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1 **NUMERICAL INVESTIGATION OF AIR INTRUSION AND**
2 **AEROBIC REACTIONS IN MUNICIPAL SOLID WASTE**
3 **LANDFILLS**

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Numerical Investigation of Air Intrusion and Aerobic Reactions in Municipal Solid Waste Landfills

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ABSTRACT: Air intrusion into municipal solid waste landfills can cause a localized switch from anaerobic to aerobic biodegradation adjacent to the intrusion. The purpose of this study was to explore the effects on temperature and gas composition of air intrusion into an idealized anaerobic landfill. Two scenarios of air intrusion and injection were simulated using a mechanistic landfill model built into TOUGH2. The modeled landfill geometry and properties are based on an actual U.S. landfill. The simulation results show that air intrusion can cause a quick switch from anaerobic to aerobic conditions and as a result, cause a fast increase in temperature of up to 30°C associated with stimulation of aerobic biodegradation reactions. Associated with the change to aerobic conditions is a decrease in CH₄/CO₂ (v/v) ratio in the landfill gas. Depending on the air flow rate intruding or injecting into the landfill, localized aerobic biodegradation is stimulated and as a result heat flux of 10 to 150 W/m³ leads to temperature increase. Temperature increase near the interim system lasts no longer than few weeks while the high temperatures in deep layers could last up to one year.

Keywords: aerobic biodegradation, modeling municipal solid waste, biodegradation of municipal solid waste, landfill gas generation

80 1. INTRODUCTION

81 Municipal solid waste (MSW) landfills are designed and constructed to operate under a
82 temperature regime that allows anaerobic biological processes to decompose organics into
83 methane gas as a renewable energy resource (National Research Council 2007). However, there is
84 an increased awareness in the solid waste industry that industrial and special wastes co-disposed
85 in MSW landfills can result in chemical reactions that generate and accumulate heat within the
86 waste, thus raising temperatures above the threshold of anaerobic biological processes (assumed
87 as exceeding 65°C or 150°F; Hartz et al. 1982; Kasali et al. 1989; Yeşiller et al. 2005; Zinder
88 1993). Examples of exothermic industrial wastes include aluminum production wastes, MSW
89 incinerator ash, coal bottom ash, lime/cement kiln dust, and fly ash (Jafari et al. 2017; Klein et al.
90 2001, 2003). The associated chemical reactions involve the corrosion of aluminum and iron
91 (Calder and Stark 2010; Jafari et al. 2014), along with hydration and carbonation of calcium oxide
92 and calcium hydroxide (Narode et al. 2021), respectively. Another possible contributor to heat
93 generation and accumulation is the introduction of air into a landfill during gas collection and
94 control operations. This is separate from landfill aeration (Ritzkowski and Stegmann 2012), which
95 explicitly uses forced air injection to promote the aerobic biodegradation of MSW to mitigate CH₄
96 emissions and enhance the rate of waste stabilization (Read et al. 2001). For example, Haug (2018)
97 observed temperatures of 70°C when air was injected into enclosed cells composed of wastewater
98 treatment sludge over 24 days. Themelis and Kim (2002) monitored a 600 m² by 3 m deep aerobic
99 cell and reported that 75% of heat generated from aerobic reactions was retained in the waste, with
100 25% heat loss occurring due to natural convection and radiation to the surroundings. These
101 demonstration studies imply that while air injection can accelerate waste stabilization, it also
102 creates a significant challenge by accumulating heat (Merz and Stone 1962). As a result, there is a

103 need to quantify the magnitude and rate of heat generation based on air flux, spatial extent of
104 aerobic reactions, and rate of heat dissipation. Hashemi et al. (2002) and Sanchez et al. (2006)
105 developed a 3D model of gas generation and transport in a hypothetical landfill and investigated
106 the effects of various physical properties of porous on gas pressure, fluid transfer, temperature.
107 Hao et al. (2020) modeled 3D hypothetical landfill to estimate heat generation, transport, and
108 accumulation. Their result showed that ash disposal causes temperature increase to 200°C within
109 first 6 years of landfilling.

110 In this study, possible pathways of air intrusion into landfills were simulated to understand
111 their potential contribution to heat generation and accumulation, along with moisture
112 redistribution, in the waste mass. The TOUGH2 Landfill Bioreactor Model (T2LBM; Oldenburg
113 2011) was used to simulate multiphase flow in an idealized landfill undergoing either anaerobic or
114 aerobic biodegradation depending on the local oxygen concentration. An idealized 2-D landfill
115 model was developed based on an operating landfill in the Midwest, with three MSW layers
116 representing waste of varying ages with a static initial moisture distribution as controlled by
117 gravity and capillary pressure, and undergoing anaerobic biodegradation with active gas extraction
118 wells. Air intrusion was modeled as occurring due to gas extraction wells unintentionally pulling
119 air into the waste mass through cracks in the soil cover, and secondly as leaks in air lines used to
120 pressurize gas well liquid pumps that remove condensate and leachate collected inside gas
121 extraction well pipes. As air permeates into the landfill from these hypothetical sources, the spatial
122 and temporal changes in temperature, gas composition, pressure, and flow rate, and liquid
123 saturation are simulated and mapped to discern the zone of influence of aerobic reactions and the
124 duration of higher temperatures and oxygen that remain in the landfill after the air intrusion has
125 been remediated. As previously stated, the air line leak included in this study was based loosely

126 on an actual air line leak event at an MSW landfill in the southern US. The input parameters (such
127 as line diameter, flow rate, and generalized depth) were obtained from field personnel associated
128 with the landfill operation.

129 While the potential for subsurface oxidation events from overpulling of air into the waste
130 mass from gas extraction wells is well understood in the solid waste industry, the magnitude and
131 reaction times from a larger scale air intrusion, such as an air line break, has not been modeled.
132 Such a numerical investigation of air intrusion and aerobic reactions can also serve to inform the
133 magnitude of temperature propagation from a larger scale event. The results of this study can
134 enable practitioners and regulators to quantify the complex and coupled biological, thermal, and
135 flow behaviors of landfills under changing anaerobic-aerobic conditions. It could also facilitate a
136 better understanding of the short- and long-term implications to of air intrusion to landfill
137 operations and maintenance, including reduced renewable energy production, localized
138 differential settlement, and reduced service life of geosynthetics (Jafari et al. 2014).

139

140 **2. T2LBM BIODEGRADATION REACTIONS**

141 The TOUGH2 Landfill Bioreactor Model (T2LBM) (Oldenburg 2001) was built onto TOUGH2
142 to allow mechanistic simulation of a simplified set of aerobic and anaerobic landfill biodegradation
143 reactions, along with the non-isothermal multiphase and multicomponent flow and transport
144 simulated by TOUGH2 (Pruess et al. 1999). T2LBM incorporates the biodegradation of a single
145 mobile biodegradable substrate proxy (MBSP) that represents all of the biodegradable material in
146 the MSW. This approach assumes implicitly that early stages of anaerobic or aerobic
147 biodegradation of organics previously occurred (hydrolysis, acetogenesis, and acidogenesis) and
148 places the model focus on the last biodegradation step of methanogenesis (landfill gas production)

149 through biodegradation of the MBSP. The earlier phases of biodegradation involving the formation
150 of MBSP can be phenomenologically modeled by the user through inputs that specify various local
151 initial concentrations or variable generation rates of MBSP (Oldenburg 2001). T2LBM uses a
152 Monod kinetic rate law to simulate the biodegradation reactions in the aqueous (liquid) phase of
153 the two-phase (gas and liquid) model system.

154 T2LBM has been verified by comparison to bench-scale laboratory and field-scale
155 configurations of anaerobic and aerobic treatment of MSW by leachate recirculation, air injection,
156 temperature control, and waste placement as described in Oldenburg (2001). Specifically, the
157 dynamics of aerobic biodegradation simulation of T2LBM were compared and verified with the
158 results from laboratory experiments of Kaiser and Soyez (1990) as documented in Kaiser (1996).
159 The methane production activity during anaerobic biodegradation of a small mass of waste mixed
160 with acetate given by Lay et al. (1998) was simulated and compared with the experimental results.
161 While some properties of the experimental system by Kaiser (1996) was used directly, some other
162 properties were derived due to the specific process model conceptualization of T2LBM. With
163 constraints on many properties of the system prescribed by the experimental specifications, there
164 are at least two important parameters to adjust to fit T2LBM results with the results shown in
165 Kaiser (1996). These included the initial mass fraction of MBSP in the liquid, and the single
166 microbial growth rate for the breakdown of a single chemical species (MBSP) as proxy for
167 numerous microbial populations and substrates. Agreement of temperature, CO₂, O₂ consumption
168 between experiment and T2LBM was good.

169 T2LBM includes five volatile chemical components distributed between gas and liquid
170 phases, which are water (H₂O), nitrogen (N₂), oxygen (O₂), carbon dioxide (CO₂), and methane
171 (CH₄). The biodegradable component, MBSP, resides only in the liquid phase. The solid phase in

172 T2LBM comprises the grains of the porous medium and is assigned the thermo-physical properties
173 of MSW material. The five volatile components are distributed between the aqueous (liquid) and
174 gas phases as controlled by the local solubility specified by Henry's law.

175 The substrate utilization rate in T2LBM follows the Monod kinetic rate equation. In
176 general, the rate of substrate utilization in T2LBM is estimated by Eq. (1):

177

$$178 \quad \frac{dS}{dt} = -\frac{1}{Y} \left(\frac{dB}{dt} + \delta B \right) = -\frac{1}{Y} (\mu_B B + \delta B) \quad (1)$$

179

180 Eq. (1) describes the mathematical relationship between microbial biomass and nutrient
181 consumption (substrate utilization) in an aqueous environment over time, where S is substrate
182 (MBSP) concentration, Y is yield coefficient, B is bacterial concentration (aerobic or anaerobic
183 depending on the presence or absence of O_2), δ is the microbial death rate, and μ_B is the microbial
184 growth rate. Yield coefficient is the ratio of the amount of biomass produced to the amount of
185 substrate consumed. The microbial growth rate is a function of several parameters in Eq. (2):

186

$$187 \quad \mu_B = \mu_{\max,B} f_B^T \frac{S}{K_{S,B} + S} - \delta \quad (2)$$

188

189 where μ_{\max} is the maximum specific growth rate, f_B^T is the coefficient of temperature-dependent
190 growth, and $K_{S,B}$ is the microbial saturation constant. In Eq. (2), μ_{\max} and $K_{S,B}$ are empirical
191 coefficients that differ between microorganism species and depend on the ambient environmental
192 conditions, e.g., temperature, pH of the aqueous phase, and composition of the microbial medium.

193 Temperature dependence of the biodegradation is included through the function f_B^T in

194 Eq. (3):

195

196

$$f_B^T = \frac{T(T_{\max,B} - T)}{\left(\frac{T_{\max,B}}{2}\right)^2} \quad (3)$$

197

198 where $T_{\max,B}$ is the maximum tolerable temperature for anaerobic and aerobic bacteria, and T is the

199 temperature at any time (°C). In this model, the maximum tolerable temperatures for anaerobic

200 and aerobic biodegradation are assumed to be 65°C and 80°C, respectively (De la Cruz et al. 2021;

201 Jafari et al. 2017; Rowe & Islam 2009; Yazdani et al. 2010; Yeşiller et al. 2005; Zinder 1993)

202 which means at temperatures above these values the biodegradation reaction is inhibited ($f_B^T = 0$).

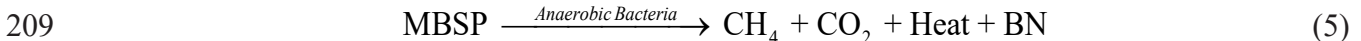
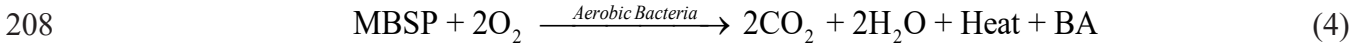
203 The idealized aerobic and anaerobic biodegradation reactions modeled in T2LBM follow the

204 formulas in Eqs. (4) – (5), where BA and BN represent Aerobic Biomass and Anaerobic Biomass,

205 respectively. Complete details of the biological reactions in T2LBM can be found in Oldenburg

206 (2001).

207



210

211 In this study, T2LBM was used to simulate the spatial and temporal variation in gas,

212 moisture, and heat transfer due to air intrusion, the process by which the MSW landfill

213 biodegradation switches from an anaerobic to aerobic process. Before simulating the air intrusion

214 into the landfill model system described in the next section, an anaerobic simulation was conducted

215 to reach initial conditions found during the methanogenesis stage of MSW, specifically the

216 temperature, fluid pressure, gas composition, and liquid saturation. The transition from anaerobic

217 to aerobic condition in T2LBM is calculated and handled at each iteration, with the results
218 weighted by an arctan switching function:

219

$$220 \quad a = \frac{1}{2} + \frac{1}{\pi} \tan^{-1} \left(\text{switchf}(X_{liq}^{O_2} - X_{critical}^{O_2}) \right) \quad (6)$$

221

222 In Eq. (6), a varies from ~ 1 for $X_{liq}^{O_2} \geq X_{critical}^{O_2}$, to ~ 0 for $X_{liq}^{O_2} \leq X_{critical}^{O_2}$. The steepness of the

223 transition around $X_{critical}^{O_2}$ is controlled by the user through the variable *switch* in the input file.

224 This approach provides a smooth transition from anaerobic to aerobic conditions. The term

225 aerobicity is given to the function a and is given as primary output from T2LBM to delineate

226 aerobic and anaerobic regions of the domain. This also makes possible that anaerobic reactions be

227 only partially inhibited by air injection, and subsequent aerobic reaction and temperature increase.

228

229 **3. LANDFILL MODEL SYSTEM**

230 **3.1. Landfill Geometry**

231 The idealized 2-D model system in Fig. 1 is representative of a specific Midwest landfill. The 2-

232 D landfill was developed with the bottom and top lengths equal to 356 m and 148 m, respectively,

233 along with a height of 48 m and side slopes of 3H:1V. The landfill domain was discretized into

234 grid blocks of sizes 1 m in the vertical direction and 2 m in the horizontal direction. The model

235 includes five horizontal layers starting from the landfill base as follows: (1) Bottom layer (1 m

236 thick) that serves as a no-flow boundary condition for gas and leachate; (2) Three MSW layers

237 (shallow, intermediate, and deep) that vary in physical, thermal, hydraulic, and biological

238 properties (i.e., density, porosity, specific heat conductivity); and (3) Surface cover layer that was

239 either modeled as a geomembrane or clay cover material with a thickness of 1 m depending on the

240 scenario analyzed. The model system represents initially a closed landfill that is capped with a
241 cover system and is operating under anaerobic conditions for several years until it is subject to air
242 intrusion. In Fig. 1, the thicknesses of shallow and intermediate MSW layers were set to 18 m
243 each, and the deep layer thickness was set to 12 m. The gas extraction wells were located 50 m
244 apart with different slot lengths and extraction rates (see Table S2).

245

246 **3.2. Boundary Conditions**

247 Conditions of constant atmospheric pressure and temperature (101 kPa and 25°C, respectively) are
248 maintained at the top of the landfill cover. Various properties of the surface clay cover material
249 are specified to model the sealing properties (no air intrusion) and the failures of the cover (e.g.,
250 cracks or other openings) depending on the scenario being simulated. The boundary condition
251 between the deep MSW layer and native foundation (bottom of domain) is modeled to prevent
252 fluid (gas and leachate) advection but allow heat transfer. In TOUGH2, by assigning infinite heat
253 capacity or infinite volume of grid block, the user can create a first-type boundary condition. In
254 this model, infinite specific heat capacity was assigned to the grid blocks of atmospheric grid
255 blocks layer so that the temperature is set and remains at 25°C ($\partial T/\partial t \sim 0$). Very low permeability
256 was assigned to clay layer to prevent any fluid flow transfer. The bottom domain boundary
257 condition is extended to the vertical side walls. Thus, the underlying geology outside of the landfill
258 boundary serves only as a heat sink.

