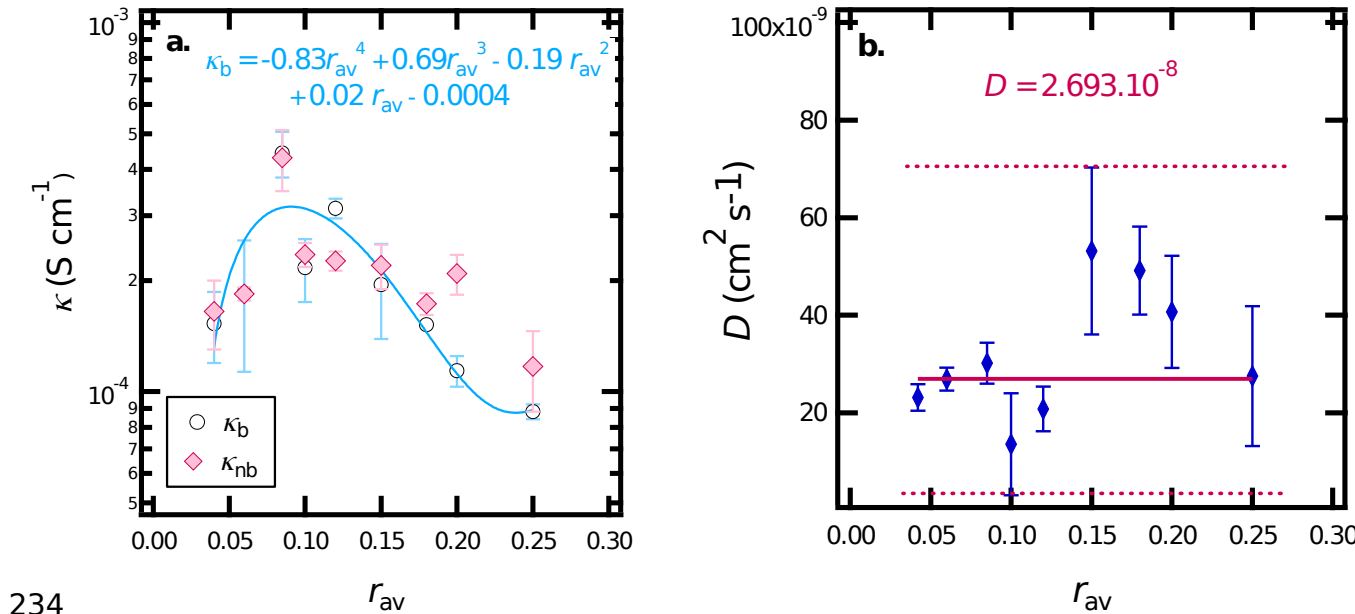
212 = 0.20). All three samples are viscoelastic solids where in G' is significantly larger than G'' . In
 213 theory, the growth of protrusion through electrolytes is a slow process governed by the low
 214 frequency shear modulus. The data in Figure 3 indicate no deterioration in the low frequency
 215 shear modulus in SEO electrolytes as a function of increasing average salt concentration. Thus, it
 216 is evident that the rapid decrease in cycle life seen in Figure 1 is not related to mechanical
 217 properties.

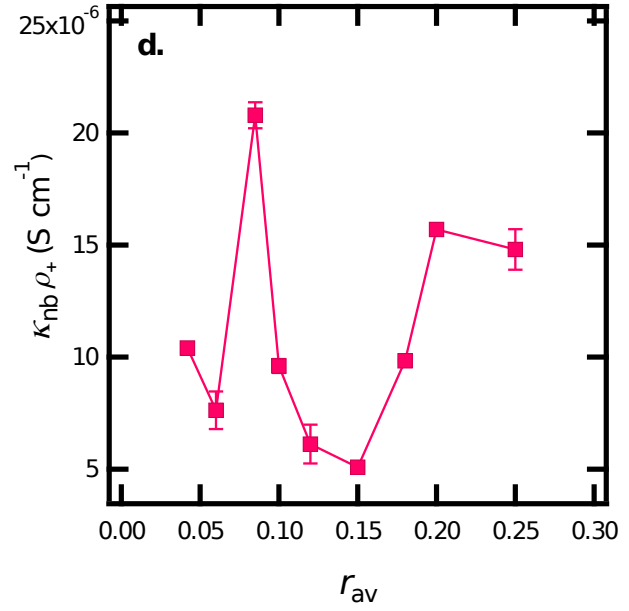
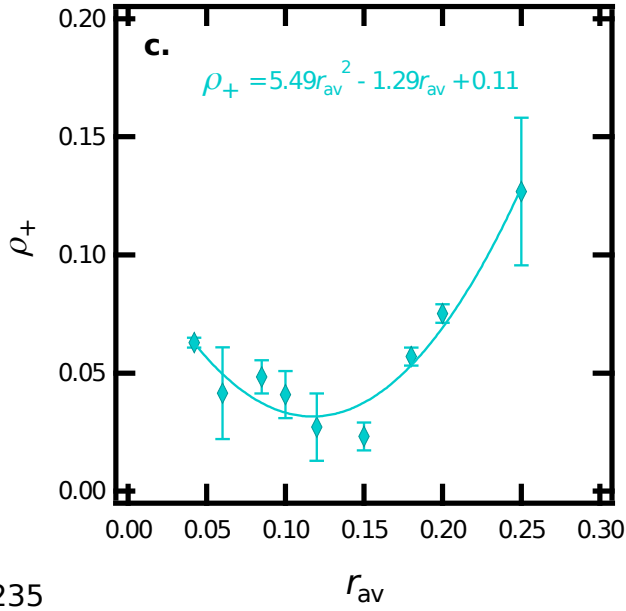


218
 219 **Figure 3.** Frequency (ω) dependence of (a) storage (G') and (b) loss (G'') moduli measured at 90
 220 $^{\circ}\text{C}$ for the neat SEO electrolyte, and salt-containing SEO electrolytes at $r_{av} = 0.085$ and $r_{av} =$
 221 0.20 . Error bars from the 3 repeated measurements for each sample are too small to be visible.

222 The results of electrochemical characterization experiments on this SEO electrolyte as a
 223 function of average salt concentration are shown in Figure 4. All electrochemical
 224 characterization was conducted at 90°C , the temperature used throughout the protrusion growth
 225 study.

226 Figure 4(a) presents the ionic conductivity from ac impedance spectroscopy of symmetric
 227 cells with blocking electrodes, κ_b , and with non-blocking electrodes, κ_{nb} , as a function of the
 228 average salt concentration. Both κ_b and κ_{nb} follow the same trend. The ionic conductivity
 229 increases with r_{av} until a maximum is reached in the vicinity of $r_{av} = 0.085$. This is followed by a
 230 decrease at higher r_{av} values. This behavior is similar to many previous reports on the ionic
 231 conductivity of SEO electrolytes.[20,46–51] The solid curve represents a polynomial fit through
 232 the κ_b data; the polynomial is given in Figure 4(a). In order to reduce the influence of
 233 experimental noise on our analysis, fits of experimental data will be used.





235
236

237 **Figure 4.** Electrochemical properties of SEO electrolytes at 90 °C as a function of salt
 238 concentration, r_{av} . (a) Ionic conductivity, κ , from ac impedance spectroscopy of symmetric cells
 239 with blocking electrodes, κ_b , and with non-blocking electrodes, κ_{nb} . (b) Salt diffusion coefficient,
 240 D , obtained by restricted diffusion in a Li/SEO/Li symmetric cell (diamonds represent the
 241 average measured diffusion coefficient). The solid line represents the average diffusion
 242 coefficient. The two dotted lines represent the upper and lower bounds of the experimental data
 243 including error bars. (c) Current fraction, ρ_+ , obtained using the steady-state current technique in
 244 a Li/SEO/Li symmetric cell. Error bars in (a), (b), and (c) represent the standard deviation from 3
 245 measurements. (d) Product of ionic conductivity, κ_{nb} , (Figure 4(a)) and steady-state current
 246 fraction, ρ_+ (Figure 4(c)). The error bars represent the standard errors calculated from the
 247 standard deviations of the measured κ_{nb} and ρ_+ .

