Title
Ohmic energy confinement saturation and core toroidal rotation reversal in Alcator C-Mod plasmas

Permalink
https://escholarship.org/uc/item/3nd0d26q

Journal
PHYSICS OF PLASMAS, 19(5)

ISSN
1070-664X

Authors
Rice, JE
Greenwald, MJ
Podpaly, YA
et al.

Publication Date
2012-05-01

DOI
10.1063/1.3695213

Peer reviewed
Ohmic energy confinement saturation and core toroidal rotation reversal in Alcator C-Mod plasmas$^{a}$

J. E. Rice,$^{1, b}$ M. J. Greenwald,$^{1}$ Y. A. Podpaly,$^{1}$ M. L. Reinke,$^{1}$ P. H. Diamond,$^{2}$ J. W. Hughes,$^{1}$ N. T. Howard,$^{1}$ Y. Ma,$^{1}$ I. Cziegler,$^{1}$ B. P. Duval,$^{3}$ P. C. Ennever,$^{1}$ D. Ernst,$^{1}$ C. L. Fiore,$^{1}$ C. Gao,$^{1}$ J. H. Irby,$^{1}$ E. S. Marmar,$^{1}$ M. Porkolab,$^{1}$ N. Tsujii,$^{1}$ and S. M. Wolfe$^{1}$

$^{1}$Plasma Science and Fusion Center, MIT, Cambridge, Massachusetts 02139, USA
$^{2}$UCSD, La Jolla, California 92903, USA
$^{3}$CRPP, EPFL, Lausanne 1015, Switzerland

(Received 30 November 2011; accepted 13 January 2012; published online 26 March 2012)

Ohmic energy confinement saturation is found to be closely related to core toroidal rotation reversals in Alcator C-Mod tokamak plasmas. Rotation reversals occur at a critical density, depending on the plasma current and toroidal magnetic field, which coincides with the density separating the linear Ohmic confinement regime from the saturated Ohmic confinement regime. The rotation is directed co-current at low density and abruptly changes direction to counter-current when the energy confinement saturates as the density is increased. Since there is a bifurcation in the direction of the rotation at this critical density, toroidal rotation reversal is a very sensitive indicator in the determination of the regime change. The reversal and confinement saturation results can be unified, since these processes occur in a particular range of the collisionality. © 2012 American Institute of Physics. [http://dx.doi.org/10.1063/1.3695213]

I. INTRODUCTION

It has been widely observed that Ohmic energy confinement in tokamaks increases linearly with electron density, and then saturates at a critical density. An example of this behavior is shown in Fig. 1, which was obtained from a shot by shot scan of the electron density in 5.2 T, 0.81 MA ($q_{95} = 4.3$) plasmas from Alcator C-Mod. The energy confinement time was determined from the kinetic profiles during the steady state portion of each discharge. The vertical shaded region indicates the separation between the linear Ohmic confinement (LOC) and saturated Ohmic confinement (SOC) regimes, at a line-averaged electron density around $0.8 \times 10^{20}/m^{3}$ for these conditions. The dashed line represents the neo-Alcator scaling, $t_{EA}(ms) = 70 \ n_{i} q_{4} \sqrt{\kappa R^{2}}$, with $a$ and $R$ in m and $n_{i}$ in $10^{20}/m^{3}$. This line is fairly close to the low density data points. For these discharges, the elongation, $\kappa$, was 1.6, with $a = 0.22$ m and $R = 0.68$ m. This particular scaling was developed for circular plasmas (with an ad hoc $\sqrt{\kappa}$ added) and does not include contemporary devices. For comparison, the solid line indicates the best linear fit to the low density points. At high density, in the saturated regime, the data points are well represented by the ITER-89P L-mode confinement time scaling, $t_{E89P}(ms) = 48 \ I^{0.85} R^{1.2} \ a^{-0.3} \ \kappa^{0.5} \ B^{0.2} \ A^{0.5} \ n_{i}^{0.1} \ T^{-0.5}$ (with I in MA, B in T and A, the atomic mass of the background ion, in AMU), shown by the dash-dot line. For these deuterium discharges, the Ohmic input power, $P$, was around 0.9 MW, and the agreement between the scaling and the observations is quite good.

