

1 ***Title:***

2

3 **Towards a universal model for carbon dioxide uptake by plants**

4

5 ***Authors:***

6

7 Han Wang^{1,2,3*}, I. Colin Prentice^{1,2,4}, Trevor F. Keenan^{2,5}, Tyler W. Davis^{4,6}, Ian J. Wright², William K.
8 Cornwell⁷, Bradley J. Evans^{2,8} and Changhui Peng^{1,9*}

9

10 ***Affiliations:***

11 ¹ State Key Laboratory of Soil Erosion and Dryland Farming on the Loess Plateau, College of Forestry,
12 Northwest A & F University, Yangling 712100, Shaanxi, China

13 ² Department of Biological Sciences, Macquarie University, North Ryde, NSW 2109, Australia

14 ³ Ecosystems Services and Management Program, International Institute for Applied Systems Analysis,
15 Laxenburg, A-2361, Austria

16 ⁴ AXA Chair of Biosphere and Climate Impacts, Department of Life Sciences, Imperial College
17 London, Silwood Park Campus, Buckhurst Road, Ascot SL5 7PY, UK

18 ⁵ Earth Sciences Division, Lawrence Berkeley National Laboratory, 1 Cyclotron Road, Berkeley, CA
19 94720, United States

20 ⁶ United States Department of Agriculture-Agricultural Research Service, Robert W. Holley Center for
21 Agriculture and Health, Ithaca, NY 14853, United States

22 ⁷ Ecology and Evolution Research Centre, School of Biological, Earth and Environmental Sciences,
23 The University of New South Wales, Randwick, NSW 2052, Australia

24 ⁸ Faculty of Agriculture and Environment, Department of Environmental Sciences, The University of
25 Sydney, NSW 2006, Australia

26 ⁹ Department of Biological Sciences, Institute of Environmental Sciences, University of Quebec at
27 Montreal, C.P. 8888, Succ. Centre-Ville, Montréal H3C 3P8, Québec, Canada

28

29 ***Manuscript type:*** Letter

30

31 ****Correspondence to:***

32 H Wang: wanghan_sci@yahoo.com, C Peng: peng.changhui@uqam.ca

34 **Gross primary production (GPP) – the uptake of CO₂ by leaves, and its conversion to sugars by**
35 **photosynthesis – is the basis for life on land. Earth System Models (ESMs) incorporating the**
36 **interactions of land ecosystems and climate are used to predict the future of the terrestrial sink**
37 **for anthropogenic carbon dioxide (CO₂)¹. ESMs require accurate representation of GPP. But**
38 **current ESMs disagree on how GPP responds to environmental variations^{1,2}, suggesting a need**
39 **for a more robust theoretical framework for modelling^{3,4}. Here we focus on a key quantity for**
40 **GPP, the ratio of leaf-internal to external CO₂ (χ). χ is tightly regulated and depends on**
41 **environmental conditions, but is represented empirically and incompletely in today’s models. We**
42 **show that a simple evolutionary optimality hypothesis^{5,6} predicts specific quantitative**
43 **dependencies of χ on temperature, vapour pressure deficit and elevation; and that these same**
44 **dependencies emerge from an independent analysis of empirical χ values, derived from a**
45 **worldwide data set of > 3500 leaf stable carbon isotope measurements. A single global equation**
46 **embodying these relationships then unifies the empirical light use efficiency (LUE) model⁷ with**
47 **the standard model of C₃ photosynthesis⁸, and successfully predicts GPP measured at eddy-**
48 **covariance flux sites. This success is notable given the equation’s simplicity and broad**
49 **applicability across biomes and plant functional types. It provides a theoretical underpinning for**
50 **the analysis of plant functional co-ordination across species and emergent properties of**
51 **ecosystems, and a potential basis for the reformulation of the controls of GPP in next-generation**
52 **ESMs.**

53 The standard model⁸ accurately describes the instantaneous environmental and physiological controls
54 of photosynthesis, whereas empirical LUE models can predict primary production over weeks to
55 months^{7,9} (Supplementary Information). The connection between these parallel modelling frameworks
56 remains unresolved⁹. Both require independent information to be provided: leaf-internal CO₂ partial
57 pressure (c_i) and photosynthetic capacities for carboxylation and electron transport (V_{cmax} and J_{max}) in
58 the Farquhar model, and environmental response functions in LUE models. There is no accepted
59 general way to do this for large-scale modelling^{10,11}, and as a result, different implementations of
60 apparently the same model can give very different answers in different ESMs.

61 The biochemical reactions of photosynthesis depend on the value of c_i ^{8,12}. CO₂ diffuses into
62 leaves through the stomata (microscopic pores in the leaf surface) towards the chloroplasts, where
63 reducing power derived from solar energy is used to assimilate CO₂ into organic forms through the
64 Calvin cycle. The term c_i refers to the partial pressure of CO₂ in the intercellular space, which is lower
65 than the ambient CO₂ partial pressure (c_a) while photosynthesis is active due to the resistance imposed
66 by the stomata. The term c_c (applying at the chloroplasts, where carbon fixation occurs) is generally
67 even smaller than c_i due to additional resistance to CO₂ transport in the mesophyll (a point that we
68 return to later) but most current models disregard this additional drawdown of CO₂. Thus, given
69 knowledge of c_a , the quantity $\chi = c_i/c_a$ becomes a key modelling target. χ is tightly regulated by the fast
70 (time scale of minutes) responses of both photosynthetic rate and stomatal aperture to environmental
71 fluctuations. However, current stomatal models used in ESMs account only for the response of χ to

72 moisture, represented by empirical and non-equivalent formulations¹³, while satellite-based products
73 based on LUE do not represent c_i at all (Supplementary Information). We propose that a firm basis for
74 the prediction of χ is an essential first step towards a first-principles representation of terrestrial plant
75 carbon uptake.

76 Long-term effective values of χ can be reconstructed from data on leaf stable carbon isotope
77 ratios ($\delta^{13}\text{C}$). Previous analyses of leaf $\delta^{13}\text{C}$ data have examined relationships with environmental
78 factors statistically, with many using leaf $\delta^{13}\text{C}$ as a palaeoclimatic indicator of moisture-related climate
79 variables only¹⁴. Here we predict the environmental responses of χ theoretically, reserving the leaf $\delta^{13}\text{C}$
80 measurements for testing. Our theoretical approach depends on the idea of evolutionary optimality in
81 balancing the costs of water loss and carbon gain – a long-standing source of hypotheses to account for
82 stomatal behavior^{15,16}. We derive theoretical dependencies of ‘optimal’ χ (termed χ_o) on growing-
83 season air temperature, vapour pressure deficit, and elevation above sea level based on the least-cost
84 hypothesis^{5,6}, which states that plants minimize the combined costs of maintaining the capacities for
85 carboxylation (maintaining the activity of Rubisco, the primary carboxylating enzyme, and other
86 photosynthetic proteins) and transpiration (maintaining living tissues to support water transport)
87 required to achieve a given assimilation rate. We derive effective growing-season values of χ from a
88 large global compilation of $\delta^{13}\text{C}$ measurements on leaves of C_3 plants¹⁷ (Supplementary Figure 1) with
89 a standard method¹⁸, and use these values to test the theory’s predictions. We then invoke the
90 hypothesis of co-limitation between carboxylation- and electron transport-limited photosynthetic rates
91 to provide a universal model of GPP in C_3 plants, which is shown to unify the Farquhar and LUE
92 models for C_3 photosynthesis. Finally the model is tested against GPP data derived from eddy-
93 covariance flux measurements.

94 The theory developed in Methods predicts that the quantity logit (χ_o) = $\ln [\chi_o / (1 - \chi_o)]$ should
95 rise with growth temperature (T_g) by ~ 0.0545 per Kelvin due to increased assimilation costs (the
96 affinity of Rubisco for CO_2 versus O_2 declines with temperature) and reduced water transport costs (the
97 viscosity of water declines). Due to the increase in transpiration costs imposed by increasing vapour
98 pressure deficit (vpd), logit (χ_o) also should fall by 0.5 per unit increase of natural log transformed D_0
99 (the vpd that would be obtained at standard atmospheric pressure under the same temperature and H_2O
100 mole fraction). With increasing elevation the saturated vapour pressure of water remains constant while
101 the actual vapour pressure (all other factors constant) declines, implying increased transpiration costs;
102 while the partial pressure of O_2 also declines, increasing the affinity of Rubisco for CO_2 and implying
103 reduced assimilation costs¹⁹. These two effects combine to yield a reduction of logit (χ_o) by ~ 0.0815
104 per km elevation (z). The theoretical model for χ_o can therefore be written in a linearized form:

$$105 \quad \ln [\chi_o / (1 - \chi_o)] \approx 0.0545 (T_g - 25) - 0.5 \ln D_0 - 0.0815 z + C \quad (1)$$

106 These predicted effects of each variable are shown here to be quantitatively consistent with the
107 corresponding partial effects (that is, effects of each variable with the others held constant)
108 independently inferred from the leaf χ data by multiple regression (Fig. 1, Table 1). Fitting this
109 equation (with fixed coefficients) to the data provided an estimate of $C = 1.189$, close to the value of

110 1.168 obtained with variable coefficients (Table 1). This constant is directly related to β , the ratio of
111 carboxylation to transpiration cost factors at 25°C, by equation (12) in Methods. The coefficients in
112 equation (1) were computed for standard conditions ($T_g = 25$ °C, $D_0 = 1$ kPa, $z = 0$ km). The coefficient
113 for elevation is sensitive to relative humidity (RH) at standard pressure, however, and becomes
114 arbitrarily large as RH approaches 100%. The value of -0.0815 was computed at RH = 50%. As
115 predicted, the fitted (negative) slope of $\ln [\chi / (1 - \chi)]$ with elevation increases with RH, most steeply at
116 high RH (Fig. 1).

