Title

Research and Development for HI Intensity Mapping

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Research and Development for HI Intensity Mapping

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Abstract: Development of the hardware, data analysis, and simulation techniques for large compact radio arrays dedicated to mapping the 21 cm line of neutral hydrogen gas has proven to be more difficult than imagined twenty years ago when such telescopes were first proposed. Despite tremendous technical and methodological advances, there are several outstanding questions on how to optimally calibrate and analyze such data. On the positive side, it has become clear that the outstanding issues are purely technical in nature and can be solved with sufficient development activity. Such activity will enable science across redshifts, from early galaxy evolution in the pre-reionization era to dark energy evolution at low redshift.

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1 Key Science Goals & Objectives

Three-dimensional surveys with the redshifted $21\,\mathrm{cm}$ line are key to achieving many of the goals outlined by Astro2020 Science White Papers. In the near future, this technique, called 21 *cm intensity mapping*, will likely surpass optical surveys in terms of volume of the cosmos surveyed. The science goals include: exploration of the cosmic Dark Ages, Cosmic Dawn and the Epoch of Reionization [1–9]; understanding inflation [9–12]; understanding dark energy and modified gravity [13]; and determining neutrino mass [14]. In addition, owing to their large fields of view and high survey speeds, many $21\,\mathrm{cm}$ intensity mapping instruments can simultaneously monitor the sky for transient events, such as pulsars and fast radio bursts (FRBs). Science white papers [15–17] outline plans to understand the FRB mechanism and use them as cosmological probes. And some intensity mapping instruments will discover new millisecond pulsars, essential for the improved pulsar timing arrays for gravitational wave detection, as described in white papers [18–23].

After the recombination of hydrogen, when the Cosmic Microwave Background (CMB) was created at redshifts around $z \sim 1150$, the baryonic portion of the universe was dominated by neutral hydrogen. As matter continued to cluster in the post-recombination universe, peaks in the matter density grew and eventually led to the formation of the first generation of stars and galaxies, which emitted radiation capable of reionizing the ambient neutral hydrogen. Between recombination and the formation of the first stars, during the high-redshift epoch generally referred to as the Dark Ages $(30 \lesssim z \lesssim 150)$, neutral hydrogen traces the overall matter distribution. $21\,\mathrm{cm}$ intensity mapping is the only known technique for accessing this epoch and could provide large-scale tomographic maps sampling vastly more of the pristine density fluctuation modes than can the CMB.

Later, between $z \sim 30$ and $z \sim 6$, first-generation stars and galaxies formed and began the process of reionizing the universe. During this epoch, including Cosmic Dawn and the Epoch of Reionization (EoR), the signal is boosted by large regions of completely ionized "bubbles" residing in a sea of otherwise largely neutral hydrogen. Probing this unexplored phase of cosmic evolution was the top-ranked science program from the Astro2010 Radio, Millimeter, and Submillimeter panel. Indeed, a number of experiments, such as LWA, HERA, PAPER, LOFAR, MWA, and GMRT, are seeking to make the first measurements of how the first luminous objects affected the large-scale distribution and ionization state of hydrogen. They are spurred on by the possible detection of the signature of the formation of the first stars in the global spectrum [24] (as opposed to maps) of the $21\,\mathrm{cm}$. Because CMB photons scatter from the ionized matter, these intensity mapping measurements are critical to interpreting CMB power spectra. In particular, they can provide independent (of the CMB) measurements of τ, the optical depth of reionization, which is required for CMB constraints on neutrino mass [25].

Finally, in the post-EoR epoch, $z \lesssim 6$, the universe is mostly ionized, with a few pockets of neutral hydrogen residing in galaxies. $21\,\mathrm{cm}$ intensity mapping can measure the large scale structure in this epoch by surveying the aggregate emission from many unresolved galaxies. Even without resolving individual objects, one can still trace the fluctuations in their number density across space and redshift on large scales, where theoretical modeling is most robust. A key goal is to determine the expansion history of the universe spanning redshifts $z = 0.3 - 6$, complementing existing measurements at low redshift while opening up new windows at high redshifts. Another goal is to measure the growth-rate of structure formation over this same wide range of redshift and thus constrain modifications of gravity over a wide range of scales and times in cosmic history. One can also observe, or constrain, the presence of inflationary relics in the primordial power spectrum and observe, or constrain, primordial non-Gaussianity. The first generation of experiments in this redshift range include GBT, CHIME, Tianlai, HIRAX, OWFA, BINGO, BMX, and PAON. The proposed PUMA experiment [26] targets these science goals over the entire post-EoR epoch. Many of these instruments also include hardware and software for detecting radio transients. CHIME, for example, has already detected 13 FRBs [27] and is expected to find many more.

