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# **Structural and Thermodynamic Properties of Magnesium-rich Liquids at Ultrahigh Pressure**

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Abstract: We explore the structural properties of Mg, MgO and MgSiO<sub>3</sub> liquids from *ab initio* computer simulations at conditions are relevant for the interiors of giant planets, stars, shock compression measurements and inertial confinement fusion experiments. Using path integral Monte Carlo and 3 density functional theory molecular dynamics, we derive the equation of state of magnesium-rich liquids in the regime of condensed and warm dense matter, with densities ranging from 0.32 to 86.11 5 g cm<sup>-3</sup> and temperatures from 20 000 K to  $5 \times 10^8$  K. We study the electronic structure of magnesium as a function of density and temperature and the correlations of the atomic motion. We find an unexpected local maximum in the pair correlation functions that emerges at high densities, which 8 decreases the coordination number of elemental magnesium and reveals a higher packing. We do not 9 observe this phenomenon in other magnesium liquids that maintain a rather constant coordination 10 number. 11

Keywords: density functional theory, silicates, coordination number

### 1. Introduction

Magnesium-rich liquids are significant minerals in planetary science because they rep-14 resent the main constituent of magma oceans [1] that formed when iron and silicates phase 15 separated during the formation of Earth and super-Earth planets [2–4]. Sizable magma 16 oceans have been predicted to persist over long periods of time [5]. Understanding how 17 the properties magnesium-rich liquids change with pressure and temperature will thus 18 enable us to better constrain the models of formation and evolution of rocky planets [6]. 19 Magnesium-rich liquids also provide valuable information for inertial confinement fusion 20 (ICF) experiments, where materials are exposed to extreme conditions [7–9] that trans-21 form liquids into warm dense matter and dense plasmas that are difficult to understand. 22 State-of-the-art laboratories, including the National Ignition Facility (NIF) at Lawrence 23 Livermore National Laboratory, the Omega laser at the University of Rochester, the Z 24 machine at Sandia National Laboratory, and the SLAC laboratory, regularly investigate 25 these conditions to explore matter in the high-energy density regime, exploring matter 26 in the high-energy density regime by probing materials at ultrahigh pressure and tem-27 perature conditions never explored before, but that are present at the interior of white 28 dwarf stars [10], rocky exoplanets [11,12], and giant planets like Jupiter [13,14]. While these 29 experiments have accessed the warm dense matter regime and were able to achieve fusion 30 conditions recently [15], theoretical methods have difficulties accessing this regime due to 31 the strong level of ionization, which makes interpretation of experimental measurements a 32 hard task. 33

The properties of magnesium-rich liquids are very interesting. Their Grüneisen parameter increases upon compression [16] and the heat capacity can increase beyond the ideal gas limit upon ionization [17]. MgO, SiO<sub>2</sub> and MgSiO<sub>3</sub> are all insulators in the solid phase but they all become modest electronical conductors in liquid form at high enough 37

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temperature and pressure, which implies that super-Earth planets can generate magnetic 38 fields in their mantle [5,18]. The structure of liquid magnesiosilicates varies substantially 39 with compression [19-21]. Some melts, such as MgSiO<sub>3</sub>, are good solvents for water. The 40 solubility was found to increase with pressure, which has important consequences for the 41 Earth's mantle [22]. At high temperatures, it is also important to identify the thermal and 42 pressure ionization regimes [23], as they modify the properties of the liquid as it becomes 43 partially ionized. Recent ab initio calculations predicted mixed coordination numbers for 44 silica between the 6-fold coordinated pyrite-type phase and the 9-fold coordinated  $Fe_2P$ -45 type phase at high pressure, as well as the formation of superoxides such as  $SiO_3$  and  $SiO_6$ , 46 which may exist in the mantle of super-Earth planets [24]. 47

In this study, we perform *ab initio* simulations of the liquids Mg, MgO, and MgSiO<sub>3</sub> using a combination of density functional theory molecular dynamics (DFT-MD) and path integral Monte Carlo (PIMC), providing a detailed characterization of the structure of the liquids.