117 χ_o values from equation (1) are consistent with observed χ across biomes ($r = 0.51$) (Fig. 2).
118 Highest values are in hot, wet, low-elevation sites (tropical forests), lowest in cold and/or dry and/or
119 high-elevation sites (deserts, polar and alpine vegetation). χ_o ranges globally from 0.4 to almost 1.0
120 with a typical value of 0.77 (Supplementary Figure 2). The reduction from the equator towards mid-
121 latitudes is due to increasing aridity while that in high latitudes is due to declining temperatures
122 (Supplementary Figure 3).

123 Using a published dataset of CO₂ and water exchange measurements²⁰, we confirmed
124 (Supplementary Table 1) that the partial effects of temperature and vpd on instantaneous gas exchange
125 are also consistent with equation (1). No elevation effect was found, however, probably due to the
126 limited elevation range in this dataset.

127 So far, we have implicitly assumed infinite mesophyll conductance and, therefore, that the
128 ratio (χ_c) of CO₂ partial pressure at the chloroplasts (c_c) to c_a equals the ratio of c_i to c_a . In Methods we
129 show that the optimal value of χ_c has the same environmental dependencies as χ_o , with an additional
130 dependency on the ratio of g_s to g_m . Values of χ_c were estimated from the leaf data using a process-
131 based model for ¹³C discrimination. Data analysis confirmed the predicted environmental responses of
132 logit (χ_c), but with a lower estimate of $C = 1.097$ (Supplementary Table 2) as expected, since finite g_m
133 implies $\chi_c < \chi$. The agreement between observed and predicted χ_c was slightly improved compared to
134 that of χ (Supplementary Table 2, Supplementary Figure 4).

135 The co-ordination or co-limitation hypothesis, stating that the two photosynthetic processes of
136 carboxylation and transport are coupled such that photosynthetic rates limited by those two processes
137 are equal under typical daytime conditions, provides the next step towards a universal model of
138 GPP^{21,22}. The hypothesis implies adjustment of V_{cmax} in time and space to match environmental
139 conditions²² and predicts environmental responses of GPP in the field that are necessarily different
140 from those observed in laboratory experiments which are typically conducted at light saturation, with
141 no time for acclimation. Extensive field measurements also point to an optimal maximum rate of
142 electron transport, J_{max} , that maximizes the photosynthetic benefits minus the costs of maintaining the
143 electron-transport chain (Supplementary Figure 5)²³. We can thereby eliminate both V_{cmax} and J_{max} as
144 independent predictors, to derive a first-principles model for C₃ photosynthesis on weekly or longer
145 time scales that has the mathematical form of a LUE model, but is nonetheless consistent with the
146 standard model of C₃ photosynthesis:

147
$$\text{GPP} = \varphi_0 I_{abs} m \sqrt{[1 - (c^*/m)^{2/3}]}$$
 (2)

148 where

149
$$m = (c_a - \Gamma^*) / \{c_a + 2\Gamma^* + 3\Gamma^* \sqrt{[1.6 \eta^* D_0 \beta^{-1} (K + \Gamma^*)^{-1}]}\}$$
 (3)

150 Here φ_0 is the intrinsic quantum yield ($1.02 \text{ g C mol}^{-1}$)²⁴, I_{abs} is the absorbed photosynthetic
 151 photon flux density (PPFD, $\text{mol m}^{-2} \text{ s}^{-1}$), Γ^* is the photorespiratory compensation point (Pa), K is the
 152 effective Michaelis-Menten coefficient of Rubisco (Pa), η^* is the viscosity of water relative to its value
 153 at 25°C, $\beta \approx 240$ from the constant C in equation (1), and c^* is proportional to the unit carbon cost for
 154 the maintenance of electron transport capacity, ≈ 0.41 (estimated from observed $J_{max}:V_{cmax}$ ratios).
 155 Although not explored here, GPP of C_4 plants under field conditions can be represented using a
 156 modification of equations (2) and (3), given that C_4 plants boost CO_2 around the chloroplasts to high
 157 levels while operating at a lower φ_0 .

158 For C_3 plants, the LUE is the product of φ_0 , m and the square-root term in equation (2). Thus
 159 GPP is proportional to I_{abs} , which can be calculated as the product of incident PPFD and remotely
 160 sensed green vegetation cover. LUE is less than the potential maximum (φ_0) due to limitations by CO_2
 161 (m) and electron transport capacity (the square-root term) leading to global mean reductions by 25%
 162 and 43%, respectively. Supplementary Figure 6 shows how the predicted global pattern of potential
 163 maximum GPP by C_3 plants is modified by those constraints.

164 Predicted monthly GPP compares well with monthly GPP derived from CO_2 flux
 165 measurements (Fig. 3). Predicted global total annual GPP is 120 Pg C, within the accepted range²⁵. The
 166 model captures the variation in observed GPP within and among different biomes as well as or better
 167 than other LUE models²⁶ (Supplementary Information, Supplementary Table 3). This level of
 168 predictability, achieved with only two free parameters (β and c^*) that are estimated from independent
 169 observations, suggests that variations in χ and LUE that are commonly represented by biome-specific
 170 parameters could be explained more parsimoniously as a consequence of optimal plant responses to the
 171 climates in which different biomes occur.

172 Enhanced LUE and GPP are predicted with increasing c_a , the magnitude of the enhancement
 173 varying with climate. A meta-analysis of 12 Free Air Carbon dioxide Enrichment experiments showed
 174 that with CO_2 increased by about 200 ppm, LUE and instantaneous water use efficiency increased by
 175 $12.2 \pm 9\%$ and $54.3 \pm 17\%$, while the ratio V_{cmax}/J_{max} and stomatal conductance changed by $-4.9 \pm$
 176 2.8% and $-20 \pm 3\%$ ²⁷. The model-predicted mean changes in these quantities in turn (Supplementary
 177 Information) are 17.2%, 55%, -22.4% and -15%. This analysis also showed a slight (non-significant)
 178 CO_2 -induced reduction in χ , consistent with the prediction of a slight decline by equation (9).
 179 Considering finite g_m slightly enhances the LUE increase and reduces V_{cmax}/J_{max} decrease due to CO_2
 180 enrichment but has no effect on the responses of water use efficiency and g_s . The model's
 181 overestimation of the CO_2 effect on V_{cmax}/J_{max} requires further analysis: for example we note that
 182 increased leaf temperature due to stomatal closure under CO_2 enrichment would impose a strong
 183 positive effect on V_{cmax}/J_{max} ($\sim 4\%$ per K), potentially compensating the CO_2 effect.

184 Consideration of finite g_m (substituting χ_c for χ_o) affects the interpretation of β , which is
185 reduced to ≈ 200 and now incorporates both the ratio of cost factors and the ratio of g_s to g_m . This
186 modification reduces global annual GPP by 2.5% and marginally improves the agreement with
187 observations ($r = 0.742$, $RMSE = 68.69 \text{ g C month}^{-1}$).

188 The spread of χ and GPP values around the model predictions may reflect variation in β and c^*
189 which have so far been assumed constant. It will be worthwhile to explore their possible dependencies
190 on plant functional traits. For example, the unit cost of transpiration is expected to depend on plant
191 hydraulic traits, including the density and permeability of conducting tissue, plant height and the
192 isohydry-anisohydry continuum, which together with soil moisture determines the maximum water
193 potential difference between soil and leaf⁵. We found no significant difference in χ between woody and
194 non-woody plants; the differences in ^{13}C discrimination among conventionally defined plant functional
195 types (PFTs) were predicted correctly by climate and elevation alone (Supplementary Figure 7).
196 Nonetheless, we did find a significant difference between gymnosperms and angiosperms (20% higher
197 water cost in gymnosperms suggested by the global carbon isotope dataset: Supplementary
198 Information) which could be explained by the narrower conducting elements of gymnosperms, and is
199 consistent with the observed high intrinsic water use efficiency of conifer forests²⁸. The unit cost of
200 V_{cmax} may be influenced by the costs of nitrogen uptake, which are likely higher (favouring investment
201 in water transport) on less fertile soils. We tested for and detected a significant negative response of χ
202 to soil pH, which indexes one dimension of soil fertility²⁹, accounting for an additional 5% of variance
203 in χ . Predicted responses of the ratio J_{max}/V_{cmax} to temperature and CO_2 made with the simplifying
204 assumption of a universally constant c^* appear to be supported by observational evidence, but should be
205 analysed with a more extensive dataset.

206 This simple model's predictive skill suggests a route towards an improved predictive
207 understanding and modelling approach for terrestrial carbon and water cycling while providing a new
208 theoretical framework for the analysis of both environmental and plant morphological influences on
209 photosynthetic traits. By making testable predictions of such influences based on quantifiable benefits
210 and costs, the evolutionary optimality approach may lead to a more robust basis for understanding and
211 modelling both the co-ordination of plant traits among species, and biological controls of the emergent
212 functional properties of ecosystems as represented in ESMs.

