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Mandatory reporting frequency, informed trading, and corporate myopia

A dissertation submitted in partial satisfaction
of the requirements for the degree
Doctor of Philosophy in Management
by
Hwa Young Kim

2022

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ABSTRACT OF THE DISSERTATION

Mandatory reporting frequency, informed trading, and corporate myopia

by

Hwa Young Kim

Doctor of Philosophy in Management

University of California, Los Angeles, 2022

Professor Henry L. Friedman, Chair

This paper examines the relationship between mandatory reporting frequency and corporate myopia in the presence of informed trading. While previous studies attribute myopia to frequent reporting, the empirical evidence of this claim is inconsistent. The results herein show that corporate myopia can be sustained under both frequent and infrequent reporting regimes. I also demonstrate that the level of myopia can even increase as mandatory reporting frequency decreases when reporting noise is sufficiently high since less frequent reporting induces more informed trading. The results offer potential explanations for the mixed empirical findings regarding the relationship between mandatory reporting frequency and corporate myopia. Moreover, they are robust to extensions, including dynamic trading, different information structures, voluntary disclosure, or an alternative market structure. Overall, this study highlights that increasing mandatory reporting frequency does not always exacerbate corporate short-termism when additional information sources are taken into account.

The dissertation of Hwa Young Kim is approved.

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2022

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Mandatory reporting frequency, informed trading, and corporate myopia

1 Introduction

Frequent mandatory reporting is often criticized for encouraging corporate short-termism. Anecdotally, firms blame quarterly reporting for adding short-term performance pressure, and regulators in different countries have expressed concerns regarding frequent disclosure requirements.¹ In 2004, the European Union (EU) considered mandating quarterly reporting but instead resorted to interim management statements (IMS), which require narrative disclosures but not financial statements.² The EU later eliminated even this requirement in 2013, citing possible costs related to short-termism and disclosure preparation (EU, 2013). In the United States, various stakeholders, such as firms, investors, and politicians, argue that the SEC should decrease mandatory reporting frequency to reduce short-term pressure. The SEC requested public comments on mandatory reporting frequency in 2019 to gather opinions on the potential costs and benefits of decreasing reporting frequency (SEC, 2019). Such interest has motivated academic research in this area. Interestingly, empirical studies find mixed results regarding the relationship between the

¹For instance, Porsche refused to comply with quarterly reporting requirements, asserting that they induce myopic corporate decision-making. Porsche was eventually expelled from the M-DAX index in 2001 over its refusal to adhere to the requirement (Edmans et al., 2016).

²"IMS should contain an explanation of material events and transactions that have taken place during the relevant period and their impact on the financial position of the issuer and its controlled undertakings, and a general description of the financial position and performance of the issuer and its controlled undertakings during the relevant period." (EU, 2004)

frequency of mandatory reporting and corporate short-termism (Ernstberger et al., 2017; Fu et al., 2020; Kajüter et al., 2019; Kraft et al., 2017; Nallareddy et al., 2017; Witte et al., 2022). While the mixed results could be attributed to differences in research designs, it remains unclear which factor drives the inconsistency in findings.

To reconcile the mixed empirical findings, this paper analytically examines myopia when investors can acquire a private signal about firm performance. I study how informed trading interacts with firm disclosure and how this interaction affects corporate myopia under frequent and infrequent reporting regimes.

In the model, a firm is run by a manager who cares about short- and long-run stock prices. The manager decides how much capital to put into short- and long-term projects, while investors choose whether to acquire costly private signals about firm value and trade based on the acquired information. In this setting, corporate myopia arises due to short-run price concerns via a capital-constrained manager overinvesting in the short-term operating project. I examine how investors' information acquisition incentives and trading behaviors change with the firm's reporting frequency. Then, I compare the firm's myopia level under the infrequent and frequent mandatory reporting regimes.

This paper first examines the baseline case where a non-zero portion of investors is endowed with a private short-term signal. Unlike in Gigler et al. (2014), where the myopia problem only appears under the frequent reporting regime, I find that corporate myopia persists even under the infrequent mandatory reporting regime. This can be attributed to the information about short-term firm performance getting reflected in the interim stock price via informed trading, even in the absence of mandated disclosure. In the main setting, I endogenize investors' information acquisition decisions. In this case, decreasing mandatory reporting frequency can aggravate the myopia problem, particularly when the interim reporting quality is relatively low. This result arises due to the interaction effect, where investors have higher information acquisition incentives under the infrequent regime. The result also highlights the importance of incorporating alternative information sources as this can lead to different predictions from the result identified in the prior

studies. Finally, I show that the results can be generalized to various extensions: a dynamic trading model, one with short- and long-run private signals, and a model featuring an alternative market microstructure.

The primary contribution of this study is to provide a better understanding of the effects of changing reporting frequency on corporate myopia by considering alternative information channels. Although informed trading is a crucial information source in the financial market, previous literature has not considered this when examining the relationship between reporting frequency and corporate short-termism. The paper highlights the importance of considering other information sources by showing that incorporating the interaction among different information channels can lead to different findings.

Moreover, this study provides a potential explanation for the mixed empirical findings by showing that reducing the mandatory reporting frequency may not always mitigate the myopia problem. With endogenous information acquisition, reducing the reporting frequency can increase corporate short-termism, particularly when the interim reporting quality is low. In addition, this paper documents conditions on reporting quality and capital under which changing reporting frequency has a stronger effect on short-sighted operating decisions. These results offer empirical implications by identifying conditions under which reducing the reporting frequency effectively mitigates corporate myopia.

Finally, this paper addresses regulators' interest in setting the optimal reporting frequency. In 2019, the SEC requested public comments to gauge the costs and benefits of quarterly reporting (SEC, 2019). Other countries have discussed the potential costs and benefits of changing reporting frequency, which indicates that the effect of varying reporting frequency is of global interest. The results in this paper provide implications to regulators that quarterly reporting requirements should be jointly considered when considering the impact of reporting frequency on corporate myopia.

2 Prior Literature

Prior studies show the potential benefits of increasing reporting frequency. Using the U.S. setting, previous studies show that increasing the mandatory reporting frequency leads to higher earnings timeliness for voluntary adopters (Butler et al., 2007) and lower information asymmetry (Fu et al., 2012). In addition, Hillegeist et al. (2020) document a positive feedback effect where managers learn more from the stock price under the frequent than under the infrequent regime.

Another stream of literature examines the potential costs of increasing reporting frequency. Gigler et al. (2014) analytically show that, while mandating firms to report more frequently disciplines overinvestment, it also comes with a cost of corporate myopia. Empirical papers test the prediction on corporate myopia using regulatory changes in several countries. Using the EU's adoption of mandated interim quarterly narrative reports, Ernstberger et al. (2017) find that real activities management becomes more pronounced as reporting frequency increases. Kraft et al. (2017) show that U.S. firms decrease capital expenditure upon switching from semi-annual to quarterly reporting. Fu et al. (2020) find a negative relationship between reporting frequency and innovation, measured by patents. However, Nallareddy et al. (2017) find no evidence that the initiation of mandatory quarterly reporting changed firms' long-term investment levels in the U.K. Using a European sample, Witte et al. (2022) document that corporate myopia persists even after firms switch from quarterly to semi-annual financial reporting. Additionally, Kajüter et al. (2019) find no evidence of stronger corporate myopia for firms that were required to change from semi-annual to quarterly reporting in Singapore. The mixed results may arise from cross-country differences in capital markets or quarterly reporting requirements. For instance, unlike the U.S., which requires quarterly financial statements, Europe's interim statements only mandated qualitative discussion; quantitative financial reports were optional.

Another line of literature examines the relationship between short-term voluntary forecasts (e.g., quarterly earnings guidance) and corporate myopia. The issuance of quarterly guidance induces additional short-term price pressure and can motivate managers to meet or beat their self-created targets by sacrificing long-term value.³ This claim has motivated researchers to examine

³Some firms ceased issuing quarterly guidance claiming that short-term guidance undermines their long-term focus. For instance, Google declined to provide quarterly guidance in 2004, saying that it would promote short-term thinking.

whether firms that provide quarterly guidance are more likely to engage in myopic behaviors. While Cheng et al. (2005) find that short-term guidance is associated with myopia, other papers document either no difference in corporate myopia between guiding and non-guiding firms (Call et al., 2014; Houston et al., 2010) or a negative relationship between short-termism and guidance issuance (Chen et al., 2015). Prior empirical evidence points to the possibility that more voluntary disclosure does not necessarily lead to higher short-termism.⁴

Building on the previous literature, I examine how incorporating an additional information channel changes the relationship between financial reporting frequency and corporate myopia.

3 Model

There are two types of players: a risk-neutral manager and risk-averse investors. The manager maximizes the weighted average of short- and long-term stock prices, P_1 and P_2 . Specifically, the manager's objective function is $\alpha P_1 + (1 - \alpha)P_2$, where $\alpha \in (0, 1)$ reflects the level of managerial short-termism.⁵ There is a continuum of investors with negative exponential utility, $U_i = -e^{-\gamma W_i}$, where W_i is investor i 's terminal wealth and $\gamma > 0$ is the degree of risk-aversion. The total mass of investors is 1.

I first provide a sketch of the model and elaborate on the details in later sections. At the beginning of the game, the manager makes an operating decision by deciding how much capital to spend on short- and long-term projects. Corporate myopia arises when the manager puts more capital into the short-term operating project than the level that maximizes the firm's cash flows in order to boost near-term performance. Under the frequent reporting regime, the short-term cash flow is disclosed to the market via mandatory disclosure in the interim period; no report is released under the infrequent regime. A later report reveals total performance in both reporting

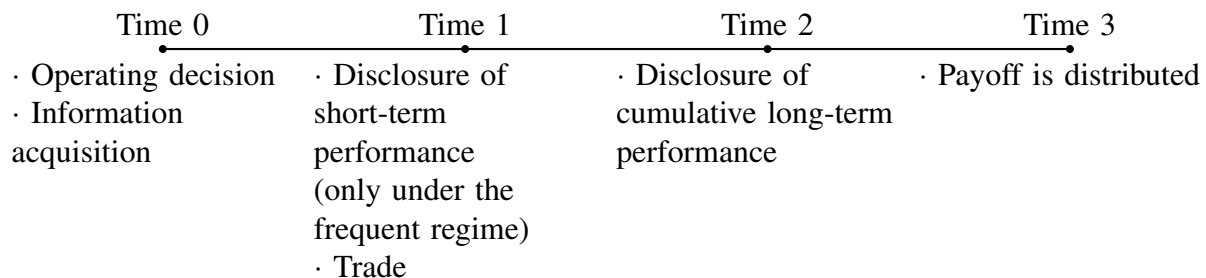
⁴In the extension, I explore the impact of voluntary disclosure by allowing a manager to voluntarily release a short-term performance report, which has the same information content as interim mandatory disclosure.

⁵Factors such as compensation, reputation, or turnover can lead to a manager's interest in short-term stock price. Prior studies that examine myopia (e.g., Stein (1989), Gigler et al. (2014), and Edmans et al. (2016)) also assume that the manager's weight on interim price is given exogenously. Endogenizing α is beyond the scope of this paper.

regimes. Investors can choose to become informed by acquiring information about short-term firm performance at a fixed cost $c > 0$. After informed traders observe the private signals and the firm's short-term performance is disclosed in the interim period, trading occurs, which determines P_1 . There is no discounting. I compare the manager's operating choice under two regimes to derive results on the effect of reporting frequency on corporate myopia.

Figure 1 summarizes the timeline of the model.

Figure 1: Timeline



3.1 Operating decision

The manager's operating decision affects short- and long-run firm performance, v_1 and v_2 , respectively. At time 0, the manager has capital I that can be spent on two projects, S and L .⁶ Projects can represent not only investments (e.g., R&D) but also operating decisions regarding production, marketing, or hiring. The two projects differ in the timing of payoff realization and the net payoff. Input of k_1 into project S gives a time 1 payoff of $y_1 = k_1\mu_1 - \frac{k_1^2}{2}$, where $0 \leq k_1 \leq I$. Spending k_2 on project L implies a time 2 payoff of $y_2 = k_2\mu_2 - \frac{k_2^2}{2}$, where $0 \leq k_2 \leq I - k_1$. I assume that $\mu_2 \geq 2\mu_1 > 0$, which indicates that the marginal benefit of L is greater than that of S . Also, this assumption is sufficient for having a positive amount of input into both projects S and L . When capital is constrained, the opportunity cost of allocating capital to the short-term project increases in the difference in expected payoffs, $\mu_2 - \mu_1$.

⁶For simplicity, the model assumes that there is no alternative way of using capital. The results do not change if an alternative capital use exists, as long as the opportunity is publicly known. The analysis incorporating alternative capital use is included in Appendix B.

Short- and long-term firm performances are defined as $v_1 = y_1 + \delta_1$ and $v_2 = y_2$. y_t is the operating outcome at time t , and $\delta_1 \sim \mathcal{N}(0, \sigma_1^2)$ is the uncontrollable factor that affects short-run firm performance at time 1.⁷ The firm's liquidating dividend at time 3 is $v_1 + v_2 = y_1 + \delta_1 + y_2$.

The manager with a short-term price concern α solves the following maximization problem:

$$\max_{k_1, k_2} \alpha E[P_1] + (1 - \alpha)E[P_2] \quad (1)$$

$$\text{s.t. } 0 \leq k_1 \leq I \quad (2)$$

$$0 \leq k_2 \leq I - k_1. \quad (3)$$

While the above parameters and the available amount of capital are public, the manager's actual operating decision (k_1, k_2) is unobservable. This is reflective of operating decisions whose expenses are aggregated into the operating expense line item. For example, while the manager can allocate resources to both short- and long-term marketing activities, it is difficult for the investors to perfectly infer how much input is spent on each activity. Likewise, while the horizon of demand forecasting and the corresponding pricing strategy could be either short- or long-term oriented, it is hard to identify the manager's operating decision even when the operating expense item is disclosed.

3.2 Trading

The market microstructure follows Grossman and Stiglitz (1980). There is a continuum of investors with CARA utility over terminal wealth and risk aversion coefficient $\gamma > 0$. The total mass of the investors is 1, with a fraction $n \in [0, 1]$ being informed and $1 - n$ being uninformed. Investor i has an initial wealth of W , and there are two assets, a risky asset (firm share) and a risk-free asset with a gross return of 1. The supply of the risky asset x follows $x \sim \mathcal{N}(0, \sigma_x^2)$. The uncertainty in supply x can be due to noise trading, and this prevents the price from fully revealing

⁷Assuming uncertainty on both time 1 and time 2 firm performances does not qualitatively change the result but complicates the analysis. Therefore, I assume that $v_2 = y_2$ for tractability. In Section 6.2, I explore the extension with both short- and long-term uncertainty, and where investors can acquire either short- or long-term private signals.

investors' private information. If investor i acquires a costly signal, the investor privately observes a conditionally independent signal $s_i = v_1 + \eta_i$, where $\eta_i \sim \mathcal{N}(0, \sigma_\eta^2)$.

3.3 Disclosure

Under the frequent regime, the firm's accounting system produces a noisy signal on short-term firm performance, $e_1 = v_1 + \varepsilon$, where $\varepsilon \sim \mathcal{N}(0, \sigma_\varepsilon^2)$. At time 2, total firm performance $\{v_1, v_2\}$ becomes public.⁸ Under the infrequent regime, there is no interim report at time 1, and the market only observes firm performance $\{v_1, v_2\}$ at time 2. I assume that the mandatory report is the only signal released by the firm.

Note that the interim performance report does not reveal the manager's operating decision, $\{k_1, k_2\}$. This setting is consistent with firms releasing signals about quarterly earnings without details about the firm's operating choices. For example, when quarterly reporting became mandatory in Europe, firms had the flexibility of which information to include in quarterly reports.⁹ As a result, many firms did not include financial statements.¹⁰ When a firm discloses quarterly financial statements, indeed, investors can acquire informative signals about certain long-term activities such as R&D, capital expenditures, or investments in intangibles.¹¹ However, there are operating activities that are relatively opaque even with financial statements: marketing, production, pricing, inventory management, or employee hiring and training. These activities can have differing horizons, and the aggregated operating expense line in a financial statement is unlikely to reveal what type of operating decision was made. For example, an IT outlay used to set up an internet-based distribution system can take time to establish, but this can provide a long-run benefit of sustainable growth as the tendency to purchase goods and services online increases. Yet,

⁸Since time 2 report does not contain noise, disclosure of $\{v_1, v_2\}$ is equivalent to cumulative firm performance $v_1 + v_2$ becoming public.

⁹Firms had an option to issue a qualitative discussion, quantitative accounting summary numbers, or financial statements.

¹⁰Nallareddy et al. (2017) examine 100 randomly selected U.K. firms and document that only ten percent of these firms issue both balance sheet and income statement.

¹¹There exist separate line items for these activities, and these are unlikely to be interpreted as short-term investments.

such expenses are mixed with other short-term activities within the SG&A account. Also, while a temporary increase in a salesperson's commission can immediately boost near-term revenue, a brand-building marketing campaign will likely lead to profits after a longer period of time. From the market's perspective, observing the operating expense on an income statement is not likely to reveal the details of the operating decisions. Overall, I expect the results in this model to best apply to cases either when the firm only provides a summary interim performance report or for operating activities that are less transparent to investors.

4 Exogenous information acquisition

I derive a rational expectations equilibrium where the market's conjecture $\{\hat{k}_1, \hat{k}_2\}$ equals the actual choice of the manager $\{k_1, k_2\}$. As shown in the analysis, the manager's operating decision depends on the known parameters. Therefore, the market can perfectly infer the manager's decision. Nevertheless, the price still plays a role in shaping the manager's operating choice since the actual choice remains unobservable to the market. I first solve for the case where a proportion $n \in [0, 1]$ of investors are informed. Then, in the next section, I endogenize the proportion of informed investors.

4.1 Benchmark

I examine the benchmark operating choice at time 0 that maximizes the long-term firm performance ($\alpha = 0$). In this case, the manager maximizes $E[P_2] = E[v_1 + v_2]$. When $I \geq \mu_1 + \mu_2$, constraints (2) and (3) are slack and capital is effectively unconstrained. Therefore, the manager can allocate optimal amounts in both projects ($k_1^* = \mu_1$ and $k_2^* = \mu_2$).

However, when capital is constrained ($I < \mu_1 + \mu_2$), constraint (3) binds (i.e., $k_2^* = I - k_1$). Solving the maximization problem gives $k_1^B = \max \left\{ \frac{I - (\mu_2 - \mu_1)}{2}, 0 \right\}$ and $k_2^B = I - k_1^B$. Note that $k_1^B < \mu_1$ since $I < \mu_1 + \mu_2$. In other words, it is inefficient to spend μ_1 in project S when the capital is constrained.

To focus on the scenario where the manager has to choose between the short- and the long-term projects, I assume that the firm's capital is constrained, $I < \mu_1 + \mu_2$. Also, I assume that $I \geq \mu_2 - \mu_1$. This condition ensures that the benchmark amount of capital spent in project S is greater than or equal to zero ($k_1^B = \frac{I - (\mu_2 - \mu_1)}{2} \geq 0$). Overall, capital I satisfies $0 < \mu_1 < \mu_2 - \mu_1 \leq I < \mu_1 + \mu_2$.

4.2 Frequent mandatory reporting regime

I solve for the perfect Bayesian equilibria where the players form rational expectations about the other players' strategies and actions and make optimal decisions given their information sets. Since investors have CARA utility and firm performance follows a normal distribution, I conjecture and verify a linear price equilibrium.

Since firm value is realized at time 2, stock price at time 2 is equal to the liquidating dividend for both reporting regimes.

$$P_{2,F} = v_1 + v_2 \quad (4)$$

Investors form a linear conjecture for time 1 price:

$$P_{1,F} = \beta + \beta_v v_1 + \beta_e e_1 + \beta_x x. \quad (5)$$

The CARA-normal setup implies that

$$D_i^F(e_1, s_i, P_{1,F}) = \frac{E(v_1 + v_2 | e_1, s_i, P_{1,F}) - P_{1,F}}{\gamma \text{Var}(v_1 + v_2 | e_1, s_i, P_{1,F})} \quad (6)$$

$$D_U^F(e_1, P_{1,F}) = \frac{E(v_1 + v_2 | e_1, P_{1,F}) - P_{1,F}}{\gamma \text{Var}(v_1 + v_2 | e_1, P_{1,F})}, \quad (7)$$

where D_i^F, D_U^F indicate informed investor i 's and uninformed investors' demand quantities under the frequent regime, respectively. Intuitively, the optimal demand is equal to the expected excess return scaled by the investor's risk aversion and the posterior variance of the asset given the information set. The price is determined so that it satisfies the market clearing condition:

$$\int_0^n D_i^F(e_1, s_i, P_{1,F}) di + (1 - n) D_U^F(e_1, P_{1,F}) = x. \quad (8)$$

Time 1 stock price under the frequent regime is characterized below.

$$\begin{aligned}
P_{1,F} = & \frac{\frac{1}{\sigma_1^2} E[v_1]}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}} + E[v_2] + \frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\beta_v}{\beta_x} \right)^2}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}} \cdot v_1 \\
& + \frac{\frac{1}{\sigma_\varepsilon^2}}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}} \cdot e_1 - \frac{\frac{1}{\sigma_x^2} \frac{n}{\gamma \sigma_\eta^2} + \gamma}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}} \cdot x \quad (9)
\end{aligned}$$

The manager chooses $\{k_1, k_2\}$ that maximize the manager's weighted average of the short- and long-run stock prices subject to the capital constraint. The lemma below summarizes the equilibrium operating choices under the frequent regime.

