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Analysis of the cloud enhancement phenomenon and its effects on photovoltaic generators based on cloud speed sensor measurements

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1 Analysis of the cloud enhancement phenomenon and its effects on photovoltaic

- 2 generators based on cloud speed sensor measurements
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11 Abstract

12

13 The irradiance incident on photovoltaic (PV) generators can considerably exceed the expected 14 clear sky irradiance. Due to this phenomenon, called cloud enhancement (CE), the maximum power 15 of the PV generator can exceed the rated power of the inverter connecting the generator to grid. CE 16 event characteristics and the effects of CE on the electrical operation of PV generators were studied 17 based on measured irradiances and cloud edge velocities. Over eleven months in San Diego, 18 California, the highest measured peak irradiance was 1466 W/m₂. In addition, the highest simulated 19 average irradiances for up to 1 MW generators were over 1400 W/m2. The largest lengths for CE 20 events exceeding 1000 W/m² were multiple kilometers. These results indicate that even large utility-21 scale PV power plants can be affected significantly by CE events. Moreover, the operation of three 22 PV plants was simulated during around 2400 measured CE events with a detailed spatio-temporal 23 model down to a PV submodule. The effects of inverter sizing on the operation of the plants were also studied and the negative impacts of CE on the operation of PV systems were shown to increase 24 25 with increasing DC/AC ratio. The operating voltage increased with increasing DC/AC ratio and 26 decreasing plant size and the highest operating voltages were 25% higher than nominal. During the 27 CE events, the energy losses due to power curtailment were from 5% to 50% of the available energy production increasing with increasing DC/AC ratio. While CE affects the operation of the PV plants, 28 29 these effects were small in terms of aggregate energy, since CE events that most strongly impact PV 30 system operation are very rare, meaning that CE do not cause major problems for the operation of PV 31 systems.

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33 **1. Introduction**

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The operation of photovoltaic (PV) generators depends on the irradiance incident on the PV cells of the generator. While solar radiation is variable (Tomson, 2013; Lappalainen and Valkealahti, 2015), the nominal electrical characteristics of PV modules are typically defined under the standard test conditions (STC), i.e., at an irradiance of 1000 W/m2 and a cell temperature of 25 °C. However, these conditions are rare in practice. In many parts of the world, clear sky irradiance, i.e., the global irradiance from cloudless sky, can be higher than the STC irradiance around solar noon (Badescu, 1997). Moreover, on partly cloudy days, irradiance can considerably exceed the expected clear sky 42 irradiance due to a phenomenon called cloud enhancement (CE), irradiance enhancement (Pecenak
43 et al., 2016) or overirradiance (Yordanov et al., 2013a).

44 Irradiance levels exceeding 1000 W/m2 (depending on module temperature) can cause the 45 actual power of the generator to exceed its nominal maximum power. Zehner et al. (2011) reported up to 30% higher power output of PV modules under high irradiance conditions compared to the STC. 46 47 High irradiance conditions can lead to the maximum PV power exceeding the maximum DC power 48 of the inverter connecting the PV generator to grid. Moreover, PV capacity is typically oversized such 49 that the nominal DC power of the PV generator is higher than the inverter nominal (AC) power (Wang et al., 2018). If the maximum power of the PV generator is higher than the maximum DC power of 50 51 the inverter, the inverter will operate in power limiting mode: By moving the inverter operating point 52 to higher voltages than those at the global maximum power point (MPP) of the generator, the current 53 and power of the inverter decrease.

In addition to the loss of available energy production, operating in power limiting mode negatively effects the operation and efficiency of the inverter: (i) The efficiency of some inverters decreases with increasing DC side voltage (Rampinelli et al., 2014) causing further losses in AC power output. (ii) The inverter capacitor lifetime shortens with increasing DC voltage (Hasegawa et al., 2018; Callegari et al., 2019). (iii) Under extreme conditions the voltage required to reduce output power may be outside the allowed voltage range of the inverter.

60 Under clear sky conditions, irradiances exceeding 1000 W/m2 are typically not an issue as the 61 exceedance is less than 10% in most areas of the world (except for high altitudes) and PV efficiency 62 losses due to high panel temperature typically far exceed 10% compared to PV efficiency at 25 °C. However, during CE irradiance can be much larger and PV temperatures are typically lower. 63 64 Gueymard (2017a) postulated that there are three types of CE effects that can strongly increase global 65 horizontal irradiance (GHI): 1) the traditional explanation of CE phenomenon: the enhancement of 66 irradiance due to cloud edges near the solar disk; 2) increase of diffuse horizontal irradiance under a 67 homogenous cloud deck before and after a CE event; and 3) partial obscuration of the sun by a thin cloud layer, while most of the sky is covered by bright clouds. In type 3, the share of diffuse irradiance 68 69 is large while the amount of direct horizontal irradiance is much lower than in types 1 and 2. Yordanov 70 et al. (2013a) demonstrated that the strongest CE is due to strong forward scattering within a small 71 angle around the solar disk. That kind of a situation may occur when the sun appears in a narrow gap 72 between clouds within 5° around the solar disk, which are thin enough to strongly forward scatter. 73 Increases over 1000 W/m2 can be substantial: Gueymard (2017b) measured global tilted irradiance 74 (GTI) of almost 2.0 kW/m₂ for a 40° tilt angle and GHI of almost 1.9 kW/m₂ in Colorado at 1829 m 75 elevation, Nascimento et al. (2019) reported GHI of over 1.8 kW/m2 at elevations of 392 m and 32 m 76 in Brazil and Yordanov et al. (2015) measured GTI of 1.6 kW/m2 near sea level at a latitude close to 77 60°N.

