Persistent charge-density-wave order in single-layer TaSe₂

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Abstract

We present the electronic characterization of single-layer 1*H*-TaSe₂ grown by **molecular beam epitaxy (MBE) using a combined angle-resolved photoemission spectroscopy (ARPES), scanning tunneling microscopy/spectroscopy (STM/STS), and density functional theory (DFT) calculations. We demonstrate that 3×3 CDW order persists despite distinct changes in the low energy electronic structure** highlighted by the reduction in the number of bands crossing the Fermi energy (E_F) **and the corresponding modification of Fermi surface (FS) topology. Enhanced spinorbit coupling and lattice distortion in the single-layer limit play a crucial role in the formation of CDW order. Our findings provide a deeper understanding of the nature of CDW order in the 2D limit.**

Table of Contents Graphic

Keywords

Transition metal dichalcogenides, 2D materials, TaSe2, charge density wave, CDW, MBE,

ARPES, STM

2D materials, such as graphene, boron nitride, and TMDs host novel electrical, optical, and topological properties that differ from their bulk forms¹⁻³ and thus provide an ideal platform to study the effects of reduced dimensionality on the electronic ground states of many-body systems. In some TMDs, such as $2H$ -TaSe₂, $2H$ -NbSe₂, $1T$ -TiSe₂, and $1T$ -TaS₂, collective electronic phases such as CDW order and superconductivity can even coexist⁴. Reducing thickness down to a few layers allows interlayer interactions to be removed and provides vertical quantum confinement, enabling 2D collective interactions to be isolated and new quantum phases to arise. Such dimensional control provides a new means of probing the origin of CDW formation in metallic TMDs as well as the interplay of the CDW order with co-existing phases such as superconductivity⁵.

Early work on bulk TMDs suggested the CDW instability arises from FS nesting, a straightforward extension of Peierls' scheme to 2D systems⁶. However, this description has been challenged by ARPES studies^{7, 8} and electronic structure calculations⁹, creating some controversy over the origin of the CDW in 2D TMD layers⁴. Alternative explanations, such as a saddle point (van Hove singularity) mechanism as well as electron-phonon coupling have been proposed¹⁰. While recent spectroscopic^{11, 12}, optical¹³, and transport¹⁴ studies on $single-layer$ $1H-NbSe₂$ were successful in observing significant suppression of superconductivity, they show contrasting results regarding CDW formation. The origin of this discrepancy is still debated.

2H-TaSe₂ provides an ideal material to investigate CDW formation in 2D TMDs without the complication of co-existing superconductivity, since superconductivity is almost completely suppressed with a transition temperature of $T_C \sim 0.2 \text{ K}^{15}$. There exist two CDW transitions in the bulk form of TaSe₂, both having higher transition temperatures compared to other TMDs. A normal-to-incommensurate CDW transition occurs at T_{N-IC} 122 K, followed by an incommensurate to commensurate CDW transition at $T_{\text{IC-CC}} \sim 90$ K.

Here we present combined ARPES/STM spectroscopy and DFT simulation indicating that when TaSe₂ thickness is reduced from bulk to single-layer the electronic band structure changes significantly due to a reduced number of bands crossing E_F in the normal state. Despite this evolution in electronic properties, however, the CDW remains unchanged. Reduced dimensionality appears to have no significant effect on either the 3×3 symmetry or T_{N-IC} . These results suggest that the CDW instability in single-layer 1*H*-TaSe₂ likely arises from electron-phonon coupling rather than FS nesting or a saddle point mechanism.

Figure 1. Growth of epitaxial single-layer 1H-TaSe₂ film. (a) Crystal structure of 1H-

TaSe₂ single-layer film on bilayer graphene over $6H-SiC(0001)$ from top view and (**b**) side view. (**c**) RHEED pattern of epitaxial bilayer graphene on 6H-SiC(0001) substrate and (**d**) 0.9 monolayer (ML, 0.9 ML means that 90% area of the substrate surface was covered by $\sin \theta$ = layer TaSe₂) 1*H*-TaSe₂ film. (**e**) LEED pattern of 0.9 ML 1*H*-TaSe₂ film. (**f**) Corelevel spectra of $1H$ -TaSe₂ single-layer taken at $15 K$ with $80 eV$ photon energy. (**g**) Largescale STM image of 0.9 ML 1H-TaSe₂/BLG (V_b = 1 V, I_t = 1 pA, T = 5 K). (**h**) Atomically resolved STM image of single-layer 1*H*-TaSe₂ shows 3x3 CDW order (V_b = 50 mV, I_t = 180 pA, $T = 5 K$).