Lemma 1. *Under the frequent mandatory reporting regime: When a measure n of investors possess private signals on short-term firm performance, a manager with α chooses*

$$k_{1,F}^* = \frac{\alpha X_F \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha X_F + 2(1 - \alpha)} \geq k_1^B,$$

where $X_F = \frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_\varepsilon^2}}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}}$ reflects time 1 price efficiency under the frequent regime.

Lemma 1 shows that $k_{1,F}^* \geq \frac{I - (\mu_2 - \mu_1)}{2} = k_1^B$, implying that inefficient corporate myopia occurs under the frequent regime.¹² Since the relevant parameters in the manager's maximization problem in (1) are publicly available, in equilibrium, the market forms a correct conjecture about the manager's operation choice. In other words, the manager's actual choice equals the conjecture. However, inefficient corporate myopia persists in this setting. This happens because of the uncertainty from the δ_1 component of v_1 . This uncertainty prevents the interim disclosure from revealing the manager's operating choice and incentivizes investors to acquire private signals, leading to corporate myopia.¹³ Also, note that the equilibrium short-term input is strictly increasing

¹²Since $I \geq \mu_2 - \mu_1$, the benchmark short-term capital input that maximizes long-term value is always weakly greater than zero.

¹³Suppose $\delta_1 = 0$ and there was no uncertainty. Then, the interim disclosure under the frequent regime always reveals the manager's operating decision since investors can back out capital inputs $\{k_1, k_2\}$. In addition, the absence of disclosure removes the investors' incentives to acquire costly signals both under frequent and infrequent regimes. Thus, the time 1 price under the frequent regime will reflect the manager's actual choice, and that under the infrequent regime will not reflect actual short-term performance.

in price informativeness of P_1 about short-term firm performance (X_F), i.e., $\frac{\partial k_{1,F}^*}{\partial X_F} > 0$. This is because, unlike in the benchmark setting where the manager only cares about long-term cumulative performance, the manager also cares about interim stock price, P_1 . The manager has a higher incentive to engage in myopic operating decisions when the interim stock price is more informative about short-term performance, v_1 . This is because the interim stock price is more responsive to the manager's operating choices when the short-term price efficiency is higher.

4.3 Infrequent mandatory reporting regime

As in Section 4.2, time 2 price is equal to the realized firm value, $P_{2,I} = v_1 + v_2$. I conjecture and verify a linear form for time 1 price, $P_{1,I} = \lambda + \lambda_v v_1 + \lambda_x x$. Solving for the price and the equilibrium operating choice following steps similar to those in the prior section gives Lemma 2.

Lemma 2. *Under the infrequent mandatory reporting regime: When a measure n of investors possess private signals on short-term firm value v_1 , a manager with α chooses*

$$k_{1,I}^* = \frac{\alpha X_I \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha X_I + 2(1 - \alpha)} \geq k_1^B,$$

where $X_I = \frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2}}$ reflects time 1 price efficiency under the infrequent regime.

Under the infrequent regime the optimal choice of $k_{1,I}^*$ is greater than or equal to $k_1^B = \frac{I - (\mu_2 - \mu_1)}{2}$. This indicates that managers make inefficient short-sighted operating decisions even under the infrequent reporting regime. The result contrasts with that in Gigler et al. (2014), where the corporate myopia problem is completely resolved under the infrequent regime. This difference arises because information on short-term firm performance is still impounded into the price under the infrequent regime via informed trading in the current model, while Gigler et al. (2014) assume that there is no information source under the infrequent regime.

4.4 Comparison of frequent and infrequent regimes

As noted earlier, equilibrium corporate myopia increases with price informativeness about the interim performance. Therefore, for comparing regimes, it suffices to examine the time 1 price efficiency under the frequent and infrequent regimes. The following proposition compares the myopia level under the two regimes.

Proposition 1. *When an exogenous measure n of investors are informed, myopia is always higher under the frequent than under the infrequent regime ($k_{1,F}^* > k_{1,I}^*$).*

Proposition 1 shows that given an exogenous proportion of informed investors, myopia is always more pronounced in the frequent than in the infrequent regime. This is because price informativeness is higher under the frequent than the infrequent regime when there is a fixed proportion of informed investors. The result is consistent with the one in Gigler et al. (2014), which shows that myopia is more pronounced under the frequent regime when a mandatory report is the only information source.

To provide intuition behind the result, note that reducing reporting frequency has two effects. First, the absence of firm disclosure decreases price informativeness. However, higher weight is put on the signal from informed trading when the firm does not disclose, which indirectly increases price informativeness. Overall, the first effect dominates, and price efficiency is always lower under the infrequent regime. Note that the result in Proposition 1 does not consider endogenous information acquisition decisions or the interaction between firm disclosure and information acquisition, which are considered in Section 5.

The next proposition examines how the gap between the corporate myopia level under the two regimes changes with parameters.

Proposition 2. *When an exogenous measure n of investors are informed, the difference in corporate myopia between the frequent and the infrequent reporting regime ($k_{1,F}^* - k_{1,I}^*$)*
(1) decreases with the proportion of informed investors (n),
(2) increases with the noise in the informed investors' private signals (σ_η^2),

(3) decreases with the mandatory reporting noise (σ_ε^2),

(4) increases (decreases) with time 1 uncertainty (σ_1^2) when $\frac{1}{\sigma_1^2} > (<) \frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma\sigma_\eta^2} \right)^2 + \frac{1}{\sigma_\varepsilon^2}$,

(5) decreases with the capital (I).

Parts (1) and (2) hold because, although $k_{1,F}^*$ and $k_{1,I}^*$ both increase with n and decrease with σ_η^2 , the effect is stronger under the infrequent regime than under the frequent regime because informed trading has a higher impact in the infrequent regime. Part (3) holds because price efficiency decreases with σ_ε^2 under the frequent regime but is independent of σ_ε^2 under the infrequent regime. Therefore, given an exogenous proportion of informed investors n , reducing the reporting frequency will be more effective in reducing corporate myopia when the mandatory reporting noise is low. The result in part (4) implies that the effect of reducing reporting frequency on myopia is nonmonotonic with respect to time 1 uncertainty. While the magnitude of the effect increases with time 1 uncertainty when σ_1^2 is relatively low, it decreases when σ_1^2 is relatively large. In part (5), the increase in capital I mitigates the myopia problem, and this effect is more pronounced under the frequent regime. Therefore, decreasing reporting frequency will be more effective in mitigating corporate myopia for firms with tighter capital constraints. Proposition 2 indicates that the effectiveness of reducing mandatory reporting frequency in mitigating the myopia problem depends on firm-specific and market-wide factors, such as uncertainty, reporting noise, capital constraints, and informed trading characteristics.

5 Endogenous information acquisition

This section endogenizes investors' information acquisition decisions and derives the equilibrium proportion of investors n who acquire information among a continuum of investors. At time 0, investor i can choose to acquire a private signal s_i at a fixed cost $c > 0$. An individual investor will pay to observe a private signal when the incremental utility of being informed is greater than or equal to the cost of observing information. I assume that an investor acquires information when indifferent.

5.1 Equilibrium proportion of informed investors

Lemmas 3 and 4 summarize the equilibrium proportion of informed investors under the infrequent and the frequent regimes.

Lemma 3. *The equilibrium proportion of informed investors under the frequent regime (n_F) is characterized below.*

- 1) When $e^{2\gamma c} - 1 > \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}}$, $n_F = 0$.
- 2) When $e^{2\gamma c} - 1 \leq \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2}$, $n_F = 1$.
- 3) Otherwise, $n_F = \gamma \sigma_x \sigma_\eta^2 \sqrt{\frac{\frac{1}{\sigma_\eta^2}}{e^{2\gamma c} - 1} - \frac{1}{\sigma_1^2} - \frac{1}{\sigma_\varepsilon^2}} \in (0, 1)$.

Lemma 4. *The equilibrium proportion of informed investors under the infrequent regime (n_I) is characterized below.*

- 1) When $e^{2\gamma c} - 1 > \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2}}$, $n_I = 0$.
- 2) When $e^{2\gamma c} - 1 \leq \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2}$, $n_I = 1$.
- 3) Otherwise, $n_I = \gamma \sigma_x \sigma_\eta^2 \sqrt{\frac{\frac{1}{\sigma_\eta^2}}{e^{2\gamma c} - 1} - \frac{1}{\sigma_1^2}} \in (0, 1)$.

Lemmas 3 and 4 show that an investor's information acquisition decision depends on the value of $e^{2\gamma c}$. A comparison of the equilibrium proportion of informed investors indicates that given an information acquisition cost, the equilibrium proportion of informed investors is always weakly greater under the infrequent regime than under the frequent regime, i.e., $n_I \geq n_F$. This is because the firm's disclosure under the frequent regime reduces the value of acquiring a private signal.

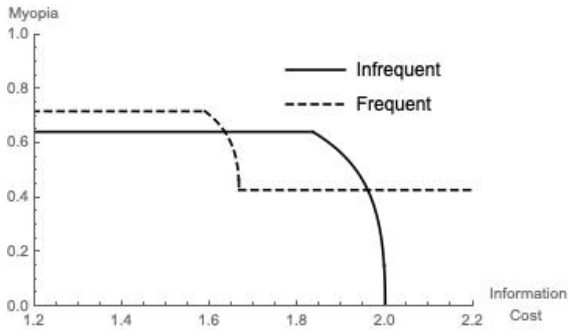
5.2 Comparison of frequent and infrequent regimes

Substituting the equilibrium n_I and n_F from Lemmas 3 and 4 into price informativeness under the infrequent and the frequent regimes in Lemma 1 and 2 allows me to compare the degree of corporate myopia under the two regimes. This comparison is summarized in Proposition 3.

Proposition 3. (a) When the reporting quality $\left(\frac{1}{\sigma_\varepsilon^2}\right)$ is relatively low such that $\frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_\eta^2} > \frac{1}{\sigma_\varepsilon^2}$, there exists an interval of information acquisition cost $[\underline{c}, \bar{c}] \subset [0, +\infty]$ such that when $c \in [\underline{c}, \bar{c}]$, corporate myopia is more pronounced under the infrequent regime than the frequent regime. When $c \notin [\underline{c}, \bar{c}]$, corporate myopia is more pronounced under the frequent regime than under the infrequent regime.

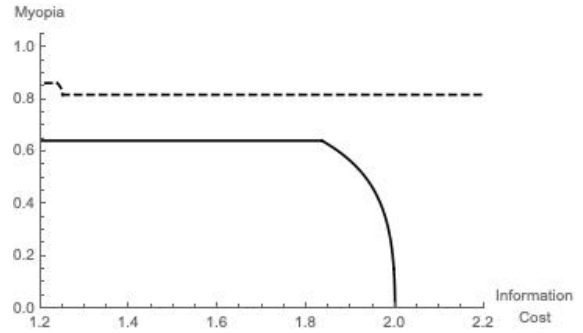
(b) When the reporting quality $\left(\frac{1}{\sigma_\varepsilon^2}\right)$ is relatively high such that $\frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_\eta^2} < \frac{1}{\sigma_\varepsilon^2}$, then corporate myopia is always more pronounced under the frequent regime than the infrequent regime.

Figure 2: Low reporting quality



$$\alpha = \gamma = \frac{1}{2}, \mu_1 = 3, \mu_2 = 10, I = 7, \\ \sigma_1^2 = \sigma_\eta^2 = \sigma_x^2 = \frac{3}{2}, \sigma_\varepsilon^2 = \frac{3}{2}$$

Figure 3: High reporting quality



$$\alpha = \gamma = \frac{1}{2}, \mu_1 = 3, \mu_2 = 10, I = 7, \\ \sigma_1^2 = \sigma_\eta^2 = \sigma_x^2 = \frac{3}{2}, \sigma_\varepsilon^2 = \frac{1}{2}$$

Proposition 3 shows that the effect of varying mandatory reporting frequency on corporate myopia depends on the interim reporting quality. Figures 2 and 3 illustrate the results in Proposition 3. These graphs show how myopia level under the two regimes changes with information acquisition cost (c) when interim reporting quality is relatively low and high, respectively. Figure 2 indicates that reducing the reporting frequency can exacerbate the myopia problem when the noise of the mandatory report is sufficiently high, especially for intermediate values of information acquisition cost. This is because the absence of disclosure can encourage more information acquisition, which increases the overall time 1 price efficiency regarding short-term performance under the infrequent regime. When the reporting quality is low, the increase in price informativeness due to informed trading can outweigh the reduction in price efficiency due to the absence of mandatory disclosure. Therefore, inefficient corporate myopia is more

pronounced under the infrequent regime than under the frequent regime. This result contrasts with the result in Gigler et al. (2014) that reducing reporting frequency mitigates the corporate myopia problem. However, Figure 3 shows that when the reporting quality is high, the second effect always dominates, and the price efficiency under the infrequent regime is lower than that under the frequent regime.

Next, I examine how the gap between the corporate myopia level under the two regimes changes with parameters.

Proposition 4. *When the proportion of informed investors n is endogenous and $n_F \in (0, 1)$, the difference in corporate myopia between the frequent and the infrequent reporting regime ($k_{1,F}^* - k_{1,I}^*$)*

(1) increases with the mandatory reporting noise (σ_ϵ^2),

(2) decreases (increases) with the capital (I) when $k_{1,F}^ > (<)k_{1,I}^*$.*

Unlike in the exogenous information acquisition case, the gap between the frequent and the infrequent regime increases with mandatory reporting noise (σ_ϵ^2). This is because the increase in reporting noise has an indirect effect on information acquisition incentives under the frequent reporting regime. A noisier mandatory report triggers more information acquisition, which increases price informativeness under the frequent regime. Thus, the gap in corporate myopia between the frequent and the infrequent regime increases with the mandatory reporting noise with endogenous information acquisition. The result indicates that when myopia is more pronounced under the frequent (infrequent) regime, decreasing (increasing) the reporting frequency will be more (less) effective in mitigating the myopia problem as the mandatory reporting quality decreases. The result implies that the difference in interim reporting quality between countries used in prior empirical studies can be a potential reason behind the mixed findings.

The comparative statics on capital I depend on whether the inefficiency arising from corporate myopia is higher under the frequent or the infrequent regime. When the inefficiency is more (less) pronounced under the frequent regime, the corporate myopia gap decreases (increases) with the capital I . This indicates that decreasing (increasing) the reporting frequency will be less effective

in mitigating the myopia problem as the capital increases. This is because a higher amount of available capital reduces short-sighted operation in both regimes, and the speed of decrease depends on the short-run price efficiencies. When the price efficiency is higher under the frequent regime ($k_{1,F}^* > k_{1,I}^*$), corporate myopia decreases faster under the frequent regime than under the infrequent regime as the available capital increases. Therefore, the gap $k_{1,F}^* - k_{1,I}^*$ decreases with capital I . On the contrary, when the price efficiency is higher under the infrequent regime ($k_{1,F}^* < k_{1,I}^*$), the speed of decrease is higher under the infrequent regime, and the myopia gap increases with I .

Overall, the comparative statics results show the importance of considering information acquisition incentives. For example, when the proportion of informed investors is fixed, switching from the frequent to the infrequent regime will be more effective in mitigating myopia when firms report with high precision. On the contrary, when investors' information acquisition decisions are endogenous, an opposite result obtains: reducing the reporting frequency will be more effective when firms report with low precision.

6 Extensions

6.1 Two trading rounds

The baseline model restricts investors to trade only just after disclosure in the frequent regime. However, investors may have an incentive to trade more aggressively early on when they expect disclosure. Therefore, the value of acquiring information under the frequent regime can increase with an additional trading opportunity. On the contrary, such incentives are less pronounced under the infrequent regime where there is no disclosure. This can potentially affect the overall price informativeness across two periods as well as the manager's operating decisions.

To address this possibility, I consider an extension where investors can trade not just at time 1 but also at time 0. In this setting, investors can also profit from price changes across the two trading periods, influencing expected price efficiencies and information acquisition incentives.

First-round trading occurs at time 0 after the manager makes an operating decision and investors make information acquisition decisions. The supply of the risky asset is x_t at time t and follows $x_t \sim \mathcal{N}(0, \sigma_x^2)$. x_1 and x_2 are independent of each other. The manager's objective function is the weighted average of interim stock prices P_0 , P_1 and P_2 : $\alpha\delta P_0 + \alpha(1 - \delta)P_1 + (1 - \alpha)P_2$, where $\alpha, \delta \in (0, 1)$. α reflects the degree to which the manager cares about interim stock prices, and δ determines the weight on P_0 relative to P_1 .

6.1.1 Exogenous information acquisition

I first analyze the case where a fixed proportion of investors observe conditionally independent signals.

Investor i 's final wealth is:

$$W_i = W + (P_1 - P_0)q_{0i} + (v_1 + v_2 - P_1)q_{1i}. \quad (10)$$

Rearranging (10) gives $W_i = W + (v_1 + v_2 - P_0)q_{0i} + (v_1 + v_2 - P_1)(q_{1i} - q_{0i})$. This equation indicates that the choice of trade timing affects the final wealth. Each investor allocates their demand across two periods to maximize the final wealth.

At time 1, investor i chooses demand that maximizes:

$$\max_{q_{1i}} E \left[-e^{-\gamma(W + (P_1 - P_0)q_{0i} + (v_1 + v_2 - P_1)q_{1i})} \mid \Omega_{1i} \right], \quad (11)$$

where Ω_{1i} indicates the investor i 's information set at time 1.

At time 0, investor i chooses time 0 demand by solving the following problem.

$$\max_{q_{0i}} E \left[\underbrace{\max_{q_{1i}} E \left[-e^{-\gamma(W + (P_1 - P_0)q_{0i} + (v_1 + v_2 - P_1)q_{1i})} \mid \Omega_{1i} \right]}_{\text{Time 1 maximization}} \right]_{\Omega_{0i}} \quad (12)$$

Time 0 maximization

where Ω_{ti} indicates the information set of investor i at time t .

Solving the maximization problem gives:

$$q_{1i}^* = \frac{E[v_1 + v_2 \mid \Omega_{1i}] - P_1}{\gamma \cdot \text{Var}[v_1 + v_2 \mid \Omega_{1i}]} \text{ and} \quad (13)$$

$$q_{0i}^* = \frac{E[(v_1 + v_2 - P_0) - (1 - h_i) \cdot (v_1 + v_2 - P_1) \mid \Omega_{0i}]}{\gamma \cdot \text{Var}[(v_1 + v_2 - P_0) - (1 - h_i) \cdot (v_1 + v_2 - P_1) \mid \Omega_{0i}]} \quad (14)$$

$$\text{where } h_i = -\frac{\text{Cov}[P_1 - P_0, v_1 + v_2 - P_1 \mid \Omega_{0i}]}{\text{Var}[v_1 + v_2 - P_1 \mid \Omega_{0i}]} \in (0, 1)$$

The demand at time 1 takes the same structure as in the baseline model. The only difference is that an investor now observes an additional signal P_0 . In the case of the time 0 demand, the numerator in (14) shows that the time 0 demand decreases with the expected return from time 1 trading ($E[v_1 + v_2 - P_1 \mid \Omega_{0i}]$). The parameter h_i determines the degree to which the investor i considers the expected return at time 1. When h_i is higher, a lower expected return at time 1 is a stronger indication of price appreciation from time 0 to time 1, which increases the investor's incentive to trade early on. Also, the denominator of equation (14) indicates that the demand is normalized by the posterior variance of expected returns and the risk aversion parameter.

Frequent mandatory reporting regime: I conjecture and verify the linear prices, $P_{0,F} = \beta^0 + \beta_v^0 v_1 + \beta_x^0 x_0$ and $P_{1,F} = \beta^1 + \beta_v^1 v_1 + \beta_x^1 x_1 + \beta_m^1 m_0$ where m_0 is the signal from P_0 ($m_0 = \frac{P_0 - \beta_0}{\beta_v^0} = v_1 + \frac{\beta_x^0}{\beta_v^0} x_0$). Solving the financial market equilibrium and deriving the optimal k_1 gives Lemma 5.