Although CE is well-known phenomenon, its characteristics relevant to the operation of PV systems, such as duration and spatial extent, have not received much attention. The durations of CE events were studied in some articles: Yordanov et al. (2013a) presented duration distributions for CE events exceeding 1100 W/m2; Zhang et al. (2018) studied the duration of CE events exceeding clear sky irradiance; and Järvelä et al. (2020) studied the duration of CE events with various irradiance limits over the land area of various PV generators. Järvelä et al. (2018, 2020) studied the land area lengths of CE events in Finland based on irradiance measurements and by invoking Taylor's hypothesis. They found typical CE event lengths to be on the order of hundreds of meters. Espinosa-Gavira et al. (2018) showed that CE can extend over land areas of 15×15 m. Weigl et al. (2012) showed that the land areas of CE events can be large enough to affect the operation of utility-scale PV power plants.

The effects of CE on the operation of PV systems have been studied in few articles: Zehner et al. (2011) studied the operation of individual PV modules under CE; Luoma et al. (2012) studied inverter sizing and energy losses due to inverter saturation under CE; Weigl et al. (2012) studied the operation of PV systems under a single CE situation; and Nascimento et al. (2019) studied the effects of CE events on the performance of PV generators focusing mainly on combiner box fuses. Tapakis and Charalambides (2014) discussed the possible effects of CE on PV inverters.

This article presents a study of CE event characteristics and the effects of CE on the electrical 95 96 operation of PV generators. The study is based on measurements of GHI and cloud edge velocity 97 from San Diego, California. First, the number, duration, and land area length of CE events exceeding 98 various irradiance limits over the land areas of various PV generators are studied. After that, the 99 operation of three PV plants, ranging from 20 to 200 kW, is simulated during around 2400 measured 100 CE events exceeding 1000 W/m2. Moreover, the effects of inverter sizing on the operation of the PV 101 plants are studied. The main novelty of this study is that, for the first time, the detailed (down to the 102 submodule) electrical operation of PV generators is extensively studied under CE based on actual 103 irradiance measurements.

The rest of this article is organized as follows. Sections 2.1–2.4 introduce the measurement data and the methods used to study the characteristics of CE events in terms of irradiance. The results of these studies are presented in Sections 2.5–2.7. The methods used to study the effects of CE on the operation of PV generators are presented in Sections 3.1 and 3.2. Section 3.3 illustrates the effects of CE on the operation of PV generators by two static example CE situations. The statistics during all the CE events identified in measured irradiance are presented in Section 3.4. The results are further discussed in Section 4 and the conclusions are given in Section 5.

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112 **2. Cloud enhancement events**

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In this section, characteristics of CE events are studied in terms of irradiance magnitudes, enhancement durations, and for point irradiance as well as the estimated average irradiances of various PV generator land areas. This section investigates how often and how long typical land areas of different PV generator sizes experience CE.

- 118
- 119 2.1. Measurement data
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The study is based on measurement data of a GHI sensor (LI-200, LI-COR Inc., USA) and a cloud speed sensor (CSS) installed on the rooftop of the EBU2 building at the University of California, San Diego (UCSD) (32°52'53"N, 117°13'59"W). The GHI measurements were performed with a sampling frequency of 0.5 Hz while the response time of the sensor is 10 μs. The CSS, presented in Fig. 1, consists of an array of nine phototransistors (TEPT4400, Vishay Intertechnology)

126 Inc., USA) (Wang et al., 2016). The phototransistors form a circular sector with a radius of 29.7 cm and a central angle of 105°. Eight of the phototransistors are located at the arc of the circular sector 127 128 around the ninth phototransistor that is positioned at the center of the circle. The data acquisition rate 129 of the CSS is irregular since it requires cloud edge passages to determine cloud motion vectors (CMVs). The minimum time between produced CMVs is 11 s, which is sufficient for cloud motion 130 estimation in the scope of this study. The procedure to calculate CMVs is presented in the Appendix. 131 The shadow movement direction is defined as direction where clouds come from relative to north. 132 133 CMVs were determined during 62 days from October 2017 to August 2018 from which also GHI 134 measurements were available. All these days, which compose the used dataset, were partially cloudy. 135



136 137 138

Fig. 1. Cloud speed sensor contained in an enclosure.

139 2.2. Identification of cloud enhancement events

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141 A CE event is often defined by comparing measured irradiance to expected clear sky 142 irradiance (Yordanov et al., 2015; Zhang et al., 2018). In that way, a CE event starts when the 143 irradiance exceeds the clear sky irradiance and ends when the irradiance decreases below the clear 144 sky irradiance. However, from PV system operation point of view, a more sensible way is to use a static irradiance value as a reference instead of the clear-sky irradiance that is location-specific. On 145 146 the other hand, the use of a static irradiance value as the limit of CE events has the drawback that, depending on the location, non-CE events with large clear sky irradiance may be included, or 147 148 situations with real CE during small clear sky irradiance that do not reach the static threshold may be 149 excluded from the study. A typical static value used to define CE events is the solar constant (Zhang et al., 2018). However, the use of solar constant is not justified from the PV power operation point of 150 view. Since the nominal ratings of PV modules are typically defined under STC, from PV system 151 152 operation point of view, a more reasonable choice for a static threshold is the STC irradiance of 1000 W/m₂. To make the results more generalizable, instead of using a single static irradiance limit, 153 we opted to use a continuous range of irradiance values starting from 1000 W/m2 and identified all 154 events where the measured irradiance, or estimated average irradiance, exceeded the irradiance limit. 155 156 Then, we systematically counted the numbers and durations of these events for each irradiance limit. 157