### 2. Simulation methods

Rigorous discussions of the PIMC [25–27] and DFT-MD [28–30] methods have been 53 provided in previous works, and the details of our simulations have been presented in 54 some of our previous publications [17,31–33]. Following earlier publications on hydrogen 55 and helium, PIMC and DFT-MD simulations have been combined to study the properties of materials with core electrons in the regime of warm dense matter such as lithium 57 fluoride [34], boron [35], aluminum [31], oxygen [36], silicon [37,38], hydrocarbons [38,39], 58 and superionic water [40,41]. However, the structure of magnesium liquids has not been 59 explored in detail in this regime of extreme conditions. We combine PIMC [42] and and DFT-60 MD simulations as implemented in the Vienna Ab initio Simulation Package (VASP) [43] to 61 generate a consistent Equation of State (EOS) for Mg, MgO, and MgSiO<sub>3</sub> that spans across 62 a wide range of ultrahigh temperatures and pressures. 63

For DFT-MD simulations, we employ Kohn-Sham DFT simulation techniques as 64 implemented in the Vienna Ab initio Simulation Package (VASP) [43] using the projector 65 augmented-wave (PAW) method [44,45], and molecular dynamics is performed in the 66 NVT ensemble, regulated with a Nosé thermostat. The time step was adapted to the 67 density and the temperature, ranging from 0.16 to 0.44 fs for simulation times from 1000 68 to 16 000 time steps, to ensure a reliable estimation of the thermodynamic quantities. The pseudopotentials used in our DFT-MD calculations freeze the electrons of the 1s orbital 70 (He-core), which leaves 10, 12, and 6 valence electrons for Mg, Si, and O atoms, respectively. 71 Exchange-correlation effects are described using the Perdew, Burke, and Ernzerhof [46] 72 (PBE) generalized gradient approximation (GGA). However, for elemental Mg, the provided 73 Mg PBE pseudopotential did not give proper results for high densities, so we switched to 74 the local density approximation (LDA). We proceed in a similar way with MgO, the highest 75 densities were also simulated using the LDA functional. As shown in Ref. [47], the choice 76 of the pseudopotential in ab initio simulations of Mg has very little effects on the computed 77 thermodynamic properties. We obtain a very good agreement between both functionals 78 for a number of densities. Electronic wave functions are expanded in a plane-wave basis 79 with a energy cut-off as high as 7000 eV in order to converge total energy. Size convergence 80 tests with up to a 65-atom simulation cell at temperatures of 10000 K and above indicate 81 that pressures are converged to better than 0.6%, while internal energies are converged 82 to better than 0.1%. We find, at temperatures above 500 000 K, that 15-atom supercells 83 are sufficient to obtain converged results for both energy and pressure, since the kinetic 84 energy far outweighs the interaction energy at such high temperatures [31,48]. The number 85 of bands in each calculation was selected such that orbitals with occupation as low as  $10^{-4}$  were included, which requires up to 14000 bands in an 15-atom cell at 2  $\times$  10<sup>6</sup> K and 87 two-fold compression. All simulations are performed at the  $\Gamma$  point of the Brillouin zone, which is sufficient for high temperature fluids, converging total energy to better than 0.01% 89 compared to a grid of *k*-points.

### 3. Results

In this section, provide a detailed characterization of the magnesium-rich liquids that we have obtained from our *ab initio* simulations of Mg [33], MgO [32], and MgSiO<sub>3</sub> [17], spanning the condensed matter, warm dense matter and plasma regimes. Computations vere performed for a series of densities and temperatures ranging from 0.321-86.11 g cm<sup>-3</sup> and  $0.10^{4}-10^{8}$  K. The full range of our EOS data points is shown in temperature-density and pressure-density space in Fig. 1, along with the shock Hugoniot curve of each material.



**Figure 1.** Temperature-density conditions of our PIMC and DFT-MD simulations. The thick dashed lines correspond to the shock Hugoniot curves that we derived for Mg, MgO, and MgSiO<sub>3</sub>, with initial densities  $\rho_0 = 1.736$  g cm<sup>-3</sup>, 3.570 g cm<sup>-3</sup>, 3.208 g cm<sup>-3</sup>, respectively. The full EOS for each material is available in Refs [17,23,32,49]. Shock Experiments on MgO from McCoy *et al.* [50], and Root *et al.* [51], and shock experiments on MgSiO<sub>3</sub> from Fratanduono *et al.* [52], are included for comparison.

