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Sumner, RW O'Brien, JF Hodgins, JK

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Animating Sand, Mud, and Snow

Robert W. Sumner

James F. O'Brien

Jessica K. Hodgins

College of Computing and Graphics, Visualization, and Usability Center Georgia Institute of Technology 801 Atlantic Drive Atlanta, GA 30332-0280 e-mail: [sumner|obrienj|jkh]@cc.gatech.edu

Abstract

Computer animations often lack the subtle environmental changes that should occur due to the actions of the characters. Squealing car tires usually leave no skid marks, airplanes rarely leave jet trails in the sky, and most runners leave no footprints. In this paper, we describe a simulation model of ground surfaces that can be deformed by the impact of rigid body models of animated characters. To demonstrate the algorithms, we show footprints made by a runner in sand, mud, and snow as well as bicycle tire tracks, a bicycle crash, and a falling runner. The shapes of the footprints in the three surfaces are quite different, but the effects were controlled through only five essentially independent parameters. To assess the realism of the resulting motion, we compare the simulated footprints to video footage of human footprints in sand.

Keywords: animation, physical simulation, ground interaction.

Introduction

To become a communication medium on a par with movies, computer animations must present a rich view into an artificial world. Texture maps applied to threedimensional models of scenery help to create some of the required visual complexity. But static scenery is only part of the answer; subtle motion of many elements of the scene is also required. Trees and bushes should move in response to the wind created by a passing car, a runner should crush the grass underfoot, and clouds should drift across the sky. While simple scenery and sparse motion can sometimes be used effectively to focus the attention of the viewer, missing or inconsistent action may also distract the viewer from the plot or intended message of the animation. One of the principles of animation is that the viewer should never be unintentionally surprised by the



Figure 1: Image of tracks left in the sand by a group of fast moving, motion blurred, alien bikers.

motion or lack of it in a scene[25].

Movie directors face a related problem because they must ensure that the viewer is presented with a consistent view of the world and the characters. An actor's clothing should not inexplicably change from scene to scene, lighting should be consistent across edits, and absent, unexpected, or anachronistic elements such as missing tire tracks, extra footprints, or jet trails must be avoided. The risk of distracting the viewer is so great that one member of the director's team, known as a "continuity girl," "floor secretary," or "second assistant director," is responsible solely for maintaining consistency[20].

Maintaining consistency is both easier and harder in computer animation. Because we are creating an artificial world, we can control the lighting conditions, layout, and other scene parameters and recreate them if we need to "shoot" a fill-in scene later. Because the world is artificial, however, we may be tempted to rearrange objects between scenes for best effect, thereby creating a series of scenes that could not exist in a consistent world. Computer-generated animations and special effects add another facet to the consistency problem because making models that move and deform appropriately is a lot of

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work. For example, most animated figures do not leave tracks in the environment as a human actor would and special effects artists have had to work hard to create subtle but essential effects such as environment maps of flickering flames. Because each detail of the scene represents additional work, computer graphics environments are often conspicuously clean and sparse. The approach presented here is a partial solution to this problem; we create a more interesting environment by allowing the character's actions to change a part of the environment.

In this paper, we describe a model of ground surfaces and explain how these surfaces can be deformed by characters in an animation. The ground material is modeled as a height field formed by vertical columns. After the impact of a rigid body model, the ground material is deformed by allowing compression of the material and movement of material between the columns. To demonstrate the algorithms, we show the creation of footprints in sand, mud, and snow. These surfaces are created by modifying only five essentially independent parameters of the simulation. We evaluate the results of the animation through comparison with video footage of human runners and through more dramatic patterns created by bicycle tire tracks (figure 1), a falling bicycle (figure 4), and a tripping runner (figure 6).

Background

Several researchers have investigated the use of procedural techniques for generating and animating background elements in computer-generated scenes. Although we are primarily interested in techniques that allow the state of the environment to be altered in response to the motions of an actor, methods for animating or modeling a part of the environment independent of the movements of the actors are also relevant because they can be modified to simulate interactions.

