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DIURNAL TEMPERATURE AND PRESSURE EFFECTS ON AXIAL TURBO-MACHINERY STABILITY IN SOLID OXIDE FUEL CELL-GAS TURBINE HYBRID SYSTEMS

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ABSTRACT

A dynamic model of a 100 MW solid oxide fuel cell-gas turbine (SOFC-GT) hybrid system has been developed and subjected to perturbations in diurnal ambient temperature and pressure as well as load sheds. The dynamic system responses monitored were the fuel cell electrolyte temperature, gas turbine shaft speed, turbine inlet temperature and compressor surge. Using a control strategy that primarily focuses on holding fuel cell electrolyte temperature constant and secondarily on maintaining gas turbine shaft speed, safe operation was found to occur for expected ambient pressure variation ranges and for ambient temperature variations up to 28 K, when tested non-simultaneously. When ambient temperature and pressure were varied simultaneously, stable operation was found to occur when the two are in phase but not when the two are out of phase. The latter case leads to shaft over-speed. Compressor surge was found to be more likely when the system is subjected to a load shed initiated at minimum ambient temperature rather than at maximum ambient temperature. Fuel cell electrolyte temperature was found to be well-controlled except in the case of shaft over-speeds. Turbine inlet temperature remained in safe bounds for all cases.

INTRODUCTION

The need for advanced coal based power generation has led to the concept of an integrated gasification fuel cell system (IGFC). The main power block in this system is comprised of a solid oxide fuel cell (SOFC) integrated with a gas turbine (GT) operating on coal syngas. Detailed descriptions of such an integrated hybrid cycle or of a simple-cycle solid oxide fuel cell (SOFC) operating on coal syngas have been outlined in the literature [1-4]. The main benefits of IGFC systems are that they allow operation on an abundant and cheap fuel and by using syngas in place of solid coal many of the toxic emissions associated with coal based power generation are removed. Additional benefits include very high electrical efficiencies that are possible by using a SOFC-GT

hybrid system [5-14], and the separated anode and cathode flows of a fuel cell that more readily enable carbon concentration for sequestration. Finally, synergies between the SOFC and various gasifiers can be exploited to further increase overall system efficiency. One such potential synergy involves creating a higher methane content syngas, which improves the cold-gas efficiency of the gasifier. This is accomplished via internal reformation within the fuel cell, which provides a means of fuel cell cooling; reducing the excess air required for cooling and averting the associated parasitic losses.

In this study a dynamic Simulink model of a 100 MW SOFC-GT operating on coal syngas is subjected to perturbations from steady state operation and the dynamic response is observed. The goals of the study are to establish and quantify the dynamic response of the turbo-machinery in hybrid SOFC-GT power blocks designed for use in IGFC applications, and, to delineate failure mechanisms and the means to mitigate failure mechanisms. The authors are unaware of any published research that characterizes the dynamic performance of turbo-machinery applied to a SOFC-GT in an IGFC system. The model approach, developed by the National Fuel Cell Research Center (NFCRC) for these purposes, has been extensively peer-reviewed and validated using dynamic experimental data from a 220 kW Siemens-Westinghouse SOFC-GT system tested at the NFCRC [15-24].

MODEL AND OPERATING CONDITIONS

The SOFC-GT system model is diagrammed in Figure 1. Coal syngas is fed to the fuel cell, while un-utilized fuel is combusted and the hot gases are expanded through a turbine to power a generator and compressor that supplies air to the fuel cell. It is assumed that the fuel cell is designed in such a way as to preheat the incoming air and fuel. This strategy was employed in the Siemens-Westinghouse design referenced above and most other fuel cell system designs. Air preheating is principally accomplished using a cathode blower that recirculates hot cathode exhaust and mixes it with the air exiting the compressor.

Figure 1. SOFC-GT hybrid system, utilizing a blower for cathode recirculation.