The ideal mixing approximation has been shown to perform well for temperatures 98 above  $10^5$  K. [53], and the magnitude of nonideal mixing effects was found to be small in this regime, leading to shock Hugoniot curves of MgO and MgSiO<sub>3</sub> that are reproduced 100 with sufficient accuracy by combining the EOSs of the elemental substances with the addi-101 tive volume rule. This concept was extended to other mixtures [49] and good agreement the 102 shock Hugoniot curves of H<sub>2</sub>O and CO<sub>2</sub> was found between laboratory measurements and 103 theoretical predictions based on the linear mixing approximation. However, this approxi-104 mation breaks down at lower temperatures, where chemical bonds play an increasingly 105 important role. These bonds change the structure of the liquid, modifying the atomic 106 coordination. Here we will study how the structure of the liquid changes with density 107 and temperature. We will demonstrate that coordination of magnesium ions is sensitive to 108 presence of silicon and oxygen. 109

### 3.1. Radial Distribution Function

The atomic trajectories obtained from DFT-MD simulations can be used to study the local structure of the liquids. Using the radial distribution function, defined by

$$g_{\alpha\beta}(r) \equiv \frac{V}{4\pi r^2 N_{\alpha} N_{\beta}} \left\langle \sum_{i=1}^{N_{\alpha}} \sum_{j\neq i}^{N_{\beta}} \delta(r - \|\vec{r}_{ij}\|) \right\rangle = \frac{V}{4\pi N_{\beta} r^2} \frac{dN_{\beta}(r)}{dr}, \tag{1}$$

we can obtain a measure of the structure of the liquid, which depends on temperature and density. Here,  $N_{\alpha}$  and  $N_{\beta}$  are the total number of nuclei of type  $\alpha$  and  $\beta$ , respectively that are contained in the volume V, while  $\vec{r}_{ij} = \vec{r}_i - \vec{r}_j$  is the separation between nuclei *i* and *j*.  $N_{\beta}(r)$  is the total number of nuclei of species  $\beta$  within a sphere of radius *r* around a nuclei of type  $\alpha$  [54,55]. This function,  $g_{\alpha\beta}(r)$ , can be interpreted as the probability of finding a particle of type  $\alpha$  at a distance *r* from a particle of type  $\beta$ .

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In Fig. 2, we compare radial distribution functions of liquid magnesium over a wide range of temperatures and densities. For every density, we observe that the average distance to the nearest neighbor, given by the location of the first maximum of the g(r), slightly decreases with increasing temperature. At 6.89 g cm<sup>-3</sup>, this distance shifts from 1.9 Å at 20 000 K to 1.8 Å at 100 000 K. This 5% decrease is caused by stronger collisions and higher kinetic energy. As expected, the distance to the nearest neighbors depends strongly on density. At the highest density explored (51.67 g cm<sup>-3</sup>), this distance decreased to 0.96 Å. This value does not depend much on temperature.



**Figure 2.** Radial distribution function of liquid elemental magnesium at 8 different densities as a function of temperature. The diagrams on the top correspond to the typical environment of a magnesium atom: surrounded by an average of 18 nearest neighbors within 2.39 Å at 12.92 g cm<sup>-3</sup> and 20 000 K (left), and surrounded by a closer shell of only 6 to 7 neighboring atoms at 25.83 g cm<sup>-3</sup> and 20 000 K. For the three highest densities in our simulations ( $\rho \ge 34.44 \text{ g cm}^{-3}$ ), the system freezes into an simple cubic structure at 20 000 K, which corresponds to the stable phase of Mg observed experimentally at pressures exceeding 1 TPa, the highest pressures ever reported in experiments of Mg to date [56]. The arrows indicate the location of an emerging intermediate local minimum.

We can also observe in Fig. 2 that the shape of the all g(r) curves at a low densities is fairly similar. All curves have two well-defined maxima and two minima. However, for densities of 19.37 g cm<sup>-3</sup> and higher, the liquid becomes significantly more structured. The curve develops an additional intermediate local maxima that result in a new local minimum at ~ 1.55 Å. As density increases, this intermediate maximum becomes more pronounced. In our simulations at 20 000 K, the system freezes into the simple cubic phase

for densities of 34.44 g cm<sup>-3</sup> and higher, which corresponds to pressures higher than 133 24381 GPa. This simple cubic phase has been observed experimentally at pressures of 134 1 TPa [56]. With crystal structure search methods, a series of other high-pressure structures 135 including body-centered cubic, face-centered cubic, and simple hexagonal and simple cubic 136 phases have been predicted for magnesium [57]. When this crystallization happens in our 137 MD simulations, the subtle features of the liquid g(r) functions become amplified. But for 138 temperatures of 30 000 K and above, we found that the system remained in a liquid state 139 for all densities. Still the local minimum at  $r_{min} \sim 1.55$  Å persisted. We will discuss these 140 changes in terms of the atomic coordination number in the next section. 141

