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# **Impacts of Adding Photovoltaic Solar System On-Board to Internal Combustion Engine Vehicles Towards Meeting 2025 Fuel Economy CAFE Standards**

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## **ABSTRACT**

The challenge of meeting the Corporate Average Fuel Economy (CAFE) standards of 2025 has led to major developments in the transportation sector, among which is the attempt to utilize clean energy sources. To date, use of solar energy as an auxiliary source of on-board fuel has not been extensively investigated. This paper is the first study at undertaking a comprehensive analysis of using solar energy on-board by means of photovoltaic (PV) technologies to enhance automotive fuel economies, extend driving ranges, reduce greenhouse gas (GHG) emissions, and ensure better economic value of internal combustion engine (ICE) -based vehicles to meet CAFE standards though 2025. This paper details and compares various aspects of hybrid solar electric vehicles with conventional ICE vehicles. Different driving locations, vehicle sizes, various driving patterns and different cost scenarios are used in order to enhance the current understanding of the applicability and effectiveness of using on-board PV modules in individual automobiles and ensure an accurate representation of driving conditions in all U.S states at any time. These times and location-dependent results obtained over a year show an increase in the combined mile per gallon (MPG) at noon in the range of 2.9-9.5% for a vehicle similar to a Tesla S, and a significant increase in the range of 10.7-42.2% for lightweight and aerodynamic efficient vehicles. In addition, by adding on-board PVs to cover less than 50% of the projected horizontal surface area of a typical mid-size vehicle (e.g., Toyota Camry or Nissan Leaf), up to 50% of total daily miles traveled by an average U.S. person could be driven by solar energy. Also, the return on investment (ROI) of adding PVs on-board with ICE vehicle over its lifetime shows only negative values when the price of gasoline remains below \$4.0 per gallon and the vehicle is driven in low-solar energy area (e.g., Boston, MA). The same ROI is more than 250% if the vehicle is driven in high-solar energy area (e.g., Arizona), even if the gasoline price remains low. For future price scenarios, this ROI is much higher - nearly 10 times the investment cost under some scenarios, with the assumption of an eventual decline in battery costs. With regard to environmental impacts, significant gasoline gallons savings (~500-3400) and CO2 emission reduction (~5.0 to 34.0 short tons) are achieved.

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## **INTRODUCTION**

Environmental concerns, high energy demand in the transport sector, and strong government regulations for 2017-2025 passenger cars and light trucks to reduce greenhouse gas (GHG) emissions and improve Corporate Average Fuel Economy (CAFE) standards [[1](#page-10-0)] have led to increased focus on creating sustainable transportation technologies, not the least of which is the utilization of clean energy sources. U.S. Department of Energy, national labs, automotive OEMs, and academic researchers have been engaged in developing many solutions and models (e.g., ADVISOR model, PSAT, FASTSim, VISION, and GREET Model) to predict vehicle performance, emissions, and cost of alternative Powertrain technologies with different energy paths.

All above-mentioned efforts have overlooked the investigation of solar energy as an auxiliary on-board fuel. Widespread use of solar energy- a free, sustainable, renewable, and clean energy source - in fuel-efficient

automobiles can ensure energy independence for U.S. while minimizing environmental impacts. Solar PV remains a promising technology for managing the on-board power systems of hybrid electric vehicles (HEVs). Technological advances in solar PVs have brought about efficiency improvements and cost reduction, and are expected to accelerate their inclusion in the automotive design process [\[2](#page-10-1)]-[\[4](#page-10-2)].

Although configurations exist for including on-board PVs in vehicles [[5](#page-10-3)]-[\[9](#page-10-4)], current understanding on the efficacy of adding on-board PV technologies to internal combustion engines (ICE) for different vehicle sizes in different U.S locations under various driving scenarios remains incomplete. This paper is the first attempt at undertaking a comprehensive analysis of using solar energy on-board by means of PV technologies to enhance automotive fuel economies to meet CAFE standards though 2025 and extending driving ranges for ICE vehicles. In addition, in this paper we also estimate the economic

return on investment (ROI) and environmental impacts of adding on-board PVs to ICE vehicles under different scenarios. The proposed assessment methodology includes three different travel patterns in different U.S. states, covering different cost analysis scenarios for current and future prices.

## **MODELING ON-BOARD PV SYSTEM FOR ICE VEHICLES**

## *Geographical Location*

Total incident solar radiation (in  $kWh/m<sup>2</sup>$ ) for a specific period is known as global horizontal solar irradiation (G or GHI). GHI has two components: DNI and DHI. DNI, or direct normal irradiance, represents the solar energy that reaches the ground directly (in a straight line) from the sun, while DHI, or diffused horizontal irradiance, is derived from either scattering or diffusion of molecules and particles in the atmosphere. As the annual GHI in U.S. varies from state to state (see [Figure 1](#page-2-0)  $[10]$  $[10]$ ), two cities which represent the extremities in terms of available solar energy were selected; (i) Phoenix, AZ and (ii) Boston, MA.



