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1 **Nonsymmorphic Symmetry-Protected Band Crossings in a**
2 **Square-Net Metal PtPb₄**

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29 **ABSTRACT**

30 Topological semimetals with symmetry-protected band crossings have emerged as a
31 rich landscape to explore intriguing electronic phenomena. Nonsymmorphic symmetries in
32 particular have been shown to play an important role in protecting the crossings along a
33 line (rather than a point) in momentum space. Here we report experimental and theoretical
34 evidence for Dirac nodal line crossings along the Brillouin zone boundaries in PtPb₄, arising
35 from the nonsymmorphic symmetry of its crystal structure. Interestingly, while the nodal
36 lines would remain gapless in the absence of spin-orbit coupling (SOC), the SOC in this case
37 plays a detrimental role to topology by lifting the band degeneracy everywhere except at a
38 set of isolated points. Nevertheless, the nodal line is observed to have a bandwidth much
39 smaller than that found in density functional theory (DFT). Our findings reveal PtPb₄ to
40 be a material system with narrow crossings approximately protected by non-symmorphic
41 crystalline symmetries.

42 **Keywords:** Topology, nonsymmorphic symmetry, electron correlations, angle-resolved
43 photoemission spectroscopy, dynamical mean field theory

44 INTRODUCTION

45 Since the discovery of topological insulators more than a decade ago, the classification of
46 quantum materials has undergone a revolution, where quantum materials are now categorized
47 by their topological properties and associated symmetries [1–8]. This is epitomized by
48 the study of topological semimetals (TSMs), which are 3-dimensional analogs to graphene
49 where the bulk bands cross without opening an energy gap [9]. Crystalline symmetries,
50 such as nonsymmorphic symmetry, can play a crucial role in protecting the band crossings
51 along a continuous line or loop in momentum space in TSMs, yielding what is known as
52 a nodal line semimetal (NLS). Nonsymmorphic symmetries combine a fractional lattice
53 translation with either a mirror reflection (glide plane) or a rotation (screw axis), resulting
54 in a band-folding with crossings at the Brillouin zone (BZ) boundaries that are protected
55 against hybridization [10, 11]. As long as the nonsymmorphic symmetry remains intact,
56 these so-called essential band crossings are impervious to the presence of SOC [10–12]. If
57 furthermore the degenerate bands only slightly disperse, one observes the symmetry-protected
58 crossings of narrow bands, which when doped to the chemical potential may host correlated
59 topological phases [13–15].

60 In contrast to the vast repository of materials with band crossings that are unprotected
61 against SOC, there are only a handful of materials that realize nonsymmorphic symmetry-
62 protected Dirac crossings. The search for nonsymmorphic topological materials has largely
63 been guided by a work from Young and Kane [16], which demonstrated that two-dimensional
64 square net motifs can generate Dirac nodes, when the square net is itself embedded in a unit
65 cell that is twice as large and hence the two atoms in the unit cell are related by a glide plane.
66 This blueprint has been followed in the case of ZrSiS, which has the nonsymmorphic space
67 group $P4/nmm$ with Si occupying a square net. ARPES measurements on ZrSiS [17, 18] and
68 several isostructural compounds [19, 20] have revealed nonsymmorphic symmetry-protected
69 Dirac nodal lines with linear dispersions over more than 2 eV. Several years onward, ZrSiS
70 and its structural analogs, whose electronic structure can be well captured by DFT, remain
71 one of the few experimental manifestations of this class of topological materials [21, 22].

72 Here we report the discovery of a nonsymmorphic symmetry protected topological
73 semimetal displaying narrow bands along the BZ boundary, PtPb₄. Distinct from a previous
74 report on PtPb₄ crystals that exhibit a crystal structure consistent with space group $Ccce$ [23],

75 our post-annealed crystals exhibit tetragonal symmetry of the space group $P4/nbm$. Our
 76 ARPES measurements reveal a set of nearly flat degenerate bands along the BZ boundary
 77 that appear to originate from the linear crossing of two bulk bands along the orthogonal
 78 momentum direction. Careful analysis of space group symmetries and their representations
 79 in the BZ shows that the band degeneracies along the BZ boundary originate from non-
 80 symmorphic symmetry elements. Surprisingly, despite the large SOC expected from the
 81 heavy elements constituting PtPb_4 , the observed splitting of the bands is much smaller than
 82 predicted by *ab initio* calculations based on DFT. By comparing our ARPES measured bands
 83 with those from both DFT and dynamic mean field theory (DMFT) calculations [24–27], we
 84 further explore the role of electron correlation effects on the band details. PtPb_4 therefore is
 85 one of the few reported nonsymmorphic symmetry-protected TSMs outside the well-known
 86 ZrSiS family that exhibits narrow bands in the presence of non-trivial topology.