### 3.2. Coordination Number

A further measure of the structure of the liquid is the coordination number, given by

$$C_{\alpha\beta} = \frac{4\pi N_{\beta}}{V} \int_0^{r_{\min}} r^2 g_{\alpha\beta}(r) dr$$
<sup>(2)</sup>

where  $C_{\alpha\beta}$  is defined to be the number of atoms of type  $\beta$  that are within a spherical region of radius  $r_{\min}$ , centered at an atom of species  $\alpha$  [54]. Here, we adopted the usual convention that  $r_{\min}$  is the location of the first minimum of the radial distribution functions  $g_{\alpha\beta}(r)$ . The integrated nucleus-nucleus pair correlation function, given by  $N_{\beta}(r)$  in Eq. (1), can be employed to define a coordination number in Eq. (2) when evaluated at the location of the first minimum, that is,  $N_{\beta}(r_{\min}) = C_{\alpha\beta}$ .

In Fig. 3, we show the radial distribution functions of liquid elemental magnesium at 30 000 K and the corresponding integrated nucleus-nucleus pair correlation functions, N(r). The shaded areas in the top panel highlights the interval  $[0, r_{min}]$  over which the integration in Eq. (2) is performed. As density increases, the position of the first local maximum shifts to smaller distances and the peak becomes narrower, which indicates that the distance to first neighbors is decreasing.  $r_{min}$ , also decreases with increasing density, reducing the total area below the curve and, hence, the coordination number.

As the atoms get closer, the liquid develops a new structure, which is reflected in 157 the intermediate local maximum that starts developing in the g(r) for densities higher 158 than 25.83 g cm<sup>-3</sup> at 30 000 K, as we can see in Fig. 3, which corresponds to a pressure 159 of 13147 GPa. The typical environment of a magnesium atom, after this intermediate 160 local maximum develops, is shown at the top of Fig. 2, where a new shell of nearest 161 neighbors forms. The slope  $(dE/d\rho)_T$  is positive, therefore pressure ionization is likely to 162 take place [23]. As described in the previous section, a transition occurs in the liquid for higher densities, where a new intermediate maximum appears, which abruptly decreases 164 the value of  $r_{\min}$  and, hence, the coordination number.

In Fig. 4, we show the resulting Mg-Mg coordination number in liquid magnesium 166 for a wide range of temperatures and densities. As we can observe in the figure, the 167 coordination number first increases from 14 to 18 at  $T = 20\,000$  K and then abruptly drops 168 to 7, consistent with the diagram shown in Fig. 2. Something similar occurs at  $T = 30\,000$  K, 169 where the coordination number drops from 18 to 8. This is an indication that the system 170 prefers a coordination similar to the simple cubic structure, where the coordination number 171 is 6. For higher temperatures, this intermediate maximum never develops for this range of 172 densities, but it is likely to appear for  $\rho > 60$  g cm<sup>-3</sup>. For  $T > 30\,000$  K, the coordination 173 number remains between 13 and 18 at all densities. 174

#### 3.3. Electronic Density of states

We also identified changes in the electronic structure of Mg at conditions where structure of the liquid changes and the new intermediate g(r) maximum appears. At ultrahigh pressure, solid magnesium has been predicted to assume an electride structure [56– 58]. In Fig. 5, we show the electronic density of occupied states (DOS) together with the electronic localization function (ELF) for liquid Mg at 30 000 K. In the DOS, we observe with increasing density a clear broadening of the 2s and 2p energy bands and a shift of 181

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**Figure 3.** Radial distribution functions, g(r), of liquid Mg at  $T = 30\,000$  K (top panel) and the corresponding integrated nucleus-nucleus pair correlation functions, N(r) (bottom panel). For densities higher than 25.83 g cm<sup>-3</sup>, the g(r) function develops an intermediate maximum, which decreases the area below the curves and, consequently, the coordination number. The vertical bars indicate the location of the first minimum for the highlighted g(r) functions, corresponding to 6.89, 25.83, and 51.67 g cm<sup>-3</sup>.