Reaching these science goals will require overcoming several challenges, including observing the 21 cm line over an enormous range of frequencies, from $\sim 10 - 1400$ MHz. However, all current observational programs, from Cosmic Dawn/EoR to post-EoR, have converged on broadly similar approaches. As outlined below, they require continued development of common hardware, data analysis, and simulation techniques. (A whitepaper focusing on Cosmic Dawn/EoR complements much of the discussion here [28].) Lessons learned from these ongoing programs will open wide a new window for astrophysics and cosmology.

2 Measurement Overview

Measuring the 21 cm signature of large scale structure promises enormous scientific payoffs. Unfortunately, the signal amplitude is small. These large volume surveys exploit large bandwidths, large fields of view, long integration times, and large numbers of receivers to maximize mapping speed. Over the past decade, measurements have evolved from using shared-facility single-dish radio telescopes and interferometers to dedicated 21 cm radio interferometers. Unlike facility interferometers (e.g. SKA), which include a mix of long and short baselines for high angular resolution imaging, intensity mapping interferometers are close-packed in order to map large-scale cosmological features. The recent revolution in low-noise radio technology allows the construction of relatively inexpensive interferometric arrays with hundreds to thousands of elements, bandwidth $\gtrsim 100$ MHz, and correlators powerful enough to process the signals from them. However, R&D can be carried out efficiently with small demonstrators, with on order ten elements. (See Table 1).

So far, Cosmic Dawn/EoR experiments have set upper limits on the 21 cm power spectrum [29,30]. These limits have steadily improved with better understanding and control of systematic effects. Post-EoR experiments have detected the 21 cm power spectrum in cross-correlation with galaxy redshift surveys [31–34] but none has so far detected it in autocorrelation, i.e. without the assistance of an optical galaxy redshift survey. These experiments face several measurement challenges, which we describe here. Later we outline how to overcome them with a coherent development plan.

Astrophysical foregrounds. Astrophysical foregrounds, primarily synchrotron emission from the Galaxy and unresolved point sources, pose the most significant measurement challenge, having much higher intensity than the 21 cm signal at all frequencies. These foregrounds have a smooth spectral shape and hence can in principle be distinguished from the 21 cm emission from large scale structure [35–38]. However, any frequency dependence in the instrument response, for example from the instrument beam or gain fluctuations, can complicate separation of the smooth foreground and the ‘spikey’ 21 cm signal [39, 40]. Removing these foregrounds drives most instrument design choices including array element uniformity, cross-polarization response, etc.

Instrument calibration. Each antenna has a characteristic response to an input sky signal, known as the instrument gain, which varies with both time and frequency. Each antenna also has a characteristic response on the sky, known as the instrument beam pattern. The gain and beam patterns must be measured well enough to remove astrophysical foreground power. Even in a ‘perfect’ instrument, the beam varies with frequency and causes features to appear in the spectrum that masquerade as structures in redshift space. If the frequency-dependent instrument response is known, these foregrounds can, in principle, be subtracted [41]. For actual post-EoR experiments, simulations for CHIME have provided a scale to the problem: the instrument response on the sky ('beam') must be understood to 0.1%, and the time-dependent response of the instrument ('gain') must be calibrated to 1% [39,40]. Uniformity and stability specifications must be carefully integrated into the instrument design and verified during testing and deployment.

FFT beamforming, real time calibration, redundant baselines, and array redundancy. For current arrays, with up to about 1000 elements, one can compute the fundamental observables of an interferometer, the correlations of RF signals from pairs of antennas (visibilities), for all pairs, using existing correlator designs. Calibration occurs offline. However, the correlation cost and data rate from future, larger arrays will require implementing other correlators, such as the EPIC correlator [42], or FFT beamforming correlators. Both use FFT-based sampling of the interferometric geometry [43–46] to reduce the computational correlation cost, from order N^2 to $N \log N$ and output data volume from N^2 to order N. Although promising first steps with EPIC and FFT beamforming [42,47] have been taken, they have not yet been demonstrated for 21 cm intensity mapping.