87 RESULTS

88 Crystal structural characterization and nonsymmorphic symmetry in PtPb_4

89 PtPb_4 , grown by the metallic flux method, forms in the tetragonal space group 125
 90 ($P4/nbm$) with lattice parameters $a = 6.66 \text{ \AA}$ and $c = 5.978 \text{ \AA}$ [28]. No structural phase
 91 transitions are found down to 2 K. A recent study on PtPb_4 suggested that this material is
 92 polymorphic, with similar formation energies for tetragonal and orthorhombic structures [23].
 93 In our study, we determined that extensive post-growth annealing (described in Supplementary
 94 Note 1 and Note 2) was critical to obtaining a single phase tetragonal material. The tetragonal
 95 crystal structure of PtPb_4 consists of staggered layers of Pt and Pb, as seen in Fig. 1a. Two
 96 layers of Pb (gold) are sandwiched between consecutive layers of Pt (blue). Each Pb layer
 97 forms a Shastry–Sutherland lattice while a square net is formed by each Pt layer. This
 98 crystal structure exhibits nonsymmorphic symmetry through a glide-mirror operation, as
 99 illustrated in Fig. 1a. For the Pb in site A, a mirror reflection operation m_z brings it to site
 100 B, which is not an allowed position in the structure. An additional fractional translation is
 101 needed ($t : \frac{1}{2}, \frac{1}{2}, 0$) to bring it to the allowed atomic site C. We note that PtPb_4 is structurally
 102 similar but not isostructural with PtSn_4 , which has been reported to exhibit Dirac nodal arc
 103 surface states [29], features that are apparently unrelated to the nonsymmorphic symmetry.

105 We investigated the electronic structure of PtPb₄ via ARPES measurements. The Fermi
 106 surfaces (FS) measured under an in-plane polarization along the horizontal direction are
 107 shown in Fig. 1b, which consists of flower-like Fermi pockets centered at the BZ center.
 108 We note that the intensity of the FS appears to indicate C₄ symmetry-breaking, which
 109 has also been reported by a laser-ARPES work [23]. However, we caution that since our
 110 polarization used is along the k_x direction, the photoemission matrix elements also break
 111 C₄ symmetry, which prevent us from concluding whether the intrinsic electronic structure
 112 breaks C₄ symmetry. However, our powder x-ray diffraction measurements show no evidence
 113 of C₂ symmetry in our annealed crystals, suggesting that our bulk bands should exhibit C₄
 114 symmetry. Notably, at a binding energy of 0.6 eV below the Fermi level (E_F), an intense
 115 grid-like feature appears along the lines that coincide with the boundaries of the BZ, as
 116 evident in the measured constant energy contour (Fig. 1c), reminiscent of the nonsymmorphic
 117 symmetry-protected features originally predicted by Young and Kane [16]. To see the band
 118 dispersions that give rise to this feature, we show the spectral images measured along the high
 119 symmetry directions of the BZ (Fig. 1d). First, along the Γ -X direction, a series of electron
 120 bands appear. Closer to the X point, we also observe two highly dispersive bands that meet
 121 at the X point. In contrast to the Γ -X direction, intensity from dispersions along the X-M
 122 direction are mostly confined within the energy window of -0.9 eV to -0.3 eV, where a set
 123 of largely flat bands appear, in particular, near -0.6 eV. These are the bands that give rise to
 124 the grid-like features outlining the BZ boundaries in the constant energy contour in Fig. 1c.
 125 To identify whether the crossing is of bulk or surface nature, we carried out a photon energy
 126 dependence study for probing along the k_z direction. A number of features in the constant
 127 energy contour taken at -0.6 eV are shown to be periodic, and therefore identified as bulk
 128 bands (Fig. 1f). In particular, we find that the bands giving rise to the Dirac crossing at the
 129 BZ boundary exhibit different band velocities at k_z=0 and π . This is illustrated in a cut
 130 near the X-R direction (Fig. 1g), where the Dirac dispersion is observed to be periodic along
 131 k_z, indicating that it is bulk in nature. The grid-like feature this band forms in the constant
 132 energy contour indeed appears at all BZ boundaries, respecting the bulk C₄ symmetry.
 133 Moreover, we also note a clear k_z broadening effect for this band, seen in the broadened
 134 intensity where this band disperses across k_z. This is an effective integration along k_z due to

135 the low resolution of the photoemission process in the out-of-plane direction [30]. We carried
 136 out semi-infinite slab calculations using DFT based on the Green's function method [31].
 137 The resulting calculated FS, shown in the bottom right panel of Fig. 1b, reproduces the
 138 series of pockets centered at Γ seen in ARPES. At -0.6 eV, large pockets centered at Γ are
 139 also reproduced. Importantly, this calculation also reproduces the grid like outline of the BZ
 140 boundaries (bottom right panel in Fig. 1c). Due to the strong k_z broadening observed, we
 141 compared the measured dispersions with the calculated k_z integrated band dispersions along
 142 Γ -X. Largely dispersive features appear to qualitatively match those seen in the ARPES
 143 data. Along the high-symmetry X-M line, a number of bands appear in the energy range
 144 centered at -0.6 eV, which likely correspond to the bands giving rise to the grid-like feature
 145 in the constant energy contour. However, the calculated dispersions along the X-M line span
 146 a larger energy window than what is observed experimentally, indicating a subtle mechanism
 147 that is not captured by the DFT calculations.

