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Y³⁺ Surface Segregation Promotes Coarsening Inhibition in Nanocrystalline Zinc Aluminate

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Abstract

The thermal stability of zinc aluminate nanoparticles is critical for their use as catalyst supports. In this study, we experimentally show that doping with 0.5 mol% Y₂O₃ improves the stability of zinc aluminate nanoparticles. The dopant spontaneously segregates to the nanoparticle surfaces in a phenomenon correlated with excess energy reduction and the hindering of coarsening. Y³⁺ was selected based on atomistic simulations on a 4 nm zinc aluminate nanoparticle singularly doped with elements of different ionic radii: Sc³⁺, In³⁺, Y³⁺, and Nd³⁺. The segregation energies were generally proportional to ionic radii, with Y³⁺ showing the highest potential for surface segregation. Direct measurements of surface thermodynamics confirmed the decreasing trend in surface energy from 0.99 for undoped to 0.85 J/m² for Y-doped nanoparticles. Diffusion coefficients calculated from coarsening curves for undoped and doped compositions at 850°C were 4.8×10^{-12} cm²/s and 2.5×10^{-12} cm²/s, respectively, indicating the coarsening inhibition induced by Y³⁺ results from a combination of a reduced driving force (surface energy) and decreased atomic mobility.

1. Introduction

Zinc aluminate (ZnAl₂O₄) spinel is an excellent material to facilitate the catalysis of toluene degradation^{1,2}, hydroformylation^{3,4}, and hydrogenation^{3,5,6} because of its characteristically wide bandgap and relatively high chemical and thermal stabilities^{3,7,8}. In the form of nanocrystals, the associated high specific surface areas increase the catalytic activity since the number of active sites directly scales with the available surface area if the support itself is the catalyst. Nanocrystals are equally attractive acting as a support alone since the available surfaces

assist in uniformly dispersing active metals. However, the excess energies associated with nanocrystals give rise to processing challenges and limitations regarding viable operating temperatures. High surface energies lead to reduced activation energies for coarsening at the nanoscale⁹, enabling grain growth at lower temperatures. Kinetic approaches have often been used to limit coarsening in the nanocrystalline regime¹⁰, but surface thermodynamics also play a significant role in dictating the coarsening process^{11,12}. Similar to other metal oxides, zinc aluminate nanoparticles grow via Ostwald ripening¹³, where small particles evaporate and precipitate or diffuse onto larger ones to reduce the surface energy of the system by mean grain enlargement¹⁴⁻¹⁶. This growth mechanism is identified by its cube-root dependence on time, as shown in **Equation 1**:

$$R_t^3 - R_0^3 = Kt \quad (1)$$

where R_t is the mean particle radius at time t , R_0 is the mean radius at the onset of growth, and K is a rate constant directly proportional to both the average particle surface energy and governing diffusion coefficient¹⁷. For systems that undergo Ostwald ripening, this relationship highlights the significance of surface energies in hindering coarsening, a dependence that is increasingly relevant at the nanoscale due to the substantial rise in surface area¹⁵.

Krill et al. derived a model describing the systematic reduction of interfacial energies from dopant segregation based on the Gibbs adsorption isotherm, and this model can potentially be applied to improve thermodynamic stability at the nanoscale^{18,19}. The model describes the relationship between interfacial energy and the concentration of a segregated species, B , as shown in **Equation 2**:

$$\gamma_s = \gamma_{s0} - \Gamma_B (RT \ln X_B - \Delta H_{seg}) \quad (2)$$

where γ_s is the surface energy of the doped material, γ_{s0} represents the surface energy of the undoped material, Γ_B is the solute excess at the interface, X_B is the concentration of the dopant, and ΔH_{seg} is the enthalpy of segregation of the dopant to the surface²⁰. The theory reflects the idea that dopants with spontaneous segregation enthalpies reduce the surface energy, thereby decreasing the driving force for coarsening.

Exploiting this concept, Hasan et al. observed limited coarsening in rare-earth doped magnesium aluminate, isostructural to zinc aluminate. After calcination at 1000°C, the specific surface area for La-doped magnesium aluminate remained ~50% larger than that of the undoped specimen²¹. Surface energy measurements revealed a reduction of ~0.3 J/m² in the doped samples that was attributed to the ion surface segregation. Similar studies don't exist in zinc aluminate, but Yang et al. showed evidence of grain growth inhibition in Al-rich zinc aluminate nanoparticles compared to the stoichiometric system²². Since excess Al commonly accumulates at spinel interfaces^{23–25}, the shift in zinc aluminate growth kinetics suggests that dopant segregation may induce a similar effect.

In this work, we study the effect of four different dopants [Sc³⁺ (74.5 pm), In³⁺ (80.0 pm), Y³⁺ (90.0 pm), and Nd³⁺ (98.3 pm)]²⁶ on the surface thermodynamics and stability of zinc aluminate nanoparticles. All dopants are isovalent with Al³⁺ but span a range of ionic radii to systematically assess the effect of the elastic strain energies (due to the size mismatch with Al³⁺) on the surface energetics²⁶. Atomistic simulations of a 4 nm nanoparticle consistently showed preferential Y³⁺ segregation to surfaces when substituting for Al³⁺ ions.

Experimental data on surface energies measured by water adsorption microcalorimetry confirmed the simulation trends, demonstrating reduced surface energies caused by Y-doping. Coarsening studies further showed the improved stability of Y-doped zinc aluminate, with the nanoparticles exhibiting reduced grain growth compared to their undoped counterparts. Fitting the data with the Ostwald ripening model leads to a better understanding of the synergistic effect of thermodynamic and kinetic effects on coarsening inhibition.

2. Methods and Experimental Procedures

2.1: Atomistic simulations on a 4 nm nanoparticle

The relative segregation potentials of four dopants (Sc³⁺, In³⁺, Y³⁺, and Nd³⁺) to zinc aluminate surfaces were investigated using molecular dynamics simulations of a 4 nm (3427 atom) nanoparticle. The structure was visualized in OVITO²⁷, and all calculations were performed with the LAMMPS²⁸ software using long-range Coulomb interactions and short-range Buckingham pair potentials as in **Equation 3**²⁹:

$$E = Ae^{-r/\rho} - \frac{C}{r^6} \quad (3)$$

where E is the potential energy of the short-range interaction between a pair of atoms, A , ρ , and C are coefficients unique to each atom pair, and r is the interatomic distance²⁹. Buckingham coefficients for all atomic pairs used in this study are included in **Table 1** below; a zero for the C parameter indicates that the interaction is dominated by the repulsion of inner-shell electrons. The short-range interactions of all cation-cation pairs were assumed to be zero as is standard practice in the literature^{30–33}. The practical justification for this is that since the ionic radius of all of the cations is less than that of oxygen, the requirement of local charge balance means that short-range cation-cation interactions are extremely unlikely, and neglecting such interactions does not preclude acceptable fits of the physical properties of the bulk material anyway.