158 2.3. PV generator land areas

160 Average irradiances over the land areas of various PV generators were estimated. The nominal powers, side lengths, and land areas of the studied virtual PV generators are compiled in Table I. The 161 162 land areas are based on typical land areas of PV generators with these power ratings (Ong et al., 2013). The selected power ratings correspond to typical power ratings of medium-sized (0.05 MW) 163 and large (0.2 MW) string inverters, and medium-sized (1 MW) and large (4 MW) central inverters. 164 165 The PV generators were assumed to have a square shape. The shape of PV generators varies greatly in practice. The shape of the generator affects the cumulative time the PV generators experience CE. 166 167 The use of a square shape is justified as it is the most typical in practice. An oblong generator shape 168 could distort the results more than a square shape: if one dimension of the generator is very short compared to the other, a small CE area (from a near-perpendicular direction) could fully cover the 169 170 generator while it could not cover a square shaped generator of the same area.

171

172 Table I. The powers, side lengths, and land areas of the studied PV generators.

| Nominal power (MWp) | Side length | Area (m2) |
|---------------------|-------------|-----------|
| 0.05 | 25 | 625 |
| 0.20 | 50 | 2500 |
| 1.00 | 125 | 15625 |
| 4.00 | 250 | 62500 |

¹⁷³

174 2.4. Assumptions and estimation of 2D average irradiances

Since CE events are the result of light scattering by clouds, the speeds and movement directions of the CE areas can be estimated based on the measured CMVs. The average irradiance of the PV generator was estimated from measured point irradiance based on three assumptions: 1) Taylor's hypothesis in the streamwise direction; 2) uniformity in the cross-stream direction; and 3) the CE areas move perpendicular to the PV generator side. Through these assumptions, the CE areas can be studied one-dimensionally allowing straightforward calculation of the average irradiances over the PV generator land areas. The assumptions and the movement of a CE area are illustrated in Fig. 2.

The assumptions are reasonable for the studied PV generator sizes. However, assumption 2 183 becomes less reasonable and the uncertainty of the results therefore increases with increasing land-184 area. Typical land area lengths of CE events have been found to be in the order of hundreds of meters 185 186 up to several kilometers (Järvelä et al., 2018). Typical land area diameters of cloud shadows have 187 been reported to be around 800 m (Lappalainen and Valkealahti, 2016). The resulting CE geometries differ from those occurring in reality since cloud and scattering geometries are three-dimensional and 188 189 complex. However, dense measurement networks that cover the spatio-temporal evolution of CE are not available. The extrapolation from a timeseries at a point to a line in the wind direction (1D) is 190 191 well documented and reasonable based on Taylor's hypothesis, and given that the spatial scale of clouds is larger than the array sizes, the extrapolation from 1D to 2D also appears to be a reasonable 192 193 assumption for the purposes of this study, which is to derive typical statistics for the effects of CE 194 events on PV generators.



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Fig. 2. Conceptual bird's eye view of a CE event that is upwind of a cloud as it impacts a PV system. Irradiance
increases from blue to red to yellow. The irradiance map is generated from time series at the GHI sensor (blue dot) that
is converted to a line in space aligned with the direction of cloud motion using Taylor's hypothesis (black line,
assumption 1) and extrapolated in the crosswind direction (assumption 2). The PV system borders are assumed to be
perpendicular to the direction of motion (assumption 3).

The average irradiance over the land area of the PV generator was calculated by averaging the measured irradiance over a time interval defined by the ratio of the PV generator dimension and the measured cloud shadow speed. Fig. 3 presents an example of the measured irradiance and the average irradiances over PV generators of different sizes. The irradiance profile becomes smoother for larger generator land areas. The peak irradiance decreases with increasing generator area, all PV generators experience average irradiances exceeding 1100 W/m₂.







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214 2.5. Number of cloud enhancement events

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The example in Fig. 3 illustrates the effect of generator land area on the number and duration of CE events identified in the estimated average irradiances of the generators. The irradiance measured by the GHI sensor exceeded 1000 W/m2 eight times, i.e., the number of identified CE events for the limit of 1000 W/m2 was eight. The estimated average irradiances of the 0.2 and 1 MW generators exceeded the limit of 1000 W/m2 three times. For the 4 MW generator, only one CE event was identified. However, the duration of this event was about two minutes, while the smaller generators and the point measurement experienced multiple shorter CE events. The number of CE events exceeding 1200 W/m² was eight, four and two for the point measurement, 0.2 MW and 1 MW generator, respectively. The largest average irradiance of the 4 MW generator was 1114 W/m². Thus, it did not experience a CE event exceeding 1200 W/m².

226 Irradiance values larger than the STC irradiance were measured during 34 days out of 62. Fig. 4 presents the daily numbers of identified CE events exceeding 1000 W/m2. For clarity, only the 227 228 days when CE was measured were included in this figure. On average, 39 CE events per day were 229 identified in measured point irradiance. The average daily numbers of identified CE events were 24, 230 18, 11, and 7 for the 0.05, 0.2, 1, and 4 MW generators, respectively. Considering only the days with 231 measured CE events, on average 71 CE events per day occurred in the measured irradiance. The 232 number of identified CE events decreased with increasing generator size due to the smoothing of 233 irradiance with increasing land area. The largest number of CE events was identified on May 17, 234 2018, with nearly 300 CE events in measured point irradiance and 55 CE events in the average 235 irradiance of the 4 MW PV generator.