The composition of the coal syngas is shown in Table 1. It is predominantly composed of hydrogen with only minor fractions of methane and carbon monoxide. The reason that the nitrogen, water and carbon dioxide fractions are so low is that the cryogenic air separation, dehydration and carbon dioxide removal steps, respectively, are carried out in the gasifier to enable carbon sequestration. A detailed model description of the gasifier and other cycle components is outside the scope of this paper that focuses upon the SOFC-GT power block. The gasifier concept, however, is also being developed by the Advanced Power and Energy Program (APEP) at the University of California, Irvine, based upon previous similar gasifier concepts found in [12], [25], and [26]. Because of the low hydrocarbon and carbon monoxide content relative to hydrogen, an external reformer is not required in the current case. Internal reformation and water-gas-shift reaction chemistry is included in the model to account for conversion of all the non-hydrogen fuel constituents.

Table 1. SOFC-GT fuel stream specifications.

Constituent	Mole Fraction (%)
N ₂	1.02
Ar	1.08
H ₂	91
CO	2.62
CO ₂	3.78
H ₂ O	0.01
CH ₄	0.49
Total (%)	100

Overall SOFC-GT Model Formulation

The 100 MW SOFC-GT employs planar fuel cell geometry and empirical axial gas turbine compressor and turbine maps obtained from GSP [27]. Fuel cell operation is restricted to a fuel utilization at or below 80%. Steady state fuel cell operation is restricted to an average cell temperature of 1,023 K +/- 25 K, a maximum temperature rise across the cathode and anode of 150 K, and air preheat within the stack of 150 K. Steady state cycle pressure is 5 atmospheres measured at the turbine inlet.

A detailed description of model development is presented in the literature [15-24]. Briefly, conservation of mass, energy and momentum equations are solved for each major component within the model. The law of continuity is applied on a molar basis assuming a well-stirred reactor.

$$V_{cv} C \frac{d\mathbf{X}_{out}}{dt} = \dot{N}_{in} (\mathbf{X}_{in} - \mathbf{X}_{out}) - \mathbf{X}_{out} \sum \mathbf{R} + \mathbf{R}$$

where, V_{cv} is the control volume (m³), C is the molar concentration of the control volume (kmol/m³), $\dot{N}_{in}$ is the molar flow rate into control volume (kmol/s), $\mathbf{X}_{out}$ is the mole fraction distribution vector out of the control volume, $\mathbf{X}_{in}$ is the mole fraction distribution vector entering the control volume, and $\mathbf{R}$ is the finite reaction rate vector (kmol/s).

The internal reformation model considers the chemical kinetics of steam reformation of methane and the water-gas shift reaction.

Conservation of energy for gaseous species is solved in each of the major components using

$$NC_v \frac{dT}{dt} = \dot{N}_{in} h_{in} - \dot{N}_{out} h_{out} + \sum \dot{Q}_{in} - \sum \dot{W}_{out}$$

where, N is the moles (kmol), $C_{v,molar}$ is the molar specific heat of the bulk mixture (J/(kmol*K)), T is the temperature of the bulk mixture (K), $\dot{N}_{in}$ is the molar flow rate into control volume (kmol/s), h_{in} is the sensible enthalpy into the control volume (J/kmol), $\dot{N}_{out}$ is the molar flow rate out of control volume (kmol/s), h_{out} is the sensible enthalpy out of the control volume (J/kmol), $\dot{Q}_{in}$ is the rate of heat energy flowing into the control volume (W) and $\dot{W}_{out}$ is the rate of work flowing out of the control volume (W).

Conservation of energy in the solid phase is solved where applicable using

$$\frac{d\rho C_{mass} TV_s}{dt} = \dot{E}_{in} - \dot{E}_{out}$$

where, C_{mass} is the specific heat of the solid (J/(kg*K)), T is the temperature of the solid (K), V_s is the volume of the solid

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(m³), $\dot{E}_{in}$ is the rate of energy flowing into the solid (W), $\dot{E}_{out}$ rate of energy flowing out of the solid (W) and ρ is the density of the solid (kg/m³).