248 Figure 4(b) presents the salt diffusion coefficient, D , obtained by the restricted diffusion
 249 method, in Li/SEO/Li symmetric cells at 90 °C. The data are scattered around an average value

250 of $2.69 \times 10^{-8} \text{ cm}^2 \text{ s}^{-1}$, represented by the solid red line in Figure 4(b). These data are consistent
251 with previous studies of SEO electrolytes.[48] For simplicity, we assume that D is independent
252 of salt concentration. The dotted lines in Figure 4(b) represent the upper and lower bounds of the
253 experimental data including error bars.

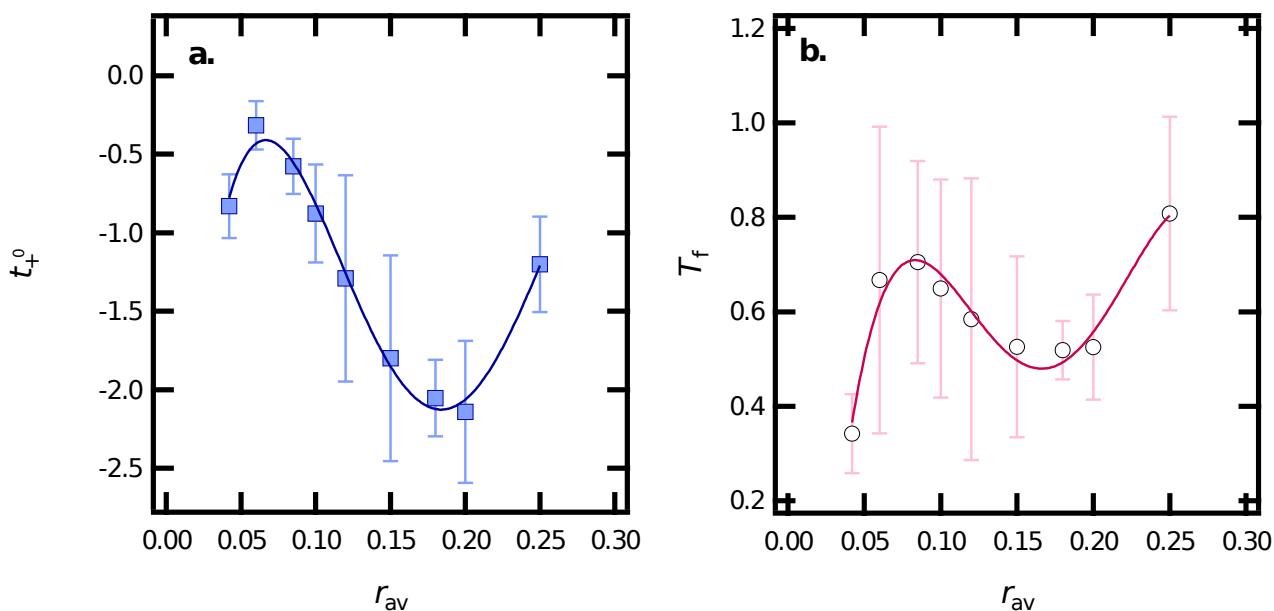
254 Figure 4(c) shows the current fraction, ρ_{+Li} , measured at 90 °C, determined by the steady-
255 state approach proposed by Bruce and Vincent.[38] This method gives the cation transference
256 number for a thermodynamically ideal dilute electrolyte. The current fraction follows a parabolic
257 trend with a minimum at $r_{av} = 0.15$, consistent with previous studies.[48,52] The solid turquoise
258 curve in Figure 4(c) represents a quadratic fit.

259 The current obtained in a Li/SEO/Li symmetric cell in the limit of small applied fields is
260 proportional to the product $\kappa_{nb} \rho_{+Li}$. [39,53–55] (For comparison, we show this product for both
261 conductivity measured with blocking and non-blocking electrodes in Figure S3 in the SI.) This
262 product is thus a measure of the efficacy of the electrolyte in the limit of infinitesimal current. In
263 Figure 4(d) we plot $\kappa_{nb} \rho_{+Li}$ versus r_{av} . The dependence of $\kappa_{nb} \rho_{+Li}$ on r_{av} is non-monotonic with a
264 sharp maximum on $r_{av} = 0.085$ and a relatively shallow maximum at $r_{av} = 0.20$.

265 Since we have already shown that the dependence of morphology and mechanical properties
266 of our SEO electrolyte on average salt concentration cannot explain the cell cycling results in
267 Figure 1, we are left with the conclusion that the electrochemical properties of the electrolyte
268 must play a role. The data in Figure 4(b) indicate that cell lifetime is not affected by the salt
269 diffusion coefficient alone, as the former is a strong function of average salt concentration and
270 the latter is independent of average salt concentration. Similarly, the dependence of the efficacy

271 of SEO electrolytes, in the limit of small applied fields, on average salt concentration is very
 272 different from the dependence of cell lifetime on average salt concentration (Figure 4(d)). We
 273 thus examine other electrochemical characteristics of our SEO electrolytes.

274 Complete electrochemical characterization of an electrolyte requires knowledge of the
 275 transference number with respect to the solvent velocity, $t_{+;i}^0$, [48,56,57] and the thermodynamic
 276 factor, T_f . We use the method described in reference [57] to determine $t_{+;i}^0$ and T_f from the data
 277 presented in Figure 4. This method requires knowledge of the open circuit potential of the
 278 electrolyte in concentration cells. In reference [52], it was shown that the open circuit potential
 279 of many different SEO electrolytes was within experimental error (see Figure S3 in SI). We use
 280 this result to calculate $t_{+;i}^0$ and T_f of our SEO electrolyte as a function of r_{av} , and these results are
 281 given in Figure 5.



282

283 **Figure 5.** (a) Cation transference number with respect to the solvent velocity, t_{+i}^0 and (b)
 284 thermodynamic factor $T_f = 1 + \frac{d \ln \gamma_{\pm}}{d \ln m}$. Fitted values from Figures 4(a), (b) and (c) are used to
 285 evaluate t_{+i}^0 and T_f . Markers are the calculated data, error bars represent the standard errors
 286 calculated from the standard deviations of the measured properties, and dotted lines are
 287 polynomial fits.

288 Equations 4 and 5 were used to determine t_{+i}^0 and T_f from experimental measurements.

289
$$t_{+i}^0 = 1 + \frac{z_{+i} R}{z_{-i} F} \ln \phi_c \quad \text{Equation 4}$$

290
$$T_f = \left(1 + \frac{d \ln \gamma_{\pm}}{d \ln m} \right) = - \frac{z_{+i} R}{z_{-i} F} \ln \phi_c \quad \text{Equation 5}$$

291 where F is the Faraday constant (C mol), R is the gas constant (J mol⁻¹ K⁻¹), c is the salt
 292 concentration (mol.cm⁻³), ϕ_c is the volume fraction of the conducting phase, m is the molality
 293 (mol kg⁻¹), $\frac{dU}{d \ln m}$ is the change in the open circuit potential, z_{+i} is the charge number, ν_{+i} is the
 294 number of cations, both z_{+i} and ν_{+i} are 1 for LiTFSI, and $\nu = \nu_{+i} + \nu_{-i}$.

295 We used fitted functions for the concentration dependent parameters on the right-hand side of
 296 Equations 4 and 5 to obtain t_{+i}^0 and T_f : the solid curves in Figures 4(a) and (c) and the horizontal
 297 line in Figure 4(b).