148 In order to shed more light on the nature of the band crossings along the edges of the
 149 BZ, we analyze in detail the measured band dispersions along and perpendicular to the X-M
 150 BZ boundary (Fig. 2). To better visualize the band dispersions, we plot the 2D curvature
 151 of the spectral image along the Γ -X-M path in Fig. 2a. The pair of bands highlighted in
 152 red in Fig. 2a disperse along Γ -X to meet at a degenerate point at X, then remain nearly
 153 degenerate across the X-M edge of the zone. To see this, we examine a series of ten cuts (C1
 154 to C10) perpendicular to the X-M direction (Fig. 2b). From C1, the linear Dirac crossing can
 155 be clearly observed near -0.6 eV. As we move away from the X point, this Dirac crossing
 156 remains centered at nearly the same energy. In C6 and C7, a gap is resolved at the Dirac
 157 point, and subsequently closes approaching the M point (C8 to C10), although a small gap
 158 may persist along the cut beyond our experimental resolution. We note that the bandwidth
 159 of this nodal line is less than 0.2 eV along the BZ boundary direction. In addition, another
 160 set of nearly degenerate bands can be observed near -0.9 eV, as marked in yellow on cuts
 161 C5 to C8. The crossing points of these bands are also indicated for clarity by yellow dots
 162 along the X-M line in Fig. 2a. We therefore conclude that what appears to be a nearly flat
 163 grid-like feature at -0.6 eV in the ARPES data is actually a set of two bands that cross or
 164 nearly cross along the X-M line at the BZ edge. This can also be seen in constant energy
 165 contours. As shown in Fig. 2c, a line segment lining the BZ boundary at -0.6 eV evolves
 166 into two separate features both above and below in energy due to the Dirac bands dispersing

167 away from the nodal crossing.

168 Symmetry analysis and calculations

169 The intriguing features in both the measured and calculated band dispersions prompted
170 us to examine these findings in the context of the nonsymmorphic symmetry of PtPb₄. The
171 glide mirror symmetries of the space group can be represented by $\hat{g}_x = \{m_{010}|\frac{1}{2}, 0, 0\}$ and
172 $\hat{g}_z = \{m_{001}|\frac{1}{2}, \frac{1}{2}, 0\}$ (Note that these operations are defined with respect to the standard
173 primitive cell for space group 125, which has its origin shifted by $(0, \frac{1}{4}, 0)$ with respect
174 to Fig. 1(a)). As these operations are orthogonal to each other (anticommuting), in the
175 absence of SOC, the bands ψ_+ and $\psi_- = \hat{g}_x\psi_+$ carry opposite eigenvalues of \hat{g}_z and are
176 hence degenerate along the BZ boundary (Fig. 3a). With the inclusion of SOC, a gap opens
177 along the BZ boundary except at the highest symmetry points, owing to the breaking of
178 the anti-commutation relation between \hat{g}_x and \hat{g}_z (Fig. 3b). With SOC present, the double
179 space-group operation requires \hat{g}_x and \hat{g}_z to *commute* in spin space as well. Thus, instead of
180 the anti-commutator $\{\hat{g}_x, \hat{g}_z\} = 0$, one has the commuting relation $[\hat{g}_x, \hat{g}_z] = 0$ under SOC.
181 As a result, the action of the glide plane on a band $\psi_- = \hat{g}_x\psi_+$ is no longer degenerate with
182 ψ_+ as they now carry the same \hat{g}_z eigenvalue. Consequently, every band along X-M (and
183 the equivalent direction R-A) is only degenerate with its Kramers' pair, except at the high
184 symmetry points at $k_y = 0$ (X) or π (M-point), where the four-fold degeneracy remains
185 due to the presence of both time reversal \hat{T} and parity \hat{P} symmetries. We therefore find
186 that, in the absence of SOC, the nonsymmorphic symmetry in PtPb₄ must protect the band
187 degeneracy along the BZ boundary, similar to earlier theoretical reports on nonsymmorphic
188 structures [11, 32]. However, the presence of SOC lifts the degeneracy except at a set of
189 isolated points. The nonsymmorphic symmetry of the crystal could also explain the strong
190 intensity asymmetry of the Dirac dispersions about the BZ boundary (Fig. 1h-i), where the
191 glide mirror symmetry switches the parity of the orbital symmetries, as has been observed in
192 the iron pnictides [33].