Atom Pair	A (eV)	ρ (Å)	C (eVÅ ⁶)	Reference
O ²⁻ - O ²⁻	9548.0	0.2192	32.0	Grimes et al. ³¹
O ²⁻ - Zn ²⁺	529.7	0.3581	0	Grimes et al. ³¹
O ²⁻ - Al ³⁺	1725.2	0.2897	0	Grimes et al. ³¹
O ²⁻ - In ³⁺	1495.7	0.3327	4.3	Grimes et al. ³¹
O ²⁻ - Y ³⁺	1766.4	0.3385	19.4	Grimes et al. ³¹
O ²⁻ - Sc ³⁺	1575.9	0.3211	0	Busker et al. ³²
O ²⁻ - Nd ³⁺	3300.1	0.2868	20.8	Migliorati et al. ³⁴

Table 1: Buckingham pair potentials used for each cation-oxygen pair in the study derived by Grimes et al.³¹, Busker et al.³², and Migliorati et al.³⁴. All other interactions were set to zero as is standard practice in the literature^{30–33}.

The particle was built by replicating a zinc aluminate unit cell and appropriately deleting atoms while maintaining a net zero charge across the particle. The resulting nanoparticle was annealed at 1000°C for 4 ns to allow charge redistribution and surface restructuring, followed by a slow quench to absolute zero. After minimizing the quenched structure, its surface energy was calculated as the difference between the potential energy of the nanoparticle and the potential energy of a bulk structure containing the same number of stoichiometric units using **Equation 4**:

$$\gamma_{s0,MD} = \frac{1}{A} (E_{NP} - E_{bulk}) \quad (4)$$

Here $\gamma_{s0,MD}$ is the surface energy of the undoped 4 nm nanoparticle, A is the surface area of the nanoparticle, and E_{NP} and E_{bulk} are the potential energies of the nanoparticle and bulk structure with the same number of stoichiometric units³⁵.

A methodology developed after Hasan et al. was used to determine the segregation potential for each dopant in the system. The method assumes that the lowest energy defect is the substitution of a trivalent dopant for an Al^{3+} atom³⁵. A series of such dopant substitutions was performed on the nanoparticles, with a single dopant atom substituted in each Al^{3+} site followed by an energy minimization³⁵. Segregation energies were estimated for each surface site in the nanoparticle by taking the potential energy difference between a substitution in the bulk and one at each surface site (defined as a site within the outer 1 Å of the nanoparticle). The average of the surface segregation energies is reported as the surface segregation energy (E_{seg}) of the dopant in the zinc aluminate nanoparticle since the experimental system involves dopant concentrations beyond the dilute limit; at experimental concentrations, 10-25% of the trivalent surface sites would be occupied by Y^{3+} depending on the particle size.

Given the values of E_{seg} for each dopant, surface energies were calculated for 4 nm zinc aluminate nanoparticles doped at concentrations equivalent to those in the experimental systems using **Equation 5**:

$$\gamma_{s,MD} = \gamma_{s0,MD} - \frac{n}{A}E_{seg} \quad (5)$$

where $\gamma_{s,MD}$ is the surface energy of the doped nanoparticle, n is the number of dopants in the system (approximately 0.5 mol% Y_2O_3), and A is the surface area of the nanoparticle. While this definition of the surface energy does not include the effect of adsorbed gas atoms that are present in experiments, the main contribution to the segregation energy is expected to be the reduction of elastic strain energy by the migration of the dopant to the free surface. Since the magnitude of this strain energy reduction should be largely independent of any adsorbed gas atoms, the simulations are expected to predict the difference $\gamma_{s,MD} - \gamma_{s0,MD}$ in the surface energy between the undoped and doped samples more accurately than the absolute values of these quantities. A second reason why the surface energies calculated from simulations could deviate from the experimental data is due to complex defect chemistry not considered here (e.g., spinel site

inversion, kinetically driven self-segregation within the particle originating from the space charge layer, local dipole effects of Y_2O_3 complexes, etc.). Nonetheless, the trends in the segregation energies should provide useful information on the relative stabilities of the four dopants in zinc aluminate.

2.2: *Synthesis and nanopowder characterization*

Y-doped (YZAO) and undoped (ZAO) zinc aluminate nanoparticles were synthesized via a modified co-precipitation route^{22,36-38}. Prior to synthesis, water contents were measured for each nitrate precursor to ensure stoichiometry control. $Zn(NO_3)_2 \cdot 6H_2O$ and $Al(NO_3)_3 \cdot 9H_2O$ (Sigma Aldrich, >98%) were dissolved in deionized water in the metal stoichiometric molar ratio of 1:2. Hydroxides were precipitated using a 2 mol/L aqueous ammonia solution under a constant pH of 8.75 to inhibit the formation of $Zn(NH_3)_4^{2+}$: precipitation of this complex limits the number of Zn^{2+} ions in the solution leading to an Al-rich environment^{22,36-38}. Precipitates were washed thrice with ethanol and dried in an oven at 80°C for 48 hours. In the case of YZAO, $Y(NO_3)_3 \cdot 6H_2O$ (Sigma Aldrich, >98%) was also dissolved in the nitrate precursor solution to give 0.5 mol% Y_2O_3 . Upon drying, the hydroxide precipitates were ground into fine powders and calcined in a Thermo Scientific Lindberg/Blue M (Thermo Fisher Scientific Inc., Waltham, MA) box furnace at 550°C for 4 hours. Calcination temperatures were chosen to ensure complete crystallization while limiting grain growth^{22,36,39}.

Phase analysis and crystallite size measurements were performed on both sets of powders using X-ray diffraction (XRD) on a Bruker D8 (Bruker, Billerica, MA) operated at 40 kV, 40 mA (CuK α radiation, $\lambda=1.5406 \text{ \AA}$). Match! software (Crystal Impact, Bonn, Germany) with reference pattern #96-900-7021 (Levy et al.⁴⁰) was used to measure crystallite sizes for all X-ray analyses in this work. Errors associated with XRD-derived crystallite size measurements are on the order of 15-20%^{41,42} and are proportional to the true crystallite size.

As-synthesized powders were imaged using scanning transmission electron microscopy (STEM) on a JEOL-ARM300F Grand ARM (JEOL, Peabody, MA) to validate crystallite size measurements from XRD. Elemental mapping was performed on coarsened YZAO nanoparticles (900°C, 1 hour) using electron energy loss spectroscopy (EELS) to confirm Y^{3+} segregation to surfaces.

ZAO and YZAO powders were also analyzed by electron microprobe analysis (EMPA) with a Cameca SX-100 (Cameca, Gennevilliers, France) to compare Al:Zn ratios. Scans were taken at 10 different points on each sample and averaged to give Al:Zn ratios of 2.16 (± 0.14) and 2.11 (± 0.06) for ZAO and YZAO, respectively. These results confirmed that cationic ratios of both powders were within error of one another.

It has been well-documented that materials rich in Zn readily form carbonate species with CO₂ and moisture in air^{43,44}. Such species could potentially impact nanoparticle coarsening behaviors (e.g., by pinning interfaces), so Fourier transform infrared spectroscopy (FTIR) was performed using a Bruker Tensor 27 (Bruker, Billerica, MA) to screen particles for Zn-rich carbonates prior to coarsening. Samples were compared to a reference pattern for zinc carbonate.

2.3: *Coarsening experiments*

Before subjecting powders to coarsening experiments, each powder was treated in a box furnace (700°C, 4 hours, O₂ environment) to remove residual carbonate species which could potentially affect the results. All coarsening experiments were performed within 12 hours of that thermal treatment with powders being stored in a desiccator to prevent readsorption of carbonate species.

