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# Placeholder structure and numerical computation

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## Introduction

This symposium explores the role of placeholder structures—systems of words, non-linguistic symbols, or procedures—in the construction and manipulation of numerical concepts. The structure supplied by a placeholder system – like the count list in English – critically constrains the potential for creating and manipulating conceptual content.

A great deal of empirical work has explored the role of placeholders in numerical cognition, in large part by investigating how children learn number word meanings when exposed to Arabic numerals and corresponding count routines (for review see Carey, 2009). One contribution of this work has been to suggest that learning a count list creates an important structure for constructing new numerical concepts. For example, learning to count is a critical precursor to acquiring large exact numerical concepts like “77”, and how such concepts are related (e.g., that 78 is greater than 77, by exactly one). According to some, this learning is guided by a semantic induction, whereby children realize that each successive numeral in the count list denotes a quantity of 1 more than the number that came before it.

Beyond these studies, relatively little work has tested the role of placeholder structures outside the Arabic numeral system. As a result, little is known about the role that this particular structure plays in numerical development, and whether the use of alternative systems might result in different conceptual outcomes. Perhaps the best evidence that placeholder structures are critical to constructing numerical concepts comes from fieldwork in the Amazon, where studies of the Piraha and Mundurucu have made clear that learning to count is important to acquiring at least some numerical concepts (Gordon, 2004; Frank et al, 200; Pica et al.). However, between the Piraha and English-speaking adults who use Arabic numerals lies a vast array of potential intermediate systems. At least some of these systems have been tested in nature by humans, and are used today. This symposium explores the role of placeholders systems to numerical development, the effects of structural variations, and how different modalities like gesture and vision are used to create alternatives to the Arabic numeral system, with different consequences for cognition.

Specifically, the symposium will include four distinct talks, each touching on different systems of numerical representations. Each talk will discuss how placeholder structures guide and constrain learning, whether by facilitating the association of symbols with quantities, guiding inductive inferences, or facilitating operations that are unique to a particular structure.

## Number word meanings and the count routine

What role does a placeholder system like counting play as children learn number word meanings? In this talk, Barner will explore the idea that counting provides one of several verification procedures that children acquire when learning number words. Acquiring these procedures does not alone result in conceptual change, but instead lays the groundwork for learning about quantity and the logical relations between numbers. In particular, Barner will discuss how learning about the structural relationship between words in the count list may allow children to derive the concept of exactness, without a radical conceptual change, but instead drawing on well-attested pragmatic inferences. Barner also explores the so-called “Cardinal Principle induction” and whether it involves a conceptual change, or whether it is instead another example of procedural learning.

## Number knowledge in a finite counting system

In this talk, Frank presents research examining a linguistic number representation used by a group of indigenous speakers of the language Momu (also known as Fas), spoken in the northern part of Papua New Guinea near the Indonesian border. The Momu count list has been reported to have a simple pair-based compositional structure that can be glossed as “one” (1), “two” (2), “two and another” (3), “two two” (4), “two two and another” (5), and “two two two” (6). The Momu count list is a fascinating case study of the relationship of placeholders to numerical competence.

Most Momu speakers had difficulty completing exact quantity matching tasks, failing to use linguistic number to track the quantity of objects presented by an experimenter. Even more surprising, Momu speakers did not agree on the structure of the Momu count list. Some speakers were able to count recursively to ten using the pair-based structure described above, while others claimed that the system was finite and bounded at “two and another” (3). The participants that did best on the matching tasks used the



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