The behavior in the LOC regime is not well understood theoretically. The commonly accepted ansatz is that at low density, electron turbulence regulates the confinement, while in the saturated regime, ion temperature gradient (ITG) modes dominate. In fact, measured turbulence changes at the LOC/SOC transition are in agreement with this concept. The LOC/SOC transition and core toroidal rotation reversals, unification of observations with collisionality, and a comparison of results from many different devices are shown in Sec. III. Additional rotation reversal observations are presented in Sec. IV, followed by discussion, including the results from gyro-kinetic code simulations, and conclusions in Sec. V.

II. EXPERIMENTAL SETUP

These experiments were performed on the Alcator C-Mod tokamak, a compact ($R_{0} = 0.67$ m, $a \sim 0.21$ m), high magnetic field ($B \leq 8$ T) device with strong shaping capabilities. For the observations presented here, the plasma current was in the range from 0.4 to 1.2 MA, the toroidal magnetic field was between 2.8 and 8 T ($2.6 \leq q_{95} \leq 7.2$) and the elongation ranged from 1.5 to 1.7. Systematic density scans were performed shot by shot from 0.3 to $2.0 \times 10^{20}/m^{3}$. Electron density and temperature profiles were measured using Thomson scattering, $Z_{eff}$ was determined from visible bremsstrahlung, and core toroidal rotation and ion temperatures were measured with a high resolution imaging x-ray spectrometer system. The energy confinement time was evaluated.

$^{b}$Invited speaker.
both from magnetics measurements\textsuperscript{24} and from complete density and temperature profiles. All observations presented here were from diverted Ohmic L-mode plasmas (no external momentum input), and the results are all averaged over sawtooth oscillations.

III. OHMIC CONFINEMENT SATURATION AND ROTATION REVERSALS

The correlation between the LOC/SOC transition and rotation reversals is demonstrated in Fig. 2, from electron density scans at 5.2 T, for two different plasma currents.

For 0.62 MA discharges ($q_{95} = 5.0$), the critical density for rotation reversal was $0.59 \times 10^{20} \text{m}^{-3}$ (bottom left), very close to the break in slope of the energy confinement time\textsuperscript{14,15} (top left). Below this density, the rotation is directed co-current, while above the threshold the rotation is in the counter-current direction (indicated by negative values). Here, the confinement time was determined from magnetic measurements, since full kinetic profiles were not available for all of the discharges. For the 1.0 MA plasmas ($q_{95} = 3.2$), the density for rotation reversal (bottom right) and confinement saturation (top right) also coincide, but in this case at $0.96 \times 10^{20} \text{m}^{-3}$. From a series of density scans at different plasma currents and fixed magnetic field (5.2 T), the LOC/SOC transition density has been determined (from shot by shot density scans of the energy confinement time) as a function of $I_p$ and is shown in the top panel of Fig. 3.

This linear increase of the confinement saturation density with plasma current has also been observed in JFT-2 M discharges.\textsuperscript{3} The dashed curve in the top frame represents an empirical scaling, $n_{\text{crit}} = 0.65 \sqrt{A B/R q}$,\textsuperscript{3} derived from four JAERI tokamaks. Shown for comparison in the bottom panel of Fig. 3 is the rotation reversal density, which has the same dependence (and slope) as for the confinement saturation,\textsuperscript{14,15} indicating the close relationship between the two phenomena. The dotted line in the bottom frame is the best fit to the data points; the dotted line in the top frame is the same as shown in the bottom frame. There are many more points for the rotation reversals, since the critical density can be determined in a single discharge from a slight density ramp, and a change in sign of the rotation velocity is quite easy to detect.\textsuperscript{14,15,26–28} To find the confinement saturation density, a complete shot by shot density scan is required.
which can take the better part of a single run day. Also, the exact density where the change in slope of the energy confinement time between LOC and SOC occurs is not as precise as the reversal density (see Figs. 1 and 2). To determine the energy confinement saturation density, fits are performed on the low density points (similar to the Alcator scaling) and high density points (similar to the L-mode scaling). The intercept of these two curves is taken as the saturation density, with error bars determined from the ranges of the two fits.

Shot by shot scans of other relevant parameters, the central electron and ion temperatures, \( Z_{\text{eff}} \) and \( R/L_n \) (evaluated at \( r/a = 0.6 \) and \( R = 0.80 \) m), for the 0.62 MA, 5.2 T discharges of Fig. 2 are shown in Fig. 4.