<span id="page-2-0"></span>Figure 1. Annually global horizontal irradiation (*G*) in U.S. states [[10\]](#page-11-0)

## *PV Device*

PV module is a packaged assembly of individual PV cells. A solar PV cell is an electronic device (p-n junction) that converts electromagnetic radiation near the visible range into direct electric current (DC). Previously, we developed two novel knowledge-based systems to evaluate and select the optimum solar PV module type for on-board vehicle applications [\[7](#page-10-5)], [[8\]](#page-10-6). Mono-crystalline silicon (mono-Si) PV type was selected as the current best commercial option. The equivalent PV cell (module) circuit is modeled as shown in [Figure 2](#page-2-1) - consisting of a current source, a parallel diode, a series resistance  $(R<sub>s</sub>)$ , and a parallel (shunt) resistance  $(R_p)$ . Four-parameter approach is used for modeling, which means that  $R_p$  is assumed to be infinite and is hence ignored. Current  $(I)$  and voltage  $(V)$  are calculated using Equations  $(1)$ ,  $(2), (3), (4)$  $(2), (3), (4)$  $(2), (3), (4)$  $(2), (3), (4)$  $(2), (3), (4)$  [\[11\]](#page-11-1), [\[12\]](#page-11-2). The current generated by incident light  $(I_{pv})$ depends on sun irradiation.  $R<sub>s</sub>$  reflects the internal resistance, while  $R<sub>p</sub>$ is typically due to manufacturing defects  $[13]$  $[13]$  $[13]$ ,  $[14]$ .



<span id="page-2-1"></span>Figure 2. PV device equivalent circuit

<span id="page-2-2"></span>
$$
I = I_{PV} - I_d - \frac{V + R_S \cdot I}{R_p}
$$

*(1)*

*(3)*

*(4)*

<span id="page-2-3"></span>
$$
I_{PV}(T) = \frac{G}{G(nom)} \left[ I_{SC}(T_{1,nom}) + (\frac{I_{SC}(T_2) - I_{SC}(T_1)}{(T_2 - T_1)})(T - T_1) \right]
$$
(2)

<span id="page-2-4"></span>
$$
I_d = I_0 \left( e^{\frac{q(V + I.R_s)}{nkT}} - 1 \right)
$$

<span id="page-2-5"></span>
$$
I_0 = \frac{I_{SC}(T_1)}{\left(e^{\frac{q.V_{CC}(T_1)}{nkT_1}}\right)} \times \left(\frac{T}{T_1}\right)^{\frac{3}{n}} \times e^{\frac{q.V_q(T_1)}{nk\left(\frac{1}{T}-\frac{1}{T_1}\right)}}
$$

A transcendental  $Equation (5)$ , which does not have a direct solution, is generated by substituting Equations  $(2)$ ,  $(3)$ ,  $(4)$  in Equation  $(1)$ .

<span id="page-2-6"></span>
$$
I - f(G, T, V_g, n, R_s, R_{Sh}, I, V) = 0
$$
\n(5)

Parameters  $I_L$  and  $I_o$  are calculated.  $V_g$  is set to 1.12, a typical value for crystalline silicon PV module. Other parameters (*n* and *Rs* ) are estimated using curve-fitting approach, where the values of these parameters are tuned, with the objective function being to minimize the maximum PV module power to be within the accuracy range of the reported peak power of the PV module manufacturer data. Highly efficient mono-Si PV module, developed by the Sunpower Company [[15\]](#page-11-5), is used to validate the results of the proposed model by comparing the actual manufacturers' data and the predicted model results, as shown in [Figure 3](#page-3-0). Solid lines represent the actual *I*-*V* curves reported by manufacturers, while the "triangle and circle" are the results of this proposed model. All the curves at 25ºC unless otherwise is indicated.

In this work, an incremental conductance algorithm [[16\]](#page-11-6) is implemented in order to track the maximum power points, implying the optimal voltage and current that the PV system needs to work. Opting for a mounted structure of PV solar module on the vehicle surface affects both temperature (*T*) and the PV module performance. An empirically based thermal model [[17\]](#page-11-7) is used to estimate the thermal performance of PV. The optimum configuration of the PV module is observed to be the open rack: glass/cell/glass configuration.

*(6)*

*(7)*



<span id="page-3-0"></span>Figure 3. I-V Curves of PV module: Actual data (solid lines) vs. model results (circles/triangles)

#### *Shadow and Sky Clearness*

DNI that reaches the PV module is affected by shadows, while, DHI component is affected by the clearness of the sky. The solar data used here is the typical daily solar irradiance data that's collected by the National Renewable Energy Laboratory (NREL) / National Solar Radiation Data Base (NSRDB. It is called Typical Meteorological Year 3 and measured on an hourly base over 30 years based on empirical radiation data collected by meteorological station and include local weather variation which can dramatically change the radiation intensity [\[18](#page-11-8)].

[Equations \(6\)](#page-3-1) and [\(7\)](#page-3-2) are used to calculate GHI in both parking (*p*) and driving (*d*) modes.

> <span id="page-3-2"></span><span id="page-3-1"></span>GHI  $_{\text{parking Mode}} = \alpha_p \times \text{DNI} \times \cos(\theta) + \Psi_p \times \text{DHI}$ GHI Driving Mode =  $\alpha_d \times \text{DNI} \times \cos(\theta) + \Psi_d \times \text{DHI}$

Where  $\alpha$  and  $\psi$  are the shadow factor and sky clearness factor respectively. The  $\alpha$  factor is vary between 0 and 1 and changes with

time and depend on weather, surroundings, and locations. While, *ψ* is already included in the collected DHI values.