FFT beamforming in particular requires that all elements of the array be redundant (that their beams be similar), placing tight requirements on element uniformity. In addition, this correlation is performed in real time, and so requires real-time calibration to account for instrumental changes (or that the instrument remain extremely stable). Real-time calibration schemes are being developed [48]. Some exploit the fact that similar interferometric baselines should see the same sky signal and so differences between them can be used to assess relative instrument gains over time. This technique, known as 'redundant baseline' calibration [49–54], requires uniform interferometric elements with uniform spacing. And while promising, redundant baseline calibration has not yet been demonstrated to be good enough for 21 cm intensity mapping [55,56].

Environmental considerations. In addition to astrophysical foregrounds, two terrestrial contaminants must be eliminated or otherwise mitigated: human-generated radio-frequency interference (RFI) and the ionosphere. Radio bands within the entire range of 21 cm redshifts are popular for communications. RFI appears at discrete frequencies and can be reduced or eliminated by a suitable choice of radio-quiet observation site [57]. Even experiments operating in locations with high degrees of interference, notably LOFAR (located in the Netherlands), have developed impressive RFI removal algorithms [58].

The ionospheric plasma disturbs long wavelength measurement through both refraction and Faraday rotation [59, 60]. The ionosphere acts in concert with the Earth's magnetic field to rotate the polarization vector of incoming light by Faraday rotation. The rotation is proportional to λ^2 as well as the number of free electrons present in the ionosphere, which varies across all time scales. While the 21 cm signal is unpolarized, most foreground emission from the Galaxy is polarized and adds a time-variable component to the foreground characterization and removal. The λ^2 dependence means it primarily affects experiments at longer wavelengths (frequencies below $\sim$ 500 MHz, $\sim z > 2$), which attempt to measure and remove this rotation using accurate maps of the magnetic field and GPS data to infer free electron content. Because signal propagation through the ionosphere is critical for satellite telecommunications, it is well modelled and current low frequency radio telescopes are working to remove signal variability from the ionosphere [61]. At even lower frequencies ionospheric refraction, which also scales with λ^2, probably becomes the dominant effect .

Required sensitivity. In the absence of systematic effects, detecting the 21 cm signal requires fielding instruments including thousands of receivers to reach the mean brightness temperature of the cosmological 21 cm signal of $\sim$ 0.1 - 1 mK within a few years. Instrument noise stems from a combination of intrinsic amplifier noise (noise temperatures for state-of-the-art radio telescopes range from 25 K cryogenic to 100 K uncooled) and sky brightness temperature (which span between 10 K - 1000 K depending on pointing and frequency). Because synchrotron emission increases at lower frequencies, at high redshifts (above $z \sim 3$) the system noise is dominated by the sky and no longer by the amplifier; improved sensitivity must be achieved by fielding more antennas rather than better performing front-end amplifiers.

Computing scale. Radio astronomy has always been at the forefront of 'big data' in astronomy. Current generation 21 cm instruments produce $\gtrsim 100\,\mathrm{TB}$ of data per day without any compression. The data volume $\propto N^2$ where N is the number of elements (currently $N \sim 10^3$), representing challenges in data reduction, transfer, storage, analysis, distribution, and simulation. Compression by a factor of $\sim N$ is achievable with the FFT beamforming mentioned above. To aid in data transport, analysis, and data quality assessment, data must be compressed further (e.g. co-adding maps in a weekly cadence). This reduces the data size but increases pressure on real-time instrument calibration. In addition, to enable transient science, fast triggers are deployed at some current generation instruments [27].

3 Technology/hardware Development

Some of these challenges require advances in instrumentation. The aim is to have interferometers made of a large number of elements, each one reasonably inexpensive and robust, ensuring easy integration, and smooth operation.

Early digitization and signal processing. As noted above, changes over time of the gain of the receiver electronics is one of the limiting factors in removal of astrophysical foreground power. One promising idea to improve stability is to digitize the analog signal directly at each antenna, rather than remotely, which is the current practice. This early digitization will avoid the use of long analog cables, and analog frequency downconversion. This approach requires stable analog amplifier systems at each antenna and avoidance of RFI generated by the digital electronics. Furthermore, the system clock signal must be distributed precisely to each of the digitizers, moving the instrument phase calibration problem from the analog system into the clock distribution system. Thermal stabilization of the low noise amplifiers (LNAs) at each antenna may be required.

