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A STUDY OF THE DECAY $\tau^- \rightarrow \pi^- \nu_\tau$ [☆]

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We present a high statistics measurement of the branching ratio for the decay $\tau^- \rightarrow \pi^- \nu_\tau$ using data obtained with the Mark II detector at the SLAC e^+e^- storage ring SPEAR. We have used events from the center-of-mass energy region 3.52 to 6.7 GeV to determine that $B(\tau^- \rightarrow \pi^- \nu_\tau) = 0.117 \pm 0.004 \pm 0.018$. From electron-muon events in the same data sample, we have determined that $B(\tau^- \rightarrow \pi^- \nu_\tau)/B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau) = 0.66 \pm 0.03 \pm 0.11$. We present measurements of the mass and spin of the τ and the mass of the τ neutrino based, for the first time, on a hadronic decay mode of the τ .

All of the properties of the τ lepton that have been measured to date are consistent with the interpretation of the τ as a sequential lepton. If this hypothesis is correct, the decay $\tau^- \rightarrow \pi^- \nu_\tau$ ^{‡1} proceeds via the

standard hadronic weak axial vector current and $B(\tau^- \rightarrow \pi^- \nu_\tau)/B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)$ can be explicitly calculated from known parameters [1]. A measurement of this ratio is an unambiguous test of the τ 's coupling to the hadronic weak axial vector current.

We present here a measurement of the branching ratio $B(\tau^- \rightarrow \pi^- \nu_\tau)$ based on data taken with the Mark II detector at the e^+e^- storage ring SPEAR. The integrated luminosity of 21 000 nb⁻¹ at center-of-mass energies from 3.52 to 6.7 GeV corresponds to 58 600 produced $\tau^+\tau^-$ pairs. We also present measurements of the spin and mass of the τ and the mass of the τ neutrino based on the $\tau^- \rightarrow \pi^- \nu_\tau$ decay mode.

All aspects of the Mark II detector pertinent to this measurement have been fully discussed elsewhere [2]. We summarize here the characteristics relevant to this analysis. Charged particles are detected over 85% of the solid angle by the 16 layers of the central, cylindrical drift chambers. The momentum resolution for tracks constrained to the interaction vertex is $\delta p/p = [(0.0145)^2 + (0.005p)^2]^{1/2}$ (p in GeV/ c) where the

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^{‡1} Throughout this paper, all particle reactions also imply the charge conjugate reaction. For example, $\tau^- \rightarrow \pi^- \nu_\tau$ stands for itself and for $\tau^+ \rightarrow \pi^+ \bar{\nu}_\tau$.

first term is from multiple-scattering and the second term reflects the 200 micron spatial resolution. Outside the drift chambers are 48 time-of-flight (TOF) scintillation counters having a 300 ps timing resolution. Next comes the solenoidal magnet coil providing a uniform field of 4.1 kG. Outside the coil are eight lead-liquid argon shower counters covering 65% of the solid angle. The energy resolution is $12\%/[E(\text{GeV})]^{1/2}$, and the photon detection efficiency ranges from greater than 95% above 500 MeV down to 20% at 100 MeV. Outside the shower counters is the muon system consisting of layers of iron separated by layers of proportional tubes. One end of the detector is instrumented with a lead-proportional chamber endcap shower counter.

Charged pions were identified as particles which (1) were not muons according to the muon system, (2) were not electrons according to the lead-liquid argon shower counters, (3) were not kaons according to the TOF system (relevant for momenta less than 1.3 GeV/c), and (4) were not protons according to the TOF system (relevant for momenta less than 2.1 GeV/c). The requirement that the particle be distinguishable from a muon rejects all particles with momenta below approximately 700 MeV/c, the range threshold for muon identification. The efficiency for identifying pions was measured with known pions from ψ and K_s^0 decays. The probability of misidentifying an electron as a pion was measured with known electrons from radiative Bhabha events and gamma conversions. For momenta above 700 MeV/c, the pion efficiency ranges from 82% to 90%, and the electron misidentification probability is less than 4%.