259

260 **3.3. Material Properties**

261 The thermal-hydraulic-physical material properties for the three MSW layers, along with the clay
262 used as the surface and bottom layers, are summarized in Table 1. The properties were selected to
263 reflect the fact that generally the degree of MSW biodegradation and consolidation increase from
264 shallow to deep layers, e.g., density increases with depth, and porosity and hydraulic conductivity
265 decrease with depth.

266 The porosity (n) of MSW also decreases with depth to reflect less void space and thus a
267 more compacted waste mass. The case study landfill on which this model is based was filled
268 rapidly over a period of around 8 years. It was assumed that the shallow layer was less than 2 years
269 old. Therefore, the shallow layer is considered to be freshly land-filled MSW, which has undergone
270 limited biological degradation and compaction compared to the older and higher density
271 intermediate and deep layers.

272 The bulk density of MSW varies from 300 to 1,734 kg/m³ (equivalent to a unit weight of
273 3 to 17 kN/m³), depending on the MSW age and applied stress as measured in laboratory
274 experiments (Beaven 2000; Kavazanjian et al. 1995; Zekkos et al. 2006). The intrinsic
275 permeability of MSW was found based on correlations with MSW density (Staub et al. 2009; Xu
276 et al. 2020). The specific intrinsic permeability values assigned to MSW layers were developed
277 based on the applied stresses estimated in the case study, and the values are within the range
278 reported in Breitmeyer and Benson (2019) and Beaven (2000). To estimate intrinsic permeability,
279 the effective stress in the middle of each MSW layer was related to permeability as a function of
280 normal stress. The estimated effective stress of 60 kPa, 213 kPa, and 360 kPa for the shallow,
281 intermediate, and deep MSW layer, respectively. The results in the study of Beaven (2000) shows
282 that in the same range of applied stress on various MSW samples, the hydraulic conductivity is

283 between 10^{-7} to 10^{-4} m/s, which is equivalent to permeability of 10^{-14} to 10^{-11} m² (assuming the
284 density and viscosity of water at ambient conditions).

285 T2LBM uses intrinsic permeability (k) of a porous medium rather than hydraulic
286 conductivity (K). At 20°C, the density and dynamic viscosity of water are $\rho_w = 1,000$ kg/m³ and η
287 $= 1 \times 10^{-3}$ kg/(m·s), respectively. Therefore, one unit of K (m/s) will be approximately equal to 1
288 $\times 10^7$ units of k (m²).

289

$$290 \quad K = \frac{\rho_w g k}{\eta_w} \quad (7)$$

291

292 The shallow layer density ($\rho = 750$ kg/m³) is adapted from Staub (2009), who found the
293 saturated vertical hydraulic conductivity to be $K_v = 3 \times 10^{-5}$ m/s at an initial volumetric moisture
294 content (θ) of 21% (gravimetric moisture content (w) of 37%) and porosity $n = 0.6$. This also aligns
295 with Beaven (2000), who reported $K_v = 2 \times 10^{-5}$ m/s for an unprocessed-fresh household waste
296 material under applied stresses ranging from $\sigma_v = 0$ to 84 kPa and $\rho = 700$ to 840 kg/m³. Beaven
297 (2000) indicated that the K_v of an excavated and aged MSW (approximately 20 years old) was $6 \times$
298 10^{-6} and 5×10^{-7} m/s ($k_v = \sim 5 \times 10^{-13}$ m²) under applied stresses of 165 and 322 kPa, respectively.
299 Because the K_v of MSW is inversely related to ρ , n , and σ_v (Townsend et al. 2015), it decreases
300 with increasing depth in the landfill. Because field observations of landfills indicate better drainage
301 in the horizontal direction, the MSW is assumed to be anisotropic with k_h that is one order of
302 magnitude higher than k_v (Jain et al. 2006). The soil water retention curves (SWRCs) and hydraulic
303 conductivity functions (HCF) for each MSW layer follow laboratory experiments by Breitmeyer
304 et al. (2019), Breitmeyer and Benson (2014), and Stoltz et al. (2010).

305 The thermal conductivity (K_T) of MSW ranges from 0.2 to 1.5 W/(m·K) (Faitli et al. 2015;
306 Gholamifard et al. 2008; Rollins et al. 2005). The K_T increases from 0.3 to 0.9 W/(m·K) with depth
307 because higher densities facilitate more particle to particle contact and increasing water content
308 facilitates heat transfer (Yeşiller et al. 2015). The heat capacity (C_p) of MSW typically involves
309 weighted averaging of the heat capacities of the individual of MSW components. For example,
310 Hanson et al. (2008) report the volumetric C_p of MSW landfills located in Michigan, New Mexico,
311 Alaska, and British Columbia as 2, 1.2, 1, and 2.2 MJ/(m³·K), respectively. The value from the
312 Michigan MSW ($C_p = 2$ MJ/m³·K) was used because our study is loosely based on a Midwestern
313 landfill. The volumetric C_p was converted to a specific C_p (J/kg·K) using the density of each MSW
314 layer. A sensitivity analysis was performed on the influence of C_p on heat transfer.

315

316 **3.4. Gravity Capillary Equilibrium**

317 T2LBM offers a choice of several SWRC functions to simulate the transport of wetting and non-
318 wetting fluid mixtures in unsaturated porous media. Laboratory and field experiments suggest that
319 the van Genuchten (1980) model captures the behavior of MSW (Breitmeyer and Benson 2014;
320 Stoltz et al. 2012). Fig. S1 shows the degree of saturation (S) as a function of matric suction (ψ)
321 for each material layer, and Table S1 lists the TOUGH2 input parameters for van Genuchten (1980)
322 function. To replicate the landfill in Fig. 1 with side slopes, a physically reasonable steady-state
323 simulation is required to reach gravity-capillary equilibrium (static steady-state moisture
324 distribution) before applying the biological reactions. Under partially saturated conditions, gravity
325 will move water down and capillarity can spread water vertically until a steady-state condition is
326 reached (Yortsos 1995). The steady-state condition is subsequently used as the initial conditions

327 for the transient analyses. The generation of gravity-capillary equilibrium for this complex 2-D
328 model is explained in detail in supplemental and shown in Fig. S2.

329 In the shallow and intermediate MSW layers, the S does not vary with depth and remains
330 constant at 32% and 43%, respectively. The matric suction values corresponding to the shallow
331 and intermediate layers are 3.5 kPa, and 1.5 kPa, respectively. In the deep MSW layer, the S
332 increases from 50% to 100% at the leachate collection system. The matric suction is less than 1
333 kPa in this layer. After reaching gravity-capillary equilibrium, the anaerobic biological reactions
334 were initiated. The modeled landfill is assumed to be at a stage where waste acceptance is near
335 completion, a surface cover system is present, and gas extraction wells are operating. At this stage,
336 the model is calibrated such that the MSW layers are undergoing anaerobic biodegradation with
337 the ratio of CH_4 to CO_2 equal to unity and the temperature profiles reflect observed waste
338 temperatures in the methanogenesis stage (Yesiller et al. 2005; Hanson et al. 2010).

339

340 **3.5. Gas Collection System: Well Properties**

341 The design of gas extraction systems is an essential element for management of large MSW
342 landfills (Fabbricino 2007). Landfill gas operators apply a vacuum of 5 cm to 50 cm of water head
343 in the well, which results in typical gas flow rates less than 25 m³/hour, equivalent to ~15 standard
344 cubic feet per minute (scfm) at 20°C and 1 atm. T2LBM provides two options to simulate gas
345 extraction. In the first option, the user can specify a fixed mass extraction rate (kg/s) to any desired
346 grid block. By this approach, the grid block will behave as a sink for the specified mass component
347 with the specified rate. The advantage is the simplicity of implementing the extraction rate in the
348 model and thus the straightforwardness in flow rate calculations for a column of grid block sinks
349 (e.g., modeling a single extraction well). On the other hand, the disadvantage is that the extraction

350 rate is a fixed term, which results in two consequences. As mentioned in earlier sections, T2LBM
351 incorporates Monod kinetics to simulate substrate utilization and biomass growth and decay. The
352 biogas generation resulting from this kinetics-controlled biodegradation process will follow a non-
353 linear path. There is no obvious method to match the fixed constant rate of mass extraction
354 specified in the sink grid block(s) with the kinetics-controlled (varying with time) production rate.
355 As a result, the gas pressure could increase or decrease unphysically and out of range of an actual
356 landfill. The other disadvantage of this option is that excessive gas extraction may cause gas-phase
357 disappearance (a situation in an unsaturated model that is physically impossible), which causes
358 non-convergence issues in the simulation.

359 The alternative option is to utilize the *well on deliverability* model available in TOUGH2.
360 The user can specify a constant vacuum pressure (P_{wb}) for any individual well grid block, and the
361 pressure difference (drawdown) will direct the fluid flow toward these gas well grid blocks at the
362 appropriate rate. The advantage of this option is that non-linear gas production rate will naturally
363 be accommodated by increasing or decreasing the well productivity. Thus, the landfill simulation
364 will more accurately model actual landfill and biogas well extraction behavior. The drawback to
365 this approach is the relative complexity in the design of the well discretization and assignment of
366 parameters for the gas well grid blocks. The heterogeneity of the MSW layers must also be taken
367 into account. If a well is located in multiple layers with different horizontal permeability, different
368 values of the productivity index (PI) should be defined.

369 In this model landfill system, six (6) gas extraction wells 50 m apart with different slot
370 lengths and extraction rates were modeled. The extraction rate equation is estimated in Eq. (8) for
371 a steady radial flow in layer l :

372

$$PI_l = \frac{2\pi(k\Delta z_l)}{\ln(r_e/r_w) + \left(\frac{s-1}{2}\right)} \quad (8)$$

$$r_e = \sqrt{A/\pi} \quad (9)$$

where Δz_l denotes the layer thickness (slot length of well in each layer), $k\Delta z_l$ is the permeability-thickness product in layer l (see Table 1 for k_x values), r_e is the effective radius of the grid block (see Eq. (9)), r_w is the well radius (12.5 cm for all gas wells), and s is the skin factor (neglected in this study), and A is the connection area (flow cross-section = 2 m²) of the grid blocks.

The skin factor represents fluid flow restriction that can cause pressure drop near the well, and it can be used as a calibration factor to match measured flow rates (Chen et al. 2021). This parameter was assumed to be unity in the present study making the skin term in Eq. (8) equal to zero. This was considered reasonable because the study is focused on replicating general landfill field conditions, with the intent on performing sensitivity analyses.

The flow rate of fluid phase into the extraction wells is calculated based on Eq. (10) (Pruess et al. 1999), where the extraction wells operate under a pressure differential with P_{wb} serving as the reference well pressure. In this option, the mass production rate of fluid phase (β) from a grid block is estimated in Eq. (10) when the phase pressure $P_\beta > P_{wb}$:

$$q_\beta = \frac{k_{r\beta}}{\mu_\beta} \rho_\beta PI (P_\beta - P_{wb}) \quad (10)$$

where $k_{r\beta}$, ρ_β , and μ_β are relative permeability, density and dynamic viscosity of fluid phase β , respectively, and P_β is the pressure of fluid phase β in the grid block(s) adjacent to the grid block at the bottom of the well. Because of the unsaturated nature of this model, the extraction wells in the landfill only collect gas phase generated in the landfill (along with air injected or leaking in from

396 external sources), not the liquid phase. Therefore, the wells are referred to as a “gas collection” system
397 in this model.

398 The well properties, operational parameters, and spacing of the landfill gas collection
399 system control gas collection efficiency. The choice to use the productivity index option as the
400 basis of the gas collection system design was discussed above. With this choice made, well spacing
401 is critical because of the direct impact of radius of influence (ROI) of the gas wells on the collection
402 efficiency. The ROI is defined as the radial distance that a vertical well can effectively extract
403 landfill gas (US EPA 2017). Vigneault et al. (2004) describe the ROI as the average radial distance
404 from a gas collection well defining a volume within which 90% of the landfill gas generated in the
405 waste is collected at the well, which primarily depends on MSW physical properties, gas
406 generation rate, and pressure (Vigneault et al. 2004). Feng et al. (2017) indicate that the varying
407 physical properties and age of MSW with depth and vacuum pressure are key parameters to
408 consider when designing the well spacing and ROI. Vigneault et al. (2004) show that a vacuum of
409 4.5 kPa (45 cm of water) results in a radial influence of 33 m at peak methane generation. Feng et
410 al. (2017) indicate that radius of influence is 25 m at a vacuum of 4 kPa (40 cm of water). In the
411 T2LBM model, the 50 m distance between gas wells requires the ROI not to be less than 25 m.
412 Thus, the vacuum of 5 kPa (50 cm of water) was applied to each gas well so that the minimum
413 ROI of 25 m for each gas well is achieved.

414

415 **3.6. Enthalpy of Reactions**

416 Due to the diversity of MSW composition, many substrates, such as proteins and carbohydrates,
417 can undergo biological biodegradation. In T2LBM, MBSP releases approximately the same heat
418 per mole as that of cellulose. Specifically, anaerobic and aerobic biodegradation of MBSP release

419 ~1.0 and 15 MJ/kg of MBSP, respectively. This approach was also implemented by Hao et al.
420 (2017), where they defined the main heat generation rates arising from aerobic and anaerobic
421 biodegradation of cellulose. The enthalpy of anaerobic and aerobic biodegradation set in the model
422 have direct correlation with maximum heat generation of these reactions which is discussed and
423 compared with heat generated from composted piles in section 5.2.

424

425 **3.7. Biological Reaction Parameters**

426 T2LBM incorporates Monod kinetics to model the biological reactions. Monod kinetics vary not
427 only for each bacterial species but also for the environment in which bacterial communities are
428 growing. Simplifications must be made to model the highly complex biological processes, and
429 calibrations are needed to tune the overall effect of simplified biodegradation reactions. The kinetic
430 parameters used for each biological reaction are listed in Table S3. Anaerobic biomass yield
431 coefficient (Y), maximum growth rate (μ_{max}), and decay rate (δ) values are within the range of
432 study results by El-Fadel et al. (1997) and Pareek et al. (1999). The yield coefficient of the aerobic
433 biomass is selected from Oldenburg (2001), which were validated against the bench-scale reactor
434 experiments by Kaiser (1996). Sensitivity assessment of input variables is a crucial part of
435 ecological and environmental related numerical simulations (Baharvand et al. 2020; Baharvand
436 and Laskar-Ara 2021). Sensitivity analysis and model calibration were conducted to determine
437 parameter values for which simulation results would fit with the real landfill data. This step of the
438 study developed the initial conditions for further modeling scenarios of air intrusion. The
439 sensitivity analyses were focused on identifying the pertinent biological reaction parameters (listed
440 in Table S3) that controlled the magnitude and time rate of gas production. In the next step, a
441 LandGEM model was developed for the landfill site, which produced a cumulative gas production

442 over 30 years based on incoming waste and air space. The MSW mass of the LandGEM and
443 T2LBM models were normalized to match a gas production curve with LandGEM (see Fig. S3).
444 While in the range reported in the literature, gas collection system performance was expanded
445 based on gas production performance of the model. Sensitivity analyses on parameters listed in
446 Table S2 were conducted such that the gas collection system was performing to metrics reported
447 in the literature.