Optical and analog design. The receiver noise temperature is dominated by loss in the antenna as well as the noise in the LNA. HIRAX, for example, has chosen to reduce the system noise by up to 30% by fabricating the LNA directly in the antenna itself, reducing the transmission loss and taking full advantage of low-noise transistors available in these bands.

Antennas for 21 cm experiments range from dipoles for long wavelength experiments to parabolic reflectors, including on-axis dishes as well as cylindrical designs, at shorter wavelengths. Low sidelobes are desirable to allow operation when the Sun is up and to minimize coupling chromatic response into foregrounds. So far, the parabolic reflectors have supported receivers at the focus with struts or tensioned cables, leading to some diffraction and reflections. To illuminate the reflector, they have also included variants of dipole feed antennas with wide beams that have non-negligible cross-talk and frequency-dependence. These choices are typically made to save cost and complexity, but make calibration more difficult. Further studies should include options such as off-axis geometries (like SKA-mid and ngVLA) and possibly horn/Gregorian receivers, keeping marginal costs low while meeting uniformity and bandwidth flatness specifications, and exploring new reflector fabrication techniques. Current instruments are limited by the fact that their interferometric elements are not similar enough and motivate assessment of fabrication tolerances in mass-production.

Calibration. Current instruments rely primarily on sky signals for calibration of the beam and gain. However, this approach has not yet been demonstrated to adequately remove foregrounds with these instruments. The frequency-dependent gain for each input must be known to $\sim 1\%$ on time scales between the integration period ($< 5\,\mathrm{s}$ scales) and a few hours, depending on the rate of appearance of on-sky radio calibration sources [39]. This challenge can be met by a combination of instrument stability and a suitable calibration scheme. CHIME [62, 63] is updating a classic radio noise-injection scheme which can be used to calibrate many signal chains at once. To implement such an active calibration technique for large arrays will require development of a stable calibration distribution network as well as passive models of gain and beam variation with temperature and dish pointing.

Because the antenna beam pattern (main beam, sidelobes, and polarization) is frequency-dependent, it can mix frequency dependence (related to redshift) and sky location. This problem is expected to be the primary source of contamination from foreground emission into the signal band, and so must be known even more accurately than the electronic gain ($\sim$0.1%) [39]. This level of calibration is difficult for 21 cm telescopes because they are stationary and designed to have large beams for improved survey speed [64]. In addition, some instruments (such as CHIME) have large antennas, which can be difficult to simulate. Many 21 cm instruments are beginning to use signals from small unmanned aerial systems (sUAS, or "drones") and satellites to map the beam shape and measure the gain [65–70]. Ultimately, the beam calibration requirement sets a specification on uniformity in antenna fabrication.

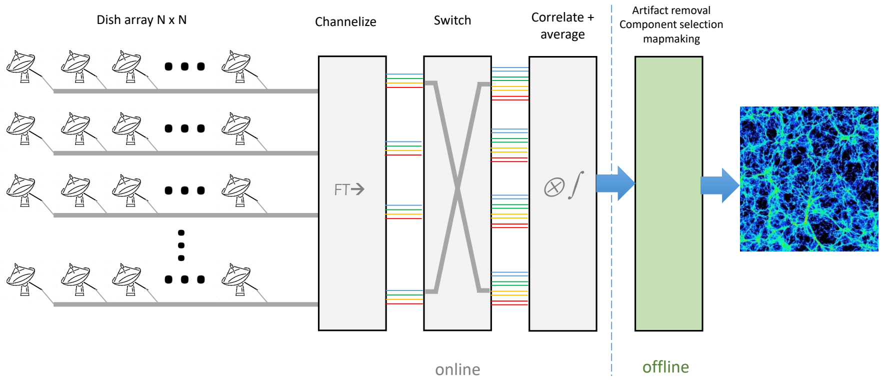

Figure 1: Illustration of anticipated data flow in a large interferometric array. Conversion of waveform data to frequency space, e.g. channelization, is accomplished close to each receiver; coincident data for each frequency bin are collected from all stations through a cross-bar switch (also called a "corner-turn" operation); correlations are constructed for each frequency bin, which can then be time-averaged and stored, followed by physics analysis.