Powders were coarsened at two temperatures, 850°C and 950°C, in a Lindberg/Blue M (Thermo Fisher Scientific Inc., Waltham, MA) tube furnace for 0.5 min, 1 min, 5 min, 15 min, 30 min, 60 min, 120 min, and 240 min to study the effects of Y-doping on zinc aluminate's Ostwald ripening behavior. Limited grain growth was observed due to the moderate temperatures, so all grain sizes in this study could be measured from the XRD patterns and the microstructures were confirmed with electron microscopy.

2.4: *Surface energy measurements*

Surface stability was evaluated for ZAO and YZAO nanoparticles (cleaned at 700°C for 4 hours under O₂) by comparing surface energies measured by water adsorption microcalorimetry⁴⁵⁻⁴⁹. This technique is comprised of a water vapor dosing system (3Flex, Micromeritics Instrument Corp., Norcross GA) attached to a differential scanning calorimeter (Sensys Evo, Setaram Inc., France). After degassing at 400°C for 16 hours and a subsequent

series of three O₂ and vacuum cycles to ensure removal of adsorbed carbonate species, samples are dosed in the 3Flex with controlled amounts of water vapor (one μmol) until surfaces are fully saturated with water. While this is happening, the calorimeter records a series of peaks associated with water adsorption occurring with each dose; when taken together with the adsorption isotherm from the 3Flex, surface energies can be calculated using thermodynamic models developed by Castro and Quach⁴⁷.

In this study, approximately 20 mg of ZAO and YZAO powders (previously degassed at 700°C for 4 hours under an O₂ environment in addition to the degassing described above) were analyzed by water adsorption microcalorimetry to determine surface energies. Reported surface energies represent an average across all surfaces present in the examined powder and were collected from a single experiment for each powder while errors were calculated by assuming a 0.15% uncertainty in relative pressures in addition to a 2% uncertainty in BET surface areas⁴⁷.

3. Results and Discussion

3.1: Dopant selection by molecular dynamics

Molecular dynamics (MD) simulations were used to compare the surface segregation energies of four candidate dopants (Sc³⁺, In³⁺, Y³⁺, and Nd³⁺) in zinc aluminate. A 4 nm nanoparticle of undoped zinc aluminate was built and subsequently annealed at 1000°C for 4 ns during which it developed specific facets as indicated in **Figure 1**. The most prominent surface facets were on (100) and (111) planes which was expected since those have previously been identified as the lowest energy surfaces in spinel oxides⁵⁰⁻⁵².

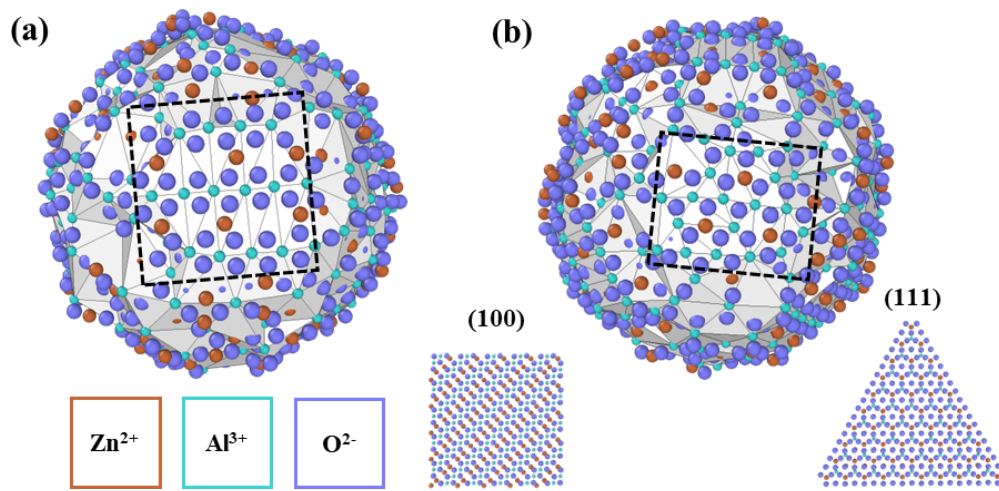


Figure 1: Different angles of the 4 nm zinc aluminate nanoparticle with Zn^{2+} , Al^{3+} , and O^{2-} represented in red, turquoise, and blue, respectively. Dashed lines highlight (a) (100) and (b) (111) surfaces that developed during an anneal at 1000°C for 4 ns. Inset images show reference structures for each of these planes. A surface mesh generated in OVITO²⁷ is overlaid on the nanoparticle.

The nanoparticle in **Figure 1** was used as the starting point for simulations of dopant segregation. A single dopant atom replaced Al^{3+} ions one at a time starting from the center of the particle, with the potential energy minimized after each replacement step. **Figure 2** summarizes the results, with all four dopants found to have positive segregation energies between 0.3-3.0 eV per dopant atom. These energies are comparable to those calculated by Hasan et al. for magnesium aluminate using two planar surfaces³⁵. The positive segregation energies indicate that zinc aluminate nanoparticles are in a lower energy state when dopants substitute at surface sites as opposed to the interior, suggesting that these dopants would all likely undergo surface segregation during synthesis. Y^{3+} had the highest segregation energy of all dopants considered at 2.78 eV with a corresponding surface energy (assuming 0.5 mol% Y_2O_3) of 1.50 J/m^2 , about 0.04 J/m^2 lower than the undoped nanoparticle.

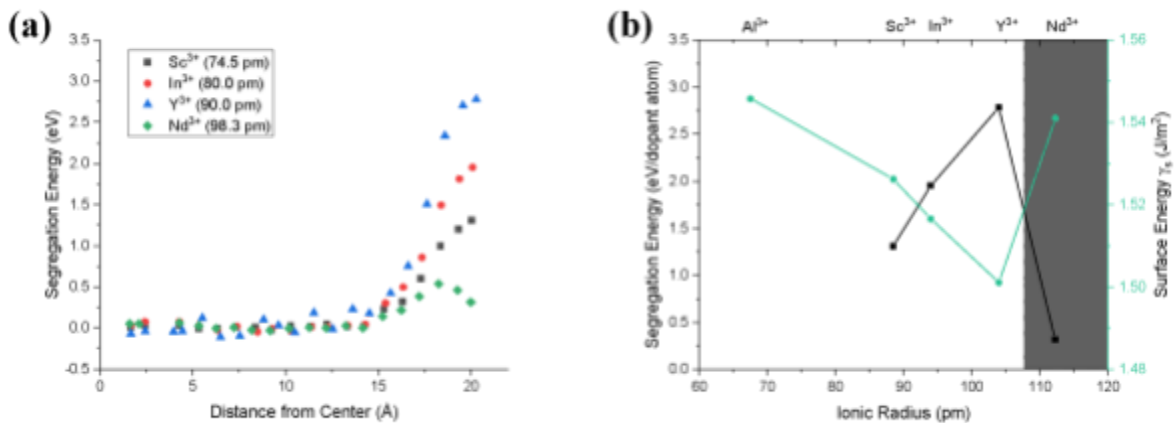


Figure 2: (a) Segregation energies for Sc^{3+} , In^{3+} , Y^{3+} , and Nd^{3+} in zinc aluminate as calculated using molecular dynamics simulations of a 4 nm nanoparticle. Energies are binned by distance from the center the particle. (b) Segregation (black) and surface (green) energies plotted against ionic radii for each cation type. A Y_2O_3 concentration of 0.5 mol%, was used to estimate surface energies. Surface energies decrease as dopant ionic radius increases, though this trend breaks down for Nd^{3+} .