236



Fig. 4. Daily numbers of CE events exceeding 1000 W/m2 for the GHI sensor and the studied PV generators. The statistics
 in this figure are not representative for the occurrence of CE events since only the days when CE occurred were included
 in the analyses.

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The highest irradiances measured by the GHI sensor and the highest average irradiances for the studied PV generators are compiled in Table II. The highest measured irradiance was 1466 W/m2. The highest average irradiances for the 0.05, 0.2, and 1 MW generators were over 1400 W/m2, i.e., over 1.4 times the STC irradiance. The highest average irradiance for the 4 MW generator was 1.34 times the STC irradiance.

247

Table II. Highest average irradiances for the GHI sensor and the studied PV generators over 62 days.

| Area | Irradiance (W/m2) |
|-------------------|-------------------|
| GHI sensor | 1466 |
| 0.05 MW generator | 1441 |
| 0.2 MW generator | 1433 |
| 1 MW generator | 1408 |
| 4 MW generator | 1339 |

The numbers of identified CE events for the studied PV generators are presented in Fig. 5 as a function of irradiance limit. The number of the CE events decreased with increasing PV generator land area and with increasing average irradiance. The measured point irradiance exceeded the STC irradiance around 2400 times during the 62 days included in the analyses. The average irradiance of the 0.05 and 4 MW generator exceeded the STC irradiance over 1500 and 400 times, respectively.







259 2.6. Duration of cloud enhancement events

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261 The cumulative durations of identified CE events for the PV generators are presented in Fig. 6 as a function of irradiance limit. Naturally, the cumulative duration of the CE events decreased with 262 increasing irradiance limit and increasing land area. The cumulative duration of the CE events 263 264 exceeding 1000 W/m2 was 11 hours and 27 minutes for the GHI sensor and 8 hours and 41 minutes for the 4 MW PV generator. The largest cumulative duration of CE events measured by the GHI 265 266 sensor in one day was 1 hour and 40 minutes while the average daily duration was just over 267 11 minutes indicating that energy losses due to operation in power limiting mode during CE events are not a major issue for PV generators. The cumulative irradiance part above the STC irradiance was 268 269 12.3 kWh/m2 for the GHI sensor and 9.2 kWh/m2 for the 4 MW generator decreasing with increasing 270 land area. For reference, a typical PV generator in San Diego produces about 1,500 kWh/m2/year or 271 255 kWh/m2 during the 62 days of the experiment.







275

276 Fig. 7 presents the maximum durations of CE events for the PV generators as a function of 277 irradiance limit. The maximum durations decrease with increasing irradiance limit. The maximum 278 durations of CE events exceeding 1000 W/m2 were around 18 minutes. The average duration of these 279 CE events was 17.2 s for the GHI sensor and increased with increasing land area up to 75.6 s for the 280 4 MW PV generator. The reason for this is that small temporary dips in measured irradiance below 281 1000 W/m₂ are smoothed out with larger land area and thus the average irradiance remains longer above 1000 W/m₂ as illustrated in Fig. 3. The longest durations of the strongest CE events with 282 283 average irradiance exceeding 1400 W/m2 were over ten seconds for the GHI sensor and the 0.05 and 284 0.2 MW PV generators.



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288



Fig. 7. Maximum durations of the identified CE events as a function of irradiance limit.

289 The measured durations of CE events are broadly consistent and slightly longer than those 290 reported in Yordanov et al. (2013a) and Järvelä et al. (2020). For example, the maximum durations 291 of CE events exceeding 1100 W/m2 reported in Yordanov et al. (2013a) and Järvelä et al. (2020) were 292 around 390 and 230 s, respectively, while in this study a duration of 420 s was measured. The 293 differences result mainly from the geographical location. In Yordanov et al. (2013a), measurements were performed in Southern Norway (latitude 58°20'N) and the sensor was oriented south (173° from 294 295 North) with a tilt angle of 39° (Imenes et al., 2011). In Järvelä et al. (2020), measurements were performed in Finland (latitude 61°75'N) with sensors oriented 23° east of due south with a tilt angle 296 297 of 45°. In this study, the latitude was 32°53'N resulting in higher clear-sky maximum irradiance 298 values because of smaller air mass even though GHI was measured, i.e. the sensor was not tilted. 299 However, the measured CE event durations between these studies are broadly consistent given all the 300 differences in the measurements.

- 301
- 302 2.7. Length of cloud enhancement areas
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The land area length of each identified CE event was calculated by multiplying the measured duration of the event by the measured cloud shadow speed. CE area length quantiles are presented in Fig. 8 as a function of irradiance limit. The lengths of CE areas decreased with increasing irradiance limit. The largest lengths for CE events exceeding 1000 and 1100 W/m2 were around 6.6 and 1.2 km, respectively, meaning that even large utility-scale PV power plants can be affected by CE events. A square-shaped 16 MW PV generator with a side length of 500 m can occasionally be totally covered

- 310 by a CE area with minimum irradiance of over 1200 W/m2. A 4 MW generator (side length 250 m)
- 311 can be fully covered by a CE area with minimum irradiance of over 1300 W/m₂. 25% and 50% of CE
- events exceeding 1250 and 1100 W/m₂, respectively, are large enough to fully cover a 0.05 MW PV
- 313 generator. It is worth noting that the land area lengths were calculated along the CE area (cloud edge) 314 movement direction. Naturally, full cover of PV generators requires that also the transverse size of a
- 315 CE event is large enough.
- 315





8 Fig. 8. 100th, 95th, 90th, 75th, and 50th percentiles of CE area length as a function of irradiance limit.

- 319 220 **3** Effects of al
- 321

320 **3. Effects of cloud enhancement on photovoltaic generators**

In this section, the effects of cloud enhancement on PV generators are studied by simulations. The electrical operation of three PV generators was simulated during all the identified CE events exceeding 1000 W/m² described in Section 2. This section investigates how CE affects the global MPP voltage and power of the PV generators, the fraction of time the generators spend in power limiting mode, and energy losses caused by power curtailment. Moreover, the effects of inverter sizing on the operation of the PV plants were studied by varying the DC/AC ratio, i.e., the ratio of the nominal PV DC power to the nominal inverter power.