## *PV Position*

GHI reaches on-board PV module depending on the tilt and azimuth angles of PV installation. In general, for both fixed ground mounted and roof-top PV applications, the optimum tilt angle is around the latitude of the geographical location, with the PV face (azimuth angle) to the south or north direction. For on-board PV use in vehicle applications, the module can face any direction in both parking and driving modes. Our results show that in such case, the optimum tilt angle is horizontal when PV module is fixed; this also eliminates any problems that may arise due to aerodynamics. However, if the PV module(s) are placed on a curved vehicle surface, different PV cells (or modules) will have different angles of incidence (*θ*) with respect to the sun, and *I* will be different for each module. If these modules

are connected in series, some of them must work with *I* not equal to *Imp*. Consequently, net *I* for the PV module series will be the lowest *I* value, and a power mismatch problem will occur. DNI depends on (*θ*), and the power mismatch between the modules will be related to the difference between these different angles of incidence.

Two PV modules placed on a curved vehicle surface are shown in [Figure 4](#page-3-3). Angles of incidence of the PV modules 1 and 2 are  $\theta_1$  and  $\theta$ <sup>2</sup> respectively. Power mismatch between the two modules is calculated using [Equation \(8\).](#page-3-4) Assume that the curvature of the vehicle surface between the two regions where the two PV modules are installed, introduces a difference in incidence angles of less than 10°. If the sun is perpendicular to module 1 ( $\theta_l = 0$ °), power mismatch losses will be minor ( $\sim$  < 1.52%). However, if  $\theta_l = 50^\circ$ (i.e. It is significant), then the power mismatch loss is around 14.3% (i.e. Power mismatch loss is also significant). Ideally, both the PV modules should be as parallel as possible.

<span id="page-3-4"></span>Missmatchloss= $|\cos(\theta_1 \cdot \pi/180) - \cos(\theta_2 \cdot \pi/180)| \times 100\%$ 



<span id="page-3-3"></span>Figure 4. Angling PV on Vehicle Surface

#### *Energy Storage and Vehicle Energy at Wheels*

Energy demand at the wheels  $(E_w)$  for a given driving cycle and given vehicle, assuming the road grade to be zero, is calculated using [Equation \(9\)](#page-3-5).

<span id="page-3-5"></span>
$$
E_W = \frac{1}{2} \cdot \rho_a \cdot C_d \cdot A_f \cdot \int_{Cycle} v^3 dt + M_v \cdot g \cdot C_r \cdot \int_{Cycle} v dt + 1.1 \cdot M_v \cdot \int_{Cycle} V \frac{dV}{dt}
$$
\n(9)

Energy generated by the PV module is stored using Li-ion polymer battery, about which full specifications and analysis are detailed elsewhere [\[19](#page-11-9)]. The slightly higher expected voltage of the PV module permits the use of the more efficient step-down DC-DC configuration. [Equations \(10\),](#page-3-6) [\(11\),](#page-4-0) [\(12\)](#page-4-1) are used to calculate the solar energy-to-battery charging efficiency [[20](#page-11-10)]. Charging efficiency is optimized when PV voltage is slightly higher than battery voltage. Optimum ratio  $V_{mn}$  to the battery voltage is equal to 1.029 and provides the best charging efficiency.

<span id="page-3-6"></span>
$$
Eff(\%) = (\frac{\text{Avg.Voltage}(V) \times \text{Change Increase}(Ah)}{\text{Avg.Solar Irrad.}(W/m^2) \times \text{PV Area}(m^2)}
$$

$$
\times \frac{\text{Battery Charg.Eff.}(\%)}{\text{Time Interval}(hr)}
$$

*(10)*

*(8)*

<span id="page-4-1"></span>*(11)*

#### Charge Increase =  $Current \times Time$

<span id="page-4-0"></span>
$$
\eta = \frac{\int_{I<0} (E_0.I)dt}{\int_{I<0} (V.I)dt}
$$
\n(12)

Total energy stored (in kWh) for varying time and varying PV installation areas in the battery at Phoenix, AZ is shown in [Figure 5.](#page-4-2) Here, approximately 0.421 kWh of stored energy is available in the battery at noon with a PV installation area of  $2.5 \text{ m}^2$  and solar efficiency at STC that is equal to 20%. Total estimated energy stored in the battery using an assumed PV module (area  $=3.26$  m<sup>2</sup>) represents the daily energy generation equal to 4.81 kWh in June in Phoenix, AZ and 1.036 kWh in December in Boston, MA (see Appendix [Table 1](#page-5-0) for estimation of stored energy at different times).



<span id="page-4-2"></span>Figure 5. Energy stored in battery in June in Phoenix, AZ

## **RELATION OF CAFE STANDARDS WITH PV INSTALLATION SURFACE AREA**

CAFE target, based on the vehicle footprint and PV output, depends on the installation area - typically the vehicle surface. We present in detail how we correlate the projected vehicle surface area with the 2020 and 2025 CAFE standards to determine the PV installation area required for these CAFE targets. Eight 2014-model vehicles with varying sizes are used: i) a two-seater car (Smart Fortwo), ii) a mini-compact car (Fiat 500e), iii) two sub-compact cars (Chevrolet Spark EV and Mitsubishi i-MiEV), iv) a compact size vehicle (Ford Focus), v) a mid-size vehicle (Nissan Leaf), vi) a large-size vehicle (Tesla Motor S), and vii) a small station wagon (Honda Fit). CAFE standard curves up to 2025 for passenger cars are provided in [Figure](#page-4-3)   $6$  [[1](#page-10-0)]. While x-axis represents the vehicle footprint in square feet (ft<sup>2</sup>), vehicle footprint is defined as the area consisting of the vehicle's wheelbase multiplied by the average track width.



