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# Bulk Properties of the System Formed in Au+Au Collisions at $\sqrt{s_{\text{NN}}} = 14.5$ GeV at STAR

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We report systematic measurements of bulk properties of the system created in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV recorded by the STAR detector at the Relativistic Heavy Ion Collider (RHIC). The transverse momentum spectra of  $\pi^{\pm}$ ,  $K^{\pm}$  and  $p(\bar{p})$  are studied at mid-rapidity (|y| < 0.1) for nine centrality intervals. The centrality, transverse momentum  $(p_T)$ , and pseudorapidity  $(\eta)$  dependence of inclusive charged particle elliptic flow  $(v_2)$ , and rapidity-odd charged particles directed flow  $(v_1)$  results near mid-rapidity are also presented. These measurements are compared with the published results from Au+Au collisions at other energies, and from Pb+Pb collisions at  $\sqrt{s_{\rm NN}} =$ 2.76 TeV. The results at  $\sqrt{s_{\rm NN}} = 14.5$  GeV show similar behavior as established at other energies and fit well in the energy dependence trend. These results are important as the 14.5 GeV energy fills the gap in  $\mu_B$ , which is of the order of 100 MeV, between  $\sqrt{s_{\rm NN}} = 11.5$  and 19.6 GeV. Comparisons of the data with UrQMD and AMPT models show poor agreement in general.

#### I. INTRODUCTION

According to quantum chromodynamics (QCD), at very high temperature and/or at high density, a deconfined phase of quarks and gluons is expected to be present. At low temperature and low density, quarks and gluons are confined inside hadrons. The exploration of the QCD phase diagram, in the plane of temperature (T) and the baryon chemical potential  $(\mu_B)$ , is one of the primary objectives of high-energy heavy-ion collision experiments [1–7]. During the initial stages of Au+Au collisions at top RHIC energies, there is evidence of a phase with partonic degrees of freedom [1–4, 8–13], which later transits into one with hadronic degrees of freedom [14– 17]. Relevant evidence includes strong suppression of high transverse momentum  $(p_{\rm T})$  hadron production in Au+Au collisions relative to p + p collisions [1–4, 8–11], large elliptic flow  $(v_2)$  for hadrons containing light as well as strange and charm valence quarks, and the difference between baryon and meson  $v_2$  at intermediate  $p_{\rm T}$  [18].

At  $\mu_B = 0$ , the phase transition is a cross-over. This region is well described by lattice QCD calculations [19, 20]. At larger  $\mu_B$ , a first-order phase transition is suggested by lattice QCD [21] and various QCD-based models [22– 25]. The end point of the first-order phase transition in the  $T, \mu_B$  plane is the QCD critical point [26, 27]. To discover this critical point and to search for the phase boundary, the Beam Energy Scan (BES-I) program [28– 31] was carried out by RHIC in the years 2010 and 2011. Au+Au collisions were recorded at  $\sqrt{s_{\rm NN}} = 7.7$ , 11.5, 19.6, 27, and 39 GeV. In the year 2014, another Au+Au collision energy at  $\sqrt{s_{\rm NN}} = 14.5$  GeV was added to this BES-I program to bridge the 100 MeV gap in  $\mu_B$  [32] between the beam energies of 11.5 and 19.6 GeV.

In this paper, we present bulk properties of the system, namely  $p_{\rm T}$  spectra  $(\pi, K, p), dN/dy, \langle p_{\rm T} \rangle$ , particle ratios, kinetic freeze-out properties, rapidity-odd directed flow  $v_1$  (charged hadrons), and  $v_2$  (charged hadrons) in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. A systematic study of these observables as a function of  $p_{\rm T}$ , pseudorapidity  $(\eta)$ , and collision centrality is discussed in detail. Comparisons of the results with those in Au+Au collisions at other RHIC energies and with Pb+Pb collisions at  $\sqrt{s_{\rm NN}} = 2.76$  TeV are presented. The results are also compared to model calculations, namely UrQMD (a hadronic transport model) [33] and AMPT (a transport model with both hadronic and partonic interactions) [34]. Earlier measurements suggest that systems at lower energies, such as 7.7 and 11.5 GeV, behave like hadron gases, while at energies of 19.6 GeV and above, they show partonic behavior [35–44]. The Au+Au collisions at  $\sqrt{s_{\rm NN}} =$  14.5 GeV, lying between these two energies, allow studies of the interplay between hadronic and partonic phases.

#### II. EXPERIMENT AND DATA ANALYSIS

#### A. STAR Detector

This paper reports the results for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV taken by the STAR detector [45] at RHIC under the BES-I program. The selected minimum-bias data triggered by the Beam Beam Counters (BBCs) [46, 47] are used for this analysis. The BBCs are two scintillator-based detectors situated on both sides of the center of STAR at pseudorapidity  $3.8 < |\eta| <$ 5.2 with full azimuthal coverage. The detector primarily used for tracking is the Time Projection Chamber (TPC) [48]. The TPC is a gas detector filled with P10 gas (90% Argon and 10% Methane). It operates at a pressure of 2 mbar above atmospheric pressure in a constant magnetic field of 0.5 Tesla in the longitudinal (z)direction. The TPC has an acceptance of  $|\eta| < 1$  in pseudorapidity and  $2\pi$  in azimuth. Through ionization energy loss  $(\langle dE/dx \rangle)$  measurements of the particles traversing the TPC gas, different particles can be identified. The Time of Flight (TOF) detector is also used for particle identification [49]. The TOF uses Multi Resistive Plate Chamber (MRPC) technology. It provides full azimuthal coverage and has a pseudorapidity acceptance of  $|\eta| < 0.9.$ 

#### **B.** Event Selection

The primary vertex of each event is determined by finding the best common point from where most of the tracks originate. Along the beam direction, a vertex position cut of  $|V_z| < 30$  cm is applied to select events for the spectra analysis. For  $v_1$  and  $v_2$  analyses, a broader cut of  $|V_z| < 70$  cm is applied to obtain reasonable statistics. In Au+Au collisions at 14.5 GeV, the mean vertex position for all events is centred at (0, -0.89) cm in x-y plane. A radial vertex position cut (defined by  $V_r = \sqrt{V_x^2 + V_y^2}$ ) of  $V_r < 1$  cm from the centre is applied to reject interactions involving the beam pipe. After these event cuts, the number of events analyzed for  $\pi$ , K, p spectra is nearly 10

#### D. Track Selection

million, while the number for inclusive charged particle  $v_1$  and  $v_2$  analyses is about 17 million.

# TABLE I. Track selection criteria in Au+Au collisions at $\sqrt{s_{\rm NN}} = 14.5$ GeV.

## C. Centrality Selection



FIG. 1. Uncorrected charged-particle multiplicity distribution (open circles) measured in the TPC within  $|\eta| < 0.5$  in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. The blue dashed line represents the charged particle multiplicity distribution from a MC Glauber model [50]. The vertical dashed lines represent the centrality selection criteria used.

	Spectra	$v_1, v_2$
$y/\eta$	y  < 0.1	$ \eta  < 1.0$
DCA (cm)	< 3	< 3
Number of fit points	$\geq 25$	$\geq 15$
Fraction of fit points	$\geq 0.52$	$\geq 0.52$
Number of $dE/dx$ points	$\geq 15$	$\geq 15$

Details of the track cuts are tabulated in Table I. The distance of closest approach (DCA) of tracks to the primary vertex is required to be less than 3 cm to suppress tracks from secondary decays. In the spectra analysis, the number of fit points associated with a track has to be 25 or more out of a maximum possible 45 hits in the TPC, while for  $v_1$  and  $v_2$  analyses, 15 or more hits are required. The cuts in these analyses are the same as the standard cuts established in previous STAR published papers. The fraction of fit points on a track is required to be greater than 52% of the total possible hits to avoid split tracks. To have a good ionization energy loss  $\langle dE/dx \rangle$  resolution for tracks, the number of TPC hits used to determine  $\langle dE/dx \rangle$  is required to be 15 or more. The spectra results are obtained for tracks within the rapidity window |y| < 0.1. Inclusive charged particle  $v_1$  and  $v_2$  analyses are carried out using tracks within pseudorapidity  $|\eta| < 1$ .

The uncorrected charged-particle multiplicity distribution is compared and fitted with Glauber Monte-Carlo (MC) simulations as shown in Fig. 1. The detailed procedure to obtain the simulated multiplicity using Glauber Monte-Carlo is similar to that described in [50]. The minimum-bias trigger events are divided into nine centrality classes: 0-5%, 5-10%, 10-20%, 20-30%, 30-40%, 40-50%, 50-60%, 60-70% and 70-80%. The quoted fractions are in terms of the total cross section obtained from the simulated events with the Glauber model. In addition, quantities such as average number of participating nucleons  $\langle N_{\rm part} \rangle$ , number of binary collisions  $\langle N_{\rm coll} \rangle$  etc. are estimated and are listed in Table III.

#### E. Particle Identification

Particle identification in the TPC is carried out by measuring the truncated mean of the ionization energy loss ( $\langle dE/dx \rangle$ ) for each of the selected tracks. The measured  $\langle dE/dx \rangle$  of the charged particles as a function of rigidity, p/q (momentum per charge in units of the electron charge) is presented in the top panel of Fig. 2. The solid curves represent theoretical values predicted by the Bichsel [51] formula. The TPC can identify pions, kaons and protons with relatively low momentum, but the separate bands start merging at higher momentum. The pions and kaons can be identified up to  $p_{\rm T}$  of 0.8 GeV/*c* and protons up to 1.0 GeV/*c*.



FIG. 2. (Upper panel) The  $\langle dE/dx \rangle$  distribution of charged particles from the TPC as a function of momentum/charge for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. The curves represent the expected mean values of  $\langle dE/dx \rangle$  for the corresponding particle species. (Lower panel)  $1/\beta$  as a function of momentum/charge from TOF in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$ GeV. The curves represent the expected values of  $1/\beta$  for the indicated particle species.

For particle identification at relatively higher momentum, the TOF detector is utilized. In this analysis, TOF information is used for particle identification in the  $p_T$ range 0.4–2.0 GeV/c (0.5–2.0 GeV/c) for pions and kaons (protons). The lower panel of Fig. 2 shows the characteristic plot for TOF in which the inverse of particle velocity in units of the speed of light,  $1/\beta$ , is plotted as a function of p/q. The solid lines are the expected values for pions, kaons and protons.

The  $\langle dE/dx \rangle$  distribution for a specific particle type in the TPC does not have a Gaussian shape [52]. It has been demonstrated that a more appropriate Gaussian variable for a given choice of particle type is the z-variable [52], defined as

$$z_X = \ln\left(\frac{\langle dE/dx \rangle}{\langle dE/dx \rangle_X^B}\right),\tag{1}$$

where X is the particle type  $(e^{\pm}, \pi^{\pm}, K^{\pm}, p \text{ or } \bar{p} \text{ in }$ the present analysis) and  $\langle dE/dx \rangle_X^B$  is the corresponding prediction of  $\langle dE/dx \rangle$  from the Bichsel function [51]. The  $z_X$  distribution for each particle type is expected to peak at 0.