Lemma 5. *Under the frequent mandatory reporting regime: When there are two trading periods and a measure n of investors are informed, a manager with $\{\alpha, \delta\}$ chooses*

$$k_{1,F}^* = \frac{\alpha [\delta X_{0,F} + (1 - \delta) X_{1,F}] \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha [\delta X_{0,F} + (1 - \delta) X_{1,F}] + 2(1 - \alpha)}$$

where $X_{t,F}$ is the price efficiency at time t under the frequent regime.

Infrequent mandatory reporting regime: I conjecture and verify the linear prices, $P_{0,I} = \lambda^0 + \lambda_v^0 v_1 + \lambda_x^0 x_0$ and $P_{1,I} = \lambda^1 + \lambda_v^1 v_1 + \lambda_x^1 x_1 + \lambda_m^1 m_0$. Solving for the financial market equilibrium and deriving the optimal k_1 gives Lemma 6.

Lemma 6. *Under the infrequent mandatory reporting regime: When there are two trading periods*

and a measure n of investors are informed, a manager with α and δ chooses

$$k_{1,I}^* = \frac{\alpha [\delta X_{0,I} + (1 - \delta)X_{1,I}] \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha [\delta X_{0,I} + (1 - \delta)X_{1,I}] + 2(1 - \alpha)},$$

where $X_{t,I}$ is the price efficiency at time t .

Comparison of frequent and infrequent regime: Exploiting similarity in expressions in Lemmas 5 and 6, the manager's operating choice on project S under regime $r \in \{I, F\}$ takes the following form.

$$k_{1,r}^* = \frac{\alpha [\delta X_{0,r} + (1 - \delta)X_{1,r}] \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha [\delta X_{0,r} + (1 - \delta)X_{1,r}] + 2(1 - \alpha)} \quad (15)$$

where $X_{t,r}$ indicates price efficiency at time t under regime $r \in \{I, F\}$. Note that the equilibrium myopia level is strictly increasing in the average price efficiency across two trading periods $[\delta X_{0,r} + (1 - \delta)X_{1,r}]$, where the averaging is based on the manager's preference, δ . Therefore, when comparing corporate myopia across regimes, it is sufficient to compare the average price informativeness under the two regimes. The following proposition compares the myopia level under the two regimes.

Proposition 5. *When there are two trading periods and a measure n of investors are informed, corporate myopia is always more pronounced under the frequent than under the infrequent regime.*

Proposition 5 indicates that given fixed n , corporate myopia is more pronounced under the frequent regime even when there is an additional trading round. The intuition behind this result is that more information about short-term firm performance is incorporated into the price at both trading periods under the frequent than the infrequent regime. In the second trading period, the same intuition as in the baseline model applies. First, increasing the reporting frequency reduces price informativeness due to the lower weight placed on information from informed trading. However, it also increases the information contained in P_1 via firm disclosure. Overall, the second effect dominates, and the price efficiency is higher under the frequent regime. In the case of the first trading round, time 1 price efficiency affects the informed investors' time 0 demand quantities in two ways. First, higher price informativeness at time 1 decreases the expected return at time

1, which increases the numerator of informed investor's time 0 demand. At the same time, higher price efficiency increases h_i , or an investor's tendency to take into account the time 1 expected return when choosing time 0 trading quantity. Together, these effects lead to a higher time 0 price efficiency under the frequent compared to the infrequent regime. Overall, the result indicates that with exogenous n , the prediction in Gigler et al. (2014) that myopia is more pronounced under the frequent than the infrequent regime still holds with dynamic trading.

6.1.2 Endogenous information acquisition

Next, I endogenize the proportion of informed investors and examine its effect on myopic operating decisions under the two regimes. As in the baseline model, investors pay a fixed cost of c to observe a private signal. I first compute the ex-ante expected utility of informed and uninformed investors in Lemma 7.

Lemma 7. *An informed investor's expected utility is:*

$$EU_I^r = e^{-\gamma(W-c)} \sqrt{\frac{\text{Var}[(v_1 + v_2 - P_0) - (1 - h_I^r)(v_1 + v_2 - P_1)|\Omega_{0I}] \cdot \text{Var}[v_1 + v_2 - P_1|\Omega_{1I}]}{\text{Var}[v_1 + v_2 - P_1] \cdot \text{Var}[P_1 - P_0] - \text{Cov}^2[P_1 - P_0, v_1 + v_2 - P_1]}}, \quad (16)$$

An uninformed investor's expected utility is:

$$EU_U^r = e^{-\gamma W} \sqrt{\frac{\text{Var}[(v_1 + v_2 - P_0) - (1 - h_U^r)(v_1 + v_2 - P_1)|\Omega_{0U}] \cdot \text{Var}[v_1 + v_2 - P_1|\Omega_{1U}]}{\text{Var}[v_1 + v_2 - P_1] \cdot \text{Var}[P_1 - P_0] - \text{Cov}^2[P_1 - P_0, v_1 + v_2 - P_1]}}, \quad (17)$$

where $r \in \{I, F\}$ indicates a reporting regime and $h_i^r = -\frac{\text{Cov}[P_1 - P_0, v_1 + v_2 - P_1|\Omega_{0i}]}{\text{Var}[v_1 + v_2 - P_1|\Omega_{0i}]}$, $i \in \{I, U\}$.

At the beginning of the game, an investor chooses to acquire information only when the incremental expected utility of obtaining information exceeds the cost c .

Lemma 7 shows that the ex-ante expected utility of acquiring information for investor $i \in \{I, U\}$ decreases with the posterior variances of time 0 trading ($\text{Var}[(v_1 + v_2 - P_0) - (1 - h_i)(v_1 +$

$v_2 - P_1|\Omega_{0i}]$) and time 1 trading ($Var[v_1 + v_2 - P_1|\Omega_{1i}]$), where I (U) indicates an informed (uninformed) trader. This result is intuitive since higher variance at the time of trading given one's information set decreases the expected profit of investors.

Under the infrequent regime, $n_I \in (0, 1)$ is an equilibrium when

$$EU_I^I(n_I, \sigma_\eta^2) = EU_U^I(n_I, \sigma_\eta^2 = \infty). \quad (18)$$

However, n_I is only implicitly defined in the above equation, and therefore comparing price efficiency by substituting the equilibrium n_I is not tractable. The same applies to the frequent regime, and $n_F \in (0, 1)$ is an equilibrium when

$$EU_I^F(n_F, \sigma_\eta^2) = EU_U^F(n_F, \sigma_\eta^2 = \infty). \quad (19)$$

Another difference from the baseline model is that the expected utility of acquiring information may not always monotonically decrease with n . The equilibrium n depends on the curvature of the value of information, which depends on the parameter values. Therefore, deriving equilibrium n in a closed-form is intractable.¹⁴ Due to these concerns, I use a numerical example to examine whether the baseline results carry over to this extension.

Comparison of frequent and infrequent regime: I first compare the price efficiencies under the two reporting regimes across trading periods in Figures 4 and 5. In Figure 4, the x- and y-axes represent the cost of information acquisition and the price efficiency at time 0, respectively. If c decreases below a certain threshold, the short-term price efficiency increases from zero to a positive value as investors start to gather information. Note that this threshold is higher under the infrequent regime, which indicates that investors start acquiring information at a higher cost under a less frequent regime. If c further decreases, then there exists a point where all investors become informed, and there is no additional increase in price efficiency. Note that this point is also greater under the infrequent regime. In Figure 5, the y-axis represents the price efficiency at time 1. As in

¹⁴More specifically, unlike in the baseline model where the value of information $\frac{EU_U(n, \sigma_\eta^2 = \infty)}{EU_I(n, \sigma_\eta^2)}$ is strictly decreasing in n , the value of information under the dynamic trading model is not always monotonic in n .

Figure 4: Comparison of time 0 price efficiency

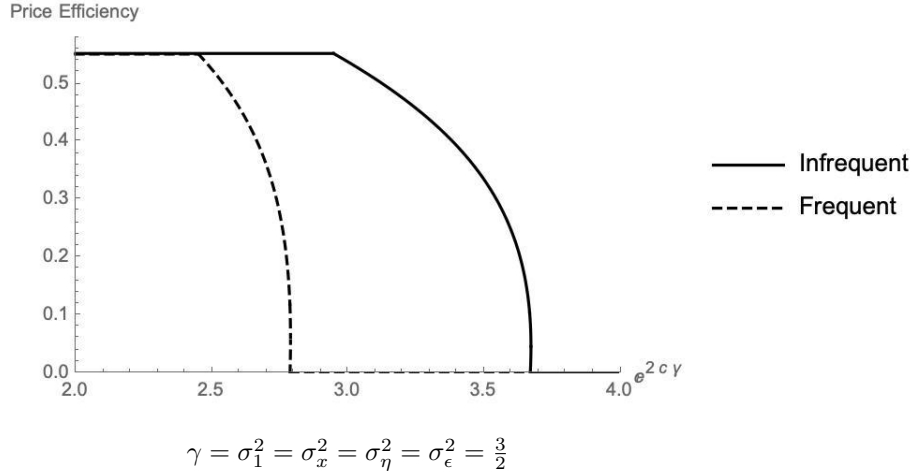


Figure 5: Comparison of time 1 price efficiency

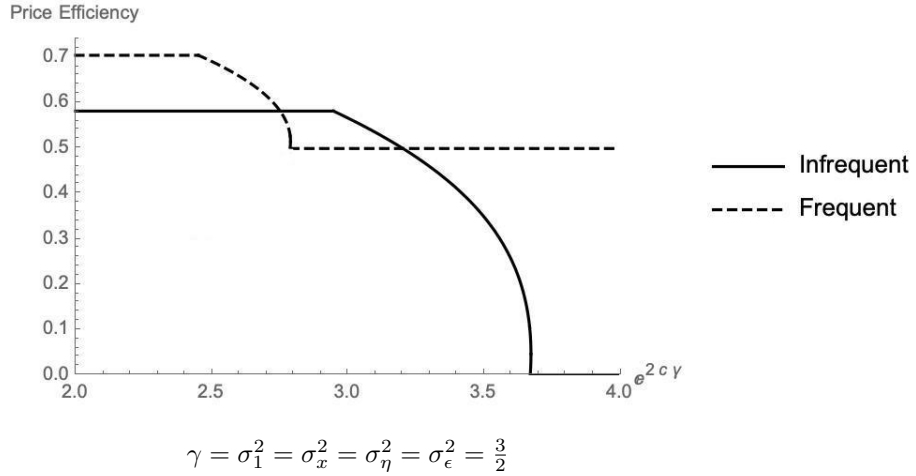
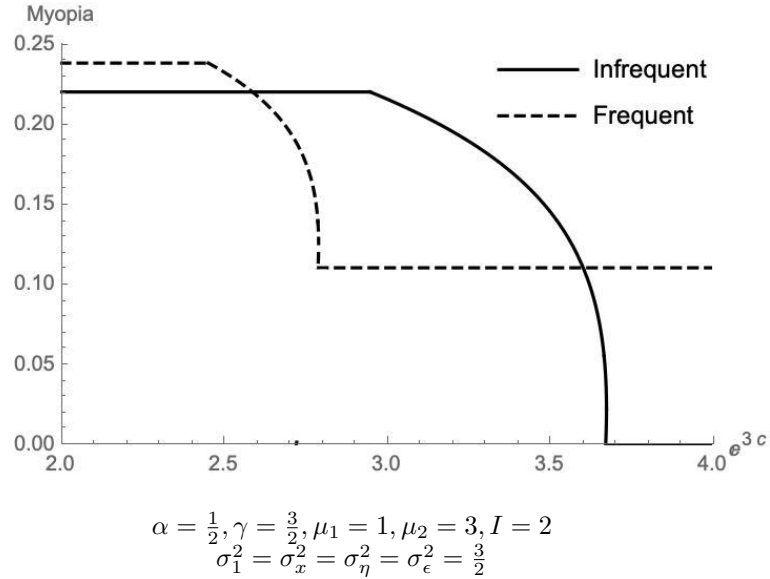


Figure 4, the graph illustrates that the percentage of informed investors is weakly greater under the infrequent regime, given an information acquisition cost of c .

Both Figures 4 and 5 indicate that there exists an interval of c where the price efficiency is higher under the infrequent regime than that under the frequent regime, consistent with the baseline model. This is because investors have stronger information acquisition incentives under the infrequent regime, even with an additional trading round.

Figure 6 compares the myopia level under the two regimes as the cost of information acquisition changes. The graph shows that there exists an interval of c where corporate myopia is higher under

Figure 6: Comparison of corporate myopia



the infrequent regime, which occurs when the average price efficiency across times 0 and 1 is higher under the infrequent regime. The result from the numerical example is summarized in Proposition 6.

Proposition 6. *When there are two trading periods, and information acquisition is endogenous, it is possible that corporate myopia is higher under the infrequent than under the frequent regime.*

Overall, the numerical example with dynamic trading confirms that even when investors are allowed to trade before disclosure, there still exist cases where short-termism is higher in the infrequent regime than in the frequent regime as long as investors' information acquisition is endogenously determined.

6.2 Different types of information

In the baseline model, investors can only gather information about short-term firm performance. However, allowing investors to learn about other types of information can also affect the price efficiency and thus operating decisions. To address this possibility, this section considers an extension where long-term performance is noisy, and investors can choose to acquire a noisy signal on either short-term or long-term firm performance. I assume that an investor is always

informed and possesses a private signal either about short-term or long-term performance. Let the firm's long-term performance be $v_2 = y_2 + \delta_2$, where y_2 is the long-term payoff from operations and $\delta_2 \sim \mathcal{N}(0, \sigma_2^2)$. If investor i chooses to acquire the short-term signal, then he/she observes $s_{1i} = v_1 + \eta_i$, where $\eta_i \sim \mathcal{N}(0, \sigma_\eta^2)$. If investor i chooses to acquire the long-term signal, then the investor observes $s_{2i} = v_2 + \zeta_i$, where $\zeta_i \sim \mathcal{N}(0, \sigma_\zeta^2)$. Investors' signals are conditionally independent, and η_i 's and ζ_i 's are mutually independent. I denote \bar{n} as the proportion of investors who are informed about short-term firm performance and $1 - \bar{n}$ as the proportion of investors informed about long-term firm performance.

6.2.1 Exogenous information acquisition

Infrequent mandatory reporting regime: Since the cumulative payoff is reported at time 2, the price is simply the realized firm value, $P_{2,I} = v_1 + v_2$. For $P_{1,I}$, I assume and verify the linear conjecture, $P_{1,I} = \lambda_0 + \lambda_1 v_1 + \lambda_2 v_2 + \lambda_x x$. Now that the investors observe either a short-term or long-term signal, information on both short- and long-term performance is incorporated into the price. As the price becomes more informative about short- (long-) run performance, myopia increases (decreases).¹⁵

Investor i who observes the short-term signal s_{1i} chooses the share demand quantity $D_{1i} = \frac{E[v_1+v_2|s_{1i}, P_1] - P_1}{\gamma \text{Var}[v_1+v_2|s_{1i}, P_1]}$. Likewise, investor j who observes the long-term signal s_{2j} chooses the demand quantity $D_{2j} = \frac{E[v_1+v_2|s_{2j}, P_1] - P_1}{\gamma \text{Var}[v_1+v_2|s_{2j}, P_1]}$.

Frequent mandatory reporting regime: Similar to the infrequent regime, $P_{2,F} = v_1 + v_2$. For $P_{1,F}$, I conjecture and verify the linear price equation, $P_{1,F} = \beta_0 + \beta_1 v_1 + \beta_2 v_2 + \beta_e e_1 + \beta_x x$. With firm disclosure, information from e_1 is also incorporated into the price. I derive the equilibrium demand for both types of informed investors and apply the market clearing condition.

Since the price coefficients are only implicitly defined, I use a numerical example to compare the price efficiencies and thus corporate myopia under the two regimes. I assume that $\sigma_1^2 = 1$, $\sigma_2^2 =$

¹⁵In a related study by Edmans (2009), the author finds that informed block-holder's exit can mitigate corporate short-termism problem when the informed traders gathers information about long-run fundamental value.

2, $\sigma_\eta^2 = 1$, $\sigma_\epsilon^2 = \frac{1}{10}$, $\sigma_\zeta^2 = 1$ and $\sigma_x^2 = 1$. Also, $I = 2$, $\mu_1 = 1$, $\mu_2 = 2$, $\alpha = \frac{1}{2}$, and $\gamma = 1$.

Comparison of corporate myopia under the two regimes: The numerical example gives the following equilibrium prices under the two regimes.

$$P_{1,I} = \lambda_0 + \underbrace{\lambda_1}_{0.228} v_1 + \underbrace{\lambda_2}_{0.435} v_2 + \underbrace{\lambda_x}_{-2.2} x \quad (20)$$

$$P_{1,F} = \beta_0 + \underbrace{\beta_1}_{0.309} v_1 + \underbrace{\beta_2}_{0.576} v_2 + \underbrace{\beta_e}_{0.806} e_1 + \underbrace{\beta_x}_{-1.319} x \quad (21)$$

Note that the equilibrium short-term operating input takes the following form.

$$k_1^* = \frac{\alpha(X_1\mu_1 + X_2(I - \mu_2)) + (1 - \alpha)(I - \mu_2 + \mu_1)}{2(1 - \alpha) + \alpha(X_1 + X_2)}, \quad (22)$$

where X_1 and X_2 indicate the price informativeness on short- and long-run firm value respectively.

Plugging in the equilibrium price coefficients under the two regimes and comparing gives the following result.

$$k_I^* = 0.461134 < k_F^* = 0.573109. \quad (23)$$

As in the baseline model, myopia is more pronounced under the frequent than under the infrequent regime with exogenous information acquisition.

6.2.2 Endogenous information acquisition

In this section, I endogenize the proportion of informed investors that observe the short-term signal, \bar{n} . I assume that the investor pays $c_1(c_2)$ to acquire $s_{1i}(s_{2i})$. I assume that $c_2 > c_1 > 0$. Also, to ensure that all investors become informed in equilibrium, the model assumes that c_1 is sufficiently small such that $EU_1(\bar{n} = 1) > c_1$. The lemma below characterizes the equilibrium proportion of investors that are informed about v_1 .

Lemma 8. *The equilibrium proportion of informed investors who are informed about short-term firm value under the regime $r \in \{I, F\}$ (\bar{n}_r) is characterized as below.*

1) When $EU_1^r(\bar{n}_r = 0) < EU_2^r(\bar{n}_r = 0)$, $\bar{n}_r = 0$.

2) When $EU_1^r(\bar{n}_r = 1) > EU_2^r(\bar{n}_r = 1)$, $\bar{n}_r = 1$.

3) Otherwise, $\bar{n}_r \in (0, 1)$ satisfies $EU_1^r(\bar{n}_r) = EU_2^r(\bar{n}_r)$,

where $r = I(F)$ indicates the infrequent (frequent) reporting regime, and $EU_{1(2)}^r$ represents the expected utility of an investor who observes short-(long-) term signal.

Comparison using numerical examples: Again, I rely on a numerical example due to tractability issues. I assume that $\sigma_1^2 = 1, \sigma_2^2 = 2, \sigma_\eta^2 = 1, \sigma_\epsilon^2 = \frac{1}{10}, \sigma_\zeta^2 = 1$ and $\sigma_x^2 = 1$. Also, $I = 2, \mu_1 = 1, \mu_2 = 2, \alpha = \frac{1}{2}, \gamma = 1$, and $c_1 = 1$ and $c_2 = 1.25$. Since characterizing the coefficients λ 's and β 's with respect to \bar{n} is intractable, I derive the equilibrium price coefficients by fixing \bar{n} first and then verifying that the given \bar{n} indeed satisfies the information acquisition equilibrium.

As in the exogenous information case, I assume and verify the linear price conjecture after deriving an investor's optimal demand and then applying market clearing. In equilibrium:

$$\bar{n}_I = 1 \quad (24)$$

$$P_{1,I} = \lambda_0 + \underbrace{\lambda_1}_{0.510} v_1 + \underbrace{\lambda_2}_0 v_2 + \underbrace{\lambda_x}_{-2.587} x \quad (25)$$

$$\bar{n}_F = 0 \quad (26)$$

$$P_{1,F} = \beta_0 + \underbrace{\beta_1}_0 v_1 + \underbrace{\beta_2}_{0.772} v_2 + \underbrace{\beta_e}_{0.909} e_1 + \underbrace{\beta_x}_{-0.926} x \quad (27)$$

I plug in the equilibrium \bar{n} as well as the equilibrium price coefficients to obtain myopic operating choice under the two regimes ($k_{1,I}^*$ and $k_{1,F}^*$):

$$k_I^* = 0.602 > k_F^* = 0.518. \quad (28)$$

Proposition 7. *When investors can acquire either short- or long-term information, and when information acquisition is endogenous, it is possible that myopia is higher under the infrequent than under the frequent regime.*

The above comparison between the frequent and the infrequent reporting regime indicates that

once I endogenize information acquisition choices, investors are more (less) likely to acquire long- (short-) term information under the frequent regime (i.e., $\bar{n}_I > \bar{n}_F$). Thus, there exist cases where myopia is more pronounced under the infrequent regime than under the frequent regime.