298 The cation transference number is negative over the entire range of average salt
 299 concentration, varying from -0.31 to -2.14 (Figure 5(a)). It is a non-monotonic function of
 300 average salt concentration with a maximum at $r_{av} = 0.06$ and a minimum at $r_{av} = 0.20$. The
 301 thermodynamic factor, shown in Figure 5(b), varies between 0.34 and 0.8. If the electrolyte were

302 thermodynamically ideal, T_f would be unity at all average salt concentrations. Even at very low
 303 average salt concentrations, our electrolytes are far from ideal.[46,48,57]

304 It is instructive to examine the salt concentration gradients that emerge in our electrolyte at i
 305 = 0.175 mA cm⁻². These gradients depend on all of the transport and thermodynamic parameters
 306 discussed in Figures 4 and 5. The importance of salt concentration gradients has been recognized
 307 by several researchers.[14,58] We used the methodology developed by Pesko *et al.*[31] to
 308 calculate $r(x)$, the salt concentration profile at steady state which is given by

$$309 \int_{r(x=0)}^{r(x)} \frac{D(r)c(r)}{r t_{-i}^0(r)} dr = \int_{r(x=0)}^{r(x)} J(r) dr = \frac{-iL}{F} \left(\frac{x}{L} \right) i, \quad \text{Equation 6}$$

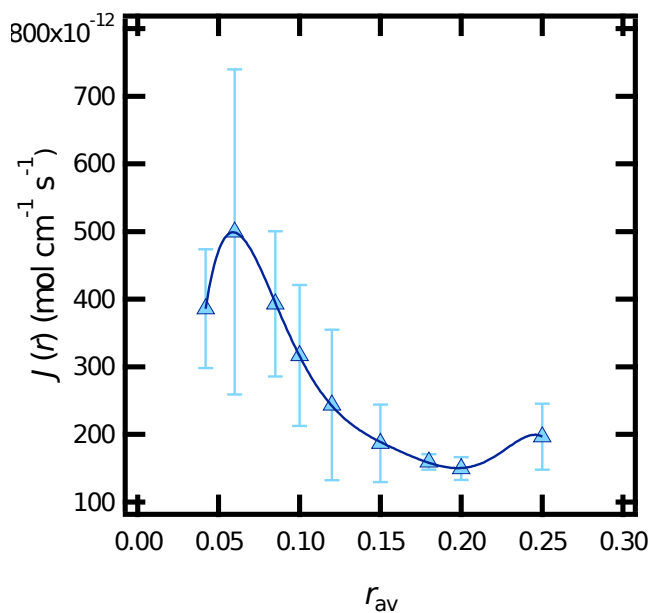
310 where $c(r)$ is the molar salt concentration, and the anion transference number, t_{-i}^0 , is defined as
 311 $1 - t_{+i}^0$.

312 Furthermore, substituting t_{-i}^0 by its equivalent using Equation 4 in $J(r)$, we can rewrite
 313 Equation 6 as:

$$314 J(r) = \frac{\kappa}{iL} \quad \text{Equation 7}$$

315 The integrand on the left side of equation 6 contains two parameters $D(r)$ and t_{-i}^0 . It is
 316 important to recognize that t_{-i}^0 (or equivalently t_{+i}^0) is not measured directly but requires
 317 combining measurements of ρ_{+i} with κ , D and $\frac{dU}{d \ln m}$ (see Equation 4). The experimental
 318 uncertainty of t_{-i}^0 is thus compounded by the experimental uncertainty of 4 independently
 319 measured parameters. In contrast, the 3 parameters given in Equation 7, ρ_{+i} , κ and $\frac{dU}{d \ln m}$ are all
 320 measured directly. Equation 7 also makes it clear that the current, i , is not dependent on D , and

321 this arises because t_{-i^0} is proportional to D . Equation 6 and 7 are based on the framework
 322 presented in [30]. For the case of thermodynamically ideal dilute electrolytes, these equations
 323 reduce to the familiar result of Bruce and Vincent in the limit of small salt concentration.[38]



324
 325 **Figure 6.** Dependence of $J(r)$ on salt concentration, r_{av} , at 90 °C. The dashed curve shows the
 326 least-squares polynomial fit. Error bars show the standard error calculated from the standard
 327 deviations of the measured electrochemical parameters.

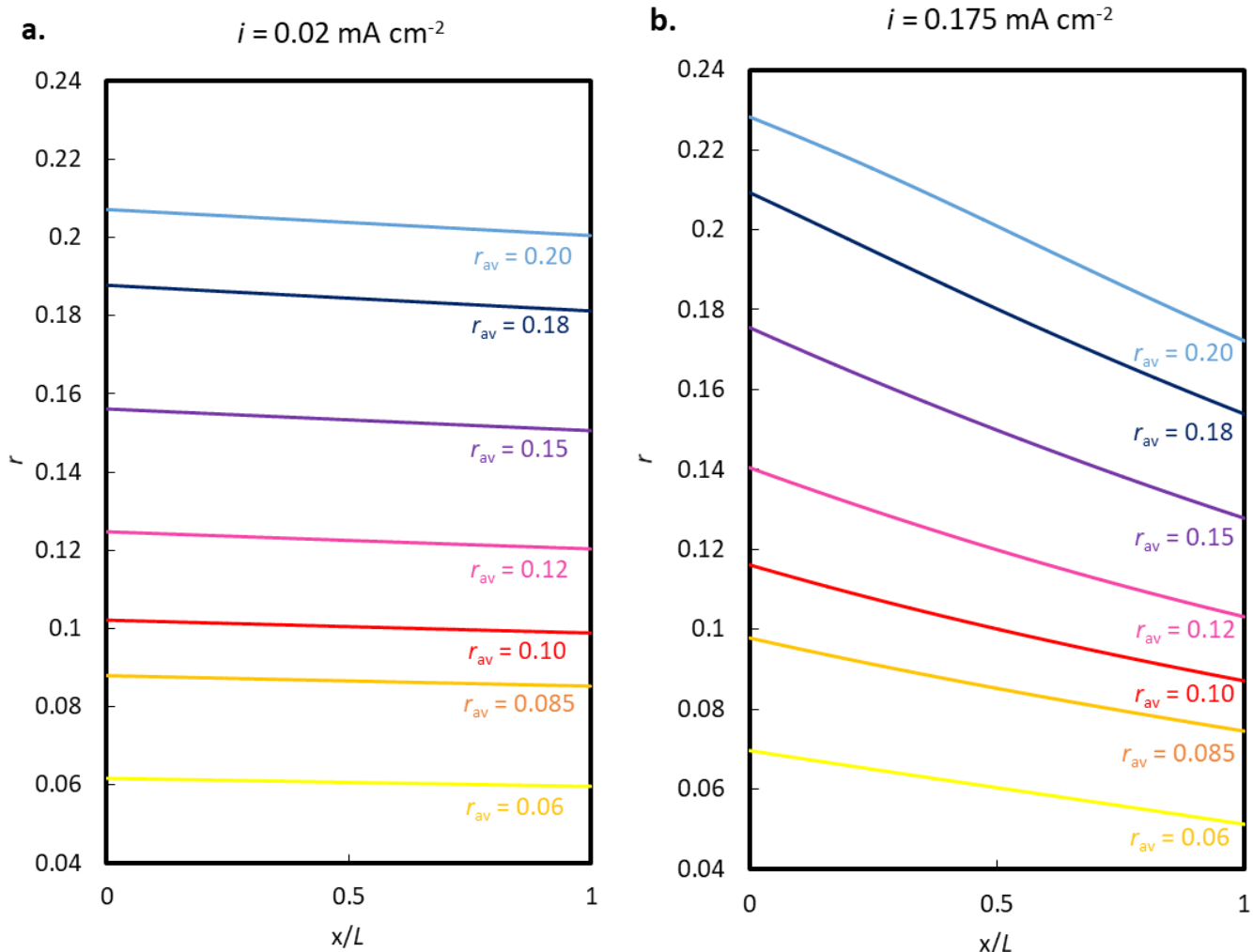
328 The integrand, $J(r)$, is a known function of salt concentration r_{av} . We plot this function in
 329 Figure 6. A polynomial fit was used to calculate the required integral. The dashed curve shows a
 330 polynomial fit of Equation 7:

$$331 \quad J(r) = i ar_{av}^6 + br_{av}^5 + cr_{av}^4 + dr_{av}^3 + er_{av}^2 + fr_{av} + g, \quad \text{Equation 8}$$