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330 3.1. Simulation model for the PV modules

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A PV submodule, i.e., a group of series-connected PV cells in a PV module protected by a bypass diode, was used as a basic unit in the simulations. The PV submodules were modeled by a MATLAB Simulink model, which utilizes the common one-diode model of a PV cell providing the following relationship between the current *I* and voltage *U* of a PV submodule:

336
$$I = I_{\rm ph} - I_{\rm o} \left(e^{\frac{U + R_{\rm s}I}{AkN_{\rm s}T/q}} - 1 \right) - \frac{U + R_{\rm s}I}{R_{\rm sh}},\tag{1}$$

337 where I_{ph} is the light-generated current, I_0 the dark saturation current, A the ideality factor, T the 338 operating temperature, R_s the series resistance, and R_{sh} the shunt resistance of the PV submodule. The 339 Boltzmann constant is represented by k, N_s is the number of PV cells in the submodule and q is the 340 elementary charge. The effect of irradiance G was taken into account when calculating I_{ph} as

341
$$I_{\rm ph} = \left(I_{\rm SC, STC} + K_I \Delta T\right) \frac{G}{G_{\rm STC}} \frac{R_{\rm s} + R_{\rm sh}}{R_{\rm sh}},\tag{2}$$

where Isc, stc is the short-circuit (SC) current in STC, K_I the temperature coefficients of Isc, and ΔT 342 343 the temperature difference compared to STC. The bypass diodes were assumed to be at the same 344 temperature as the submodules and were modeled using Eq. (1) by assuming $I_{\rm ph}$ to be zero and $R_{\rm sh}$ 345 infinite. The characteristics of the simulation model were fitted to the characteristics of NAPS NP190GKg PV modules, which are composed of three submodules of 18 multicrystalline silicon PV 346 347 cells. Details of the fitting process and the experimental verification of the simulation model are 348 available in Mäki et al. (2012). Table III presents the SC current and open-circuit (OC) voltage of the 349 submodule in STC and the parameter values of the simulation model.

350 351

Table III. Parameter values of the simulation model for the PV submodules and bypass diodes.

| Parameter | Value |
|------------|------------------------|
| Isc, stc | 8.02 A |
| UOC, STC | 11.0 V |
| Α | 1.30 |
| Kı | 4.70 mA/K |
| Ns | 18 |
| Rs | 0.110 Ω |
| Rsh | 62.6 Ω |
| Abypass | 1.50 |
| Io, bypass | 3.20 µA |
| Rs, bypass | $20.0 \text{ m}\Omega$ |

352

354

353 3.2. Modeling of PV generators under cloud enhancement events

355 The electrical operation of three PV generators was studied during the CE events exceeding 1000 W/m2 described in Section 2. The STC irradiance of 1000 W/m2 was selected as the limit since 356 357 the nominal ratings of PV modules and PV generators are typically defined for this irradiance. The generators consisted of 6 parallel strings of 16 series-connected PV modules, 24 strings of 358 359 20 modules, and 36 strings of 28 modules. These generator sizes correspond to typical ratings of 360 small (6 \times 16), medium-sized (24 \times 20), and large (36 \times 28) string inverters. The PV modules were 361 installed facing south with a 20° tilt angle with respect to the horizon. The module strings were located 362 in straight lines without gaps between the modules and with a 1.5 m gap between the strings. The 363 details of the studied PV generators are compiled in Table IV.

364

365 Table IV. Numbers of modules, powers, and dimensions of the studied PV generators.

| Number of modules (parallel \times series) | Nominal power (kWp) | Dimensions (m) | Area (m ₂) |
|--|---------------------|-----------------|------------------------|
| 6×16 | 18.2 | 13.1 × 23.6 | 308 |
| 24×20 | 91.2 | 56.7 	imes 29.5 | 1674 |
| 36×28 | 191.5 | 85.9 × 41.3 | 3546 |

366

The operation of the PV generators was studied during the movement of the identified CE events over the generators using assumptions 1) and 2) used earlier to estimate the average irradiances (see Section 2.4) with the difference that the CE areas were not assumed to move perpendicular to the PV generator side but measured movement directions were used. Moreover, the CE area speed and movement direction were assumed constant while the CE areas move over the PV generators. The speeds and movement directions for the CE events were calculated from the measured CMVs. The CMVs measured during a CE event were decomposed into north-south and east-west directions and the median value of each was used to recompose one median filtered CMV, which was used for the CE event.