213 **Full Methods** and any associated references are available in the online version of the paper.

214 **Author Information** Correspondence and requests for materials should be addressed to H.W. and C.P.
215 (wanghan_sci@yahoo.com, peng.changhui@uqam.ca)

216 **Acknowledgements**

217 We thank Yan-Shih Lin, Vincent Maire, Belinda Medlyn, Beni Stocker, and IIASA colleagues for
218 discussions, and Ralph Keeling for comments on successive drafts. The paper is a contribution to the
219 AXA Chair Programme on Biosphere and Climate Impacts and Imperial College's initiative on Grand
220 Challenges in Ecosystems and the Environment. Research is supported by National Basic Research

221 Programme of China (2013CB956602) grant to CP and HW, National Natural Science Foundation of
222 China (Grant no. 31600388) to HW, an Australian Research Council Discovery grant ('Next-
223 generation vegetation model based on functional traits') to ICP and IJW, an Australian National Data
224 Service (ANDS) grant ('Ecosystem production in space and time') to ICP, and Terrestrial Ecosystem
225 Research Council (TERN) grants ('Ecosystem Modelling and Scaling Infrastructure') to ICP and BJE.
226 TERN and ANDS are supported by the Australian Government National Collaborative Infrastructure
227 Strategy (NCRIS). TFK acknowledges financial support from the Laboratory Directed Research and
228 Development (LDRD) fund under the auspices of DOE, BER Office of Science at Lawrence Berkeley
229 National Laboratory, and a Macquarie University Research Fellowship. In addition to authors of this
230 paper, data were provided by Margaret Barbour, Lucas Cernusak, Todd Dawson, David Ellsworth,
231 Graham Farquhar, Howard Griffiths, Claudia Keitel, Alexander Knohl, Peter Reich, Dave Williams,
232 Radika Bhaskar, Hans Cornelissen, Anna Richards, Susanne Schmidt, Fernando Valladares, Christian
233 Körner, Ernst-Detlef Schulze, Nina Buchmann and Lou Santiago. We used 'free and fair use' eddy-
234 covariance data acquired by the FLUXNET community and, in particular, by the following networks:
235 AmeriFlux (US Department of Energy, Biological and Environmental Research, Terrestrial Carbon
236 Program), AsiaFlux, CarboEuropeIP, Fluxnet-Canada (supported by CFCAS, NSERC, BIOCAP,
237 Environment Canada, and NRCan), OzFlux and TCOS-Siberia. We acknowledge the financial support
238 to the eddy-covariance data harmonization provided by CarboEuropeIP, FAO- GTOS-TCO, iLEAPS,
239 Max Planck Institute for Biogeochemistry, National Science Foundation, University of Tuscia,
240 Université Laval and Environment Canada and US Department of Energy and the database
241 development and technical support from Berkeley Water Center, Lawrence Berkeley National
242 Laboratory, Microsoft Research eScience, Oak Ridge National Laboratory, University of California-
243 Berkeley, University of Virginia.

244 **Author contributions**

245 H.W. and I.C.P. derived the predictions. H.W. carried out all the analyses and constructed the Figures
246 and Tables. I.C.P. and T.F.K. contributed to the analysis and writing. T.W.D., B.J.E. and I.C.P.
247 developed and tested the flux partitioning method. T.W.D. developed the global flux database and all
248 the GPP computations. I.J.W. proposed least-cost hypothesis and contributed to the analysis. W.K.C.
249 originated and compiled the $\Delta^{13}\text{C}$ data set. H.W. and I.C.P. wrote the first draft, and all authors
250 contributed to the final draft.

251 **Competing financial interests** The authors declare no competing financial interests.

252 **References**

- 253 1 Ciais, P. *et al.* Carbon and other biogeochemical cycles. in *Climate change 2013: the physical*
254 *science basis. Contribution of Working Group I to the Fifth Assessment Report of the*
255 *Intergovernmental Panel on Climate Change* (eds Thomas F Stocker *et al.*) Ch. 6, 465-570
256 (Cambridge University Press, 2014).
- 257 2 Friedlingstein, P. *et al.* Uncertainties in CMIP5 climate projections due to carbon cycle
258 feedbacks. *Journal of Climate* **27**, 511-526 (2014).

259 3 Prentice, I. C., Liang, X., Medlyn, B. E. & Wang, Y. P. Reliable, robust and realistic: the three
260 R's of next-generation land-surface modelling. *Atmospheric Chemistry and Physics* **15**, 5987-
261 6005 (2015).

262 4 Wang, H., Prentice, I. C. & Davis, T. W. Biophysical constraints on gross primary production
263 by the terrestrial biosphere. *Biogeosciences* **11**, 5987-6001 (2014).

264 5 Prentice, I. C., Dong, N., Gleason, S. M., Maire, V. & Wright, I. J. Balancing the costs of
265 carbon gain and water transport: testing a new theoretical framework for plant functional
266 ecology. *Ecology letters* **17**, 82-91 (2014).

267 6 Wright, I. J., Reich, P. B. & Westoby, M. Least - Cost Input Mixtures of Water and Nitrogen
268 for Photosynthesis. *The American Naturalist* **161**, 98-111 (2003).

269 7 Monteith, J. L. Solar radiation and productivity in tropical ecosystems. *Journal of Applied*
270 *Ecology* **9**, 747-766 (1972).

271 8 Farquhar, G. D., von Caemmerer, S. & Berry, J. A. A biochemical model of photosynthetic
272 CO₂ assimilation in leaves of C₃ species. *Planta* **149**, 78-90 (1980).

273 9 Medlyn, B. E. Physiological basis of the light use efficiency model. *Tree Physiology* **18**, 167-
274 176 (1998).

275 10 Ali, A. *et al.* A global scale mechanistic model of the photosynthetic capacity. *Geoscientific*
276 *Model Development Discussions* **8**, 6217–6266 (2015).

277 11 Cai, W. *et al.* Large differences in terrestrial vegetation production derived from satellite-
278 based light use efficiency models. *Remote Sensing* **6**, 8945-8965 (2014).

279 12 De Kauwe, M. G. *et al.* Forest water use and water use efficiency at elevated CO₂: a model -
280 data intercomparison at two contrasting temperate forest FACE sites. *Global Change Biology*
281 **19**, 1759-1779 (2013).

282 13 Medlyn, B. E. *et al.* Reconciling the optimal and empirical approaches to modelling stomatal
283 conductance. *Global Change Biology* **17**, 2134-2144 (2011).

284 14 Diefendorf, A. F., Mueller, K. E., Wing, S. L., Koch, P. L. & Freeman, K. H. Global patterns
285 in leaf $\delta^{13}\text{C}$ discrimination and implications for studies of past and future climate. *Proceedings*
286 *of the National Academy of Sciences* **107**, 5738-5743 (2010).

287 15 Cowan, I. & Farquhar, G. Stomatal function in relation to leaf metabolism and environment.
288 *Symposia of the Society for Experimental Biology*, 471-505 (1977).

289 16 Givnish, T. J. *On the Economy of Plant Form and Function*. Vol. 6 (Cambridge University
290 Press, 1986).

291 17 Cornwell, W. K. *et al.* A global dataset of leaf $\Delta^{13}\text{C}$ values. doi:10.5281/zenodo.569501
292 (2017).

293 18 Farquhar, G. D., Ehleringer, J. R. & Hubick, K. T. Carbon isotope discrimination and
294 photosynthesis. *Annual review of plant biology* **40**, 503-537 (1989).

295 19 Körner, C., Farquhar, G. & Wong, S. Carbon isotope discrimination by plants follows
296 latitudinal and altitudinal trends. *Oecologia* **88**, 30-40 (1991).

297 20 Lin, Y.-S. *et al.* Optimal stomatal behaviour around the world. *Nature Climate Change* **5**,
298 459–464 (2015).

299 21 Maire, V. *et al.* The coordination of leaf photosynthesis links C and N fluxes in C3 plant
300 species. *PloS one* **7**, e38345 (2012).

301 22 Haxeltine, A. & Prentice, I. C. A general model for the light-use efficiency of primary
302 production. *Funct. Ecol.* **10**, 551-561, doi:10.2307/2390165 (1996).

303 23 Kattge, J. & Knorr, W. Temperature acclimation in a biochemical model of photosynthesis: a
304 reanalysis of data from 36 species. *Plant, cell & environment* **30**, 1176-1190 (2007).

305 24 Collatz, G., Berry, J., Farquhar, G. & Pierce, J. The relationship between the Rubisco reaction
306 mechanism and models of photosynthesis. *Plant, Cell & Environment* **13**, 219-225 (1990).

307 25 Beer, C. *et al.* Terrestrial gross carbon dioxide uptake: global distribution and covariation with
308 climate. *Science* **329**, 834-838 (2010).

309 26 Yuan, W. *et al.* Global comparison of light use efficiency models for simulating terrestrial
310 vegetation gross primary production based on the LaThuile database. *Agricultural and forest
311 meteorology* **192**, 108-120 (2014).