332 with fitting parameters $a = -4 \times 10^{-4}$, $b = 4 \times 10^{-4}$, $c = -1 \times 10^{-4}$, $d = 3 \times 10^{-5}$, $e = -3 \times 10^{-6}$, $f = 2 \times$
 333 10^{-7} , and $g = -3 \times 10^{-9}$. Our goal is to establish $r(x)$ for a given value of r_{av} and i . This is achieved

334 by first assuming $r(x = 0)$ and solving for $r(x)$ using Equation 7 for all x from 0^+ to L by
335 numerical integration.

336 Figure 7(a) presents the salt concentration profile at steady state for all salt concentrations at
337 a current density of 0.02 mA cm^{-2} , the current density used during the conditioning cycles. Figure
338 7(b) presents the salt concentration profile at steady state for all salt concentrations at a current
339 density of 0.175 mA cm^{-2} , the current density used during in our study of protrusion growth. For
340 both sets of calculations, the electrolyte thickness was assumed to be 0.005 cm . As expected,
341 increasing current density results in steeper concentration gradients. The magnitude of the
342 gradients also increases with average salt concentration. This is seen more clearly in Figure 7(b).

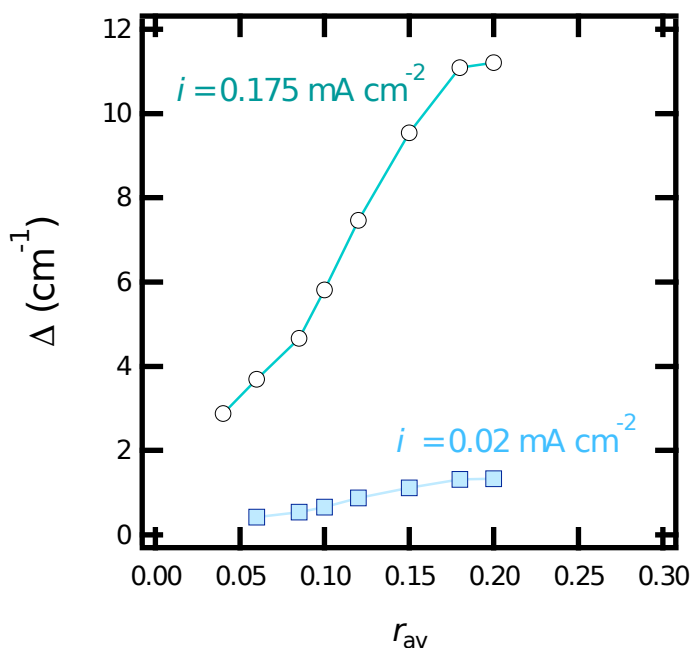


343

344 **Figure 7.** Concentration profiles in SEO electrolytes predicted by concentrated solution theory at
 345 steady-state at 90 °C. (a) Concentration profiles for $i = 0.02 \text{ mA cm}^{-2}$, the current density used
 346 during conditioning cycles. (b) Concentration profiles for $i = 0.175 \text{ mA cm}^{-2}$, the current density
 347 used in our study of protrusion growth during cell cycling. The anode is at $x/L = 0$ and the
 348 cathode is at $x/L = 1$.

349 In order to quantify differences in salt concentration profiles (Figure 7), we define an average
 350 salt concentration gradient, Δ , to be the difference of salt concentration between the anode and
 351 cathode electrodes, divided by the thickness of the cell. Figure 8 presents the calculated salt

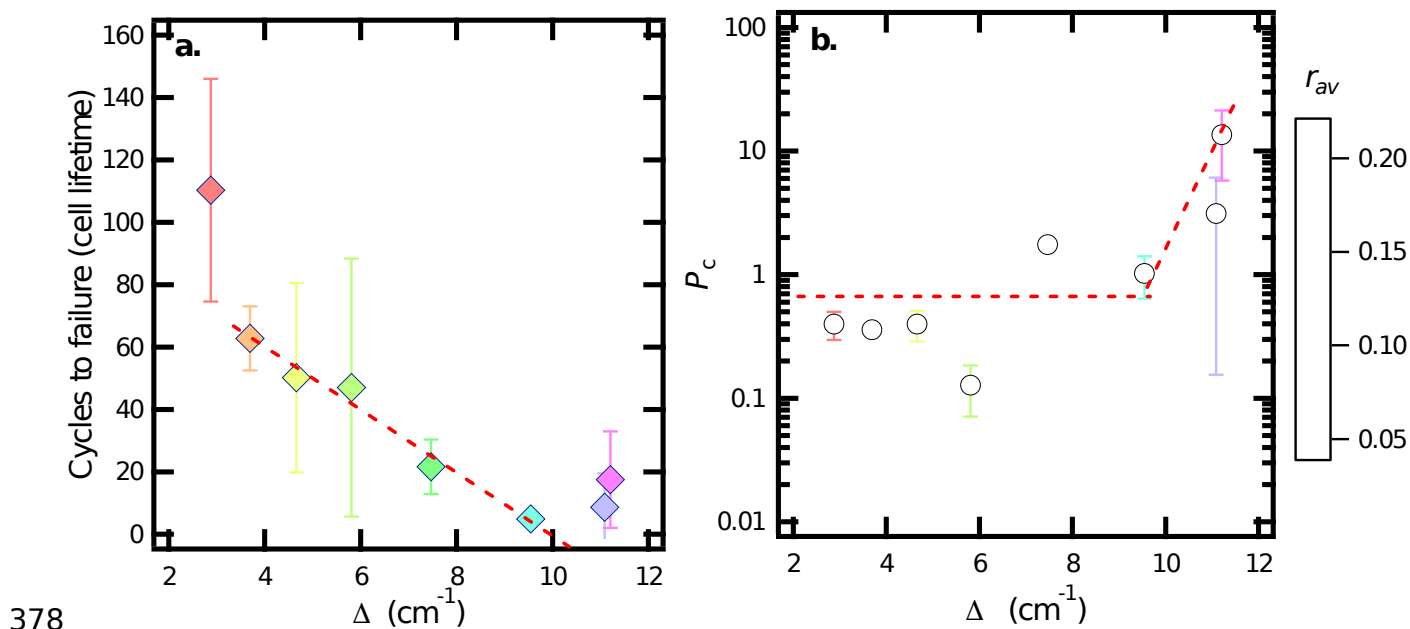
352 concentration gradients as a function of average salt concentration for the two current densities
 353 of interest. During the conditioning cycles (blue squares), salt concentration gradients are small,
 354 varying from 0.4 cm^{-1} for $r_{av} = 0.06$ to 1.3 cm^{-1} for $r_{av} = 0.20$. However, for the higher current
 355 density (turquoise circles), the gradients are large and about 10 times higher than that during the
 356 conditioning cycles. One may use the magnitude of Δ as a measure of the efficacy of an
 357 electrolyte at the current density of interest. The magnitude of the salt concentration gradient to
 358 maintain a current density of $i = 0.175 \text{ mA cm}^{-2}$ increases monotonically with salt concentration.
 359 Many theories[59,60] suggest that lithium dendrite growth is affected by the magnitude of salt
 360 concentration gradients. It is therefore instructive to examine the cycling behavior of our cells as
 361 a function of Δ .