<span id="page-4-3"></span>Figure 6. CAFE (MPG) Standard Curves for Passenger Cars [\[1\]](#page-10-0), edited for clearness

CAFE target (MPG) curves for years 2020 and 2025 can be re-written as a criterion [\(13\)](#page-4-4).

<span id="page-4-4"></span>

$f/MPG$	$CAFE 2020$	$CAFE 2025$
$f/2 \leq 3.8m^2$	$49$	$61$
$3.8m^2 < f/2 < 5.1m^2$	$-0.93. f/2^2 + 87.07$	$-1.07. f/2^2 + 104.93$
$f/2 \leq 5.1m^2$	$36$	$46$

Where *ft* is in square feet...

Correlation between the reported values of vehicles' footprints and the projected horizontal surface areas of the eight selected vehicles is shown in Figure 7. Projected horizontal surface area for each vehicle is calculated based on the length and the width of the concerned vehicle. The predicted relationship [\(Equation 14\)](#page-4-5) shows a linear relationship with  $R^2$  equal to 0.9637, which is too high.

<span id="page-4-5"></span>Predicted Projected Horizontal Area = 
$$
2.28 \times ft - 1.56
$$

*(14)*

*Where*, *ft* and predicted projected horizontal area are in square meters  $(m<sup>2</sup>)$ .

The maximum error between the actual and predicted values of projected horizontal surface areas is found in the case of I-MiEV and Ford Focus vehicles - about  $0.75$  m<sup>2</sup> and  $0.32$  m<sup>2</sup> respectively - while for most other vehicles, the error is less than  $0.1 \text{ m}^2$ . The relation between the projected horizontal surface areas of vehicles and their CAFE targets in 2020 and 2025 is expressed using the criterion [\(15\)](#page-4-6).

<span id="page-4-6"></span>
$$
\begin{cases}\n 1.1 \text{ m}^2 & \text{CAFE in 2020} \\
7.1 \text{ m}^2 & \text{49} \\
7.1 \text{ m}^2 & \text{36} - 49 \\
7.1 \text{ m}^2 & \text{36} \\
7.1 \text{ m}^2 & \text{36} \\
46 & \text{46}\n\end{cases}
$$

*(15)*



Figure 7. Predicted projected horizontal surface based on vehicle footprint for selected 2014 EVs

Consequently, for the highest CAFE target related to a vehicle footprint of less than 41 ft<sup>2</sup> (3.8 m<sup>2</sup>) the horizontal projected surface  $(HS)$  area is less than 7.1 m<sup>2</sup>. However, the vehicle design must be optimized to install PV modules on the entirety of this area for a typical vehicle, which is challenging. Since we have assumed only 50% of the projected horizontal surface area as being covered with PV modules, this turns out to be approximately  $3.26 \text{ m}^2$ , roughly the area of two assumed PV modules [\[15](#page-11-5)].

## **DRIVING PATTERN SCENARIOS**

Most vehicles are rarely driven for long distances in the U.S., with the average daily vehicle trips approximately 36 miles with an average person trip length is 9.75 miles [[21\]](#page-11-11). The percent (%) of person-trips by time of day (how frequent the U.S driver starts the trip by specific time) is shown in Figure  $8$  [[21\]](#page-11-11). As can be seen, approximately 85% of all trips occur between 6 am and 7 pm, when solar energy is available. In this duration, three driving time scenarios are assumed: 9-10 am, 12 noon-1 pm, and 4-5 pm, since the highest percent of trips in a typical day occur during these times.



<span id="page-5-1"></span>Figure 8. The percent of trips by day in the U.S [Data from [\[21](#page-11-11)])

## **RESULTS AND DISCUSSION**

#### *Assumptions*

Five vehicles with different sizes are analyzed (See [Table 1](#page-5-0)). Key assumptions used in this analysis are tabulated in [Table 2](#page-6-0). Area of the PV base module is  $1.63 \text{ m}^2 (1.559 \text{ m} \text{ x } 1.046 \text{ m})$  [[15\]](#page-11-5), with the vehicle surface fitted with this PV module. Assumed installed PV area is 3.26 m<sup>2</sup>, with the assumption of a constant width and a variable length with series connection to perform the required PV area (constrained by a constant PV efficiency). To ensure an accurate representation of driving conditions in all U.S states at any time, two scenarios are used: minimum values for the vehicle driven in Boston, MA in December; and maximum values for the vehicle driven in Phoenix, AZ in June.

<span id="page-5-0"></span>

#### Table 1. Different size assumed vehicles

#### Table 2. Main assumptions



#### <span id="page-6-0"></span>*Contribution of On-Board PV toward CAFE 2025*

Fuel economy (FE) in terms of MPG in given driving cycles is calculated using [Equation \(16\)](#page-6-1).