312 27 Ainsworth, E. A. & Long, S. P. What have we learned from 15 years of free - air CO₂
313 enrichment (FACE)? A meta - analytic review of the responses of photosynthesis, canopy
314 properties and plant production to rising CO₂. *New Phytologist* **165**, 351-372 (2005).

315 28 Frank, D. C. *et al.* Water-use efficiency and transpiration across European forests during the
316 Anthropocene. *Nature Climate Change* **5**, 579-583 (2015).

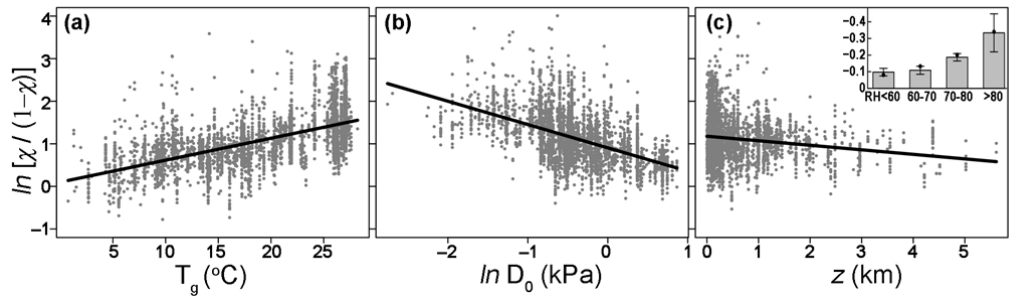
317 29 Maire, V. *et al.* Global effects of soil and climate on leaf photosynthetic traits and rates.
318 *Global Ecology and Biogeography* **24**, 706-717 (2015).

319 30 Kaplan, J. O. Geophysical applications of vegetation modeling. (Lund University, 2001).

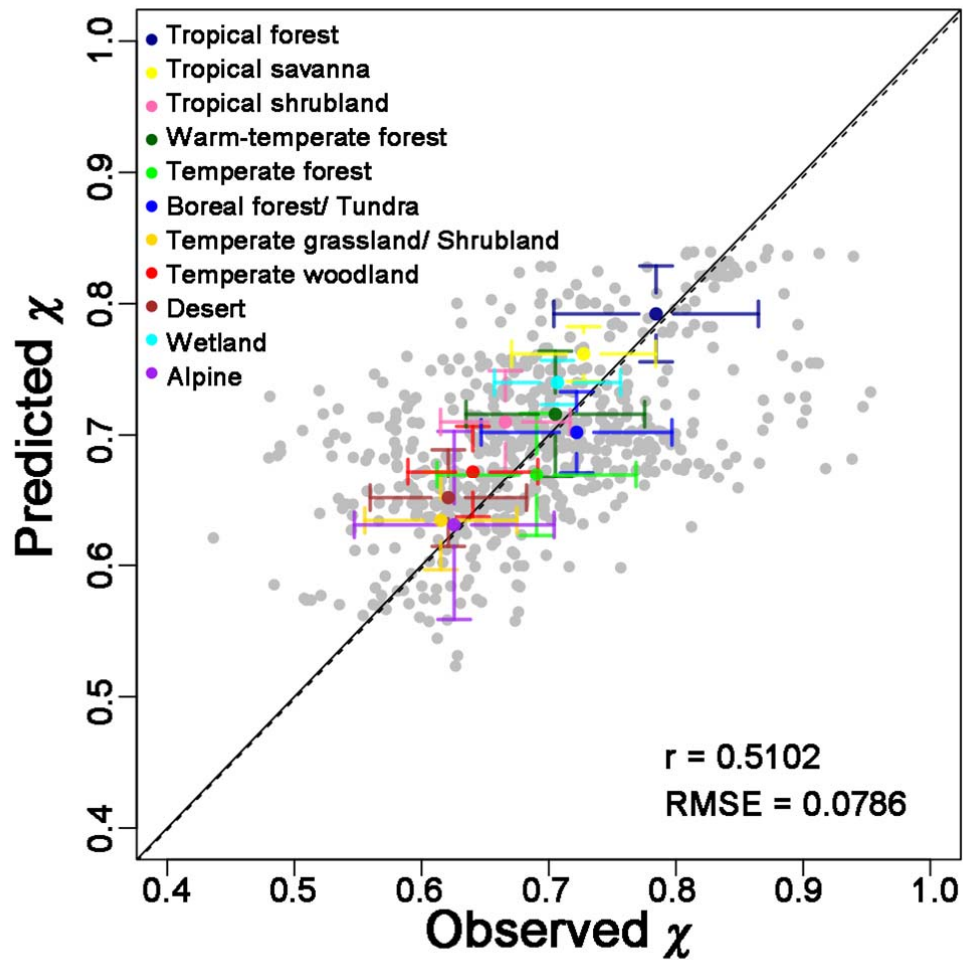
320 **Table 1 | Summary statistics for the environmental dependencies of χ (the ratio of leaf-internal to**
321 **ambient CO₂ partial pressure).** Logit-transformed values of χ derived from the global leaf stable
322 carbon isotope dataset using a standard method¹⁸ were regressed against the difference between
323 growing-season mean temperature T_g and 25°C (ΔT_g , °C), the natural logarithm of growing-season
324 mean vapour pressure deficit at standard atmospheric pressure ($\ln D_0$, kPa), and elevation (z , km).
325 Theoretical values, shown for comparison, are partial derivatives of logit-transformed predicted
326 ‘optimal’ χ with respect to each predictor, evaluated for standard conditions ($T_g = 25$ °C, $D_0 = 1$ kPa, z
327 = 0 km).
328

Predictor	Theoretical value	Fitted coefficient	Confidence intervals		Multiple R ²
			2.5%	97.5%	
ΔT_g	0.0545	0.0515	0.0456	0.0575	0.391
$\ln D_0$	-0.5	-0.5478	-0.6111	-0.4846	
z	-0.0815	-0.1065	-0.1315	-0.0815	
intercept	1.189	1.1680	1.0464	1.2896	

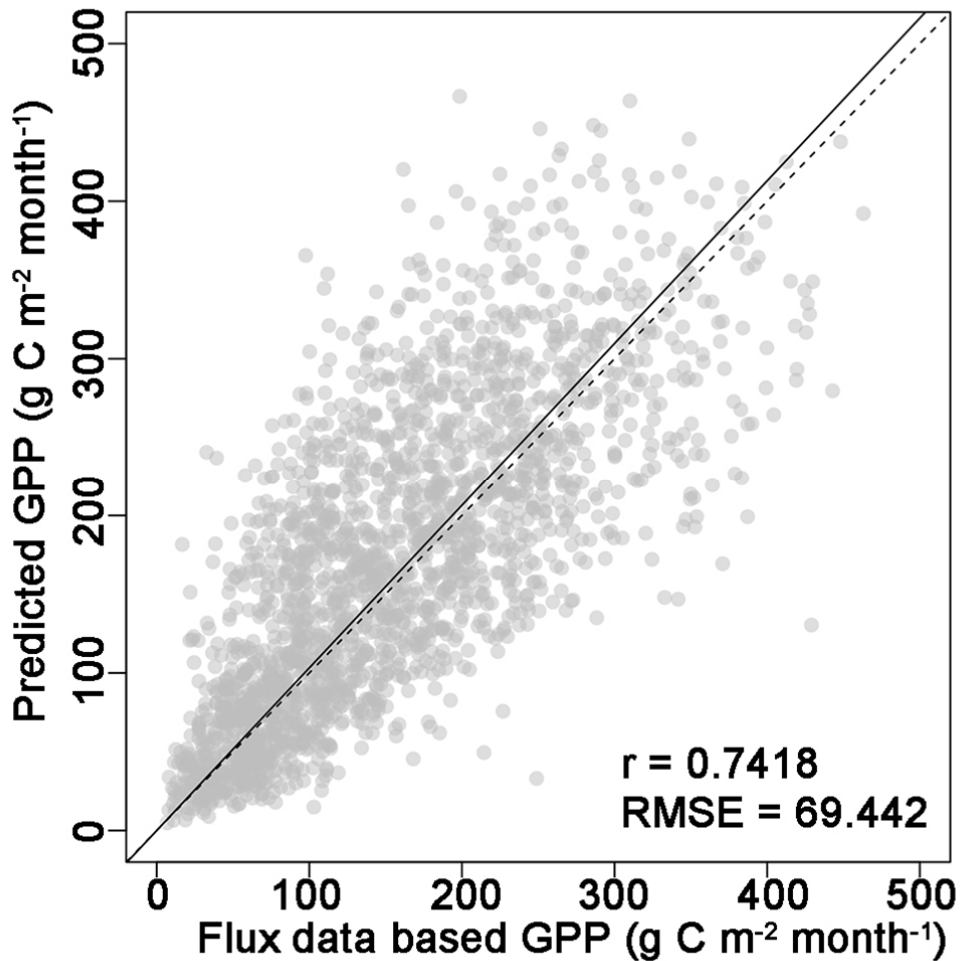
329 **Figure 1 | Partial residual plots from the regression of logit-transformed values of χ (the ratio of**
330 **leaf-internal to ambient CO₂ partial pressure) derived from the global leaf stable carbon isotope**
331 **dataset against environmental predictors. T_g : growing-season mean temperature. $\ln D_0$: the natural**
332 **logarithm of growing-season mean vapour pressure deficit at standard atmospheric pressure. z :**
333 **elevation. Inset shows elevation responses for relative humidity (RH, %) classes with error bars**
334 **showing 95% confidence intervals, compared to predicted responses (black dots) evaluated at the**
335 **centre of each RH class.**



336 **Figure 2 | Site-mean values of the ratio of leaf-internal to ambient CO₂ partial pressure (χ).**
337 Predictions (χ_o) are from the theoretical model driven by three environmental predictors (equation 1).
338 Observations (χ) are from the global leaf stable carbon isotope dataset. Mean and standard deviation
339 are shown for each biome. Biome types were assigned based on BIOME4³⁰ for consistency except for
340 ‘wetland’ and ‘alpine’ types, which were assigned from source publications. The solid line is the
341 regression through the origin; the dashed line is the 1:1 line. r : Pearson correlation between observed
342 and predicted values; RMSE: root-mean-squared error of prediction.