362
 363 **Figure 8.** A plot of average salt concentration gradient at $90 \text{ }^\circ\text{C}$, Δ , defined as the salt
 364 concentration difference between the cathode and the anode normalized by electrolyte thickness,
 365 as a function of the average salt concentration, r_{av} , for current density used in the conditioning

366 cycles at $i = 0.02 \text{ mA cm}^{-2}$ (turquoise circles) and for current density used in our study of
 367 protrusion growth during cell cycling at $i = 0.175 \text{ mA cm}^{-2}$ (blue squares).

368 In Figure 9(a) we plot cell lifetime as a function of Δ . We see a direct correlation between the
 369 two parameters. Cell lifetime decreases precipitously as Δ increases from 2.8 cm^{-1} to 9.5 cm^{-1} .
 370 The average salt concentrations used to obtain each of the data points is indicated using the color
 371 scheme shown on the right. Cell lifetimes obtained at the two highest values of Δ are slightly
 372 higher than that at 9.5 cm^{-1} , an observation that requires further investigation. Nevertheless, the
 373 data in Figure 9(a) indicate that Δ must be significantly less than 9 cm^{-1} for stable cycling of
 374 lithium-lithium symmetric cells. We note in passing that Δ for the conditioning cycles ranges
 375 from 0.4 to 1.3 cm^{-1} . This range is well outside the range of gradients where rapid cell failure is
 376 expected. Planar and stable deposition might be expected in this range as seen by Maslyn *et al.*
 377 [28]



379 **Figure 9.** (a) Cell lifetime (cycles to failure) and (b) average number of defects per cycle, P_c , as a
380 function of salt concentration gradient, Δ at 90 °C. Data points are color-coded according to salt
381 concentration, r_{av} , using the color scale presented on the right. Dashed lines are guides for the
382 eye.

383 An important characteristic of failed cells is the areal density of defects on the electrodes at
384 the point of failure. Since different cells exhibited different lifetimes, it makes sense to examine
385 the average number of defects per cycle P_c , in all of the failed cells. The procedure for
386 quantifying P_c is presented in ref.[29] In Figure 9(b), we plot P_c versus Δ . To a good
387 approximation, P_c is independent of Δ when Δ increases from 2.8 cm⁻¹ to 9.5 cm⁻¹, suggesting
388 that areal defect density in this regime is related to an intrinsic property of lithium metal rather
389 than the applied current. Note that cell lifetime decreases rapidly over the same range of Δ
390 values. In the regime $\Delta > 9.5$ cm⁻¹, P_c increases substantially with Δ , suggesting that defects
391 density in this regime is affected by the applied current. Many of the defects seen at high salt
392 concentration do not protrude significantly into the electrolyte (see Figure S5 in the SI). Since
393 cell-failure requires a protrusion to span the thickness of the electrolyte, our experiments do not
394 shed light on the effect of these defects on cell-failure.

395 CONCLUSION

396 We have studied both the failure of cycled Li/SEO/Li symmetric cells due to the defective
397 electrodeposition of lithium and the formation of lithium protrusions as a function of salt
398 concentration in the SEO electrolyte (r_{av}) at a fixed current density. The SEO electrolyte presents
399 a lamellar morphology at all salt concentrations. We find that the cell lifetime decreases by a
400 factor of 100 when salt concentration in the SEO electrolyte is increased from $r_{av} = 0.04$ to 0.15,

401 and it remains low at the highest salt concentrations tested. The average number of defective
402 deposits on the electrodes is also considerably higher at high salt concentrations. We know that
403 the defective electrodeposition of lithium is controlled by electrochemical and mechanical
404 properties of the electrolyte. Since these properties depend on the morphology of the electrolyte,
405 we first studied the effect of salt on electrolyte morphology. We found no qualitative differences
406 in the morphology as a function of salt concentration. We also found no significant difference in
407 the mechanical properties as a function of r_{av} . The electrochemical properties were quantified by
408 measuring the ionic conductivity, salt diffusion coefficient, transference number, and
409 thermodynamic factor. None of these properties deteriorated rapidly with increasing salt
410 concentration. We used these properties to compute salt concentration profiles in the symmetric
411 cells using Newman's concentrated solution theory. We posit that Δ , the average salt
412 concentration gradient across the electrolyte, governs protrusion growth from a lithium metal
413 cathode through an electrolyte. We show that cell lifetime decreases linearly with Δ .

414 Since the early work by Monroe and Newman,[24,44,45] it has been clear that the growth of
415 lithium protrusions is related to the electrochemical and mechanical properties of the electrolyte.
416 Which of these properties is directly relevant for the observed protrusions has not yet been
417 established. It is common to report parameters such as modulus, conductivity, and transference
418 number. These parameters characterize the linear response of the electrolyte as they are relevant
419 when the electrolyte is slightly perturbed away from equilibrium. The shear modulus describes
420 stress-strain behavior in the limit of infinitesimal strain, conductivity describes the voltage-
421 current relationship in the limit of infinitesimal current densities, and the transference number
422 describes the migration of ions at uniform concentration. In this work, we have shown that cell

423 lifetime and protrusion density are not dependent on these parameters. Instead, we find that cell
424 lifetime and protrusion density appear to be correlated with the concentration gradient, Δ , a
425 parameter that reflects the nonlinear response of the electrolyte to the applied current density
426 used in the cycling experiments. It would be interesting to see if the relationship between lithium
427 protrusion growth and electrochemical properties in different classes of electrolytes can be
428 understood in term of Δ .

429 ASSOCIATED CONTENT

430 The following file is available free of charge.

431 Supplementary Information (PDF)

432 AUTHOR INFORMATION

433 **Corresponding Author**

434 * E-mail: nbalsara@berkeley.edu. Phone: 1-510-642-8973

435 * Address: 201C Gilman Hall, Berkeley, CA 94720

436 **ORCID**

437 Louise Frenck: 0000-0001-7116-2144

438 Vijay D. Veeraraghavan: 0000-0001-7327-7316

439 Jacqueline A. Maslyn: 0000-0002-6481-2070

440 Alexander Müller: 0000-0002-8049-6610

441 Alec S. Ho: 0000-0003-1373-5332

442 Whitney S. Loo: 0000-0002-9773-3571

443 Andrew M. Minor: 0000-0003-3606-8309

444 Nitash P. Balsara: 0000-0002-0106-5565

445

446 **Author Contributions**

447 J.A.M. and W.S.L. synthesized SEO block copolymer. L.F., J.A.M., and V.V. fabricated samples

448 and performed the experiments. A. M. acquired scanning electron micrographs. A.S.H.

449 contributed to calculations. L.F. and N.P.B. prepared figures and composed the manuscript.

450 N.P.B. directed the work.

451 **Notes**

452 The authors declare no competing financial interest.

453 **ACKNOWLEDGMENT**

454 Funding to support this work was provided by the Energy & Biosciences Institute through
455 the EBI-Shell program. J.A.M. was supported by a National Science Foundation Graduate
456 Research Fellowship DGE-2752814. Program. Funding for the electron microscopy work was
457 provided by the Soft Matter Electron Microscopy Program, supported by the Office of Science,
458 Office of Basic Energy Science, U.S. Department of Energy, under Contract No. DEAC02-
459 05CH11231. Work at the Molecular Foundry was supported by the Office of Science, Office of
460 Basic Energy Sciences, of the U.S. Department of Energy under Contract No. DE-AC02-
461 05CH11231. A.S.H. was supported by the Vehicle Technologies Office of the U.S. Department
462 of Energy's Office of Energy Efficiency and Renewable Energy under the guidance of the
463 Advanced Battery Cell Research Program (eXtreme fast charge Cell Evaluation of Lithium-ion
464 batteries, XCEL). W.S.L. was supported by a National Science Foundation Graduate Research
465 Fellowship DGE-1106400. We acknowledge helpful discussions with Dr. Ryan Stephens of
466 Shell International Exploration and Production Inc, Houston.