The  $z_X$  distributions are constructed for a particular choice of particle, for a given  $p_{\rm T}$  range within rapidity |y| < 0.1. The top panel of Fig. 3 shows the  $z_{\pi}$  distribution for positively charged tracks of  $0.30 < p_{\rm T} < 0.35$ GeV/c. The distributions are then fitted by a multi-Gaussian function to extract the raw yield. The area under the Gaussian curve for the particle under consideration gives the yield of that particle for that  $p_{\rm T}$  range. As can be noticed from Fig. 3, the pion peak is slightly shifted towards the negative side of zero on the  $z_{\pi}$  axis. This could be due to issues related to calibration. However, any shift of the pion peak from zero does not have an impact on the raw yield value. This method is applicable for low  $p_{\rm T}$  values, up to the point where the distributions for pions, kaons and protons are well separated. For higher  $p_{\rm T}$ , where the distributions start to overlap, the widths of the Gaussian distributions are constrained according to the values at lower  $p_{\rm T}$ . Following a similar procedure for each particle type, raw yields are extracted for different  $p_{\rm T}$  ranges in nine centrality classes.

The raw yields from TOF are obtained using the  $m^2$  variable defined as

$$m^{2} = p^{2} \left( \frac{c^{2} T^{2}}{L^{2}} - 1 \right), \qquad (2)$$

where p, T, L, and c are particle momentum, Timeof-flight, path length of the particle, and the speed of light, respectively. Within |y| < 0.1, the  $m^2$  distributions are obtained for the particle of interest in a given  $p_{\rm T}$  range, and one example is shown in the bottom panel of Fig. 3 for the case of  $\pi^+$ . To extract the raw yields using  $m^2$  distributions, we follow the same procedure as done in Refs. [32, 53]. In this method, the  $m^2$  distributions from data are fitted using the predicted  $m^2$  distributions. The predicted  $m^2$  distribution is generated by the measured time-of-flight from experimental data, thus including the TOF detector response behavior, for a given dE/dx-identified particle. It is observed that the predicted  $m^2$  distributions do not change much with  $p_T$ and can be extended to higher  $p_T$  where dE/dx identification is limited. These predicted  $m^2$  distributions of pions, kaons and protons are used simultaneously to fit the measured  $m^2$  distributions to obtain the raw yield as shown for  $\pi^+$  in the bottom panel of Fig. 3 for  $p_T$  range 0.5-0.6 GeV/c. In this way, the raw yields are obtained for all  $p_T$  bins, centralities and different particles.

#### F. Flow Analysis

The azimuthal distribution of emitted particles with respect to the reaction plane can be decomposed in a Fourier series [54]. The harmonic coefficients  $(v_n)$  in this



FIG. 3. (Top panel) The  $z_{\pi}$  distribution at midrapidity (|y| < 0.1) for the  $p_{\rm T}$  range 0.30–0.35 GeV/c in 0–5% central Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. The curves are Gaussian fits representing contributions from pions (dashed red), electrons (dotted green), kaons (dash-dotted blue), and protons (dash-dot-dotted magenta). The uncertainties are statistical only. (Bottom panel) The  $m^2$  distributions used to obtain the raw yields from TOF for  $\pi^+$  within |y| < 0.1 in the  $p_{\rm T}$  range 0.50–0.60 GeV/c. These distributions are for 0–5% centrality in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. The curves are fits to the  $m^2$  distribution, representing contributions from pions (red), kaons (blue) and protons (magenta).

expansion are defined as,

$$v_n = \langle \cos n(\phi - \Psi_R) \rangle. \tag{3}$$

Here, angle brackets denote an average over all particles in all events for a given  $p_{\rm T}$  or  $\eta$  bin, and  $\Psi_R$  is the azimuth of the reaction plane angle. The first harmonic coefficient is called the directed flow  $(v_1)$ , while the second is called the elliptic flow  $(v_2)$ . Since the  $\Psi_R$  is unknown experimentally, it is estimated from

$$\Psi_n = \frac{1}{n} \tan^{-1} \left( \frac{\sum\limits_{i=1}^N w_i \sin(n\phi_i)}{\sum\limits_{i=1}^N w_i \cos(n\phi_i)} \right), \tag{4}$$

where  $\Psi_n$  is  $n^{th}$ -order event plane azimuth,  $w_i$  are weights, and N is the total number of particles in an event used for the event plane calculation [54]. The observed  $v_n^{\text{obs}}$  is calculated with respect to the reconstructed event plane using

$$v_n^{\text{obs}} = \langle \cos n(\phi - \Psi_n) \rangle. \tag{5}$$

The observed  $v_n$  are then corrected for event plane resolution [55, 56].

Two types of event plane angles are used in this analysis: the TPC event plane [50] and the BBC event plane [57]. In the TPC event plane method, a secondorder event plane angle ( $\Psi_2$ ) is reconstructed from TPC tracks at mid-rapidity ( $|\eta| < 1$ ). To reduce nonflow contributions, we utilize the  $\eta$ -sub method, with an additional  $\eta$ -gap of 0.1 between the sub-events, and then average the results from the two sub-events [50]. In the BBC event plane method, a first-order event plane ( $\Psi_1$ ), reconstructed using the hits in both BBC detectors in opposite hemispheres ( $3.8 < |\eta| < 5.2$ ), is used to calculate  $v_1$  and  $v_2$ . Re-centering and shift techniques were applied for each  $\eta$  hemisphere independently to flatten the TPC event plane and BBC event plane [54]. More details about these methods can be found in a previous publication [50].

In addition to the event plane method, the multiparticle correlation method [58, 59] is used to calculate  $v_2$ of charged particles. In this method, the reference flow (e.g., integrated over  $p_{\rm T}$ ) can be estimated both from two- and four-particle cumulants:

$$v_n\{2\} = \sqrt{c_n\{2\}},$$
 (6)

$$v_n\{4\} = \sqrt[4]{-c_n\{4\}}.$$
 (7)

Here  $c_n\{2\}$  and  $c_n\{4\}$  are two- and four-particle cumulants. The two- and four-particle cumulants without detector bias then can be formulated as

$$c_n\{2\} = \langle \langle e^{in(\phi_1 - \phi_2)} \rangle \rangle, \tag{8}$$

$$c_n\{4\} = \langle \langle e^{in(\phi_1 + \phi_2 - \phi_3 - \phi_4)} \rangle \rangle - 2 \times \langle \langle e^{in(\phi_1 - \phi_2)} \rangle \rangle.$$
(9)

Here, double angle brackets denote an average over all events. More details about these methods are presented in [50].

#### **III. CORRECTION FACTORS**

#### A. Monte-Carlo Embedding Technique

Several correction factors for the  $p_{\rm T}$  spectra are calculated from MC simulations known as the embedding technique. The method is outlined below and more details can be found in Refs. [28, 32, 60]. For a given particle, MC tracks having flat rapidity and  $p_{\rm T}$  distributions are simulated in the STAR detector using GEANT3. Those simulated tracks are then embedded into real events at the raw data level. The multiplicity of embedded tracks in any real event is no more than 5% of the measured real charged particle multiplicity of that event. These embedded tracks are reconstructed in the same manner as the real data reconstruction. The embedding sample is used to calculate various correction factors such as tracking efficiency and acceptance, and energy loss correction as discussed below.

#### **B.** Energy Loss Correction

The TPC track reconstruction algorithm assumes the pion mass for each particle when correcting for multiple Coulomb scattering and energy loss in the TPC gas, which mostly affect particles of low momenta. Therefore, a correction for momentum loss by heavier particles like  $K^{\pm}$  and  $p(\bar{p})$  is needed. This correction is obtained from MC simulation or embedding techniques. The distribution of momentum difference between reconstructed momentum  $p_{\rm T}^{\rm REC}$  and initial momentum  $p_{\rm T}^{\rm MC}$  as a function of  $p_{\rm T}^{\rm REC}$  gives the amount of energy loss correction for each track. The relevant plot for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV, showing the  $p_{\rm T}$  dependence of energy loss, is presented in Fig. 4 for pions (left), kaons (middle) and protons (right). The red curve represents a functional fit to the data points in the case of kaons and protons,

$$f(p_{\rm T}) = A + B \left(1 + \frac{C}{p_{\rm T}^2}\right)^D,$$
 (10)

where A, B, C and D are fit parameters. This energy loss fraction is the same for all centrality classes for a particular particle type. All the results shown in this paper have been corrected for this energy loss effect.

#### C. Tracking Efficiency and Acceptance

A correction for detector efficiency and acceptance needs to be applied to the  $p_{\rm T}$  spectra of analyzed particles. This correction factor is obtained from the embedding technique described above. The combined tracking efficiency and acceptance is the ratio of the distribution of reconstructed to original Monte-Carlo tracks as a function of  $p_{\rm T}$  in the rapidity range of interest. This functional dependence of combined tracking efficiency and acceptance on  $p_{\rm T}$  is presented in Fig. 5 for reconstructed pions (left), kaons (middle), and protons (right) in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. The curves represent the functional fit of the form  $p_0 \exp[-(p_1/p_T)^{p_2}]$ , used to parameterize the efficiency. This correction factor is thus calculated for each particle type in nine centrality classes and each  $p_{\rm T}$  spectrum is divided by this fraction.

#### D. TOF Matching Efficiency

The TOF detectors form a curved cylindrical surface surrounding the TPC and have a reduced geometric acceptance compared to the TPC. Circumstances arise where TPC tracks are not detected in TOF, especially at low momentum, either because the track is out of the TOF acceptance or because of the TOF inefficiency. As a result, the yield of particles identified by TOF needs to be corrected, in addition to the TPC track reconstruction efficiency. This is referred to as the TOF matching efficiency or TOF particle identification efficiency for TPC tracks. This efficiency is calculated from the STAR data as the ratio of the number of tracks detected in TOF to the total number of tracks in the TPC within the acceptance under study. It is shown as a function of  $p_{\rm T}$  in Fig. 6 for pions (left), kaons (middle) and protons (right) in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV for 0–5% centrality. The raw yields obtained using TOF are divided



FIG. 4. The  $p_{\rm T}$  difference of reconstructed momentum  $p_{\rm T}^{\rm REC}$  and MC momentum  $p_{\rm T}^{\rm MC}$  as a function of  $p_{\rm T}^{\rm REC}$  for pions (left), kaons (middle) and protons (right) in 0-5% central Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. The red curves represent the functional fit of the form  $f(p_{\rm T}) = A + B \left(1 + \frac{C}{p_{\rm T}^2}\right)^D$ .



FIG. 5. The combined tracking efficiency and acceptance as a function of  $p_{\rm T}$  calculated from the Monte-Carlo embedding technique for reconstructed pions (left), kaons (middle) and protons (right) at midrapidity (|y| < 0.1) for 0-5% Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. The curves represent the functional fit of the form  $p_0 \exp[-(p_1/p_T)^{p_2}]$ .



FIG. 6. TOF matching efficiency as a function of  $p_{\rm T}$  for pions (left), kaons (middle) and protons (right) at midrapidity (|y| < 0.1) in 0-5% Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV.

by the matching efficiency for each centrality,  $p_{\rm T}$  range, and for each particle type.

#### E. Pion Background Correction

The measured pions get a contribution from the feeddown of weak decays, muon contamination, and background pions produced in the detector material. Therefore, it is important to remove these background contributions from the total pion yield. To obtain this correction, we used the same approach as done in Refs. [32, 60]. The Monte-Carlo simulated events are generated by HI-JING [61] and are processed through the STAR detector simulated by GEANT3 [62]. These events are reconstructed in the same manner as real data. In the MC sample, the pion background fraction is estimated since different contributions to the total pion yield are known. The pion background fraction decreases exponentially with  $p_{\rm T}$ . Its value at low  $p_{\rm T}(=0.225 {\rm ~GeV}/c)$ is ~ 16% and becomes negligible above 0.6 GeV/c. It shows negligible centrality dependence, hence the same correction is applied for all centrality classes.