376 A simulation period was the period when the CE area covered at least one submodule of the 377 PV generator, i.e., the simulation period started when the irradiance of the first PV submodule of the generator exceeded the limit of 1000 W/m2 and ended when the edge of the CE area moved away 378 379 from the last submodule. For each time step of 0.1 s, the irradiance at the center of a submodule was 380 taken as the irradiance of the submodule. The operating temperature of the PV submodules was 25 °C during the simulations. Since temperature measurements over the land areas of the simulated 381 382 generators were not available and modeling temperature under transient conditions is a challenge, we opted for this assumption. Note that Weigl et al. (2012) also assumed a constant PV module 383 384 temperature, albeit at 40 °C. The effects of this assumption are further discussed in Section 4. The 385 total duration of the identified CE events for the PV generators increased with increasing generator 386 land area, being around 135 hours for the smallest and 208 hours for the largest generator.

387 MPP tracking of the PV plants was assumed ideal, meaning that the generator is operating at 388 the global MPP unless it is in power limiting mode, i.e., the power at global MPP is higher than the 389 nominal power of the inverter. In that case, the generator is operating on the right-hand side of the 390 global MPP at the lowest voltage where the nominal power of the inverter is not exceeded. The 391 DC/AC ratio was varied from 1.0 to 2.0.

392

393 3.3. Static example cloud enhancement situations

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395 The effects of CE on the operation of PV plants is first illustrated by two examples. In these 396 examples, the CE event with the largest measured irradiance (1466 W/m₂) is located at the center of 397 the plants. Parallel and perpendicular CE area movement with respect to the strings of the plants are 398 considered. The irradiance levels received by the PV submodules of the plants are presented in Fig. 9 and average irradiances are compiled in Table V. The average irradiances decreased with increasing 399 400 plant size. The average irradiances of the 24×20 and 36×28 plants are larger in the case of parallel 401 CE area movement. However, the average irradiance of the smallest plant is larger in the case of 402 perpendicular movement.



Fig. 9. Irradiance levels received by the PV submodules of the studied PV plants at 12:34 on June 5, 2018, the time of the
largest measured irradiance during the experiment. The PV plants of different sizes are presented in top of each other so
that the centers coincide. The modules inside the red and blue rectangle form the 6 × 16 and 24 × 20 plant, respectively.
Each row of PV modules is one string.

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 $410 \qquad \text{Table V. Average irradiances (W/m_2) of the studied PV plants in the snapshot in Fig. 9.}$

| PV plant | Parallel movement | Perpendicular movement |
|----------------|-------------------|------------------------|
| 6 × 16 | 1335 | 1403 |
| 24×20 | 1286 | 1143 |
| 36 	imes 28 | 1211 | 1082 |

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412 The power-voltage (P-U) curves of the studied generators at the same time are presented in Fig. 10. In the case of parallel CE area movement, there are irradiance differences within PV module 413 414 strings. These irradiance differences cause mismatch losses (Lappalainen and Valkealahti, 2017), and 415 lead to multiple peaks in the P-U curves. The global MPP powers of the generators are from 10% to 416 20% higher than nominal due to CE. The voltages of the global MPPs are from 5% to 7% higher than 417 the nominal. Conversely, the perpendicular movement of the CE area does not cause irradiance 418 differences within PV strings. Thus, there are only minor mismatch losses and the P-U curves are 419 smooth (Lappalainen and Valkealahti, 2017). The global MPP powers are from 7% up to 40% larger 420 than nominal while the global MPP voltages are close to nominal.



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Fig. 10. Power–voltage curves of the studied PV generators in the examples of parallel (a) and perpendicular (b) CE area
movement illustrated in Fig. 9. The values are presented with respect to the nominal STC values of the generators.



428 CE affects the global MPP voltages as illustrated in Fig. 10. Analysis of the operational 429 voltage ranges of PV plants is useful to properly specify the voltage range of the inverter. Fig. 11 (a) presents the cumulative frequencies of the global MPP voltage for the studied PV generators during 430 431 the identified CE events. The global MPP voltage was most of the time near the nominal value. The 432 share of time when the global MPP voltage was higher than nominal increased with increasing generator size. The global MPP voltage was within 2% of the nominal value 87%, 79%, and 69% of 433 434 the time for the 6×16 , 24×20 , and 36×28 generator, respectively. The highest global MPP voltage 435 was about 12% higher than the nominal value for all the studied PV generators.



Fig. 11. Relative cumulative frequencies of the global MPP voltage (a) and power (b) for the studied PV generators during
 the identified CE events. Only CE events are considered in this graph, i.e., these statistics are not representative of overall
 PV operation.

442 The cumulative frequencies of the global MPP power are presented in Fig. 11 (b) for the 443 studied PV generators during the identified CE events. The global MPP power during the CE events 444 typically increased with smaller generator land area, as illustrated in Fig. 10. Thus, the share of time 445 when the global MPP power was larger than nominal decreased with larger generator size. However, 446 the share was over 57% for all the studied generators. The share of time when the maximum power 447 was more than 1.2 times the nominal MPP power was from 1.8% to 4.5% depending on the generator 448 size. The maximum instantaneous power of all the studied PV generators was over 1.4 times the 449 nominal MPP power.

Fig. 12 presents the shares of time when the studied PV plants were operating in power limiting mode as a function of DC/AC ratio. The share of time when the PV plants were operating in power limiting mode increased with decreasing plant size. With a 1.0 DC/AC ratio, the PV plants were operating in power limiting mode from 57% to 83% and these shares increased rapidly with increasing DC/AC ratio. The DC/AC ratio from which the PV plant was operating more than 99% of time in power limiting mode were 1.26, 1.47, and 1.63 for the 6×16 , 24×20 , and 36×28 plant, respectively.