Events were selected if they had a charged pion and exactly one other, oppositely charged particle (X). The requirement of exactly two charged particles takes advantage of the low multiplicities typical of τ events and dramatically reduces contamination from hadronic events. To reduce background from events involving neutrals, particularly the decay $\tau^- \rightarrow \rho^- \nu_\tau \rightarrow \pi^- \pi^0 \nu_\tau$, we rejected any event having a photon with energy above 100 MeV. Photons less than 36 cm from a charged particle, measured at the liquid argon module, were ignored because of potential pattern recognition problems. To minimize beam-gas contamination, we required that the event vertex be within 10 cm, along the beam direction, of the beam crossing point. To reduce backgrounds from mis-identified Bhabha and μ -pair events, we accepted only

events with acoplanarity angle greater than 20° . The acoplanarity angle is $180^\circ - \Delta\phi$ where $\Delta\phi$ is the difference in azimuthal angles of the two charged particles.

There were 2150 $\pi^\pm X^\mp$ events satisfying the above criteria. Events in which both particles were identified as π 's were counted twice. The estimated backgrounds are given in table 1. The feed-down from events with more than two produced charged particles was measured with events satisfying the same criteria as the $\pi^\pm X^\mp$ events except that the two particles had the same charge. Assuming the probability of missing a particle was independent of the charge of the particle ^{#2}, the feed-down to $\pi^\pm X^\mp$ events was twice ^{#3} the number of $\pi^\pm X^\pm$ events. The beam-gas background was calculated from the number of $\pi^\pm X^\mp$ events with a vertex between 15 and 25 cm, along the beam direction, from the interaction point. The other backgrounds were calculated from a Monte Carlo simulation program. The errors in these backgrounds are a combination of uncertainties in the models and uncertainties in the simulation of the detector by the Monte Carlo program. The net number of $\pi^\pm X^\mp$ events was $1138 \pm 46 \pm 174$ ^{#4} events.

^{#2} This is not true of two-photon production where the scattered e^+e^- are usually not detected. These events were accounted for separately.

^{#3} For four-charged particles with a total charge of zero, there are four ways of pairing them so that they have opposite charges and two ways such that they have the same charge.

^{#4} The first error of all quantities is statistical, and the second is systematic.

Table 1

Estimated backgrounds to πX events. Except for multiprong events, all backgrounds refer to events with exactly two produced charged particles.

Source	Number
multiprong events	80 ± 9
beam-gas	14 ± 4
other τ decays (primarily $\tau^- \rightarrow \rho^- \nu_\tau$ and $\tau^- \rightarrow \pi^- \pi^0 \pi^0 \nu_\tau$)	590 ± 170
charm production	49 ± 24
non-charm hadronic production	97 ± 19
$e^+e^- \rightarrow e^+e^-\gamma$	63 ± 13
$e^+e^- \rightarrow \mu^+\mu^-\gamma$	5 ± 1
2-photon production	114 ± 15
total	1012 ± 174

The number of πX events after background subtraction ($N_{\pi X}$) is related to the branching ratio (B_{π}) for $\tau^- \rightarrow \pi^- \nu_{\tau}$ by

$$N_{\pi X} = 2B_{\pi} \sum_i \sigma_{\tau\tau}^i L^i \sum_j B_j \epsilon_{\pi j}^i, \quad (1)$$

where the first sum (index i) is over center-of-mass energies and the second sum (index j) is over decay modes of the τ . The quantity $\sigma_{\tau\tau}^i$ is the radiatively corrected τ -pair production cross section, L^i is the integrated luminosity, B_j is the branching ratio to decay mode j , and $\epsilon_{\pi j}^i$ is the efficiency for detecting a πX event when one τ decays to $\pi \nu_{\tau}$ and the other τ decays via decay mode j . The branching ratios assumed are shown in table 2. Since the sum over decay modes includes the decay $\tau^- \rightarrow \pi^- \nu_{\tau}$, eq. (1) is a quadratic equation in B_{π} , which was easily solved once the $\epsilon_{\pi j}^i$'s were determined by a Monte Carlo program. It was necessary to correct the efficiencies for loss of events due to the creation of spurious "photons" by the pattern recognition program from a combination of real deposited energy and electronic noise. This correction was measured in events with the same topology as the πX events (two charged particles and no real photons), namely μ -pairs ($e^+e^- \rightarrow \mu^+\mu^-$), Bhabha events ($e^+e^- \rightarrow e^+e^-$), and cosmic rays. After a 3% correction of the Bhabha events for real, radiative photons, all three types of events agreed within 1%, giving an average correction of 6%. The average efficiencies were $\epsilon_{\pi\pi} = 0.154$ and $\sum_{j \neq \pi} B_j \epsilon_{\pi j} = 0.0654$ yielding $\epsilon^{\pm 4}$

$$B(\tau^- \rightarrow \pi^- \nu_{\tau}) = 0.117 \pm 0.004 \pm 0.018. \quad (2)$$