#### F. Proton Background Correction

The yield of protons has a significant contribution from background protons coming from interactions of highly energetic particles with the detector material. In order to estimate the proton background fraction, we follow the same procedure as used in Refs. [32, 60, 63]. This fraction is estimated by comparing the proton and antiproton DCA distributions obtained from real data. The difference between the proton and antiproton DCA distribution gives the estimate of proton background contribution. The proton background fraction decreases as a function of  $p_{\rm T}$  and decreases from peripheral to central collisions. At  $p_T = 0.60-0.65 \text{ GeV}/c$ , its typical value is about 40% in peripheral collisions and 2% in central collisions. For minimum bias collisions, proton background at low  $p_{\rm T}$  is around 15% and becomes almost negligible for  $p_{\rm T} > 1.2 \text{ GeV}/c$ . The (anti)protons also have a contribution of feed-down from weak decays of hyperons, which include particles like  $\Sigma$  which has not been measured. Contrary to pions, the analysis cut of DCA < 3cm includes almost all daughter particles from hyperon decays [64, 65]. Thus, (anti)proton yields presented here are all inclusive similar to those at other RHIC energies [32, 60].

#### IV. SYSTEMATIC UNCERTAINTIES

To estimate the size of systematic uncertainties associated with the  $p_{\rm T}$  spectra of the particles under study, we vary the event and track cuts, and the quality of fits to  $\langle dE/dx \rangle$  measurements. The following parameters are varied: the event  $V_z$  range (from  $|V_z| < 30$  cm to  $|V_z| < 50$  cm), track cuts like DCA (from 3 cm to 2 cm), number of fit points (from 25 to 20), and number of  $\langle dE/dx \rangle$  points (from 15 to 10). We have also varied the fit range for the z distribution and the PID selection (using  $\langle dE/dx \rangle$ ) cut of a given particle used for the predicted  $m^2$  distribution.

TABLE II. Systematic uncertainties related to  $\pi$ , K and  $p(\bar{p})$  integrated particle yields in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV.

	$\pi$	K	$p \bar{p}$
$V_z$	1%	1%	1%
Track Cuts	4%	4%	6%
PID	6%	8%	7%
Extrapolation	5%	4%	6%
Corrections	5%	5%	5%
Proton Background	-	-	5-6%
Total	10%	10%	12%

Apart from these systematic uncertainties for the case of  $p_{\rm T}$  spectra, an additional error of 5% is added in quadrature due to detector tracking efficiency and acceptance [32, 60, 65]. The pion feed-down correction and the proton background fraction also contribute to the systematic uncertainty; however, the former is negligible and the latter contributes about 5–6% only at low  $p_{\rm T}$ . All the sources of systematic uncertainty are added in quadrature and are tabulated in Table II. The total systematic uncertainties on pion, kaon and proton yields are 10%, 10% and 12%, respectively.

The calculation of  $p_{\rm T}$  integrated particle yields (dN/dy) and  $\langle p_{\rm T} \rangle$  requires a fitting function to extrapolate the  $p_{\rm T}$  spectra to the unmeasured  $p_{\rm T}$  region. Thus, another important source of systematic uncertainty in dN/dy and  $\langle p_{\rm T} \rangle$  is extrapolation. For pions, kaons and protons, the default fit functions used to extract yields are Bose-Einstein,  $m_T$ -exponential, and double exponential, respectively. To estimate the systematic uncertainty, these fit functions for pions, kaons and protons are changed to  $p_{\rm T}$ -exponential, Boltzmann and  $m_T$ exponential functions, respectively. The relevant functional forms are

- Bose-Einstein:  $\propto 1/(\exp(m_T/T_{\rm BE}) 1)$
- $p_T$ -exponential:  $\propto \exp(-p_T/T_{p_T})$
- $m_T$ -exponential:  $\propto \exp(-m_T/T_{m_T})$
- Boltzmann:  $\propto m_T \exp(-m_T/T_B)$

• Double-exponential:  $A e^{-p_T^2/T_1^2} + B e^{-p_T^2/T_2^2}$ 

The systematic uncertainty on mean  $p_{\rm T}$  mainly comes from the errors associated with extrapolation of  $p_{\rm T}$  spectra. The fitting range of the fit function also affects the value of  $\langle p_{\rm T} \rangle$ , which is included as a source of systematic uncertainty. The systematic uncertainty on  $\langle p_{\rm T} \rangle$  for pions, kaons and protons is 5%, 2% and 6%, respectively.

The systematic uncertainty on integrated particle ratios is calculated from the systematic uncertainty on dN/dy. The systematic uncertainty due to tracking efficiency cancels in particle ratios. The error associated with extrapolation mostly cancels in the case of particle to antiparticle ratios, but does not cancel for the ratios of different particle species.

The Blast-Wave fit [66] to particle  $p_{\rm T}$  spectra provides the kinetic freeze-out parameters. The point-to-point systematic uncertainty associated with the  $p_{\rm T}$  spectra propagates to the systematic uncertainties on the kinetic freeze-out parameters. The  $p_{\rm T}$  ranges used for fitting also affect the results. These variations are included in the systematic uncertainty on kinetic freeze-out parameters.

The systematic uncertainties for  $v_1$  and  $v_2$  measurements are estimated by varying event and track cut parameters from their default values. The z-position of the primary vertex is varied between 60 and 80 cm. The DCA of the primary tracks is varied between 2.0 cm and 3.0 cm. The number of fit points is varied from 18 to 25. In the case of  $v_2$  measurements, the  $\eta$ -gap is varied between 0.05 and 0.075. In total, about 100 combinations of such cut variations are considered and the RMS of the variation is taken as the systematic uncertainty. A maximum of 2% relative systematic uncertainty due to event cuts, and 1% due to track cuts, is found for the various centrality classes and for the various  $p_T$  and  $\eta$  bins.

#### V. RESULTS AND DISCUSSIONS

#### A. Transverse Momentum Spectra

The transverse momentum spectra for  $\pi^+$ ,  $\pi^-$ ,  $K^+$ ,  $K^-$ , p, and  $\bar{p}$  in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5 \ {\rm GeV}$ are presented in Fig. 7. The spectra are plotted for nine collision centralities 0-5%, 5-10%, 10-20%, 20-30%, 30-40%, 40–50%, 50–60%, 60–70%, 70–80%. Further information can be extracted from the particle  $p_{\rm T}$  spectra through functional fitting in terms of dN/dy and  $\langle p_{\rm T} \rangle$ . As mentioned earlier the functions used for this purpose are Bose-Einstein,  $m_T$ -exponential and double exponential for pions, kaons and protons, respectively. It can be inferred that the invariant yields exhibit a  $p_{\rm T}$  dependence (decrease with increasing  $p_{\rm T}$ ) as well as a centrality dependence (decrease towards the peripheral collisions). The shapes of the kaon and (anti)proton spectra show a gradual flattening from peripheral to central collisions. The trend is less pronounced for pions. This flattening

reflects a stronger effect of radial flow on particles with higher mass and for events with increasing centrality.

#### B. Average Transverse Momenta

Average transverse momenta quantitatively reflect the slopes of the measured  $p_{\rm T}$  spectra of the particles. i.e., the transverse dynamics influences  $\langle p_{\rm T} \rangle$ . The dependence of  $\langle p_{\rm T} \rangle$  on the number of nucleon participants  $\langle N_{\rm part} \rangle$  is shown in Fig. 8 for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$ GeV. These averages are compared with the corresponding results from Au+Au collisions at  $\sqrt{s_{\rm NN}} = 7.7, 11.5$ , 19.6, 27, 39, 62.4, and 200 GeV measured by STAR in earlier runs [8–11, 32, 60, 65]. It is seen from the figure that  $\langle p_{\rm T} \rangle$  of  $\pi^{\pm}$ ,  $K^{\pm}$  and  $p(\bar{p})$  increases with increasing  $\langle N_{\rm part} \rangle$ . This indicates an increase of radial flow from peripheral to central collisions [67]. Mean  $p_T$  and inferred radial flow also increase from pions to kaons, and from kaons to protons. The behavior of  $\langle p_{\rm T} \rangle$  as a function of  $\langle N_{\rm part} \rangle$  in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV is similar within error bars to what is observed at other BES-I energies, although it slowly increases with collision energy. The values of  $\langle p_{\rm T} \rangle$  for  $\pi^+$ ,  $\pi^-$ ,  $K^+$ ,  $K^-$ , p, and  $\bar{p}$  are listed in Table V for Au+Au collisions at  $\sqrt{s_{\rm NN}} =$ 14.5 GeV.

#### C. Particle Yields

The particle production in a collision centrality interval is defined as dN/dy or particle yield, which we measure at midrapidity (|y| < 0.1) and is obtained by integrating over  $p_{\rm T}$ . The measured dN/dy is shown in Fig. 9 for  $\pi^+$ ,  $\pi^-$ ,  $K^+$ ,  $K^-$ , p and  $\bar{p}$ , normalized with  $0.5 \times \langle N_{\rm part} \rangle$ , as a function of  $\langle N_{\rm part} \rangle$  in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$ GeV. These yields are compared with the corresponding results from Au+Au collisions at  $\sqrt{s_{\rm NN}} = 7.7$ , 11.5, 19.6, 27, 39, 62.4, and 200 GeV measured by STAR in earlier runs [8–11, 32, 60, 65]. The values of dN/dy for  $\pi^+$ ,  $\pi^-$ ,  $K^+$ ,  $K^-$ , p, and  $\bar{p}$  are also tabulated in Table IV for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV.

The pion, kaon, and proton yields slowly increase from peripheral to central collisions. This may indicate contributions from hard processes which depend on the number of nucleon-nucleon binary collisions, increasing with  $N_{\text{part}}$  more than linearly [68]. The antiproton yields remain almost flat with centrality. This may be due to an increasing baryon-antibaryon annihilation effect with increasing centrality. The yields of pions, kaons, and antiprotons all increase with increasing collision energy. However, the yield of protons shows the opposite trend and decreases up to 39 GeV after which it starts to increase. This reflects an increase in baryon density due to baryon stopping at lower energies [28, 32, 69]. The



FIG. 7. The  $p_{\rm T}$  spectra of  $\pi^{\pm}$ ,  $K^{\pm}$ , p ( $\bar{p}$ ) measured at midrapidity (|y| < 0.1) in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. Spectra are plotted for nine centrality classes, with some spectra multiplied by a scale factor to improve clarity, as indicated in the legend. The data points shown for  $p_{\rm T} = 0.4$ -2.0 GeV/c for pions and kaons, and for 0.5-2.0 GeV/c for protons, are obtained using both TPC and TOF. Data points measured using only the TPC are shown for  $p_{\rm T}$  in the range 0.2-0.8, 0.3-0.8 and 0.5-1.0 GeV/c for pions, kaons and protons, respectively. The  $p_{\rm T}$  range 0.4-0.8 GeV/c, 0.4-0.8 GeV/c and 0.5-1.0 GeV/c for pions, kaons and protons, respectively, is the overlap region containing data measurements in both categories, namely, TPC only, and TPC+TOF. The  $p_{\rm T}$ -spectra are fitted with a Bose-Einstein function for pions, an  $m_T$ -exponential for kaons, and a double exponential for (anti)protons. Statistical and systematic uncertainties are added in quadrature.