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Fig. 12. Shares of time when the studied PV plants operated in power limiting mode as a function of DC/AC ratio. Only
 CE events are considered in this graph, i.e., these statistics are not representative of overall PV operation.

Fig. 13 presents the distributions of the operating voltage of the 36×28 PV plant for different DC/AC ratios. When the power of the generator was not limited, i.e., the generator operated all the time at the global MPP, the operating voltage was most of the time near the nominal MPP voltage. With a 1.0 DC/AC ratio, the peak of the voltage distribution is still near the nominal voltage, but the distribution spreads over larger voltage range. With larger DC/AC ratios, the peak of the distribution moves towards higher voltages. Moreover, the distribution becomes narrower with larger DC/AC ratio.



Fig. 13. Distributions of the operating voltage of the 36×28 plant for different DC/AC ratios. The voltage is with respect to the nominal MPP voltage of the plant. Only CE events are considered in this graph, i.e., these statistics are not representative of overall PV operation.

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In Fig. 14, the highest and median operating voltages for studied PV plants are presented as a function of DC/AC ratio. There were only minor differences in the highest voltages between the studied PV plants. The highest voltages were from 17% to 25% higher than the nominal global MPP voltage. The median operating voltage increased more with increasing DC/AC ratio than the highest voltage. The operating voltage was higher for smaller plants. With DC/AC ratios larger than 1.85, the median operating voltage was over 20% higher than the nominal global MPP voltage. These results indicate that increase of operating voltage due to CE is not a major problem for PV systems.



Fig. 14. Highest and median operating voltage as a function of DC/AC ratio. The voltage is with respect to the nominal
 MPP voltage of the plant. Only CE events are considered in this graph, i.e., these statistics are not representative of overall
 PV operation.

488 Operation in power limiting mode causes energy losses compared to the operation at the global MPP. These energy losses are presented in Fig. 15 for the studied PV plants as a function of 489 490 DC/AC ratio. Relative energy losses due to power curtailment increased with increasing DC/AC ratio 491 since the larger the DC/AC ratio the more the AC power is limited and the larger is the share of time spent in power limiting mode. While the differences between the studied plants were small, the 492 493 relative energy losses increased with decreasing plant size. With a DC/AC ratio of 1.0, the energy 494 losses were around 5% and with 2.0 DC/AC ratio, about half of the available energy production was 495 lost due to power curtailment. With small DC/AC ratios, the energy losses due to power curtailment 496 are very small given the fact that only CE events were considered. 497





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502 **4. Discussion**

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The effects of CE on the operation of PV systems were shown to depend on the DC/AC ratio of the system. Especially, the time spent in power limiting mode and the energy losses caused by power curtailment were found to increase with increasing DC/AC ratio. With small DC/AC ratio, the increase of operating voltages as well as the energy losses due to power curtailment are small having only minor impact on the overall operation of PV systems. However, relative energy losses due to curtailment increased with increasing DC/AC ratio being around 50% for DC/AC ratio of 2.0. Thus, 510 oversizing of PV generators with respect to inverters is not recommended from the CE point of view.

- 511 However, PV generators are typically oversized since oversizing of the PV generators brings many
- 512 financial and operational benefits (Wang et al., 2018). The optimal DC/AC ratio depends on many
- 513 factors such as insolation conditions and inverter characteristics (Peippo and Lund, 1994). Peippo and
- 514 Lund (1994) stated that the optimal DC/AC ratio region is quite flat and up to 20% changes from the
- optimal value typically leads to less than 2% losses. Zhu et al. (2011) recommended that DC/AC ratio should be from 1.1 to 1.7. The results of this study show that if the intention is to avoid power
- 517 curtailment caused by CE, DC/AC ratio should be less than 1.0.

The relatively small increase of operating voltages due to CE, even with large DC/AC ratios (Fig. 14) indicates that CE does not cause increased risk of short-term equipment damage or disconnection for PV systems. However, the increasing operating voltage may cause further losses for PV systems since the increasing DC side voltage reduces the efficiency of some inverters. Moreover, the increasing operating voltage can affect the operating temperatures and lifetimes of certain components used in the inverters.

The negative impacts of CE on the operation of PV systems decreased with increasing generator size, meaning that CE is less of a problem for utility-scale PV generators. CE events that have strongest impacts on the operation of PV systems are rare. In conclusion, the results of this study show that CE events do not cause major problems for the operation of PV systems. However, multiple assumptions and simplifications were applied in this study, which may affect the results. These issues have been discussed in the following paragraphs.

530 The CE event characteristics were based on the GHI measurements by a single sensor with a sampling frequency of 0.5 Hz. Measurements of multiple sensors spread over a large land area would 531 532 be required to measure the actual irradiances and shapes of the CE areas accurately. It has been stated 533 in Yordanov et al. (2013b) that a sampling frequency on the order of 10 Hz is needed to identify all 534 CE events. However, a sampling frequency of 0.5 Hz is high enough to identify all CE events, which 535 affect the operation of PV generators. However, the uncertainty of CE event results increases with 536 decreasing sampling frequency. Due to the low sampling frequency in our study, the durations of identified CE events are underestimated, short CE events might not be identified, and several CE 537 538 events within a short time period might be aggregated into one event.

539 GHI measurements were used to study the effects of CE on the electrical operation of PV 540 generators. Results would be more accurate if actual plane of array irradiance measurements were 541 used. Unfortunately, those were not available. The use of actual plane of array irradiance 542 measurements would probably lead to somewhat larger CE irradiances and longer CE events. 543 However, the difference between GHI and plane of array irradiance was relatively small due to small 544 tilt angle (20°).