Figs. 1a and b show the crystal structure of single-layer $TaSe_2$, which consists a layer of Ta atoms sandwiched between two layers of Se atoms in a trigonal prismatic coordination. The substrate is bilayer graphene (BLG) terminated 6H-SiC(0001). Sharp reflection high-energy electron diffraction (RHEED) patterns for single-layer film of $TaSe₂$ (Fig. 1d) indicate the high quality of films growing in a layer-by-layer mode. BLG diffraction spots observed in submonolayer $TaSe_2$ films (Fig. 1c) disappear when the $TaSe_2$ film coverage reaches a single layer. The low energy electron diffraction (LEED) pattern observed for single-layer TaSe₂ films (Fig. 1e) aligns well with the BLG diffraction pattern, indicating that $T\alpha$ Se₂ has the same lattice orientation as the substrate. The angle-integrated core level spectrum (Fig. 1f) displays sharp characteristic peaks for Ta and Se, demonstrating the purity of the TaSe₂ film as well as consistency with previous reports on bulk samples¹⁶. Fig. 1g shows a large scale STM image illustrating the typical morphology of the single-layer TaSe₂ films. A zoom-in of the STM topography obtained at 5 K (Fig. 1h) exhibits a clear 3×3 CDW superlattice, the same as seen in bulk TaSe₂ single crystals¹⁵.

Figure 2. Electron band structure and Fermi surface of TaSe2. (**a**) ARPES and (**b**) calculated Fermi surface (FS) map in normal state (150 K). (**c**) ARPES and (**d**) calculated FS in CDW state (15 K). Solid lines in **a** and **c** mark the 2D Brillouin zone of TaSe₂. Insets at the right bottom corner in (**c**) and (**d**) are the region marked by yellow dotted square around Γ with different color scale to display the low intensity features better. Calculated band structure and Fermi surface of normal-state TaSe₂ in its (e, f) bulk form with spinorbit coupling (SOC), (**g, h**) single layer form without SOC, and (**i, j**) single layer form with SOC.

To investigate the electronic structure of single-layer TaSe₂, we first focus on the FS topology measured by *in situ* ARPES. Fig. 2 shows ARPES FS maps at temperatures above (Fig. 2a) and below (Fig. 2c) the CDW transition temperature, along with the simulated FS using DFT for the normal state (Fig. 2b) and CDW state (Fig. 2d). The calculated FS map

in CDW state is obtained from the unfolded band structures at chemical potential of -50 meV potentially due to the substrate effect. Since there is no detailed study on the interface structure between $T\alpha$ Se₂ and graphene, we tested the substrate effect using several possible arrangements in our calculations. This yields that the chemical potential is always shifted downwards consistently, with the amount of energy shift dependent on the assumed structures. The FS of single-layer TaSe₂ in the normal state (Figs. 2a and b) is similar to the FS of bulk TaSe₂^{17, 18} in that it displays circular hole pockets around the Γ and K points and a dogbone-shaped electron pocket around the M points, but there is a significant difference. In contrast to bulk TaSe₂, the Γ point hole pocket and the M point electron pocket of single-layer TaSe₂ are not separated. This is due to a single band crossing E_F along the Γ-M direction, as a result of the reduced number of bands, from two to one, when TaSe₂ thickness is reduced to a single layer (Figs. 2e - j). The reduced number of bands crossing E_F and the resulting changes in FS are similar to what is seen for single-layer $NbSe₂¹¹$. Our ARPES results are consistent with our calculation (Fig. 2b) as well as previous theoretical report 18 .

The FS topology of TaSe₂ in the CDW state (Figs. 2c and d) also exhibits noticeable deviation from bulk TaSe₂. For example, the small triangular pocket seen previously around the K points is not observed in single-layer $TaSe_2^{17, 19}$. Instead, a circular hole pocket is observed, similar to what is seen in the normal state. The absence of a triangular pocket around the K point is consistent with our calculated FS in the CDW state (Fig. 2d). Another important aspect of the FS topology in the CDW phase is that we clearly observe an extra

circular pocket around the Γ point (Inset of Fig. 2c) resulting from the folded bands, which has not been reported in the experimental FS of bulk $\text{TaSe}_2^{\{17,19\}}$. Our calculations suggest that enhanced amplitude of the lattice distortion in the CDW phase for the single-layer causes the absence of the triangular K pocket as well as the presence of band-folding around the Γ point (Inset of Fig. 2d).