FIG. 8.  $\langle p_{\rm T} \rangle$  of  $\pi^+$ ,  $K^+$  and p as a function of  $\langle N_{\rm part} \rangle$  for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. These averages are compared with the corresponding results from Au+Au collisions at  $\sqrt{s_{\rm NN}} = 7.7$ , 11.5, 19.6, 27, 39, 62.4, and 200 GeV measured by STAR in earlier runs [32, 60, 65]. Statistical and systematic uncertainties have been added in quadrature.

results in Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 14.5$  GeV show a similar behaviour as observed by STAR at other energies [8–11, 32, 60, 65].

#### D. Particle Ratios

Particle ratios provide additional information about particle production and the system evolution in highenergy heavy-ion collisions. In this context, we have analyzed particle ratios in Au+Au collisions at  $\sqrt{s_{\rm NN}} =$ 14.5 GeV, and compared to published results for Au+Au



FIG. 9. dN/dy of  $\pi^+$ ,  $\pi^-$ ,  $K^+$ ,  $K^-$ , p and  $\bar{p}$  scaled by  $(0.5 \times \langle N_{\text{part}} \rangle)$  as a function of  $\langle N_{\text{part}} \rangle$  for Au+Au collisions at  $\sqrt{s_{\text{NN}}} =$  14.5 GeV. These yields are compared with the corresponding results from Au+Au collisions at  $\sqrt{s_{\text{NN}}} =$  7.7, 11.5, 19.6, 27, 39, 62.4, and 200 GeV measured by STAR in earlier runs [32, 60, 65]. Statistical and systematic uncertainties have been added in quadrature.



FIG. 10.  $\pi^{-}/\pi^{+}$ ,  $K^{-}/K^{+}$  and  $\bar{p}/p$  ratios as a function of  $\langle N_{\text{part}} \rangle$  in Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 14.5$  GeV. These ratios are compared with the corresponding results from Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 7.7$ , 11.5, 19.6, 27, 39, 62.4, and 200 GeV measured by STAR in earlier runs [32, 60, 65]. Statistical and systematic uncertainties have been added in quadrature.

collisions at other collision energies [8–11, 32, 60, 65].

Figure 10 shows the dependence of the antiparticle to particle ratios on  $\langle N_{\rm part} \rangle$  in Au+Au collisions at  $\sqrt{s_{\rm NN}} =$ 14.5 GeV. These ratios are compared with the corresponding results from Au+Au collisions at  $\sqrt{s_{\rm NN}} =$  7.7, 11.5, 19.6, 27, 39, 62.4, and 200 GeV measured by STAR in earlier runs [8–11, 32, 60, 65]. The  $\pi^-/\pi^+$  ratio has no significant centrality dependence and hovers around unity for all energies. At lower energies, including Au+Au collisions at  $\sqrt{s_{\rm NN}} =$  14.5 GeV, this ratio is slightly greater than one, which is due to isospin conservation and the contribution from decays of resonances like  $\Delta$  baryons [28, 32]. This effect is more visible at lower energies due to the comparatively smaller yield of pions. The  $K^-/K^+$  ratio is almost flat within uncertainties across all centralities. However, this  $K^-/K^+$  ratio shows an increase with increasing beam energy. This is because at lower energies, associated production is the dominant mechanism, producing only  $K^+$ , whereas with increasing energy, pair production dominates, producing both  $K^+$  and  $K^-$  [28, 32]. The  $\bar{p}/p$  ratio shows a modest increase from central to peripheral collisions, which could



FIG. 11.  $K^+/\pi^+$ ,  $K^-/\pi^-$ ,  $p/\pi^+$  and  $\bar{p}/\pi^-$  ratios as a function of  $\langle N_{\text{part}} \rangle$  in Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 14.5$  GeV. These ratios are compared with the corresponding results from Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 7.7$ , 11.5, 19.6, 27, 39, 62.4, and 200 GeV measured by STAR in earlier runs [32, 60, 65]. Statistical and systematic uncertainties have been added in quadrature.

be attributed to an increase in proton yields as a result of baryon stopping and/or a decrease in antiproton yields due to annihilation in central collisions [28, 32]. This ratio also increases with increasing collision energy. All these antiparticle-to-particle ratios in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV follow the same general patterns as observed at other energies [8–11, 32, 60, 65].

Various ratios of different particle species such as  $K^+/\pi^+$ ,  $K^-/\pi^-$ ,  $p/\pi^+$  and  $\bar{p}/\pi^-$  are shown in Fig. 11 for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. Previously published results from the STAR experiment at other beam energies [8–11, 32, 60, 65] are also shown for comparison. Both  $K^+/\pi^+$  and  $K^-/\pi^-$  ratios increase from peripheral to mid-central collisions and then remain almost independent of  $\langle N_{\rm part} \rangle$ . This pattern is due to strangeness equilibrium described in various thermodynamical models [70, 71] and is also impacted by baryon stopping at midrapidity. The results from Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV fit well in the energy dependence trend. The  $p/\pi^+$  ratio increases slowly from peripheral to central collisions, whereas the  $\bar{p}/\pi^-$  ratio

stays flat across all values of  $\langle N_{\rm part} \rangle$ . Also, there is a decrease in the  $p/\pi^+$  ratio and an increase of the  $\bar{p}/\pi^-$  ratio with increasing collision energy, which together can be attributed to baryon stopping at lower energies being prominent for central collisions.

#### E. Kinetic Freeze-out Properties

The invariant yields and  $p_{\rm T}$  spectra of particles give us tools to study the freeze-out properties of the system. There are two freeze-out stages observed in high-energy heavy-ion collision experiments: chemical freeze-out and kinetic freeze-out. First, inelastic collisions among the particles cease, defining the chemical freeze-out stage. After that point, there is no further production of new particles, and the yields of particle types becomes fixed. Various thermodynamic models are widely applied to extract the information of this stage in terms of chemical freeze-out temperature and baryon chemical potential [4, 32, 72, 73]. Thereafter, the particles collide only elastically. After further expansion of the system, as the inter-particle separation becomes large, such elastic collisions between particles also cease, leading to the kinetic freeze-out stage. The momenta of the particles are fixed after this point, and the particles freely propagate to the detector. The particle  $p_{\rm T}$  spectra thus contain information about the kinetic freeze-out stage. Hydrodynamics inspired models such as the Blast-Wave model are used to extract the kinetic freeze-out properties [4, 32, 60, 66]. This stage is characterized by the kinetic freeze-out temperature  $T_k$  and radial flow velocity  $\beta$ , which carry signatures of the transverse expansion of the system. Here, we follow the previously adopted procedures to study the kinetic freeze-out properties in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. The chemical freeze-out properties are not discussed in this paper as the final measurements for strange hadrons yields for  $\Lambda$  and  $\Xi$  are not available. These will be reported in a future STAR paper.

The calculation of kinetic freeze-out parameters is carried out through a Blast-Wave model [66] fit to the measured particle  $p_{\rm T}$  spectra in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. It is a hydrodynamics inspired model in which the particles are assumed to be locally thermalized at the kinetic freeze-out temperature  $T_k$  and move with a common radial flow velocity  $\beta$ . For such a radially boosted uniform hard sphere, the transverse momentum distribution of the produced particles can be written as [32, 60, 66]

$$\frac{dN}{p_{\rm T}dp_{\rm T}} \propto \int_0^R r dr \, m_T I_0\left(\frac{p_{\rm T}\sinh\rho(r)}{T_k}\right) \\ \times K_1\left(\frac{m_T\cosh\rho(r)}{T_k}\right), \qquad (11)$$

where  $m_T = \sqrt{p_T^2 + m^2}$  is the transverse mass of the particle,  $\rho(r) = \tanh^{-1}\beta$ , and  $I_0$  and  $K_1$  are modified Bessel functions. A flow velocity profile of the following form is used [32, 60, 66].

$$\beta = \beta_s (r/R)^n, \tag{12}$$

where  $\beta_S$  is the surface velocity, r/R is the radial position in the thermal source with radius R, and the exponent n in the flow velocity profile is a parameter. The average transverse radial flow velocity  $\langle \beta \rangle$  is given by  $\langle \beta \rangle = \frac{2}{2+n} \beta_S$ .



FIG. 12. Simultaneous Blast-Wave model fits to the  $p_{\rm T}$ -spectra of  $\pi^{\pm}$ ,  $K^{\pm}$ ,  $p(\bar{p})$  from 0–5% central Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. Uncertainties on experimental data represent statistical and systematic uncertainties added in quadrature, mostly smaller than the symbol size.

To extract the kinetic freeze-out parameters, simultaneous Blast-Wave model fits to the  $\pi^{\pm}$ ,  $K^{\pm}$  and  $p(\bar{p})$ spectra are performed [32, 60, 66] as plotted in Fig. 12 for central Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. The low- $p_{\rm T}$  region of the pion spectra is affected by resonance decays, and therefore the pion spectra above  $p_{\rm T} > 0.5$ GeV/c are used for fitting. The Blast-Wave model is not very suitable for fitting the high  $p_{\rm T}$  region of the  $p_{\rm T}$  spectra [74]. Hence, the Blast-Wave model fits are very sensitive to the  $p_{\rm T}$  range used [75]. The previously optimized  $p_{\rm T}$  ranges [32, 60, 75] are used for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV to extract the kinetic freeze-out parameters. The fit ranges used for pions, kaons, and protons are 0.5–1.35 GeV/c, 0.3–1.35 GeV/c, and 0.5–1.25 GeV/c, respectively.

Figure 13 presents the kinetic freeze-out parameters  $T_k$  (left) and  $\langle \beta \rangle$  (middle) as a function of  $N_{\text{part}}$ , and presents the correlation between  $T_k$  and  $\beta$  (right) for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. These results are compared with published data for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 7.7, 11.5, 19.6, 27, 39, 62.4, \text{ and } 200 \text{ GeV}$ measured by STAR in earlier runs [32, 60].  $T_k$  shows a dependence on  $N_{\text{part}}$ , decreasing from peripheral to central collisions. This observation supports the prediction of a short-lived fireball in the case of peripheral collisions [76]. The average flow velocity  $\langle \beta \rangle$ , on the other hand, increases from peripheral to central collisions. This indicates a higher rate of expansion of the system in central collisions. It is also seen that higher RHIC energies such as 62.4 and 200 GeV, have comparatively higher  $\beta$  than other BES-I energies. Lastly, the correlation plot between  $T_k$  and  $\beta$  confirms an anti-correlation between these two quantities, i.e. as  $T_k$  decreases,  $\beta$  increases. The behavior of the kinetic freeze-out parameters in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV is consis-



FIG. 13. Left panel:  $T_k$  as a function of  $\langle N_{\text{part}} \rangle$ . Middle panel:  $\beta$  as a function of  $\langle N_{\text{part}} \rangle$ . Right panel: variation of  $T_k$  with  $\beta$ . In all three panels, present results for Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 14.5$  GeV are shown in comparison with the same quantities for Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 7.7$ , 11.5, 19.6, 27, 39, 62.4, and 200 GeV measured by STAR in earlier runs [32]. Systematic uncertainties are shown. Statistical uncertainties are much smaller than systematic ones.

tent with previous observations [32, 60]. The extracted fit parameters  $T_k$ ,  $\langle \beta \rangle$ , and n along with the  $\chi^2$ /ndf values from the Blast-Wave model fits in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV are reported in Table VI.