The systematic errors are 15% for the background subtraction, 6% for the luminosity measurement, 5% for initial state radiative corrections, 5% for electron-

pion separation, 5% for muon-pion separation, 1% for the spurious photon correction, and 5% for uncertainties in the branching ratios in $\sum_{j \neq \pi} B_j \epsilon_{\pi j}^i$. When these errors are propagated through eq. (1), the net systematic error on $B(\tau^- \rightarrow \pi^- \nu_{\tau})$ is 15%.

To reduce some of the systematic errors, such as the luminosity, in the ratio $B(\tau^- \rightarrow \pi^- \nu_{\tau})/B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_{\tau})$, we have measured the τ leptonic branching ratio from the same data sample used for the $\tau^- \rightarrow \pi^- \nu_{\tau}$ analysis. We selected events having an electron identified by the liquid argon system, an oppositely charged muon identified by the muon system, and no other particles. There were 294 $e^+\mu^{\mp}$ events of which 5 ± 3 were estimated to come from charm production, 30 ± 7 from other τ decays, and 2 ± 1 from multiprong hadronic production. This gives a net signal of $257 \pm 17 \pm 8 e^{\pm} \mu^{\mp}$ events. The average efficiency for detecting $e\mu$ events was 0.071, giving

$$B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_{\tau}) B(\tau^+ \rightarrow \mu^+ \nu_{\mu} \bar{\nu}_{\tau}) = 0.030 \pm 0.002 \pm 0.004. \quad (3)$$

The systematic error comes from the following added in quadrature: 6% for the luminosity, 5% for radiative corrections to the τ -pair production cross section, 3% for the efficiency calculation, 5% for electron identification, 5% for muon identification, 3% for the background subtraction, and 1% for the spurious photon correction. Assuming that $B(\tau^- \rightarrow \mu^- \bar{\nu}_{\mu} \nu_{\tau})/B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_{\tau})$ is equal to the theoretical [1] value of 0.973, we have

$$B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_{\tau}) = 0.176 \pm 0.006 \pm 0.010. \quad (4)$$

$$B(\tau^- \rightarrow \mu^- \bar{\nu}_{\mu} \nu_{\tau}) = 0.171 \pm 0.006 \pm 0.010.$$

This is in excellent agreement with the world average [3] of $B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_{\tau}) = 0.170 \pm 0.011$ and $B(\tau^- \rightarrow \mu^- \bar{\nu}_{\mu} \nu_{\tau}) = 0.179 \pm 0.015$.

Combining eqs. (2) and (4) gives

$$B(\tau^- \rightarrow \pi^- \nu_{\tau})/B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_{\tau}) = 0.66 \pm 0.03 \pm 0.11.$$

This is in good agreement with the theoretical [1] prediction of 0.58 and with previous measurements [4] by Mark I (0.53 ± 0.23), PLUTO (0.51 ± 0.17), and DELCO (0.46 ± 0.18).

In order to demonstrate that these πX events are consistent with τ production and subsequent decay, we have performed several additional measurements

Table 2
Branching ratios used for efficiency calculations.

Decay mode	Branching ratio
$\tau^- \rightarrow e^- \bar{\nu}_e \nu_{\tau}$	0.176
$\mu^- \bar{\nu}_{\mu} \nu_{\tau}$	0.171
$\rho^- \nu_{\tau}$	0.216
$\pi^- \pi^0 \pi^0 \nu_{\tau}$	0.05
$\pi^- \pi^0 \pi^0 \pi^0 \nu_{\tau}$	0.02
$K^- \nu_{\tau}$	0.007
$K^{* -} \nu_{\tau}$	0.015

on the data. A subset of these events having an identified lepton opposite the π were studied. The lepton could either be an electron identified by the liquid argon system or a muon identified by the muon system. The lepton energy spectra for the $e\pi$ and $\mu\pi$ events, fig. 1, are in good agreement with the hard spectra expected from τ decays. Semi-leptonic decays of charmed particles give considerably softer decays.