448 The critical O₂ concentration in the model was set to 0.18 mg/L (~ 2% v/v in gas phase).
449 The concept of critical O₂ simply means that the aerobic bacteria cannot grow at O₂ concentrations
450 below that value. Different results were reported by various researchers for this value. Aerobic
451 activities were observed at O₂ levels of 1 to 3% v/v (Hale Boothe et al. 2001; Powell et al. 2006),
452 while Yazdani et al. (2010) indicated that even at O₂ levels above 15% the aerobic activity was
453 either not observed or very difficult to achieve at some locations of a aerated MSW landfill cell.
454 Megalla et al. (2016) shows that aerobic activity starts at 2 to 3% v/v and reaches to peak aerobic
455 activity at O₂ level of 9% v/v.

456

457 **4. DEVELOPMENT OF ANAEROBIC INITIAL CONDITIONS**

458 **4.1. Biogas Generation**

459 LandGEM was used to calibrate the anaerobic biological parameters and verify the gas production
460 of the system (Alexander et al. 2005). The conventional value for CH₄ generation constant (k_M) in
461 the non-arid region (0.04 year⁻¹) was selected, along with the potential methane generation capacity
462 (L_o) of 100 m³/Mg. The case study considers landfilled ~15 million Mg over 8 years. To compare
463 LandGEM gas generation to T2LBM, the gas generation rates were normalized to the Mg of waste
464 in each respective model. For example, the T2LBM model consists of 12,000 Mg of MSW (volume

465 per grid block \times bulk density of MSW \times number of grid blocks). As a result, gas generation was
466 modeled to replicate the LandGEM gas production such that the maximum biogas was generated
467 over the first 8 years and the rate of biodegradation exponentially decreased over the next 50 years.
468 The cumulative biogas production in Fig. S3 represents the six gas wells over the \sim 60 years of
469 operation.

470

471 **4.2. Gas Collection System Performance**

472 The parameters r_e , r_w , and s in Eq. (8). were fit and listed in Table S2 such that the gas extraction
473 flow rates range between 1.7 to 34 m³/min and the ROI of adjacent wells overlap (i.e., ROI is at
474 least 50 m). This design basis and related sensitivity analyses led us to assign the specified values
475 for each well at different layers in Table S2. The gas collection wells typically operate with a
476 controllable vacuum, where the gas flow rates range from 0 to 25 m³/hour (0 to 15 scfm) depending
477 on the screen length and location. Thus, the proper PI and P_{wb} were assigned to the gas wells to
478 reflect this range of gas extraction. In particular, Fig. S4 shows gas wells GW-3 and GW-4 extract
479 the most biogas, peak of 6 m³/yr/Mg MSW after \sim 5 years before exponentially decreasing to less
480 than 3 m³/yr/Mg MSW after \sim 20 yrs. In contrast, the gas wells GW-1, 2, 5, and 6 collect less than
481 1 m³/yr/Mg MSW. Thus, the majority of the gas extraction stems from the central two gas wells.
482 The total gas extraction rate peaks at 14 m³/yr/Mg MSW (\sim 11 scfm) after \sim 5 yrs.

483

484 **4.3. Temperature and Pressure**

485 Fig. 2 shows the spatial and temporal changes in temperature and pressure with the onset of
486 anaerobic decomposition. In particular, Fig. 2(a) shows that the maximum temperature occurs
487 within the middle third of the landfill after year 5. Fig. S5 shows temperature contour plots for the

488 landfill at years 1, 5, 15, and 30, which are parabolic with the maximum temperature in the middle
489 depth. The atmosphere and underlying soil below the composite liner system serve as heat sinks.
490 Fig. 2(b) shows the gas pressure remains constant with depth until it reaches the lowest MSW
491 layer. The vectors in Fig. 2(b) correspond to the direction and magnitude of gas flowing to the gas
492 extraction wells. For example, the shallow layer exhibits the most gas flow, collected by GW-3
493 and GW-4, because of the lower hydraulic conductivity and less decomposition. This implies that
494 slot lengths extending closer to the surface could be an effective tool in collecting high methane
495 yields in shallow layers. The performance of each gas collection well is shown in Fig. S4, where
496 the maximum gas collection is occurring at year 5.

497 In Fig. 2(c), the modeled landfill temperatures are presented 1, 5, 15, 20, and 30 years after
498 initiating the simulation. Landfill temperatures are simulated for 60 years for anaerobic
499 biodegradation, but the temperature is constant after 30 years. Although the inhibiting temperature
500 for anaerobic biodegradation is assumed to be 65°C and above, the temperature reaches to a
501 maximum value of 60°C after 6 years which is dependent on anaerobic heat generation rate,
502 moisture content, available substrate, and thermo-physical properties of MSW. At 6 years, the gas
503 generation rate is also at its maximum, and the gas collection system is operating at its highest
504 recovery rate (see Eq. 10). The temperatures are spatially distributed such that the middle third of
505 the landfill is warmest and coolest at the surface cover system-atmosphere boundary, which aligns
506 with the results of Hanson et al. (2010). The temperature profile after 15 years indicates that heat
507 generation from anaerobic microbial activity is decreasing after reaching the peak of microbial
508 activity, resulting in lower temperatures compared to year 5 because of heat loss through the top
509 boundary. The temperature decreases to 45°C in the center of the landfill after 30 years.

510 The temporal variation of landfill gas pressures in Fig. 2(d) are obtained from the center
511 line in Fig. 2(b). Gas pressures increase concomitantly with increasing gas production, from
512 atmospheric pressure at the start of simulations to 35 kPa at year 5. At peak gas production (year
513 5), the gas pressure is 36 kPa, and it decreases to 8 kPa by year 30. This suggests that excess gas
514 pressures exist even though the gas wells are extracting gas at a vacuum of 5 kPa. The gas pressure
515 is constant along the depth of shallow and intermediate MSW layers, but it increases with depth in
516 the deep MSW layer. This is likely attributed to the degree of saturation increasing the deep layer
517 towards the leachate level and thus inhibiting gas transport (i.e., build up occurs).

518

519 **5. RESULTS AND DISCUSSION OF AIR INTRUSION**

520 **5.1. Scenario 1: Air intrusion through interim clay cover system.**

521 Scenario 1 is focused on air intrusion occurring through cracks in the daily and interim soil cover
522 layer. Landfill methane emissions depend on several factors, e.g., cover soils, gas collection
523 efficiency, changes in barometric pressure, etc.; rising barometric pressure suppressed the
524 emission, while falling barometric pressure enhances the emission (Bogner et al. 2011; Xu et al.
525 2014; Young 1990, 1992). In Scenario 1, this barometric pumping is overcome by the pressure
526 differential between the landfill and atmosphere from the gas extraction wells, especially on side
527 slopes with nearby gas wells where landfill capping is not as easily compacted (Di Trapani et al.
528 2013). This results in air ingress and a rapid aerobic conversion of the MSW with temperatures
529 rising in a few days. One month of air ingress was selected to reflect the time-elevated
530 concentrations of O₂ and N₂ that are anecdotally observed in gas wells. Simulation results in Fig.
531 S8(a) show the landfill operating under a steady anaerobic condition with average temperature
532 profiles reported in Fig. 2. Air intrusion occurs because of a pressure differential of 5 kPa combined

533 with a single grid block of the clay cover simulated as a high-permeability material to reflect a
534 crack. This leads air flowing into MSW with rate of 0.34 m³/hour (0.2 scfm). In Fig. S8(b), the
535 temperature rapidly rises to 80°C after 1 month of air ingress. The surrounding region impacted
536 by air intrusion and thus aerobic reactions is localized to less than 10m into the waste, with O₂
537 completely consumed at the entrance location. In contrast, the N₂ penetrates deeper into the
538 landfill, which could explain why N₂ is observed in gas wells with limited corresponding O₂. In
539 Fig. S8(c), the temperature decreases to 60°C after 1 month as the system returns to anaerobic
540 conditions. This may be attributed to the small impacted region and heat transfer to the surrounding
541 waste and to the atmosphere. Temperature approach normal conditions in Fig. S8(d) after 1 year.

542 The spatial distribution of gas composition in Fig. 3 is compared after the first week and
543 after 1 month of air intrusion. In particular, N₂ progresses ~50 m into the shallow MSW layer and
544 only 10 m in the intermediate MSW layer after 1 week. The lower permeability of the intermediate
545 layer explains the significantly lower penetration of N₂. After 1 month, N₂ extends farther into the
546 waste mass (approximately 100 m and 50 m into the shallow and intermediate layers, respectively),
547 where it intersects with the GW2 and GW3 extraction wells. Oxygen remains localized during the
548 intrusion because of the high aerobic biodegradation activity of the waste, meaning that O₂
549 consumption relies on the availability of biodegradable substrates, critical O₂ for aerobic
550 biodegradation, and the number of aerobic bacteria. As a result, the simulations indicate that high
551 aerobic activity at the location of intrusion consume all of the O₂ entering into MSW and
552 simultaneously 40% water vapor is produced as the result of high aerobic biodegrading. The CH₄
553 and CO₂ concentrations in the landfill decrease instantly at the onset of air intrusion. After 1 month
554 of air intrusion, CH₄ level drops significantly and CO₂ concentrations increase to ~15%. If CO₂
555 concentration were only controlled by the aerobic reaction, the concentration by volume of the gas

556 phase would be approximately 50%. The fact that the CO₂ concentration only reaches 15%
557 confirms that the CO₂ levels are a product of aerobic biodegradation and air ingress.

558 In Fig. S9(a), the time-history of biogas production is compared before and after air
559 intrusion. The simulations indicate that the maximum biogas remaining in the system is 2,400 m³
560 6 years after the landfill closure. The air intrusion occurs 30 years after the closure and continues
561 for 1 month. During the air intrusion, CO₂ and CH₄ concentrations in the biogas concurrently
562 decrease but not equally. For example, the CO₂ volume in the biogas decreases from 1,800 m³ to
563 1,500 m³ (at temperature and pressures inside the landfill), whereas the CH₄ volume reduces to
564 1200 m³. Fig. S9(a) confirms that the higher CO₂ production is related to aerobic biodegradation.
565 Air injection experiments by Powell et al. (2006) also show the reduction in CH₄ concentration is
566 attributed to a combination of presence of air and inhibition of anaerobic biodegradation. The
567 simulation results in Fig. S9(b) also indicate that more than one year was required after the repair
568 of the air intrusion to re-establish normal anaerobic conditions.

569

570 **5.2. Scenario 2: Air leakage from an air line break.**

571 Scenario 2 involves simulating air ingress from air line breaks. These air lines are installed below
572 the soil cover system in the waste mass, and they are used to provide air pressure to operate the
573 pneumatic pumps removing liquids from gas extraction wells. The air lines can become buried
574 deeper into the landfill as waste lifts are added over time, which is why in Scenario 2 the air line
575 break was placed at the interface between shallow and intermediate MSW layers. The air lines
576 contain atmospheric air pressurized to approximately 500 kPa (73 psi). Although rare, the air line
577 may break because of differential settlement and reduced service life of the HDPE piping. An air
578 line break was simulated by applying a constant mass flow rate of 2.58×10^{-3} kg/s and 7.3×10^{-4}

579 kg/s for N₂ and O₂, respectively. This is approximately equal to 11.9 m³/hour (7 scfm) of air flow
580 rate injecting into the MSW. The leakage occurs in a grid block at the interface of the shallow and
581 intermediate MSW layers, located at the depth of 17 m. As previously stated, the air line leak
582 included in this study was based loosely on an actual air line leak event at an MSW landfill in the
583 southern US. The input parameters (such as line diameter, flow rate, and generalized depth) were
584 obtained from field personnel associated with the landfill operation.

585 Similar to Fig. S8(a), the landfill is operating under anaerobic conditions prior to the air
586 line break in Fig. 4(a). After the onset of the air line break, it is assumed that the air line break is
587 repaired after 1 week. The landfill temperatures rise to 80°C in that timeframe, quicker than was
588 observed in Scenario 1. Based on Fig. 4(b), the area of heat generation is approximately 50 m wide
589 and approximately 5 times greater than the area of influence in Scenario 1. This is attributed to a
590 higher air-injection flowrate from the pressurized air line. After the air line is repaired, Fig. 4(c)
591 implies that the heat accumulation region remains at 80°C after 1 month. The simulation results in
592 Fig. 4(d) indicate that temperatures still remain elevated (~60°C) one year after the air line break.
593 This suggests that heat generated by the reactions stimulated by an air line break can persist for a
594 long time, which can facilitate other chemical reactions, impact methane energy recovery, and
595 performance of geosynthetics (Jafari et al. 2014, 2017). The maximum heat flux produced by the
596 anaerobic reactions in this model is approximately 2 W/m³. In contrast, the maximum heat flux
597 increases to ~500 W/m³ in the aerobic scenario.

598 Due to aerobic heat generation, the degree of water (aqueous phase) saturation also
599 dramatically changes at the air line break. In Fig. 5, the degree of saturation decreases from over
600 30% to 10% at the boundary between the shallow and intermediate layers, which also corresponds
601 to the zone of heat accumulation. The temperature profile shows that the higher temperatures are

602 predominantly in the shallow layer between the depths 10 m to 18 m. This is attributed to the
603 higher permeability of shallow layers facilitating heat conduction and gas transport. Thus, more
604 O₂ is available to the aerobic microorganisms located in the shallow layer, and additional aerobic
605 biodegradation will result in temperature increase and moisture redistribution in a wider region.

606 The spatial distribution of gas composition from Scenario 2 in Fig. S10 compares gas
607 composition after one week of the broken air line and one year after the repair. During the air line
608 break, air reaches the interim soil cover due to the relatively high mass flow rate and permeability
609 of the shallow MSW layer, impacting a region that is 150 m wide. Effective gas capture at the
610 surface of the landfill becomes a vital operation in this scenario to avoid ballooning of gas under
611 an exposed geomembrane at the landfill surface as a result of gas migration to the surface
612 (Townsend et al. 2015b). Oxygen concentration at the air line break is ~12% v/v and decreases to
613 5% v/v at the interim soil cover. At the center of the aerobic reactions, the gas composition is 8%
614 v/v O₂ and 50% v/v N₂, with the remaining gas composed of 42% v/v water vapor. The ratio of N₂
615 to O₂ is correspondingly 6.25, which is significantly higher than 3.76 for air. This implies that
616 increasing N₂ to O₂ ratios signify consumed O₂ from aerobic reactions. The excessive O₂
617 concentration is observed because of the imbalance between the O₂ consumption rate by aerobic
618 bacteria and injection rate from pressurized air line. After the air line is repaired, traces of N₂ are
619 found at the top of the landfill. The CH₄ and CO₂ concentrations are almost fully recovered after
620 1 year of the air line break, and there is no O₂ remaining in the landfill.