193 To demonstrate this protected degeneracy revealed in the above symmetry analysis, we
194 first carried out DFT calculations without SOC (Fig. 4c). For illustration purposes, we show
195 the calculated dispersions along the Z-R-A direction. Bands along additional directions are
196 shown in the Supplementary Figure 4. Throughout the BZ, we observe pairs of bands that

197 disperse along Z-R and meet at the R point and then remain completely degenerate along the
 198 R-A line. One example of such pairs of bands is highlighted in green. This degeneracy exists
 199 for all bands along the BZ boundaries X-M and R-A, and is protected by the two orthogonal
 200 glide symmetries as previously discussed, resulting in a nodal line network in PtPb₄. While
 201 DFT confirms the symmetry analysis presented earlier and show qualitative agreement with
 202 our experimental measured dispersions, we note that DFT calculated band velocities appear
 203 to be larger than that from the data, suggesting the need to investigate electronic correlations
 204 as one of the possible factors affecting the details of the electronic structure that is missing
 205 in DFT calculations. To quantify such discrepancies, we extract a number of observable
 206 quantities from the data (shown for the projected cut $\bar{\Gamma} - \bar{X} - \bar{M}$), including the bandwidth
 207 of the lower part of the dispersion along $\bar{\Gamma} - \bar{X}$ (E_α), its Fermi velocity (v_F), and the portion
 208 of the hole-like dispersion along $\bar{X} - \bar{M}$ that is below E_F (E_β), and plot in Fig. 4e. It is clear
 209 that the DFT calculated bands exhibit larger bandwidth. To understand the potential role
 210 of correlation effects, we carried out DFT+U ($U = 3$ eV) calculations, which accounts for
 211 the static interactions of the Pt d -orbitals. While the bandwidth E_α is slightly renormalized,
 212 large deviations from measurements still remain.

213 Next, we consider the effect of SOC, which is expected to be substantial in PtPb₄. When
 214 SOC is included into the DFT+U calculation (Fig. 4c), the degeneracy between each pair of
 215 bands along the R-A (and X-M) line is lifted. Nevertheless, a fourfold degeneracy is indeed
 216 retained at the high-symmetry R and A points (as well as X and M), as predicted to be
 217 protected by the nonsymmorphic symmetry. Although the above symmetry analysis only
 218 guarantees the band crossings at isolated points (X, M, R, A) on the zone boundary, it does
 219 not preclude accidental crossings of the bands between these points on the R-A (X-M) line.
 220 Indeed as seen in calculations with SOC, accidental crossings between pairs of bands do
 221 happen and are marked by circles in Fig. 4c. We emphasize that these crossings are not
 222 symmetry-enforced – they are accidental – but once the bands cross, the screw rotation
 223 $\hat{s}_{2y} = \{2_{010}|\frac{1}{2}, 0, 0\}$ protects the crossing from being gapped (see the Supplementary Note 4
 224 for more details).

225 While the DFT+U calculations show qualitative agreement with our experimental obser-
 226 vations, we note that some inconsistencies remain. One example is the bandwidth of Dirac
 227 nodal lines along the BZ boundary, which remain well above that observed experimentally
 228 (0.2 eV). Another example is the band highlighted in green along X/R to M/A in the

229 measured dispersions shown in Fig. 4b, which also has a larger bandwidth and remains above
 230 E_F along R–A cut (Fig. 4c), in contrast to the data. We note that while the k_z broadening
 231 effect could possibly explain the dispersion of this band towards E_F (see Supplementary
 232 Note 3 and Note 6), one still needs a mechanism to reduce the bandwidth towards that
 233 experimentally observed. We then examine factors missing in DFT and DFT + U calcula-
 234 tions. One possibility is the dynamic correlation effects, which we probe with DMFT by
 235 calculating the energy-momentum-dependent spectral function (see Supplementary Note 7 for
 236 details). From the orbital-resolved density of states (Fig. 4d), the Pt d -orbitals and the Pb
 237 p -orbitals both contribute significantly near E_F . We therefore examine the effect of dynamic
 238 correlations in each. We study the effect of the on-site Coulomb interactions (U_d) of the Pt
 239 d -orbitals and find that an increase from 3 eV to 8 eV causes the reduction of the bandwidth
 240 of the green-highlighted band along Z-R-A, resulting in the portion along R-A crossing
 241 E_F (Supplementary Figure 8). This demonstrates an overall systematic improvement with
 242 the experimental observations from DFT and DFT+U, as captured by all of the extracted
 243 quantities in Fig. 4e. Similar theoretical experiment on U_p^{Pb} (while smaller than U_d^{Pt}) also
 244 shows a positive modification of this band, as demonstrated by the comparison in Fig. 4e. In
 245 particular, the dispersive hole band shows an improvement over the DFT+U results in terms
 246 of its agreement with the experimental observation. However, the bandwidth of the nodal
 247 lines still remain sizeable, indicating that other effects such as orbital-dependent correlations
 248 may need to be further explored. We note that a recent optical study also reported electron
 249 correlation effects that flatten the nodal lines in ZrSiS [34].