<span id="page-6-1"></span>
$$
MPG = \eta_{T2W} \times \frac{E_{gasoline}}{E_{cycle}} \times I_{Cycle}
$$

*(16)*

Where  $E_{\text{gasoline}}$  is the energy for a gallon of gasoline, assumed to be 33.7 kWh/gallon,  $I_{\text{Cycle}}$  is the cycle length, which depends on the driving cycle,  $E_{\text{cycle}}$  is the vehicle energy consumption depends on the vehicle parameters as well as driving cycle, and  $\eta_{T2W}$  is tank-to-wheel efficiency, based on Powertrain configurations and driving cycle. The combined fuel economy (FE) is calculated based on the city and the highway driving cycles using [Equation \(17\).](#page-6-2) The weights of the city and highway driving cycles are considered as 55% and 45% respectively.

<span id="page-6-2"></span>FE (combined) = 
$$
\frac{1}{\frac{0.55}{\text{City FE}} + \frac{0.45}{\text{Hwy FE}}}
$$
(17)

 $\eta_{\text{T2W}}$  varies from low values as in the case of gasoline vehicles (typically 15-25%) to extremely high values as in the case of electric vehicles - for example, Tesla's electric Powertrain has an efficiency of 88%. [Equations \(18\)](#page-6-3) and [\(19\)](#page-6-4) are then used to calculate the contribution of on-board PV in increasing FE.

<span id="page-6-3"></span>
$$
MPGCity = \etaT2Wcity \times \frac{Egasoline}{(Ecitycycle - EPV at wheel-citycycle)} \times Icitycycle
$$
\n(18)

<span id="page-6-4"></span>
$$
MPG_{Hwy} = \eta_{T2W_{Hwy}} \times \frac{E_{gasoline}}{(E_{Hwycycle} - E_{PV at wheel-Hwycycle})} \times I_{Hwycycle}
$$
\n(19)

Where,  $E_{\text{PV at wheel-city cycle}}$  is the PV energy provided at the wheel in the duration of the city driving cycle,  $E_{\text{PV at the wheel-Hwy cycle}}$  is the PV energy provided at the wheel in the duration of the highway driving cycle, while  $\eta_{\text{T2W} \text{ city}}$  and  $\eta_{\text{T2W} \text{ Hwy}}$  are the tank-to-wheel efficiencies of the ICE conventional vehicle (prior to adding PV) in both city and highway cycles respectively. PV energy that reaches the wheels  $(E_{\text{pv}})$ at the wheel) in a given driving cycle is calculated using  $Equation (20)$ .

<span id="page-6-5"></span>
$$
E_{\text{PV at wheel}} = T_{\text{cycle}} \times \eta_{\text{pv2W}} \times E_{\text{PV-hourly}}
$$
\n
$$
(20)
$$

Where,  $E_{\text{PV hourly}}$ , is a PV hourly energy generation at a specific time and location (see Appendix [Table 1\)](#page-5-0),  $T_{\text{cycle}}$  is the cycle duration in hours (e.g.,  $T_{cycle} = 0.38$  in city cycle and 0.2125 in highway cycle), and  $\eta_{\text{pv2W}}$  is tank-to-wheel efficiency from PV module to wheels, assumed here as 90% (close to Tesla efficiency). Sophisticated estimation for  $\eta_{\text{PV2W}}$  requires further optimization for both the specific vehicle component size and the specific driving pattern. The idea here is to minimize energy conversion losses through the use of any available solar energy directly to the wheels without storing energy in the battery unless the system is forced to do so (e.g. SOC). However, such optimization depends on many parameters, specifically the size of the components, battery SOC, driving cycle, and control strategy [[22\]](#page-11-12).

Percentage (%) increase in combined MPG after adding the proposed PV on-board for different conventional gasoline vehicles at different times is illustrated in [Figure 9](#page-7-0). Five vehicle specifications covering a wide range of vehicles were analyzed (see [Table 1\)](#page-5-0). We calculated the combined fuel economy (mpg) prior to the addition of PV modules for all the above-mentioned vehicles, as shown in [Figure 9](#page-7-0) (x-axis) by assuming that all vehicles have a conventional internal combustion engine with  $\eta_{\text{T2W} \text{ city}} = 15\%$  and  $\eta_{\text{T2W} \text{ Hwy}} = 20\%$ . On the y-axis is plotted the minimum and maximum percentage increase in mpg for the three driving times: 9-10 am, 12 noon-1 pm, and 4-5 pm. The minimum and maximum values refer to the vehicles driven in Boston, MA in December, and in Phoenix, AZ in June respectively.

An increase in the combined MPG was found ranging between the minor value of 0.46% and the significantly higher value of 42.16%, with vehicle specifications, time, location, and month being the major determinants of the final mpg. For example, an increment in the combined mpg at noon for vehicle 4 (similar to Toyota Camry) ranged from 3.88% to 12.88%. Since the original combined mpg for vehicle 4 is 32 mpg, the minimum increase in its mpg after addition of PV is 1.24 mpg (3.88% x 32 mpg) if the vehicle is driven in December in Boston, MA while the maximum increment is 4.12 mpg (12.88% x 32 mpg) if the vehicle is driven in Phoenix, AZ in June.



Figure 9. On-board PV contribution in the combined fuel economy (MPG) in different scenarios

As shown in [Figure 9,](#page-7-0) the maximum PV contribution in vehicle 5 (similar to Tesla) is 9.54% of 24 mpg, equal to 2.29 mpg - because of the relative heaviest curb weight and cycle time, this is a relatively short value when compared to the total number of hours in a day when the sun is available. For vehicle 2, FE increased during the 4-5 pm driving time by 1.64% of 81 mpg, equal to 1.33 mpg in December in Boston, MA. A similar increase was seen in the 12 noon-1 pm driving time in Phoenix, AZ with an increase in FE to 34.15 mpg (42.16% of 81 mpg). For a typical mid-size car (Nissan Leaf or Toyota Camry), FE increased up to 4.2 MPG on using on-board PV system at noon.