#### F. Azimuthal Anisotropy

#### 1. The event plane resolution

Due to the finite multiplicity in each event, the event plane angle  $(\Psi_n)$  deviates from the reaction plane azimuthal angle  $(\Psi_R)$ . Hence a resolution correction needs to be performed to obtain the correct measurement of the flow coefficients  $(v_n)$  [54]. For this analysis, the event planes are determined from the TPC in the midrapidity region, and from the BBC at forward rapidity.

Figure 14 shows the second-order event-plane resolution from the TPC (left panel) and the first-order eventplane resolution from the BBC (right panel) as a function of centrality in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$ GeV. The event plane resolution has been calculated for nine collision centralities: 0-5%, 5-10%, 10-20%, 20-30%, 30-40%, 40-50%, 50-60%, 60-70% and 70-80%. As the event plane resolution depends on the number of particles used for event plane reconstruction, it shows a tendency to increase from peripheral to central collisions. On the other hand, the event plane is calculated using the anisotropic flow of the event itself, and therefore it tends to decrease towards central collisions where flow values are small. Because of these two competing effects, the overall resolution first increases from peripheral to mid-central collisions and then decreases. Figure 14 includes event plane resolutions for the same methods at other BES-I energies studied previously by

STAR. Due to limited statistics and poor BBC resolution, the FTPC [77] event plane is used instead of BBC at 39 GeV. As expected the resolution of the TPC and BBC event planes decreases as the collision energy increases, since the resolution depends on the multiplicity and on the  $v_2$  signal [54]. The 14.5 GeV resolution does not lie between that observed at the adjacent beam energies above and below, and instead is slightly lower than a smooth trend would predict. This is a consequence of the additional material of the Heavy Flavor Tracker close to the beam pipe, which was present only during the 2014 run at 14.5 GeV. The event plane resolution corrections to the observed  $v_n$  are applied on an event-by-event basis [55, 56]. In this method, the resolution correction has been applied by dividing the flow coefficient of each track,  $\cos n(\phi - \Psi_n)$ , by the event-plane resolution  $\langle R \rangle$  for the appropriate centrality class.

#### 2. Comparison of $v_2$ from different methods

Figure 15 presents inclusive charged particle  $v_2(p_{\rm T})$ , using various methods, for Au+Au collisions at  $\sqrt{s_{\rm NN}} =$ 14.5 GeV. The methods have different sensitivities to nonflow effects and  $v_2$  fluctuations. For the purpose of exact comparisons,  $v_2$  for each method is divided by the elliptic flow based on the two-particle cumulant method (denoted  $v_2\{2\}$ ) and the ratios are shown in the lower panels of Fig. 15. The difference of  $v_2\{2\}$  compared to  $v_2$ {BBC},  $v_2$ {4}, and  $v_2$ { $\eta$ -sub} depends on the  $p_{\rm T}$  range. A larger difference is observed in the low $p_{\rm T}$  region ( $p_{\rm T} < 1 \ {\rm GeV}/c$ ). From  $p_{\rm T} \sim 1 \ {\rm GeV}/c$  and above, the difference stays roughly constant. The difference between  $v_2$ {BBC} and  $v_2$ {4} is relatively small, and is less dependent on  $p_{\rm T}$ . The results suggest that nonflow contributions to the event plane and two-particle correlation methods depend on  $p_{\rm T}$ . They also indicate that the



FIG. 14. The event plane resolution calculated for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV (solid star) as a function of centrality. The current results are compared with those for 7.7, 11.5, 14.5, 19.6, 27 and 39 GeV. The left panel shows the second-order event plane resolution reconstructed by using the TPC tracks ( $|\eta| < 1$ ). The right panel shows the second-order event plane resolution for 39 GeV from the FTPC ( $2.5 < |\eta| < 4.0$ ) and the first-order event plane resolution from the inner tiles of the BBC ( $3.8 < |\eta| < 5.2$ ).



FIG. 15. Inclusive charged particle  $v_2$  at mid-pseudorapidity ( $|\eta| < 1.0$ ) as a function of  $p_T$  for 10–20% (left), 20–30% (middle) and 30–40% (right) centralities in Au + Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. Results are shown for the  $\eta$ -sub event plane method (circles), BBC event plane (open triangles), 2-particle (solid squares) and 4-particle (open squares) cumulants. The bottom panels show the ratio of  $v_2$  measured using the various methods with respect to the 2-particle cumulant result,  $v_2\{2\}$ . Errors are statistical. Systematic uncertainties are small (~ 2%).



FIG. 16. Inclusive charged particle elliptic flow  $v_2$  at mid-pseudorapidity ( $|\eta| < 1.0$ ) as a function of transverse momentum  $p_{\rm T}$  (top) and the  $p_{\rm T}$ -integrated  $v_2(\eta)$  for six centrality classes (bottom), obtained using the  $\eta$ -sub event plane method in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. Statistical uncertainties are shown by error bars, while systematic uncertainties are smaller and are plotted as caps.

use of the first-order reaction plane (BBC event plane) to study the second harmonic flow reduces flow fluctuations which are not correlated between different harmonics.

#### 3. Dependence of v<sub>2</sub> on transverse momentum, pseudorapidity and centrality



Results for charged particle  $v_2$  as a function of  $p_T$  for six collision centrality intervals are presented in the top panel of Fig. 16. The  $v_2$  shows a monotonically increasing trend with increasing  $p_T$  for Au+Au collisions at  $\sqrt{s_{\rm NN}} =$ 14.5 GeV. The differential  $v_2$  also exhibits centrality dependence. The trends of  $v_2(p_T)$  are similar to those observed at other BES-I energies. The bottom panel of Fig. 16 presents the  $p_T$ -integrated  $v_2(\eta)$  for six centrality classes. The  $v_2$  has a weak dependence on  $\eta$ . Also, there is a clear centrality dependence observed in  $v_2$ . The trend of  $v_2(\eta)$  is similar to that for other BES-I energies [8– 11, 32, 60, 65].

The larger magnitude of  $v_2$  in peripheral collisions can be attributed to the larger initial eccentricity in coordinate space for peripheral collisions. The participant eccentricity is the initial configuration space eccentricity of the participating nucleons. The root-mean-square participant eccentricity ( $\epsilon_{\text{part}}\{2\}$ ) is calculated from a MC Glauber model [78, 79] and reported in Table III.

In Fig. 17, the centrality dependence of  $v_2(p_T)$  over eccentricity  $\epsilon_{\text{part}}\{2\}$  is shown for Au + Au collisions at  $\sqrt{s_{\text{NN}}} = 14.5$  GeV for 10–20%, 30–40%, and 50– 60% collision centralities. Central collisions have higher  $v_2/\epsilon_{\text{part}}\{2\}$  than peripheral collisions. This finding is consistent with a picture where collective interactions are stronger in collisions with a larger number of participants. The centrality dependence of  $v_2/\epsilon_{\text{part}}\{2\}$  is observed to be similar to that reported previously by STAR [8–11, 32, 60, 65].

#### 4. Beam energy dependence of $v_2$

The BES-I data from the STAR experiment offer an opportunity to study the collision energy dependence of  $v_2$  using a wide-acceptance detector at midrapidity. Figure 18 shows the comparison of the  $p_{\rm T}$  dependence of  $v_2\{4\}$  for  $\sqrt{s_{\rm NN}} = 14.5$  GeV at 10–20%, 20–30%, and 30-40% centralities with other published results from STAR [8–11, 32, 60, 65, 80, 81] and ALICE [82]. One reason to select the  $v_2{4}$  results for this comparison is to keep the method for  $v_2$  extraction consistent with the published results from ALICE. Another reason is that  $v_{2}{4}$  is found to have low sensitivity to nonflow correlations. The 200 GeV data are empirically fit by a fifthorder polynomial function. For comparison, the  $v_2$  from other energies are divided by the fit function and shown in the lower panels of Fig. 18. We choose the 200 GeV data as a reference because its statistical uncertainties are smallest. For  $p_{\rm T}$  below 2 GeV/c, the  $v_2$  values rise with increasing collision energy. Above  $p_{\rm T} \sim 2 \ {\rm GeV}/c$ , the  $v_2$  values are comparable within statistical uncertainties. The increase of  $v_2(p_{\rm T})$  as a function of energy can be attributed to the change of chemical composition from low to high energies [32] and/or larger collectivity at the higher collision energies.

Figure 19 presents the  $\eta$  dependence of  $v_2\{\eta-\text{sub}\}$  for  $\sqrt{s_{\text{NN}}} = 7.7$  to 200 GeV. The 14.5 GeV data points are plotted as solid red stars. The dashed red line in the upper panel in Fig. 19 shows an empirical fit to the results from Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 7.7$  GeV. The bottom panel presents the ratio of  $v_2(\eta)$  from all beam energies with respect to this fitted curve. The  $v_2(\eta)$  changes shape as the beam energy decreases. The  $v_2(\eta)$  shape at 14.5 GeV follows the trend of other beam energies.

## 5. Transverse momentum, pseudorapidity, and centrality dependence of $v_1$

Measurements of the charged particle  $v_1(p_T)$  in three centralities (0-10%, 10-40% and 40-80%) in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 7.7 - 39$  GeV are presented in Fig. 20. This work focuses only on the (pseudo)rapidity-odd component of the first harmonic coefficient (directed flow). Since this component by definition has the property  $v_1(-\eta, p_T) = -v_1(\eta, p_T)$ , the integral of  $v_1(\eta, p_T)$  over





FIG. 18. The upper panels show inclusive charged particle elliptic flow  $v_2\{4\}$  versus  $p_T$  for various collision energies ( $\sqrt{s_{NN}} =$  7.7 GeV to 2.76 TeV) at three centralities: 10–20%, 20–30%, and 30–40%. The present results at 14.5 GeV (and also for other energies except 2.76 TeV) are for mid-pseudorapidity ( $|\eta| < 1.0$ ). The measurement of  $v_2$  at 2.76 TeV was done at mid-pseudorapidity ( $|\eta| < 0.8$ ). Furthermore, all results for  $\sqrt{s_{NN}} = 7.7$  to 200 GeV are for Au+Au collisions and those for 2.76 TeV are for Pb+Pb collisions. The dashed red curves show 5th-order polynomial function fits to the results from Au+Au collisions at  $\sqrt{s_{NN}} = 200$  GeV. The lower panels show the ratio of  $v_2\{4\}$  versus  $p_T$  for all  $\sqrt{s_{NN}}$  with respect to the fit curve. Error bars are shown only for statistical uncertainties. Systematic uncertainties are small ( $\sim 2\%$ )

any symmetric  $\eta$  range is zero. Therefore, in presenting the above-mentioned pseudorapidity-integrated  $p_T$ dependence, the  $v_1$  at negative  $\eta$  is multiplied by -1. By definition,  $v_1(p_T)$  must approach zero as  $p_T$  approaches zero. The observed  $v_1$  starts from a negative value, then crosses zero around  $p_T \sim 1-2$  GeV depending on collision energy and centrality. We see that, in more peripheral collisions and/or at higher energies, the sign change might occur at higher  $p_T$  compared to more central collisions and lower energies. The values of the charged particle  $v_1(p_T)$  for three centralities (0-10%, 10–40% and 40-80%) in Au+Au Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$ GeV are listed in Table VII.

Figure 21 presents the charged particle  $v_1$  as a function of  $\eta$  for three centrality classes in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 7.7 - 39$  GeV. The  $v_1$  slope at midrapidity for charged particles increases from central to peripheral collisions. The trend in  $v_1(p_{\rm T}, \eta)$  as a function of centrality for  $\sqrt{s_{\rm NN}} = 7.7 - 39$  GeV shows a similar behavior as observed in other STAR published data [8–11, 32, 60, 65]. The values of the charged particle  $v_1$  as a function of  $\eta$  for three centrality classes in Au+Au Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV are listed in Table VIII.