We also find that spin-orbit coupling (SOC) plays a crucial role in determining the observed electronic structure and FS topology of single-layer TaSe₂. DFT calculations performed without (Figs. 2g and h) and with (Figs. 2i and j) SOC yields very different results. Without SOC only a single band crosses E_F along the Γ -K-M direction, very similar to what is seen for single-layer $NbSe₂¹¹$. Inclusion of SOC, however, splits this band into two, thus separating the dogbone-shaped pocket around the M point. Our ARPES results are best explained by the calculation that includes SOC, implying that SOC plays a key role in determining the electronic structure of single-layer TaSe₂.

Figure 3. Electronic structure of single-layer TaSe₂ along high symmetry directions. ARPES spectra of normal-state (150 K) single-layer TaSe₂ along (a) Γ-M, (b) Γ-K, and (c) M-K directions compared with (**d**-**f**) calculated band structure. Red and blue bands in **d**-**f** denote Ta *d* and Se *p* orbital character, respectively. ARPES spectra of single-layer TaSe₂ in CDW state (T=15 K) along (**g**) Γ-M, (**h**) Γ-K, and (**i**) M-K directions compared to (**j**-**l**) calculated band structure. Insets at the right bottom corner in (**c**, **g**-**i**) are the secondderivative ARPES spectra of the region marked by yellow dotted square around Γ to enhance the visibility of low intensity features. Position C in **h** indicates saddle point along Γ-K direction located ~0.25 eV below E_F .

To further understand the electronic structure of single-layer TaSe₂, ARPES spectra along the high symmetry directions were measured at temperatures both above and below the CDW transition temperature (Fig. 3). The ARPES spectra in the normal state (Figs. 3ac) are consistent with the reduced number of bands crossing E_F along the Γ-M direction, and nicely match our calculated band structure (Figs. 3d-f). The features near $E < -1$ eV, which arises mainly from the Se *p* state, show some discrepancy between theory and experiment, likely due to the ill-description of electron correlations in LDA/GGA exchange correlation functional. The binding energy Se *p* band is indeed reasonably described by employing the mBJ method^{20, 21} for bulk TaSe₂ (SI Fig. S2).

Fig. 3 also shows the measured ARPES band structures below the CDW transition temperature (Fig. 3g-i) as well as the DFT-calculated band structure including the 3×3 CDW-modulated supercell (Fig. 3j-l). The calculated bands are unfolded into a primitive cell from the fully relaxed $3\times3\times1$ CDW-modulated supercell (see SI). The ARPES data and the calculated band structures show reasonable agreement in the dispersive band width and the binding energy of the Ta *d* orbital. The folded bands (i.e. the weak intensity spectra) around Γ and M for *E* - *E*^F > -0.5 eV are observed in ARPES and nicely reproduced in the calculation.

Figure 4. Temperature dependent band gap in single-layer TaSe₂ from ARPES. Temperature dependent EDCs at momentum positions (**a**) A and (**b**) B marked in Fig. 2**a**. Red tick marks indicate the peaks from which the gap is estimated. The EDCs have been divided by the Fermi-Dirac distribution function at corresponding temperatures to eliminate the effect of thermal broadening (see SI). (**c)** Band gap evolution with temperature shows BCS-like behavior.

To investigate the evolution of electronic structure as temperature is varied across the CDW transition temperature, temperature-dependent ARPES measurements were performed at the positions A and B of Fig. 2a. Energy gap values were determined by fitting peaks to the energy distribution curves (EDCs) and are indicated by red tick marks. The curves in Fig. 4a clearly show the temperature-dependent CDW gap opening at position A, whereas no gap is detected at position B. The single-layer CDW gap at $T = 15$ K is estimated to be 100 ± 13 meV, slightly larger than the bulk CDW gap measured previously to lie in the range 12 meV $\leq E_{\text{gap}} \leq 80$ meV via ARPES, STS and optical spectroscopy^{4, 8,} ^{17, 19}. The single-layer TaSe₂ coupling ratio, $2\Delta/k_BT_{\text{N-IC}}$, is thus seen to be 17.85, much larger than the value of 3.52 obtained by mean-field theory for weak-coupled CDW as well as the experimental values of 6.4 and 11 obtained for bulk $TaSe_2$ ^{17, 19}. Fig. 4c shows the square of the measured CDW gap as a function of temperature, which is seen to closely follow a BCS gap equation²². The gap value decreases with increasing temperature until it reaches 0 at $T \sim 130$ K, thus yields a transition temperature of $T_{\text{N-IC}} = 130 \pm 5$ K for the transition from the normal phase to the ICDW phase of single-layer $T\alpha\text{Se}_2$. This is slightly larger than the value of $T_{\text{N-IC}} = 122 \text{ K}$ measured for bulk TaSe_2^2 . TaSe₂ thus exhibits the same general trend as $NbSe₂$ in that it displays a robust CDW transition even in single layer