Heat transfer is calculated in each layer of the cell, consisting of anode separator plate, anode fuel flow, anode, electrolyte, cathode, cathode air flow and cathode separator plate, as well as for internal reformation. Heat transfer in the form of solid conduction, gases convection, sensible enthalpy of the gases and a heat generation term are accounted for; radiation is neglected.

Applying Newton's Second Law on a fluid element the pressure loss is given by

$$P_{in} - P_{out} = \Delta P = f \frac{L}{D_h} \frac{\rho U^2}{2}$$

where, P_{in} is the pressure of the gas entering the control volume (Pa), P_{out} is the pressure of the gas leaving the control volume (Pa), ΔP is the pressure change of the gas through control volume (Pa), f is the friction factor through theory/experiment, L is the length of the fuel cell in the direction of flow (m), D_h is the hydraulic diameter of the channel (m), U is the bulk velocity of the fluid in the channel (m/s) and ρ is the density of the solid (kg/m³). The flow inside the fuel cell is assumed to be fully developed laminar flow.

Fuel cell voltage is calculated using the Nernst equation and activation, ohmic and concentration polarizations are accounted for.

The lumped parameter gas turbine model uses steady state gas turbine maps with dynamic mass storage and shaft speed equations.

Control

The system was found to require control for stable and safe operation. The control strategy employed utilizes a cascade proportional-integral (PI) controller (Figure 2). The controller provides stable SOFC temperature by using a variable speed gas turbine to deliver the proper air flow rate. This type of control was found to be necessary to avoid damaging fuel cell temperature excursions during dynamic response to system perturbations. Fuel cell electrolyte temperature is controlled to be constant at 1,100 K while gas turbine shaft speed is secondarily controlled to remain close to the set-point value of 3,600 RPM.

Figure 2. Cascade controller used to control SOFC temperature with a variable speed gas turbine.

A cascade controller, very similar to that employed on the SOFC-GT, is used to control the blower/compressor mixture temperature at 800 K and to secondarily control blower speed. The blower is driven by an electrical motor. Due to the fuel cell control temperature of 1,100 K, the blower is routinely operated near this temperature, which may not be practical using available technology.

The perturbation and dynamic response analysis consists of diurnal ambient temperature and pressure variations both separately and together. The diurnal temperature variation is also imposed for a case where the system is subjected to a 25% load shed.

The goal during the perturbation and dynamic response analysis is to maintain stable turbo-machinery throughout as well as to maintain the SOFC control temperature of 1,100 K. For safe turbo-machinery operation compressor surge and gas turbine shaft over-speed must be avoided, also, turbine inlet temperature (TIT) must be remain below 1,123 K.

RESULTS AND DISCUSSION

Diurnal Ambient Temperature Fluctuations

When the hybrid system is subjected to a diurnal sinusoidal oscillation in ambient temperature of 298 K +/- 14 K (Figure 3), the compressor remains in a stable region of operation. As ambient temperature rises, shaft speed increases in an effort to maintain the set-point temperature of 1,100 K. This pushes compressor operation away from the surge line. However, as ambient temperature drops, the opposite is true and the compressor approaches the surge line.

Figure 3. Compressor response to a diurnal temperature fluctuation of 28 K.

When ambient temperature oscillates from 284 - 312 K (Figure 4), gas turbine shaft speed oscillates from 3,475 - 3,745 RPM.

Figure 4. Ambient temperature and gas turbine shaft speed vs. time for a diurnal temperature fluctuation of 28 K.

When ambient temperature oscillates from 284 - 312 K (Figure 5), turbine inlet temperature oscillates from 1,004 - 1,012 K and fuel cell electrolyte temperature remains constant at 1,110 K. The results for the case of a diurnal sinusoidal oscillation in ambient temperature of 298 K $\pm$ 14 K show turbo-machinery operation within safe boundaries, but with a reduction in the surge margin that occurs in the trough of ambient temperature.