There were 372 (231) $e\pi$ ($\mu\pi$) events of which 168 ± 29 (77 ± 15) were calculated to be background (primarily from other τ decays, as with the πX events). The average efficiency for detecting $e\pi$ ($\mu\pi$) events from τ decays was 0.0955 (0.0542) which gives

$$B_e B_\pi = 0.018 \pm 0.002 \pm 0.004, \quad (5)$$

$$B_\mu B_\pi = 0.024 \pm 0.002 \pm 0.006. \quad (6)$$

Dividing (5) by (6) gives $B_\mu/B_e = 1.33 \pm 0.18 \pm 0.36$ in agreement with the theoretical expectation [1] of 0.973. Setting B_μ/B_e equal to 0.973 and using eq. (4) gives

$$B_\pi = 0.119 \pm 0.009 \pm 0.020, \quad (7)$$

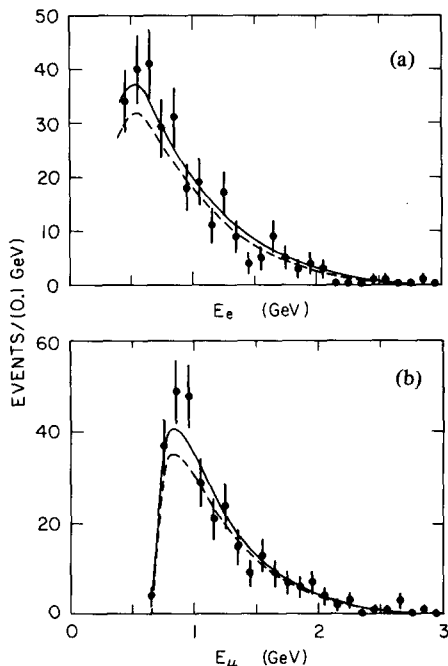


Fig. 1. (a) Electron energy spectrum for $e\pi$ events. Dashed curve is the Monte Carlo expectation for signal events. Solid curve is the Monte Carlo expectation for signal plus background. (b) Muon energy spectrum for $\mu\pi$ events.

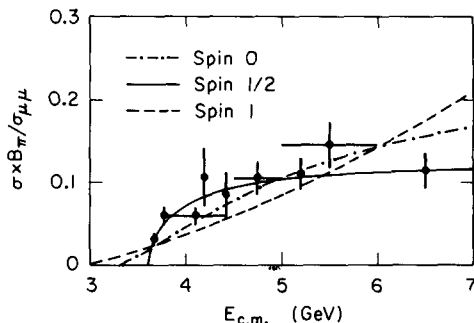


Fig. 2. τ -pair production cross section measured from the $\tau^- \rightarrow \pi^- \nu_\tau$ decay mode. The curves are fits for different spin assignments for the τ . The errors include an estimated 15% point-to-point systematic uncertainty from background subtractions.

$$B_\pi/B_e = 0.68 \pm 0.07 \pm 0.10. \quad (8)$$

There is good agreement with the results obtained from the πX events.

In fig. 2 we plot the product of $B(\tau^- \rightarrow \pi^- \nu_\tau)$ and the τ production cross section (calculated from eq. (1), assuming $B_\pi = 0.117$ in the sum over j) as a function of the center-of-mass energy. We have fit the production cross section to the hypothesis that the τ is a point-like particle [5] ^{±5} with spin 0, 1/2, or 1. The free parameters in the fit were m_τ , $B(\tau^- \rightarrow \pi^- \nu_\tau)$, and, for the spin 1 case, two additional parameters described in refs. [5-7]. Since the branching fraction is a parameter in the fit, it serves as the normalization, and hence the fit constitutes a test of the shape of the production cross section. The spin 0 and spin 1 hypotheses are eliminated at the 95% confidence level ($\chi^2/\text{DOF} = 27/8$ and $48/6$). On the other hand, the data are well fit by the spin 1/2 hypothesis ($\chi^2/\text{DOF} = 8/8$). The fit to the spin 1/2 hypothesis yields $m_\tau = 1.803 \pm 0.016 \text{ GeV}/c^2$, in agreement with measurements [8] by DELCO ($1.782^{+0.002}$), DESY-Heidelberg ($1.787^{+0.010}_{-0.007}$), and DSP (1.807 ± 0.020).