467

468

469 **LIST OF SYMBOLS**

470 C_d , Charge density passed (C.cm⁻²); Δ , salt concentration gradient; d , Domain spacing (nm); D ,
471 restricted salt diffusion coefficient; $\frac{dU}{d\ln m}$, change in the open circuit potential; ΔV , potential
472 applied (V); F , Faraday constant (G' , Storage shear modulus; G'' , loss shear modulus; i ,

473 Applied current density (mA cm^{-2}); i_0 , measured initial current (A); i_Ω , calculated initial current
474 (A); κ_b , ionic conductivity from measurements with blocking electrodes (S.cm^{-1}); κ_{nb} , ionic
475 conductivity from measurements with non-blocking electrodes (S cm^{-1}); L , electrolyte thickness;
476 Li , Lithium; $Li\text{-ion}$, Lithium-ion battery; $LiTFSI$, Lithium bis (trifluoromethanesulfonyl) imide;
477 m , molality (mol kg^{-1}); NMP , N-methylpyrrolidone; ρ_+ , steady-state current fraction; ϕ_c ,
478 volume fraction of the conducting phase; P_c , average number of defects per cycle; PEO ,
479 Poly(ethylene oxide); PS , Polystyrene; R , gas constant ($\text{J mol}^{-1} \text{K}^{-1}$); r_{av} , Average salt
480 concentration; $R_{b,0}$, initial bulk resistance (Ω); $R_{i,0}$, initial interfacial resistance (Ω); $R_{i,ss}$,
481 interfacial resistance at steady state (Ω); SEI , Solid Electrolyte Interphase; SEO , Polystyrene-*b*-
482 poly(ethylene) oxide; T , temperature; t_{+i} , cation transference number; t_{-i} , anion transference
483 number; T_f , thermodynamic factor; U , open-circuit voltage (V); v_{+i} , number of cations for
484 LiTFSI; z_{+i} , the charge number for LiTFSI.

485

486 REFERENCES

- 487 [1] J. Yamaki, S. Tobishima, K. Hayashi, Keiichi Saito, Y. Nemoto, M. Arakawa, A
488 consideration of the morphology of electrochemically deposited lithium in an organic
489 electrolyte, *Journal of Power Sources*. 74 (1998) 219–227. [https://doi.org/10.1016/S0378-](https://doi.org/10.1016/S0378-7753(98)00067-6)
490 [7753\(98\)00067-6](https://doi.org/10.1016/S0378-7753(98)00067-6).
491 [2] Y. Takeda, O. Yamamoto, N. Imanishi, Lithium Dendrite Formation on a Lithium Metal
492 Anode from Liquid, Polymer and Solid Electrolytes, *Electrochemistry*. 84 (2016) 210–218.
493 <https://doi.org/10.5796/electrochemistry.84.210>.
494 [3] K.N. Wood, E. Kazyak, A.F. Chadwick, K.-H. Chen, J.-G. Zhang, K. Thornton, N.P.
495 Dasgupta, Dendrites and Pits: Untangling the Complex Behavior of Lithium Metal Anodes
496 through Operando Video Microscopy, *ACS Cent. Sci.* 2 (2016) 790–801.
497 <https://doi.org/10.1021/acscentsci.6b00260>.
498 [4] E.J. Cheng, A. Sharafi, J. Sakamoto, Intergranular Li metal propagation through
499 polycrystalline $\text{Li}_{6.25}\text{Al}_{10.25}\text{La}_3\text{Zr}_{20}\text{O}_{12}$ ceramic electrolyte, *Electrochimica Acta*. 223
500 (2017) 85–91. <https://doi.org/10.1016/j.electacta.2016.12.018>.
501 [5] L. Frenck, G.K. Sethi, J.A. Maslyn, N.P. Balsara, Factors That Control the Formation of
502 Dendrites and Other Morphologies on Lithium Metal Anodes, *Front. Energy Res.* 7 (2019).
503 <https://doi.org/10.3389/fenrg.2019.00115>.

- 504 [6] M.M. Thackeray, C. Wolverton, E.D. Isaacs, Electrical energy storage for transportation—
505 approaching the limits of, and going beyond, lithium-ion batteries, *Energy Environ. Sci.* 5
506 (2012) 7854–7863. <https://doi.org/10.1039/C2EE21892E>.
- 507 [7] D. Aurbach, E. Zinigrad, Y. Cohen, H. Teller, A short review of failure mechanisms of
508 lithium metal and lithiated graphite anodes in liquid electrolyte solutions, *Solid State Ionics*.
509 148 (2002) 405–416. [https://doi.org/10.1016/S0167-2738\(02\)00080-2](https://doi.org/10.1016/S0167-2738(02)00080-2).
- 510 [8] P.G. Bruce, S.A. Freunberger, L.J. Hardwick, J.-M. Tarascon, Li–O₂ and Li–S batteries
511 with high energy storage, *Nature Materials*. 11 (2012) 19–29.
512 <https://doi.org/10.1038/nmat3191>.
- 513 [9] D. Lin, Y. Liu, Y. Cui, Reviving the lithium metal anode for high-energy batteries, *Nature*
514 *Nanotechnology*. 12 (2017) 194–206. <https://doi.org/10.1038/nnano.2017.16>.
- 515 [10] K.N. Wood, M. Noked, N.P. Dasgupta, Lithium Metal Anodes: Toward an Improved
516 Understanding of Coupled Morphological, Electrochemical, and Mechanical Behavior,
517 *ACS Energy Lett.* 2 (2017) 664–672. <https://doi.org/10.1021/acsenerylett.6b00650>.
- 518 [11] C. Brissot, M. Rosso, J.-N. Chazalviel, S. Lascaud, Dendritic growth mechanisms in
519 lithium/polymer cells, *Journal of Power Sources*. 81–82 (1999) 925–929.
520 [https://doi.org/10.1016/S0378-7753\(98\)00242-0](https://doi.org/10.1016/S0378-7753(98)00242-0).
- 521 [12] C. Brissot, M. Rosso, J.-N. Chazalviel, P. Baudry, S. Lascaud, In situ study of dendritic
522 growth in lithium/PEO-salt/lithium cells, *Electrochimica Acta*. 43 (1998) 1569–1574.
523 [https://doi.org/10.1016/S0013-4686\(97\)10055-X](https://doi.org/10.1016/S0013-4686(97)10055-X).
- 524 [13] A. Teyssot, C. Belhomme, R. Bouchet, M. Rosso, S. Lascaud, M. Armand, Inter-electrode
525 in situ concentration cartography in lithium/polymer electrolyte/lithium cells, *Journal of*
526 *Electroanalytical Chemistry*. 584 (2005) 70–74.
527 <https://doi.org/10.1016/j.jelechem.2005.01.037>.
- 528 [14] M. Rosso, J.-N. Chazalviel, E. Chassaing, Calculation of the space charge in
529 electrodeposition from a binary electrolyte, *Journal of Electroanalytical Chemistry*. 587
530 (2006) 323–328. <https://doi.org/10.1016/j.jelechem.2005.11.030>.
- 531 [15] P. Barai, K. Higa, V. Srinivasan, Effect of Initial State of Lithium on the Propensity for
532 Dendrite Formation: A Theoretical Study, *J. Electrochem. Soc.* 164 (2017) A180–A189.
533 <https://doi.org/10.1149/2.0661702jes>.
- 534 [16] P. Barai, K. Higa, V. Srinivasan, Impact of External Pressure and Electrolyte Transport
535 Properties on Lithium Dendrite Growth, *J. Electrochem. Soc.* 165 (2018) A2654–A2666.
536 <https://doi.org/10.1149/2.0651811jes>.
- 537 [17] J.-M. Tarascon, M. Armand, Issues and challenges facing rechargeable lithium batteries,
538 *Nature*. (2001). <https://doi.org/10.1038/35104644>.
- 539 [18] A. Lisowska-Oleksiak, The interface between lithium and poly(ethylene-oxide), *Solid State*
540 *Ionics*. 119 (1999) 205–209. [https://doi.org/10.1016/S0167-2738\(98\)00504-9](https://doi.org/10.1016/S0167-2738(98)00504-9).
- 541 [19] M. Armand, The history of polymer electrolytes, *Solid State Ionics*. 69 (1994) 309–319.
542 [https://doi.org/10.1016/0167-2738\(94\)90419-7](https://doi.org/10.1016/0167-2738(94)90419-7).
- 543 [20] R. Bouchet, S. Maria, R. Meziane, A. Aboulaich, L. Lienafa, J.-P. Bonnet, T.N.T. Phan, D.
544 Bertin, D. Gigmes, D. Devaux, R. Denoyel, M. Armand, Single-ion BAB triblock
545 copolymers as highly efficient electrolytes for lithium-metal batteries, *Nature Materials*. 12
546 (2013) 452–457. <https://doi.org/10.1038/nmat3602>.