343 **Figure 3 | Monthly gross primary production (GPP) at flux sites.** Predictions from equations (2)
344 and (3); observations based on CO₂ flux data in the FLUXNET archive. The solid line is the regression
345 through the origin; the dashed line is the 1:1 line. *r*: Pearson correlation between observed and
346 predicted values; RMSE: root-mean-squared error of prediction.



347 **Methods**

348 **Theory for the environmental controls on χ**

349 Optimality hypotheses to account for the environmental responses of stomata have a long history, with
350 pioneering contributions especially by Cowan and Farquhar and Givnish^{15,16}. Cowan and Farquhar
351 hypothesized that stomata act to maximize marginal carbon gain (assimilation, A) while minimizing
352 marginal water loss (transpiration, E), i.e. $\partial E / \partial A = \lambda$ where λ is a parameter representing the ‘marginal
353 carbon cost of water’. This approach successfully addresses many observed features of stomatal
354 behaviour but leaves the value of λ undefined and, as noted by Givnish, does not explicitly consider the
355 costs of maintaining photosynthetic capacity. These limitations are avoided by the *least-cost*
356 *hypothesis*, which states that plants should minimize the combined carbon costs (per unit of
357 assimilation) of maintaining the required capacities for carboxylation and transpiration. This hypothesis
358 was first proposed explicitly by Wright et al.⁶, and applied in the context of the standard model of
359 photosynthesis⁸ by Prentice et al.⁵ who defined the following optimality criterion for χ :

360
$$a \cdot \partial(E/A) / \partial \chi + b \cdot \partial(V_{cmax}/A) / \partial \chi = 0 \quad (4)$$

361 Here, a and b are dimensionless cost factors for E and V_{cmax} respectively.

362 The *coordination hypothesis* states that V_{cmax} of leaves at any level in the canopy acclimates spatially
363 and temporally to the prevailing daytime incident PPFD (the absorbed photosynthetic photon flux
364 density) in such a way as to be neither in excess (entailing additional, futile maintenance respiration),
365 nor less than required for full exploitation of the available light^{21,22,31}. In other words, under typical
366 daytime conditions when most photosynthesis takes place, the Rubisco-limited photosynthetic rate is
367 equal to electron-transport limited photosynthetic rate ($A=A_c=A_j$). Therefore, Rubisco-limited
368 photosynthesis in the standard biochemical model⁸ can be rewritten as a prediction of V_{cmax}/A :

369
$$V_{cmax}/A = (\chi c_a + K) / (\chi c_a - \Gamma^*), \quad (5)$$

370 Fick’s law of diffusion applied to both H₂O and CO₂ allows prediction of E/A :

371
$$E/A = 1.6(D/c_a)/(1-\chi) \quad (6)$$

372 where D is vapour pressure deficit. Initially neglecting Γ^* for simplicity (i.e. assuming $\chi c_a \gg \Gamma^*$),
373 substituting equations (5) and (6) in (4) and taking derivatives, the optimal value of χ satisfies:

374
$$1.6(aD/c_a)/(1-\chi)^2 - bK/\chi^2 c_a = 0 \quad (7)$$

375 The solution to equation (7) provides the required optimal value (χ_o):

376
$$\chi_o = \zeta / (\zeta + \sqrt{D}), \text{ where } \zeta = \sqrt{(bK/1.6a)} \quad (8)$$

377 Omitting the assumption $\chi c_a \gg \Gamma^*$ yields the more exact form:

378 $\chi_o = \Gamma^*/c_a + (1 - \Gamma^*/c_a) \zeta/(\zeta + \sqrt{D})$, where $\zeta = \sqrt{[b(K + \Gamma^*)/1.6a]}$ (9)

379 The parameter ζ expresses the sensitivity of χ_o to D . The ratio of stem respiration to transpiration
 380 capacity (a) depends (among other things) on the viscosity of water. The ratio of mitochondrial
 381 respiration to carboxylation capacity (b) is generally taken as constant⁸. As only the ratio b/a (not the
 382 individual terms b and a) affects χ_o , we will later use the composite parameter β to denote the value of
 383 b/a at 25°C.

384 Given the particular form of equation (8), logit transformation simplifies the derivation of its
 385 sensitivities to environmental variables, as follows:

386 $\text{logit}(\chi_o) = \ln[\chi_o/(1 - \chi_o)] = \frac{1}{2} \ln b - \frac{1}{2} \ln a + \frac{1}{2} \ln K - \frac{1}{2} \ln D - \frac{1}{2} \ln 1.6$ (10)

387 The dependencies of a (through the viscosity of water η) and K (through the Michaelis-Menten
 388 coefficients of Rubisco for carboxylation (K_c) and oxygenation (K_o)) on temperature (T), and the
 389 dependency of K (through P_o , the partial pressure of O₂) and D on elevation, are denoted by $f_1(T)$, $f_2(T)$,
 390 $g_1(z)$ and $g_2(z)$. The elevation effect here includes the effect of the vapour pressure decline because
 391 humidity statistics in the 3D-gridded datasets used for global analysis do not account for it. Thus, we
 392 substitute D with D_0 (the vpd that would be obtained at standard atmospheric pressure under the same
 393 temperature and H₂O mole fraction). Equation (10) is then equivalent to:

394 $\ln[\chi_o/(1 - \chi_o)] = -\frac{1}{2} \ln f_1(T) + \frac{1}{2} \ln f_2(T) + \frac{1}{2} \ln g_1(z) - \frac{1}{2} \ln D_0 - \frac{1}{2} \ln g_2(z) + C$, (11)

395 where $C = \frac{1}{2} (\ln b - \ln a_{ref} + \ln K_{ref} - \ln 1.6) = \frac{1}{2} (\ln \beta + \ln K_{ref} - \ln 1.6)$ (12)

396 a_{ref} and K_{ref} are the values of a and K under standard conditions ($T = 298$ K, $z = 0$). Equation (11)
 397 predicts the coefficient of $\ln D_0$ as -0.5 .

398 **Temperature dependency of a**

399 The parameter a is directly proportional to η , according to equation (11) in ref. 5. The temperature
 400 dependency of η can be well approximated by the Vogel equation³²:

401 $\eta = 10^{-3} \exp [A + B/(C + T)]$ (13)

402 where $A = -3.719$, $B = 580$ and $C = -138$. Thus, the sensitivity of η to temperature is given by:

403 $(1/\eta) \partial \eta / \partial T = \partial \ln \eta / \partial T = -B/(C + T)^2$ (14)

404 allowing the response of η to T , within the physiologically relevant range, to be well approximated by
 405 an exponential response to $\Delta T = T - 298$ K relative to a reference value at $T = 298$ K (η_{ref}):

406 $f_1(T) = \eta/\eta_{ref} \approx \exp [-B/(C + T)^2 \Delta T]$ (15)

407 **Temperature and elevation dependencies of K**

408 K (in partial pressure units) is given by:

409
$$K = K_c (1 + P_o/K_o), \quad (16)$$

410 P_o can be expressed as a simple function of elevation (in km) using a standard approximation for the
411 decline in atmospheric pressure with elevation³³:

412
$$P_o = 21000 \exp(-0.114 z) \quad (17)$$

413 The Arrhenius relationship describing the response of a biochemical rate parameter (x , such as K_c and
414 K_o) to temperature can be expressed as:

415
$$\partial \ln x / \partial T = (\Delta H/R) \cdot (1/T^2) \quad (18)$$

416 where $R = 8.3145 \text{ J mol}^{-1} \text{ K}^{-1}$ and the activation energies ΔH are $79.43 \text{ kJ mol}^{-1}$ for K_c and 36.38 kJ
417 mol^{-1} for K_o , denoted as ΔH_c and ΔH_o , respectively, from *in vivo* determinations³⁴.