Realtime data flow and processing. Large-N arrays are becoming increasingly software based, particularly when it comes to real-time data compression. Computing requirements for large interferometers come from the correlation burden, real-time calibration, RFI-excision, and the data reduction, transfer, storage, analysis, and synthetic data production (Fig.1). The correlator computation requires development in computing approaches which can improve the cost scaling both for equipment and power. Examples could include using commodity-hosted FPGA's, combined FPGA/CPU systems [71, 72], using/developing dedicated ASIC's [73], or using GPUs to exploit fast-paced hardware updates for correlator computation.

4 Data Analysis Development

Releasing science deliverables for the community from a 21 cm experiment depends crucially on developing an analysis pipeline that can transform vast quantities of data into well characterized frequency maps and power spectra. This is a computationally costly exercise, but does not require continuous real time processing. The analysis challenges center both on the methodology (optimal algorithms have yet to be demonstrated) and software engineering (data volumes are incredibly large). We can divide the analysis up into three broad areas.

Flagging, calibration, and pre-processing at scale. The acquired data are processed to reduce remaining systematic effects. Of particular importance is cleaning of RFI by flagging times and frequency channels that have been contaminated. The problem is well understood within radio astronomy [58], though the effects of residual RFI at the small level of the 21 cm signal is only starting to be addressed [74]. Though much of the calibration must be done in real-time (see above) there are still degrees of freedom that must be corrected in later analysis.

Astrophysical foreground removal. Foreground mitigation falls broadly into two classes: foreground avoidance and foreground cleaning. Foreground avoidance is the simplest of these two approaches, relying on the fact that contamination produced by a typical interferometer configuration is strongest in certain regions of k-space. Producing cosmological results using only the cleanest modes is a simple and effective technique, but it becomes deeply unsatisfactory at low frequencies, particularly in the dark ages. Here Galactic synchrotron and extragalactic point source radiation quickly becomes very bright even at high Galactic latitudes. At the same time, the window of clean modes dramatically narrows due to the relative scaling of the angular diameter distance and Hubble parameter with redshift [75]. Combined, this means that at a given threshold for contamination we exclude increasingly large regions of k-space at high redshifts, significantly degrading any cosmological result.

Foreground cleaning instead of (or in conjunction with) foreground avoidance then becomes an attractive option. These methods rely on detailed knowledge of the instrument response and the sky to predict and subtract the actual foreground signal. The residual contamination is set by both the amplitude of the raw contamination and the accuracy with which the beam has been measured.

Cosmological processing. The next step after foreground cleaning is to compute cosmologically useful quantities such as power spectra and sky maps. This step has been done within the CMB and LSS communities for many years but radio interferometric data brings unique challenges. Nevertheless, conceptual frameworks have been developed to tackle these problems [39, 76, 77]. Several areas of data analysis, then, will require research investment to ensure the success of a large scale 21 cm intensity mapping survey:

1. **Scaling.** A significant challenge is scaling existing analysis techniques to work with the vast increase in expected data in an energy-constrained/post-Moore's Law computing landscape. This process will require optimization of algorithms to reduce the computational cost, and ensuring that the techniques can operate in parallel on leading edge supercomputers.
2. **Systematic robustness.** Both astrophysical uncertainties (such as the exact nature of foregrounds) and instrumental uncertainties (such as calibration and beam optics) cause foreground contamination. Developing more robust cleaning techniques will reduce systematic biases, and

may lead to cost savings by reducing instrumental tolerance requirements.

3. **Improving signal recovery.** The loss of significant numbers of modes during foreground removal reduces our constraining ability generally and particularly affects science that needs access to the largest scales. Foreground removal methods like tidal reconstruction [78, 79] need to be developed that reduce the effect of the 'foreground wedge' [80]. Similarly, traditional reconstruction techniques [81, 82] that recover non-linear modes need to be adapted for the peculiarities of 21 cm intensity mapping.

5 Simulation needs & challenges

The challenges facing 21 cm surveys are significant but well understood. However, our ability to tackle them requires sophisticated approaches in instrumental design and offline analysis. It is therefore essential to use simulations to close a feedback loop that allows prediction, and thus refinement, of the effectiveness of a design and analysis strategy. The importance of this testing is especially evident in the face of sophisticated foreground mitigation strategies with the potential for significant signal loss [83]. While expensive to implement, an end-to-end simulation of the entire measurement process is necessary for designing a successful instrument and observational program.