The temperatures and \( Z_{\text{eff}} \) vary monotonically with density. At the LOC/SOC transition, the value of \( T_e/T_i \) was \( \sim 1.35 \); this is close to \( T_e/T_i \sim 1.5 \) observed in ASDEX Upgrade at the LOC/SOC transition.\(^{19}\) In contrast, there is an abrupt change in slope of the density gradient scale length (bottom frame) at the transition density. In the LOC regime, as the density increases, the electron density profile becomes more peaked. In the saturated regime, the density profile maintains its shape. Similar behavior has been observed in ASDEX Upgrade plasmas as well,\(^{16,19}\) at the LOC-SOC transition, the value of \( R/L_n \) at the mid radius was \( \sim 5.5 \), the same as for C-Mod in Fig. 4.

In an attempt to unify the rotation reversal and confinement saturation observations, and in order to understand why the processes occur at a different electron density for different plasma currents, the collisionality has been examined. Shown in Fig. 5 are the central rotation velocities as a function of effective collisionality in the core for the density scans at 0.62 and 1.0 MA.

Here, \( \nu_{\text{eff}} \) is the ratio between the collision frequency and the curvature drift frequency, given by
\[
\nu_{\text{eff}} \approx R Z_{\text{eff}} n_e / T_e^2,
\]
with \( R \) in m, \( n_e \) in \( 10^{20} / \text{m}^3 \) and \( T_e \) in keV.\(^{22}\) The reversals occur for similar values of \( \nu_{\text{eff}} \), 0.32 for the lower current and 0.42 for the higher current plasmas. These numbers are somewhat similar in magnitude to \( \nu_{\text{eff}} = 0.9 \) where the turbulence propagation (measured by Doppler reflectometry) changed sign in ASDEX Upgrade plasmas.\(^{22}\) The rotation reversals also coincide (for the same scans) using the collisionality \( \nu_s \), the ratio of collision frequency to the bounce frequency \( (\nu_s \equiv 0.0118 q R Z_{\text{eff}} n_e / T_e^2)^{1.5} \) as shown in Fig. 6.

For this plot, \( \nu_s \) was evaluated at the \( q = 3/2 \) surface, which is the radius inside of which the rotation reversal occurs.\(^{14}\) For the 0.62 MA and 1.0 MA discharges, the \( q = 3/2 \) surfaces were located at \( r/a \sim 0.5 \) and 0.7, respectively. In this case, the \( \nu_s \) values for the reversals are very close, 0.41 for

FIG. 4. The electron and ion temperatures (top), their ratio (second frame), effective Z (third frame), and inverse density gradient scale length (bottom) at \( r/a = 0.6 \) (\( R = 0.80 \) m) as a function of electron density for 0.62 MA, 5.2 T discharges. The dotted vertical line indicates the LOC/SOC transition density.

FIG. 5. The core toroidal rotation velocities as a function of \( \nu_{\text{eff}} \) for plasma currents of 0.62 MA (top) and 1.0 MA (bottom). Vertical lines indicate the co- to counter-current rotation boundary.

FIG. 6. The core toroidal rotation velocities as a function of \( \nu_s \) for plasma currents of 0.62 MA (top) and 1.0 MA (bottom). Vertical lines indicate the co- to counter-current rotation boundary.
0.62 MA and 0.45 for 1.0 MA. This agreement may be fortu-
tous, since \( R/C_2 \) is very sensitive to the electron temperature; at
other radial locations, the agreement may not be so good.
These values are also very close to the number \( R/C_2 = 0.35 \) eval-
uated at \( r/a = 0.7 \), where the turbulence propagation reversals
were observed at ASDEX Upgrade.22

Since the density for rotation reversal and confinement
saturation is proportional to plasma current \( (n_{\text{crit}} \propto I_p \propto q^{-1}) \), it is not surprising that this occurs at \( \nu_e \propto n_q = \text{const.} \)
This speculation can be further supported by comparing con-
finement saturation results from several devices referenced
in the Sec. I. Shown in Fig. 7 is the density of the LOC/SOC
transition at fixed \( q \) (between 2.8 and 3.8) as a function of
major radius for various tokamaks.