## <span id="page-7-0"></span>**PV SOLAR DAILY RANGE EXTENDER**

The daily pure PV solar range extender is estimated for all assumed vehicles by adding the on-board PV system (see [Figure 10](#page-8-0)). Efficiency (Wh/mile) for vehicles 1, 3, and 5 are calculated based on the reported EPA rated combined FE [[23](#page-11-13)]. For non-electric vehicles 2 and 4, we estimated the driving ranges based on the optimized powertrain configuration  $\eta_{T2W}$  = 90% (as shown in y-axis, [Figure 10](#page-8-0)). Extended daily driving ranges fell in the range of 3.0 to 62.5 miles as shown in [Figure 10](#page-8-0). For highly efficient vehicles (e.g., vehicle 2), the driving range is from 13.5 to 62.5 miles for any daily drive in any part of US. Results also indicate that of the total daily miles driven by a motorist in the US in a mid-size vehicle (vehicle 3 and 4), 50% could be powered via PVs. For a lightweight and aerodynamically efficient vehicle (vehicle 2), it is triple of the previous figure, up to 174%.





**<sup>■</sup>Maximum: Phoenix, AZ (June)** • Minimum: Boston, MA (Dec.)

Figure 10. Solar PV daily range extender

# **RETURN ON INVESTMENT (ROI) OF HYBRID ICE VEHICLE WITH ON-BOARD PV SYSTEM**

This section details the estimated rates of return on money (cost of adding on-board PV system) per period for an ICE vehicle, otherwise known as ROI, as expressed in [Equation \(21\).](#page-8-1)

<span id="page-8-1"></span>
$$
ROI(\%) = \frac{Gain of Investment - Cost of Investment}{Cost of Investment} \times 100\%
$$
 (21)

Total cost of investment is calculated using [Equation \(22\)](#page-8-2), which includes lifetime cost of the entire powertrain components. We used two cost scenarios (*j*) for market price - current and projected future. Assumptions and detailed calculations are found in Appendix ([Table 2\)](#page-6-0).

<span id="page-8-2"></span>Cost of Investment 
$$
(\$)
$$
 =  $\sum_{j} [PV module + Battery + Motor]$  (22)

Cost of the PV module is estimated based on both current and future prices [[24\]](#page-11-14). Costs of battery and motor with controller were calculated using [Equations \(23\)](#page-8-3) and [\(24\)](#page-8-4), both of which are already in use in NREL Future Automotive Systems Technology Simulator [[25\]](#page-11-15).

<span id="page-8-3"></span>Motor and Controller $(\$) = $21.7/kW + $425$ 

<span id="page-8-4"></span>
$$
Battery(\$) = \$22/kW + \$500/kWh + \$680
$$

*(24)*

*(23)*

Developments in battery technology have yielded a concurrent decline in price over the last few years. Priced at around \$500/kWh in 2012, battery prices have fallen to \$325/kWh in 2014, and are expected to decline further to \$125/kWh by 2022 [\[26](#page-11-16)]. [Equation \(24\)](#page-8-4) is modified to reflect these changes in costs, and the battery was also sized appropriately to accommodate energy demand in the maximum scenario. [Equation \(25\)](#page-8-5) is used to calculate the gain on investment, specifically through analysis using three prices of a gallon of gas: \$2.0, \$4.0 and \$8.0.

<span id="page-8-5"></span>Gain on Investment<sub>j</sub> = 
$$
\frac{1}{\text{Vehicle MPG}} \times \text{PV Daily Solar Range}
$$
  
× Cost of Gasoline Gallon × 365 × Vehicle lifetime in Year ] (25)

The PV daily solar ranges are based on the minimum (i.e., driving in December in Boston, MA) and maximum scenarios (driving in June in Phoenix, AZ). Life of the vehicle was set at 12 years based on an average daily use of 36 miles, culminating in a total of 160,000 miles over the car's lifetime  $[21]$  $[21]$ ,  $[27]$  $[27]$ . Results for the three scenarios are shown in [Figures 11,](#page-8-6) [12](#page-8-7) and [13](#page-9-0). When the price of a gallon of gas was \$2.0 for current PV and battery prices (see [Figure 11\)](#page-8-6) and the car was driven in the low solar climate of Boston, MA, ROI had a negative value in the range -73.0 to -60.0%. When the price of a

<span id="page-8-0"></span>gallon of gas was \$4.0 for current PV and battery prices (see [Figure](#page-8-7)  [12](#page-8-7)) and the car was driven in the low solar climate of Boston, MA, ROI had a negative value in the range -21.0 to -46.0%.