418 Therefore, the sensitivity of K to temperature from equation (16) is given by:

419
$$(1/K) \partial K / \partial T = [(\Delta H_c/R)(1/T^2) (P_o + K_o) - (\Delta H_o/R)(1/T^2) P_o] / (P_o + K_o) \quad (19)$$

420 leading to:

421
$$f_2(T) = \exp([(\Delta H_c/R)(1/T^2) (P_o + K_o) - (\Delta H_o/R)(1/T^2) P_o] / (P_o + K_o) \Delta T) \quad (20)$$

422 The sensitivity of K to elevation due to declination in P_o can then be derived from equation (16):

423
$$(1/K) \partial K / \partial z = -0.114 P_o / (P_o + K_o) \quad (21)$$

424 Therefore,

425
$$g_1(z) = \exp[-0.114 P_o / (P_o + K_o) z] \quad (22)$$

426 **Elevation dependency of D**

427 D can similarly be expressed as a function of elevation:

428
$$D = e_s - e_{a0} \exp(-0.114 z) \quad (23)$$

429 where e_s is the saturation vapour pressure and e_{a0} is the actual vapour pressure that would be obtained
430 at sea level under the same H_2O mole fraction and temperature. Since $\exp(-0.114z)$ can be taken as
431 equal to unity, to a good approximation, within the relevant range of z , the dependency of D on
432 elevation here approximated as:

433 $\partial \ln D / \partial z = 0.114 e_{a0} / D_0 = 0.114 RH / (1 - RH),$ (24)

434 Therefore,

435 $g_2(z) = \exp \{0.114 [RH / (1 - RH)] z\}$ (25)

436 Note that this theoretically derived elevation effect on D varies strongly with RH , approaching infinity
437 as RH tends to 1.

438 ***Linearized expressions for χ_o in terms of environmental predictors***

439 Evaluating equations (15), (20), (22) and (25) at standard temperature ($T = 298$ K, $z = 0$ and $RH_0 =$
440 50%) and substituting the resulting expressions in equation (11), we obtain:

441 $\ln [\chi_o / (1 - \chi_o)] = \frac{1}{2} (0.0864 + 0.0227) \Delta T - \frac{1}{2} (0.0491 + 0.114) z - \frac{1}{2} \ln D_0 + C$
442 $= 0.0545 \Delta T - 0.0815 z - 0.5 \ln D_0 + C$ (26)

443 $C \approx 1.189$, estimated as the intercept in a generalized linear model (GLM) fitted to the data with
444 imposed regression coefficients for all three environmental effects in equation (26). This allows us to
445 estimate $\beta \approx 240$ from equation (12). Therefore, the optimal leaf-internal partial pressure of CO_2 can be
446 derived from the more exact expression for χ_o (equation 9):

447 $c_i = \frac{\xi c_a + \Gamma^* \sqrt{D}}{\xi + \sqrt{D}}, \xi = \sqrt{\frac{\beta(K + \Gamma^*)}{1.6\eta^*}}$, (27)

448 Here η^* is the viscosity of water relative to its value at 25°C, representing the effect of changing
449 viscosity on the value of a .

450 **Testing the theory with global $\delta^{13}\text{C}$ data**

451 Vascular-plant leaf stable carbon isotope data were compiled from published and unpublished
452 sources¹⁷. Inferred carbon isotope discrimination (Δ) values for 3549 leaf samples of C_3 plants were
453 converted to estimates of χ by a standard equation¹⁸:

454 $\chi = \frac{\Delta - a'}{b' - a'}$ (28)

455 where a' and b' have standard values 4.4 and 27, representing the diffusional and biochemical
456 components of carbon isotope discrimination, respectively. The Climatic Research Unit CL2.0 10-
457 minute gridded monthly climatology³⁵ of mean, maximum and minimum temperatures and relative
458 humidity provided mean temperature (T_g , °C) and vapour pressure deficit (D_0 , kPa) values for the
459 period with daily mean temperatures $> 0^\circ\text{C}$. Values of $\ln [\chi / (1 - \chi)]$ were fitted using a GLM with $\Delta T_g =$
460 $T_g - 25^\circ\text{C}$, $\ln D_0$, and site-specific elevation (z , km) as predictors. Standard errors estimated by the

461 GLM were combined quadratically with standard errors for the uncertainty of the effective Rubisco
 462 discrimination parameter b' , the latter obtained by generating 10^4 normally distributed values of b'
 463 (mean = 27, standard deviation = 0.27) and repeating the estimation of χ and the GLM fitting 10^4 times
 464 with different b' values.

465 **Incorporating finite g_m into the least-cost framework and testing with global $\delta^{13}\text{C}$ data**

466 Mesophyll conductance, the liquid-phase conductance between the intercellular spaces and the
 467 chloroplasts, is assumed arbitrarily large in most large-scale ecophysiological data analysis and
 468 models³⁶, since the mechanisms behind its environmental responses remain unclear. The prediction of
 469 g_m still largely relies on empirical relationships³⁷. However, the effect of finite g_m can be incorporated
 470 into the least-cost framework naturally due to its impact on carboxylation, and furthermore leads to an
 471 optimal ratio of the chloroplastic to ambient CO_2 (χ_c) under the simplifying assumption that the ratio of
 472 g_s (stomata conductance) to g_m is independent of environmental factors³⁸⁻⁴¹.

473 Assuming that the total conductance (g) for CO_2 diffusing from the ambient atmosphere to the
 474 chloroplasts is principally controlled by g_s and g_m :

$$475 \quad 1/g = 1/g_s + 1/g_m \quad (29)$$

476 Note that g_m affects CO_2 diffusion for carboxylation, but not H_2O diffusion during transpiration.
 477 Replacing stomatal with total conductance for carboxylation, equation (6) therefore becomes:

$$478 \quad E/A = 1.6 (D/c_a) (g_s + g_m) / [(1 - \chi_c) g_m] \quad (30)$$

479 The leaf-internal CO_2 concentration ($\chi_c c_a$) in equation (5) can then be replaced by the chloroplastic CO_2
 480 concentration ($\chi_c c_a$):

$$481 \quad V_{cmax}/A = (\chi_c c_a + K)/(\chi_c c_a - \Gamma^*) \quad (31)$$

482 Applying the optimality criterion:

$$483 \quad a \cdot \partial(E/A_c) / \partial \chi_c + b \cdot \partial(V_{cmax}/A_c) / \partial \chi_c = 0 \quad (32)$$

484 to equations (30) and (31), the optimal ratio of chloroplast to ambient CO_2 (χ_{co}) is given by (assuming
 485 $\chi_c c_a \gg \Gamma^*$):

$$486 \quad \chi_{co} = \zeta_c / (\zeta_c + \sqrt{D}), \text{ where } \zeta_c = \sqrt{[bK/1.6a/(1 + g_s/g_m)]} = \zeta / \sqrt{(1 + g_s/g_m)}, \quad (33)$$

487 or, if we relax the assumption $\chi_c c_a \gg \Gamma^*$, by:

$$488 \quad \chi_{co} = \Gamma^*/c_a + (1 - \Gamma^*/c_a) \zeta_c / (\zeta_c + \sqrt{D}), \text{ where } \zeta_c = \sqrt{\{b(K + \Gamma^*)/[1.6a(1 + g_s/g_m)]\}} \quad (34)$$

489 Here χ_{co} is not influenced by g_s and g_m separately, but by their ratio. The form of the model for χ_{co}
 490 resembles that for χ_o , but the sensitivity parameter ζ is adjusted by a factor $\sqrt{[1/(1 + g_s/g_m)]}$.

491 In the model for χ_{co} the ratio of g_s to g_m is assumed to be independent of environment. Even though
 492 both g_s and g_m vary with environmental conditions, including light, moisture and temperature, their
 493 covariation under a wide range of conditions supports this assumption at least as a first
 494 approximation³⁸⁻⁴¹. Moreover, data indicate that the value of g_s/g_m is quite conservative, with a median
 495 of about 1.4 (I.J. Wright, unpublished data). The derivation of the environmental dependencies of χ_{co}
 496 then follows the same logical steps as that for χ . Further refinement of the model for χ_{co} however would
 497 require deeper understanding of the regulation of g_s and g_m .

498 The estimated value of the ratio of cost factors b to a at reference temperature is updated to a value of
 499 343 after deducting the term of $(g_s/g_m + 1)^{-1}$ from constant C . This time we obtained C based on
 500 observational χ_c estimated from the global carbon isotope dataset with the “comprehensive” equation in
 501 Ubierna & Farquhar⁴² but following the first three simplifying assumptions listed in their Figure 1: (1)
 502 that the ternary effect is negligible; (2) the fractionations associated with Rubisco carboxylation, during
 503 respiration and photorespiration are far less than 1; (3) infinite boundary-layer conductance. We also
 504 assumed leaf dark respiration $R_d \ll A$, so that $R_d/(R_d + A) \approx R_d/A$. The “comprehensive” equation for Δ
 505 can then be rewritten more simply as:

$$506 \quad \Delta = a_s (1 - \chi) + a_m (\chi - \chi_c) + b\chi_c - eb_0(\chi_c + \kappa) - f\gamma \quad (35)$$

507 Here, a_s , a_m , b , e and f are the fractionations associated with diffusion in air (4.4‰), in water (1.8‰),
 508 by Rubisco carboxylation (27 to 30‰), during respiration (0 to -5‰) and photorespiration (8 to 16‰),
 509 respectively. $b_0 = R_d/V_{cmax} = 0.015^8$, $\kappa = K/c_a$ and $\gamma = \Gamma^*/c_a$.