In general, the decrease in surface energies is attributed to the elastic strains that arise due to ionic size mismatch in the lattice being relieved by the presence of a free surface³⁵. Unlike previous studies³⁵, the proportionality between the segregation energy and the ionic radius broke down for the largest studied ion, Nd³⁺, which showed the lowest segregation energy. No such breakdown has been reported in computational or experimental studies on interfacial segregation of dopants before this. The limited surface segregation for Nd³⁺ compared to Y³⁺ can be explained by comparing the nearest neighbors for both dopants in the bulk. Y³⁺ and Nd³⁺ have the same coordination in the bulk where both are surrounded by six O²⁻ nearest neighbors; however, the nearest neighbors are ~0.1 Å closer to Nd³⁺ atoms than Y³⁺ atoms. This decrease in nearest neighbor distance for Nd³⁺ is associated with enhanced stability in the bulk compared to Y³⁺ which limits surface segregation. This change in nearest neighbor distance is perhaps due to the complex f orbital behavior found in Nd³⁺ which reportedly leads to a seven-fold coordination in neodymium oxide⁵³.

The molecular dynamics studies also provide critical insight into the local environments that support the excess elastic strain caused by doping zinc aluminate with Y³⁺. **Figure 3** shows two angles of the 4 nm zinc aluminate nanoparticle with a surface mesh color-coded to represent the segregation energy of Y³⁺ to the nearest trivalent surface sites. **Figure 3a** shows a (100) facet that developed during the annealing and quenching process; the light blue coloring that spans the entire facet indicates low segregation energies (1.3-1.5 eV) of Y³⁺. In fact, low segregation energies for highly ordered sites are found throughout the particle: **Figure 3b** shows another (100) facet where certain trivalent sites have low segregation energies (e.g., site (ii)).

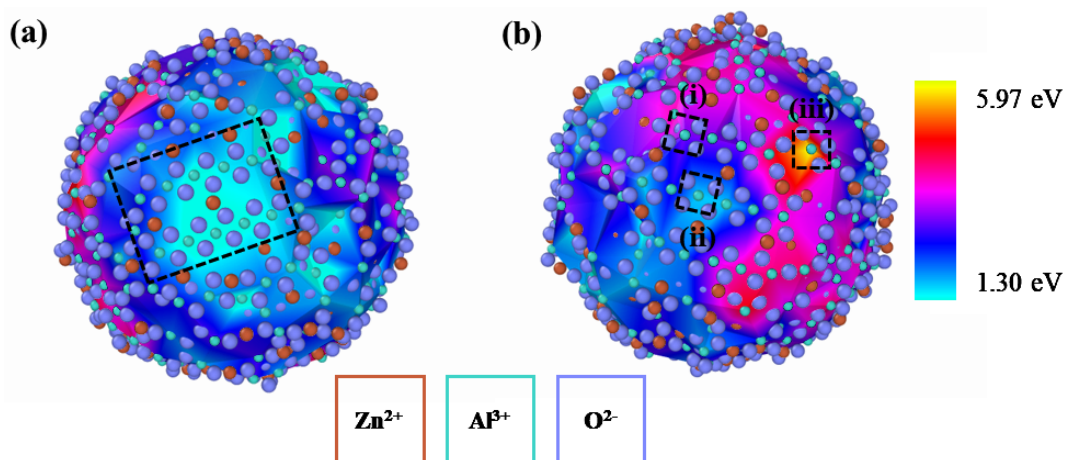


Figure 3: Two angles of the 4 nm zinc aluminate particle with a color gradient representing the segregation energies of Y^{3+} to trivalent surface sites. (a) A dashed (100) surface plane with relatively low segregation energies. (b) Three Al^{3+} sites with distinct energies of (i) 3.02 eV, (ii) 1.61 eV, and (iii) 5.97 eV where sites (i) and (ii) lie in a (100) facet.

Further examination of the facet in **Figure 3b** reveals a wider spread of energies than for the one in **Figure 3a** though. Sites (i) and (ii) are near the same facet and are surrounded by similar local environments but have segregation energies of 3.02 eV and 1.61 eV, respectively. This energy difference between similar sites highlights the role of nearest neighbor coordination on dopant segregation energies: the O^{2-} atoms neighboring site (ii) are near the center of the facet and highly coordinated relative to those in site (i), allowing the presence of the free surface to relieve less of the elastic strain induced by substitution of Y^{3+} . This is even more apparent in site (iii), which has lower coordination than the other two sites (only three O^{2-} atoms on the surface), resulting in a segregation energy of 5.97 eV.

This relationship between segregation energies and relative positions of sites on the surface (i.e., proximity to facets and nearest neighbor coordination) predicts that Y^{3+} will preferentially segregate to sites with lower coordination. This idea has been proposed in the literature⁵⁴ and is consistent with the fact that defects present at edges and corners directly impact nanoparticle surface energies, as demonstrated by Hummer et al. for titanium oxide⁵⁵. These effects tend to be less pronounced for particle sizes larger than ~ 7 nm, suggesting that the segregation trends predicted here by molecular dynamics could change as zinc aluminate nanoparticles enlarge, facets develop, and the density of ledges is reduced. Explicit investigation of this size dependence is beyond the scope of the current study.

3.2: *Synthesis and coarsening study*

Based on the segregation energies by atomistic simulations, Y^{3+} shows the most potential to segregate to zinc aluminate interfaces, and hence was selected for further experimental studies. X-ray diffraction patterns (**Figure 4**) of undoped (ZAO) and Y-doped (YZAO) zinc aluminate nanoparticles synthesized by co-precipitation revealed both sets of powders consisted of a single spinel phase. Crystallite sizes were calculated at 5.9 and 6.5 nm for doped and

undoped nanoparticles, respectively. These results were consistent with exemplary TEM images of both sets of nanoparticles shown in **Figure 4b** and **Figure 4c**.