621 Depending on the mass balance between air injection rate (and duration) and rapid oxygen
622 consumption rate during aerobic biodegradation at the injection location, oxygen could transfer to
623 the adjacent grid blocks and create a larger area of aerobic impact. Each grid block receives various
624 amounts of oxygen at any time and hence generates various amounts of heat. As an illustrating

625 example, input parameter values were considered for air injection rate = 18 m³/hour (10.4 scfm),
626 horizontal permeability $k_x = 3.75 \times 10^{-11}$ m², specific heat capacity $C_p = 1000$ J/kg·K. Results
627 showed that after 2 days of injection the aerobic zone was 12 m². After 7 days of injection, 250
628 grid blocks experienced aerobic reactions and the area increased to 500 m². To better understand
629 the amount of heat generated inside the aerobic zone, the grid blocks exhibiting aerobic activity
630 and temperature above 75°C were identified and compiled first. To calculate the amount of aerobic
631 heat generated to cause a temperature change, with the assumptions that the fluid pressure remains
632 constant within the one week of injection and solid-fluid phase change temperature together, Eq.
633 (11) was used to calculate aerobic heat of enthalpy:

634

$$635 \quad Q = \left[(1-n)(\rho_s \cdot C_s) + n(\rho_g \cdot C_g + \rho_l \cdot C_l) \right] \Delta T \quad (11)$$

636

637 where Q is expressed as kJ/m³, n is porosity, ρ is density, C is specific heat capacity, ΔT is
638 temperature change during each time step of simulation, and s , g , and l stand for solid, gas, and
639 liquid phase, respectively. To calculate the amount of heat flux generated by each cell, Eq. (12)
640 was used:

641

$$642 \quad q = \frac{Q}{\Delta t} \quad (12)$$

643

644 where q is expressed as W/m³, and Δt is the simulation time step. Presented in Fig. 6, the
645 (1) temperature, (2) heat of enthalpy, and (3) heat flux at grid blocks located at the injection
646 location, along with 10 m and 30 m to the left side of it. At the injection location, the temperature
647 increases by 30°C but at a slower rate (3 to 4 days) because of the cooling effect of injected air

648 temperature (25°C). Temperature increased by 35°C within 1 day at the 10 m and 30 m left of the
649 injection point. The aerobic reaction generated 200-250 kJ/m³ of heat of enthalpy, equivalent to
650 400-500 W/m³ of heat flux inside the individual grid blocks (if considering the third dimension of
651 each grid block to be 1 m into the page).

652 To calculate the average heat flux generated by each individual grid block, the area under
653 dashed line was divided by the time of occurrence. For example, for the 30 m grid block, the area
654 under dashed line was ~ 360 W·day/m³ which divided by 2 days of heat generation (day 4.5 to day
655 6.5), an estimation of 180 W/m³ as the average heat flux was resulted. The same approach was
656 used to calculate the average heat flux of each grid block inside of the aerobic zone, and were
657 summed and averaged within all the grid blocks. Results are shown in Fig. S11 for four (4) air
658 flow rates.

659 Fig. 7 shows the correlation between aerobic zone, average heat flux, specific heat,
660 horizontal permeability, and air flow. In this figure, the aerobic zone was reported after 7 days of
661 air injection. Based on the sensitivity analysis, the heat flux and aerobic zone non-linearly rise with
662 increasing air flow, coming to an asymptote at the higher air flow rates. When C_p increases from
663 1,000 to 3,000 J/kg·K, the area also increases by a factor of 3. The effect of C_p is less pronounced
664 with heat flux, where a higher C_p corresponds to slightly higher heat flux. The sensitivity analysis
665 confirms that a higher C_p corresponds to a waste with more capacity to accumulate heat before the
666 temperatures increases. Results in Fig. 7 indicate that heat generation rates increase linearly to 8.5
667 m³/hour (~5 scfm) before approaching an asymptote at 140 W/m³. The heat generation is also
668 relatively equal over the range of C_p , which signifies that the aerobic reactions are independent of
669 physical properties. The air flow rate of 0.34 m³/hour (0.2 scfm) corresponding to scenario 1 results
670 in an aerobic zone area of less than 20 m² and heat generation rate of ~20 W/m³. The latter is close

671 to the results of Megalla et al. (2016), where the maximum heat generation from aerobic heat
672 generation from surface air intrusion was reported 44.6 W/m^3 and is comparable to values
673 measured in aerobic composting piles (Zambra et al. 2011). In contrast, the air flow rate of 11.9
674 m^3/hour (7 scfm) from scenario 2 corresponds to heat generation of 100 W/m^3 and an aerobic area
675 of 250 m^2 . While the C_P does not influence heat generation, it plays a major role in the formation
676 of the aerobic zone. For example, a C_P of $1,000 \text{ J/kg}\cdot\text{K}$ corresponds to area of 200 m^2 at an air
677 flow of 5 scfm , compared to 140 m^2 and 60 m^2 for heat capacities of $2,000 \text{ J/kg}\cdot\text{K}$ and $3,000$
678 $\text{J/kg}\cdot\text{K}$, respectively. This trend is observed because the heat generated from aerobic reactions is
679 first used to raise the waste temperature, which requires more at higher C_P (e.g., $3,000 \text{ J/kg}\cdot\text{K}$).
680 Therefore, the additional heat available for $1,000 \text{ J/kg}\cdot\text{K}$ can propagate further outward from the
681 air line break and raise the temperature of adjacent waste.

682 Heat generation rate values above 100 W/m^3 may perhaps be beyond of available published
683 data. This output stems from the TOUGH code, where the multiphase and multiphysics processes
684 have been previously verified and validated (Jung et al. 2010; Kling and Korkealaakso 2006;
685 Nastev et al. 2001; Oldenburg et al. 2002; Pruess 2004; Vigneault et al. 2004). The simulations
686 performed and reported herein are within the constraints of TOUGH capabilities. Moreover, it is
687 important to report possible upper bound heat generations as worst-case scenario when excess
688 aeration/air intrusion incidents occur.

689

690 **6. PRACTICAL IMPLICATIONS**

691 The solid waste industry faces many challenges, including a better understanding of the cause of
692 significant changes in temperatures within the waste mass (other than normal anaerobic
693 decomposition heat) and control of greenhouse gas emissions to the atmosphere under ever

694 restrictive regulations. At a minimum, standard operational practice for control of emissions
695 includes the effective extraction of landfills gas, especially during interim stages of operation
696 where a final cover system is not in place. Well field tuning is a common operation and
697 management (O&M) task that optimizes gas extraction while not overpulling on each individual
698 gas well. Historical practice limits overpulling on a gas well to prevent air flow into the waste mass
699 through the interim cover system and cause a landfill fire. As a result, standard gas well design
700 includes use of solid pipe (with no slots) in the upper 6 m to 9 m (20 to 30 ft) of pipe from top of
701 waste (e.g., Fig. 1 red slots in the gas wells) such that application of a vacuum is limited in the
702 upper-most portion of the waste mass, and installation of a bentonite plug at the waste/soil interface
703 to prevent potential air intrusion. When the interim cover is less than optimal, the potential result
704 of localized higher concentration of methane emissions are possible, a concern where emissions
705 are more tightly controlled by regulation.

706 Scenario 1 in this T2LBM modeling study indicated that the pulling of atmospheric oxygen
707 into the waste mass by the gas well could cause heat accumulation due to aerobic reactions near
708 the landfill side slope (Fig. S8). However, this localized volume (that is flux) of oxygen is not
709 sufficient to cause an exothermic reaction beyond the proximity to the well bore. For a larger-
710 scale exothermic event to occur due to aerobic reactions, a larger flux of air (such as an air line
711 break) is required to increase heat generation rates (Fig. 7). This observation is important to the
712 solid waste industry, as it could revise gas well design and allow slotted pipe to be located closer
713 to the top of waste. This correspondingly could facilitate improved methane collection in shallower
714 waste layers (see large vectors pointed toward GW-3 and GW-4 in Fig. 2(b) in the shallow MSW
715 layer) and hence improved productivity for renewable energy plants, as long as the vacuum applied
716 to the well is optimized to limit air intrusion. This theory from modeled results needs to be field

717 verified across multiple landfills to demonstrate reproducibility before a broad application of the
718 results are implemented. Moreover, comprehensive numerical sensitivity analyses should be
719 performed considering interim cover system, leachate and gas pressures, waste decomposition
720 stage and composition, landfilling history, climate conditions, among many factors.

721 Secondary implications of aerobic reactions from the T2LBM model include higher
722 temperatures impacting geosynthetic components in drainage systems (specifically horizontal and
723 vertical gravity drainage pipes) and accelerated decomposition leading to differential settlement.
724 In particular, temperatures from 70 to 80°C can reduce the elastic modulus of the pipe (Bilgin et
725 al. 2007) and accelerate antioxidant completion and thus reduce the time to stress cracking of high-
726 density polyethylene (HDPE) (Hsuan and Koerner, 1998), which can dramatically reduce the
727 service life and efficacy of internal drainage pipes within the waste mass. While this condition was
728 not modeled, the technical opinion that even localized air intrusion could result in damage to the
729 integrity to HDPE piping systems is reasonable and should be considered by the industry in design
730 and operation of gas extraction systems.

731 Monitoring of signs of pre-cursors to an exothermic event, in this case from air intrusion,
732 is important to the industry. In addition to the monitoring of oxygen in gas wells, visual inspections
733 designed to identify unexplained differential settlement should be part of the routine O&M
734 activities at an MSW landfill. Accounting for differential landfill settlement caused by aerobic
735 decomposition could be important for operation of the landfill gas extraction system, i.e., necessary
736 for the piping to be graded such that condensate cannot collect in low spots and block the flow of
737 landfill gas. While limited settlement data is available, field monitoring of aerobic landfill cells
738 suggest that the magnitude of settlement is relatively similar to leachate recirculation but likely at
739 a quicker rate (Mehta et al. 2002; Yazdani et al. 2006; Merz and Stone 1962; Borglin et al. 2004).

740 This implies that regions impacted by subsurface air line breaks could experience rapid differential
741 settlement, which could correspondingly serve as a lagging indicator of an air line break. Routine
742 operation and maintenance inspections could be implemented to check the integrity of air lines
743 and gas header pipes as mitigation measures.

744

745 **7. CONCLUSIONS**

746 The prediction of heat generation and temperature increase, along with changes in gas composition
747 and concentration, as result of air intrusion are provided in this study using T2LBM. The model
748 incorporated aerobic and anaerobic biodegradation processes, heat generation, and fluid transfer.
749 The model geometry, layering, material properties, and gas extraction were developed based on a
750 landfill in the Midwestern U.S. The model was qualitatively calibrated by using trends in field
751 temperature profiles and biogas production rates from LandGEM. Air intrusion through the cover
752 system and air leakage from air line system were simulated to investigate the impact of air intrusion
753 into MSW landfill. The effect of air intrusion on biodegradation processes, along with subsequent
754 change in heat generation and gas composition in the landfill were presented. The following
755 conclusions are inferred from the numerical simulation results in this study:

756 Aerobic biodegradation releases a heat flux of 10 to 140 W/m³ depending on the rate of air
757 flow, which rapidly causes the waste temperature in the vicinity of the reactions to increase up to
758 80°C. Similar heat generation fluxes are attainable when low air flow rates intrude into the waste
759 mass, as compared with compost piles. Field investigations are needed to document the air line
760 flow rates to corroborate this study. The rapid rate of O₂ consumption by aerobic microbes near
761 the point of entry hinders O₂ transport (penetration) farther into the waste mass, which
762 correspondingly limits the impacted area to less than 10 m near the cracked interim soil cover.

763 Moreover, heat conduction from MSW towards the atmosphere causes the temperature to decrease
764 to less than 60°C a few months after the air intrusion is ceased. For scenario 2 air line break, the
765 zone of heat accumulation remains elevated above baseline for normal biochemical waste
766 degradation for 12 months after the air line is repaired, negatively impacts the settlement and
767 methane generation rates. A high flux infusion of O₂ in an air line break can facilitate exothermic
768 reactions and therefore should be a key focus from the solid waste industry in their efforts to
769 prevent heat accumulations. However, the simulations were performed assuming MSW as a
770 homogeneous material in each layer. This is not the case and hence the simulation results likely
771 represent a conservative estimate on the zone of heat accumulation.

772 The oxygen concentration varies spatially after entering into the landfill. Oxygen consumption
773 is controlled by aerobic bacteria concentration, critical O₂ concentration, O₂ intrusion rate,
774 temperature, moisture content, and Monod kinetic parameters. The ratio of N₂ to O₂ increases from
775 3.76 for atmospheric air to higher values depending on the rate of air intrusion. The ratio of CH₄
776 to CO₂ starts at unity for anaerobic decomposition, but air intrusion causes a decrease due to a
777 combination of the presence of air replacing CH₄ and CO₂ and inhibition of anaerobic
778 biodegradation. At the same time, aerobic biodegradation produces CO₂ as a byproduct. Thus, a
779 signal of aerobic decomposition for landfill operators is not only the decrease in the ratio of CH₄
780 to CO₂ but also relative increase in CO₂ flow rate.

781 The lower vertical permeability compared to horizontal, causes the air to flow further laterally
782 and therefore the heat accumulation zone forms an elliptical area that can be quantified in Fig. 7.
783 The elliptical aerobic area is influenced by the air flow rate and specific heat capacity, higher heat
784 capacity corresponding to smaller heat accumulation zones. Results from this study helps
785 practitioners to estimate the magnitude and area of impact of the aerobic transition. However, the

786 simulated heat accumulation zones are likely a conservative prediction because the MSW was
 787 considered as a homogeneous material.

788

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Nomenclature			
<i>Letters</i>			
A	Area	w	Gravimetric moisture content
B	Bacteria (Biomass)	x	Horizontal
BA	Aerobic bacteria	Y	Yield coefficient
BN	Anaerobic bacteria	z	Vertical
C_p	Specific heat capacity		
f	Coefficient of temperature dependent growth	<i>Greek symbols</i>	
g	Gravity	μ	Growth rate
K	Hydraulic conductivity	δ	Death rate
K_T	Thermal conductivity	ρ	Density
k	Intrinsic permeability	σ	Stress
k_r	Relative permeability	β	Fluid
n	Porosity	η	Dynamic viscosity
P	Pressure		
q	Flow rate	<i>Subscript</i>	
r_e	Effective radius of grid block	T	Temperature
r_w	Well radius	w	Water

<i>S</i>	Substrate	<i>v</i>	Vertical
<i>T</i>	Temperature	<i>wb</i>	Wellbore
<i>t</i>	Time		

795

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1035 **Table 1.** Summary of material properties for MSW and clay layers

Material Properties	Unit	Shallow MSW	Intermediate MSW	Deep MSW	Clay
Bulk Density, ρ	kg/m ³	750	920	1110	1200
Porosity, n	-	0.6	0.5	0.4	0.7

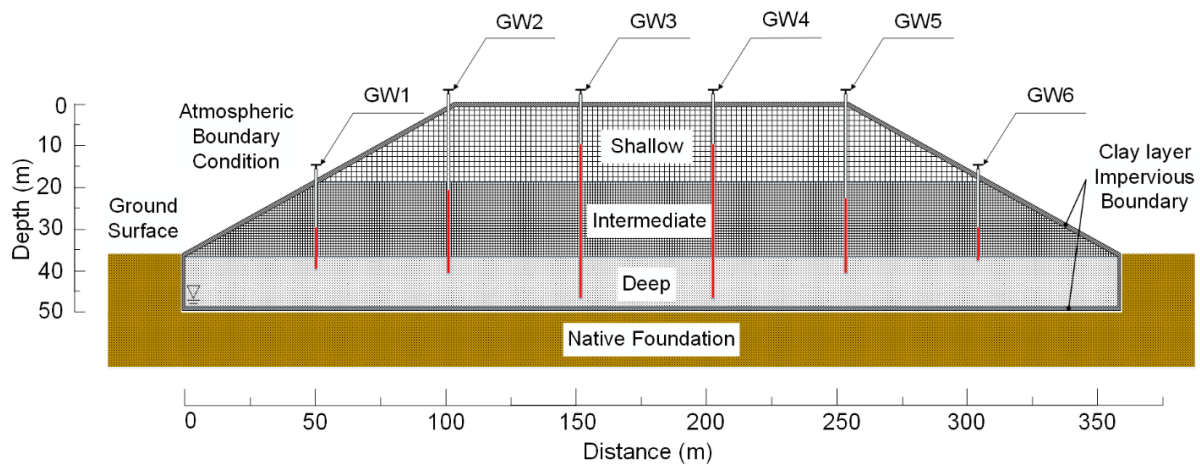
Permeability, k_x¹	m^2	3.8×10^{-11}	3.8×10^{-12}	3.8×10^{-13}	1×10^{-15}
Permeability, k_z²	m^2	3.8×10^{-12}	3.8×10^{-13}	3.8×10^{-14}	1×10^{-16}
Thermal conductivity, K_T	$W/(m \cdot K)$	0.3	0.6	0.9	2.1
Heat capacity, C_p	$J/(kg \cdot K)$	1080-3000	1080-3000	1080-3000	935.8
Grid counts	-	1528	2653	1914	370