These results are consistent with a 1/R scaling. The
point from tokamak configuration variable (TCV) (Ref. 26)
and those from C-Mod without error bars are from rotation
reversals. For ITER plasmas, the boundary density between
LOC and SOC is expected to be \( \leq 1 \times 10^{20}/m^3 \), based on an
extrapolation of Fig. 7. These results suggest that confinement
saturation may occur in a range of collisionality, with \( \nu_e \propto n_R q = \text{const.} \)
The C-Mod and ASDEX Upgrade (AUG)
results are consistent with a value \( \nu_e \sim 0.4 \) for \( r/a \sim 0.7 \).

There is a factor of \( Z_{\text{eff}}/T_\text{e}^2 \) in the expressions for the col-
lisionality. It turns out that this is a weakly varying function
of density near the transition point, as can be seen in Fig. 8,
which was derived from Fig. 4.

The ratio is about 0.8 at the reversal density, and only
changes by \( \sim 20\% \) over this density range, thus contributing
to the collisionality variation only slightly.

IV. ROTATION REVERSAL CHARACTERISTICS

In Sec. III, rotation reversals were obtained by changing
the electron density, either by means of dynamic ramps or
during shot to shot scans. Reversals can also be induced by
changing the plasma current, as is demonstrated in Fig. 9.

The plasma current was ramped down in steps for this 6.3 T
discharge, while the density was held fixed.

As the plasma current was reduced, the rotation reversed
direction and incremented in the counter-current direction.
There was a delay in the response of the rotation to the current
ramps. This delay is between the momentum confinement
time (\( \sim 30 \text{ ms} \)) and the current relaxation time. The depend-
extence of the core toroidal rotation velocity on plasma current is
shown in Fig. 10, from a shot by shot scan at fixed magnetic
field (5.2 T) and electron density \( (0.8\sim1.2 \times 10^{20}/m^3) \).

There is a linear increase in the velocity with plasma current,30,31
 trending in the co-current direction. The velocity

FIG. 7. The transition density from LOC to SOC as a function of major radius for different devices at fixed values of \( q \). The solid curve represents 1/R.

FIG. 8. The ratio \( Z_{\text{eff}}/T_\text{e}^2 \) as a function of density for the 5.2 T, 0.62 MA discharges of Fig. 4, in the vicinity of the LOC-SOC transition point.

FIG. 9. The electron density (top), plasma current (middle), and core rotation velocity (bottom) for a 6.3 T discharge with downward current ramps.
reverses direction at around 0.9 MA for this range of density, consistent with the density ramp results at fixed current.\textsuperscript{14} This trend with plasma current in Ohmic L-mode plasmas is the inverse of the current dependence in H-mode, I-mode, and other enhanced confinement regimes, where the toroidal rotation velocity was found to scale $\propto 1/I_p$.\textsuperscript{32--34}

Rotation reversals have also been observed with magnetic field ramps at fixed density.\textsuperscript{14} Shown in Fig. 11 are the parameter time histories in a 0.8 MA discharge with a downward magnetic field ramp.

As the magnetic field was decreased, the core toroidal rotation velocity incremented in the co-current direction and eventually reversed. In general, with increasing magnetic field, the rotation velocity becomes more counter-current.\textsuperscript{30,35} Shown in Fig. 12 is the core rotation velocity as a function of magnetic field at fixed plasma current (1.0 MA) and electron density ($1.17 \times 10^{20}/m^3$) from a shot by shot scan.

Although the rotation velocity did not reverse in this scan, it would be expected to change direction around 6 T, consistent with other observations.\textsuperscript{14} Unlike the density dependence, where an abrupt rotation reversal is seen for a small change in $n_e$, there is a continuous dependence on plasma current and magnetic field at fixed density, with weaker bifurcation. This may explain the reduced hysteresis seen with magnetic field ramps.\textsuperscript{14} Regardless of the dynamics, these trends with plasma current and magnetic field are consistent with the notion that reversals occur in a limited range of collisionality, with $\nu_s \propto n_q = \text{const}$.

An important clue to the underlying cause for the rotation reversals and the LOC-SOC transition can be found by examining associated changes in the core turbulence characteristics. At low density with co-current rotation, in the LOC regime, a feature in the spectra of density fluctuations (measured with the phase contrast imaging diagnostic) extending up to and above $k_h \sim 10$ cm$^{-1}$ is present,\textsuperscript{14,15} which disappears abruptly as the density is raised and the rotation reverses direction to counter-current. An example of the fluctuation spectrum $S(k,f)$ for a 5.2 T, 1.0 MA discharge is shown in Fig. 13.