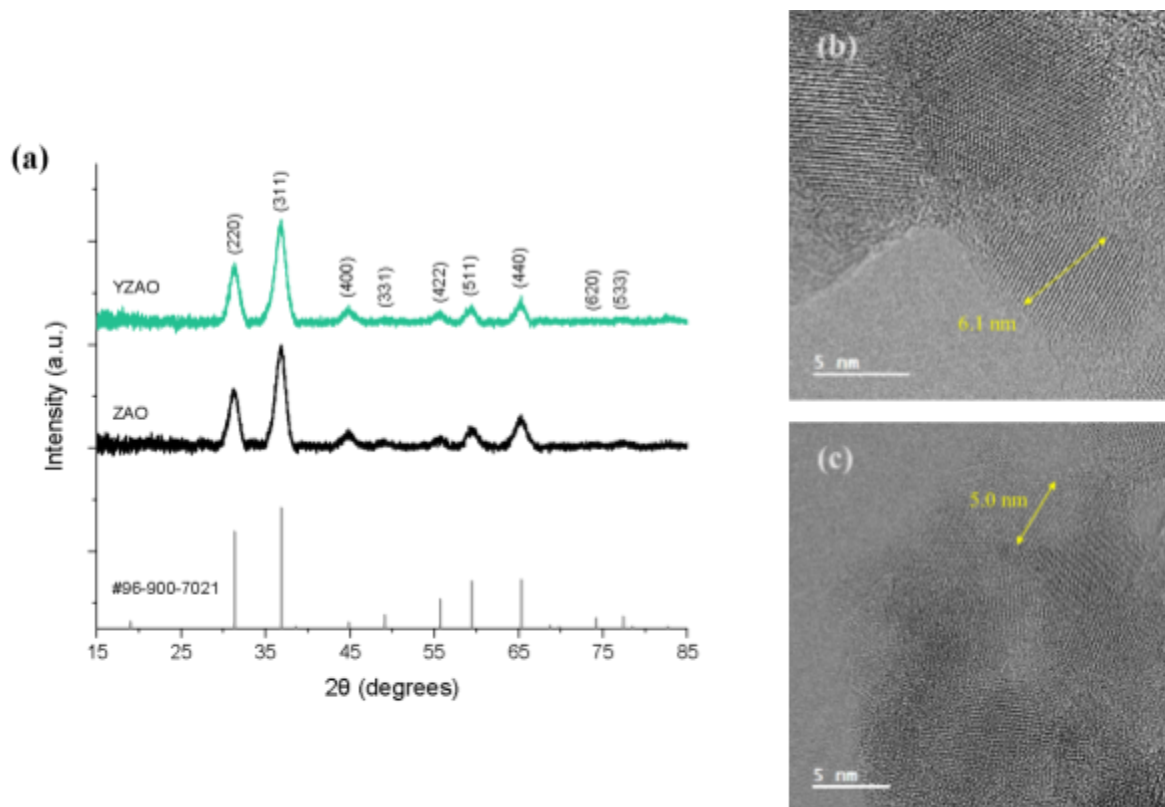


Figure 4: (a) X-ray diffraction patterns of ZAO (black) and YZAO (green) nanoparticles calcined at 550°C for 4 hours along with reference pattern #96-900-7021 from Levy et al.⁴⁰, (b) bright field transmission electron microscopy (TEM) images of ZAO nanoparticles, and (c) of YZAO nanoparticles. XRD peaks and TEM images both confirm particles exhibit a single spinel phase along with uniform crystallite sizes in the nanoscale.

Since zinc and yttrium are likely to form stable carbonate structures, both doped and undoped nanoparticles were screened for surface carbonate species using FTIR spectroscopy prior to further studies. ZAO and YZAO prepared at 550°C and 700°C (under O₂) for 4 hours were compared to a zinc carbonate standard. **Figure 5** shows that both ZAO and YZAO nanoparticles contain zinc carbonate peaks at about 1480 and 135 cm⁻¹ when calcined at 550°C. The broad peak around 1630-1650 cm⁻¹ in both patterns is attributed to the vibration of adsorbed water⁵⁶. Each of the three peaks is absent in ZAO cleaned at 700°C, confirming these conditions are appropriate for removing zinc carbonates in zinc aluminate. YZAO nanoparticles treated at 700°C still showed two low-intensity broad peaks at lower wavenumbers. However, the shift in

peaks' positions indicates the carbonate groups are now only physically bonded CO_2 , absorbed during transferring of the samples from the furnace to the FTIR spectrometer⁵⁷. Because they are loosely bound, such carbonates should have a negligible effect on coarsening and water adsorption studies as we assume the exposure to elevated temperatures (850°C and 900°C in coarsening experiments and degassing at 400°C for 16 hours) for even short times should effectively remove these species.

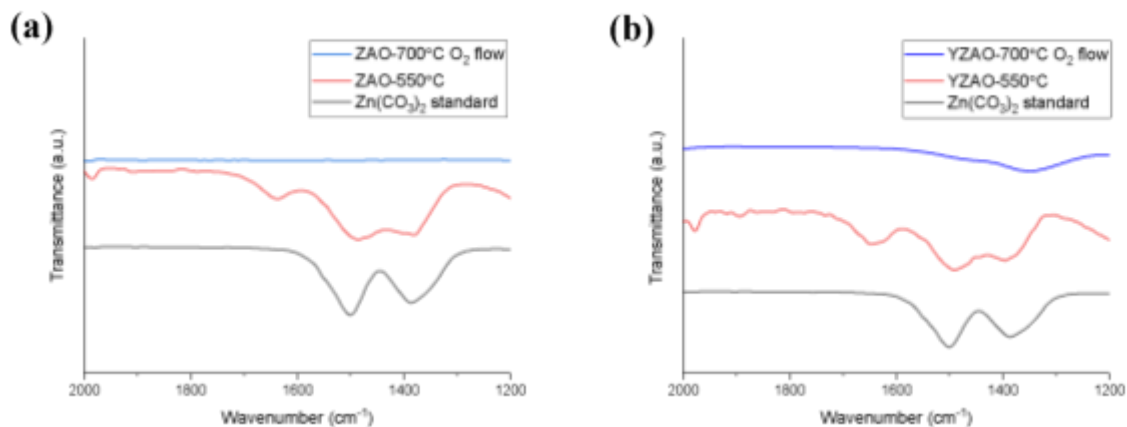


Figure 5: FTIR scans of: (a) ZAO calcined at 550°C for 4 hours, at 700°C under O_2 flow for 4 hours, and a zinc carbonate standard; (b) YZAO prepared under the same conditions. Zinc carbonate shows two characteristic peaks around wavenumbers 1481 and 1385 cm^{-1} which are also present in ZAO and YZAO calcined at 550°C . A broader peak from 1630 - 1650 cm^{-1} was also found in both sets of powders at 550°C as a result of vibrations from water adsorbed to particle surfaces⁵⁶.

ZAO and YZAO nanoparticles were coarsened at 850°C and 900°C for up to 4 hours to analyze the effects of doping on the coarsening behavior. ZAO and YZAO crystallite sizes were measured at 13.0 and 13.3 nm , respectively, after the annealing (cleaning) at 700°C . **Figure 6** shows typical coarsening patterns for both samples, with fast grain enlargement in the early stages of coarsening and a plateau at longer times, dependent on temperature and composition. ZAO nanoparticles coarsened to an average diameter of 24.5 nm when subjected to a temperature of 850°C for 4 hours, while YZAO only grew to 19.0 nm . Similarly, at 900°C , ZAO underwent more growth (29.8 nm) than YZAO (22.6 nm) after 4 hours. The coarsening curves at both temperatures show a difference in growth behaviors for doped and undoped nanoparticles

where YZAO particles undergo limited growth, potentially due to enhanced surface stability from Y^{3+} segregation, as discussed further below.