Figure 5. Ambient temperature, turbine inlet temperature and fuel cell electrolyte temperature vs. time for a diurnal temperature fluctuation of 28 K.

When the hybrid system is subjected to a diurnal sinusoidal oscillation in ambient temperature of 298 K $\pm$ 16 K (Figure 6), the compressor over-speeds in an effort to maintain the fuel cell set-point temperature during the initial rise in ambient temperature. The magnitude of diurnal temperature oscillation here may occur in many regions (especially deserts) and, as a result, must be considered during design to ensure stable and safe operation. Compressor over-speed in this case is considered a turbo-machinery failure.

Figure 6. Compressor response to a diurnal temperature fluctuation of 32 K.

Diurnal Ambient Temperature Fluctuations (Fuel Cell Subjected to a 25% Decrease in Current Demand)

When the hybrid system is subjected to a 25% decrease in fuel cell current demand (Figure 7), compressor surge is approached at the minimum load value.

Figure 7. Compressor response to a 25% reduction in fuel cell current demand.

When the hybrid system is subjected to perturbations of a diurnal sinusoidal oscillation in ambient temperature of 298 K $\pm$ 14 K (Figure 8) and a 25% reduction in fuel cell current initiated at the minimum ambient temperature the compressor crosses the surge line almost immediately. This is a result of operating the compressor near the surge line at minimum ambient temperature, the point of minimum mass flow and RPM requirement for the controlled fuel cell set-point temperature of 1,100 K. Compressor surge in this case is considered a failure.

Figure 8. Compressor response to a diurnal temperature fluctuation of 28 K and a 25% reduction in fuel cell current demand initiated at minimum ambient temperature.

When the hybrid system is subjected to a diurnal sinusoidal oscillation in ambient temperature of 298 K $\pm$ 14 K (Figure 9) and a 25% reduction in fuel cell current demand initiated at the maximum ambient temperature, the compressor crosses the surge line only once the minimum load is reached. Surge is initially avoided due to compressor operation far from the surge line at maximum ambient temperature, the point of maximum mass flow and RPM requirement for the controlled fuel cell set-point temperature of 1,100 K. Compressor surge in this case is considered a failure.

Figure 9. Compressor response to a diurnal temperature fluctuation of 28 K and a 25% reduction in fuel cell current demand initiated at maximum ambient temperature.

Diurnal Ambient Pressure Fluctuations

When the hybrid system is subjected to a diurnal sinusoidal oscillation in ambient pressure of 101.3 kPa $\pm$ 2 kPa (Figure 10), the compressor remains in a stable region of operation. Ambient pressure oscillations exceeding $\pm$ 2 kPa are unlikely to occur. When ambient pressure reaches a minimum, gas turbine shaft speed reaches a maximum as it is more difficult to cool the fuel cell with a less dense fluid. The converse is true as ambient pressure reaches a maximum.

Figure 10. Compressor response to a diurnal pressure fluctuation of 4 kPa.

When ambient pressure oscillates from 99.3 - 103.3 kPa (Figure 11), gas turbine shaft speed oscillates from 3,579 - 3,626 RPM.

Figure 11. Ambient pressure and gas turbine shaft speed vs. time for a diurnal pressure fluctuation of 4 kPa.

When ambient pressure oscillates from 99.3 - 103.3 kPa (Figure 12), turbine inlet temperature oscillates from 1,007 - 1,008 K and fuel cell electrolyte temperature remains constant at 1,110 K. The results for the case of a diurnal sinusoidal oscillation in ambient pressure of 101.3 kPa $\pm$ 2 kPa show turbo-machinery operation within safe boundaries.

Figure 12. Ambient pressure, turbine inlet temperature and fuel cell electrolyte temperature vs. time for a diurnal pressure fluctuation of 4 kPa.