However, when the car was driven in the high solar climate of Phoenix, AZ with the same price for a gallon of gas, ROI was positive for the previous two scenarios and varied in the range 147%-263% (in case of scenario II), depending upon the vehicle specifications. For example, using the proposed on-board PV system with vehicle 4 (e.g. Toyota Camry) in Arizona, gain on investment was 2.5 times the investment cost. At gasoline price of \$8.0/gallon and projected PV and battery prices (see [Figure 13](#page-9-0)), in the low solar energy location of Boston, positive ROI was obtained, ranging between 62% and 135%. Naturally, this same ROI was more than 900% for the same vehicle operating in the sunny climate of Arizona. Although the lifetime of an average vehicle is approximately 12 years, lifetime of the PV module within those cars is more than 30 years. Our calculations are restricted to the vehicle lifetime, with the assumption being that these PV modules can be transferred to other applications after the vehicle is recycled. We intend to analyze this enhanced economic consideration in our future research.



 $-\bullet$ -Min (ROI%)  $-\bullet$ -Max (ROI %)

<span id="page-8-6"></span>Figure 11. Minimum and maximum ROI of adding on-board PV for different ICE vehicles (Scenario I)



ROI-Scenario II: Gasoline Price \$4.0/gallon and

<span id="page-8-7"></span>Figure 12. Minimum and maximum ROI of adding on-board PV for different ICE vehicles (Scenario II)



The economic considerations of the annual degradation of PV performance were not examined in this research. However, this is minor, the PV module efficiency is degraded linearly by 0.5% per year for the lifespan of 30 years. This mean based on the vehicle lifetime, the difference between the average efficiency of PV module consider this degradation compared to what used in this study is only 0.72%.





<span id="page-9-0"></span>Figure 13. Minimum and maximum ROI of adding on-board PV for different ICE vehicles (Scenario III)

# **ENVIRONMENTAL IMPACT OF THE HYBRID ICE VEHICLE WITH ON-BOARD PV SYSTEM**

Reduction in gasoline burning (see [Figure 14](#page-9-1)) and carbon dioxide  $(CO<sub>2</sub>)$  emissions (see [Figure 15](#page-9-2)) by using hybrid solar vehicle in place of a conventional ICE vehicle over a 12-year life cycle was compared. Based on our calculations, a reduction of ~500 to 3400 gallons in gasoline use was obtained compared to a conventional ICE vehicle. Burning a single gallon of gasoline produces on an average around 19.64 pounds of  $CO<sub>2</sub>$ , so over a 12-year life cycle for both cars, approximately  $\sim$  5.0 to 34 U.S (short) tons of CO<sub>2</sub> reduction could be achieved by adding PVs with the ICE vehicles.





<span id="page-9-1"></span>Figure 14. Minimum and maximum gallons of gasoline reduce per vehicle lifetime by adding on-board PV



<span id="page-9-2"></span>Figure 15. Minimum and maximum U.S. tons of CO<sub>2</sub> reduce per vehicle lifetime by adding on-board PV

# **EFFECTS OF MOUNTING ON-BOARD PV ON VEHICLE AERODYNAMICS**

The preferred mounting option for PVs is the roof rack option compared to the insulated back option. However, the insulated back option may be preferred for aesthetic issues and will not affect the vehicle aerodynamics. The mono-Si PV module thickness is around 4.6 mm, which is very minor compared to the vehicle frontal area (□ 2.0 m2 ). The roof rack option resulted with a minor effect on the fuel economy by (1-3%) depending on vehicle parameters, e.g., added roof rack ~2% fuel economy for vehicle test with weight 1408 kg and the frontal area was  $2.15 \text{ m}^2$  [ $28$ ], [ $29$ ], which means around 4 Wh energy consumption is increased per a mile, if the on-board PV module with roof rack option is installed in a vehicle with the original driving efficiency of 200 Wh/mile. However, future works are needed to test the aerodynamic impacts for specific targeted vehicles.

## **CHALLENGES OF VEHICLE DESIGN WITH ON-BOARD PV**

Some of the previous discussions entailed optimizing solar power from the sun to the wheels via surface area, mounting, and orientation. Here, we detail concerns with the weight of the vehicle on incorporating onboard PVs in a conventional vehicle, specifically engine and battery mass scaling, both of which are based [on](#page-9-3)  [Equations \(26\)](#page-9-3) and [\(27\)](#page-9-4) respectively [[30](#page-11-20)].

<span id="page-9-3"></span>
$$
Engineering mass = 0.47 \times Engine Power + 61
$$

$$
(26)
$$

<span id="page-9-4"></span>Li-ion Battery mass =  $8.5 \times$  Batt. Energy + 58

$$
(27)
$$

Where engine mass and battery mass are represented in kilograms (kg), engine power is represented in kilowatts (kW), and battery energy is represented in kilowatt hours (kWh).

The electric motor is similar to that used in Stella solar vehicle [[5](#page-10-3)]. Weight analysis from the addition of a PV module to a gasoline vehicle is shown in Appendix [Table 3](#page-12-0). Current scenario shows extra weight in the range of the 130.0 to 147 kg. The extra weight of Powertrain components should be balanced by light-weighting of some other components in the vehicle to keep the curb weight constant.

Comparing the weights of the real vehicles with solar race vehicles are still far away. For example, Eindhoven's solar powered car Stella weighs is only 380 kg  $[5]$  $[5]$ , with energy consumption is around 40.2 Wh per mile.

## **CONCLUSIONS**

Solar PV technology shows great promise for managing on-board power systems of HEVs and PHEVs. Widespread use of solar energy - a free, sustainable, renewable, and environmentally clean energy source - will help ensure energy independence for US while allowing the manufacture of fuel-efficient automobiles. This study presented a novel comprehensive assessment methodology regarding the use of PV solar technologies on-board with gasoline ICE vehicles to meet CAFE 2025 standards.