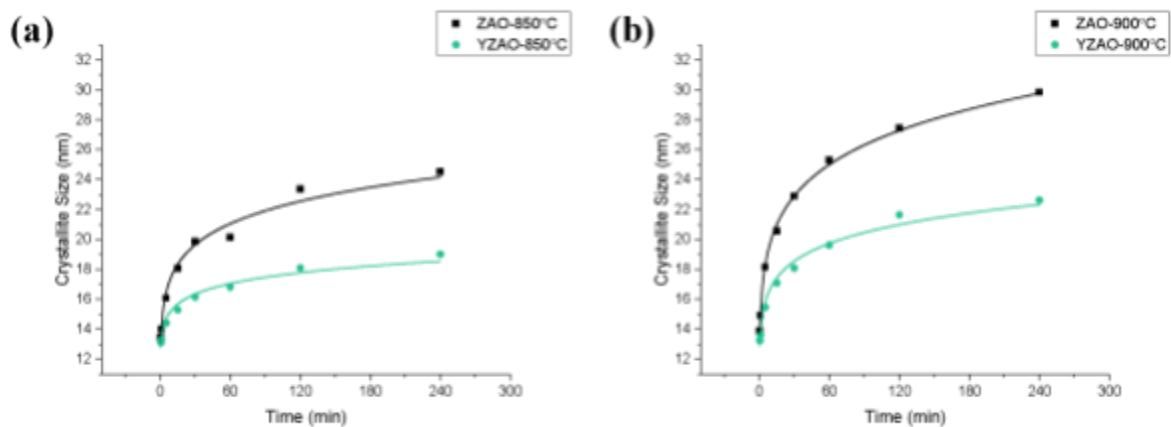


Figure 6: Coarsening curves at (a) 850°C and (b) 900°C for clean ZAO and YZAO powders with crystallite sizes estimated using XRD. YZAO particles grow less than 1 nm between 2 and 4 hours at 850°C while ZAO continues growing up until the 4-hour mark, with a similar trend found in data collected at 900°C. These results indicate doped nanoparticles undergo limited growth relative to their undoped counterparts which may be attributed to surface segregation of dopants. Expected errors in crystallite size measurements are between 2-5 nm depending on coarsening time.

3.3: Surface stability characterization

Anhydrous surface energies of clean ZAO and YZAO were measured using water adsorption microcalorimetry to understand the difference in coarsening behaviors and directly test the predicted reduction of surface energies. The method uses water as a probe for surface reactivity and thermodynamic models to correlate the heat of adsorption to the surface energies of the particles. **Figure 7** shows the adsorption isotherm and the enthalpies of water adsorption for ZAO and YZAO. In **Figure 7a**, a typical type-II isotherm demonstrates water molecules adsorbed strongly to surfaces at low pressures, consistent with a chemisorption process (i.e., dissociative), with a change in slope above a relative pressure of 0.05. As shown in the inset, Y-doped samples show slightly lower slopes, consistent with lower surface reactivities. As the adsorption progresses, the curves converge as water adsorption becomes more physical (i.e., without dissociation). The small step at 0.4 is an artificial inconsistency caused by an automatic

shift in the pressure gauge (equipment feature). **Figure 7b** shows the enthalpies of adsorption as a function of water coverage. For both samples, the water reactivity is high at low water coverages, attributed to dissociation reactions, and decreases with increasing coverage of the surface. Generally, more exothermic heats at similar coverages are observed in ZAO compared to YZAO, indicating improved surface stability (less reactivity) of Y-doped zinc aluminate nanoparticles.

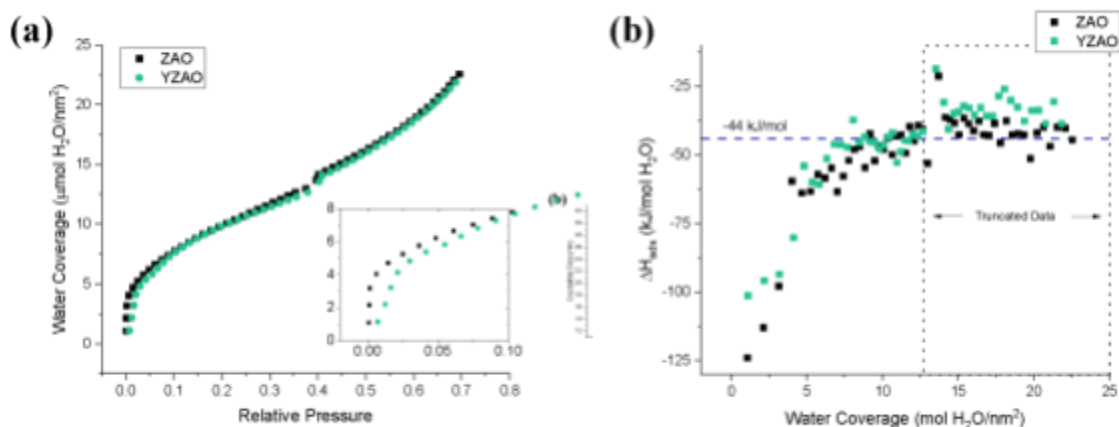


Figure 7: (a) Adsorption isotherm and (b) enthalpies of adsorption as a function of surface coverage for both ZAO and YZAO nanoparticles obtained via water adsorption microcalorimetry with a horizontal dashed line at the heat of liquefaction of water (-44 kJ/mol)⁴⁶. The dotted line encloses data that was neglected for surface energy measurements due to low (in magnitude) heats of adsorption resulting from a combination of heat effects. Lower (in magnitude) enthalpies of adsorption in YZAO imply enhanced surface stability upon doping.

After successive dosing, the enthalpies of water adsorption converged to the enthalpy of liquefaction of water which has a theoretical value of -44 kJ/mol ⁴⁶. In **Figure 7b**, both ZAO and YZAO particles initially plateau at -44 kJ/mol between coverages of $10.5\text{--}12.5 \text{ mol H}_2\text{O}/\text{nm}^2$ but then continue to decrease in magnitude past this point. This decrease signals a different endothermic reaction taking place throughout the process of physical water adsorption, such as the formation of yttrium and zinc hydroxides on the surface, which is thermodynamically favorable^{58,59}. These additional processes convolute the heat effects at high coverages, making it difficult to determine the enthalpy of water adsorption. Because processes like hydroxide formation have relatively slow kinetics at room temperature and neutral pHs, we assume these

reactions are negligible at low coverages and that both sets of data can be safely truncated prior to the endothermic event at 12.5 H₂O/nm² to allow for quantitative analysis of the heat of adsorption. This approach still allows for an accurate surface energy calculation, as detailed by Castro and Quach⁴⁷ and later by Drazin and Castro⁴⁶. Therefore, anhydrous surface energies were calculated for both samples using the thermodynamic model for water adsorption developed by Castro and Quach⁴⁷. This method uses a thermodynamic description of the adsorption of water to the surfaces of particles whereby the free energy of the system is reduced as water adsorption progresses. If the bulk energy is unaffected by the adsorption process and one assumes negligible entropic and PV terms, the surface energy change can be calculated by:

$$\gamma_{s,\theta} = \gamma_s + \theta \cdot \Delta H_{ads} \quad (6)$$

where ΔH_{ads} is the measured heat of adsorption, γ_s is the anhydrous surface energy, and $\gamma_{s,\theta}$ is the surface energy at a given surface coverage, θ . To minimize the contributions from the chemical potential of water, the surface energy was assumed to be equivalent to the surface energy of liquid water, 0.072 J/m², at the point where the heat of adsorption converged to -44 kJ/mol. Beyond this point, adsorption peaks represent water molecules adhering to layers of water on the surface⁴⁶. This procedure allowed the heat of adsorption data to be used to calculate the anhydrous surface energies of both sets of nanoparticles as with other nanocrystalline oxides^{45,47,48,60}.