510 Given that the CO₂ flux from the outside to the intercellular spaces must be the same as that from the
 511 intercellular spaces to the chloroplast, denoting the ratio of g_m to g_s as θ , we have:

$$512 \quad (1 - \chi) g_s = (\chi - \chi_c) \theta g_s \quad (36)$$

513 Therefore:

$$514 \quad 1 - \chi = \theta (1 - \chi_c)/(1 + \theta) \quad (37)$$

515 and

$$516 \quad \chi - \chi_c = (1 - \chi_c)/(1 + \theta) \quad (38)$$

517 Substituting these expressions into equation (35) and solving for χ_c gives:

$$518 \quad \chi_c = \frac{\Delta - \frac{\theta a_s + a_m}{1 + \theta} + eb_0 \kappa + f\gamma}{b - \frac{\theta a_s + a_m}{1 + \theta} - eb_0} \quad (39)$$

519 We assumed a constant value of $\theta = 1.4$, based on data compiled by IJW, and consistent with values in
 520 the literature⁴³.

521 Given the uncertainties in parameters b , e and f , we chose the values ($b = 30$, $e = 0$, $f = 16$) that
 522 produced the best fit ($R^2 = 0.5057$) in the regression of χ_c against temperature, \ln vpd and elevation
 523 (Supplementary Table 2).

524 **Light-use efficiency model**

525 The model proposed by Wang et al.⁴ assumed that the electron-transport and Rubisco-limited rates of
 526 photosynthesis (A_J , A_c) as described by the biochemical photosynthesis model⁸ are coordinated (that is,
 527 $A = A_J = A_c$) under typical daytime conditions^{21,22,31}, allowing GPP to be predicted from A_J at a monthly
 528 time scale by:

$$529 \quad A_J = \varphi_0 I_{abs} (c_i - \Gamma^*) / (c_i + 2\Gamma^*) \quad (40)$$

530 LUE is the product of φ_0 and the CO₂ limitation term of $(c_i - \Gamma^*) / (c_i + 2\Gamma^*)$ (denoted here by m).
 531 Incorporating the exact equation for c_i (equation 27) yields:

$$532 \quad A = \varphi_0 I_{abs} m \quad (41)$$

533 where

$$534 \quad m = \frac{c_a - \Gamma^*}{c_a + 2\Gamma^* + 3\Gamma^* \sqrt{\frac{1.6D\eta^*}{\beta(K + \Gamma^*)}}} \quad (42)$$

535 Equations (41) and (42) assume that the light response of A is linear up to the coordination point, i.e.
 536 that the maximum electron-transport rate (J_{max}) is arbitrarily large. In reality J_{max} limitation can be
 537 significant, especially at high temperatures. We therefore modified equation (41) to allow for a non-
 538 rectangular hyperbola relationship between A and I_{abs} ^{44,45}.

$$539 \quad A = \varphi_0 I_{abs} m \frac{1}{\sqrt{1 + \left(\frac{4\varphi_0 I_{abs}}{J_{max}} \right)^2}} \quad (43)$$

540 This does not have the form of a LUE model, because of the non-linear dependence on I_{abs} . However,
 541 the apparent discrepancy between the non-linear light response observed at short time scales (sub-
 542 daily) and the linear light response described by the empirical LUE model on longer time scales
 543 (weekly to monthly) can be resolved if it is assumed J_{max} acclimates to I_{abs} over longer time scales. To
 544 show this, we further assume that (a) there exists an optimal J_{max} for given average light conditions that
 545 maximizes the differences between the benefit and cost of maintaining this value of J_{max} , which
 546 conceptually includes the maintenance of light-harvesting complexes and the various proteins involved
 547 in electron transport; (b) the benefit is the assimilation rate A , whereas the cost is the product of J_{max}
 548 and a parameter c (defined as the unit cost of maintaining J_{max}); (c) V_{cmax} and J_{max} vary with

549 environmental conditions on a monthly time scale, while the unit costs b and c of maintaining V_{cmax} and
 550 J_{max} respectively are unchanged; and (d) V_{cmax} and J_{max} are related via the coordination hypothesis ($A_c =$
 551 $A_j = A$). The optimality criterion for J_{max} is then simply:

$$552 \quad \partial A / \partial J_{max} = c \quad (44)$$

553 Taking the partial derivative of A with respect to J_{max} in equation (43) leads to:

$$554 \quad c = \frac{\partial A}{\partial J_{max}} = \frac{m(\varphi_0 I_{abs})^3}{4 \sqrt{\left[(\varphi_0 I_{abs})^2 + \left(\frac{J_{max}}{4} \right)^2 \right]^3}} \quad (45)$$

555 Equation (43) can now be rewritten as

$$556 \quad A = \varphi_0 I_{abs} m \sqrt{1 - \left(\frac{4c}{m} \right)^{\frac{2}{3}}} \quad (46)$$

557 This is a key algebraic result because A is now, once again, proportional to I_{abs} .

558 Next, applying the coordination hypothesis ($A_c = A_j = A$):

$$559 \quad \frac{\varphi_0 I_{abs}}{\sqrt{\left(\varphi_0 I_{abs} \right)^2 + \left(\frac{J_{max}}{4} \right)^2}} = \frac{4V_{cmax}(c_i - \Gamma^*)}{J_{max}(c_i + K)m} \quad (47)$$

560 Substituting equation (47) into equation (45) and expanding the CO₂ limitation term m , we can express
 561 equation (45) as:

$$562 \quad c = \frac{\partial A}{\partial J_{max}} = 16(c_i + 2\Gamma^*)^2 (c_i - \Gamma^*) \left(\frac{V_{cmax}}{J_{max}(c_i + K)} \right)^3 \quad (48)$$

563 Taking typical values of $J_{max}/V_{cmax} = 1.88^{23}$ and $\chi = 0.8^{46}$, we estimate $c = 0.103$ for standard conditions
 564 ($T = 25$ °C, $z = 0$ km, $c_a = 400$ ppm), leading to:

$$565 \quad A = \varphi_0 I_{abs} m \sqrt{1 - \left(\frac{c^*}{m} \right)^{\frac{2}{3}}} \quad (49)$$

566 where

567
$$m = \frac{c_a - \Gamma^*}{c_a + 2\Gamma^* + 3\Gamma^* \sqrt{\frac{1.6D\eta^*}{\beta(K + \Gamma^*)}}} \quad (50)$$

568 and the constant c^* is 4 times c , the unit cost of maintaining J_{max} . As an indirect test of the assumptions,
 569 the responses of J_{max}/V_{cmax} to temperature and CO₂ from equation (48) are compared with observations
 570 (Supplementary Information).

571 A fuller derivation of χ , χ_c and light-use efficiency model is provided in Supplementary Information.

572 **GPP data-model comparison**

573 Equations (2)-(3) yielded modelled site-specific monthly GPP values for comparison with values
 574 independently derived from eddy-covariance measurements of CO₂ exchange in the Free and Fair Use
 575 subset of the FLUXNET archive, using a consistent gap-filling procedure (Supplementary
 576 Information). The monthly GPP data derived from flux measurements are archived in BitBucket (Data
 577 link: <https://bitbucket.org/labprentice/gepisat/src/8d34456aafcd/results>) for public access. For the
 578 modelled values, monthly LUE was estimated based on temperature and vapour pressure extracted
 579 from CRU time-series (TS 3.22) data at 0.5° resolution⁴⁷ and site-observed c_a . Monthly absorbed PPF
 580 was estimated as the product of PPF (0.45 times the WATCH incident surface shortwave radiation⁴⁸,
 581 divided by 0.22 J μmol^{-1}) and the MODIS Enhanced Vegetation Index (EVI), equated to the fraction of
 582 photosynthetically active radiation absorbed by foliage⁴⁹. To match the WATCH data resolution,
 583 wherever each site was located, EVI was upscaled from to the 0.5° grid cell based on the arithmetic
 584 mean of the 100 valid 0.05° pixels within each pixel at the 0.5° resolution.

585 Data availability

586 The global carbon isotope dataset used here is available in GitHub with DOI:
 587 10.5281/zenodo.569501¹⁷.

588

589 **References**

- 590 1 Ciais, P. *et al.* Carbon and other biogeochemical cycles. in *Climate change 2013: the physical*
 591 *science basis. Contribution of Working Group I to the Fifth Assessment Report of the*
 592 *Intergovernmental Panel on Climate Change* (eds Thomas F Stocker *et al.*) Ch. 6, 465-570
 593 (Cambridge University Press, 2014).
 594 2 Friedlingstein, P. *et al.* Uncertainties in CMIP5 climate projections due to carbon cycle
 595 feedbacks. *Journal of Climate* **27**, 511-526 (2014).
 596 3 Prentice, I. C., Liang, X., Medlyn, B. E. & Wang, Y. P. Reliable, robust and realistic: the three
 597 R's of next-generation land-surface modelling. *Atmospheric Chemistry and Physics* **15**, 5987-
 598 6005 (2015).

599 4 Wang, H., Prentice, I. C. & Davis, T. W. Biophysical constraints on gross primary production
600 by the terrestrial biosphere. *Biogeosciences* **11**, 5987-6001 (2014).

601 5 Prentice, I. C., Dong, N., Gleason, S. M., Maire, V. & Wright, I. J. Balancing the costs of
602 carbon gain and water transport: testing a new theoretical framework for plant functional
603 ecology. *Ecology letters* **17**, 82-91 (2014).