250 **The topology of band structure in PtPb₄**

251 Lastly, we note that PtPb₄ is also classified as a strong topological insulator based on
 252 the symmetry indicator and topological quantum chemistry classification [6–8, 35, 36] in
 253 DFT calculations without U . While the chemical potential crosses the bands, there exists
 254 a continuous direct gap between the valence and conduction bands buried deep (about
 255 1 eV) below the chemical potential in certain parts of the BZ (see Supplementary Figure
 256 4 in the Supplementary Materials). PtPb₄ can thus be adiabatically transformed into an
 257 insulator without closing this gap, which protects its topological insulating nature. If one
 258 further considers U in a DFT + U calculation as we have done in this work, the valence and

259 conduction bands (shown as blue and red lines in Supplementary Figure 5, respectively) will
260 cross with a stable crossing point between Γ and Z , transforming PtPb₄ into a semimetal.
261 Despite the lack of a bulk gap in this case, the $k_z = 0$ and $k_z = \pi$ planes still preserve
262 time-reversal symmetry and are fully gaped. Thus, we have two 2D topological invariants
263 \mathcal{Z}_2 validly defined for these two planes. $\mathcal{Z}_2 = 1(0)$ at $k_z = 0(\pi)$ planes, indicating that
264 the semimetal phase of PtPb₄ at $U = 3$ eV is topological as well. We conclude that the
265 static interaction included in the DFT + U calculation triggers a phase transition between a
266 topological insulating state and a topological semimetal state in PtPb₄.

267 DISCUSSION

268 In summary, we have established that PtPb₄ is a Dirac nodal line material which hosts
269 band crossings protected by the nonsymmorphic symmetry of the crystal structure and
270 narrow, nearly flat bands along the BZ boundary. Moreover, we have demonstrated that
271 the narrow bands are beyond the prediction of DFT and DFT + U calculations, which may
272 indicate a non-negligible orbital-dependent dynamical electron correlation or other subtle
273 mechanism. PtPb₄ offers a platform for studying the interplay of nearly flat bands and the
274 spin-orbit coupling against the backdrop of topological protection offered by nonsymmorphic
275 crystalline symmetries.

276 METHODS

277 Sample preparation and characterization

278 Single crystals of PtPb₄ were grown using the self-flux method with a Pt:Pb ratio of
279 12.5:87.5. The starting reagents were combined in an alumina crucible and sealed in an
280 evacuated quartz tube under a partial pressure of argon. The metals were melted and
281 homogenized at 500 °C, rapidly cooled to 360 °C and then cooled at 0.5 °C/hour to 300 °C,
282 at which point the crystals were separated from excess liquid flux using a centrifuge. PtPb₄
283 forms in plate-like crystals that cleave easily with size up to 1 cm. The as-grown crystals
284 were observed to have stacking faults which could be cured by post-growth annealing, for
285 two weeks at 250 °C (see the Supplementary Note 1 and Note 2 for more details).

286 High resolution synchrotron powder X-ray diffraction data ($\lambda = 0.457861 \text{ \AA}$) were collected
287 up to $2\theta = 28^\circ$ degrees at the 11-BM beamline at the Advanced Photon Source (APS) of
288 Argonne National Laboratory. Discrete detectors collected data points every 0.001° and
289 a scan speed of $0.1^\circ \text{ sec}^{-1}$ at room temperature. Rietveld refinement, carried out with
290 TOPAS-Academic software, confirms that PtPb_4 crystallizes in the tetragonal $P4/nbm$ space
291 group (125), as previously determined [28]. Attempts to refine the model in other space
292 groups previously used for PtSn_4 such as $Aba2$ [37] or $Ccca$ [38] cannot account for the
293 reflections. We also evaluated the $(1, 1, l/2)$ positions and do not see additional reflections, in
294 contrast to the report in Ref. [23].

295 **ARPES measurements**

296 ARPES measurements were carried out at beamlines 10.0.1 and 4.0.3 of the Advanced
297 Light Source and beamline 5-2 of the Stanford Synchrotron Radiation Lightsource using a
298 R4000, R8000 and a DA30 electron analyzer, respectively. The energy and angular resolutions
299 were set to 20 meV and 0.3° , respectively. An *s*-polarization geometry is used throughout.
300 The samples were cleaved *in-situ* and kept in ultra high vacuum with a base pressure lower
301 than 4×10^{-11} torr during measurements.

302 **Theoretical calculations and details**

303 The first-principle calculations in this work were carried out by employing the Vienna Ab
304 initio Simulation Package (VASP) with the projector augmented wave (PAW) method [39].
305 We used the generalized gradient approximation (GGA), as implemented in the Perdew-
306 Burke-Ernzerhof (PBE) functional [40]. The cutoff parameter for the wave functions was
307 set to be 500 eV. The Brillouin Zone (BZ) was sampled by the gamma-centered method
308 with a k-mesh $9 \times 9 \times 9$. The surface states and the Wilson loop were calculated by using
309 our in-house code *TMC* (Library for Topological Material Calculations) with the iterative
310 Green's function approach [31] based on the maximally localized Wannier functions [41]
311 obtained through the VASP2WANNIER90 [42]. The DMFT full charge self-consistency with
312 DFT was achieved by employing the embedded-DMFT package [43]. We first obtain the
313 band structure using DFT with the PBE exchange correlation functional in Wien2k. The

314 impurity problem was solved with continuous-time quantum Monte Carlo method [44–47].