The calculations resulted in surface energies of 0.99 (± 0.02) and 0.85 (± 0.02) J/m² for ZAO and YZAO, respectively. The decrease in measured surface energy for YZAO relative to that of ZAO suggests that surface stability is enhanced by doping zinc aluminate with Y³⁺, further supporting the predictions from molecular dynamics simulations.

As simulations suggest that the cause of the reduced surface energies is dopant segregation to the surfaces, EELS mapping was performed on coarsened YZAO particles to analyze the segregation behavior of Y³⁺. Shown in **Figure 8** are the EELS maps (**Figure 8a**) and the results from successive box scans on an individual Y-doped nanoparticle (**Figure 8b**). Due to its low concentration, it is difficult to visualize Y³⁺ in the EELS map, but it is apparent that Al³⁺ ions have accumulated in the vicinity of the surface as is evident from the purple shade. This is supported by the results from the box scans, which show that there is Al³⁺ enrichment (represented in red) within 3 nm of the surface edge, corroborating reports of excess Al

segregating to interfaces in Al-rich spinels^{22,24,25}. The box scans further reveal that this region is depleted in Y^{3+} , but as we move toward the surface edge, the spectrum detects a sharp increase in Y^{3+} . This increase in Y^{3+} concentration coincides with a lowering of Zn^{2+} and Al^{3+} , further validating the claims of Y^{3+} segregation to zinc aluminate surfaces. It is important to observe that the defect chemistry involved in the segregation of Y^{3+} to the surface is significantly more complex than is indicated by the molecular dynamics simulations. Namely, the presence of the surface has an effect on ion distribution in a layer roughly 3 nm thick because of the redistribution of Al^{3+} and Y^{3+} . The Zn^{2+} distribution remains primarily constant, suggesting Y^{3+} and Al^{3+} share octahedral sites in the spinel structure. Presumably the large ionic radii of Y^{3+} atoms generate large lattice strains which drive them toward the surfaces and force Al^{3+} to redistribute accordingly. All of that said and despite the simplified defect chemistry, molecular dynamics did effectively predict the segregation of Y^{3+} .

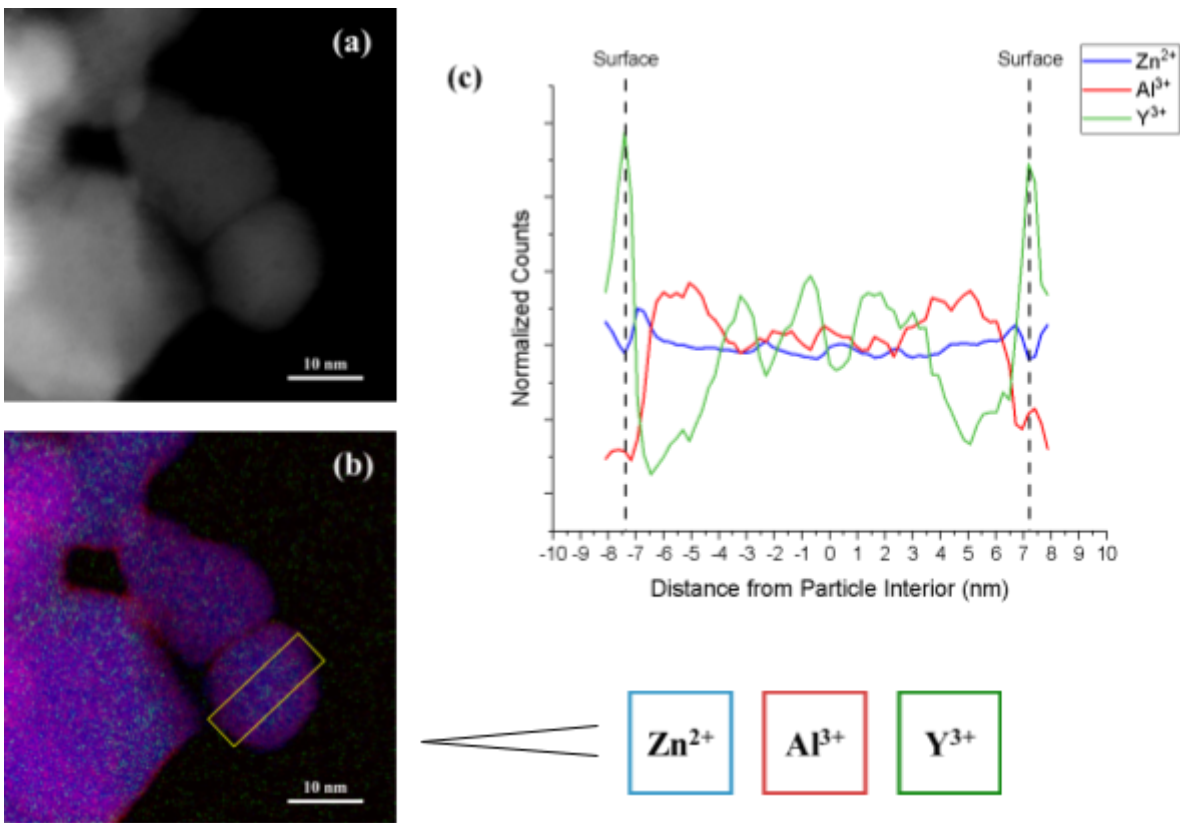


Figure 8: (a) Dark field TEM image of YZAO nanoparticles coarsened at 900°C for 1 hour, (b) elemental map of Zn^{2+} (blue), Al^{3+} (red), and Y^{3+} (green) taken with EELS, and (c) normalized counts of each zinc aluminate cation measured by successive box scans across the region boxed in yellow. The EELS map indicates there are two layers near the particle surfaces with different

compositions than the bulk: approximately 3-6 nm away from the center of the particle, there is an increase in Al^{3+} content and a depletion of Y^{3+} followed by a spike in Y^{3+} at the surface. Al^{3+} enrichment near the particle surfaces is also visible in the colored map (b).

3.4: Discussion

Ostwald ripening theory states that particle growth should follow a cubic time dependence as outlined in **Equation 1**. The equation indicates that there are two main parameters to potentially control grain enlargement: the surface energy and the diffusion coefficient. There is limited work focused on decoupling these parameters to provide a holistic understanding of coarsening control. To that end, each coarsening curve for doped and undoped zinc aluminate was plotted with a cubic dependence in **Figure 9**.

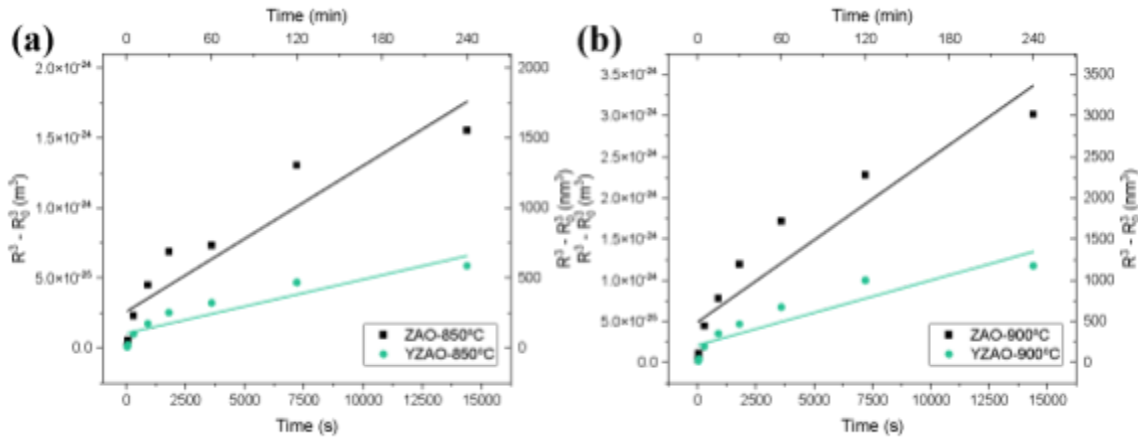


Figure 9: Coarsening data for both compositions at (a) 850°C and (b) 900°C plotted according to the Ostwald ripening equation¹⁷. A linear fit is overlaid on each set of data, although crystallite sizes deviate from this fit at both short and long times.