604 6 Wright, I. J., Reich, P. B. & Westoby, M. Least - cost input mixtures of water and nitrogen for
605 photosynthesis. *The American Naturalist* **161**, 98-111 (2003).

606 7 Monteith, J. L. Solar radiation and productivity in tropical ecosystems. *Journal of Applied*
607 *Ecology* **9**, 747-766 (1972).

608 8 Farquhar, G. D., von Caemmerer, S. & Berry, J. A. A biochemical model of photosynthetic
609 CO₂ assimilation in leaves of C₃ species. *Planta* **149**, 78-90 (1980).

610 9 Medlyn, B. E. Physiological basis of the light use efficiency model. *Tree Physiology* **18**, 167-
611 176 (1998).

612 10 Ali, A. *et al.* A global scale mechanistic model of the photosynthetic capacity. *Geoscientific*
613 *Model Development Discussions* **8**, 6217–6266 (2015).

614 11 Cai, W. *et al.* Large differences in terrestrial vegetation production derived from satellite-
615 based light use efficiency models. *Remote Sensing* **6**, 8945-8965 (2014).

616 12 De Kauwe, M. G. *et al.* Forest water use and water use efficiency at elevated CO₂: a model -
617 data intercomparison at two contrasting temperate forest FACE sites. *Global Change Biology*
618 **19**, 1759-1779 (2013).

619 13 Medlyn, B. E. *et al.* Reconciling the optimal and empirical approaches to modelling stomatal
620 conductance. *Global Change Biology* **17**, 2134-2144 (2011).

621 14 Diefendorf, A. F., Mueller, K. E., Wing, S. L., Koch, P. L. & Freeman, K. H. Global patterns
622 in leaf ¹³C discrimination and implications for studies of past and future climate. *Proceedings*
623 *of the National Academy of Sciences* **107**, 5738-5743 (2010).

624 15 Cowan, I. & Farquhar, G. Stomatal function in relation to leaf metabolism and environment.
625 *Symposia of the Society for Experimental Biology*, 471-505 (1977).

626 16 Givnish, T. J. *On the Economy of Plant Form and Function*. Vol. 6 (Cambridge University
627 Press, 1986).

628 17 Cornwell, W. K. *et al.* A global dataset of leaf $\Delta^{13}\text{C}$ values. doi:10.5281/zenodo.569501
629 (2017).

630 18 Farquhar, G. D., Ehleringer, J. R. & Hubick, K. T. Carbon isotope discrimination and
631 photosynthesis. *Annual review of plant biology* **40**, 503-537 (1989).

632 19 Körner, C., Farquhar, G. & Wong, S. Carbon isotope discrimination by plants follows
633 latitudinal and altitudinal trends. *Oecologia* **88**, 30-40 (1991).

634 20 Lin, Y.-S. *et al.* Optimal stomatal behaviour around the world. *Nature Climate Change* **5**,
635 459–464 (2015).

636 21 Maire, V. *et al.* The coordination of leaf photosynthesis links C and N fluxes in C₃ plant
637 species. *PloS one* **7**, e38345 (2012).

- 638 22 Haxeltine, A. & Prentice, I. C. A general model for the light-use efficiency of primary
639 production. *Funct. Ecol.* **10**, 551-561, doi:10.2307/2390165 (1996).
- 640 23 Kattge, J. & Knorr, W. Temperature acclimation in a biochemical model of photosynthesis: a
641 reanalysis of data from 36 species. *Plant, cell & environment* **30**, 1176-1190 (2007).
- 642 24 Collatz, G., Berry, J., Farquhar, G. & Pierce, J. The relationship between the Rubisco reaction
643 mechanism and models of photosynthesis. *Plant, Cell & Environment* **13**, 219-225 (1990).
- 644 25 Beer, C. *et al.* Terrestrial gross carbon dioxide uptake: global distribution and covariation with
645 climate. *Science* **329**, 834-838 (2010).
- 646 26 Yuan, W. *et al.* Global comparison of light use efficiency models for simulating terrestrial
647 vegetation gross primary production based on the LaThuile database. *Agricultural and forest
648 meteorology* **192**, 108-120 (2014).
- 649 27 Ainsworth, E. A. & Long, S. P. What have we learned from 15 years of free - air CO₂
650 enrichment (FACE)? A meta - analytic review of the responses of photosynthesis, canopy
651 properties and plant production to rising CO₂. *New Phytologist* **165**, 351-372 (2005).
- 652 28 Frank, D. C. *et al.* Water-use efficiency and transpiration across European forests during the
653 Anthropocene. *Nature Climate Change* **5**, 579-583 (2015).
- 654 29 Maire, V. *et al.* Global effects of soil and climate on leaf photosynthetic traits and rates.
655 *Global Ecology and Biogeography* **24**, 706-717 (2015).
- 656 30 Kaplan, J. O. Geophysical applications of vegetation modeling. (Lund University, 2001).
- 657 31 Chen, J.-L., Reynolds, J. F., Harley, P. C. & Tenhunen, J. D. Coordination theory of leaf
658 nitrogen distribution in a canopy. *Oecologia* **93**, 63-69 (1993).
- 659 32 Vogel, H. Temperaturabhängigkeitsgesetz der Viskosität von Flüssigkeiten. *Physik Z* **22**, 645-
660 646 (1921).
- 661 33 Jacob, D. *Introduction to atmospheric chemistry.* (Princeton University Press, 1999).
- 662 34 Bernacchi, C. J., Singsaas, E. L., Pimentel, C., Portis Jr, A. R. & Long, S. P. Improved
663 temperature response functions for models of Rubisco - limited photosynthesis. *Plant, Cell &
664 Environment* **24**, 253-259 (2001).
- 665 35 New, M., Lister, D., Hulme, M. & Makin, I. A high-resolution data set of surface climate over
666 global land areas. *Climate research* **21**, 1-25 (2002).
- 667 36 Keenan, T. F., Sabate, S. & Gracia, C. Soil water stress and coupled photosynthesis-
668 conductance models: Bridging the gap between conflicting reports on the relative roles of
669 stomatal, mesophyll conductance and biochemical limitations to photosynthesis. *Agricultural
670 and Forest Meteorology* **150**, 443-453 (2010).
- 671 37 Sun, Y. *et al.* Impact of mesophyll diffusion on estimated global land CO₂ fertilization.
672 *Proceedings of the National Academy of Sciences* **111**, 15774-15779 (2014).
- 673 38 Flexas, J., Ribas - Carbo, M., DIAZ - ESPEJO, A., GalmES, J. & Medrano, H. Mesophyll
674 conductance to CO₂: current knowledge and future prospects. *Plant, Cell & Environment* **31**,
675 602-621 (2008).

676 39 Gu, J., Yin, X., Stomph, T.-J., Wang, H. & Struik, P. C. Physiological basis of genetic
677 variation in leaf photosynthesis among rice (*Oryza sativa* L.) introgression lines under drought
678 and well-watered conditions. *Journal of experimental botany* **63**, 5137-5153 (2012).

679 40 Douthe, C., Dreyer, E., Epron, D. & Warren, C. Mesophyll conductance to CO₂, assessed
680 from online TDL-AS records of ¹³CO₂ discrimination, displays small but significant short-
681 term responses to CO₂ and irradiance in *Eucalyptus* seedlings. *Journal of Experimental*
682 *Botany* **62**, 5335-5346 (2011).

683 41 Barbour, M., Warren, C., Farquhar, G., Forrester, G. & Brown, H. Variability in mesophyll
684 conductance between barley genotypes, and effects on transpiration efficiency and carbon
685 isotope discrimination. *Plant, Cell & Environment* **33** (2010).

686 42 Ubierna, N. & Farquhar, G. D. Advances in measurements and models of photosynthetic
687 carbon isotope discrimination in C₃ plants. *Plant, cell & environment* **37**, 1494-1498 (2014).

688 43 Warren, C. R. Stand aside stomata, another actor deserves centre stage: the forgotten role of
689 the internal conductance to CO₂ transfer. *Journal of Experimental Botany* **59**, 1475-1487
690 (2008).

691 44 Smith, E. L. The influence of light and carbon dioxide on photosynthesis. *The Journal of*
692 *general physiology* **20**, 807-830 (1937).

693 45 Harley, P. C., Thomas, R. B., Reynolds, J. F. & Strain, B. R. Modelling photosynthesis of
694 cotton grown in elevated CO₂. *Plant, Cell & Environment* **15**, 271-282 (1992).

695 46 Lloyd, J. & Farquhar, G. D. ¹³C discrimination during CO₂ assimilation by the terrestrial
696 biosphere. *Oecologia* **99**, 201-215 (1994).

697 47 Harris, I., Jones, P., Osborn, T. & Lister, D. Updated high-resolution grids of monthly climatic
698 observations—the CRU TS3.10 Dataset. *International Journal of Climatology* **34**, 623-642
699 (2014).

700 48 Weedon, G. P. *et al.* The WFDEI meteorological forcing data set: WATCH Forcing Data
701 methodology applied to ERA-Interim reanalysis data. *Water Resources Research* **50**, 7505-
702 7514 (2014).

703 49 Xiao, X., Zhang, Q., Hollinger, D., Aber, J. & Moore, B. I. Modeling gross primary
704 production of an evergreen needleleaf forest using MODIS and climate data. *Ecol. Appl.* **15**,
705 954-969 (2005).

706