315 **DATA AVAILABILITY**

316 The data that support the findings of this study are available from the corresponding
317 author upon reasonable request.

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345 **COMPETING INTERESTS**

346 The authors declare no competing interests.

347 **AUTHOR CONTRIBUTIONS**

348 The project was initiated by A.M.H. The single crystals were grown by A.M.H. and E.M.
349 The ARPES measurements and analyses were carried out by H.W., J.W.H., J.S.O., R. J. B.
350 and M.Y. with the help of S.-K.M., J.D., D.H.L., and M.H. The theoretical calculations were
351 carried out by X.C.C., G.L. and V.L. with contributions from A.N. Powder X-ray diffraction
352 and Rietveld refinement was carried out by A.W., G.T.M. and J.Y.C. The manuscript was
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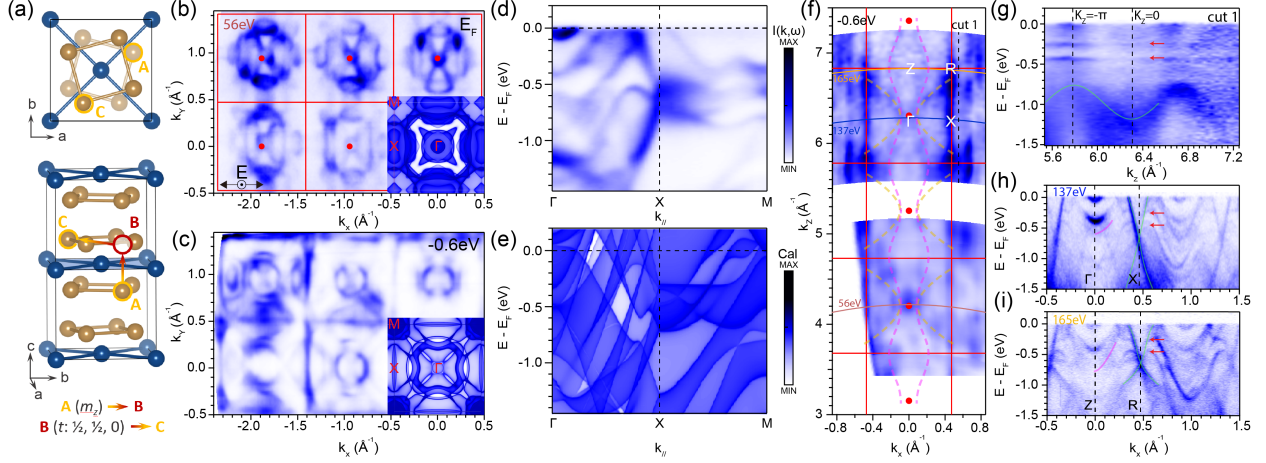


FIG. 1. **Crystal structure and electronic structure of PtPb₄.** (a) Top view and side view of the crystal structure of PtPb₄ (Pt: blue; Pb: gold). Illustration of a non-symmorphic group operation is indicated at the bottom that includes a mirror reflection and a translation. (b) Measured Fermi surface in the k_x - k_y plane integrated within 10 meV of the Fermi level. Polarization vector is as shown. DFT slab-calculation is shown for comparison. (c) ARPES constant energy contour at -0.6 eV below the Fermi level. Corresponding slab calculation is shown. (d) Band dispersions measured along the Γ -X-M direction. (e) Calculated k_z -integrated dispersions along Γ -X-M from slab calculation. Only bulk states are shown. Spin-orbit coupling (SOC) is not included in this set of calculations. (f) Constant energy contour taken at -0.6eV from a photon energy dependence study. An inner potential of 17eV was used. Selected bulk bands that are dispersive along k_z are marked. (g) A dispersion cut along cut 1 shown in (f). (h)-(i) Measured dispersions taken at 137eV and 165eV, respectively. Data in (b),(c) are taken at 25 K. Data in (d) are taken at 100 K.