The linear approximation in **Figure 9** overestimates crystallite sizes at short times (less than 5 minutes) and underestimates them at longer times. The fact that this crossover is present in all four curves suggests that either (1) the growth mechanism transitions from Ostwald ripening to a slower mechanism (e.g., migration and coalescence) as the particles enlarge, or (2) the defining rate constant for Ostwald ripening changes throughout the coarsening process.

Shifts in growth mechanisms involving Ostwald ripening have been reported in the past for metal nanoparticles^{14,61}. Hansen et al. observed nickel nanoparticles in a magnesium aluminate matrix under a TEM, where they noticed particle migration and coalescence even 13

seconds after being exposed to elevated temperatures¹⁴. A transition in growth mechanisms is a consequence of a change in the relative activation energies for two mechanisms; in the case of the nickel nanoparticles, the transition from Ostwald ripening to migration and coalescence was attributed to a severe decrease in vapor pressure as the particle sizes increased¹⁴. Shifts away from Ostwald ripening are more likely in metals than ceramics though since ceramic vapor pressures are much lower than in metals even at the nanoscale⁶², meaning that ripening likely occurs via different transport mechanisms than in metals. Additionally, these types of transitions typically lead to sharp changes in the rate of crystal growth with time⁶¹. The coarsening curves in **Figure 6** instead show gradual changes in growth rate for both compositions at 850°C and 900°C, implying that the observed zinc aluminate growth behavior is unlikely to be due to a change in the dominant growth mechanism. Instead, the crossover in the Ostwald ripening curves is attributed to a gradual decrease in the rate constant throughout the growth process that could result from a reduced diffusion coefficient or a continuous decrease in surface energies as particles grow.

For the purposes of comparing the effects of dopant segregation on the coarsening behaviors of doped and undoped zinc aluminate nanoparticles, we assume that changes in growth mechanisms and/or rate constants (i.e., surface energies) are negligible within the first five minutes of coarsening. Data before and at five minutes was used to calculate self-diffusion coefficients for both samples at 850°C and 900°C using a modified version of the Ostwald ripening rate constant developed by Lifshitz et al. which assumes atmospheric air acts as an ideal gas:

$$K = \frac{8\gamma_s P V_m^2 D}{9R^2 T^2} \quad (7)$$

where γ_s is the surface energy, P is the vapor pressure, V_m is the molar volume, D is the diffusion coefficient of the material, R is the ideal gas constant, and T is the temperature¹⁷. Although the ideal gas assumption is questionable at room temperature, these calculations still provide a basis for comparing the kinetics of Ostwald ripening in both zinc aluminate samples. Diffusion coefficients for ZAO and YZAO along with experimental and computational surface energies are summarized in **Table 2**. Diffusion coefficients calculated for both undoped and Y-doped zinc aluminate are on the order of 10^{-12} cm²/s which agrees well with diffusion coefficients calculated

for other solids at homologous temperatures^{63,64}. Juxtaposing these values makes it evident that self-diffusion is faster in undoped zinc aluminate than Y-doped zinc aluminate at both temperatures.

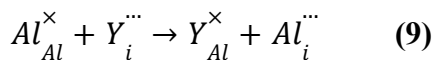
Dopant Content	γ_s (J/m ²)	$D_{850^\circ\text{C}}$ (cm ² /s)	$D_{900^\circ\text{C}}$ (cm ² /s)
Undoped	0.99 (± 0.02)	4.8×10^{-12}	10.1×10^{-12}
0.5 mol% Y ₂ O ₃	0.85 (± 0.02)	2.5×10^{-12}	5.1×10^{-12}

Table 2: Surface energies and self-diffusion coefficients calculated for Y-doped and undoped zinc aluminate nanoparticles.

On the atomic scale, a change in diffusion coefficient for YZAO represents a change in the rate-controlling defect for zinc aluminate self-diffusion. This defect can be identified experimentally by calculating activation energies for self-diffusion from coarsening studies and comparing them with literature values for defect formation energies. However, the present coarsening studies were limited to two temperatures which would skew such calculations. Unfortunately, to the best of our knowledge, no work has been done to identify the defects that dominate diffusion in zinc aluminate. Ting et al. found diffusion in magnesium aluminate to be controlled primarily by Schottky defects, with oxygen vacancies being the slowest diffusing species⁶⁵. Given that magnesium aluminate is isostructural with zinc aluminate (spinel), it is reasonable to assume defect formation energies to be similar. Hence, the dominant defect reaction in zinc aluminate is assumed to be:

$$\Phi = V_{Zn}'' + 2V_{Al}'' + 4V_O'' \quad (8)$$

with oxygen vacancies being the rate-controlling species. This would corroborate the trends in diffusion coefficients between doped and undoped samples: because oxygen vacancies are positively charged defects, cationic dopants in zinc aluminate (e.g., Y³⁺) would prevent the formation of oxygen vacancies and thereby limit diffusion. Furthermore, the positive charge caused by excess Y³⁺ in the surface layer would need to be accommodated by negatively charged defects²³. A candidate defect reaction is the delocalization of Al³⁺:



which would likely be compensated by site inversion with the tetrahedral site, similar to magnesium aluminate²³. Some accumulation of Al³⁺ is already found in the elemental maps in **Figure 8**, supporting the idea that this series of defects could be leading to the distinct diffusive properties of ZAO and YZAO.

4. Conclusions

This work focused on the possibility of tailoring the growth behavior of zinc aluminate nanoparticles by tuning the thermochemistry of surfaces. Molecular dynamics simulations indicated that among several trivalent dopants, Y³⁺ was the most likely to segregate to nanoparticle surfaces. Despite the limitations of the simulations, synthesized zinc aluminate doped with 0.5 mol% Y₂O₃ indeed showed excess Y³⁺ located at the particle surfaces along with a more complex distribution of ions in the near-surface regions. Al³⁺ ions were depleted at the surface edge but enriched in the immediate vicinity (within 3 nm). Water adsorption microcalorimetry estimated a reduction in surface energy for doped samples consistent with the segregated Y³⁺. Coarsening studies at 850°C and 900°C demonstrated that doped (YZAO) nanoparticles exhibit more resistance to coarsening compared to undoped (ZAO) nanoparticles. This behavior results from a combination of a reduced surface energy with increasing particle size for coarsening and a decrease in the diffusion coefficient, with the latter likely stemming from the unique chemistry in the surface regions impeding the formation of the rate-limiting defect in zinc aluminate. The present work represents an important step toward controlling the coarsening behavior of nanoparticles to enable the design of stable catalytic materials.

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