6.3 Alternative market microstructure

Next, I examine whether the results hold under a Kyle (1985) setup. Unlike in the setting in Grossman and Stiglitz (1980) where an individual investor is infinitesimally small, the market microstructure in this extension features an imperfectly competitive market. Thus, an investor's trading has a price impact. There are three risk-neutral market participants besides the manager: a market maker, an informed investor, and noise traders. The investor submits market orders to the market maker. The primary differences with the baseline model are that the investor is risk-neutral, and the trading has a price impact.

I find that in a Kyle (1985) setting, corporate myopia increases with mandatory reporting frequency under exogenous information acquisition. However, once I endogenize the information acquisition decision, the level of inefficient short-term operation can decrease with reporting frequency when the firm's reporting quality is low. Overall, the main results in Proposition 1 and Proposition 3 are sustained in this alternative setup. The details of the results are included in Appendix B.

6.4 Voluntary disclosure

Finally, I incorporate a firm's voluntary disclosure decision. The manager can disclose a short-term signal e_1 voluntarily at a cost $c_v > 0$ under the infrequent regime.¹⁶ Since the signal is always disclosed under the frequent reporting regime, voluntary disclosure is redundant there.¹⁷ Due to tractability issues arising from nonlinear prices, I examine the impact of voluntary disclosure

¹⁶The voluntary disclosure cost can be interpreted as the manager's personal cost (e.g., time, resources) required to prepare voluntary disclosure.

¹⁷I assume that the cost of mandatory disclosure (c_m) is equal to zero to maintain consistency with the prior analysis. However, a positive mandatory disclosure cost does not affect the result.

under the Kyle (1985) setting. Intuitively, a higher voluntary disclosure cost decreases the price informativeness under the infrequent regime when a fixed number of investors are informed. When investors can choose to acquire information, a higher voluntary disclosure cost increases the investor's information acquisition incentive, which increases price informativeness about short-term performance. Together, the effect of changing the voluntary disclosure cost on corporate myopia is qualitatively the same as that of changing the mandatory reporting frequency. This is because a firm's voluntary and mandatory disclosure has the same information and the firm's signal has a substitutive relationship with the informed trader's signal. The details of the results are included in Appendix B.

7 Discussion

In this section, I discuss the main results and their implications for the empirical literature. First, this study highlights the importance of examining the overall information environment when testing the effect of mandatory reporting frequency on corporate myopia. A previous analytical study by Gigler et al. (2014) shows that reducing reporting frequency can completely mitigate the myopia problem. However, this paper shows that with additional information sources (e.g., informed trading), information about short-term firm value can still get incorporated into the interim stock price, which induces myopia even under the infrequent regime. With endogenous information acquisition, the myopia level can be more pronounced under the infrequent regime rather than the frequent regime when the mandatory reporting noise is sufficiently high. This indicates that the mixed findings in prior studies that examine the relationship between reporting frequency and myopia using different countries (e.g., Ernstberger et al. (2017), Fu et al. (2020), Kajüter et al. (2019), Kraft et al. (2017), Nallareddy et al. (2017)) could be due to differences in quarterly reporting quality, and the presence of informed traders.

If quarterly reporting quality differs across countries, changing the mandatory reporting frequency can have different effects on myopia. For instance, unlike in the U.S., where firms

are required to disclose quarterly financial statements, the EU gives more flexibility regarding the content of mandated quarterly reporting. Consequently, some companies only issued qualitative reports without incorporating quantitative information such as earnings or sales. Ernstberger et al. (2017) find that between the years 2005 and 2014, only 8.9 percent of the quarterly reports included financial statements, and 51.4 percent reported quarterly earnings numbers. Also, the authors document that the percentage of firms that issued quantitative earnings signals was second-lowest in the U.K. among the European countries included in their sample.¹⁸ Suppose this indicates that the quarterly reporting quality was lower in the U.K. compared to other European countries that mandated quarterly reporting. In that case, the result in Propositions 3 indicates that switching from semi-annual to quarterly reporting may not mitigate the short-termism problem in the U.K. and can even exacerbate the corporate myopia problem depending on the information acquisition cost.

Second, the comparative statics results provide empirically testable hypotheses based on firm-specific characteristics. For example, Proposition 4 shows that the gap in myopia under the frequent and the infrequent regime increases with mandatory reporting noise. Hence, when the short-termism problem is more pronounced under the frequent regime, switching from semi-annual to quarterly reporting will be more effective in mitigating myopia for firms with lower reporting quality. Nallareddy et al. (2017) find that the flexibility in quarterly reporting for European firms leads to higher variance in reporting quality, which indicates that researchers should be cautious when testing the average effect. That is, variation in firm-specific reporting quality can lead to insignificant findings. Therefore, future papers should condition on firm-specific characteristics and examine whether the change in reporting regime affects firms differentially. Also, Proposition 4 shows that a firm's capital can also affect the effectiveness of reducing the mandatory reporting frequency. Overall, the results in Proposition 4 emphasize the importance of considering firm-specific characteristics when examining the effect of changing the reporting frequency on the

¹⁸Also, Nallareddy et al. (2017) find that, between the years 2007 and 2009, only 5 percent of the U.K. firms that mandatorily switched from semi-annual to quarterly reporting practices included quantitative information in their reporting.

short-termism problem.

Finally, the results in this paper can be generalized to alternative information channels such as analyst reports and information spillover from peer firm disclosure that can also interact with mandatory disclosure. I expect similar results to hold as long as the information from alternative sources has a substitutive relationship with the firm's mandatory disclosure content. If the information is complementary to firm disclosure, the disclosure will encourage more information acquisition. However, its effect on myopia will depend on the nature of the information. For instance, if the complementary information is about long-term firm performance, this will mitigate the myopia problem. On the contrary, if the complementary signal concerns short-term firm performance, then more information acquisition will exacerbate the short-termism problem.

8 Conclusion

This study examines the relationship between mandatory reporting frequency and corporate myopia in the presence of alternative information channels. I find that inefficient corporate myopia is sustained even when the mandatory reporting frequency is low. In addition, I provide conditions for a negative relation between mandatory reporting frequency and myopic operating decisions. When the number of informed investors is determined endogenously, switching to a less frequent reporting regime can exacerbate the myopia problem when mandatory disclosure quality is sufficiently low.

This paper offers practical implications for regulators who are debating the benefits and costs of changing reporting frequency. Among potential benefits and costs, this study focuses on the cost of short-termism. The results show that increasing the reporting frequency may not always lead to higher corporate myopia. Moreover, the effectiveness of mitigating short-termism problems depends on both market-related and firm-specific factors. Hence, regulators should carefully examine capital market features such as information acquisition incentives and the firm's reporting quality when evaluating the total cost of increasing reporting frequency.

Appendix A: Proofs

Proof of Lemma 1.

I derive the informed and uninformed investors' demand function.

the CARA-normal setup implies that

$$D_i^F(e_1, s_i, P_{1,F}) = \frac{E(v_1 + v_2 | e_1, s_i, P_{1,F}) - P_{1,F}}{\gamma \text{Var}(v_1 + v_2 | e_1, s_i, P_{1,F})} \quad (29)$$

$$D_U^F(e_1, P_{1,F}) = \frac{E(v_1 + v_2 | e_1, P_{1,F}) - P_{1,F}}{\gamma \text{Var}(v_1 + v_2 | e_1, P_{1,F})}, \quad (30)$$

where D_i^F, D_U^F each indicates informed investor i 's and uninformed investors' demand quantities under the frequent regime.

The prices are determined so that it satisfies the market clearing condition.

$$\int_0^n D_i^F(e_1, s_i, P_{1,F}) di + (1 - n) D_U^F(e_1, P_{1,F}) = x \quad (31)$$

Solving for the market clearing condition gives the following price equation at time 1.

$$P_{1,F} = \underbrace{\frac{\frac{1}{\sigma_1^2} E[v_1]}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\beta_v}{\beta_x}\right)^2 + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}}}_{\beta} + E[v_2] + \underbrace{\frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\beta_v}{\beta_x}\right)^2}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\beta_v}{\beta_x}\right)^2 + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}}}_{\beta_v} v_1$$

$$+ \underbrace{\frac{\frac{1}{\sigma_\varepsilon^2}}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\beta_v}{\beta_x}\right)^2 + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}}}_{\beta_e} e_1 + \underbrace{\frac{\frac{1}{\sigma_x^2} \frac{\beta_v}{\beta_x} - \gamma}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\beta_v}{\beta_x}\right)^2 + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}}}_{\beta_x} x, \quad (32)$$

where $\frac{\beta_v}{\beta_x} = -\frac{n}{\gamma \sigma_\eta^2}$

Given the equilibrium prices, the manager chooses k_1 that maximizes

$$k_1, k_2 \in \arg \max \alpha E[P_{1,F}] + (1 - \alpha) E[P_{2,F}] \quad (33)$$

$$\text{s.t. } 0 \leq k_1 \leq I \quad (34)$$

$$0 \leq k_2 \leq I - k_1. \quad (35)$$

Solving for the above maximization gives:

$$k_{1,F}^* = \min \left\{ \frac{\alpha X_F \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha X_F + 2(1 - \alpha)}, I \right\} \quad (36)$$

where $X_F = \frac{\frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_\varepsilon^2}}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right) + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}}$. Note that $\frac{\alpha X_F \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha X_F + 2(1 - \alpha)} < I$ under the assumption $0 < \mu_1 < \mu_2 - \mu_1 \leq I < \mu_1 + \mu_2$.

Rearranging $\frac{\alpha X_F \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha X_F + 2(1 - \alpha)} < I$ gives:

$$\alpha X_F \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1) < I(\alpha X_F + 2(1 - \alpha)) \quad (37)$$

$$\iff -(I - \mu_1) \cdot (\alpha X_F + (1 - \alpha)) < \mu_2(1 - \alpha) \quad (38)$$

(38) is always satisfied under the parameter constraint $0 < \mu_1 < \mu_2 - \mu_1 \leq I < \mu_1 + \mu_2$ since the left-hand side of (38) is negative, and the right-hand side is positive. Therefore, $k_{1,F}^* = \frac{\alpha X_F \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha X_F + 2(1 - \alpha)}$

Note that the equilibrium short-term capital input is strictly increasing in price informativeness of P_1 about short-term firm performance (X_F), or $\frac{\partial k_{1,F}^*}{\partial X_F} > 0$. Therefore, $X_F \geq 0$ indicates $k_{1,F}^* \geq k_1^B$.

Proof of Lemma 2.

The CARA-normal setup implies that

$$D_i^I(s_i, P_{1,I}) = \frac{E(v_1 + v_2 | s_i, P_{1,I}) - P_{1,I}}{\gamma \text{Var}(v_1 + v_2 | s_i, P_{1,I})} \quad (39)$$

$$D_U^I(P_{1,I}) = \frac{E(v_1 + v_2 | P_{1,I}) - P_{1,I}}{\gamma \text{Var}(v_1 + v_2 | P_{1,I})}, \quad (40)$$

where D_i^I and D_U^I each indicates informed investors i 's and uninformed investors' demand quantities under the infrequent regime.

Given random supply of the risky asset (x), market clearing condition indicates:

$$P_{1,I} = \underbrace{\frac{\frac{1}{\sigma_1^2} E[v_1]}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\lambda_v}{\lambda_x}\right)^2 + \frac{1}{\sigma_1^2}}}_{\lambda} + E[v_2] + \underbrace{\frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\lambda_v}{\lambda_x}\right)^2}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\lambda_v}{\lambda_x}\right)^2 + \frac{1}{\sigma_1^2}}}_{\lambda_v} v_1 + \underbrace{\frac{\frac{1}{\sigma_x^2} \frac{\lambda_v}{\lambda_x} - \gamma}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\lambda_v}{\lambda_x}\right)^2 + \frac{1}{\sigma_1^2}}}_{\lambda_x} x, \quad (41)$$

where $\frac{\lambda_v}{\lambda_x} = -\frac{n}{\gamma\sigma_\eta^2}$

Given the equilibrium prices, the manager chooses k_1 that maximizes

$$\max_{k_1} \alpha E[P_{1,I}] + (1 - \alpha) E[P_{2,I}] \quad (42)$$

$$\text{s.t. } 0 \leq k_1 \leq I \quad (43)$$

$$0 \leq k_2 \leq I - k_1. \quad (44)$$

Solving for the maximization problem gives:

$$k_{1,I}^* = \min \left\{ \frac{\alpha X_I \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha X_I + 2(1 - \alpha)}, I \right\}, \quad (45)$$

where $X_I = \frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma\sigma_\eta^2}\right)^2}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_1^2}}$. Under the parameter constraint $\mu_2 - \mu_1 \leq I < \mu_1 + \mu_2$ and $2\mu_1 < \mu_2$, $\frac{\alpha X_I \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha X_I + 2(1 - \alpha)} < I$ and $k_{1,I}^* = \frac{\alpha X_I \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha X_I + 2(1 - \alpha)}$.

Note that the equilibrium short-term capital input is strictly increasing in price informativeness of P_1 about short-term firm performance (X_I), or $\frac{\partial k_{1,I}^*}{\partial X_I} > 0$. Therefore, $k_{1,I}^* \geq k_1^B$ since $X_I \geq 0$.

Proof of Proposition 1.

From Lemma 1 and Lemma 2, note that the equilibrium capital spent on the short-term project k_1^* takes the following form, where X is the price efficiency at time 1:

$$k_1^* = \frac{\alpha(X)\mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha(X) + 2(1 - \alpha)}. \quad (46)$$

Also, k_1^* is increasing in the time 1 price efficiency X .

$$\frac{\partial k_1^*}{\partial X} = \frac{\alpha(1-\alpha)(\mu_2 + \mu_1 - I)}{(\alpha(X) + 2(1-\alpha))^2} > 0. \quad (47)$$

I examine time 1 price efficiency under the frequent and the infrequent regime to compare $k_{1,F}^*$ and $k_{1,I}^*$.

Comparing $X_I = \frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma\sigma_\eta^2}\right)^2}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_1^2}}$ and $X_F = \frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_\epsilon^2}}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_\epsilon^2}}$, $X_F > X_I$ holds given a fixed proportion of informed investors (n).

Proof of Proposition 2

Taking FOC of $k_{1,F}^* - k_{1,I}^*$ with respect to $n, \sigma_\eta^2, \sigma_\epsilon^2$ and I gives the following results.

$$\frac{\partial(k_{1,F}^* - k_{1,I}^*)}{\partial n} = -\frac{(\alpha-2)(\alpha-1)\alpha\gamma^4(I-\mu_1-\mu_2)\sigma_1^4\sigma_\eta^8\sigma_x^4(2n+\gamma^2\sigma_\eta^2\sigma_x^2)A_1}{D_1 \cdot D_2} < 0 \quad (48)$$

$$\frac{\partial(k_{1,F}^* - k_{1,I}^*)}{\partial \sigma_\eta^2} = \frac{(\alpha-2)(\alpha-1)\alpha\gamma^4 n(I-\mu_1-\mu_2)\sigma_1^4\sigma_\eta^6\sigma_x^4(2n+\gamma^2\sigma_\eta^2\sigma_x^2) \cdot A_1}{D_1 \cdot D_2} > 0 \quad (49)$$

$$\begin{aligned} \frac{\partial(k_{1,F}^* - k_{1,I}^*)}{\partial \sigma_\epsilon^2} &= -\frac{(\alpha-1)\alpha\gamma^4(I-\mu_1-\mu_2)\sigma_1^2\sigma_\eta^8\sigma_x^4}{((\alpha-2)\sigma_1^2(n\sigma_\epsilon^2(n+\gamma^2\sigma_\eta^2\sigma_x^2)+\gamma^2(\sigma_\eta^2)^2\sigma_x^2)+2(\alpha-1)\gamma^2(\sigma_\eta^2)^2\sigma_x^2\sigma_\epsilon^2)^2} < 0 \end{aligned} \quad (50)$$

$$\begin{aligned} \frac{\partial}{\partial \sigma_1^2}(k_{1,F}^* - k_{1,I}^*) &= \frac{\partial k_{1,F}^*}{\partial X_F} \cdot \left(\frac{\partial X_I}{\partial \sigma_1^2} - \frac{\partial X_F}{\partial \sigma_1^2} \right) \\ &= \underbrace{\frac{\partial k_{1,F}^*}{\partial X_F}}_{=\frac{\partial k_{1,I}^*}{\partial X_I}} \cdot \frac{1}{\sigma_1^4} \left(\frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_\epsilon^2}}{\left(\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_\epsilon^2} + \frac{1}{\sigma_1^2}\right)^2} - \frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma\sigma_\eta^2}\right)^2}{\left(\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_1^2}\right)^2} \right) \\ &> (<)0 \text{ when } \frac{1}{\sigma_1^2} > (<) \frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_\epsilon^2} \end{aligned} \quad (51)$$

$$\frac{\partial}{\partial I}(k_{1,F}^* - k_{1,I}^*) = -\frac{(\alpha-1)\alpha(X_I - X_F)}{(\alpha(X_I - 2) + 2)(\alpha(X_F - 2) + 2)} < 0 \quad (52)$$

where

$$A_1 = ((\alpha-2)\sigma_1^2(2n\sigma_\epsilon^2(n+\gamma^2\sigma_\eta^2\sigma_x^2)+\gamma^2(\sigma_\eta^2)^2\sigma_x^2)+4(\alpha-1)\gamma^2(\sigma_\eta^2)^2\sigma_x^2\sigma_\epsilon^2) < 0,$$

$$D_1 = ((\alpha-2)n\sigma_1^2(n+\gamma^2\sigma_\eta^2\sigma_x^2)+2(\alpha-1)\gamma^2(\sigma_\eta^2)^2\sigma_x^2)^2 > 0,$$

$$\text{and } D_2 = ((\alpha-2)\sigma_1^2(n\sigma_\epsilon^2(n+\gamma^2\sigma_\eta^2\sigma_x^2)+\gamma^2(\sigma_\eta^2)^2\sigma_x^2)+2(\alpha-1)\gamma^2(\sigma_\eta^2)^2\sigma_x^2\sigma_\epsilon^2)^2 > 0.$$

The result in (51) can be derived by analyzing how $\frac{\partial X_F}{\partial \sigma_1^2}$ changes with $\frac{1}{\sigma_\epsilon^2}$. Note that $\frac{\partial X_F}{\partial \sigma_1^2} = \frac{\partial X_I}{\partial \sigma_1^2}$, when $\sigma_\epsilon^2 = \infty$.

$$\begin{aligned} \frac{\partial}{\partial \frac{1}{\sigma_\epsilon^2}} \left(\frac{\partial X_F}{\partial \sigma_1^2} \right) &= \frac{1}{\sigma_1^4} \cdot \frac{\partial}{\partial \frac{1}{\sigma_\epsilon^2}} \left(\frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_\epsilon^2}}{\left(\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_\epsilon^2} + \frac{1}{\sigma_1^2} \right)^2} \right) \\ &= \frac{\left(\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_\epsilon^2} + \frac{1}{\sigma_1^2} \right) \left(\frac{1}{\sigma_1^2} - \left(\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_\epsilon^2} \right) \right)}{\left(\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_\epsilon^2} + \frac{1}{\sigma_1^2} \right)^4} \end{aligned} \quad (53)$$

$$> (<)0 \text{ when } \frac{1}{\sigma_1^2} - \left(\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_\epsilon^2} \right) > (<)0 \quad (54)$$

Proof of Lemmas 3 and 4

Lemma 4. The informed investor's expected utility under the infrequent regime is characterized as in the following lemma. The ex-ante expected utility can be calculated as below.