#### 6. Beam-energy dependence of $v_1$

The left panel in Fig. 22 shows a comparison of  $v_1(\eta)$  at 30-60% centrality for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 7.7$  – 200 GeV and for Pb+Pb collisions at  $\sqrt{s_{\rm NN}} = 2.76$  TeV. We observe a clear energy dependence in the  $v_1(\eta)$  for  $\sqrt{s_{\rm NN}} = 7.7 \,\,{\rm GeV} - 2.76 \,\,{\rm TeV}$ . To calculate the slope of  $v_1$ , we fit the data with a function  $F1 \times y + F3 \times y^3$ . The linear term in this function (F1) gives the  $v_1$  slope  $(dv_1/dy)$ . The right panel in Fig. 22 shows the beam energy dependence of  $dv_1/dy$  for 0-10%, 10–40% and 40-80% centralities for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 7.7 - 200$  GeV. The  $dv_1/dy$  for 30-60% centrality for the above energies are compared with the same from the published data from Au+Au collisions at  $\sqrt{s_{\rm NN}} = 200$  GeV at RHIC and Pb+Pb collisions at  $\sqrt{s_{\rm NN}} = 2.76$  TeV at the LHC. We observe a smooth increase in the magnitude of  $dv_1/dy$ at mid-pseudorapidity with decreasing beam energy for 30-60% centrality.

#### G. Model Comparisons

Measurements from STAR suggest that at 7.7 GeV and 11.5 GeV, particle production is dominated by hadronic processes, whereas at energies around 20 GeV and above, partonic degrees of freedom become more important [38–42]. The  $\sqrt{s_{\rm NN}} = 14.5$  GeV Au+Au collisions analyzed



FIG. 19. The upper panel shows inclusive charged particle elliptic flow  $v_2(\eta$ -sub) versus  $\eta$  at mid-pseudorapidity for various collision energies ( $\sqrt{s_{\rm NN}} = 7.7$  GeV to 200 GeV). The dashed red curve shows an empirical fit to the result from Au+Au collisions at  $\sqrt{s_{\rm NN}} = 7.7$  GeV. The lower panels shows the ratio of  $v_2$ {4} versus  $\eta$  for all  $\sqrt{s_{\rm NN}}$  with respect to the fit curve. The results are shown for 10–40% collision centrality. Error bars are shown only for statistical uncertainties.

here thus lie in a transition region of great interest. Various bulk properties of the system like  $\langle p_{\rm T} \rangle$ , dN/dy, particle ratios, elliptic flow  $v_2$ , and directed flow  $v_1$  measured in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV are compared with calculations from AMPT (version 2.25t7d) [34] and UrQMD (version 3.3p1) [33]. The initial parameter settings for the models follow the recommendations in the cited papers. The UrQMD model treats only hadronic interactions whereas AMPT has two versions — a string melting version (denoted AMPT-SM) which allows for both partonic and hadronic interactions among the particles, while the default version of AMPT treats only hadronic interactions. Recently, there have been studies with the AMPT-SM model to explain the particle multiplicity and flow measurements at RHIC and LHC using different values of the parton cascade scattering crosssection such as 1.5 mb and 10 mb. It was found that a 1.5 mb scattering cross-section gives a better description of data at these energies [83, 84]. We have generated AMPT-SM events with two different partonic cross sections (1.5 mb and 10 mb), denoted as AMPT 1.5 mb and AMPT 10mb. The larger the partonic cross section, the later the hadronic cascade begins.

#### 1. Mean transverse momentum

The average  $p_{\rm T}$  of  $\pi^+$ ,  $K^+$  and p as a function of  $\langle N_{\rm part} \rangle$  obtained from UrQMD, AMPT 1.5mb and AMPT 10mb model calculations are compared with STAR measurements for Au+Au collisions at  $\sqrt{s_{\rm NN}} =$ 14.5 GeV in Fig. 23. The value of  $\langle p_{\rm T} \rangle$  for all the studied particles is found to be too low in all AMPT-SM calculations. UrQMD is generally too low in  $\langle p_{\rm T} \rangle$  also, but is closer to the data, and shows good agreement for protons.

#### 2. Particle yields

Figure 24 shows dN/dy divided by  $0.5 \times \langle N_{\text{part}} \rangle$  versus  $\langle N_{\text{part}} \rangle$  for  $\pi^+$ ,  $K^+$  and p from Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 14.5$  GeV. The STAR measurements are compared with UrQMD and with AMPT 1.5mb and AMPT 10mb. UrQMD and AMPT are close to the  $\pi^+$  data for central collisions, but deviate for peripheral collisions. All models disagree markedly with  $K^+$  measurements. In the case of protons, AMPT-SM is close, with AMPT 1.5mb being slightly but consistently closer, while UrQMD lies well below the data at all centralities.



FIG. 20. Charged particle  $v_1$  as a function of  $p_T$  in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 7.7 - 39$  GeV for 0–10%, 10–40% and 40–80% centrality intervals. Error bars are shown only for statistical uncertainties. Systematic uncertainties are small (~ 2%).

#### 3. Particle ratios

Antiparticle to particle ratios  $(\pi^-/\pi^+, K^-/K^+)$  and  $\bar{p}/p)$  as a function of  $\langle N_{\text{part}} \rangle$  in Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 14.5$  GeV are shown in Fig. 25. These measured ratios are compared with UrQMD and AMPT-SM calculations. The pion ratios from all models are in close agreement with experiment, while AMPT gets the wrong trends for the kaons. The proton ratios from AMPT-SM are in good agreement with experiment, while UrQMD shows poor agreement.

Figure 26 shows STAR measurements of  $K^+/\pi^+$ ,  $K^-/\pi^-$ ,  $p/\pi^+$  and  $\bar{p}/\pi^-$  ratios as a function of  $\langle N_{\text{part}} \rangle$ in Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 14.5$  GeV, along with UrQMD and AMPT-SM model calculations.  $K^+/\pi^+$ and  $K^-/\pi^-$  ratios are under-predicted by all model calculations. In the case of  $p/\pi^+$ , AMPT-SM straddles the data, and in the case of  $\bar{p}/\pi^-$ , AMPT-SM shows good agreement. On the other hand, the latter two ratios are not tracked by UrQMD.

#### 4. Elliptic flow

The upper panels of Fig. 27 present the  $p_T$  dependence of  $v_2\{\eta-\text{sub}\}$  for 14.5 GeV Au+Au collisions at 10–20%, 20–30% and 30–40% centralities. The STAR measurements are compared with UrQMD, AMPT 1.5mb, and AMPT 10mb. The lower panels of Fig. 27 present the ratio of the experimental data to each model calculation. The AMPT 1.5mb calculation exhibits the best agreement, with AMPT 10mb being consistently too high and UrQMD consistently too low. Figure 28 presents very similar comparisons as Fig. 27, except transverse momentum dependence is replaced by pseudorapidity dependence. Here, again we observe similar behavior, i.e. the AMPT 1.5mb calculation exhibits the better agreement.

#### 5. Directed flow

Figure 29 presents charged particle  $v_1(p_T)$  (left panel) and  $v_1(\eta)$  (right panel) for 10–40% centrality Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. These STAR measurements are compared to UrQMD, AMPT, AMPT 1.5mb, and AMPT 10mb model calculations.

UrQMD shows poor agreement with the  $v_1$  measurements, whereas the default AMPT roughly tracks  $v_1(p_T)$ up to  $p_T \sim 1.8 \text{ GeV}/c$ . AMPT 1.5mb and AMPT 10mb are both significantly worse than the default AMPT for  $v_1(p_T)$ . No model calculation agrees with the measured



FIG. 21. Charged particle  $v_1$  as a function of  $\eta$  in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 7.7 - 39$  GeV for 0–10%, 10–40% and 40–80% centrality intervals. Error bars are shown only for statistical uncertainties. Systematic uncertainties are small (~ 2%).



FIG. 22. Left panel: Charged particle  $v_1$  as a function of  $\eta$  in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 7.7-39$  GeV for 30–60% centrality interval. Results are compared to 62.4 and 200 GeV Au+Au collisions at RHIC and to 2.76 TeV Pb+Pb collisions at the LHC. Right panel: Charged particle  $v_1$  slope,  $dv_1/dy$ , at mid-pseudorapidity as a function of  $\sqrt{s_{\rm NN}}$  for different centralities. Error bars are shown only for statistical uncertainties. Systematic uncertainties are small (~ 2%).

data for  $v_1(\eta)$ . The latest state-of-the-art models do not show even qualitative agreement with  $v_1$  measurements for identified particles at BES-I energies [85]. It should be noted that in both AMPT-SM options, antibaryons violate  $v_1 = 0$  at y = 0, as required by symmetry. This is a known artefact of the implementation of the quark coalescence mechanism in AMPT. A recent paper has shown that this artefact can be fixed with a modified quark coalescence prescription [86].



FIG. 23.  $\langle p_{\rm T} \rangle$  of  $\pi^+$ ,  $K^+$  and p as a function of  $\langle N_{\rm part} \rangle$  for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV in STAR. These measurements are compared with UrQMD, AMPT 1.5mb and AMPT 10mb.



FIG. 24.  $(dN/dy)/(0.5 \times \langle N_{\text{part}} \rangle)$  for  $\pi^+$ ,  $K^+$  and p as a function of  $\langle N_{\text{part}} \rangle$  in Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 14.5$  GeV in STAR. These measurements are compared with UrQMD, AMPT 1.5mb and AMPT 10mb.



FIG. 25.  $\pi^-/\pi^+$ ,  $K^-/K^+$  and  $\bar{p}/p$  ratios as a function of  $\langle N_{\text{part}} \rangle$  in Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 14.5$  GeV in STAR. These experimental ratios are compared with UrQMD, AMPT 1.5mb and AMPT 10mb.

#### VI. SUMMARY

We have presented basic observables for identified particles in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. The transverse momentum spectra of  $\pi$ , K, p, and  $\bar{p}$  at midrapidity (|y| < 0.1) are measured for nine centralities: 0– 5%, 5–10%, 10–20%, 20–30%, 30–40%, 40–50%, 50–60%, 60–70% and 70–80%. Bulk properties such as average transverse momentum  $\langle p_{\rm T} \rangle$ , particle yields dN/dy, particle ratios, chemical and kinetic freeze-out properties, charged particle elliptic and directed flow ( $v_2$  and  $v_1$ ) are extracted for Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. All the results are compared with the published measurements at other collisions energies.

The mean  $\langle p_{\rm T} \rangle$  values for  $\pi$ , K and p increase from peripheral to central collisions – an indication of increasing radial flow in more central collisions. The centrality dependence of radial flow is more pronounced in kaons compared to pions, and in protons compared to kaons.



FIG. 26.  $K^+/\pi^+$ ,  $K^-/\pi^-$ ,  $p/\pi^+$  and  $\bar{p}/\pi^-$  ratios as a function of  $\langle N_{\text{part}} \rangle$  in Au+Au collisions at  $\sqrt{s_{\text{NN}}} = 14.5$  GeV in STAR. These experimental ratios are compared with UrQMD, AMPT 1.5mb and AMPT 10mb.