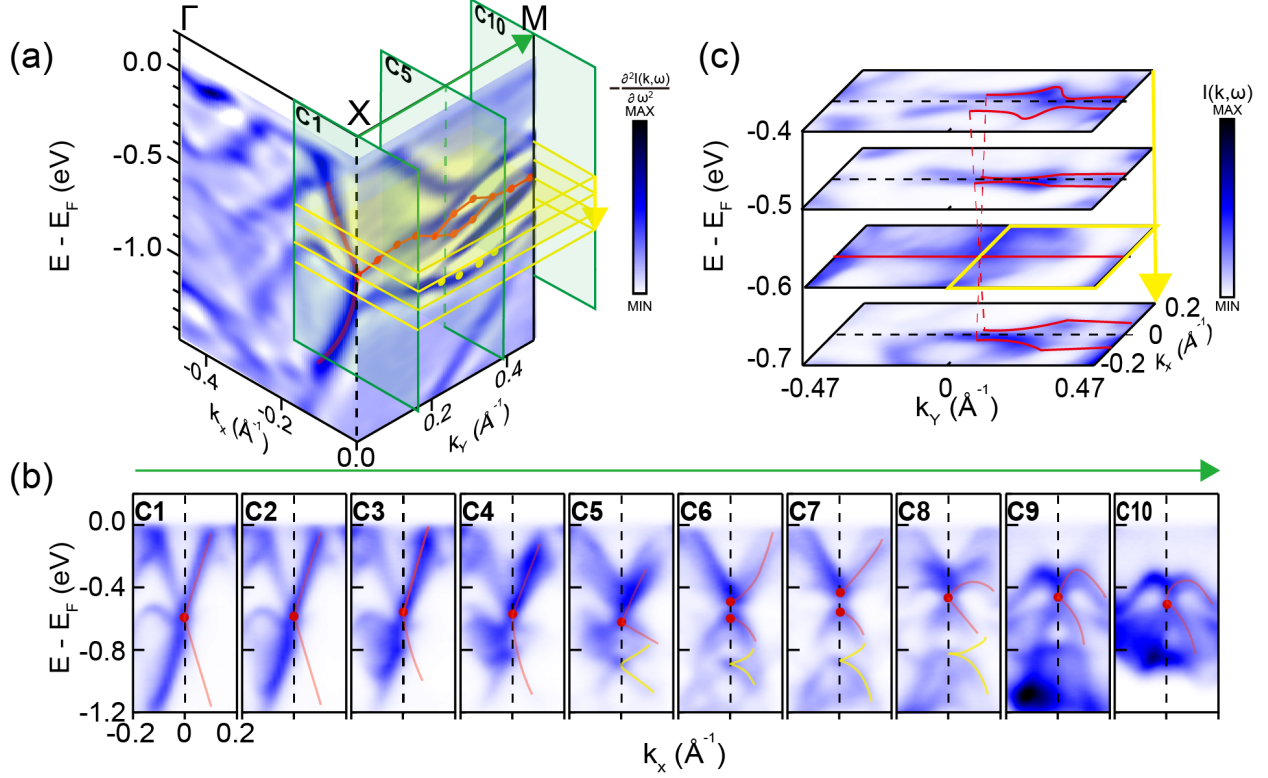


FIG. 2. **Dirac crossings along the nearly flat nodal line.** (a) 2D curvature of measured spectral image along the Γ -X-M direction. Red lines along Γ -X are guides to the eye of the dispersive band for the Dirac crossing at X. Markers along X-M indicate the fitted positions of the band crossings from energy distribution curves. (b) Dispersions measured along the direction orthogonal to X-M as shown by green slices in (a). Band crossings with unresolvable gaps are indicated by red arrows while gapped crossings are indicated by green and blue arrows. A second set of Dirac crossings are marked by yellow lines, where the crossing energies are marked as yellow markers in panel (a). (c) Constant energy contours as indicated in panel (a) along X-M to show the evolution of the crossings leading to the nodal line around -0.6 eV. Data is taken at 100 K. The polarization used is the same as in Fig. 1(d).