Producing realistic simulations of data from any instrument configuration and propagating these to final cosmological results is a conceptually straightforward prospect:

1. **Produce a suite of full-sky maps of the "true" sky.** These include both the 21 cm cosmic signal and foregrounds, with one map per frequency bin observed by the instrument.
2. **"Observe" these maps with a simulation pipeline.** This step requires a detailed enough instrument model to provide realistic mock visibility data streams, including effects such as far side lobes, instrumental parameters drift, etc.; and
3. **Feed these mock observations into the data analysis pipeline and produce reduced data cosmological analyses.** This pipeline, discussed Section 4, is the same that would be used on real data. This step requires software tools to compute power spectra ($P(k)/C(\ell,\nu)$) from 3D sky maps or directly from visibilities, or higher order statistics. These tools could then be used to evaluate the realistic performance of different instrument configurations for constraining cosmological models and parameters.

For verification of foreground removal effectiveness, Gaussian or pseudo-Gaussian 21 cm simulations are largely sufficient [39, 85]. However, for targeting sensitivity to specific effects (e.g. non-Gaussian initial conditions), or in cross-correlation with other probes, more accurate simulations constructed from mock-catalogues will be required. This allows us to produce correctly correlated maps for additional tracers (e.g. LSST photometric galaxies), and also for radio point source contribution to the foregrounds.

Though the relation between HI density and total matter density involves complex environment-dependent processes, simulating it can be done efficiently. Recent work has shown that one can take advantage of the fact that neutral hydrogen in the post-reionization era resides almost entirely inside dark matter halos [84]. Thus, one can calibrate the relation between dark matter halos and HI using hydrodynamic simulations and create 21 cm maps (Fig. 2) via less expensive methods such as N-body or fast numerical simulations [86–94]. Similarly, while there are large-scale hydrodynamic EoR simulations (e.g. DRAGONS), modelers are parameterizing these numerical methods, and finding efficient ways to constrain those parameters [95].

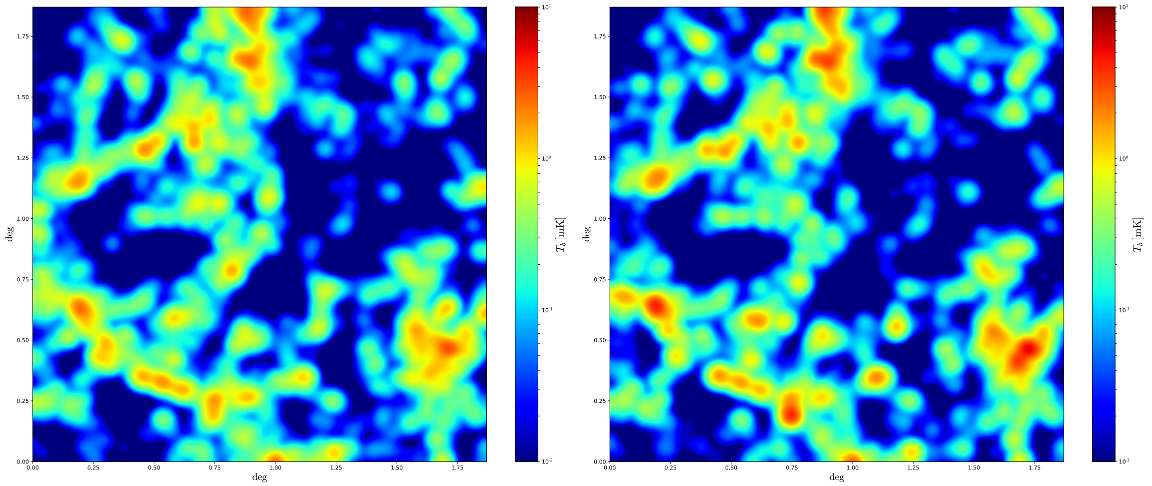

Figure 2: 21 cm maps at a frequency of 710 MHz over a channel width of 1 MHz with an angular resolution of 1.5’ over an area of $\simeq 4\ \mathrm{deg}^2$. The map on the left has been created from the state-of-the-art magneto-hydrodynamic simulation IllustrisTNG with a computational cost of $\simeq$18 million cpu hours. The map on the right panel has been generated by assigning HI to dark matter halos of an N-body simulation using the a simplification of the ingredients outlined in [84]. The computational cost of the N-body simulation is much lower than that of the full hydrodynamical simulation, and allows modelling of the HI field in a very precise and robust manner. The shapes of the power spectra of these two simulations differ by only $\sim 5\%$ from the largest scales down to $k = 1\mathrm{h}\ \mathrm{Mpc}^{-1}$.