**Figure 4.** Coordination number  $C_{Mg-Mg}$  of liquid magnesium as a function of density for five different temperatures. For densities higher than 25.83 g cm<sup>-3</sup>, the g(r) function develops an intermediate maximum, which increases the coordination number. The labels next to the symbols in the right panel indicate the pressure of selected simulations, and the open symbols indicate the coordination number obtained if we ignore the intermediate minimum and perform the integration in Eq. (2) up to the next local minimum.

the eigenvalues towards lower energies. This broadening does not affect the electrons in 182 the conduction band (3s) in a significant way. However, at 21.53 g cm<sup>-3</sup>, the broadening 183 of the other bands is significant and almost closes the gap between the 2s and 2p bands. 184 According to Ref. [33], these conditions fall in the regime of pressure ionization where the 185 effects of thermal ionization are expected to be small. The ELF depicts location of electronic 186 charge in the between void between the nuclei, which is the typical electride behavior that 187 results from the repulsion of core electrons. For the simple cubic phase of Mg, this has 188 recently been reported by a experimental-theoretical study [56]. With ab initio methods, 189 this has been predicted to occur in many solid structures at high pressure [59]. In Fig. 5, we 190 show that also the Mg liquid exhibits electride behavior, which shares similarities to earlier 191 predictions for liquid iron [60].



**Figure 5.** Top: Electronic density of occupied states of Mg based on our DFT-MD simulations at different densities for a temperature of 30 000 K. The energies of all MD configurations were shifted so that the Fermi energies are aligned at E = 0 eV. Bottom: ELF function of liquid (left) and solid Mg in the simple cubic phase (right) at 25.83 g cm<sup>-3</sup>. In the solid phase (right), the electronic charge (yellow pockets) is localized in the voids between the nuclei, which depicts the typical electride behavior that has been predicted with *ab initio* method to occur in many solid structures including K [58,61,62] and Mg [56]. Here we also find the Mg liquid to exhibit electride behavior (left), which has been predicted to occur in liquid Fe [60].

### 3.4. MgO and MgSiO<sub>3</sub>

We do not observe an intermediate maximum or similar structural change in our simulations of MgO. In Fig. 6, we plot the radial distribution functions (left panel) of MgO which show that the peaks becomes more pronounced with increasing density, but there

is no significant change in the topology of these functions as we observed in elemental <sup>197</sup> Mg, indicating that the structure of the liquid varies smoothly with both temperature <sup>198</sup> and density. At densities of 24.99 g cm<sup>-3</sup> and higher, the Mg-Mg and O-O coordination <sup>199</sup> increases, as shown by the separation of the radial distribution function in two distinctive <sup>200</sup> peaks that separates the first nearest neighbors from the second nearest neighbors.



**Figure 6.** Coordination number of liquid MgO (right panel) as a function of density for five different temperatures. The radial distribution functions of MgO (left panel) show the location of the first local minimum (vertical bars for Mg-O), used to calculate the coordination number using Eq. (2). The small number near the vertical bars indicate the Mg-O coordination number at that local minimum. The Mg-O and O-O g(r) functions have been shifted upwards for clarity. The four text labels in the lowest right panel indicate the pressure in the simulations at the lower and highest temperatures for two density values.

The Mg-Mg coordination number is much higher in liquid, elemental Mg ( $\sim$ 14) than in 202 liquid MgO. In the presence of oxygen, the Mg-Mg coordination number decreases from 8 203 to 4-6 with increasing density, as we observe in the right panel of Fig. 6. However, this lower 204 coordination is comparable to that of elemental Mg ( $\sim$ 7-10) if the density of that system is 205 high and the temperature is low, as we showed in Fig. 4. The Mg-O coordination number 206 was found to be around 7 for all temperatures and densities, consistent with previous 207 studies of MgO at high temperatures and densities [19]. Similarly, the O-O coordination 208 number remained approximately 6. This is smaller that the value found for the molecular 209 fluid  $GeO_2$  liquid, where the average O-O coordination number was found to be around 9 210 and a Ge-O coordination number of 2 at 1500 K and low temperatures [63,64]. This is not 211 the case of MgO, which behaves as an atomic fluid. This is comparable to silica, which is 212 predicted to a have a mixed coordination between the 6-fold coordinated pyrite-type phase 213 and the 9-fold coordinated Fe<sub>2</sub>P-type phase at high pressure [24]. Therefore, coordination 214 numbers with oxygen between 6 and 9 are expected at these conditions. 215