The first example of animated ground tracks for computer animation can be found in work done by Lundin[12, 13]. He describes how prints can be created efficiently by rendering the underside of an object to create a bump map and then applying the bump map to the ground surface to create impressions where the objects have contacted the ground.

The most closely related previous work is that of Li and Moshell[11]. They developed a model of soil that allows interactions between the soil and the blades of digging machinery. Soil spread over a terrain is modeled using a height field. Soil that is pushed in front of a bulldozer's blade is modeled as discrete chunks. Although they discount several factors that contribute to soil behavior in favor of a more tractable model, their technique is physically based and they arrive at their simulation formulation after a detailed analysis of soil dynamics. As the authors note, actual soil dynamics are complex and their model, therefore, focuses on a specific set of actions that can be performed on the soil, namely the effect of horizontal forces acting on the soil causing displacements and soil slippage. The method we present here has obvious similarities to that of Li and Moshell, but we focus on modeling a different set of phenomena at different scales. We also adopt a more appearance-based approach in the interest of developing a technique that can easily model a wide variety of ground materials for animation purposes.

Another method for modeling the appearance of ground surfaces is described by Chanclou, Luciani, and Habibi[1]. They use a simulation-based ground surface model that behaves essentially like an elastic sheet. The sheet deforms plasticly when acted on by other objects. While their model allows objects to make smooth impressions in the ground surface, they do not describe how their technique could be used to realistically model real world ground materials.

Other environmental effects that have been animated include water, clouds, and gases[5, 23, 7], fire[2, 23], lightning[18], and leaves blowing in the wind[26]. Among these, water has received the most attention. Early work by Peachey[17] and by Fournier and Reeves[8] used procedural models based on specially designed wave functions to model ocean waves as they travel and break on a beach. Later work by Kass and Miller[10] developed a more general approach using shallow water equations to model the behavior of water under more general of conditions. Their model also modified the appearance of a sand texture as it became wet. O'Brien and Hodgins[16] extended the work of Kass and Miller to allow the behavior of the water simulation to be affected by the motion of other objects in the environment and to allow the water to affect the motion of the other objects. They included examples of objects floating on the surface and simulated humans diving into pools of water. More recently Foster and Metaxas[6] used a variation of the three-dimensional Navier-Stokes equations to model fluids. In addition to these surface and volumetric approaches, particle-based methods have been used to model water spray and other loosely packed materials. Supplementing particle models with inter-particle dynamics allows a wider range of phenomena to be modeled. Examples of these systems include Reeves[19], Sims[21], Miller and Pearce[15], and Terzopoulos, Platt, and Fleischer[24].

Simulation of interactions with the environment can also be used to generate still models. Several researchers have described techniques for generating complex plant models from grammars describing how the plant should



Figure 2: The uniform grid forms a height field that defines the ground surface. Each grid point within the height field represents a vertical column of ground material with the top of the column centered at the grid point.

develop or grow over time. Měch and Prusinkiewicz[14] developed techniques for allowing developing plants to affect and be affected by their environment. Dorsey and her colleagues[3, 4] used simulation to model how an object's surface changes over time as environmental factors act on it.

Simulation of Sand, Mud, Snow

In this paper, we present a general model of a deformable ground material. The model consists of a height field supported by vertical columns of material. Using displacement and compression algorithms, we animate the deformations that are created when rigid geometric objects impact the ground material and create footprints, tire tracks, or other patterns on the ground. The properties of the model can be varied to produce the behavior of different ground materials such as sand, mud, and snow.

Model of Ground Material

Our simulation model discritizes a continuous volume of ground material by dividing the surface of the volume into a uniform rectilinear grid that defines a height field (figure 2). The resolution of the grid must be chosen appropriately for the size of the desired features in the ground surface. For example, in figure 1 the resolution of the grid is 1 cm and the bicycles are approximately 2 meters long with 8 cm wide tires.