Using certainty equivalent, an investor i 's expected utility of acquiring information at time 0 is:

$$E[U_i(W + D_i(v_1 + v_2 - P_1) - c)] = E_{P_1, s_i} [E_{v_1, v_2} [U_j(W + D_i(v_1 + v_2 - P_1) - c) | P_1, s_i]] \quad (55)$$

$$= E_{P_1, s_i} \left[-\exp \left\{ -\gamma(W - c) + \frac{1}{2} \frac{(E[v_1 + v_2 | P_1, s_i - P_1])^2}{\text{Var}[v_1 + v_2 | P_1, s_i]} \right\} \right] \quad (56)$$

$$= -\exp \{ -\gamma(W - c) \} \int_{P_1} \int_{s_i} \exp \left\{ \frac{1}{2} \frac{(E[v_1 + v_2 | P_1, s_i - P_1])^2}{\text{Var}[v_1 + v_2 | P_1, s_i]} \right\} f(P_1, s_i) ds_i dP_1, \quad (57)$$

where $f(P_1, s_i)$ is the joint p.d.f of P_1 and s_i :

$$\begin{pmatrix} P_1 \\ s_i \end{pmatrix} \sim \mathcal{N} \left(\begin{pmatrix} E[P_1] \\ E[v_1] \end{pmatrix}, \begin{pmatrix} \text{Var}[P_1] & \text{Cov}[P_1, s_i] \\ \text{Cov}[P_1, s_i] & \text{Var}[s_i] \end{pmatrix} \right).$$

Simplifying (57) gives individual investor's ex ante expected utility of acquiring information:

$$EU_i(\hat{\sigma}_\eta^2, \hat{c}, n) = -e^{\gamma \hat{c} - \gamma W} \sqrt{\frac{\frac{1}{\sigma_1^2}}{\left(\frac{\sigma_x^2}{\gamma \sigma_1^2} \right)^2 + \frac{\sigma_x^2}{\sigma_1^2} \left(\frac{n}{\gamma^2 \sigma_\eta^2} + \sigma_x^2 \right)^2}} \sqrt{\text{Var}[v_1 + v_2 - P_1 | \{s_j, P_1\}]} \quad (58)$$

$$\sqrt{\left(\frac{n}{\sigma_\eta^2} \frac{\sigma_x^2}{\gamma} + \frac{1}{\gamma} \left(\frac{n}{\gamma^2 \sigma_\eta^2} \right)^2 + \frac{\sigma_x^2}{\gamma \sigma_1^2} \right)^2}$$

$$= -e^{\gamma\hat{c}-\gamma W} \sqrt{\frac{\frac{1}{\sigma_1^2}}{\frac{\left(\frac{\sigma_x^2}{\gamma\sigma_1^2}\right)^2 + \frac{\sigma_x^2}{\sigma_1^2} \left(\frac{n}{\gamma^2\sigma_\eta^2} + \sigma_x^2\right)^2} \left(\frac{1}{\hat{\sigma}_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_1^2}\right)}{\left(\frac{n}{\sigma_\eta^2} \frac{\sigma_x^2}{\gamma} + \frac{1}{\gamma} \left(\frac{n}{\gamma^2\sigma_\eta^2}\right)^2 + \frac{\sigma_x^2}{\gamma\sigma_1^2}\right)^2}}, \quad (59)$$

where $\hat{\sigma}_\eta^2$ and \hat{c} indicate the investor i 's choice.

1) $n_I = 0$ is an equilibrium when

$$EU(\sigma_\eta^2, c, n_I = 0) < EU(\infty, 0, n_I = 0) \quad (60)$$

$$\text{or when, } -e^{\gamma c - \gamma W} \sqrt{\frac{\frac{1}{\sigma_1^2}}{\frac{\left(\frac{\sigma_x^2}{\gamma\sigma_1^2}\right)^2 + \frac{\sigma_x^2}{\sigma_1^2} (\sigma_x^2)^2} \left(\frac{1}{\sigma_\eta^2} + \frac{1}{\sigma_1^2}\right)}} < -e^{-\gamma W} \sqrt{\frac{\frac{1}{\sigma_1^2}}{\frac{\left(\frac{\sigma_x^2}{\gamma\sigma_1^2}\right)^2 + \frac{\sigma_x^2}{\sigma_1^2} (\sigma_x^2)^2} \left(\frac{1}{\sigma_1^2}\right)}}. \quad (61)$$

Above condition can be summarized as $e^{2\gamma c} - 1 > \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2}}$.

2) $n_I = 1$ is an equilibrium when

$$EU(\sigma_\eta^2, c, n_I = 1) \geq EU(\infty, 0, n_I = 1) \quad (62)$$

or when,

$$\begin{aligned} & -e^{\gamma c - \gamma W} \sqrt{\frac{\frac{1}{\sigma_1^2}}{\frac{\left(\frac{\sigma_x^2}{\gamma\sigma_1^2}\right)^2 + \frac{\sigma_x^2}{\sigma_1^2} \left(\frac{1}{\gamma^2\sigma_\eta^2} + \sigma_x^2\right)^2} \left(\frac{1}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_1^2}\right)}{\left(\frac{1}{\sigma_\eta^2} \frac{\sigma_x^2}{\gamma} + \frac{1}{\gamma} \left(\frac{1}{\gamma^2\sigma_\eta^2}\right)^2 + \frac{\sigma_x^2}{\gamma\sigma_1^2}\right)^2}} \\ & > -e^{-\gamma W} \sqrt{\frac{\frac{1}{\sigma_1^2}}{\frac{\left(\frac{\sigma_x^2}{\gamma\sigma_1^2}\right)^2 + \frac{\sigma_x^2}{\sigma_1^2} \left(\frac{1}{\gamma^2\sigma_\eta^2} + \sigma_x^2\right)^2} \left(\frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_1^2}\right)}{\left(\frac{1}{\sigma_\eta^2} \frac{\sigma_x^2}{\gamma} + \frac{1}{\gamma} \left(\frac{1}{\gamma^2\sigma_\eta^2}\right)^2 + \frac{\sigma_x^2}{\gamma\sigma_1^2}\right)^2}}. \end{aligned} \quad (63)$$

$$\text{The condition is summarized as } e^{2\gamma c} - 1 < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2} \quad (64)$$

3) Otherwise, $n_I \in (0, 1)$ and equilibrium n_I satisfies

$$EU(\sigma_\eta^2, c, n_I) = EU(\infty, 0, n_I) \quad (65)$$

Therefore, equilibrium proportion of informed investors under the infrequent regime (n_I) is:

$$n_I = \gamma \sigma_x \sigma_\eta^2 \sqrt{\frac{\frac{1}{\sigma_\eta^2}}{e^{2\gamma c} - 1} - \frac{1}{\sigma_1^2}} \quad (66)$$

Lemma 3. Diamond (1985) shows that the information acquisition decision with firm disclosure is identical to the case where investors have prior precision $\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}$ instead of $\frac{1}{\sigma_1^2}$. Using the same method, an individual investor i 's ex ante expected utility given $\{n, \sigma_\eta^2, c\}$ is given by

$$EU_i(\hat{\sigma}_\eta^2, \hat{c}, n) = -e^{\gamma \hat{c} - \gamma W} \sqrt{\frac{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}}{\left(\frac{\sigma_x^2}{\gamma \sigma_1^2}\right)^2 + \frac{\sigma_x^2}{\sigma_1^2} \left(\frac{n}{\gamma^2 \sigma_\eta^2} + \sigma_x^2\right)^2} \left(\frac{1}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2}\right)^2 + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}\right)} \quad (67)$$

$$= -e^{\gamma \hat{c} - \gamma W} \sqrt{\frac{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}}{\left(\frac{\sigma_x^2}{\gamma \sigma_1^2}\right)^2 + \frac{\sigma_x^2}{\sigma_1^2} \left(\frac{n}{\gamma^2 \sigma_\eta^2} + \sigma_x^2\right)^2} \sqrt{\text{Var}[v_1 + v_2 - P_1|\{e_1, P_1, s_j\}]} \quad (68)$$

1) $n_F = 0$ is an equilibrium when

$$EU(\sigma_\eta^2, c, n_F = 0) < EU(\infty, 0, n_F = 0) \quad (69)$$

$$\text{or when, } e^{2\gamma c} - 1 > \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}} \quad (70)$$

2) $n_F = 1$ is an equilibrium when

$$EU(\sigma_\eta^2, c, n_F = 1) > EU(\infty, 0, n_F = 1) \quad (71)$$

$$\text{or when, } e^{2\gamma c} - 1 \leq \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_\varepsilon^2} + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2}\right)^2} \quad (72)$$

3) Otherwise, $n_F \in (0, 1)$ and equilibrium n_F satisfies

$$EU(\sigma_\eta^2, c, n_F) = EU(\infty, 0, n_F) \quad (73)$$

Therefore, equilibrium proportion of informed investors under the frequent regime (n_F) is:

$$n_F = \gamma \sigma_x \sigma_\eta^2 \sqrt{\frac{\frac{1}{\sigma_\eta^2}}{e^{2\gamma c} - 1} - \frac{1}{\sigma_1^2} - \frac{1}{\sigma_\varepsilon^2}} \quad (74)$$

Proof of Proposition 3.

Case A. I first consider the case where $\frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2 > \frac{1}{\sigma_\varepsilon^2}$ holds.

$\frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2 > \frac{1}{\sigma_\varepsilon^2}$ implies the following.

$$\frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2} < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2} < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}} < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2}} \quad (75)$$

Therefore, depending on the value of $e^{2\gamma c} - 1$, there are five cases.

(1) When $e^{2\gamma c} - 1 < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2}$,

$n_I = n_F = 1$.

$$X_F = \frac{\frac{1}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_\varepsilon^2}}{\frac{1}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}} \quad (76)$$

$$X_I = \frac{\frac{1}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2}{\frac{1}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2}} \quad (77)$$

and therefore, $X_F > X_I$ and $k_{1,F}^* > k_{1,I}^*$.

(2) When $\frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2} \leq e^{2\gamma c} - 1 < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2}$,

$n_I = 1, n_F = \gamma \sigma_x \sigma_\eta^2 \sqrt{\frac{\frac{1}{\sigma_\eta^2}}{e^{2\gamma c} - 1} - \frac{1}{\sigma_1^2} - \frac{1}{\sigma_\varepsilon^2}}$.

X_F is continuous and strictly decreasing in the value of $e^{2\gamma c} - 1$. Also, $X_F > X_I$ when $e^{2\gamma c} - 1$ takes the minimum possible value in this region $\left(\frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2} \right)$. Similarly, when $e^{2\gamma c} - 1$ takes the

maximum possible value in this region $\left(\frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2} \right)$, $n_F = \gamma \sigma_x \sigma_\eta^2 \sqrt{\frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2 - \frac{1}{\sigma_\varepsilon^2}}$. Plugging

n_F into X_F gives:

$$X_F = \frac{\frac{n_F}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2} \right)^2}{\frac{n_F}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2}} \quad (78)$$

which is smaller than X_I since $n_F < n_I = 1$.

Together, this indicates that there exists a threshold value \underline{c} above which $X_I > X_F$ holds.

(3) When $\frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2} \right)^2} \leq e^{2\gamma c} - 1 < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}}$, $n_F < n_I \in (0, 1]$. Using the same logic as in (2), equilibrium n_I and n_F can be derived. Plugging these back into X_I, X_F gives:

$$X_I = \frac{\frac{n_I}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2} \right)^2}{\frac{n_I}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2}} \quad (79)$$

$$X_F = \frac{\frac{n_F}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2} \right)^2}{\frac{n_F}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2}} \quad (80)$$

Since $n_F < n_I$, $X_F < X_I$.

(4) When $\frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}} \leq e^{2\gamma c} - 1 < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2}}$, $n_F = 0$ and $n_I \in (0, 1)$. Using the same logic as in Case 2, it can be shown that there exists a threshold value \bar{c} below which $X_I > X_F$.

(5) When $\frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2}} < e^{2\gamma c} - 1$, $n_I = n_F = 0$ and $X_F > X_I$.

Case B. Next I consider the case where $\frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2} \right)^2 < \frac{1}{\sigma_\varepsilon^2} < \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2} \right)^2 + \frac{1}{\sigma_\eta^2}$ holds.

$\frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2} \right)^2 < \frac{1}{\sigma_\varepsilon^2}$ implies:

$$\frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2} \right)^2} < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}} < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2} \right)^2} < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2}} \quad (81)$$

(1) When $e^{2\gamma c} - 1 < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2}$,
 $n_I = n_F = 1$ and thus $X_F > X_I$.

(2) When $\frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2} \leq e^{2\gamma c} - 1 < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}}$,

$$n_I = 1, n_F = \gamma\sigma_x\sigma_\eta^2 \sqrt{\frac{\frac{1}{\sigma_\eta^2}}{e^{2\gamma c} - 1} - \frac{1}{\sigma_1^2} - \frac{1}{\sigma_\varepsilon^2}}.$$

Using the same logic as in Case A, X_F is continuous and strictly decreasing in the value of $e^{2\gamma c} - 1$ and $X_F > X_I$ when $e^{2\gamma c} - 1$ takes the minimum possible value in this region, $\frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2}$. Finally, when $e^{2\gamma c} - 1$ takes the maximum possible value in this region, $\frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}}$, $n_F = 0$. Plugging p_F into X_F gives:

$$X_F = \frac{\frac{1}{\sigma_\varepsilon^2}}{\frac{1}{\sigma_\varepsilon^2} + \frac{1}{\sigma_1^2}} \quad (82)$$

which is smaller than X_I since $\frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2 < \frac{1}{\sigma_\varepsilon^2} < \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_\eta^2}$.

Together, this indicates that there exists a threshold value \underline{c} above which $X_I > X_F$ holds.

(3) When $\frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\varepsilon^2}} \leq e^{2\gamma c} - 1 < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2}$, $0 = n_F < n_I = 1$. Plugging these back into X_I, X_F gives:

$$X_I = \frac{\frac{1}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2}{\frac{1}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2 + \frac{1}{\sigma_1^2}} \quad (83)$$

$$X_F = \frac{\frac{1}{\sigma_\varepsilon^2}}{\frac{1}{\sigma_\varepsilon^2} + \frac{1}{\sigma_1^2}} \quad (84)$$

Therefore, $X_F < X_I$.

(4) When $\frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma\sigma_\eta^2}\right)^2} \leq e^{2\gamma c} - 1 < \frac{\frac{1}{\sigma_\eta^2}}{\frac{1}{\sigma_1^2}}$, $n_F = 0$ and $n_I \in (0, 1)$. Using the same logic as in Case 2, it can be shown that there exists a threshold value \bar{c} below which $X_I > X_F$.

(5) When $\frac{1}{\sigma_\eta^2} < e^{2\gamma c} - 1$, $n_I = n_F = 0$ and $X_F > X_I$.

Case C. Finally, I consider the case where $\frac{1}{\sigma_\epsilon^2} > \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_\eta^2}$. In this case, the same ordering applies as in Case B. However, given the assumption $\frac{1}{\sigma_\epsilon^2} > \frac{1}{\sigma_x^2} \left(\frac{1}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_\eta^2}$, $X_F > X_I$ in all five regions.

Proof of Proposition 4.

Since $k_{1,I}^*$ does not change with σ_ϵ^2 ,

$$\frac{\partial}{\partial \sigma_\epsilon^2} (k_{1,F}^* - k_{1,I}^*) = \frac{\partial k_{1,F}^*}{\partial \sigma_\epsilon^2} = \frac{\partial k_{1,F}^*}{\partial X_F} \cdot \frac{\partial X_F}{\partial \sigma_\epsilon^2} > 0 \quad (85)$$

$$\frac{\partial}{\partial I} (k_{1,F}^* - k_{1,I}^*) = -\frac{(\alpha - 1)\alpha(X_I - X_F)}{(\alpha(X_I - 2) + 2)(\alpha(X_F - 2) + 2)} < 0 \text{ when } X_F > X_I \quad (86)$$

$$> 0 \text{ when } X_F < X_I. \quad (87)$$

Proof of Lemma 5.

Time 1

At time 1, informed (q_{1i}^*) and uninformed investors (q_{1u}^*) choose the following quantity.

$$q_{1i}^* = \frac{1}{\gamma} \left(\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\epsilon^2} + \frac{1}{\left(\frac{\beta_x^0}{\beta_v^0} \right)^2 \sigma_x^2} + \frac{1}{\left(\frac{\beta_x^1}{\beta_v^1} \right)^2 \sigma_x^2} + \frac{1}{\sigma_\eta^2} \right) \cdot \left[\frac{\frac{1}{\sigma_1^2} \cdot E(v_1) + \frac{1}{\sigma_\epsilon^2} \cdot e_1 + \frac{1}{\left(\frac{\beta_x^0}{\beta_v^0} \right)^2 \sigma_x^2} \cdot m_0 + \frac{1}{\left(\frac{\beta_x^1}{\beta_v^1} \right)^2 \sigma_x^2} \cdot m_1 + \frac{1}{\sigma_\eta^2} \cdot s_i}{\left(\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\epsilon^2} + \frac{1}{\left(\frac{\beta_x^0}{\beta_v^0} \right)^2 \sigma_x^2} + \frac{1}{\left(\frac{\beta_x^1}{\beta_v^1} \right)^2 \sigma_x^2} + \frac{1}{\sigma_\eta^2} \right)} \right] + \frac{1}{\gamma} \left(\frac{1}{\sigma_1^2} + \frac{1}{\sigma_\epsilon^2} + \frac{1}{\left(\frac{\beta_x^0}{\beta_v^0} \right)^2 \sigma_x^2} + \frac{1}{\left(\frac{\beta_x^1}{\beta_v^1} \right)^2 \sigma_x^2} + \frac{1}{\sigma_\eta^2} \right) [(E(v_2) - P_1)] \quad (88)$$

$$\begin{aligned}
q_{1u}^* &= \frac{1}{\gamma} \left(\frac{1}{\sigma_1^2} + \frac{1}{\left(\frac{\beta_x^0}{\beta_v^0}\right)^2 \sigma_x^2} + \frac{1}{\left(\frac{\beta_x^1}{\beta_v^1}\right)^2 \sigma_x^2} + \frac{1}{\sigma_\epsilon^2} \right) \\
&\cdot \left[\frac{\frac{1}{\sigma_1^2} \cdot E(v_1) + \frac{1}{\sigma_\epsilon^2} \cdot e_1 + \frac{1}{\left(\frac{\beta_x^0}{\beta_v^0}\right)^2 \sigma_x^2} \cdot m_0 + \frac{1}{\left(\frac{\beta_x^1}{\beta_v^1}\right)^2 \sigma_x^2} \cdot m_1}{\left(\frac{1}{\sigma_1^2} + \frac{1}{\left(\frac{\beta_x^0}{\beta_v^0}\right)^2 \sigma_x^2} + \frac{1}{\left(\frac{\beta_x^1}{\beta_v^1}\right)^2 \sigma_x^2} + \frac{1}{\sigma_\epsilon^2} \right)} \right] \\
&+ \frac{1}{\gamma} \left(\frac{1}{\sigma_1^2} + \frac{1}{\left(\frac{\beta_x^0}{\beta_v^0}\right)^2 \sigma_x^2} + \frac{1}{\left(\frac{\beta_x^1}{\beta_v^1}\right)^2 \sigma_x^2} + \frac{1}{\sigma_\epsilon^2} \right) [(E(v_2) - P_1)]
\end{aligned} \tag{89}$$

where $m_1(m_0)$ is a signal from $P_1(P_0)$.