Simultaneous Diurnal Ambient Temperature and Pressure Fluctuations

When the hybrid system is subjected to a simultaneous, in phase, diurnal sinusoidal oscillation in ambient temperature of 298 K $\pm$ 14 K and ambient pressure of 101.3 kPa $\pm$ 2 kPa (Figure 13), the compressor remains in a stable region of operation. When compared to the case where only ambient temperature is varied by 28 K (Figure 3) or only ambient pressure is varied by 4 kPa (Figure 10), the simultaneous, in phase variation damps the oscillation so that surge is less of a possibility.

Figure 13. Compressor response to a diurnal temperature fluctuation of 28 K and pressure fluctuation of 4 kPa in phase with each other.

When ambient temperature oscillates from 284 - 312 K simultaneously in phase with ambient pressure oscillating from 99.3 - 103.3 kPa (Figure 14), gas turbine shaft speed oscillates from 3,494 - 3,718 RPM.

Figure 14. Ambient temperature, ambient pressure and gas turbine shaft speed vs. time for a diurnal temperature fluctuation of 28 K and pressure fluctuation of 4 kPa in phase with each other.

When ambient temperature oscillates from 284 - 312 K simultaneously in phase with ambient pressure oscillating from 99.3 - 103.3 kPa (Figure 15), turbine inlet temperature oscillates from 1,004-1,011 K and fuel cell electrolyte temperature remains constant at 1,110 K. The results for the case of a diurnal sinusoidal oscillation in ambient temperature of 298 K $\pm$ 14 K and in ambient pressure of 101.3 kPa $\pm$ 2 kPa in-phase show turbo-machinery operation within safe boundaries.

Figure 15. Ambient pressure, turbine inlet temperature and fuel cell electrolyte temperature vs. time for a diurnal temperature fluctuation of 28 K and pressure fluctuation of 4 kPa in phase with each other.

When the hybrid system is subjected to a simultaneous, out of phase, diurnal sinusoidal oscillation in ambient temperature of 298 K $\pm$ 14 K and ambient pressure of 101.3 kPa $\pm$ 2 kPa (Figure 16), the compressor over-speeds. When compared to the case where only ambient temperature is varied by 28 K (Figure 3) or only ambient pressure is varied by 4 kPa (Figure 10), the simultaneous, out

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of phase variation boosts the oscillation to a maximum RPM leading to over-speed. Compressor over-speed in this case is considered a failure.

Figure 16. Compressor response to a diurnal temperature fluctuation of 28 K and pressure fluctuation of 4 kPa out of phase with each other.

The question arises as to whether ambient temperature and pressure occur in or out of phase in the atmosphere. Plotting the data obtained from an atmospheric monitoring station located at Argonne National Laboratory [28] shows that either relationship is possible as seen in Figure 17 and Figure 18.

Figure 17. Hourly ambient temperature and ambient pressure vs. time for September 1, 2005. Source: Argonne National Laboratory.

Figure 18. Hourly ambient temperature and ambient pressure vs. time for December 1, 2005. Source: Argonne National Laboratory.

CONCLUSIONS

A dynamic model of a 100 MW SOFC-GT hybrid system has been developed and subjected to perturbations in diurnal ambient temperature and pressure as well as load sheds. The dynamic system responses monitored were fuel cell electrolyte temperature, gas turbine shaft speed, turbine inlet temperature and compressor surge. The hybrid system was found to operate within stable bounds for all cases tested except for excessive ambient temperature swings, simultaneous ambient temperature and pressure variations that are out of phase and load sheds, especially those that occur in the presence of ambient temperature variations. The diurnal temperature ranges that led to system failures are likely to occur in many applications and need, as a result, to be considered in the design of turbomachinery and control systems for hybrid SOFC-GT systems. Special care should also be taken to minimize the impact of simultaneous environmental variations that may, by themselves, not be a concern. The confounding perturbations of environmental condition variations, such as ambient temperature variation, with operational condition variations, such as a load shed, were found to significantly impact operational stability.

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