Initial conditions for the height of each grid point can be created procedurally or imported from a variety of sources. We implemented initial conditions with noise generated on an integer lattice and interpolated with cubic Catmull-Rom splines (a variation of a two-dimensional Perlin noise function[5]). Terrain data or the output from a modeling program could also be used for the initial height field. Alternatively, the initial conditions could be the output of a previous simulation run. For example, the pock-marked surface of a public beach at the end of a busy summer day could be modeled by simulating many criss-crossing footfalls.

Motion of the Ground Material

The height field represented by the top of the columns is deformed as rigid geometric objects push into the grid. For the examples given in this paper, the geometric objects are a runner's shoe, a bicycle tire and frame, and a jointed human figure. The motion of the rigid bodies was computed using a dynamic simulation of a human running, bicycling, or falling down on a smooth, hard ground plane[9]. The resulting motion was given as input to the simulation of the ground material in the form of trajectories of positions and orientations of the geometric objects. Because of this generic specification of the motion, the input motion need not be dynamically simulated but could be keyframe or motion capture data.

The simulation approximates the motion of the columns of ground material by compressing or displacing the material under the rigid geometric objects. At each time step, a test is performed to determine whether any of the rigid objects have intersected the height field. The height of the affected columns is reduced until they no longer penetrate the surface of the rigid object. The material that was displaced is either compressed or forced outward to surrounding columns. A series of erosion steps are then performed to reduce the magnitude of the slopes between neighboring columns. Finally, particles can be generated from the contacting surface of the rigid object to mimic the spray of material that is often seen following an impact. We now discuss each step of the algorithm in more detail: collision, displacement, erosion, and particle generation.

Collision. The collision algorithm determines whether a rigid object has collided with the ground surface. For each column, a ray is cast from the bottom of the column through the vertex at the top. If the ray intersects a rigid object before it hits the vertex, then the rigid object has penetrated the surface and the top of the column is moved down to the intersection point. A flag is set to indicate that the column was moved, and the change in height is stored. The computational costs of the ray intersection tests are reduced by partitioning the polygons of the rigid body models using an axis-aligned bounding box hierarchy[22].

Using a vertex coloring algorithm, the simulation also computes a contour map with the distance from each column that has collided with the object to the closest column that has not collided (figure 3). This information is used when the material displaced by the collision is distributed. As an initialization step, columns not in contact with the object are assigned the value zero. During sub-



Figure 3: The contour map represents the distance from each column in contact with the foot to a column that is not in contact. For this illustration, we used columns that are four-way connected. However, in the examples in this paper we used eight-way connectivity because we found that the higher connectivity yielded smoother results.

sequent iterations, unlabeled columns adjacent to labeled columns are assigned a value equal to the value of the lowest adjacent column plus one.

Displacement. Ground material from the columns that are in contact with the object is either compressed or distributed to surrounding columns that are not in contact with the object. The compression ratio α is chosen by the user and is one of the parameters available for controlling the visual appearance of the ground material. The material to be distributed, Δh , is computed by $\Delta h = \alpha m$, where m is the total amount of displaced material. The material that is not compressed is equally distributed among the neighbors with lower contour values, so that the ground material is redistributed to the closest ring of columns not in contact with the rigid object. The heights of the columns in this ring are increased to reflect the newly deposited material.

Erosion. Because the displacement algorithm deposits material only in the first ring of columns not in contact with the object, the heights of these columns may be increased in an unrealistic fashion. An "erosion" algorithm is used to identify columns that form steep slopes with their neighbors and move material down the slope to form a more realistic mound. Several parameters allow the user to control the shape of the mound and model different ground materials.