 $limit¹¹$.

Figure 5. STS characterization of CDW state in single-layer TaSe₂. (a) Wide-bias STM dI/dV spectrum of single-layer TaSe₂ ($f = 401$ Hz, $I_t = 10$ pA, $V_{RMS} = 10$ mV, $T = 5K$). (b) Topographic image of single-layer TaSe₂ shows 25×25 grid where low-bias d*I*/d*V* spectra were obtained. **(c)** Low-bias dI/dV spectrum of single-layer TaSe₂ (average of spectra obtained over 25×25 grid shown in **(b)** ($f = 401$ Hz, $I_t = 100$ pA, $V_{RMS} = 1$ mV, $T = 5K$). STS partial gap width is $2\Delta_{\text{STS}} = 15.3 \pm 3.5$ meV (see SI).

STM/STS is complementary to ARPES in that it provides real-space identification of CDW order and related modification of low-energy electronic structure²⁴⁻²⁶. Fig. 5a shows a typical STM d*I*/d*V* spectrum of single-layer TaSe₂ acquired over a large bias range. In the filled state regime ($V < 0$) the spectrum is relatively flat and featureless until $V = -1$ V is reached, where a steep rise in d*I*/d*V* is seen as voltage is lowered. This is consistent with

our ARPES results since the local density of states (LDOS) for bands centered at *k*-values far from Γ (-0.5 eV $\leq E \leq 0$) is expected to be low, whereas the LDOS for bands centered at Γ (-0.5 eV < E < 0) is expected to be high^{27, 28}. The dominant feature in the empty state regime is a broad peak centered at $E \approx -0.5$ eV, likely due to a van Hove singularity at Γ in the conduction band¹⁸. A slight dip is seen at E_F . Overall, the wide-energy single-layer TaSe₂ spectrum of Fig. 5a is similar to what is seen for single-layer NbSe₂³.

In order to better understand the low-energy electronic structure TaSe₂, we performed more highly-resolved d/dV spectroscopy in the range -100 meV $V < V < +100$ meV. d/dV spectra were obtained on a 25×25 grid spread over a 20 Å × 20 Å region of the surface as shown in Fig. 5b. The average of theses spectra is shown in Fig. 5c (individual point spectra are shown in SI). A clear partial gap is observed that is centered at E_F ($V=0$) and has width $2\Delta_{\rm STS}$ = 15.3 \pm 3.5 meV (see SI). A partially-opened STS gap is consistent with our ARPES measurements, as STS integrates over the contribution of all *k* points in reciprocal space, some of which are gapped (e.g., point A in Fig. 2a) and some of which are not (e.g., point B in Fig. 2a). In comparison to the CDW gap size of $\Delta = 100 \pm 13$ meV measured at the single k point A by ARPES, the reduced STS gap size suggest that the momentumintegrated STS spectrum is modified by the low-energy dispersion of in-gap states.

Our results allow us to draw some conclusions regarding the origin of the CDW instability of single-layer TaSe₂. First we note that FS nesting can be ruled out due to incompatibility between nesting (q_N) and CDW (q_{CDW}) wavevectors. Our results show that the CDW *q* for single-layer TaSe₂ is $q_{CDW} = (1/3, 0, 0)$ whereas the geometric nesting of

the single-layer FS occurs at $q_N = (1/3, 1/3, 0)$ (similar to bulk TaSe₂⁹). Single-layer TaSe₂, however, does exhibit gaps at different points along the FS, suggesting that FS nesting is not a necessary condition for CDW gap-opening.