The pion energy spectrum, after bin-by-bin background subtractions and efficiency corrections, is shown in fig. 3 for different center-of-mass energies. Since $\tau^- \rightarrow \pi^- \nu_\tau$ is a two-body decay, the expected pion energy spectrum is flat for monoenergetic τ 's produced at a fixed center-of-mass energy. All spectra

^{±5} Tsai originally used data from DELCO on $\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau$ to eliminate the spin 0 and spin 1 hypotheses for the τ [6]. The DELCO analysis of the same data is in ref. [7].

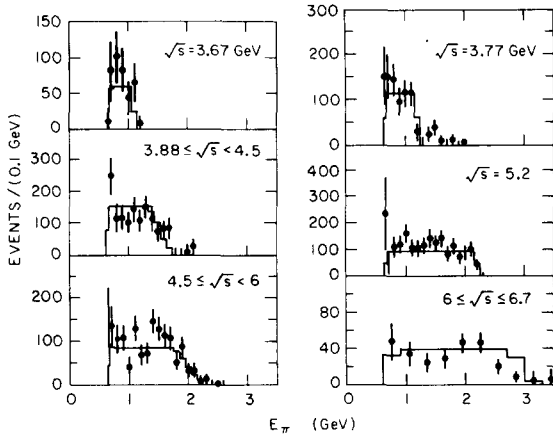


Fig. 3. Pion energy spectrum for π -X events with bin-by-bin background subtraction and efficiency corrections. The curves are the expected spectra for $m_\tau = 1.782 \text{ GeV}/c^2$, $m_\nu = 0$, and $B_\pi = 0.117$.

are flat and do not peak at high energies as expected for Bhabha and μ -pair events or at low energies as is typical of hadronic and two-photon events.

The end point of the pion energy spectrum is determined by the pion, τ , and τ neutrino masses. We have fit the pion spectrum to obtain an upper limit for m_{ν_τ} . Since this fit is sensitive to systematic variations in efficiencies and background subtraction for data from different center-of-mass energies, we used only data from the largest block of fixed energy running (5.2 GeV) in the fit. In fig. 4, we plot the upper limit on m_{ν_τ} as a function of the assumed τ mass. For $m_\tau = 1.782 \text{ GeV}/c^2$, the result is $m_{\nu_\tau}^2 = 0.010 \pm 0.025 \text{ GeV}^2/c^4$, which gives a two-standard deviation upper

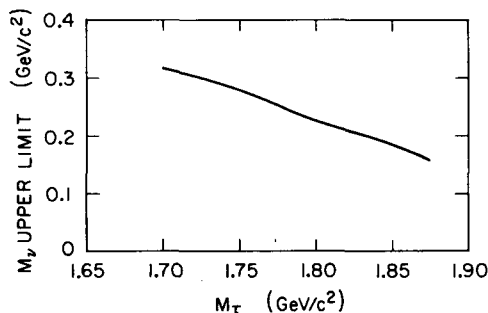


Fig. 4. Upper limit (95% confidence level) on the mass of the τ neutrino as a function of the mass of the τ .

limit on the τ neutrino mass of $0.25 \text{ GeV}/c^2$. The DELCO group has obtained a similar limit [9] from the electron spectrum from $\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau$.

In summary, we have measured $B(\tau^- \rightarrow \pi^- \nu_\tau)$ to be $0.117 \pm 0.004 \pm 0.018$. From the same data, we have measured $B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)B(\tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau)$ to be $0.030 \pm 0.002 \pm 0.004$. Assuming the ratio of the electronic and muonic decay rates of the τ to be the theoretically expected value, these results were combined to give $B(\tau^- \rightarrow \pi^- \nu_\tau)/B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau) = 0.66 \pm 0.03 \pm 0.11$. This is in good agreement with previous experiments [4] and with the theoretical prediction [1] of 0.58. The τ production cross section favors a spin 1/2 assignment for the τ and disfavors spin 0 and spin 1. From the τ production cross section, we measure m_τ to be $1.803 \pm 0.016 \text{ GeV}/c^2$, in agreement with previous experiments [8]. From the energy spectrum of the pion in these decays, we have placed a two-standard deviation upper limit of $250 \text{ MeV}/c^2$ on the mass of the τ neutrino. These measurements support the sequential lepton model of the τ and indicate that the hadronic weak axial vector current couples to the τ with the expected relative strength.

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