In the case of MgSiO<sub>3</sub>, the Mg-O coordination number is also between 6 and 8, as we 216 can see in Fig. 7, but slightly larger than 8 at some densities. The Mg-Mg g(r) functions in 217 the left panel show that magnesium atoms are not correlated, with no clear signature of 218 a local minimum at most of the conditions that allows to identify a layer of first nearest 219 neighbors. When the identification is possible, the Mg-Mg coordination number in MgSiO<sub>3</sub> 220 lies between 2 and 4. While the Mg-O coordination number seems to decrease with 221 density, the Si-O coordination number increases with increasing density, regardless of the 222 temperature, from 6 to 8. The O-O coordination number is larger in the MgSiO<sub>3</sub> liquid 223 than in the MgO liquid, reaching values between 7 to 9 in the latter case, while MgO 224

shows an average of 6 for most conditions. Regarding the distance to nearest neighbors, or <sup>225</sup> bond length, we find that the Mg-O bond length is larger in MgSiO<sub>3</sub> than in MgO. For a <sup>226</sup> comparable denisity of  $\sim$ 25 g cm<sup>-3</sup>, this distance is 1.3 Å in MgSiO<sub>3</sub>, while for MgO, this <sup>227</sup> distance is about 1.2 Å. At all conditions, the Si-O bond length is smaller than the Mg-O, <sup>228</sup> and both are larger than the O-O bond length. As in the case of MgO, there no signature of <sup>229</sup> an abrupt structure transition, as we observed in pure Mg.



**Figure 7.** Coordination number of liquid MgSiO<sub>3</sub> (right panel) as a function of density for four different temperatures. The radial distribution functions of MgSiO<sub>3</sub> (left panel) show the location of the first local minimum, used to calculate the coordination number using Eq. (2). The Mg-O, Si-O, and O-O g(r) functions have been shifted upwards for clarity. The text labels on top of the symbols of the right panel indicate the pressure of the sample at the corresponding density and temperature.

### 4. Conclusions

We have studied the structural properties of magnesium liquids in a broad range of 232 temperatures and densities using *ab initio* simulations. We found evidence of a structural 233 transition in liquid Mg around 20 g cm<sup>-3</sup>, where the emergence of a new intermediate 234 maximum in the radial distribution function leads to an abrupt decrease in the coordination 235 number with increasing density for low temperatures. The structural change in liquid 236 elemental magnesium is an indication of a transition to electride-type behavior, consistent 237 with recent experimental finding of electride phases of Mg at ultrahigh pressure [56]. 238 This transition does not occur in the other magnesium liquids, MgO and MgSiO<sub>3</sub>, where 239 compression introduces only gradual changes in the coordination. Under no conditions 240 we found a signature of a stable molecular bond between Mg and O species. However, 241 the Mg and O nuclei exhibit positive correlations that are stronger than those between the 242 other pairs. The presence of silicon increases the O-O coordination number, which is larger 243 in  $MgSiO_3$  than in MgO. The Mg-O bond length is smaller in MgO when compared to 244 MgSiO<sub>3</sub> at similar conditions, and it is always larger that the Si-O bond length within the 245 same MgSiO<sub>3</sub> liquid. We did not observe the formation of any molecule, making Mg, MgO, 246 and MgSiO<sub>3</sub> atomic fluids at the conditions studied. 247

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**Data Availability Statement:** The equation of state of Mg, MgO, and MgSiO<sub>3</sub> can be found in the supplementary material of Refs. [17,32,33], respectively. 250

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		Conflicts of Interest: The authors declare no conflict of interest.			
		Abbreviations			255
		The following abbreviations are used in this manuscript:			256
					257
		DFT-MD PIMC	Density Functional Theory Molecular Dynamics Path Integral Monte Carlo		250
		VASP	Vienna Ab initio Simulation Package		250
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