FIG. 27. Upper panels:  $p_T$  dependence of  $v_2\{\eta-\text{sub}\}$  for 14.5 GeV Au+Au collisions at 10–20%, 20–30% and 30–40% centralities, as measured by STAR. Calculations from UrQMD, AMPT 1.5mb, and AMPT 10mb are also plotted. Lower panels: ratios of the experimental data to each model calculation.

Midrapidity particle yields for  $\pi$ , K and p show a mild centrality dependence, while no dependence on centrality is observed for  $\bar{p}$ . The  $(dN/dy)/(0.5 \times \langle N_{\text{part}} \rangle)$  for  $\pi$ , K and  $\bar{p}$  increase with collision energy, while for p it decreases with collision energy up to 39 GeV and then increases. This effect is attributed to baryon stopping at lower RHIC energies. case of  $\pi^-/\pi^+$  and  $K^-/K^+$  ratios.  $\pi^-/\pi^+$  is slightly greater than unity, which is due to isospin conservation and the contribution from decays of resonances like the  $\Delta$ . The  $\bar{p}/p$  ratio slightly decreases from peripheral to central collisions as a consequence of increasing baryon stopping in central collisions. The  $K^+/\pi^+$  and  $K^-/\pi^$ ratio increases with increasing centrality and follow the energy dependence trend established at other energies.

No significant centrality dependence is observed in the



FIG. 28. Upper panels: pseudorapidity ( $\eta$ ) dependence of  $v_2\{\eta-\text{sub}\}$  for 14.5 GeV Au+Au collisions at 10–20%, 20–30% and 30–40% centralities, as measured by STAR. Calculations from UrQMD, AMPT 1.5mb, and AMPT 10mb are also plotted. Lower panels: ratios of the experimental data to each model calculation.



FIG. 29. Charged particle  $v_1(p_T)$  (left panel) and  $v_1(\eta)$  (right panel) for 10–40% centrality Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV. The measured directed flow is compared to UrQMD, AMPT, AMPT 1.5mb, and AMPT 10mb model calculations.

The energy dependence is due to the dominance of pair production over associated production at higher energies. The  $p/\pi^+$  ratio increases from peripheral to central collisions, but no significant dependence on centrality is observed in the case of  $\bar{p}/\pi^-$  ratio.

Kinetic freeze-out parameters are obtained from simultaneous Blast-Wave model fits to the  $p_{\rm T}$  spectra for  $\pi^{\pm}$ ,  $K^{\pm}$  and  $p(\bar{p})$ . The kinetic freeze-out temperature  $T_k$ decreases from peripheral to central collisions, which is suggestive of a short-lived fireball in peripheral collisions. On the other hand, average flow velocity  $\langle \beta \rangle$  increases from peripheral to central collisions, indicating larger radial flow for central collisions, consistent with  $\langle p_T \rangle$  results.

The measured bulk observables are compared to UrQMD and AMPT model calculations. Values of  $\langle p_{\rm T} \rangle$  are underestimated by both the UrQMD and AMPT models. The AMPT model agrees with the measured dN/dy for pions ( $\langle N_{\rm part} \rangle > 100$ ) and protons, but does not reproduce kaon dN/dy. The UrQMD model mostly shows poor agreement with dN/dy for all the measured particles.  $\pi^-/\pi^+$  ratios are reproduced within uncer-

tainties by both AMPT and UrQMD models. All models show poor agreement with STAR data of  $K^-/K^+$  and  $K/\pi$  ratios. The  $\bar{p}/p$  ratio is well described by AMPT but not by UrQMD. The measured  $p/\pi^+$  and  $\bar{p}/\pi^-$  ratios are poorly reproduced by UrQMD, while AMPT does better. The dependence of  $v_2$  of charged particles at midrapdity, on  $p_{\rm T}$  and  $\eta$  is similar to that observed at other BES-I energies. The  $v_2$  in peripheral collisions is larger than in central collisions. A clear centrality dependence is observed in  $v_2$ . A weak dependence of the  $p_{\rm T}$ -integrated charged particle  $v_2$  on  $\eta$  is observed. The shape of  $v_2(\eta)$ at 14.5 GeV resembles that reported at other beam energies.

The magnitude of charged particle  $v_1$  increases from central to peripheral collisions at 14.5 GeV, and a similar pattern is observed at other beam energies. The magnitude of  $v_1$  decreases with increasing beam energy.

The UrQMD model underpredicts the STAR measurement of charged particle  $v_2$  at 14.5 GeV. The AMPT string melting option with 10 mb parton-parton interaction cross section overpredicts the data, while the 1.5 mb option is closer. The UrQMD model shows poor agreement with both  $v_1(p_T)$  and  $v_1(\eta)$  at 14.5 GeV.

The measured observables ( $\langle p_{\rm T} \rangle$ , dN/dy, particle ratios, chemical and kinetic freeze-out parameters,  $v_2$  and  $v_1$ ) in Au+Au collisions at  $\sqrt{s_{\rm NN}} = 14.5$  GeV conform to the smooth trend of beam energy dependence reported in prior publications. The results at 14.5 GeV are important since they fill the gap in  $\mu_B$  of the order of about 100 MeV between beam energies 11.5 GeV and 19.6 GeV. The results will help in tuning the parameters of various models intended to explain the low energy data. Previous measurements by the STAR collaboration have revealed interesting trends related to the dominance of hadronic interaction and partonic interactions in observables such as higher moments of conserved quantities [35],  $v_1$  [36], correlations [37], azimuthal anisotropy [38], and  $R_{CP}$  [44] between  $\sqrt{s_{\rm NN}} = 11.5$  and 19.6 GeV. The data set at 14.5 GeV has provided a clearer understanding of the beamenergy dependence of bulk observables.

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TABLE III. Summary of centrality bins, average number of participants  $N_{\text{part}}$ , number of binary collisions  $N_{\text{coll}}$ , reaction plane eccentricity  $\epsilon_{\text{RP}}$ , participant eccentricity  $\epsilon_{\text{part}}$ , root-mean-square of the participant eccentricity  $\epsilon_{\text{part}}\{2\}$ , and transverse area  $S_{\text{part}}$  from MC Glauber simulations at  $\sqrt{s_{NN}} = 14.5$  GeV. The errors are systematic uncertainties.

Centrality (%)	$\langle N_{\rm part} \rangle$	$\langle N_{\rm coll} \rangle$	$\langle \epsilon_{ m RP}  angle$	$\langle \epsilon_{\mathrm{part}} \rangle$	$\epsilon_{\text{part}}\{2\}$	$\langle S_{\rm part} \rangle$
0 - 5	$338 \pm 2$	$788 \pm 30$	$0.04 \pm 0.01$	$0.10 \pm 0.01$	$0.12\pm0.01$	$25.5 \pm 0.6$
5 - 10	$289 \pm 6$	$634\pm20$	$0.11\pm0.01$	$0.15 \pm 0.01$	$0.16\pm0.01$	$22.9\pm0.7$
10 - 20	$226\pm8$	$454\pm24$	$0.18\pm0.01$	$0.22\pm0.01$	$0.24\pm0.01$	$19.3\pm0.8$
20 - 30	$159 \pm 10$	$283\pm24$	$0.27\pm0.01$	$0.30 \pm 0.01$	$0.32\pm0.01$	$15.5\pm0.9$
30 - 40	$108\pm10$	$168\pm22$	$0.32 \pm 0.01$	$0.37\pm0.01$	$0.40\pm0.01$	$12.4 \pm 1.0$
40 - 50	$70 \pm 8$	$94 \pm 18$	$0.37\pm0.01$	$0.44 \pm 0.01$	$0.47\pm0.01$	$9.8\pm1.1$
50 - 60	$44 \pm 8$	$50 \pm 12$	$0.39\pm0.01$	$0.51 \pm 0.01$	$0.54\pm0.01$	$7.6\pm1.1$
60 - 70	$26 \pm 7$	$25 \pm 9$	$0.40 \pm 0.01$	$0.59 \pm 0.01$	$0.62 \pm 0.01$	$5.6 \pm 1.2$
70 - 80	$14 \pm 5$	$12 \pm 5$	$0.37\pm0.01$	$0.68\pm0.01$	$0.72\pm0.01$	$3.5\pm1.2$

TABLE IV. dN/dy values for  $\pi^+$ ,  $\pi^-$ ,  $K^+$ ,  $K^-$ , p, and  $\bar{p}$  from Au+Au collisions at  $\sqrt{s_{NN}} = 14.5$  GeV. The uncertainties represent statistical and systematic uncertainties, respectively.

Centra- lity(%)	$\pi^+$	$\pi^{-}$	$K^+$	$K^{-}$	p	$\bar{p}$
0 - 5	$141 \pm 0.2 \pm 14$	$145 \pm 0.2 \pm 15$	$26.7 \pm 0.04 \pm 2.8$	$14.9 \pm 0.03 \pm 1.6$	39.0 pm 0.03 $\pm$ 4.7	$2.5 \pm 0.02 \pm 0.3$
5 - 10	$112 \pm 0.2 \pm 11$	$116 \pm 0.1 \pm 12$	$22.3\pm0.04\pm2.4$	$12.4 \pm 0.03 \pm 1.2$	$33.1 \pm 0.03 \pm 4.0$	$2.0\pm0.01\pm0.2$
10 - 20	$87.3 \pm 0.1 \pm 9.1$	$90.0 \pm 0.1 \pm 9.2$	$16.4 \pm 0.03 \pm 1.7$	$9.5 \pm 0.02 \pm 1.0$	$24.5 \pm 0.03 \pm 2.9$	$1.6\pm0.01\pm0.2$
20 - 30	$59.1 \pm 0.1 \pm 6.1$	$61.3 \pm 0.1 \pm 6.4$	$10.8\pm0.02\pm1.1$	$6.3 \pm 0.02 \pm 0.6$	$16.2 \pm 0.02 \pm 2.0$	$1.2\pm0.01\pm0.1$
30 - 40	$38.6 \pm 0.1 \pm 4.0$	$40.0\pm0.1\pm4.1$	$6.8\pm0.02\pm0.7$	$4.1 \pm 0.01 \pm 0.4$	$10.5 \pm 0.02 \pm 1.3$	$0.9\pm0.01\pm0.1$
40 - 50	$24.6 \pm 0.1 \pm 2.6$	$25.5 \pm 0.1 \pm 2.6$	$4.1\pm0.01\pm0.4$	$2.4 \pm 0.01 \pm 0.3$	$6.3 \pm 0.01 \pm 0.8$	$0.60\pm0.004\pm0.07$
50 - 60	$14.7\pm0.04\pm1.5$	$15.4 \pm 0.04 \pm 1.5$	$2.2\pm0.01\pm0.2$	$1.3\pm0.01\pm0.1$	$3.5\pm0.01\pm0.4$	$0.33 \pm 0.003 \pm 0.04$
60 - 70	$8.5\pm0.03\pm0.9$	$8.8 \pm 0.03 \pm 0.9$	$1.2\pm0.01\pm0.1$	$0.72\pm0.01\pm0.07$	$1.9\pm0.01\pm0.2$	$0.16 \pm 0.003 \pm 0.02$
70 - 80	$4.5\pm0.03\pm0.5$	$4.8 \pm 0.03 \pm 0.6$	$0.55\pm0.01\pm0.06$	$0.36\pm0.01\pm0.04$	$0.6 \pm 0.01 \pm 0.1$	$0.11\pm0.002\pm0.01$

TABLE V. The  $\langle p_{\rm T} \rangle$  (MeV/c) values for  $\pi^+$ ,  $\pi^-$ ,  $K^+$ ,  $K^-$ , p, and  $\bar{p}$  from Au+Au collisions at  $\sqrt{s_{NN}} = 14.5$  GeV. The uncertainties represent statistical and systematic uncertainties, respectively.