The erosion algorithm examines the slope between each pair of adjacent columns in the grid (assuming eightway connectivity). For a column *ij* and a neighboring column kl, the slope, s, is

$$x = \tan^{-1}(h_{ij} - h_{kl})/d$$
 (1)

where h_{ij} is the height of column ij and d is the distance between the two columns. If the slope is greater than a threshold θ_{out} , then ground material is moved from the higher column down the slope to the lower column. Ground material is moved by computing the average difference in height, Δh_a , for the *n* neighboring columns with too great a downhill slope:

$$\Delta h_a = \frac{\sum (h_{ij} - h_{kl})}{n}.$$
 (2)

The average difference in height is multiplied by a fractional constant, σ , and the resulting quantity is equally distributed among the downhill neighbors. The algorithm repeats until all slopes are below a threshold, θ_{stop} . In the special case that a neighboring column is in contact with the geometric object, a different threshold, θ_{in} , is used to provide independent control of the inner slope around the geometric object.

Particle Generation. We use a particle system to model portions of the ground material that are thrown into the air by the motion of the geometric objects. The user controls the adhesiveness between the object and the material as well as the rate at which the particles fall from the object. Each triangle of the object that is in contact with the ground picks up a volume of the ground material during contact. The volume of material is determined by the area of the triangle multiplied by an adhesion constant for the material. When the triangle is no longer in contact with the ground, it drops the attached material as particles according to an exponential decay rate.

$$\Delta v = v(e^{(-t+t_c + \Delta t)/h} - e^{(-t+t_c)/h})$$
(3)

where v is the initial volume attached to the triangle, t is the current time, t_c is the time at which the triangle left the ground, Δt is the time step size, and h is a half life parameter that controls how quickly the material falls off. The number of particles released on a given time step is determined by $n = \Delta v \phi$, where $1/\phi$ is the volume of each particle.

The initial positions, \mathbf{p}_0 , for a particle is randomly distributed over the surface of the triangle according to:

$$\mathbf{p_0} = b_a \mathbf{x}_a + b_b \mathbf{x}_b + b_c \mathbf{x}_c \tag{4}$$

where \mathbf{x}_a , \mathbf{x}_b , and \mathbf{x}_c are the coordinates of the vertices of the triangle and b_a , b_b , and b_c are the barycentric coordinates of \mathbf{p}_0 given by

$$b_a = 1.0 - \sqrt{\rho_a} \tag{5}$$

$$b_b = \rho_b (1.0 - b_a) \tag{6}$$

$$b_c = 1.0 - (b_a + b_b) \tag{7}$$

where ρ_a and ρ_b are independent random variables evenly distributed between [0..1]. This computation results in a uniform distribution over the triangle.

The initial velocity of a particle is computed from the velocity of the rigid object:

$$\dot{\mathbf{p}}_0 = \nu + \omega \times \mathbf{p}_0 \tag{8}$$

where ν and ω are the linear and angular velocity of the object. To give a more realistic and appealing look to the particle motion, the initial velocities are randomly perturbed.

The final component of the particle creation algorithm accounts for the greater probability that material will fall off fast moving objects. A particle is only created if $(|\dot{\mathbf{p}}_0|/s)^{\gamma} > \rho$, where *s* is the minimal speed at which all potential particles will be dropped, γ controls the variation of the probability of particle creation with speed, and ρ is a random variable evenly distributed in the range [0..1].

If particles are only generated at the beginning of a time step then the resulting particle distribution will have a discrete, sheet-like appearance. We avoid this undesirable effect by randomly distributing each particle's creation time within the time step interval. The information used to calculate the initial position and velocity is interpolated within the interval to obtain information appropriate for the particle's creation time.

Once generated, the particles fall under the influence of gravity. When a particle hits the surface of a column, its volume is added to the column.

Implementation and Optimization

Simulations of terrain generally span a large area. For example, we would like to be able to simulate a runner jogging on a beach, a skier gliding down a snow-covered slope, and a stampede of animals crossing a sandy valley. A naive implementation of the entire terrain would be intractable because of the memory and computation requirements. The next two sections describe optimizations that allow us to achieve reasonable performance by storing and simulating only the active portions of the surface and by parallelizing the computation.