- 547 [21] D. Xu, B. Wang, Q. Wang, S. Gu, W. Li, J. Jin, C. Chen, Z. Wen, High-Strength Internal
548 Cross-Linking Bacterial Cellulose-Network-Based Gel Polymer Electrolyte for Dendrite-
549 Suppressing and High-Rate Lithium Batteries, *ACS Appl. Mater. Interfaces*. 10 (2018)
550 17809–17819. <https://doi.org/10.1021/acsami.8b00034>.
- 551 [22] D. Li, L. Chen, T. Wang, L.-Z. Fan, 3D Fiber-Network-Reinforced Bicontinuous
552 Composite Solid Electrolyte for Dendrite-free Lithium Metal Batteries, *ACS Appl. Mater.*
553 *Interfaces*. 10 (2018) 7069–7078. <https://doi.org/10.1021/acsami.7b18123>.
- 554 [23] J. Hu, J. Tian, C. Li, Nanostructured Carbon Nitride Polymer-Reinforced Electrolyte To
555 Enable Dendrite-Suppressed Lithium Metal Batteries, *ACS Appl. Mater. Interfaces*. 9
556 (2017) 11615–11625. <https://doi.org/10.1021/acsami.7b00478>.
- 557 [24] C. Monroe, J. Newman, Dendrite Growth in Lithium/Polymer Systems A Propagation
558 Model for Liquid Electrolytes under Galvanostatic Conditions, *J. Electrochem. Soc.* 150
559 (2003) A1377–A1384. <https://doi.org/10.1149/1.1606686>.
- 560 [25] Y. Yamada, M. Yaegashi, T. Abe, A. Yamada, A superconcentrated ether electrolyte for
561 fast-charging Li-ion batteries, *Chem. Commun.* 49 (2013) 11194–11196.
562 <https://doi.org/10.1039/C3CC46665E>.
- 563 [26] Y. Yamada, J. Wang, S. Ko, E. Watanabe, A. Yamada, Advances and issues in developing
564 salt-concentrated battery electrolytes, *Nature Energy*. 4 (2019) 269–280.
565 <https://doi.org/10.1038/s41560-019-0336-z>.
- 566 [27] N.S. Schauer, K.J. Harry, D.Y. Parkinson, H. Watanabe, N.P. Balsara, Lithium Dendrite
567 Growth in Glassy and Rubbery Nanostructured Block Copolymer Electrolytes, *J.*
568 *Electrochem. Soc.* 162 (2015) A398–A405. <https://doi.org/10.1149/2.0511503jes>.
- 569 [28] J.A. Maslyn, W.S. Loo, K.D. McEntush, H.J. Oh, K.J. Harry, D.Y. Parkinson, N.P. Balsara,
570 Growth of Lithium Dendrites and Globules through a Solid Block Copolymer Electrolyte as
571 a Function of Current Density, *J. Phys. Chem. C*. 122 (2018) 26797–26804. [https://doi.org/](https://doi.org/10.1021/acs.jpcc.8b06355)
572 [10.1021/acs.jpcc.8b06355](https://doi.org/10.1021/acs.jpcc.8b06355).
- 573 [29] L. Frenck, J.A. Maslyn, W.S. Loo, D.Y. Parkinson, N.P. Balsara, Impact of Salt
574 Concentration on Nonuniform Lithium Electrodeposition through Rigid Block Copolymer
575 Electrolytes, *ACS Appl. Mater. Interfaces*. (2019). <https://doi.org/10.1021/acsami.9b15606>.
- 576 [30] Newman, J.; Thomas-Alya, K. E., *Electrochemical Systems, 3rd Edition | Wiley, 2004.*
- 577 [31] D.M. Pesko, Z. Feng, S. Sawhney, J. Newman, V. Srinivasan, N.P. Balsara, Comparing
578 Cycling Characteristics of Symmetric Lithium-Polymer-Lithium Cells with Theoretical
579 Predictions, *J. Electrochem. Soc.* 165 (2018) A3186–A3194.
580 <https://doi.org/10.1149/2.0921813jes>.
- 581 [32] P.G. Bruce, C.A. Vincent, Polymer electrolytes, *J. Chem. Soc., Faraday Trans.* 89 (1993)
582 3187–3203. <https://doi.org/10.1039/FT9938903187>.
- 583 [33] M. Singh, O. Odusanya, G.M. Wilmes, H.B. Eitouni, E.D. Gomez, A.J. Patel, V.L. Chen,
584 M.J. Park, P. Fragouli, H. Iatrou, N. Hadjichristidis, D. Cookson, N.P. Balsara, Effect of
585 Molecular Weight on the Mechanical and Electrical Properties of Block Copolymer
586 Electrolytes, *Macromolecules*. 40 (2007) 4578–4585. <https://doi.org/10.1021/ma0629541>.
- 587 [34] S.A. Mullin, G.M. Stone, A. Panday, N.P. Balsara, Salt Diffusion Coefficients in Block
588 Copolymer Electrolytes, *J. Electrochem. Soc.* 158 (2011) A619–A627.
589 <https://doi.org/10.1149/1.3563802>.