$\frac{\text{Centra-}}{\text{lity}(\%)}$	$\pi^+$	$\pi^{-}$	$K^+$	$K^{-}$	p	$\bar{p}$
0 - 5	$395 \pm 0.1 \pm 22$	$392 \pm 0.1 \pm 21$	$586 \pm 0.1 \pm 32$	$560 \pm 0.1 \pm 30$	$811 \pm 0.1 \pm 53$	$807 \pm 0.2 \pm 69$
5 - 10	$393\pm0.1\pm22$	$390 \pm 0.1 \pm 21$	$575\pm0.1\pm32$	$559 \pm 0.1 \pm 30$	$798\pm0.1\pm52$	$800 \pm 0.2 \pm 68$
10 - 20	$393 \pm 0.2 \pm 22$	$388 \pm 0.2 \pm 21$	$574\pm0.1\pm32$	$552 \pm 0.1 \pm 30$	$781\pm0.1\pm51$	$776 \pm 0.2 \pm 66$
20 - 30	$389 \pm 0.2 \pm 21$	$384 \pm 0.2 \pm 20$	$560\pm0.2\pm31$	$540 \pm 0.1 \pm 29$	$765\pm0.1\pm50$	$751 \pm 0.3 \pm 64$
30 - 40	$382 \pm 0.2 \pm 21$	$380\pm0.2\pm20$	$555\pm0.2\pm31$	$532 \pm 0.1 \pm 29$	$730 \pm 0.1 \pm 48$	$726 \pm 0.3 \pm 62$
40 - 50	$374 \pm 0.3 \pm 21$	$374 \pm 0.3 \pm 20$	$530 \pm 0.2 \pm 29$	$513 \pm 0.1 \pm 28$	$686\pm0.1{\pm}45$	$675 \pm 0.4 \pm 57$
50 - 60	$365\pm0.3\pm20$	$366 \pm 0.3 \pm 19$	$518\pm0.3\pm29$	$495\pm0.2\pm27$	$646\pm0.1\pm42$	$640 \pm 0.4 \pm 54$
60 - 70	$356\pm0.4\pm20$	$355 \pm 0.4 \pm 19$	$496\pm0.4\pm27$	$475 \pm 0.2 \pm 26$	$627 \pm 0.1 \pm 40$	$606\pm0.1\pm52$
70 - 80	$349 \pm 1 \pm 19$	$347 \pm 1 \pm 18$	$484 \pm 1 \pm 27$	$460 \pm 1 \pm 25$	$587 \pm 2 \pm 38$	$573 \pm 1 \pm 49$

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Centrality(%)	$T_k \; ({\rm MeV})$	$\langle \beta \rangle$	n	$\chi^2/\mathrm{ndf}$
0 - 5	$114 \pm 7$	$0.485 \pm 0.036$	$0.97 \pm 0.28$	0.119
5 - 10	$116 \pm 7$	$0.442 \pm 0.035$	$0.98 \pm 0.29$	0.097
10 - 20	$118 \pm 7$	$0.429 \pm 0.034$	$0.99\pm0.33$	0.119
20 - 30	$122 \pm 7$	$0.401 \pm 0.034$	$1.00 \pm 0.39$	0.056
30 - 40	$124 \pm 8$	$0.371 \pm 0.042$	$1.34 \pm 0.42$	0.123
40 - 50	$130 \pm 6$	$0.312 \pm 0.036$	$1.73 \pm 0.61$	0.232
50 - 60	$134 \pm 6$	$0.238 \pm 0.031$	$2.26 \pm 0.78$	0.398
60 - 70	$136 \pm 6$	$0.194 \pm 0.030$	$2.76 \pm 0.87$	0.484
70 - 80	$139 \pm 7$	$0.168 \pm 0.030$	$2.83 \pm 1.20$	0.354

TABLE VI. Kinetic freeze-out parameters  $T_k$ ,  $\langle \beta \rangle$ , n and  $\chi^2$ /ndf values from Blast-Wave fits in Au+Au collisions at  $\sqrt{s_{NN}} =$  14.5 GeV. The quoted errors are total statistical and systematic uncertainties added in quadrature.

TABLE VII. Inclusive charged particle  $v_1$  as function of  $p_T$  in Au+Au collisions at  $\sqrt{s_{NN}} = 14.5$  GeV. The uncertainties represent statistical and systematic uncertainties, respectively.

$p_{\rm T} \; ({\rm GeV}/c)$	$v_1(0-10\%)$	$v_1 \ (10-40\%)$	$v_1 (40-80\%)$
0.30	$-0.0027 \pm 0.0003 \pm 0.0001$	$-0.0071 \pm 0.0001 \pm 0.0004$	$-0.0130 \pm 0.0002 \pm 0.0007$
0.50	$-0.0034 \pm 0.0003 \pm 0.0002$	$-0.0093 \pm 0.0001 \pm 0.0005$	$-0.0176 \pm 0.0002 \pm 0.0008$
0.70	$-0.0032 \pm 0.0004 \pm 0.0002$	$-0.0096 \pm 0.0001 \pm 0.0004$	$-0.0201 \pm 0.0003 \pm 0.0009$
0.90	$-0.0024 \pm 0.0006 \pm 0.0003$	$-0.0087 \pm 0.0002 \pm 0.0003$	$-0.0216 \pm 0.0004 \pm 0.0010$
1.10	$0.0014 \pm 0.0008 \pm 0.0005$	$-0.0070 \pm 0.0003 \pm 0.0004$	$-0.0219 \pm 0.0006 \pm 0.0007$
1.30	$0.0019 \pm 0.0010 \pm 0.0005$	$-0.0045 \pm 0.0003 \pm 0.0001$	$-0.0226 \pm 0.0008 \pm 0.0005$
1.50	$0.0047 \pm 0.0014 \pm 0.0007$	$-0.0025 \pm 0.0005 \pm 0.0003$	$-0.0209 \pm 0.0011 \pm 0.0009$
1.70	$0.0040 \pm 0.0019 \pm 0.0007$	$-0.0002 \pm 0.0006 \pm 0.0003$	$-0.0185 \pm 0.0016 \pm 0.0008$
1.90	$0.0079 \pm 0.0026 \pm 0.0007$	$0.0024 \pm 0.0009 \pm 0.0003$	$-0.0179 \pm 0.0023 \pm 0.0008$
2.10	$0.0095 \pm 0.0036 \pm 0.0014$	$0.0059 \pm 0.0012 \pm 0.0004$	$-0.0173 \pm 0.0032 \pm 0.0013$
2.30	$0.0155 \pm 0.0050 \pm 0.0021$	$0.0097 \pm 0.0017 \pm 0.0007$	$-0.0125 \pm 0.0046 \pm 0.0015$
2.50	$0.0089 \pm 0.0069 \pm 0.0024$	$0.0081 \pm 0.0024 \pm 0.0007$	$-0.0067 \pm 0.0065 \pm 0.0024$

TABLE VIII. Inclusive charged particle  $v_1$  as function of  $\eta$  in Au+Au collisions at  $\sqrt{s_{NN}} = 14.5$  GeV. The uncertainties represent statistical and systematic uncertainties, respectively.

η	$v_1(0-10\%)$	$v_1 (10-40\%)$	$v_1 (40-80\%)$
-0.95	$0.0059 \pm 0.0008 \pm 0.0007$	$0.0157 \pm 0.0003 \pm 0.0005$	$0.0334 \pm 0.0006 \pm 0.0000$
-0.85	$0.0048 \pm 0.0008 \pm 0.0006$	$0.0137 \pm 0.0003 \pm 0.0003$	$0.0295 \pm 0.0005 \pm 0.0000$
-0.75	$0.0034 \pm 0.0008 \pm 0.0003$	$0.0119 \pm 0.0002 \pm 0.0001$	$0.0258 \pm 0.0005 \pm 0.0000$
-0.65	$0.0030 \pm 0.0007 \pm 0.0003$	$0.0108 \pm 0.0002 \pm 0.0001$	$0.0211 \pm 0.0005 \pm 0.0000$
-0.55	$0.0019 \pm 0.0007 \pm 0.0003$	$0.0089 \pm 0.0002 \pm 0.0001$	$0.0186 \pm 0.0005 \pm 0.0000$
-0.45	$0.0015 \pm 0.0007 \pm 0.0003$	$0.0073 \pm 0.0002 \pm 0.0001$	$0.0137 \pm 0.0005 \pm 0.0000$
-0.35	$0.0032 \pm 0.0007 \pm 0.0003$	$0.0054 \pm 0.0002 \pm 0.0000$	$0.0111 \pm 0.0005 \pm 0.0002$
-0.25	$0.0015 \pm 0.0007 \pm 0.0003$	$0.0043 \pm 0.0002 \pm 0.0001$	$0.0083 \pm 0.0005 \pm 0.0001$
-0.15	$0.0015 \pm 0.0007 \pm 0.0006$	$0.0026 \pm 0.0002 \pm 0.0001$	$0.0049 \pm 0.0005 \pm 0.0001$
-0.05	$0.0007 \pm 0.0007 \pm 0.0004$	$0.0005 \pm 0.0002 \pm 0.0001$	$0.0013 \pm 0.0005 \pm 0.0001$
0.05	$-0.0004 \pm 0.0007 \pm 0.0003$	$-0.0007 \pm 0.0002 \pm 0.0001$	$-0.0025 \pm 0.0005 \pm 0.0002$
0.15	$-0.0008 \pm 0.0007 \pm 0.0003$	$-0.0028 \pm 0.0002 \pm 0.0001$	$-0.0051 \pm 0.0005 \pm 0.0001$
0.25	$-0.0013 \pm 0.0007 \pm 0.0004$	$-0.0045 \pm 0.0002 \pm 0.0001$	$-0.0072 \pm 0.0005 \pm 0.0001$
0.35	$-0.0011 \pm 0.0007 \pm 0.0002$	$-0.0058 \pm 0.0002 \pm 0.0001$	$-0.0123 \pm 0.0005 \pm 0.0001$
0.45	$-0.0009 \pm 0.0007 \pm 0.0003$	$-0.0078 \pm 0.0002 \pm 0.0002$	$-0.0151 \pm 0.0005 \pm 0.0002$
0.55	$-0.0035 \pm 0.0007 \pm 0.0003$	$-0.0088 \pm 0.0002 \pm 0.0002$	$-0.0182 \pm 0.0005 \pm 0.0003$
0.65	$-0.0029 \pm 0.0007 \pm 0.0003$	$-0.0107 \pm 0.0002 \pm 0.0001$	$-0.0230 \pm 0.0005 \pm 0.0001$
0.75	$-0.0034 \pm 0.0008 \pm 0.0003$	$-0.0123 \pm 0.0002 \pm 0.0000$	$-0.0255 \pm 0.0005 \pm 0.0002$
0.85	$-0.0041 \pm 0.0008 \pm 0.0008$	$-0.0134 \pm 0.0002 \pm 0.0001$	$-0.0285 \pm 0.0005 \pm 0.0004$
0.95	$-0.0027 \pm 0.0008 \pm 0.0007$	$-0.0154 \pm 0.0003 \pm 0.0002$	$-0.0338 \pm 0.0006 \pm 0.0005$