We uniquely related the 2020 and 2025 CAFE standard curves to the projected horizontal vehicle surface area for eight different vehicles of varying sizes in our study to estimate the maximum possible PV installation area for each CAFE target. We then determined the maximum contribution of on-board PV in enhancing fuel economy in the combined driving cycle for three travel patterns and five different vehicle sizes. The vehicle driven in December in Boston, MA was the minimal scenario while the maximum was the vehicle driven in June in Phoenix, AZ to determine the mean average for driving conditions in the other 48 U.S states at any time. A slight increase in the combined MPG (range 2.9-9.5%) at noon was observed for a vehicle similar to Tesla 2013 S while a significant increase in combined MPG (range 10.7-42.2%) was observed for lightweight and aerodynamic efficient vehicles. However, the short duration of the driving cycle - as little as 0.38 hours in the city cycle and 0.21 hours in the highway cycle - made comparing the hours in day of solar energy availability difficult.

Next, estimation of the pure PV solar range (PV range extender) for five different size vehicles was presented. It was determined that the addition of an on-board PV covered less than  $50\%$  (3.2 m<sup>2</sup>) of the projected horizontal surface area of a typical vehicle. It was effective in extending the pure solar PV ranges to 50% of the total daily drive time of a U.S. mid-size vehicle. In addition, the combination of a lightweight and aerodynamically efficient vehicle with proposed PVs increased the total person miles of travel per day in the U.S. (using solar energy) by 174%. The daily driving range was observed to extend between 3.0 and 62.5 miles, based on vehicle specifications, locations, and time. For example, the addition of the proposed PV module to very lightweight and aerodynamically efficient vehicles could extend the daily range to between 13.5 miles and 62.5 miles. In the specific case of vehicle similar to Nissan Leaf, the range was extended - a minimum of 3.5 miles and a maximum of 16.0 miles. For a heavier vehicle similar to Tesla Model S 2013, a totally solar powered PV extended the driving range to between 3.0 and 13.7 miles.

When the vehicle was driven in a low solar energy location (e.g., Boston, MA) with the average price of a gallon of gas less than \$4.0 and at today's PV and battery prices, ROI was negative. Under the same price in a high solar environment (e.g., Arizona), however, ROI was positive, varying between 147%-257%, depending upon on the vehicle specifications. If the price of a gallon of gas was \$8.0 with the assumption of an eventual decline in battery costs, even in low solar energy locations a positive ROI was possible in the range of 60-135%, while ROI goes up to 1000% for vehicles in high solar energy locations. These results are based on an average 12-year life cycle of the vehicle. However, the life of the PV module extends well beyond this time by as much as 18 years, meaning that it can be transferred into another application after the vehicle is recycled. Economic considerations of this transfer though were not examined in this research. For an ICE vehicle with an assumed life-expectancy of 12 years and with an on-board PV system, estimates of gas savings ranged from a minimum of 500 to more than 3,400 gallons, with a concurrent reduction in nearly 5 to 33 U.S (short) metric tons of  $CO<sub>2</sub>$ emissions also reduced during that time.

The results of this dynamic model, which can reflect the various PV module areas, efficiencies, installation locations, times, and weather, are applicable for determining the on-board PV contribution for any vehicle size. Specifically, the proposed work can be used to develop a tool for decision-makers to use during the conceptual design stage, since its results are capable of reflecting changes in fuel consumption, GHG emissions and cost for different locations and driving scenarios in order to facilitate the deployment of a sustainable transportation system towards meeting CAFE 2025 targets.

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## **DEFINITIONS/ABBREVIATIONS/ NOMENCLATURE**

- **Mono-Si** mono-crystalline silicon
- **PV cell** Photovoltaic solar cell
- **ICE Vehicle** Internal combustion engine powered vehicle
- **CAFE** Corporate Average Fuel Economy
- *Rs* Series resistance
- *I <sup>d</sup>* Shockley diode current
- $I_{pV}$  Incident light
- $I_{SC}$  Short circuit current
- *V*<sub>ac</sub> Open circuit voltage
- *Rp* - Parallel resistance
- *n* Diode ideally factor
- *q* Electron charge
- *k* Boltzmann constant
- *G* Global solar irradiation
- *G(nom)* Nominal solar irradiation (1000 W/m2 )
- *T1* - Reference temperature 25°C)
- *T2* - Arbitrary temperature
- $I_{\text{SC}}(T)$  Short circuit current at specific temperature
- *T* Cell temperature
- *I*<sub>0</sub> Reverse saturation current
- $C_d$  Aerodynamic drag
- *ρa* - Density of air
- **DHI** Diffuse horizontal irradiance
- **DNI** Direct normal irradiance
- *Af* - Frontal projected area
- *Cr* - Rolling resistance
- *v* Vehicle velocity
- **MPG** Mile per gallon
- **STC** Standard test conditions: solar irradiance of 1000 W/m2 , AM 1.5, and cell temperature 25 °C
- **ROI** Return on Investment
- $\eta_{\text{T2W}}$  Tank to wheel efficiency

# **APPENDIX**

#### Table 1. Total energy stored in battery by proposed PV module system



#### <span id="page-12-0"></span>Table 2. Total cost of investment for entire hybrid solar powertrain components



## Table 3. Weight analysis by PV added on-board to gasoline vehicle



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