¹ Horizontal intrinsic permeability

² Vertical intrinsic permeability

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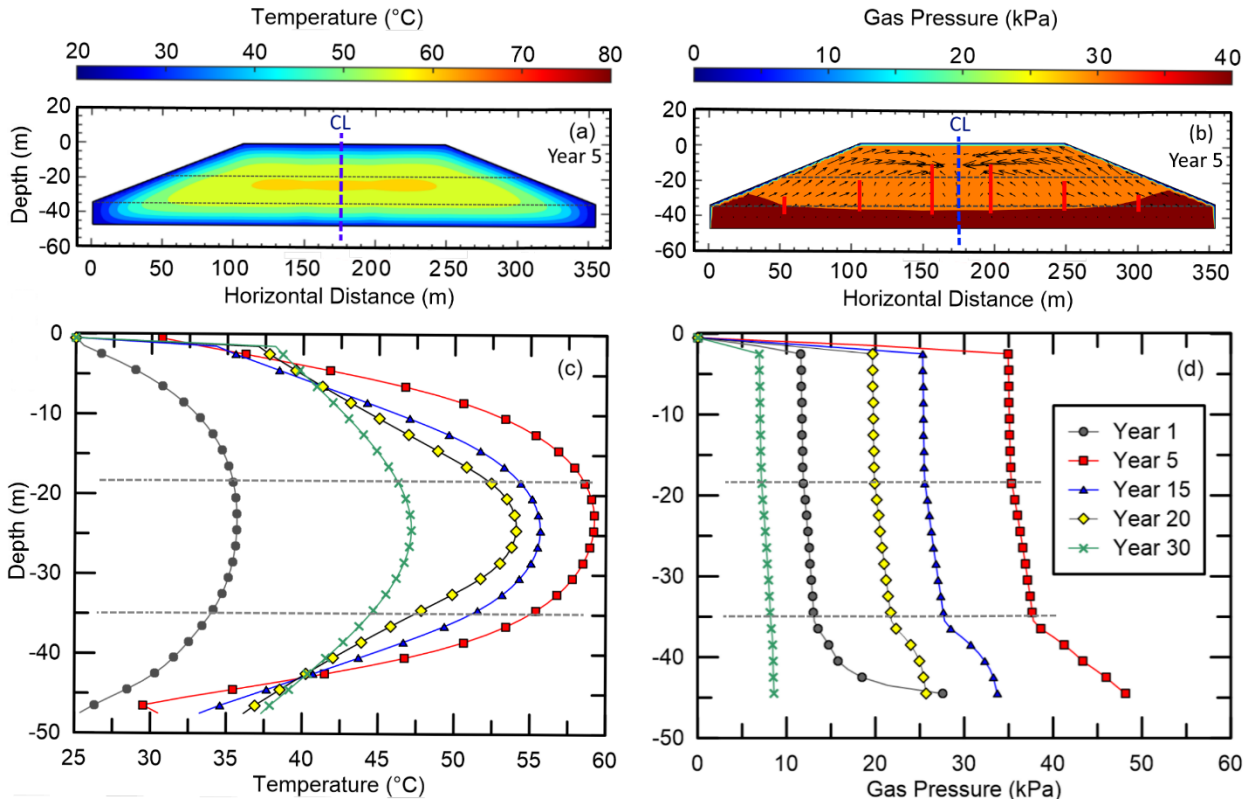
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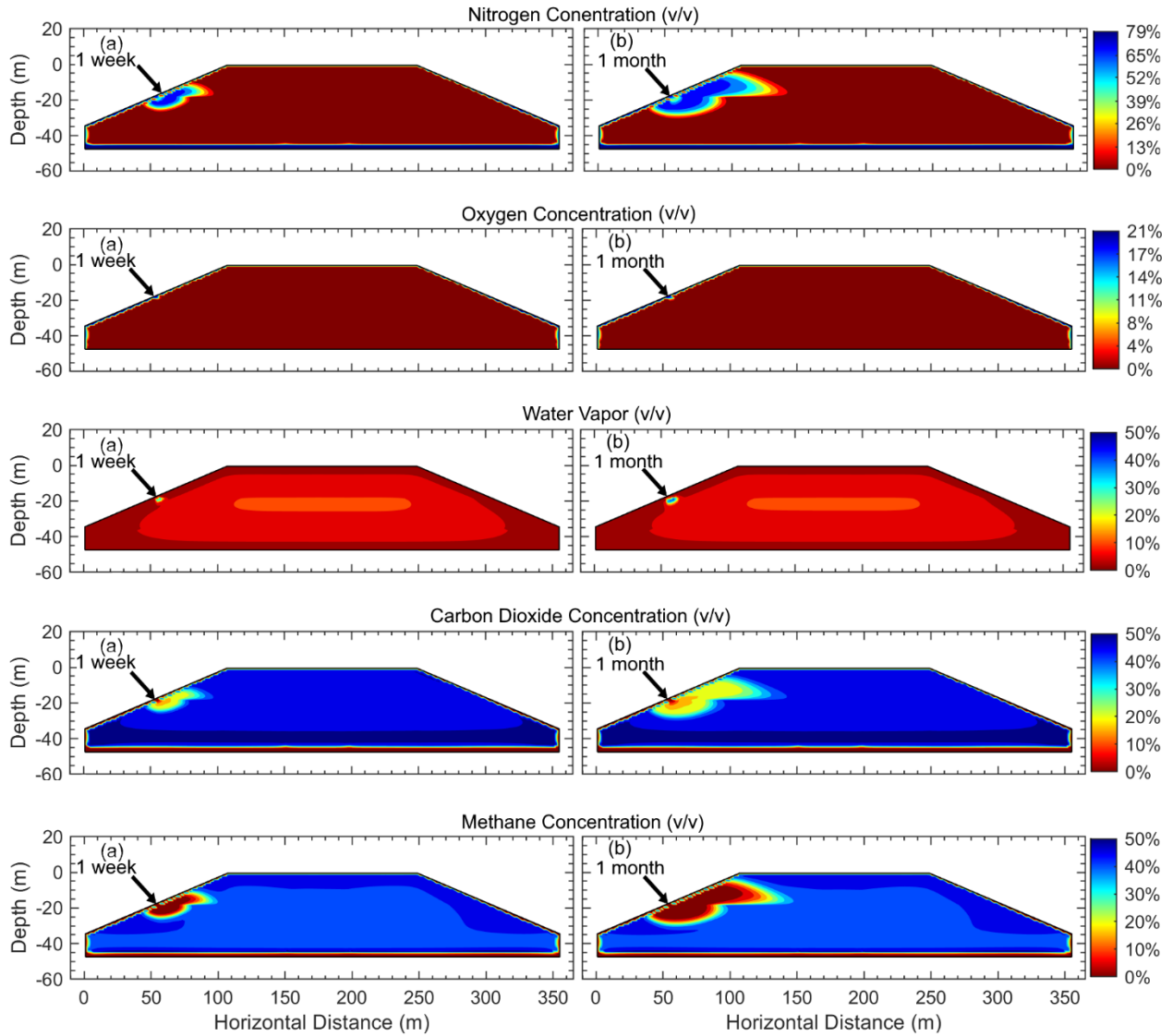
Fig. 1. Cross-section of the idealized landfill system consisting of three MSW layers and six gas extraction wells (red color indicates gas well slot length). Figure is not to scale.

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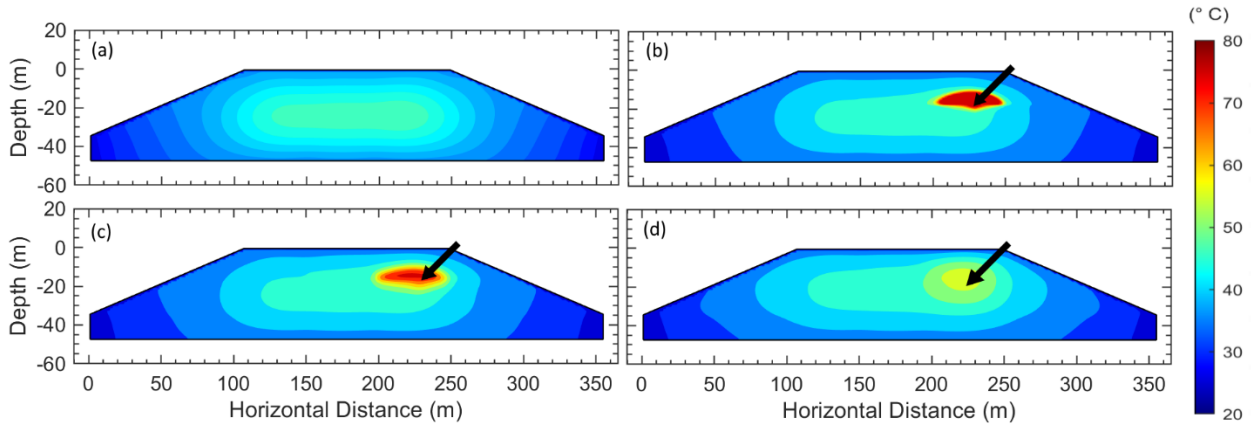
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Fig. 2. Temporal changes at the center of the landfill: (a and c) Temperature, and (b and d) Gas pressure. The intersections of MSW layers are showed with dashed lines and the gas collection wells are signified by vertical red lines.



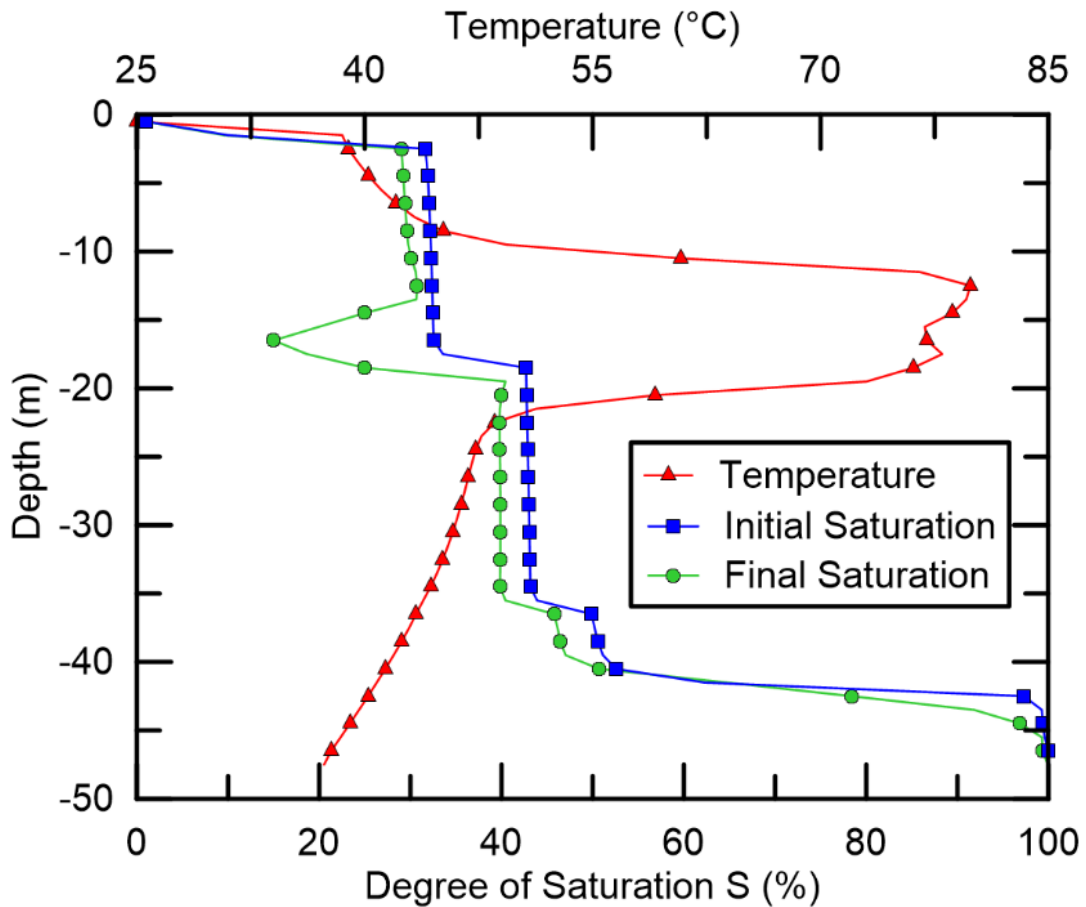
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Fig. 3. Spatial distribution of gas composition after 1 week and 1 month of air intrusion. The air intrusion location is indicated by the arrow.

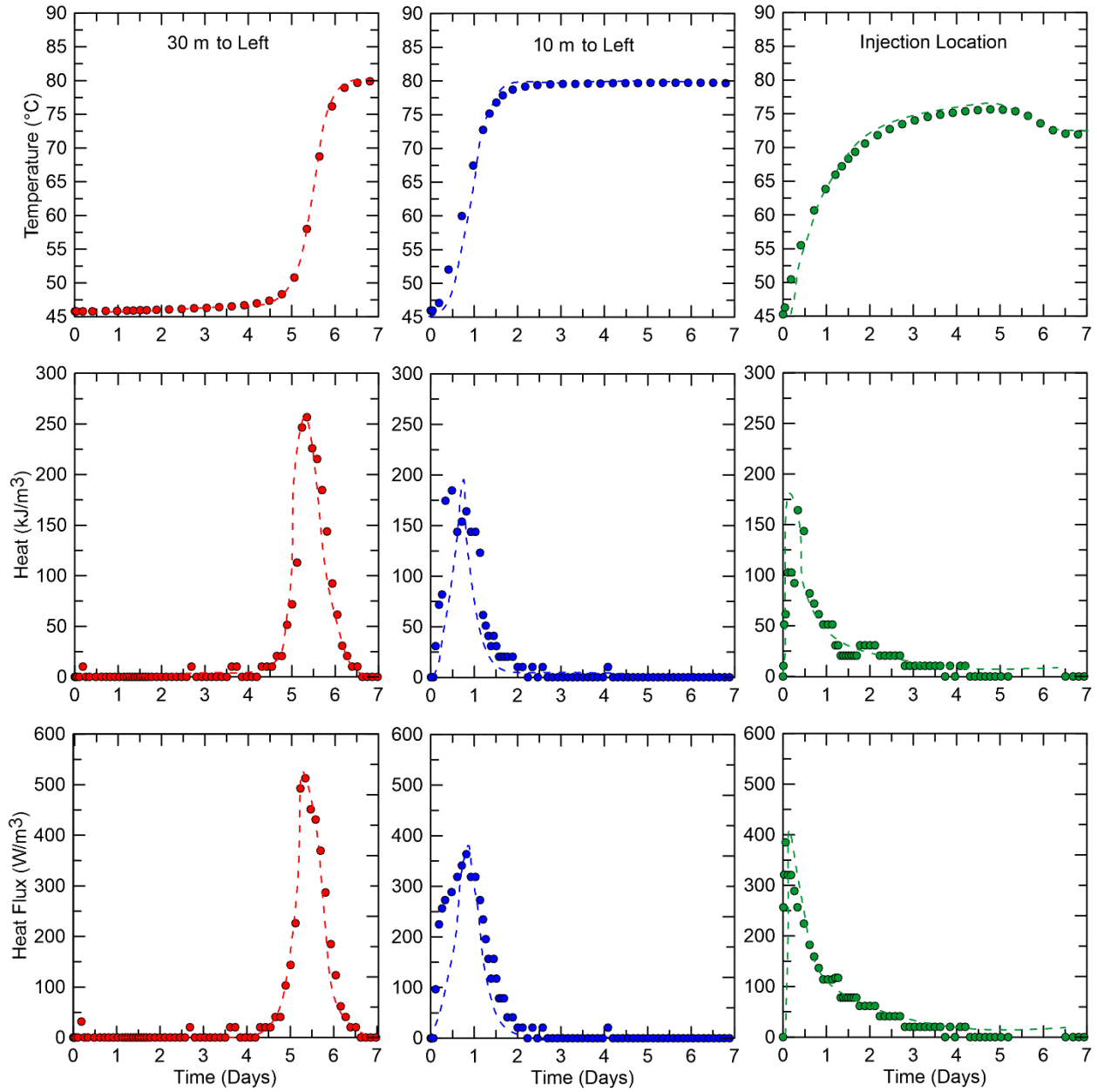


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 1053 **Fig. 4.** Temperature development during Scenario 2: (a) Initial anaerobic conditions, (b) after 1
 1054 week of air intrusion, (c) 1 month after repairing the leak, and (d) 1 year after the air line break.
 1055 The air line break is indicated by the arrow.