- 590 [35] K.J. Harry, D.T. Hallinan, D.Y. Parkinson, A.A. MacDowell, N.P. Balsara, Detection of
591 subsurface structures underneath dendrites formed on cycled lithium metal electrodes,
592 *Nature Materials*. 13 (2014) 69–73. <https://doi.org/10.1038/nmat3793>.
- 593 [36] K.J. Harry, X. Liao, D.Y. Parkinson, A.M. Minor, N.P. Balsara, Electrochemical
594 Deposition and Stripping Behavior of Lithium Metal across a Rigid Block Copolymer
595 Electrolyte Membrane, *J. Electrochem. Soc.* 162 (2015) A2699–A2706.
596 <https://doi.org/10.1149/2.0321514jes>.
- 597 [37] K.J. Harry, K. Higa, V. Srinivasan, N.P. Balsara, Influence of Electrolyte Modulus on the
598 Local Current Density at a Dendrite Tip on a Lithium Metal Electrode, *J. Electrochem. Soc.*
599 163 (2016) A2216–A2224. <https://doi.org/10.1149/2.0191610jes>.
- 600 [38] P.G. Bruce, C.A. Vincent, Steady state current flow in solid binary electrolyte cells, *Journal*
601 *of Electroanalytical Chemistry and Interfacial Electrochemistry*. 225 (1987) 1–17.
602 [https://doi.org/10.1016/0022-0728\(87\)80001-3](https://doi.org/10.1016/0022-0728(87)80001-3).
- 603 [39] M.D. Galluzzo, J.A. Maslyn, D.B. Shah, N.P. Balsara, Ohm’s law for ion conduction in
604 lithium and beyond-lithium battery electrolytes, *J. Chem. Phys.* 151 (2019) 020901. <https://doi.org/10.1063/1.5109684>.
- 605
- 606 [40] E.W. Cochran, C.J. Garcia-Cervera, G.H. Fredrickson, Stability of the Gyroid Phase in
607 Diblock Copolymers at Strong Segregation, *Macromolecules*. 39 (2006) 2449–2451. <https://doi.org/10.1021/ma0527707>.
- 608
- 609 [41] F.S. Bates, J.H. Rosedale, G.H. Fredrickson, Fluctuation effects in a symmetric diblock
610 copolymer near the order–disorder transition, *J. Chem. Phys.* 92 (1990) 6255–6270. <https://doi.org/10.1063/1.458350>.
- 611
- 612 [42] A. Panday, S. Mullin, E.D. Gomez, N. Wanakule, V.L. Chen, A. Hexemer, J. Pople, N.P.
613 Balsara, Effect of Molecular Weight and Salt Concentration on Conductivity of Block
614 Copolymer Electrolytes, *Macromolecules*. 42 (2009) 4632–4637.
615 <https://doi.org/10.1021/ma900451e>.
- 616 [43] G.M. Stone, S.A. Mullin, A.A. Teran, D.T. Hallinan, A.M. Minor, A. Hexemer, N.P.
617 Balsara, Resolution of the Modulus versus Adhesion Dilemma in Solid Polymer
618 Electrolytes for Rechargeable Lithium Metal Batteries, *J. Electrochem. Soc.* 159 (2012)
619 A222–A227. <https://doi.org/10.1149/2.030203jes>.
- 620 [44] C. Monroe, J. Newman, The Effect of Interfacial Deformation on Electrodeposition
621 Kinetics, *J. Electrochem. Soc.* 151 (2004) A880–A886. <https://doi.org/10.1149/1.1710893>.
- 622 [45] C. Monroe, J. Newman, The Impact of Elastic Deformation on Deposition Kinetics at
623 Lithium/Polymer Interfaces, *J. Electrochem. Soc.* 152 (2005) A396–A404.
624 <https://doi.org/10.1149/1.1850854>.
- 625 [46] Y. Ma, M. Doyle, T.F. Fuller, M.M. Doeff, L.C.D. Jonghe, J. Newman, The Measurement
626 of a Complete Set of Transport Properties for a Concentrated Solid Polymer Electrolyte
627 Solution, *J. Electrochem. Soc.* 142 (1995) 1859–1868. <https://doi.org/10.1149/1.2044206>.
- 628 [47] K.I.S. Mongcopa, M. Tyagi, J.P. Mailoa, G. Samsonidze, B. Kozinsky, S.A. Mullin, D.A.
629 Gribble, H. Watanabe, N.P. Balsara, Relationship between Segmental Dynamics Measured
630 by Quasi-Elastic Neutron Scattering and Conductivity in Polymer Electrolytes, *ACS Macro*
631 *Lett.* 7 (2018) 504–508. <https://doi.org/10.1021/acsmacrolett.8b00159>.
- 632 [48] I. Villaluenga, D.M. Pesko, K. Timachova, Z. Feng, J. Newman, V. Srinivasan, N.P.
633 Balsara, Negative Stefan-Maxwell Diffusion Coefficients and Complete Electrochemical

634 Transport Characterization of Homopolymer and Block Copolymer Electrolytes, *J.*
635 *Electrochem. Soc.* 165 (2018) A2766–A2773. <https://doi.org/10.1149/2.0641811jes>.
636 [49] W.-S. Young, W.-F. Kuan, T.H. Epps, Block copolymer electrolytes for rechargeable
637 lithium batteries, *Journal of Polymer Science Part B: Polymer Physics.* 52 (2014) 1–16.
638 <https://doi.org/10.1002/polb.23404>.
639 [50] W.-S. Young, T.H. Epps, Ionic Conductivities of Block Copolymer Electrolytes with
640 Various Conducting Pathways: Sample Preparation and Processing Considerations,
641 *Macromolecules.* 45 (2012) 4689–4697. <https://doi.org/10.1021/ma300362f>.
642 [51] Y. Gu, S. Zhang, L. Martinetti, K.H. Lee, L.D. McIntosh, C.D. Frisbie, T.P. Lodge, High
643 Toughness, High Conductivity Ion Gels by Sequential Triblock Copolymer Self-Assembly
644 and Chemical Cross-Linking, *J. Am. Chem. Soc.* 135 (2013) 9652–9655.
645 <https://doi.org/10.1021/ja4051394>.
646 [52] M.D. Galluzzo, W.S. Loo, A.A. Wang, A. Walton, J.A. Maslyn, N.P. Balsara,
647 Measurement of Three Transport Coefficients and the Thermodynamic Factor in Block
648 Copolymer Electrolytes with Different Morphologies, *J. Phys. Chem. B.* (2020).
649 <https://doi.org/10.1021/acs.jpcc.9b11066>.
650 [53] Q. Zheng, D.M. Pesko, B.M. Savoie, K. Timachova, A.L. Hasan, M.C. Smith, T.F. Miller,
651 G.W. Coates, N.P. Balsara, Optimizing Ion Transport in Polyether-Based Electrolytes for
652 Lithium Batteries, *Macromolecules.* 51 (2018) 2847–2858.
653 <https://doi.org/10.1021/acs.macromol.7b02706>.
654 [54] Y. Tominaga, K. Yamazaki, V. Nanthana, Effect of Anions on Lithium Ion Conduction in
655 Poly(ethylene carbonate)-based Polymer Electrolytes, *J. Electrochem. Soc.* 162 (2015)
656 A3133–A3136. <https://doi.org/10.1149/2.0211502jes>.
657 [55] D.B. Shah, K.R. Olson, A. Karny, S.J. Mecham, J.M. DeSimone, N.P. Balsara, Effect of
658 Anion Size on Conductivity and Transference Number of Perfluoroether Electrolytes with
659 Lithium Salts, *J. Electrochem. Soc.* 164 (2017) A3511–A3517.
660 <https://doi.org/10.1149/2.0301714jes>.
661 [56] N.P. Balsara, J. Newman, Relationship between Steady-State Current in Symmetric Cells
662 and Transference Number of Electrolytes Comprising Univalent and Multivalent Ions, *J.*
663 *Electrochem. Soc.* 162 (2015) A2720–A2722. <https://doi.org/10.1149/2.0651514jes>.
664 [57] D.M. Pesko, K. Timachova, R. Bhattacharya, M.C. Smith, I. Villaluenga, J. Newman, N.P.
665 Balsara, Negative Transference Numbers in Poly(ethylene oxide)-Based Electrolytes, *J.*
666 *Electrochem. Soc.* 164 (2017) E3569–E3575. <https://doi.org/10.1149/2.0581711jes>.
667 [58] P. Barai, K. Higa, V. Srinivasan, Lithium dendrite growth mechanisms in polymer
668 electrolytes and prevention strategies, *Phys. Chem. Chem. Phys.* 19 (2017) 20493–20505.
669 <https://doi.org/10.1039/C7CP03304D>.
670 [59] J.-N. Chazalviel, Electrochemical aspects of the generation of ramified metallic
671 electrodeposits, *Phys. Rev. A.* 42 (1990) 7355–7367.
672 <https://doi.org/10.1103/PhysRevA.42.7355>.
673 [60] Barton J. L., Bockris J. O' m., Ubbelohde Alfred Rene Jean Paul, The electrolytic growth of
674 dendrites from ionic solutions, *Proceedings of the Royal Society of London. Series A.*
675 *Mathematical and Physical Sciences.* 268 (1962) 485–505.
676 <https://doi.org/10.1098/rspa.1962.0154>.
677