Galactic synchrotron is the largest foreground contaminant and simulations must ensure they are not artificially easy to clean. A simple approximation can be produced by proceeding from a full sky map at a radio frequency and scaling to different frequencies based on the known spectral index of Galactic synchrotron radiation. However this is not sufficient at the dynamic range between the foregrounds and the 21 cm signal and one must be careful to include: spectral variations about a pure power law; small scale angular fluctuations not captured in existing surveys; and polarization, including the effects of emission at a wide range of Faraday depths which generates significant spectral structure in the polarized emission [39]. More sophisticated Galactic models, for example from MHD simulations, could also be developed and used here. Additional observations with existing instruments will better characterize the spectral behavior of the foregrounds.

In Step 2, a realistic instrument simulation pipeline would take the maps discussed and convolve them with the complex beam for each antenna in the interferometer [96]. This can be done by direct convolution utilizing the fact that for a transit telescope it is sufficient to generate a single day of data. However, for wide-field transit interferometers this can be performed more efficiently in harmonic space using the m-mode formalism [40] ($O(N \log N)$ instead of $O(N^2)$). Some of the required code would be similar to code used in CMB science, such as the TOAST package using fast numerical techniques for beam convolution [97].

These simulations require realistic models of the telescope beams. Electromagnetic simulation codes such as CST, GRASP and HFSS can be used for this, but achieving the accuracy required is challenging computationally [98–100]. A complementary approach is to generate synthetic beams with sufficient complexity to capture the challenges posed by real beams. These are computationally easier to produce, but must be informed by real measurements and electromagnetic simulations to ensure their realism, and may be aided by machine learning algorithms.

Capturing non-idealities in the analog system, particularly gain variations, is mostly straightforward as these can be applied directly to the ideal timestreams. Additionally, one needs to include

Name	Optimized	Steerable	Type	Elements	Redshift	First light
Existing w/ data:						
GMRT [101]	N	Y	interferometer	30 dual-pol × 45 m dishes	28	1995
GBT [102]	N	Y	single dish	1 dual-pol on 100 m dish	$\sim$0.8	2009
Dedicated exp'ts:						
OVRO-LWA [103, 104]	Y	N	interferometer	288 dual-pol dipoles	16 – 52	2012
MWA [105, 106]	Y	electronic	interferometer	256 tiles of 16 dual-pol dipoles	3.7–16	2013
PAPER [107, 108]	Y	N	interferometer	128 dual-pol dipole/reflector	7–12	2010
HERA [109, 110]	Y	N	interferometer	350 dual-pol 14 m dish (staged deploy't)	6–30	2016
LOFAR [111, 112]	Y	electronic	interferometer	3400 tiles of 16 dual-pol dipoles	5–11	2007
				4224 dual-pol dipoles	17–141	
CHIME [113, 114]	Y	N	cylinder interferometer	1024 dual-pol over 4 cyl	0.75 – 2.5	2017
HIRAX [115, 116]	Y	limited	dish interferometer	1024 dual-pol × 6 m dishes	0.75 – 2.5	2020
Tianlai Dish [117, 118]	Y	Y	dish interferometer	16 dual-pol × 6 m dishes	0 – 1.5	2016
Tianlai Cylinder [117, 118]	Y	N	cylinder interferometer	96 dual-pol over 3 cyl	0 – 1.5	2016
OWFA [119, 120]	N	Y	cylinder interferometer	264 single-pol	$\sim 3.4\pm0.3$	2019
BINGO [121, 122]	Y	N	single dish	$\sim$60 dual-pol sharing $\sim$50 m dish	0.12 – 0.45	2020
Dedicated R&D:						
BMX	Y	N	dish interferometer	4 dual-pol ×4 m off-axis dishes	0 – 0.3	2017
NCLE [123]	Y	N	satellite	3×5 m monopole ant. at Earth-Moon L_2	> 17	2018
PAON-4 [124, 125]	Y	limited	dish interferometer	4 dual-pol ×5 m dishes	0 – 0.14	2015
Non-dedicated:						
MeerKAT	N	Y	single-sish	64 dual-pol × 13.5 m dishes	0 – 1.4	2016
SKA1-MID	N	Y	single-dish	$\sim$ 200 dual-pol × $\sim$ 15 m dishes	0 – 3	2028
SKA1-LOW [126]	N	electronic	interferometer	269,312 dual-pol dipoles	3–27	2028
Proposed:						
PUMA [26, 127]	Y	limited	dish interferometer	5000, 32000 or 64000 dual-pol × 6 m dishes	0.3 – 6	<2030