Applying market clearing condition,

$$\int_i q_{1i}^* d_i + (1 - n) \cdot q_{1u}^* = x_1 \tag{90}$$

Solving for the market clearing condition gives:

$$\begin{aligned}
P_{1,F} &= \frac{\frac{1}{\sigma_1^2} E[v_1]}{\underbrace{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\beta_v^0}{\beta_x^0}\right)^2 + \frac{1}{\sigma_x^2} \left(\frac{\beta_v^1}{\beta_x^1}\right)^2 + \frac{1}{\sigma_\epsilon^2} + \frac{1}{\sigma_1^2}}_{\beta^1}} + E[v_2] + \frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\beta_v^1}{\beta_x^1}\right)^2}{\underbrace{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\beta_v^0}{\beta_x^0}\right)^2 + \frac{1}{\sigma_x^2} \left(\frac{\beta_v^1}{\beta_x^1}\right)^2 + \frac{1}{\sigma_\epsilon^2} + \frac{1}{\sigma_1^2}}_{\beta_v^1}} v_1 \\
&+ \frac{\frac{1}{\sigma_x^2} \left(\frac{\beta_v^0}{\beta_x^0}\right)^2}{\underbrace{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\beta_v^0}{\beta_x^0}\right)^2 + \frac{1}{\sigma_x^2} \left(\frac{\beta_v^1}{\beta_x^1}\right)^2 + \frac{1}{\sigma_\epsilon^2} + \frac{1}{\sigma_1^2}}_{\beta_m^1}} m_0 + \frac{\frac{1}{\sigma_\epsilon^2}}{\underbrace{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\beta_v^0}{\beta_x^0}\right)^2 + \frac{1}{\sigma_x^2} \left(\frac{\beta_v^1}{\beta_x^1}\right)^2 + \frac{1}{\sigma_\epsilon^2} + \frac{1}{\sigma_1^2}}_{\beta_\epsilon^1}} e_1 \\
&+ \frac{\frac{1}{\sigma_x^2} \frac{\beta_v^1}{\beta_x^1} - \gamma}{\underbrace{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\beta_v^0}{\beta_x^0}\right)^2 + \frac{1}{\sigma_x^2} \left(\frac{\beta_v^1}{\beta_x^1}\right)^2 + \frac{1}{\sigma_\epsilon^2} + \frac{1}{\sigma_1^2}}_{\beta_x^1}} x_1,
\end{aligned} \tag{91}$$

$$\text{where } \frac{\beta_v^1}{\beta_x^1} = -\frac{n}{\gamma \sigma_\eta^2}$$

Time 0

$$q_{0u}^* = \frac{[(E[P_1 | m_0] - P_0) + h_u^F \cdot (E[v_1 + v_2 - P_1 | m_0])]}{\text{Var}[P_1 - P_0 + h_u^F(v_1 + v_2 - P_1) | \{m_0\}]} \quad (92)$$

$$= \frac{E[v_1 + v_2 - P_0 | m_0] - (1 - h_u^F)E[v_1 + v_2 - P_1 | m_0]}{\text{Var}[P_1 - P_0 + h_u^F(v_1 + v_2 - P_1) | \{m_0\}]} \quad (93)$$

where

$$\text{Var}[P_1 - P_0 + h_u^F(v_1 + v_2 - P_1) | \{m_0\}] = \frac{\gamma \cdot \text{Var}[v_1 | m_0] \cdot (\beta_x^1)^2 \sigma_x^2 + (\beta_e^1)^2 \sigma_e^2}{(1 - \beta_v^1 - \beta_e^1)^2 \cdot \text{Var}[v_1 | m_0] + (\beta_x^1)^2 \sigma_x^2 + (\beta_e^1)^2 \sigma_e^2},$$

$$h_u^F = \frac{(\beta_x^1)^2 \sigma_x^2 + (\beta_e^1)^2 \sigma_e^2 - (\beta_v^1 + \beta_e^1) (1 - \beta_v^1 - \beta_e^1) \cdot \text{Var}[v_1 | m_0]}{(1 - \beta_v^1 - \beta_e^1)^2 \cdot \text{Var}[v_1 | m_0] + (\beta_x^1)^2 \sigma_x^2} \in (0, 1).$$

$$q_{0i}^* = \frac{[(E[P_1 | m_0, s_i] - P_0) + h_i^F \cdot (E[v_1 + v_2 - P_1 | m_0, s_i])]}{\text{Var}[P_1 - P_0 + h_u^F(v_1 + v_2 - P_1) | \{m_0, s_i\}]} \quad (94)$$

$$= \frac{[E[v_1 + v_2 - P_0 | m_0] - (1 - h_i^F)E[v_1 + v_2 - P_1 | m_0]]}{\text{Var}[P_1 - P_0 + h_u^F(v_1 + v_2 - P_1) | \{m_0, s_i\}]}$$

where

$$\text{Var}[P_1 - P_0 + h_u^F(v_1 + v_2 - P_1) | \{m_0, s_i\}] = \frac{\gamma \cdot \text{Var}[v_1 | m_0, s_i] \cdot (\beta_x^1)^2 \sigma_x^2 + (\beta_e^1)^2 \sigma_e^2}{(1 - \beta_v^1 - \beta_e^1)^2 \cdot \text{Var}[v_1 | m_0, s_i] + (\beta_x^1)^2 \sigma_x^2 + (\beta_e^1)^2 \sigma_e^2}$$

$$h_i^F = \frac{(\beta_x^1)^2 \sigma_x^2 + (\beta_e^1)^2 \sigma_e^2 - (\beta_v^1 + \beta_e^1) (1 - \beta_v^1 - \beta_e^1) \cdot \text{Var}[v_1 | m_0, s_i]}{(1 - \beta_v^1 - \beta_e^1)^2 \cdot \text{Var}[v_1 | m_0, s_i] + (\beta_x^1)^2 \sigma_x^2} \in (0, 1)$$

Applying market clearing condition gives the equilibrium price equation at time 0.

$$P_{0,F} = \beta^0 + v_1 \cdot \frac{\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \cdot \sigma_x^2} + \frac{n}{\sigma_\eta^2} + \frac{(1 - \beta_v^1 - \beta_e^1) \cdot \beta_m^1}{(\beta_x^1)^2 \sigma_x^2 + (\beta_e^1)^2 \sigma_e^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \cdot \sigma_x^2} + \frac{n}{\sigma_\eta^2} + \frac{(1 - \beta_v^1 - \beta_e^1)^2}{(\beta_x^1)^2 \sigma_x^2 + (\beta_e^1)^2 \sigma_e^2}} + x_0 \cdot \beta_x^0 \quad (95)$$

$$\text{where } \beta^0 = \frac{\left(\beta^1 \frac{(1 - \beta_v^1 - \beta_e^1)}{(\beta_x^1)^2 \sigma_x^2 + (\beta_e^1)^2 \sigma_e^2} + E[v_1] \cdot \frac{1}{\sigma_1^2} - E[v_2] \cdot \left(\frac{(1 - \beta_v^1 - \beta_e^1) \cdot (\beta_v^1 + \beta_e^1)}{(\beta_x^1)^2 \sigma_x^2 + (\beta_e^1)^2 \sigma_e^2} - \frac{1}{\sigma_1^2} - \frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \sigma_x^2} - \frac{n}{\sigma_\eta^2} \right) \right)}{\frac{1}{\sigma_1^2} + \frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \cdot \sigma_x^2} + \frac{n}{\sigma_\eta^2} + \frac{(1 - \beta_v^1 - \beta_e^1)^2}{(\beta_x^1)^2 \sigma_x^2 + (\beta_e^1)^2 \sigma_e^2}}$$

$$\text{and } \beta_x^0 = \frac{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \cdot \sigma_x^2} + \frac{n}{\sigma_\eta^2} + \frac{(1-\beta_v^1 - \beta_e^1) \cdot \beta_m^1}{(\beta_x^1)^2 \sigma_x^2 + (\beta_e^1)^2 \sigma_\epsilon^2} \right) \left(-\frac{\gamma \sigma_\eta^2}{n} \right)}{\frac{1}{\sigma_1^2} + \frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \cdot \sigma_x^2} + \frac{n}{\sigma_\eta^2} + \frac{(1-\beta_v^1 - \beta_e^1)^2}{(\beta_x^1)^2 \sigma_x^2 + (\beta_e^1)^2 \sigma_\epsilon^2}}.$$

Plugging in the price coefficients gives the following price informativeness at time 1 and time 0.

$$X_{1,F} = \frac{\frac{1}{\sigma_\epsilon^2} + \frac{2}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2}}{\frac{1}{\sigma_\epsilon^2} + \frac{n}{\sigma_\eta^2} + \frac{2}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2}}, X_{0,F} = \frac{\frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2} + \frac{\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} \left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \frac{1}{\sigma_1^2} \right)}{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \gamma \right) \sigma_x^2 + \frac{1}{\sigma_\epsilon^2}}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2} + \frac{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \frac{1}{\sigma_1^2} \right)}{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \gamma \right) \sigma_x^2 + \frac{1}{\sigma_\epsilon^2}}}. \quad (96)$$

Plugging in price efficiencies into the manager's equilibrium operating decision gives the equilibrium input on project S .

Proof of Lemma 6.

Time 1

At time 1, informed (q_{1i}^*) and uninformed investors (q_{1u}^*) choose the following quantity.

$$q_{1i}^* = \frac{1}{\gamma} \left(\frac{1}{\sigma_1^2} + \frac{1}{\left(\frac{\lambda_x^0}{\lambda_v^0} \right)^2 \sigma_x^2} + \frac{1}{\left(\frac{\lambda_x^1}{\lambda_v^1} \right)^2 \sigma_x^2} + \frac{1}{\sigma_\eta^2} \right) \quad (97)$$

$$\cdot \left[\frac{\frac{1}{\sigma_1^2} \cdot E(v_1) + \frac{1}{\left(\frac{\lambda_x^0}{\lambda_v^0} \right)^2 \sigma_x^2} \cdot m_0 + \frac{1}{\left(\frac{\lambda_x^1}{\lambda_v^1} \right)^2 \sigma_x^2} \cdot m_1 + \frac{1}{\sigma_\eta^2} \cdot s_i}{\left(\frac{1}{\sigma_1^2} + \frac{1}{\left(\frac{\lambda_x^0}{\lambda_v^0} \right)^2 \sigma_x^2} + \frac{1}{\left(\frac{\lambda_x^1}{\lambda_v^1} \right)^2 \sigma_x^2} + \frac{1}{\sigma_\eta^2} \right)} + (E(v_2) - P_1) \right]$$

$$q_{1u}^* = \frac{1}{\gamma} \left(\frac{1}{\sigma_1^2} + \frac{1}{\left(\frac{\lambda_x^0}{\lambda_v^0} \right)^2 \sigma_x^2} + \frac{1}{\left(\frac{\lambda_x^1}{\lambda_v^1} \right)^2 \sigma_x^2} \right) \quad (98)$$

$$\left[\frac{\frac{1}{\sigma_1^2} \cdot E(v_1) + \frac{1}{\left(\frac{\lambda_x^0}{\lambda_v^0}\right)^2} \cdot m_0 + \frac{1}{\left(\frac{\lambda_x^1}{\lambda_v^1}\right)^2} \cdot m_1}{\left(\frac{1}{\sigma_1^2} + \frac{1}{\left(\frac{\lambda_x^0}{\lambda_v^0}\right)^2} + \frac{1}{\left(\frac{\lambda_x^1}{\lambda_v^1}\right)^2}\right)} + (E(v_2) - P_1) \right]$$

where m_1 is a signal from $P_1, m_1 = \frac{1}{\lambda_v^1}(P_1 - \lambda^1 - \lambda_m^1 m_0) = v_1 + \frac{\lambda_x^1}{\lambda_v^1} x_1$, and m_0 a signal from P_0 .

Applying market clearing condition,

$$\int_i q_{1i}^* d_i + (1 - n) \cdot q_{1u}^* = x_1 \quad (99)$$

Solving for the market clearing condition gives:

$$\begin{aligned} P_{1,I} = & \underbrace{\frac{\frac{1}{\sigma_1^2} E[v_1]}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\lambda_v^0}{\lambda_x^0}\right)^2 + \frac{1}{\sigma_x^2} \left(\frac{\lambda_v^1}{\lambda_x^1}\right)^2 + \frac{1}{\sigma_1^2}}}_{\lambda^1} + E[v_2] + \underbrace{\frac{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\lambda_v^1}{\lambda_x^1}\right)^2}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\lambda_v^0}{\lambda_x^0}\right)^2 + \frac{1}{\sigma_x^2} \left(\frac{\lambda_v^1}{\lambda_x^1}\right)^2 + \frac{1}{\sigma_1^2}}}_{\lambda_v^1} v_1 \\ & + \underbrace{\frac{\frac{1}{\sigma_x^2} \left(\frac{\lambda_v^0}{\lambda_x^0}\right)^2}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\lambda_v^0}{\lambda_x^0}\right)^2 + \frac{1}{\sigma_x^2} \left(\frac{\lambda_v^1}{\lambda_x^1}\right)^2 + \frac{1}{\sigma_1^2}}}_{\lambda_m^1} m_0 + \underbrace{\frac{\frac{1}{\sigma_x^2} \frac{\lambda_v^1}{\lambda_x^1} - \gamma}{\frac{n}{\sigma_\eta^2} + \frac{1}{\sigma_x^2} \left(\frac{\lambda_v^0}{\lambda_x^0}\right)^2 + \frac{1}{\sigma_x^2} \left(\frac{\lambda_v^1}{\lambda_x^1}\right)^2 + \frac{1}{\sigma_1^2}}}_{\lambda_x^1} x_1, \end{aligned} \quad (100)$$

$$\text{where } \frac{\lambda_v^1}{\lambda_x^1} = -\frac{n}{\gamma \sigma_\eta^2}$$

Time 0

Time 0 quantity of investor i follows

$$q_{0i}^* = \frac{(E[P_1 | \Omega_{0i}] - P_0) + h_i^I \cdot E[v_1 + v_2 - P_1 | \Omega_{0i}]}{\gamma (Var[P_1 - P_0 | \Omega_{0j}] + h_i^I \cdot Cov[P_1 - P_0, v_1 + v_2 - P_1 | \Omega_{0i}])} \quad (101)$$

$$\text{where } h_i^I = -\frac{Cov[P_1 - P_0, v_1 + v_2 - P_1 | \Omega_{0i}]}{Var[v_1 + v_2 - P_1 | \Omega_{0i}]}$$

Under the infrequent regime, an uninformed investor's information set at time 0 is $\Omega_{0u} = \{m_0\}$. An informed investor's information set at time 0 is $\Omega_{0i} = \{m_0, s_i\}$. Calculating conditional expectation and variance, and then plugging into the equilibrium time 0 demand gives the following.

$$\begin{aligned}
q_{0u}^* &= \frac{(1 - \lambda_v^1)^2 \cdot \text{Var} [v_1 | m_0] + (\lambda_x^1)^2 \sigma_x^2}{\underbrace{\gamma \cdot \text{Var} [v_1 | m_0] \cdot (\lambda_x^1)^2 \sigma_x^2}_{\text{Var}^{-1}[P_1 - P_0 + h_u^I(v_1 + v_2 - P_1) | \{m_0\}]}} \\
&\left[(E [P_1 | m_0] - P_0) + \underbrace{\frac{(\lambda_x^1)^2 \sigma_x^2 - \lambda_v^1 (1 - \lambda_v^1) \cdot \text{Var} [v_1 | m_0]}{(1 - \lambda_v^1)^2 \cdot \text{Var} [v_1 | m_0] + (\lambda_x^1)^2 \sigma_x^2}}_{h_u^I \in (0,1)} \cdot (E[v_1 + v_2 - P_1 | m_0]) \right] \quad (102) \\
&= \frac{(1 - \lambda_v^1)^2 \cdot \text{Var} [v_1 | m_0] + (\lambda_x^1)^2 \sigma_x^2}{\underbrace{\gamma \cdot \text{Var} [v_1 | m_0] \cdot (\lambda_x^1)^2 \sigma_x^2}_{\text{Var}^{-1}[P_1 - P_0 + h_u^I(v_1 + v_2 - P_1) | \{m_0\}]}} [E[v_1 + v_2 - P_0 | m_0] - (1 - h_u^I)E[v_1 + v_2 - P_1 | m_0]] \\
&\quad (103)
\end{aligned}$$

$$\begin{aligned}
q_{0i}^* &= \frac{(1 - \lambda_v^1)^2 \cdot \text{Var} [v_1 | m_0, s_i] + (\lambda_x^1)^2 \sigma_x^2}{\underbrace{\gamma \cdot \text{Var} [v_1 | m_0, s_i] \cdot (\lambda_x^1)^2 \sigma_x^2}_{\text{Var}^{-1}[P_1 - P_0 + h_i^I(v_1 + v_2 - P_1) | \{m_0, s_i\}]}} \\
&\left[(E [P_1 | m_0, s_i] - P_0) + \underbrace{\frac{(\lambda_x^1)^2 \sigma_x^2 - \lambda_v^1 (1 - \lambda_v^1) \cdot \text{Var} [v_1 | m_0, s_i]}{(1 - \lambda_v^1)^2 \cdot \text{Var} [v_1 | m_0, s_i] + (\lambda_x^1)^2 \sigma_x^2}}_{h_i^I \in (0,1)} \cdot (E[v_1 + v_2 - P_1 | m_0, s_i]) \right] \quad (104) \\
&= \frac{(1 - \lambda_v^1)^2 \cdot \text{Var} [v_1 | m_0, s_i] + (\lambda_x^1)^2 \sigma_x^2}{\underbrace{\gamma \cdot \text{Var} [v_1 | m_0, s_i] \cdot (\lambda_x^1)^2 \sigma_x^2}_{\text{Var}^{-1}[P_1 - P_0 + h_i^I(v_1 + v_2 - P_1) | \{m_0, s_i\}]}} [E[v_1 + v_2 - P_0 | m_0] - (1 - h_i^I)E[v_1 + v_2 - P_1 | m_0, s_i]] \\
&\quad (105)
\end{aligned}$$

Applying market clearing condition gives the equilibrium price equation at time 0.

$$P_{0,I} = \lambda^0 + v_1 \cdot \frac{\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \cdot \sigma_x^2} + \frac{n}{\sigma_\eta^2} + \frac{(1 - \lambda_v^1) \cdot \lambda_m^1}{(\lambda_x^1)^2 \sigma_x^2}}{\underbrace{\frac{1}{\sigma_1^2} + \frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \cdot \sigma_x^2} + \frac{n}{\sigma_\eta^2} + \frac{(1 - \lambda_v^1)^2}{(\lambda_x^1)^2 \sigma_x^2}}_{\lambda_v^0}} + x_0 \cdot \lambda_x^0 \quad (106)$$

$$\text{where } \lambda^0 = \frac{\left(\lambda^1 \frac{1-\lambda_v^1}{(\lambda_x^1)^2 \sigma_x^2} + E[v_1] \cdot \frac{1}{\sigma_1^2} - E[v_2] \cdot \left(\frac{\lambda_v^1(1-\lambda_v^1)}{(\lambda_x^1)^2 \sigma_x^2} - \frac{1}{\sigma_1^2} - \frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \sigma_x^2} - \frac{n}{\sigma_\eta^2} \right) \right)}{\frac{1}{\sigma_1^2} + \frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \sigma_x^2} + \frac{n}{\sigma_\eta^2} + \frac{(1-\lambda_1^1)^2}{(\lambda_x^1)^2 \sigma_x^2}}$$

$$\text{and } \lambda_x^0 = \frac{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \sigma_x^2} + \frac{n}{\sigma_\eta^2} + \frac{(1-\lambda_v^1) \cdot \lambda_m^1}{(\lambda_x^1)^2 \sigma_x^2} \right) \left(-\frac{\gamma \sigma_\eta^2}{n} \right)}{\frac{1}{\sigma_1^2} + \frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \sigma_x^2} + \frac{n}{\sigma_\eta^2} + \frac{(1-\lambda_1^1)^2}{(\lambda_x^1)^2 \sigma_x^2}}$$

Substituting the equilibrium price coefficients gives the following price informativeness at time 1 and time 0 respectively.

$$X_{1,I} = \frac{\frac{2}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2}}{\frac{n}{\sigma_\eta^2} + \frac{2}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2}}, X_{0,I} = \frac{\frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2} + \frac{\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \sigma_x^2} \left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \sigma_x^2} + \frac{1}{\sigma_1^2} \right)}{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \sigma_x^2} + \gamma \right) \sigma_x^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2} + \frac{\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \sigma_x^2} \left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \sigma_x^2} + \frac{1}{\sigma_1^2} \right)}{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n}\right)^2 \sigma_x^2} + \gamma \right) \sigma_x^2}}. \quad (107)$$

Plugging in price efficiencies into $k_{1,I}^* = \frac{\alpha [\delta X_{0,I} + (1-\delta)X_{1,I}] \mu_1 + (1-\alpha)(I - \mu_1 + \mu_2)}{\alpha [\delta X_{0,I} + (1-\delta)X_{1,I}] + 2(1-\alpha)}$ gives the equilibrium short-term operating input. Due to parameter constraint, $k_{1,I}^* < I$.

Proof of Proposition 5.

Solving for the maximization problem gives the equilibrium short-term capital input k_1^* :

$$k_1^* = \frac{\alpha [\delta X_0 + (1-\delta)X_1] \mu_1 + (1-\alpha)(I - \mu_2 + \mu_1)}{\alpha [\delta X_0 + (1-\delta)X_1] + 2(1-\alpha)} \quad (108)$$

where X_t indicates price efficiency at time t .

Since k_1^* is increasing in the aggregate price efficiency at time 0 and time 1 $[\delta X_0 + (1 - \delta)X_1]$ it suffices to compare the price efficiency under the two regimes.

Time 1

	Infrequent	Frequent
Time 1	$\frac{\frac{2}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2}}{\frac{n}{\sigma_\eta^2} + \frac{2}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2}}$	$\frac{\frac{1}{\sigma_\epsilon^2} + \frac{2}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2}}{\frac{1}{\sigma_\epsilon^2} + \frac{n}{\sigma_\eta^2} + \frac{2}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{1}{\sigma_1^2}}$

Given fixed number of informed investors, the price efficiency at time 1 is higher under the frequent regime.

Time 0

	Infrequent	Frequent
Time 0	$\frac{\frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2} + \frac{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} \left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \frac{1}{\sigma_1^2} \right)}{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \gamma \right) \sigma_x^2}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2} + \frac{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \frac{1}{\sigma_1^2} \right)}{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \gamma \right) \sigma_x^2}}$	$\frac{\frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2} + \frac{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} \left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \frac{1}{\sigma_1^2} \right)}{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \gamma \right) \sigma_x^2 + \frac{1}{\sigma_\epsilon^2}}}{\frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2} + \frac{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \frac{1}{\sigma_1^2} \right)}{\left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \gamma \right) \sigma_x^2 + \frac{1}{\sigma_\epsilon^2}}}$

It can be shown that the price efficiency is higher under the frequent regime following the logic below.