Our data also indicates that a saddle point (van Hove singularity) mechanism¹⁰ is not a suitable explanation for the origin of the CDW instability in T_0S_2 . The saddle point mechanism predicts that the CDW gap will be centered at the saddle point along Γ-K (point C in Fig. 3h) which is located ~ 0.25 eV below E_F . However, our spectroscopic results indicate that the CDW gap is centered at the Fermi level. Our DFT calculations, consistent with previous report¹⁸, reveal that both electron-phonon coupling constant and electronic susceptibility in single-layer TaSe₂ are much enhanced at q_{CDW} , suggesting that strong momentum-dependent electron-phonon coupling is the likely driving force of the CDW order.

In conclusion, we have explored how dimensionality affects the CDW instability and electronic structure of in TaSe₂. Although single-layer TaSe₂ films exhibit different electronic structure compared to bulk TaSe₂, the 3×3 CDW order remains unchanged from the bulk case. We find that SOC and enhanced lattice distortion play an important role in the electronic structure of single-layer TaSe₂. These results suggest that the electronphonon coupling rather than Fermi surface nesting or a saddle-point-based mechanism is the origin of CDW order in this material class.

Experimental Section

Thin film growth and ARPES. 1*H*-TaSe₂ was grown by MBE (base pressure 2×10^{-10}) Torr) on epitaxial BLG^{29} on 6H-SiC(0001) and transferred directly into the ARPES analysis chamber (base pressure 3×10^{-11} Torr) for the measurement at the HERS endstation of Beamline 10.0.1, Advanced Light Source, Lawrence Berkeley National Laboratory. High purity Ta (99.9%) and Se (99.999%) were evaporated from an e-beam evaporator and a standard Knudsen cell, respectively, with flux ratio Ta:Se = 1:3 and substrate temperature 550 ℃ . This yields the growth rate of ~20 min per single-layer monitored by *in-situ* RHEED. The ARPES system was equipped with a Scienta R4000 electron analyzer. The photon energy was set at 55 eV with energy and angular resolution of 25 meV and 0.1 degree, respectively. Se capping layers \sim 10 nm were deposited onto single-layer 1*H*-TaSe₂ film at room temperature to prevent the contamination during transport through air to the ultrahigh vacuum scanning tunneling microscopy (UHV-STM) chamber. Se capping layers were removed by annealing the sample to \sim 520 K overnight in the UHV STM system before the STM/STS measurement.

RHEED, LEED, and large scale STM measurements were performed on 0.9 ML TaSe, sample in order to display the nature of the growth by showing the regions in which graphene, monolayer $TaSe_2$, and bilayer $TaSe_2$ coexist. The actual ARPES measurements were performed on 0.7 ML TaSe₂, which allows us to obtain only monolayer and graphene signal, since bilayer TaSe, starts to grow after \sim 70% of the substrate area is covered by monolayer. The ARPES signal from graphene near Fermi energy is isolated around the Kpoints of graphene, which exist at larger momenta than the first Brillouin zone boundary

of TaSe₂. Therefore, the low energy electronic structures measured by ARPES from graphene and from TaSe, do not interfere each other, allowing us to obtain ARPES spectra only from TaSe₂.

 STM/STS measurement: STM/STS measurements were performed using a commercial Omicron LT-STM/AFM under UHV conditions at $T = 5$ K with tungsten tips. STM topography was obtained in constant-current mode. STM tips were calibrated on a Au(111) surface by measuring the Au(111) Shockley surface state before all STS measurements. STS was performed under open feedback conditions by lock-in detection of an alternating-current tunnel current with a small bias modulation at 401 Hz added to the tunneling bias. WSxM software was used to process the STM images.

 Electronic structure calculation. For density functional theory (DFT) band calculations, we employed the *ab-initio* full-potential method implemented in Wien2k. The Vienna ab-initio simulation package (VASP) was also used for the band-unfolding³⁰ and structural relaxation. The generalized-gradient approximation (GGA) was utilized for the exchange-correlation potential. The electronic charge density was evaluated up to the kinetic energy cut-off of 600 eV. The Brillouin-zone (BZ) integration for self-consistent calculations was carried out with 20×20×6 *k*-points. SOC was included in the second variation manner. The Hellmann-Feynman force scheme was used for structural optimization. For the single-layer calculations, the distance of the out-of-plane is fixed at $c = 15$ Å, much larger than its natural value, in order to isolate one layer from the adjacent layers.

Supporting Information

Electronic structure calculation, Single-layer TaSe2 STS gap determination, Single-layer TaSe2 ARPES bandgap determination, Mean field behavior of the temperature dependent gap

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