545 In the simulations, three assumptions were made regarding the movement of the identified CE 546 events over the PV generators (see Section 3.2). Although the assumptions are reasonable considering 547 the small sizes of the studied PV generators, the uncertainty of the results increases with larger land 548 areas. Especially, the assumption of irradiance uniformity in the cross-stream direction might not hold 549 for larger land areas. Moreover, the operating temperature of the PV generators was assumed 550 constant. The operating temperature of the PV cells of a PV generator in California, especially during 551 CE events, can be much higher than the STC temperature. The OC voltage and MPP power of a PV cell decrease and the SC current increases slightly with increasing temperature. Thus, the assumption of constant temperature affects mainly the results of the global MPP and operating voltages. However, the use of STC temperature, which is almost always lower than real operating temperatures, leads to an overestimation of the operating voltages. Thus, real operating voltages are expected to be smaller than reported in this study.

557 The electrical simulation model for the PV modules naturally contains assumptions and simplifications. Firstly, a PV submodule was used as a basic unit in the simulations. However, only 558 559 negligible irradiance differences between the PV cells of a submodule existed during the studied CE 560 events. Thus, the results of the study would change only marginally if the simulation were conducted on a PV cell level. Secondly, the PV submodules were modeled by the widely used one-diode model 561 562 of a PV cell, which is a simplification of the more accurate two-diode model. However, the one-diode model provides a good trade-off between accuracy and complexity and is accurate enough for the 563 564 analysis that was presented in this article. Moreover, the results could slightly change if different PV 565 modules were used as a reference for the simulation model. However, the basic behavior would not 566 change since the electrical characteristics of crystalline silicon PV modules are essentially identical. 567 Crystalline silicon was selected as it is by far the most important PV technology.

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569 **5. Conclusions**

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571 In this article, CE event characteristics and the effects of CE on the electrical operation of PV 572 generators were studied. The study was based on GHI and cloud edge velocity measurements on 62 days. The number, duration, and length of CE events exceeding various irradiance limits from 573 574 1000 W/m² over the land areas of various PV generators were studied. The average irradiance over 575 the land areas was calculated by averaging the measured GHI over a time interval defined by the ratio 576 of the PV generator dimension and the measured cloud shadow speed. Moreover, the operation of 577 three PV generators, ranging from 20 to 200 kW, was simulated during all CE events. The effects of 578 inverter sizing on the operation of the PV generators were studied by varying DC/AC ratio from 1.0 579 to 2.0.

580 In total, 2401 CE events exceeding 1000 W/m2 were identified in the measured GHI. The average irradiance of the 0.05 and 4 MW generator exceeded the STC irradiance over 1500 and 581 582 400 times, respectively. The highest measured peak irradiance was 1466 W/m² and the highest 583 average irradiances for the studied PV generator up to 1 MW generators were also over 1400 W/m2. The maximum durations of CE events exceeding 1300 W/m2 were around one minute. The largest 584 585 lengths for CE events exceeding 1000 W/m2 were multiple kilometers. A square-shaped PV generator 586 of up to 16 MW can occasionally be totally covered by a CE area with minimum irradiance of over 587 1200 W/m₂. These results mean that even large utility-scale PV power plants can be affected by CE 588 events.

The simulation results showed that CE affects the operation of the PV plants but the effects are mainly small. Although the highest global MPP voltage and power were about 12% and 40% higher than the nominal STC values, the global MPP voltage was most of the time near the nominal value. The negative impacts of CE on the operation of PV systems were found to increase with increasing DC/AC ratio. With a 1.0 DC/AC ratio, all the PV plants were operating in power limiting 594 mode over half of the time of the CE events and these shares increased rapidly with increasing DC/AC ratio. The highest operating voltages were from 17% to 25% higher than the nominal global MPP 595 596 voltage. The operating voltage increased with increasing DC/AC ratio and decreasing plant size. With 597 DC/AC ratios larger than 1.85, the median operating voltage was over 20% higher than the nominal global MPP voltage. The energy losses due to power curtailment were from 5% to 50% of the 598 599 available energy production during the CE events increasing with increasing DC/AC ratio. To avoid 600 power curtailment caused by CE, DC/AC ratios should be less than 1.0. In conclusion, the results of 601 this study show that CE do not cause major problems for the operation of PV systems.

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609 610 The data that support the findings of this study are available from the corresponding author upon 611 reasonable request.

- 612
- 613 Appendix
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615 The CSS detects the component of cloud shadow velocity normal to the shadow edge, i.e., 616 cloud shadow edge velocity, v_e (speed v_e and movement direction α_e), which underestimates the actual 617 shadow velocity v (speed v and movement direction α). A weighted non-linear regression of v and α 618 to the NCMV CMVs collected in a time period of 30 min was used to calculate v from v_e as

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$$w_i v_e^i = v \cos(\alpha_e^i - \alpha),$$

(A.1)

where wi is a weighting factor calculated as 620

Data Availability Statement

 $w_i = |t_f - t_o| - |t_i - t_o| + 1,$ 621

(A.2) where t_f is the timestamp furthest from the present time t_0 in the time period and t_i the timestamp of 622 623 the *i*th CMV. If the CMVs collected in the time period show variation of α_e smaller than 20°, the 624 shadow movement direction is almost perpendicular to the shadow edge and the non-linear regression is not needed. In these cases, and if NCMV is too small for reliable regression (less than 9), the CMVs 625 626 are decomposed into north-south and east-west directions, and the median value of each is used to 627 recompose the resulting CMV.

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