Suppose $A_1 = \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2}$, $A_2 = \frac{1}{\sigma_1^2} + \frac{1}{\sigma_x^2} \left(\frac{n}{\gamma \sigma_\eta^2} \right)^2 + \frac{n}{\sigma_\eta^2}$

$$B_1 = \frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} \left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \frac{1}{\sigma_1^2} \right), B_2 = \left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \frac{1}{\sigma_1^2} \right)^2$$

$$C = \left(\frac{1}{\left(\frac{\gamma \sigma_\eta^2}{n} \right)^2 \sigma_x^2} + \gamma \right)^2 \sigma_x^2.$$

then, the price efficiency at time 0 under the frequent regime can be written as $\frac{A_1 + \frac{B_1}{C + \frac{1}{\sigma_\epsilon^2}}}{A_2 + \frac{B_2}{C + \frac{1}{\sigma_\epsilon^2}}}$.

$$\frac{\partial}{\partial \frac{1}{\sigma_\epsilon^2}} \frac{A_1 + \frac{B_1}{C + \frac{1}{\sigma_\epsilon^2}}}{A_2 + \frac{B_2}{C + \frac{1}{\sigma_\epsilon^2}}} = -\frac{1}{\left(C + \frac{1}{\sigma_\epsilon^2} \right)^2} \frac{B_1 A_2 - A_1 B_2}{\left(A_2 + \frac{B_2}{C + \frac{1}{\sigma_\epsilon^2}} \right)^2} > 0 \quad (109)$$

since $B_1A_2 - A_1B_2 < 0$.

Proof of Lemma 7.

Let's denote expected utility of investor j at time zero as E_j^0 :

$$E_j^0 = \max E \left[E \left[-e^{-\gamma(W+(P_1-P_0)q_{0j}+(P_2-P_1)q_{1j})} \mid \Omega_{1j} \right] \mid \Omega_{0j} \right] \quad (110)$$

$$= -e^{-\gamma W} \underbrace{\min_{q_{0j}} E \left[e^{-\gamma(P_1-P_0)q_{0j}} \cdot \underbrace{\min_{q_{1j}} E \left[e^{-\gamma(P_2-P_1)q_{1j}} \mid \Omega_{1j} \right]}_{\text{Time 1 maximization}} \right]}_{\text{Time 0 maximization}} \mid \Omega_{0j} \right] \quad (111)$$

E_j^0 can be derived by plugging in equilibrium q_{j1} and q_{j0} into the utility function and taking expectation as below.

$$E_j^0 = \sqrt{\frac{\text{Var}(v_1 + v_2 - P_1 \mid \Omega_{1j})}{\text{Var}(v_1 + v_2 - P_1 \mid \Omega_{0j})}} \exp \left\{ -\frac{1}{2\text{Var}(P_1 - P_0 + h_j(v_1 + v_2 - P_1) \mid \Omega_{0j})} Y \right\}, \quad (112)$$

where

$$Y = E^2[P_1 - P_0 \mid \Omega_{0j} + 2h_j E[P_1 - P_0 \mid \Omega_{0j}] E[v_1 + v_2 - P_1 \mid \Omega_{0j}] + \frac{\text{Var}[P_1 - P_0 \mid \Omega_{0j}]}{\text{Var}[v_1 + v_2 - P_1 \mid \Omega_{0j}]} E^2[v_1 + v_2 - P_1 \mid \Omega_{0j}]].$$

The ex-ante expected utility can be derived by taking expectation of E_j^0 , or $E[E_j^0]$. Both E_j^0 and $E[E_j^0]$ can be derived by using the following formula.

$$\begin{aligned} & E[\exp\{b_1X_1 + b_2X_2 + a_{11}X_1^2 + 2a_{12}X_1X_2 + a_{22}X_2^2\}] \\ &= \frac{1}{S^{1/2}} \exp \left\{ \frac{1}{S} \left\{ \frac{1}{2} [b_1^2(\sigma_1^2 - 2a_{22}|\Sigma|) + 2b_1b_2(\sigma_{12} + 2a_{12}|\Sigma|) + b_2^2(\sigma_2^2 - 2a_{11}|\Sigma|)] \right\} \right\} \\ &+ \frac{1}{S^{1/2}} \exp \left\{ \frac{1}{S} \left\{ \mu_1 [b_1 + 2(a_{11}b_2 - a_{12}b_1)\sigma_{12} + 2(a_{12}b_2 - a_{22}b_1)\sigma_2^2] \right\} \right\} \\ &+ \frac{1}{S^{1/2}} \exp \left\{ \frac{1}{S} \left\{ \mu_2 [b_2 + 2(a_{12}b_1 - a_{11}b_2)\sigma_1^2 + 2(a_{22}b_1 - a_{12}b_2)\sigma_{12}] \right\} \right\} \\ &+ \frac{1}{S^{1/2}} \exp \left\{ \frac{1}{S} \left\{ \mu_1^2 1_{11}(1 - 2a_{22}\sigma_2^2) + 2\mu_1\mu_2(a_{12} + 2|A|\sigma_{12} + \mu_2^2 a_{22}(1 - 2a_{11}\sigma_1^2)) \right\} \right\} \quad (113) \end{aligned}$$

when $X_1 \sim \mathcal{N}(\mu_1, \sigma_1^2)$, $X_2 \sim \mathcal{N}(\mu_2, \sigma_2^2)$, $Cov(X_1, X_2) = \sigma_{12}$, and $S = |I - 2\Sigma A| = 1 - 2(a_{11}\sigma_1^2 + 2a_{12}\sigma_{12} + a_{22}\sigma_2^2) + 4|A||\Sigma|$, $|A| = a_{11}a_{22} - a_{12}^2$, and $|\Sigma| = \sigma_1^2\sigma_2^2 - \sigma_{12}^2$.

Proof of Lemma 8.

As in Lemma 7, the expected utility of investor i with information set Ω_i at time 1 gives

$$EU_i = -\exp\{-\gamma(W - c)\} \sqrt{\frac{\text{Var}[v_1 + v_2 - P_1 | \Omega_i]}{\text{Var}[v_1 + v_2 - P_1]}}. \quad (114)$$

The ratio of expected utilities for short- and long-term information under the infrequent regime is:

$$\frac{EU_1^I}{EU_2^I} = \exp(\gamma(c_1 - c_2)) \sqrt{\frac{N_I}{D_I}}, \quad (115)$$

where

$$N_I = (\sigma_2^2 \sigma_\eta^2 (\lambda_1^2 \sigma_1^2 + \lambda_x^2 \sigma_x^2) - 2\lambda_1 \lambda_2 \sigma_1^2 \sigma_2^2 \sigma_\eta^2 + \sigma_1^2 \sigma_\eta^2 (\lambda_2^2 \sigma_2^2 + \lambda_x^2 \sigma_x^2) + \lambda_x^2 \sigma_1^2 \sigma_2^2 \sigma_x^2) ((\sigma_2^2 + \sigma_\zeta^2) (\lambda_1^2 \sigma_1^2 + \lambda_2^2 \sigma_2^2 + \lambda_x^2 \sigma_x^2) - \lambda_2^2 \sigma_2^4),$$

$$\text{and } D_I = ((\sigma_1^2 + \sigma_\eta^2) (\lambda_1^2 \sigma_1^2 + \lambda_2^2 \sigma_2^2 + \lambda_x^2 \sigma_x^2) - \lambda_1^2 \sigma_1^4) (\sigma_2^2 \sigma_\zeta^2 (\lambda_1^2 \sigma_1^2 + \lambda_x^2 \sigma_x^2) - 2\lambda_1 \lambda_2 \sigma_1^2 \sigma_2^2 \sigma_\zeta^2 + \sigma_1^2 \sigma_\zeta^2 (\lambda_2^2 \sigma_2^2 + \lambda_x^2 \sigma_x^2) + \lambda_x^2 \sigma_1^2 \sigma_2^2 \sigma_x^2).$$

The ratio of expected utilities for short- and long-term information is under the frequent regime is:

$$\frac{EU_1^F}{EU_2^F} = \exp(\gamma(c_1 - c_2)) \sqrt{\frac{N_1 \cdot N_2}{D_1 \cdot D_2}} \quad (116)$$

$$\text{where } N = 1(\sigma_1^2 \sigma_2^2 \sigma_\eta^2 \sigma_\epsilon^2 (\beta_1 - \beta_2^2 + \beta_x^2 \sigma_x^2 (\sigma_1^2 \sigma_2^2 (\sigma_\eta^2 + \sigma_\epsilon^2) + \sigma_1^2 \sigma_\eta^2 \sigma_\epsilon^2 + \sigma_2^2 \sigma_\eta^2 \sigma_\epsilon^2))) \quad (117)$$

$$N_2 = (\beta_1^2 \sigma_1^2 \sigma_\epsilon^2 (\sigma_2^2 + \sigma_\zeta^2) + \beta_2^2 \sigma_2^2 \sigma_\zeta^2 (\sigma_1^2 + \sigma_\epsilon^2) + \beta_x^2 \sigma_x^2 (\sigma_1^2 + \sigma_\epsilon^2) (\sigma_2^2 + \sigma_\zeta^2)) \quad (118)$$

$$D_1 = \beta_1^2 \sigma_1^2 \sigma_\eta^2 \sigma_\epsilon^2 + \beta_2^2 \sigma_2^2 (\sigma_1^2 (\sigma_\eta^2 + \sigma_\epsilon^2) + \sigma_\eta^2 \sigma_\epsilon^2) + \beta_x^2 \sigma_x^2 (\sigma_1^2 (\sigma_\eta^2 + \sigma_\epsilon^2) + \sigma_\eta^2 \sigma_\epsilon^2) \quad (119)$$

$$D_2 = \sigma_1^2 \sigma_2^2 \sigma_\zeta^2 \sigma_\epsilon^2 (\beta_1 - \beta_2^2 + \beta_x^2 \sigma_x^2 (\sigma_1^2 \sigma_2^2 (\sigma_\zeta^2 + \sigma_\epsilon^2) + \sigma_1^2 \sigma_\zeta^2 \sigma_\epsilon^2 + \sigma_2^2 \sigma_\zeta^2 \sigma_\epsilon^2)) \quad (120)$$

Proof of Proposition 7.

Infrequent regime

Let's set $\bar{n}_I = 1$. Then, the equilibrium price is:

$$P_{1,I} = \lambda_0 + \underbrace{\lambda_1}_{0.510} v_1 + \underbrace{\lambda_2}_0 v_2 + \underbrace{\lambda_x}_{-2.587} x \quad (121)$$

Next, I verify that the above equilibrium \bar{n}_I is indeed the endogenous equilibrium.

$$EU_1^I(\bar{n}_I = 1) - EU_2^I(\bar{n}_I = 1) = 0.165 > 0 \quad (122)$$

The above relation indicates that $\bar{n}_I = 1$ is indeed an information acquisition equilibrium.

Frequent regime

Let's set $\bar{n}_F = 0$. Then, the equilibrium price is:

$$P_{1,F} = \beta_0 + \underbrace{\beta_1}_0 v_1 + \underbrace{\beta_2}_{0.772} v_2 + \underbrace{\beta_e}_{0.909} e_1 + \underbrace{\beta_x}_{-0.926} x \quad (123)$$

Next, I verify that the above equilibrium $\bar{n}_F = 0$ is indeed the endogenous equilibrium.

$$EU_1^F(\bar{n}_F = 0) - EU_2^F(\bar{n}_F = 0) = -0.014 < 0 \quad (124)$$

The above relation indicates that $\bar{n}_F = 0$ is an information acquisition equilibrium.

Comparison of the equilibrium myopia level

I plug in the equilibrium \bar{n} 's as well as the equilibrium price coefficients to obtain equilibrium operating decisions under the two regimes ($k_{1,I}^*$ and $k_{1,F}^*$).

$$k_I^* = 0.602 > k_F^* = 0.518 \quad (125)$$

Appendix B

Analysis when there exists an alternative capital use

Suppose the manager now has an investment option with an interest rate of r_t in each period $t \in \{1, 2\}$. Interest rates are common knowledge. Also, time 1 payoff can be reinvested at time 2. Now, investors form a conjecture not just on k_1 and k_2 , but also on z . As in the main model, since all investment opportunities are common knowledge, the market's conjecture in equilibrium is correct. I analyze the frequent reporting case with interim performance report without informed trading and $I > \mu_1 + \mu_2 - r_1(2 + r_2)$. With z

representing capital allocated to this new opportunity, following equations characterize the expected time 1 and time 2 firm value.

$$E[v_1] = k_1\mu_1 - \frac{k_1^2}{2} + r_1 \cdot z \quad (126)$$

$$E[v_2] = \left(k_2\mu_2 - \frac{k_2^2}{2}\right) + \left(k_1\mu_1 - \frac{k_1^2}{2} + r_1z\right) \cdot r_2 \cdot z \quad (127)$$

Prices are characterized below.

$$P_1 = E[v_1|\hat{k}_1, \hat{k}_2, \hat{z}, e_1] \cdot (1 + r_2) + E\left[k_2\mu_2 - \frac{k_2^2}{2}|\hat{k}_2\right] \quad (128)$$

$$P_2 = v_1 + v_2 = \left(k_1\mu_1 - \frac{k_1^2}{2} + r_1 \cdot z\right) \cdot (1 + r_2) + \left(k_2\mu_2 - \frac{k_2^2}{2}\right) \quad (129)$$

The manager with α solves the following program.

$$\max_{k_1, k_2, z} \alpha \cdot E[P_1] + (1 - \alpha) \cdot E[P_2] \quad (130)$$

$$\text{s.t. } k_1 + k_2 + z \leq I \quad (131)$$

Solving for the maximization problem gives the following equilibrium input into each projects.

$$k_1^* = \mu_1 - r_1 \quad (132)$$

$$k_2^* = \mu_2 - \frac{\alpha \frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2} + (1 - \alpha)}{1 - \alpha} \cdot r_1(1 + r_2) \quad (133)$$

$$z^* = I - k_1^* - k_2^* \quad (134)$$

To examine whether corporate myopia arises, I evaluate the benchmark case where the manager only cares about the liquidating firm value. The benchmark operating decision is characterized below.

$$k_1^b = \mu_1 - r_1 \quad (135)$$

$$k_2^b = \mu_2 - r_1(1 + r_2) \quad (136)$$

$$z^b = I - k_1^b - k_2^b \quad (137)$$

Comparing the equilibrium input and benchmark input indicates that the manager still engages in myopia in this setting by decreasing capital input into long-term projects. Interestingly, myopia arises in this setting even without a capital constraint. The same logic applies to the infrequent regime when there exist informed traders.

Proof of the result in Section 6.3

The notations are the same as in the baseline model.

Exogenous information acquisition

Proposition 8. *When an investor is informed, myopia is always higher under the frequent than under the infrequent regime ($k_{1,F}^* > k_{1,I}^*$).*

Proof of Proposition 8. As in the baseline model, a manager's operating choice follows below equation:

$$k_1^* = \frac{\alpha(X)\mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha(X) + 2(1 - \alpha)}, \quad (138)$$

where X is the price informativeness regarding short-term performance. To examine price efficiency under the two regimes, I derive the financial market equilibrium under a Kyle (1985) setting.

Frequent regime

I conjecture the following.

$$P_1 = E[v_1|e_1, \hat{k}_1] + \lambda_F \cdot z_F + E[v_2|\hat{k}_1] \quad (139)$$

$$q_F = \gamma_F \left(s_1 - E[v_1|e_1, \hat{k}_1] \right) \quad (140)$$

$$z_F = q_{i,F} + x = \gamma_F \left(s_1 - E[v_1|e_1, \hat{k}_1] \right) + x, \quad (141)$$

where q_F indicates the informed investor's demand at time 1 under the frequent regime and z_F indicates order flow at time 1 under the frequent regime. q_F shows that the informed investor trades based on the incremental information in their private signals given mandatory disclosure e_1 ($s_1 - E[v_1|e_1, \hat{k}_1]$). Using

Bayesian updating, P_1 is characterized as below.

$$P_1 = E[v_1|e_1, z_F, \hat{k}_1] + E[v_2|\hat{k}_1] \quad (142)$$

$$= \underbrace{\left(\hat{k}_1 \mu_1 - \frac{\hat{k}_1^2}{2} \right) + \frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2} (e_1 - E[e_1|\hat{k}_1]) + \frac{\gamma_F \frac{\sigma_1^2 \sigma_\varepsilon^2}{\sigma_1^2 + \sigma_\varepsilon^2}}{\gamma_F^2 \left(\frac{\sigma_1^2 \sigma_\varepsilon^2}{\sigma_1^2 + \sigma_\varepsilon^2} + \sigma_\eta^2 \right) + \sigma_x^2} z_F}_{E[v_1|e_1, z_F, \hat{k}_1]} \quad (143)$$

$$+ \underbrace{\left((I - \hat{k}_1) \mu_2 - \frac{(I - \hat{k}_1)^2}{2} \right)}_{E[v_2|\hat{k}_1]},$$

where z_F is the order flow under the frequent regime.

Informed investor chooses q_F after e_1 is disclosed so that q_F maximizes the expected profit.

$$\max_{q_F} E[q_F(v_1 + v_2 - P_1)|e_1, s_1] = \max_{q_F} E[q_F(v_1 - E[v_1|e_1, \hat{k}_1] - \lambda_F z_F)|e_1, s_1] \quad (144)$$

Taking FOC gives:

$$q_F^* = \frac{1}{\underbrace{2\lambda_F \frac{\sigma_1^2 \sigma_\varepsilon^2}{\sigma_1^2 + \sigma_\varepsilon^2} + \sigma_1^2 \sigma_\eta^2 + \sigma_\varepsilon^2 \sigma_\eta^2}_{\gamma_F}} (s_1 - E[v_1|e_1, \hat{k}_1]) \quad (145)$$

Solving (143) and (145) jointly gives:

$$\gamma_F = \frac{\sigma_x}{\sqrt{(\sigma_1^2 \sigma_\varepsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\varepsilon^2 \sigma_\eta^2)}} \sqrt{\sigma_1^2 + \sigma_\varepsilon^2} \quad (146)$$

$$\lambda_F = \frac{\sigma_1^2 \sigma_\varepsilon^2}{2(\sigma_1^2 \sigma_\varepsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\varepsilon^2 \sigma_\eta^2)} \frac{1}{\sigma_x} \sqrt{\frac{\sigma_1^2 \sigma_\varepsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\varepsilon^2 \sigma_\eta^2}{\sigma_1^2 + \sigma_\varepsilon^2}} \quad (147)$$

Infrequent regime

I conjecture the following.

$$P_1 = E[v_1|\hat{k}_1] + \lambda_I z_I + E[v_2|\hat{k}_1] \quad (148)$$

$$q_I = \gamma_I (s_1 - E[v_1|\hat{k}_1]) \quad (149)$$

$$z_I = q_I + x \quad (150)$$

$$= \gamma_I \left(s_1 - E[v_1|\hat{k}_1] \right) + x \quad (151)$$

where q_I indicates informed trader's demand at time 1 under the infrequent regime and z_I indicates order flow at time 1. Using Bayesian updating, P_1 is characterized as below.

$$P_1 = E[v_1|z_I, \hat{k}_1] + E[v_2|\hat{k}_1] \quad (152)$$

$$= \underbrace{\left(\hat{k}_1 \mu_1 - \frac{\hat{k}_1^2}{2} \right)}_{E[v_1|\hat{k}_1]} + \underbrace{\frac{\gamma_I \sigma_1^2}{\gamma_I^2 (\sigma_1^2 + \sigma_\eta^2) + \sigma_x^2}}_{\lambda_I} z_I + \underbrace{\left((I - \hat{k}_1) \mu_2 - \frac{(I - \hat{k}_1)^2}{2} \right)}_{E[v_2|\hat{k}_1]} \quad (153)$$

The informed investor chooses q_I that maximizes the expected profit: Simplifying the demand function gives

$$q_I^* = \frac{1}{2\lambda_I} \left[(E[v_1|s_1] - E[v_1|\hat{k}_1]) \right] \quad (154)$$

$$= \frac{1}{2\lambda_I} \underbrace{\frac{\sigma_1^2}{\sigma_1^2 + \sigma_\eta^2}}_{\gamma_I} (s_1 - E[v_1|\hat{k}_1]) \quad (155)$$

Solving (153) and (155) jointly gives:

$$\gamma_I = \frac{\sigma_x}{\sqrt{(\sigma_1^2 + \sigma_\eta^2)}}, \quad \lambda_I = \frac{\sigma_1^2}{2(\sigma_1^2 + \sigma_\eta^2)} \frac{\sqrt{(\sigma_1^2 + \sigma_\eta^2)}}{\sigma_x} \quad (156)$$

The price efficiency under infrequent and frequent regime is characterized as below.

$$X_I = \left(\frac{\sigma_1^2}{2(\sigma_1^2 + \sigma_\eta^2)} \right) \quad (157)$$

$$X_F = \left(\frac{\sigma_1^2}{\sigma_1^2 + \sigma_\epsilon^2} + \frac{\sigma_1^2 \sigma_\epsilon^2}{2(\sigma_1^2 \sigma_\epsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\epsilon^2 \sigma_\eta^2)} \cdot \frac{\sigma_\epsilon^2}{\sigma_1^2 + \sigma_\epsilon^2} \right) \quad (158)$$

X_F is strictly decreasing in σ_ϵ^2 . Also, when $\sigma_\epsilon^2 \rightarrow 0$, $X_F \rightarrow 1 > X_I$. When $\sigma_\epsilon^2 \rightarrow \infty$, $X_F \rightarrow X_I$. This indicates that the price efficiency with exogenous information acquisition is always higher under the frequent regime than under the infrequent regime. Therefore, $k_{1,F}^* > k_{1,I}^*$.