This dispersion plot is the difference between spectra obtained at electron densities of $0.98 \times 10^{20}/m^3$ (co-current rotation, LOC regime) and $1.07 \times 10^{20}/m^3$ (counter-current rotation, SOC regime). These density fluctuations from the core of the plasma, which are only present below the critical reversal density (LOC regime), have $k_\theta$ between 2 and 11 cm$^{-1}$ and $k_\theta \rho_s$ between 0.15 and 0.7, consistent in nature with trapped electron modes (TEMs).\textsuperscript{15} at least for the higher k values. (ITG modes can also be present in this range.) The
slopes of the features in Fig. 13 indicates a phase velocity of around 3 km/s.

V. DISCUSSION AND CONCLUSIONS

The connection among rotation reversals, the transition between the LOC and SOC regimes, and changes in turbulence are well established. These observations can be unified with the following ansatz:15,16,36–41 at low collisionality, the core toroidal rotation is directed co-current, the turbulence is dominated by TEMs, and Ohmic energy confinement and density profile peaking increase with increasing collisionality. At a critical value of the collisionality at \( \nu = 0.6 \) (\( \nu_c \approx 0.4 \)), the density profile peaking stops, TEMs abruptly disappear, ITG modes dominate, the rotation switches to the counter-current direction and Ohmic energy confinement saturates. Unfortunately for the present observations, there are no direct measurements verifying the dominance of ITG modes at high densities following the reversal.

In order to test this concept, simulations have been performed using the gyro-kinetic code GYRO.42 Shown in Fig. 14 are contour plots of the linear growth rates of the most unstable modes with \( 0.25 < k_i \rho_i < 0.75 \) in the \( a/L_t-a/L_T \) plane. These calculations were performed at \( r/a = 0.6 \), and the aspect ratio was 3.12. The solid lines going from the bottom left to top right in both frames separate the regions of TEM and ITG dominance.

Depicted by the + in the plot on the right is the operational point for a 0.62 MA discharge (\( q_{95} = 5.6 \)) with an electron density of \( 1.2 \times 10^{20}/m^3 \), which indicates that the most unstable mode is ITG. Other parameters for the simulation on the right were \( n_e = 1.2 \times 10^{20}/m^3 \), \( T_e = 1.06 \) keV, \( T_i/T_e \approx 1.2 \), and \( Z_{eff} = 1.5 \), a safety factor of 2.0, and a local shear of 1.43. \( a/L_T = 3.18 \) was held fixed during the scan. Lowering the density (collisionality), a factor of 4 moves the operational point to the TEM branch, as shown on the left. This is in qualitative agreement with the observations and the scenario described above.

Some open questions which remain regard why the LOC/SOC transition appears to occur near \( \nu_c = 0.4 \) and for \( T_i/T_e \approx 1.4 \).

In summary, the close connection between rotation reversal and Ohmic energy confinement saturation has been demonstrated. Concomitant changes in the nature of density fluctuations and electron density profile peaking are also observed. These phenomena occur at a very specific value of the electron density, which increases with plasma current. A comparison of Ohmic confinement saturation on a large number of devices indicates that this critical density scales with the inverse of the device major radius. The last two points suggest that these processes occur in a limited collisionality window.

ACKNOWLEDGEMENTS

The authors thank C. L. Angioni, D. Pace, J. L. Terry, and A. E. White for enlightening discussions, R. S. Granetz for magnetics measurements, and the Alcator C-Mod operations group for expert running of the tokamak. Work supported at MIT by DoE Contract No. DE-FC02-99ER54512.

FIG. 13. The density fluctuation spectrum \( S(k,f) \) of the difference between the LOC and SOC regimes, and changes in turbulence are well established. These observations can be unified with the inverse of the device major radius. The last two points suggest that these processes occur in a limited collisionality window.

FIG. 14. Contour plots of the linear growth rates (in units of \( c_i/a_i \)) of the most unstable modes (with \( 0.25 < k_i \rho_i < 0.75 \)) in the \( a/L_t-a/L_T \) plane, for \( r/a = 0.6 \). The + signs indicate the operational point of discharges with \( n_e = 0.3 \times 10^{20}/m^3 \) (left) and \( 1.2 \times 10^{20}/m^3 \) (right).