Algorithm Complexity. Because the ground model is a two-dimensional rectilinear grid, the most straightforward implementation is a two-dimensional array of nodes containing the height and other information about the column. If an animation required a grid of *i* rows and *j* columns, $i \times j$ nodes would be needed, and computation time and memory would grow linearly with the number of grid points. Thus, a patch of ground 10 m × 10 m with a grid resolution of 1 cm yields a 1000×1000 grid with one million nodes. If each node requires 10 bytes of memory, the entire grid requires 10 Mbytes of storage. Even this relatively small patch of ground requires significant system resources. However, most of the ground nodes are static throughout the simulation, allowing a much more efficient algorithm that creates and simulates only the active nodes.

The active area of the ground surface is determined by projecting an enlarged bounding box for the rigid objects onto the surface as shown in figure 4. The nodes within the projection are marked as active, and the collision detection, displacement, and erosion algorithms are applied, not to the entire grid, but only to these active grid points. Additionally, nodes are not allocated for the entire ground surface, rather they are created on demand as they become active. The i, j position of a particular node is used as the index into a hash table allowing the algorithms to be implemented as if a simple array of nodes were being used.

Because only the active grid points are processed, the computation time is now a function of the size of the rigid objects in the scene rather than the total grid size. Memory requirements are also significantly reduced, although the state of all modified nodes must be stored even after they are no longer active.

Parallel Implementation. Despite the optimization provided by simulating only active nodes, the computation time grows linearly with the projected area of the rigid objects. Adding a second character will approximately double the active area, but the computation time for multiple characters can be reduced by using parallel processing when the characters are contacting independent patches of ground.

In our parallel implementation, a parent process maintains the state of the grid and spawns a child process for every character in the animation. Each child process maintains a local copy of the grid and the multiple copies of the grid are synchronized through a two stage communication protocol at the end of each time step. First, each child reports the changes in its copy of the grid to the parent process. The parent process then updates the master copy of the grid and reports all changes to the children. This parallel implementation assumes that the projected bounding boxes of the rigid objects for different characters do not overlap. A more sophisticated implementation could handle this case by assigning characters with overlapping bounding boxes to the same processor.

We have implemented this design on a 16 processor SGI Power Challenge using UNIX sockets to handle communication. Because the parallel implementation does not rely on shared memory, we can also use multiple single processor machines, although the network delays between multiple machines are more significant than the



Figure 4: The left figure shows the ground area that has been created in the hash table. The currently active area is highlighted in red. The right figure shows the same scene rendered over the initial ground surface. There are approximately 37,000 columns in the active area and 90,000 stored in the hash table, while the number of columns in the entire virtual grid is greater than 2 million.



Figure 5: Images from video footage of a human runner stepping in sand and a simulated runner stepping in sand, mud, and snow. The human runner images are separated by 0.133 s; the simulated images are separated by 0.1 s.



Figure 6: Images of runner tripping over an obstacle and falling onto the sand. The final image shows the pattern she made in the sand.

communication time on a single multiprocessor machine.

Animation Parameters

One goal of this research is to create a tool that allows animators to easily generate a significant fraction of the variety seen in ground materials. Five parameters of the simulation can be changed by the user in order to achieve different effects: liquidity, roughness, inside slope, outside slope, and compression. The first four are used by the erosion algorithm, and the fifth is used by the displacement algorithm.

Liquidity, θ_{stop} , determines how watery the material appears by modifying how many times the erosion function is called per time step. With less erosion per time step, the surface appears to flow outward from the intersecting object; with more erosion, the surface moves to its final state more quickly.

Roughness, σ , controls the irregularity of the ground deformations by changing the amount of material that is moved from one column to another during erosion. Small values yield a smooth mound of material while larger values give a rough, irregular surface.