Table 1: Current and planned 21 cm intensity mapping experiments. The "First light" column refers to first light for 21 cm observations for non-dedicated experiments. In the "Optimized" column, we note whether the telescope has been designed with intensity mapping as its primary scientific goal. For MeerKAT and SKA-MID, dishes will likely be used in a single-dish mode, with interferometric capability used only for gain calibration.

time-dependent beam convolution (including position and brightness) for temporally varying sources such as solar, jovian and lunar emission as well as the effects of RFI at low levels [74]. Including calibration uncertainties poses a particular challenge, because of the realtime calibration and compression of the instrument. Simulating these effects requires either: generating data at the full uncompressed rate, applying gain variations, and then performing the calibration and compression processes; or the computationally easier alternative of generating models of the effective calibration uncertainties.

After the first two stages, mock observations are then fed to the proposed data analysis pipeline, and propagated through to final cosmological products, to assess analysis systematics, instrument design, real-time calibration, etc. to determine whether the pipeline is sufficient to meet the science goals. Though the simulation program is well defined, there are many open challenges to address:

1. **Understanding the HI Distribution.** To map the HI distribution to the cosmologically useful matter distribution requires cutting edge hydrodynamic simulations to capture the small halos that HI favours over a cosmologically interesting volume.
2. **Scale.** We need to be able to produce large numbers of emulators that Monte-Carlo over the experimental uncertainties.
3. **Improving the feedback loop.** While a straightforward version of the simulation loop above can tell us whether a proposed design meets requirements, it does not show how to improve the design to ensure that it does. For a complex instrument with many design parameters it is essential to be able to guide this process to find the most relevant combinations of changes.

6 Participation in Current and Near-term (Stage I) Programs

Support for both small dedicated test-bed instruments and participation in existing and future large-scale initiatives, both US-led and international, will enable development and testing of the methods presented above and will benefit 21 cm intensity mapping efforts ranging from the Dark Ages to the post-EoR epoch. We believe that with rather modest investment of resources, such R&D will enable current experiments to extract maximum science while paving the way for future and even more exciting telescopes (Table 1). In particular, these efforts are the only way to make progress in foreground removal, instrument calibration, correlating signals from large arrays, dealing with RFI, achieving adequate sensitivity, and analyzing huge data cubes.

While there has been considerable funding from the US for Cosmic Dawn/EoR programs, currently there is no significant US funding for any of the existing post-EoR Stage I programs (CHIME, HIRAX, Tianlai). Post-EoR 21 cm intensity mapping is an unexploited probe of dark energy and inflation that is complementary to CMB and optical surveys. Participation in these efforts, or a new effort, would enable a coherent development plan that would include:

1. Construction of a test bed with 10-100 interferometer elements to test technologies (antennas and electronic as well as internal calibration systems).
2. Construction of a large, ~ 1000 element array to understand specific problems of operating such an array, including calibration and stability issues. Such an array should be operated with a (pairwise) correlator system first.
3. Development of an FFT beamformer and associated real-time calibration for this array.
4. Construction of a Stage II array with $10^4 - 10^5$ elements. An instrument of this scale is necessary to survey the entire post-EoR epoch.

Hardware development is not enough. An increasingly large share of the budget for all 21 cm intensity mapping programs is in the development of production- or system-level software. We need to pay close attention to developing software that does the real-time analysis (calibration, RFI excision, etc.), integrate it into a system, and fully test it.

7 Conclusion

A wide range of Astro2020 science goals depend on the success of 21 cm intensity mapping for measuring large scale structure in the universe over enormously larger volumes than possible today. This white paper has described a plan to advance this technique over the next decade and includes 1) development and testing of key technologies for reliable, robust single antenna systems which could be assembled as transit interferometric arrays, and associated central real time control/acquisition and computing systems. Most subsystems would be common to Cosmic Dawn/EoR and post-EoR observations. It also includes development of software for 2) data analysis and 3) simulations to realistically evaluate different instrument configurations. A significant fraction of the software tools would be common to all epochs. These technical achievements require 4) support for participation in current (Stage I) experiments to lay the groundwork for next generation (Stage II) experiments. As described above, Stage I experiments have already taught many lessons which must be understood before embarking on the next generation.

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