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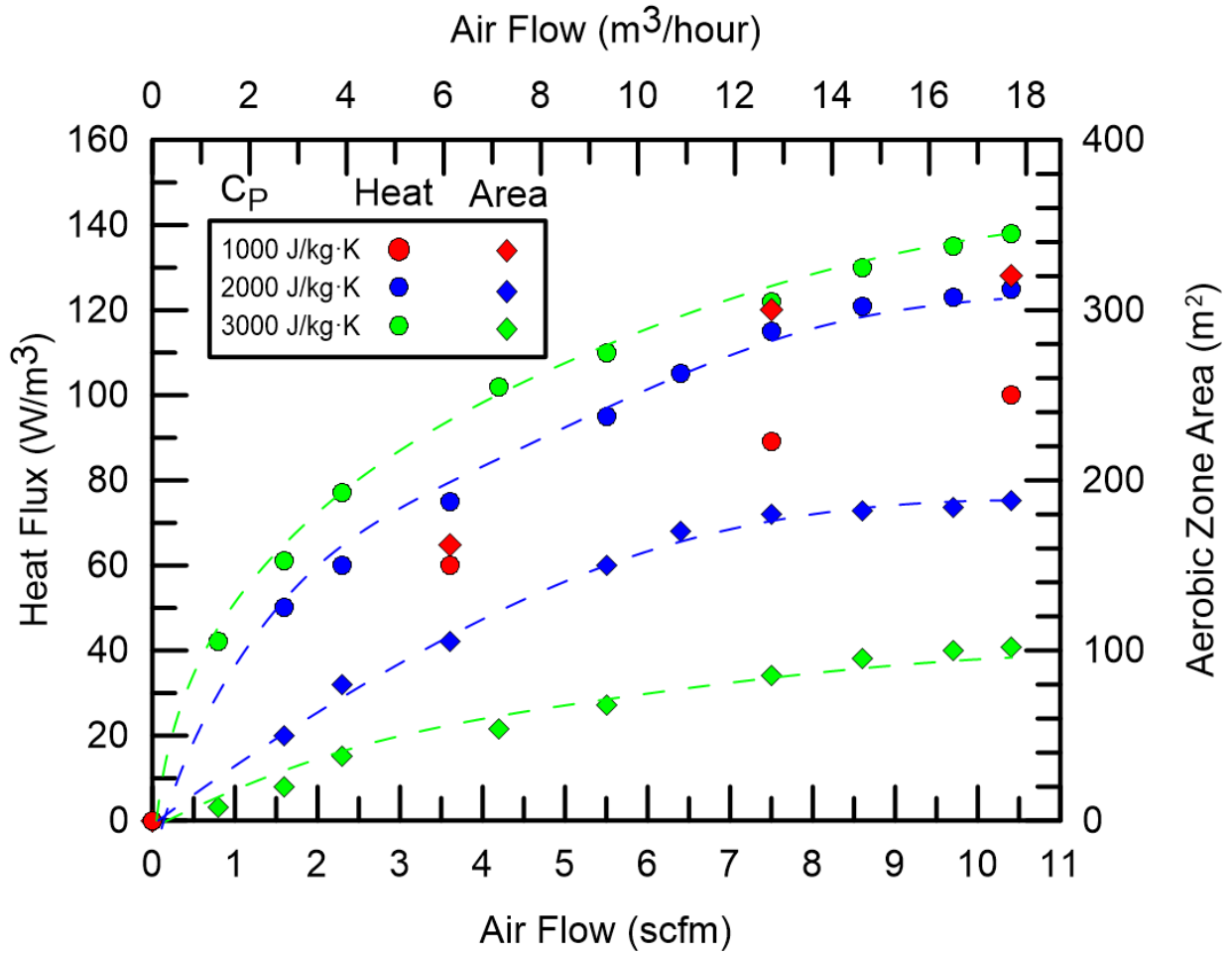


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 1058 **Fig. 5.** Temperature and degree of saturation profiles after one week of air leak along the depth at
 1059 the location of air line break.
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Fig. 6. Horizontal variation of temperature, heat of enthalpy, and heat flux during 1 week of air line break.



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Fig. 7. Sensitivity of heat generation and aerobic zone area as a function of heat capacity and air flow after one week of air injection into MSW.

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SUPPLEMENTARY MATERIAL
NUMERICAL INVESTIGATION OF AIR INTRUSION AND AEROBIC REACTIONS
IN MUNICIPAL SOLID WASTE LANDFILLS

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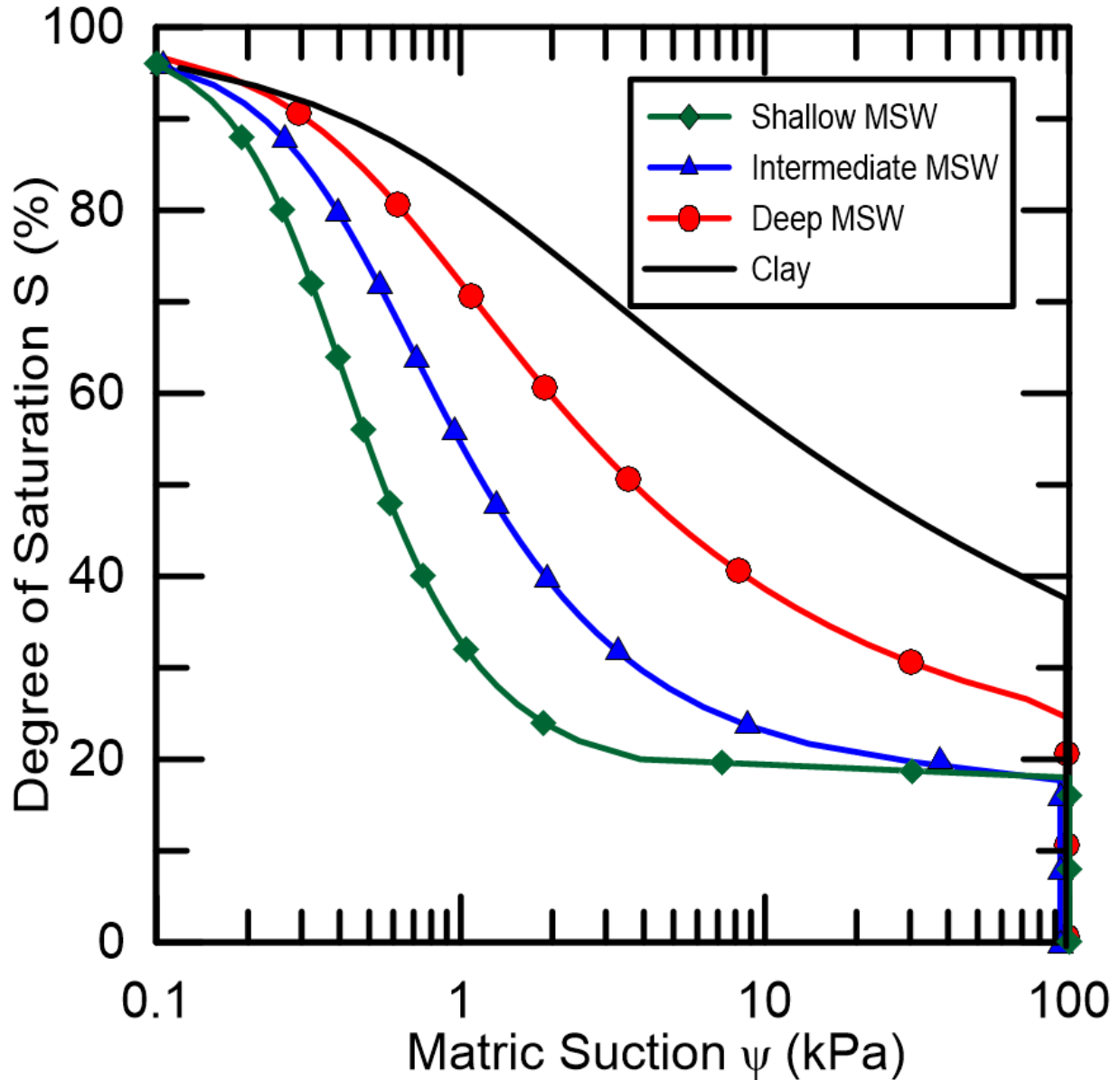
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<https://doi.org/10.1016/j.wasman.2022.05.009>

October 3, 2022

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Fig. S1 shows the degree of saturation (S) as a function of matric suction (ψ) for each material layer, and Table S1 lists the TOUGH2 input parameters for van Genuchten (1980) function.



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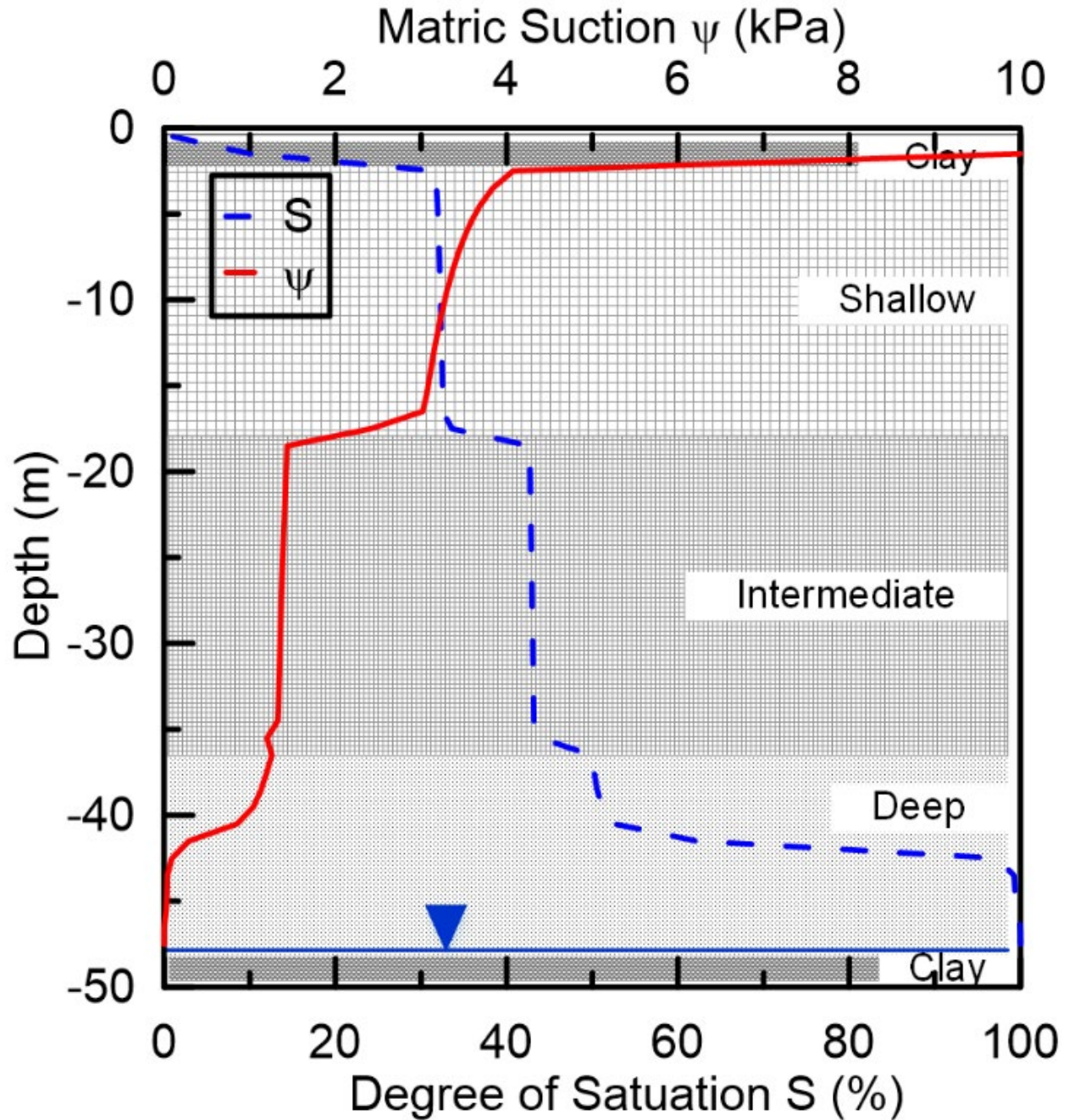
Fig. S8. SWRC for the three MSW and clay layers in the model landfill system.

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First, gravity capillary equilibrium is simulated in a 1-D column spanning the height of the landfill from bottom liner to surface cover, with 48 grid blocks composed of one MSW layer and a water table that is assigned at a depth of 47 m. The water-table single grid block in this step is assigned a volume of $1 \times 10^{50} \text{ m}^3$, high permeability, and zero capillary pressure to ensure this grid block permanently remains saturated and avoids any changes in the hydrostatic leachate level. The other 47 grid blocks are assigned a volume of 2 m^3 and regular capillary pressure based on the values in Table S1 and results shown in Fig. S1. The simulation time for this step

1128 must be extremely large, more than 100 years, such that the capillary fringe level reaches to the
1129 top layers of the landfill and a steady state is achieved. The next step consists of changing the
1130 large-volume of the water-table grid block back to 2 m³ and assigning no-flux boundary
1131 conditions (second-type boundary condition) of the clay cover layer by manually changing the
1132 properties and saturation level of the top-layer and bottom-layer grid blocks to match those from
1133 the gravity capillary steady-state and again running the simulation for 100 years. Finally, the
1134 atmospheric boundary condition was assigned to the top grid block by prescribing constant
1135 pressure and temperature to 101 kPa and 25 °C, respectively as the first-type boundary condition.