The inside and outside slope parameters, θ_{in} and θ_{out} , modify the shape of a mound of ground material by changing the slope adjacent to intersecting geometry and the slope on the outer part of the mound. Small values lead to more erosion and a more gradual slope; large values yield less erosion and a steeper slope.

The compression parameter, α , offers a way to model substances of different densities determining how much displaced material is distributed outward from an object that has intersected the grid. A value of one causes all material to be displaced; a value less than one allows some of the material to be compressed.

Additionally, when particles are used, the rate of creation of particles is controlled primarily by a parameter representing the adhesion between the ground material and the object. We included particles in the animations of sand but did not include them in the animations of mud or snow. Other more dynamic motions such as skiing might generate significant spray but running in snow appears to generate clumps of snow rather than particles.

Results and Discussion

Figure 5 shows images of a human runner stepping in sand and a simulated runner stepping in sand, mud, and snow. The parameters used for the simulations of the three ground materials are given in table 1. The footprints left by the real and simulated runners in sand are quite similar.

Figures 4 and 6 show more complicated patterns created in the sand by a falling bicycle and a tripping runner.

Variable	Sand	Mud	Snow
liquidity (θ_{stop})	0.8	1.1	1.57
roughness (σ)	0.2	0.2	0.2
inside slope (θ_{in})	0.8	1.57	1.57
outside slope (θ_{out})	0.436	1.1	1.57
compression (α)	0.3	0.41	0.0

Table 1: Table of parameters for the three ground materials.



Figure 7: Images of actual tire tracks in snow and human footprints in snow and in mud.

For each of these simulations, we used a grid resolution of 1 cm by 1 cm yielding a virtual grid size of 2048×1024 for the bicycle and 4096×512 for the runner.

The simulation described in this paper allows us to capture with relative ease many of the behaviors of substances such as sand, mud, and snow. Only about fifteen iterations were required to hand tune the parameters for the desired effect with each material. The computation time is not burdensome: a 3-second simulation of the running figure interacting with a 1 cm by 1 cm resolution ground material required less than 2 minutes of computation time on a single MIPS R10000 processor.

Many effects are missed by this model. For example, wet sand and crusty mud often crack and form large clumps, but our model can only generate smooth surfaces and particles. Actual ground material is not uniform but contains both small grains of sand or dirt as well as larger objects such as rocks, leaves, and sea shells. More generally, many factors go into creating the appearance of a given patch of ground: water and wind erosion, plant growth, and the footprints of many people and animals. Some of these more subtle effects are illustrated by the human footprints in snow and mud shown in figure 7.

One significant approximation in this simulation system is that the motion of the rigid objects is not affected by the deformations of the surface. For the sequences presented here, each of the rigid body simulations interacted with a flat, smooth ground plane. A more accurate and realistic simulation system would allow the bike and runner to experience the undulations in the initial terrain as well as the changes in friction caused by the deforming surfaces. For example, a bike is slowed down significantly when rolling on sand and a runner's foot slips slightly with each step on soft ground.

The motions of sand, mud, and snow that we gener-

ated are distinctly different from each other because of changes to the simulation parameters. Although much of the difference is due to the deformations determined by our simulations, part of the visual difference results from different surface properties used for rendering. To generate the images in this paper, we had not only to select appropriate parameters for the simulation but also to select parameters for rendering. A more complete investigation of techniques for selecting rendering parameters and texture maps might prove useful.

We regard this simulation as appearance-based rather than engineering-based because most of the parameters bear only a scant resemblance to the physical parameters of the material being modeled. The liquidity parameter, for example, varies between 0.0 and $\pi/2$ rather than representing the quantity of water in a given amount of sand. It is our hope that this representation for the parameters allows for intuitive adjustment of the resulting animation without requiring a deep understanding of the simulation algorithms or soil mechanics. The evaluation is also qualitative or appearance-based in that we compare simulated and video images of the footprints rather than matching initial and final conditions quantitatively.

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