Endogenous information acquisition

Let's define the informed investor's ex-ante expected profit of observing information as Π_r , where $r \in \{F, I\}$.

$$\Pi_F = \lambda_F \sigma_x^2 = \frac{\sigma_1^2 \sigma_\varepsilon^2}{2(\sigma_1^2 \sigma_\varepsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\varepsilon^2 \sigma_\eta^2)} \sqrt{\frac{(\sigma_1^2 \sigma_\varepsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\varepsilon^2 \sigma_\eta^2)}{(\sigma_1^2 + \sigma_\varepsilon^2)}} \sigma_x \quad (159)$$

$$\Pi_I = \lambda_I \sigma_x^2 = \frac{\sigma_1^2}{2(\sigma_1^2 + \sigma_\eta^2)} \sqrt{\sigma_1^2 + \sigma_\eta^2} \sigma_x \quad (160)$$

Table B.1 summarizes the price efficiencies under the frequent and infrequent regime depending on the information acquisition cost. $\pi_{F(I)}$ indicates the expected profit of acquiring information under the frequent (infrequent) regime, where $\pi_F \leq \pi_I$.

Table 1: Comparison of price efficiency

	Frequent	Infrequent
(A) $c \leq \pi_F$	$X_F = \frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2} + \frac{\sigma_1^2 \sigma_\varepsilon^2}{2(\sigma_1^2 \sigma_\varepsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\varepsilon^2 \sigma_\eta^2)} \cdot \frac{\sigma_\varepsilon^2}{\sigma_1^2 + \sigma_\varepsilon^2}$	$X_I = \left(\frac{\sigma_1^2}{2(\sigma_1^2 + \sigma_\eta^2)} \right)$
(B) $\pi_F < c < \pi_I$	$X_F = \frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2}$	$X_I = \left(\frac{\sigma_1^2}{2(\sigma_1^2 + \sigma_\eta^2)} \right)$
(C) $\pi_I < c$	$X_F = \frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2}$	$X_I = 0$

Proposition 9. *When $c \leq \pi_F$, or $\pi_I < c$, the myopia level is higher under the frequent regime than under the infrequent regime.*

When $\pi_F < c \leq \pi_I$, the myopia level is lower (higher) under the frequent regime than under the infrequent regime when $\sigma_\varepsilon^2 > \sigma_1^2 + 2\sigma_\eta^2$.

Under cases (A) and (C), there is no difference in the information acquisition incentives under the frequent and the infrequent regime. Therefore, as in the exogenous information acquisition case, price efficiency is always higher under the frequent compared to the infrequent regime. However, under case (B), information acquisition only occurs under the infrequent regime. In this case, it is possible that corporate myopia is stronger under the less frequent regime. Consistent with the baseline model, this happens when the reporting quality is sufficiently low. I also document the same results when a single informed investor chooses the precision of his signal.

Proof of the results in Section 6.4 with voluntary disclosure

Frequent Regime

Since the voluntary disclosure signal e_1 is identical to the mandated interim report, voluntary disclosure is redundant under the frequent regime and the same equilibrium as in the previous section where a maximum number of informed investor is one takes place.

Infrequent Regime

I analyze P_1 under disclosure and nondisclosure, assuming that the investor is informed. Then, I derive the manager's equilibrium voluntary disclosure strategy.

When the manager discloses ($m = e_1$),

I conjecture the following.

$$P_{1,I}^d = E[v_1|e_1, \hat{k}_1] + \lambda_I^d \cdot z_I^d + E[v_2|\hat{k}_1] \quad (161)$$

$$q_I^d = \gamma_I^d \left(s - E[v_1|e_1, \hat{k}_1] \right) \quad (162)$$

$$z_I^d = q_I^d + x \quad (163)$$

where q_I^d indicates informed trader's demand at time 1 and z_I^d indicates order flow at time 1. Also, given disclosure of e_1 , the expected value of time 2 price $P_2^d = v_1 + v_2$ from the manager's perspective follows the equation below:

$$E[P_2^d|e_1, k_1] = E[v_1|e_1, k_1] + E[v_2|k_1]. \quad (164)$$

Jointly solving for γ_I^d, λ_I^d using bayesian updating and optimal demand q_I^d gives:

$$\gamma_I^d = \frac{\sigma_x}{\sqrt{\text{Var}(v_1|e_1)}} \sqrt{\frac{\sigma_1^2 \sigma_\epsilon^2}{\sigma_1^2 \sigma_\epsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\epsilon^2 \sigma_\eta^2}}, \quad \lambda_I^d = \frac{\sqrt{\text{Var}(v_1|e_1)}}{2\sigma_x} \sqrt{\frac{\sigma_1^2 \sigma_\epsilon^2}{\sigma_1^2 \sigma_\epsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\epsilon^2 \sigma_\eta^2}} \quad (165)$$

When the manager withholds ($m = \emptyset$),

I conjecture the following.

$$P_{1,I}^{nd} = E[v_1|\emptyset, \hat{k}_1] + \lambda_I^{nd} \cdot z_I^{nd} + E[v_2|\hat{k}_1] \quad (166)$$

$$q_I^{nd} = \gamma_I^{nd} \left(s - E[v_1|\emptyset, \hat{k}_1] \right) \quad (167)$$

$$z_I^{nd} = q_I^{nd} + x \quad (168)$$

where q_I^{nd} indicates informed trader's demand at time 1 and z_I^{nd} is the order flow at time 1. Also, the expected value of time 2 price $P_2^{nd} = v_1 + v_2$ from the manager's perspective is the same as when the manager discloses e_1 . This is because regardless of disclosure decision, the manager always knows the value of e_1 .

$$E[P_2^{nd}|e_1, k_1] = E[v_1|e_1, k_1] + E[v_2|k_1] \quad (169)$$

Using the same method as before, the coefficients can be derived using bayesian updating and the optimal demand by the informed trader. Jointly solving for these equations leads to the following.

$$\gamma_I^{nd} = \frac{\sigma_x}{\sqrt{\text{Var}(v_1|\emptyset) \frac{\sigma_1^2 \sigma_\epsilon^2}{\sigma_1^2 \sigma_\epsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\epsilon^2 \sigma_\eta^2} - \sigma_\eta^2}} \quad (170)$$

$$\lambda_I^{nd} = \frac{\sqrt{\text{Var}(v_1|\emptyset) \frac{\sigma_1^2 \sigma_\epsilon^2}{\sigma_1^2 \sigma_\epsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\epsilon^2 \sigma_\eta^2} - \sigma_\eta^2}}{2\sigma_x} \frac{\sigma_1^2 \sigma_\epsilon^2}{\sigma_1^2 \sigma_\epsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\epsilon^2 \sigma_\eta^2} \quad (171)$$

Next, I characterize the equilibrium voluntary disclosure decision by the manager at time 1. Given the manager's information set at time 1 $\{e_1, k_1\}$, the manager discloses e_1 if and only if:

$$\alpha E[P_1^d - P_1^{nd}|e_1, k_1] > c_v \quad (172)$$

Since P_1^d is increasing in e_1 , I conjecture a threshold voluntary disclosure strategy with threshold t . I assume that the manager withholds information when indifferent. Under the rational expectations

equilibrium ($k_1 = \hat{k}_1$), the equation (172) can be rewritten as:

$$\frac{\alpha}{2} \left[\frac{\sigma_1^2}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \frac{2\sigma_1^2\sigma_\eta^2 + \sigma_1^2\sigma_\varepsilon^2 + 2\sigma_\varepsilon^2 + \sigma_\eta^2 - \sigma_\varepsilon^4}{\sigma_1^2\sigma_\eta^2 + \sigma_1^2\sigma_\varepsilon^2 + \sigma_\varepsilon^2\sigma_\eta^2} \left(\frac{e_1 - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} + \frac{\phi\left(\frac{e_1 - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}}\right)}{\Phi\left(\frac{e_1 - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}}\right)} \right) \right] > c_v \quad (173)$$

The next lemma establishes the existence of the voluntary disclosure threshold when the investor is informed.

Lemma 9. *Suppose the firm is under the infrequent reporting regime with voluntary disclosure. When the trader acquires information ($N = 1$), there exists a unique threshold t , above which the manager discloses and below which the manager withholds. The equilibrium threshold t satisfies the following under the rational expectations equilibrium ($k_1 = \hat{k}_1$).*

$$\frac{\alpha}{2} \left[\frac{\sigma_1^2}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \frac{2\sigma_1^2\sigma_\eta^2 + \sigma_1^2\sigma_\varepsilon^2 + 2\sigma_\varepsilon^2 + \sigma_\eta^2 - \sigma_\varepsilon^4}{\sigma_1^2\sigma_\eta^2 + \sigma_1^2\sigma_\varepsilon^2 + \sigma_\varepsilon^2\sigma_\eta^2} \left(\frac{t - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} + \frac{\phi\left(\frac{t - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}}\right)}{\Phi\left(\frac{t - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}}\right)} \right) \right] = c_v \quad (174)$$

Proof of Lemma 9. Let's define $F(e_1) = \frac{\alpha}{2} \left[\frac{\sigma_1^2}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \frac{2\sigma_1^2\sigma_\eta^2 + \sigma_1^2\sigma_\varepsilon^2 + 2\sigma_\varepsilon^2 + \sigma_\eta^2 - \sigma_\varepsilon^4}{\sigma_1^2\sigma_\eta^2 + \sigma_1^2\sigma_\varepsilon^2 + \sigma_\varepsilon^2\sigma_\eta^2} \left(\frac{e_1 - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} + \frac{\phi\left(\frac{e_1 - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}}\right)}{\Phi\left(\frac{e_1 - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}}\right)} \right) \right] - c_v$. Note that $F(e_1)$ is strictly increasing in e_1 due to Sampford's inequality. Also, when $e_1 \rightarrow -\infty$, $F(e_1) \rightarrow -c_v$ and when $e_1 \rightarrow \infty$, $F(e_1) \rightarrow \infty$. Together, these indicate that there exists a unique value t that satisfies $F(t) = 0$.

Note that the following holds. The ex-ante expected profit of acquiring information when the manager voluntarily discloses e_1 (Π_I^d) is the following.

$$\Pi_I^d = E[(v_1 + v_2 - P_1) q_1 | m \neq \emptyset] = \frac{\sigma_x \sqrt{\text{Var}(v_1 | e_1)}}{2} \sqrt{\frac{\sigma_1^2 \sigma_\varepsilon^2}{\sigma_1^2 \sigma_\varepsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\varepsilon^2 \sigma_\eta^2}} \quad (175)$$

The ex-ante expected profit of acquiring information when the manager withholds the signal ($m = \emptyset$) is the

following.

$$\Pi_I^{nd} = E[(v_1 + v_2 - P_1) q_1 | m = \emptyset] = \frac{\sigma_x \sqrt{\text{Var}(v_1 | \emptyset) \frac{\sigma_1^2 \sigma_\epsilon^2}{\sigma_1^2 \sigma_\epsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\epsilon^2 \sigma_\eta^2} - \sigma_\eta^2}}{2} \frac{\sigma_1^2 \sigma_\epsilon^2}{\sigma_1^2 \sigma_\epsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\epsilon^2 \sigma_\eta^2} \quad (176)$$

$$= \frac{\sigma_x \sqrt{(\text{Var}(v_1 | e_1) + (\text{Var}(v_1 | \emptyset) - \text{Var}(v_1 | e_1))) \frac{\sigma_1^2 \sigma_\epsilon^2}{\sigma_1^2 \sigma_\epsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\epsilon^2 \sigma_\eta^2} - \sigma_\eta^2}}{2} \frac{\sigma_1^2 \sigma_\epsilon^2}{\sigma_1^2 \sigma_\epsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\epsilon^2 \sigma_\eta^2} \quad (177)$$

$$= \frac{\sigma_x \sqrt{\text{Var}(v_1 | e_1) + (\text{Var}(v_1 | \emptyset) - \text{Var}(v_1 | e_1)) \frac{\sigma_1^2 \sigma_\epsilon^2}{\sigma_1^2 \sigma_\epsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\epsilon^2 \sigma_\eta^2}}}{2} \sqrt{\frac{\sigma_1^2 \sigma_\epsilon^2}{\sigma_1^2 \sigma_\epsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\epsilon^2 \sigma_\eta^2}} > \Pi_I^d \quad (178)$$

Lemma 9 pins down the ex-ante expected benefit of acquiring information under the infrequent regime. The informed trader acquires information at time 0 if and only if the information acquisition cost c is lower than or equal to the expected benefit under infrequent regime with voluntary disclosure Π_I^v .

$$c \leq \Pi_I^v = \Phi\left(\frac{t - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\epsilon^2}}\right) \Pi_I^{nd} + \left(1 - \Phi\left(\frac{t - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\epsilon^2}}\right)\right) \Pi_I^d \quad (179)$$

Next, I characterize the price equations and the manager's operating decision depending on the investor's information acquisition decision.

Case 1: $c \leq \Pi_I^v$

When $c \leq \Pi_I^v$, then the investor acquires information s at a cost c . Then the following price equations hold, whose coefficients satisfy (165), (170) and (171).

$$P_1 = E[v_1 | \hat{k}_1, m] + \lambda_I^j \left(\gamma_I^j (s - E[v_1 | \hat{k}_1, m]) + x \right) + E[v_2 | \hat{k}_1] \quad (180)$$

$$P_2 = v_1 + v_2 \quad (181)$$

where $j \in \{d, nd\}$

When making an operating decision at time 0, the manager solves the following.

$$\max_{k_1} \alpha E[P_1] + (1 - \alpha) E[P_2] \quad (182)$$

Case 2 : $c > \Pi_I^v$

When $c > \Pi_I^v$, or when $N = 0$, then voluntary disclosure is the only source of information under the infrequent regime. The following price equations hold.

$$P_1 = E[v_1|m, \hat{k}_1] + E[v_1|\hat{k}_1] \quad (183)$$

$$P_2 = v_1 + v_2 \quad (184)$$

When there is no informed trading, the below Lemma shows the existence of a threshold voluntary disclosure T .

Lemma 10. *Suppose the firm is under an infrequent reporting regime with voluntary disclosure. When the investor does not acquire information, there exists a unique threshold T , above which the manager discloses and below which the manager withholds. The equilibrium threshold T satisfies the following under the rational expectations equilibrium ($k_1 = \hat{k}_1$).*

$$\alpha \left[\frac{\sigma_1^2}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \left(\frac{T - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} + \frac{\phi \left(\frac{T - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \right)}{\Phi \left(\frac{T - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \right)} \right) \right] = c_v \quad (185)$$

Proof of Lemma 10. The proof of Lemma 10 follows the same logic as in Lemma 9.

Using the voluntary disclosure thresholds in Cases 1 and 2, I derive the myopia level when the investor is informed and when the investor is not informed.

Lemma 11. *Suppose the firm is under the infrequent mandatory reporting regime with voluntary disclosure. When $c \leq \Pi_I^v$ such that informed trader acquires information, a manager with α chooses the minimum of I and the following:*

$$\frac{\alpha \left(\Phi \left(\frac{t - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \right) \cdot X + \left(1 - \Phi \left(\frac{t - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \right) \right) \cdot \left(\frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2} + \frac{\sigma_\varepsilon^2}{\sigma_1^2 + \sigma_\varepsilon^2} \cdot X \right) \right) \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha \left(\Phi \left(\frac{t - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \right) \cdot X + \left(1 - \Phi \left(\frac{t - E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \right) \right) \cdot \left(\frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2} + \frac{\sigma_\varepsilon^2}{\sigma_1^2 + \sigma_\varepsilon^2} \cdot X \right) \right) + 2(1 - \alpha)},$$

where $X = \frac{\sigma_1^2 \sigma_\varepsilon^2}{2(\sigma_1^2 \sigma_\varepsilon^2 + \sigma_1^2 \sigma_\eta^2 + \sigma_\varepsilon^2 \sigma_\eta^2)}$.

When $c > \Pi_I^v$ such that informed trader does not acquire information, a manager with α chooses

$$k_{1,I}^* = \min \left\{ \frac{\alpha \left(1 - \Phi \left(\frac{T-E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \right) \cdot \left(\frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2} \right) \right) \mu_1 + (1 - \alpha)(I - \mu_2 + \mu_1)}{\alpha \left(1 - \Phi \left(\frac{T-E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \right) \cdot \left(\frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2} \right) \right) + 2(1 - \alpha)}, I \right\}.$$

Table B.2 summarizes the price efficiency at time 1 under the frequent and infrequent regime depending on the information acquisition cost. Π_F and Π_I^v indicate the expected profit of acquiring information under the frequent regime and under the infrequent regime with voluntary disclosure. Since the myopia level directly depends on the price efficiency at time 1, comparing short-term capital input amount is equivalent to comparing time 1 price efficiency.

Table 2: Comparison of time 1 price efficiency

	Frequent	Infrequent
(A) $c \leq \Pi_F$	$\frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2} + X \frac{\sigma_\varepsilon^2}{\sigma_1^2 + \sigma_\varepsilon^2}$	$\Phi \left(\frac{t-E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \right) X + \left(1 - \Phi \left(\frac{t-E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \right) \right) \left(\frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2} + \frac{\sigma_\varepsilon^2}{\sigma_1^2 + \sigma_\varepsilon^2} X \right)$
(B) $\Pi_F < c < \Pi_I^v$	$\frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2}$	$\Phi \left(\frac{t-E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \right) X + \left(1 - \Phi \left(\frac{t-E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \right) \right) \left(\frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2} + \frac{\sigma_\varepsilon^2}{\sigma_1^2 + \sigma_\varepsilon^2} X \right)$
(C) $\Pi_I^v < c$	$\frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2}$	$\left(1 - \Phi \left(\frac{T-E[e_1]}{\sqrt{\sigma_1^2 + \sigma_\varepsilon^2}} \right) \right) \left(\frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2} \right)$

Note that when $N_I = N_F$ (cases (A) and (C)), the price efficiency is always higher under the frequent regime since $X < \frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2}$ and thus $X < \frac{\sigma_1^2}{\sigma_1^2 + \sigma_\varepsilon^2} + \frac{\sigma_\varepsilon^2}{\sigma_1^2 + \sigma_\varepsilon^2} \cdot X$. On the contrary, under case (B), $N_I = 1$ and $N_F = 0$. Therefore, the price efficiency at time 1 can be higher under the infrequent regime when the voluntary disclosure cost c_v is sufficiently low. This is because the price efficiency decreases with c_v , and at the extreme when $c_v = 0$, the price efficiency under the infrequent regime is strictly higher than that under the frequent regime. This confirms the result in the baseline model with informed trading only that there exist cases where reducing the reporting frequency can increase short-term oriented operating decisions.

Next, I examine 1) the effect of the voluntary disclosure cost on myopia given an exogenous number of informed investors and 2) the effect of the voluntary disclosure cost on investors' information acquisition incentives.

Proposition 10. *Given an exogenous number of informed investors,*

a) *the corporate myopia level under the infrequent regime $k_{1,I}^*$ decreases with the voluntary disclosure cost*

c_v , and

b) the difference between the corporate myopia level under the two regimes $k_{1,F}^* - k_{1,I}^*$ increases with the voluntary disclosure cost c_v .

Proof of Proposition 10. The change in c_v only affects $k_{1,I}^*$. Since higher c_v decreases voluntary disclosure it decreases $k_{1,I}^*$. Therefore, $k_{1,F} - k_{1,I}^*$ increases with c_v .

Proposition 11. The increase in c_v does not affect the range of parameter c corresponding to case (A), increases the range corresponding to case (B), and decreases the range corresponding to case (C).

Proof of Proposition 11. Π_I^v is increasing in c_v , since higher value of c_v reduces the probability of voluntary disclosure under the infrequent regime. As c_v increases, Π_I^v increases while Π_F does not change with c_v . Therefore, the interval for case (B) increases.

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