1136 The next step accounts for the landfill side slopes and the slight change in atmospheric
1137 gas density, which is achieved by replicating the 1-D column across the 2-D rectangular model.
1138 The grid blocks not associated with the landfill (i.e., above the sloping cover system) are
1139 subsequently deleted. The last step is to assign the specified MSW properties in Table 1 and
1140 supplementary Table 2 to relevant grid blocks and then rerunning the system to gravity-capillary
1141 equilibrium. The result of this series of steps is the static gravity-capillary equilibrium shown in
1142 Fig. S2, where the blue dashed line is showing the degree of saturation along the depth. The
1143 degree of saturation is nearly zero at the top cover and 31% in the shallow layer, 45% in the
1144 intermediate layer, 50% to 99% in the deep layer, and 100% at the top of the bottom clay layer
1145 where the water table (leachate level) is located. The red line in Fig. S2 indicates the
1146 corresponding capillary pressure with depth based on the SWRC shown in Fig. S1.
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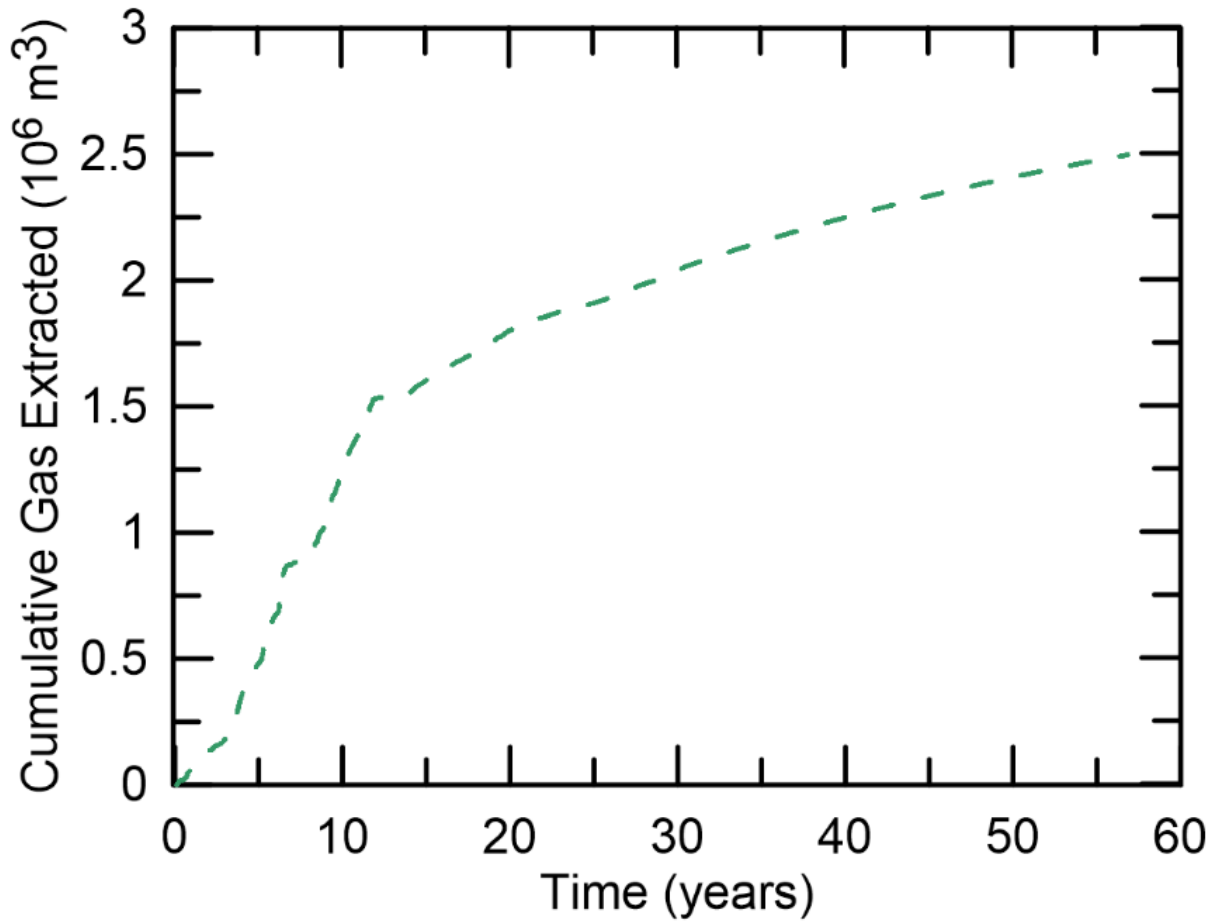
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Fig. S9. Simulated static gravity-capillary equilibrium showing the unsaturated zone matric suction and degree of saturation that are used as the initial condition for subsequent biodegradation and air-intrusion processes.

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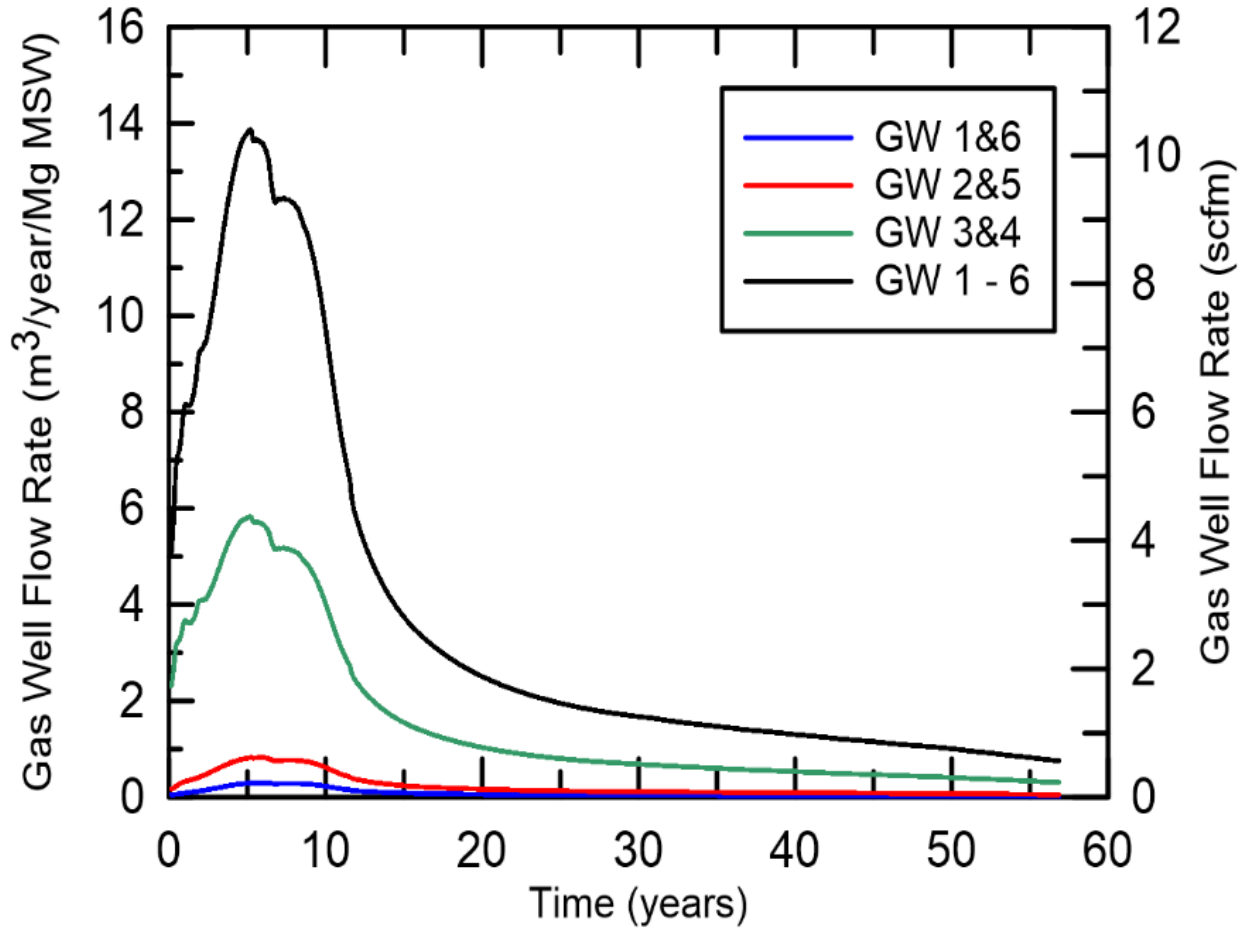
In the T2LBM model system, the gas pressure builds up quickly (20 to 30 kPa) between years 5 to 20, which correspond to the period with highest gas generation rate as shown in supplementary Fig. S3. Steady-state gas pressures are reached after 30 years, where the pressure is slightly higher than atmospheric pressure. The pressure distribution in supplementary Fig. S4 shows a constant profile with depth, which may be attributed to the gas extraction wells redistributing gas from high to low pressure. There are limited gas pressure measurements in landfills to validate the simulated gas pressures shown in supplementary Fig. S4. Anecdotal

1159 evidence of landfill gas operations suggests that biogas can accumulate under the interim cover
1160 system, leading to bulges in geomembrane liners.
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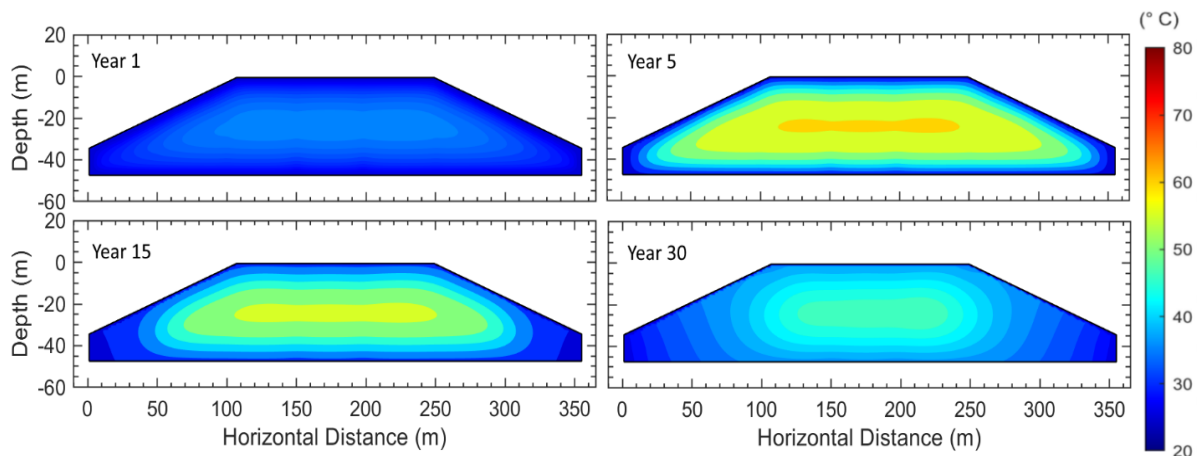
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1163 *Fig. S10. Cumulative gas extracted due to anaerobic MSW biodegradation.*

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1166 *Figure S11. Gas well collection performance during the anaerobic biodegradation period.*

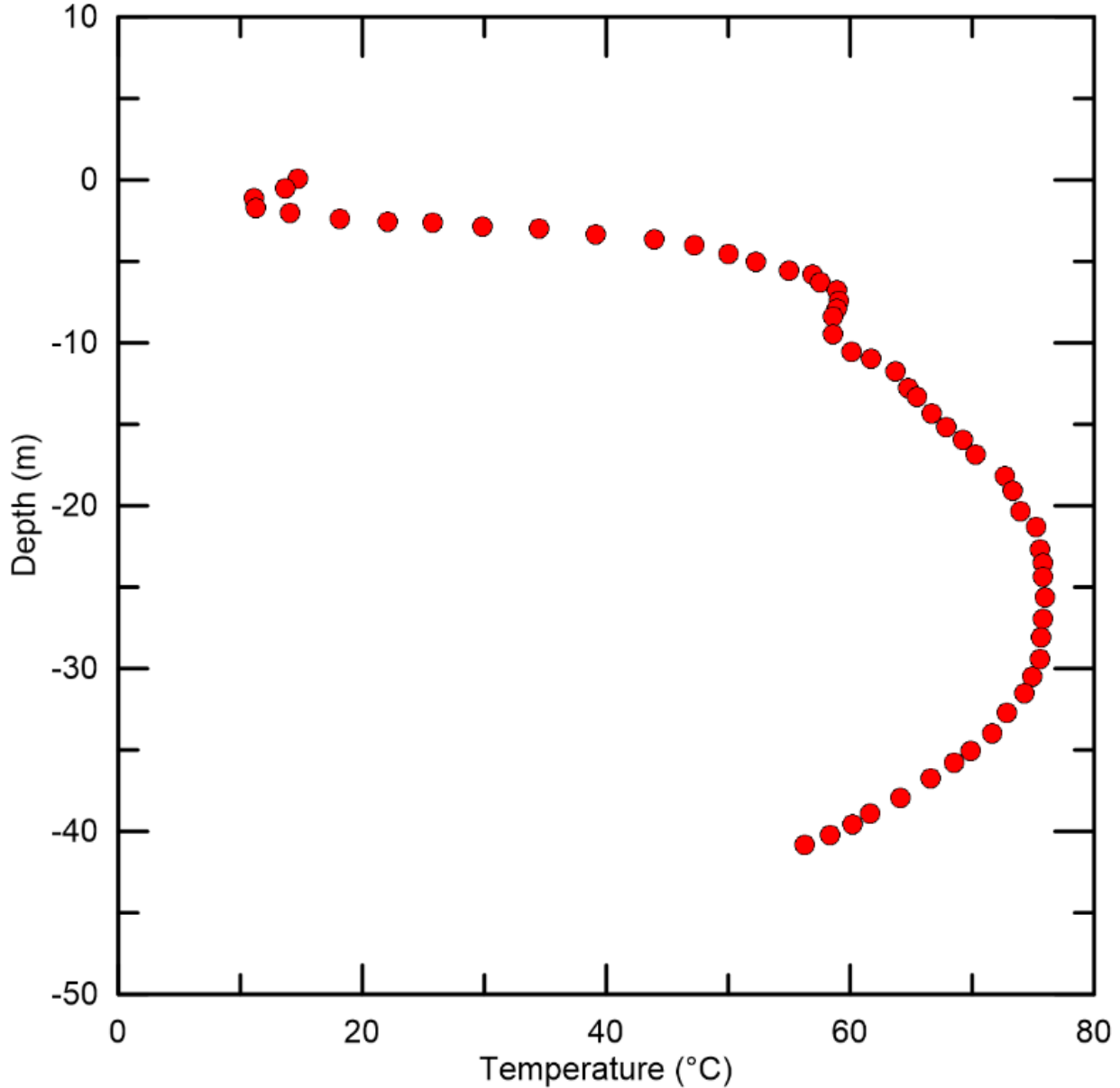
1167
1168 Fig. S5 shows the temperature contours inside the landfill at years 1, 5, 15, and 30, which
1169 are parabolic with the maximum temperature in the middle depth.
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1173 *Fig. S12. Temperature evolution during anaerobic biodegradation.*

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1175 The simulated anaerobic temperature profile was calibrated based on the real landfill temperature
1176 profile. In Fig. S6, MSW temperatures in the month of February approached 76°C (170 °F) in the
1177 middle of the landfill. The impetus for using this temperature data was to replicate the
1178 temperature profile with depth. The objective was not to match the actual temperatures.



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1180

Fig. S13. Real Landfill Temperature Profile

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1182 Fig. S7 shows the gas pressure contours inside the landfill at years 1, 5, 15, and 30, and
1183 the arrows show the direction of landfill biogas flowing towards the gas collection wells. Large
1184 arrows at the shallow layer represent the higher gas flow rates compared to the small arrows in
1185 the deep layer.