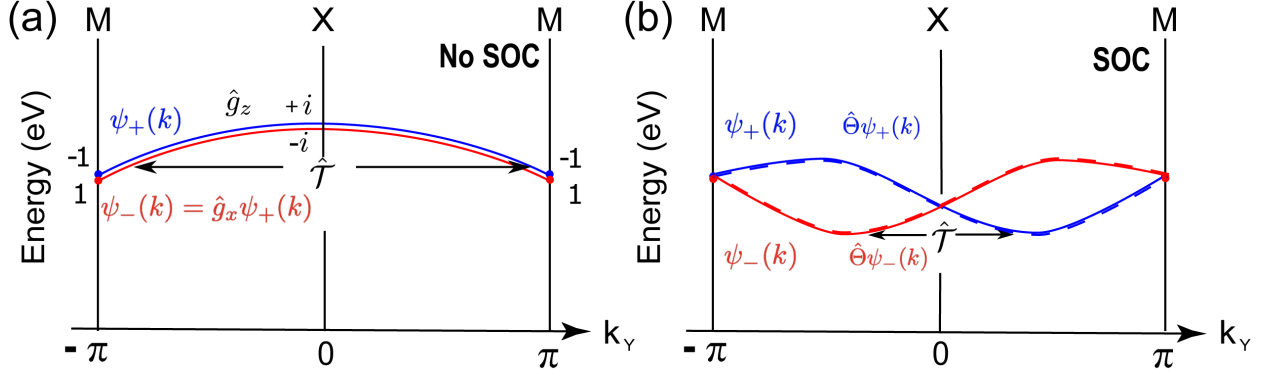


FIG. 3. **Nonsymmorphic symmetry-protected band degeneracy.** (a) Without SOC, glide symmetries \hat{g}_z and \hat{g}_x guarantee the degeneracy of the two bands ψ_+ and $\psi_- = \hat{g}_x \psi_+$. Here the blue and red solid lines denote the two bands with $\pm \hat{g}_z$ eigenvalues $\pm i e^{-k_y/2}$. Furthermore, These two bands become symmetric with respect to $\mathbf{k}_y = 0$ under time reversal symmetry (\hat{T}). (b) With SOC, the blue and red bands have to separate and each of them becomes doubly degenerate due to the Kramer's pairing. The presence of both time reversal \hat{T} and parity \hat{P} symmetries enforces the four-fold band crossings at $\mathbf{k}_y = 0, \pm\pi$ (X and M).

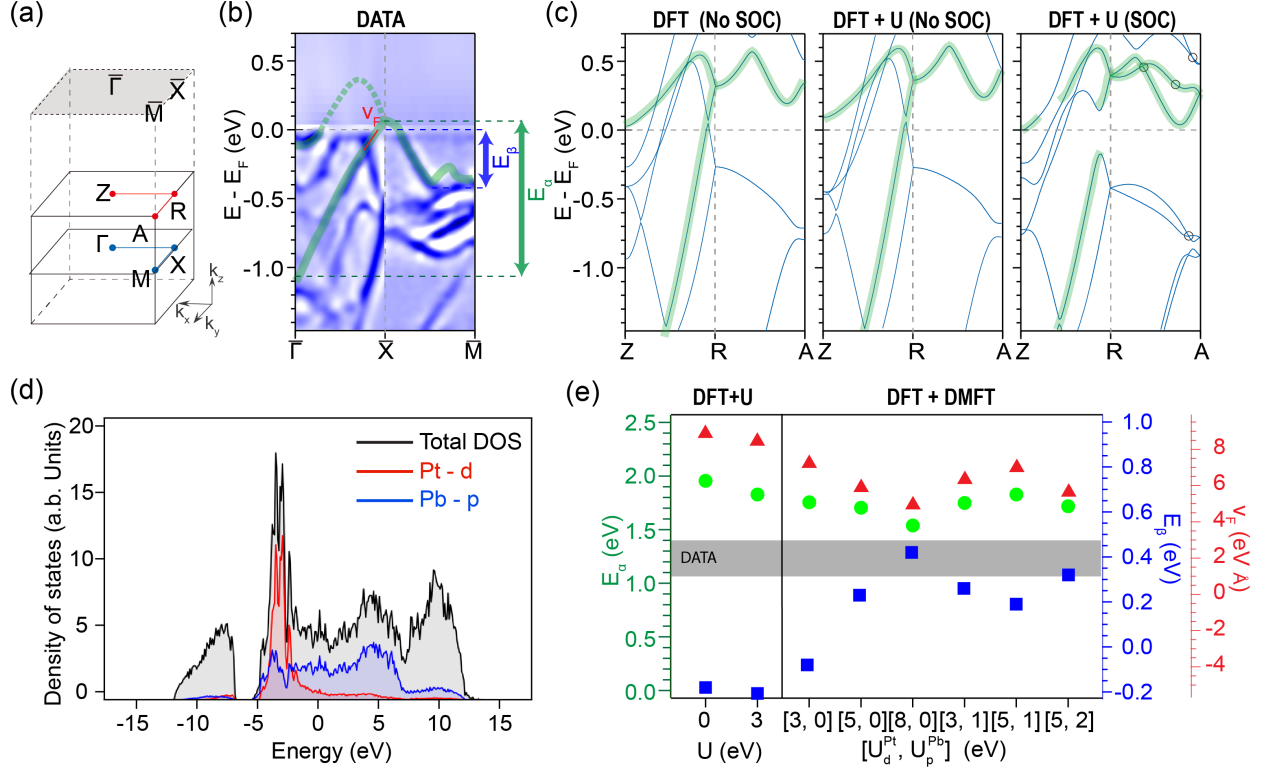


FIG. 4. **First-principle calculations of the electronic structure.** (a) BZ notations for the tetragonal unit cell and the projected surface BZ. (b) 2D curvature of measured spectral image along $\bar{\Gamma}-\bar{X}-\bar{M}$ for comparison. (c) DFT, DFT+U ($U = 3$ eV), and DFT+U with SOC calculations along the Z-R-A directions. Accidental crossings protected by the nonsymmorphic symmetry in the presence of SOC along R-A are circled. (d) Calculated partial density of states from DFT. (e) Extracted quantities as defined in (b) for DFT+U as well as DFT+DMFT (see Supplementary Materials Supplementary Figure 8) calculations shown compared to the value from measurement, indicated by the position of the gray bar for all three axes. E_α is the bandwidth of the lower branch of the green highlighted band along Z-R; v_F is its Fermi velocity; E_β is the portion of the green branch along R-A below E_F .