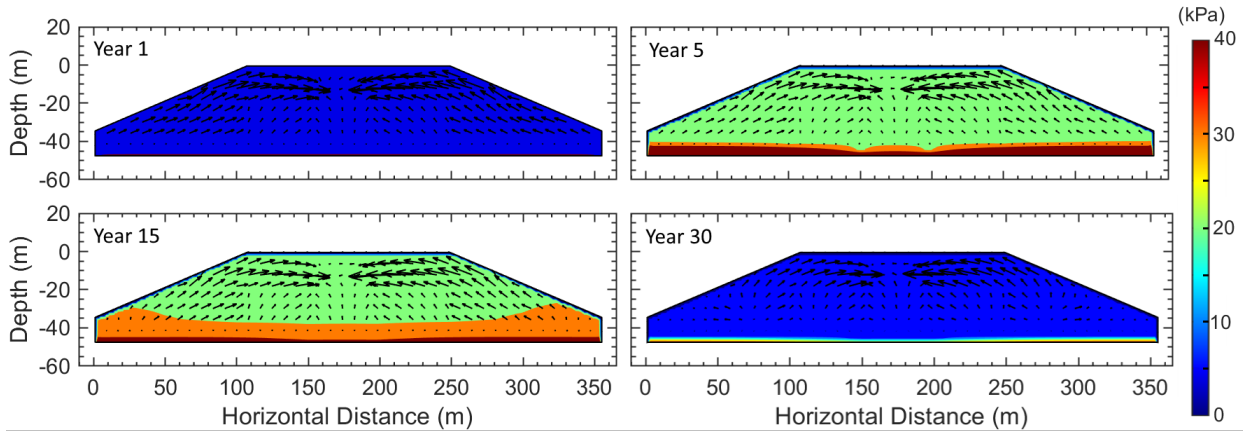


Fig. S14. Pressure evolution during anaerobic biodegradation

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1189 Simulation results in Fig. S8(a) show the landfill operating under a steady anaerobic condition
 1190 with average temperature profiles reported in Fig. 2. Air intrusion occurs because of a pressure
 1191 differential of 5 kPa combined with a single grid block of the clay cover simulated as a high-
 1192 permeability material to reflect a crack. This leads air flowing into MSW with rate of 0.34
 1193 m³/hour (0.2 scfm).
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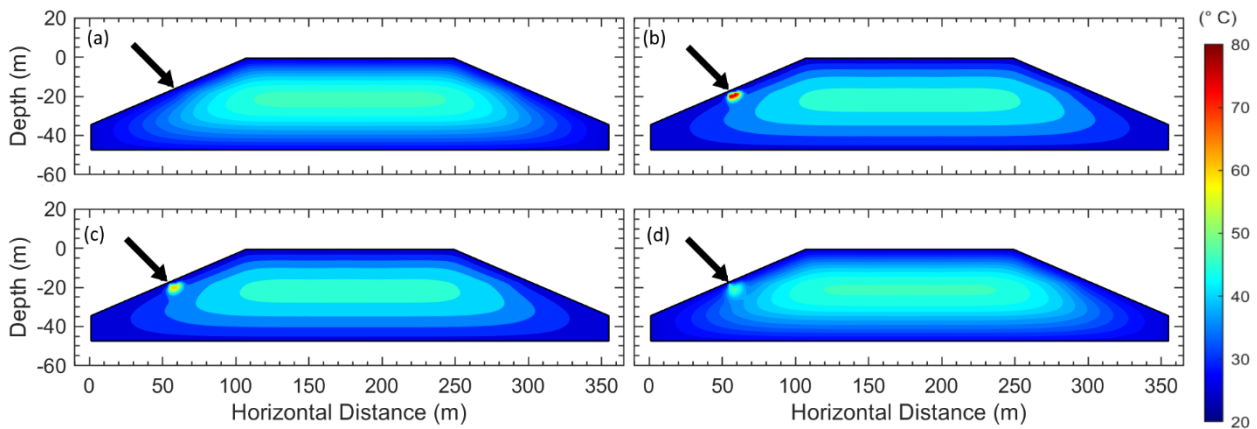


Fig. S8. Temperature development during an air intrusion from crack in surface clay cover: (a) Initial normal landfill temperature, (b) after one month of air intrusion, (c) one month after repairing the opening, and (d) one year after the repair of the opening. The air intrusion location is shown by the arrow.

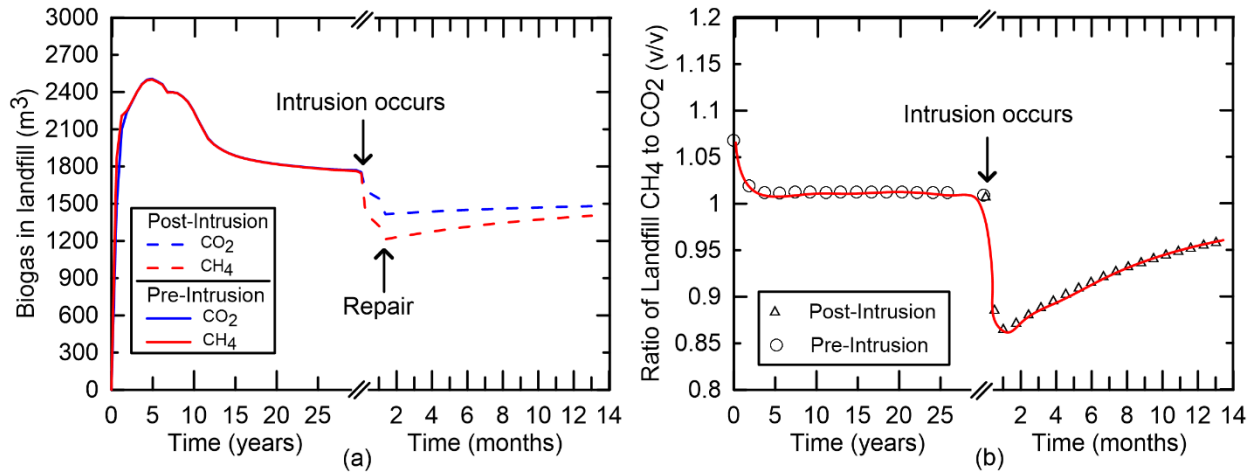
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1201 In Fig. S9(a), the time-history of biogas production is compared before and after air intrusion.

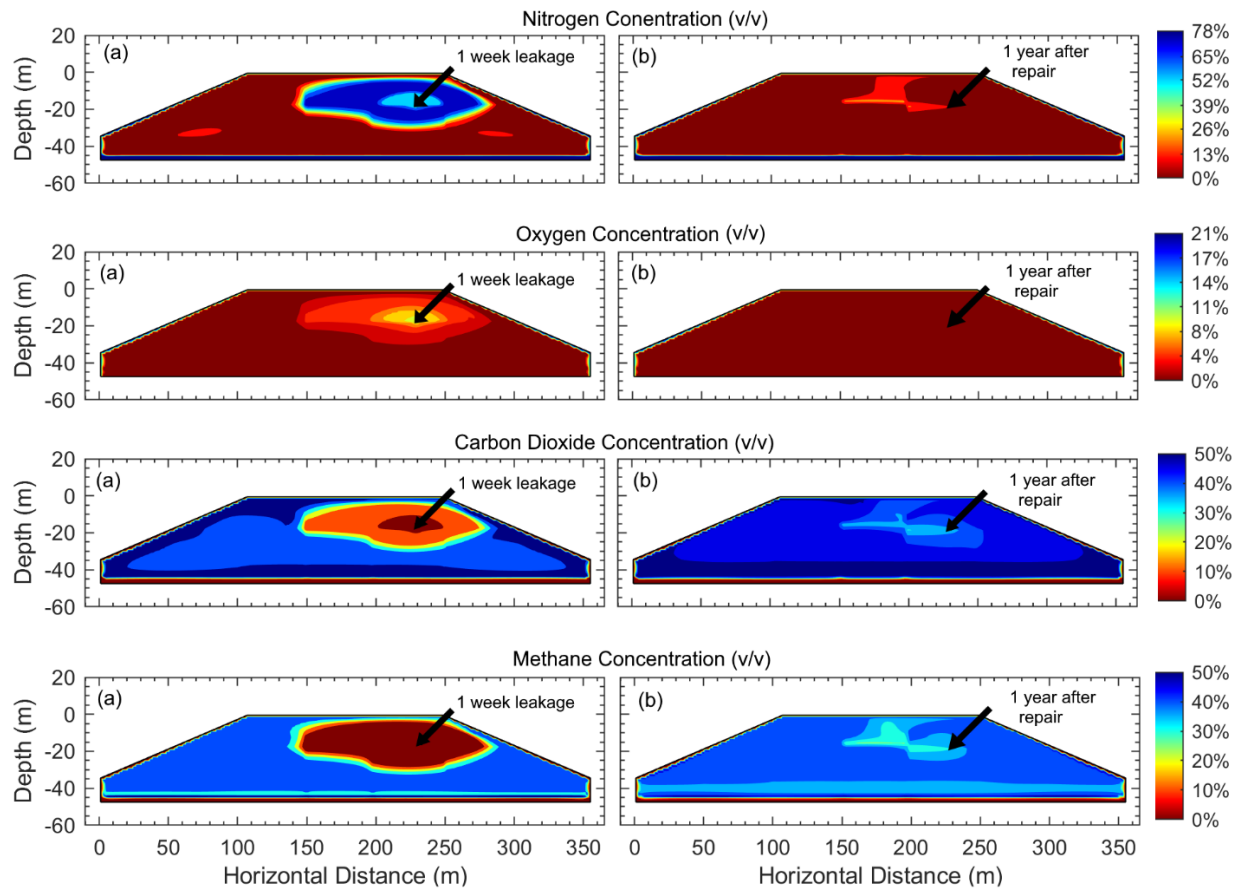
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Fig. S9. Pre- and post-intrusion landfill biogas composition.

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Fig. S10. Spatial distribution of landfill gas composition during 1 week of air line break and 1 year after the repair. The arrow points to the location of the air line break.

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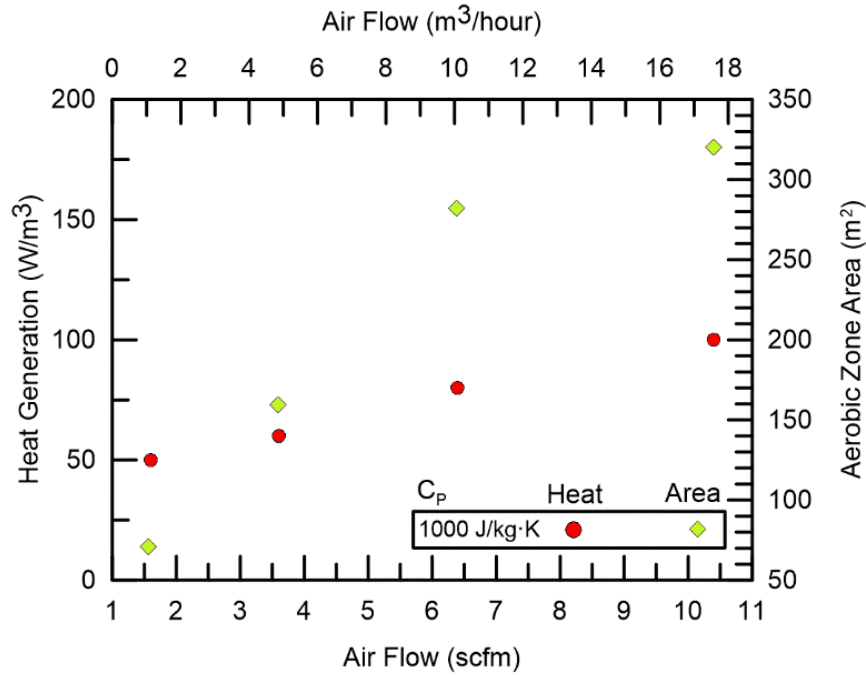
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To calculate the average heat flux generated by each individual grid block, the area under dashed line (in Fig. 6) was divided by the time of occurrence. For example, for the 30 m grid block, the area under dashed line was $\sim 360 \text{ W}\cdot\text{day}/\text{m}^3$ and then divided by 2 days of heat

1213 generation (day 4.5 to day 6.5), we estimated $\sim 180 \text{ W/m}^3$ as the average heat flux. The same
 1214 approached was used to calculate the average heat flux of each grid block inside of the aerobic
 1215 zone. Then, we summed and averaged within all the grid blocks. Results are shown int the figure
 1216 below for four (4) air flow rates.



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 1218 **Fig. S11.** Comparison of heat generation and impacted area of aerobic biodegradation in MSWs
 1219 with specific heat capacity of $1000 \text{ J}/(\text{kg}\cdot\text{K})$ and $2000 \text{ J}/(\text{kg}\cdot\text{K})$.

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 1221 *Table S2. Summary of van Genuchten parameters for clay and MSW layers.*

van Genuchten Parameter	Shallow MSW		Intermediate MSW		Deep MSW		Clay layer	
	R.P. ¹	C.P. ²	R.P.	C.P.	R.P.	C.P.	R.P.	C.P.

$\lambda^{(3)}$	0.61	0.6	0.41	0.45	0.31	0.3	0.21	0.2
S_{lr}	0.31	0.35	0.41	0.3	0.34	0.3	0.11	0.1
S_{ls}	1	1	1	1	1	1	1	1
S_{gr}	5×10^{-3}	---	5×10^{-3}	---	5×10^{-3}	---	0.02	---
$1/P_0^4$	---	3×10^{-3}	---	3×10^{-3}	---	3×10^{-3}	---	8×10^{-4}
P_{max} (kPa) ⁵	---	100	---	100	---	100	---	100

¹ Relative Permeability functions parameters.

² Capillary Pressure functions parameters.

³ Parameter λ is m in van Genuchten's (1980) notation in TOUGH2, where $m = 1 - 1/n$ (m and n are the empirical shape-defining and dimensionless parameters in the van Genuchten equation).

⁴ Equal to $\alpha/(\rho_w \times g)$

⁵ P_{max} is implemented as an upper boundary based on available field observations that suggest landfill matrix suction values are low (Breitmeyer 2011).

1222

1223 The parameters used in Eq. 8. and fitted values are listed in Table S2.

1224 *Table S3. Summary of gas extraction well input properties.*

Well ID	PI (m ³) in MSW layer			Slot length (m) in MSW layer			P_{wb} (kPa)
	Deep	Intermediate	Shallow	Deep	Intermediate	Shallow	
GW1	3.86×10^{-12}	9.05×10^{-11}	---	3	7	---	95
GW2	6.46×10^{-12}	2.32×10^{-10}	1.29×10^{-11}	5	18	1	95
GW3	1.16×10^{-11}	2.32×10^{-10}	1.16×10^{-09}	9	18	9	95
GW4	1.16×10^{-11}	2.32×10^{-10}	1.16×10^{-09}	9	18	9	95
GW5	6.46×10^{-12}	1.81×10^{-10}	1.29×10^{-12}	5	18	1	95
GW6	1.03×10^{-10}	---	---	8	---	---	95

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1228 The kinetic parameters used for aerobic and anaerobic biological reactions are listed in Table S3.

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1230 *Table S4. Biological parameters used in T2LBM model*

Parameter	Unit	Anaerobic	Aerobic
Yield coefficient, Y	kg/kg of MBSP	0.2	0.2
Maximum growth rate, μ_{max}	Day ⁻¹	0.16	20
Inhibiting temperature	°C	65	80
Saturation constant of microbes	kg/kg of aqueous phase	8×10^{-3}	8×10^{-3}
Microbial death (decay) rate, δ	Day ⁻¹	0.06	0.6
Initial microbes fraction	kg/kg of aqueous phase	1×10^{-4}	1×10^{-4}
Enthalpy of bioreaction	MJ/kg of MBSP	1.0	15
Critical oxygen concentration	kg/kg of aqueous phase	---	1.8×10^{-7}

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