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Generalized single excitation configuration interaction: an investigation into the impact of the inclusion of non-orthogonality on the calculation of core-excited states

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Abstract

In this paper, we investigate different non-orthogonal generalizations of the configuration interaction with single substitutions (CIS) method for the calculation of core-excited states. Fully non-orthogonal CIS (NOCIS) has been described previously for species with singlet and doublet ground states, and this paper reports the extension to molecules in their triplet ground state. In addition to NOCIS, we present a novel method, one-center NOCIS (1C-NOCIS), for open-shell molecules which is intermediate between NOCIS and the computationally less demanding static exchange approximation (STEX). We explore this hierarchy of spin-pure methods for core excitations of molecules with singlet, doublet, and triplet ground states. We conclude that, while NOCIS provides the best results and preserves the spatial symmetry of the wavefunction, 1C-NOCIS retains much of the accuracy of NOCIS at a dramatically reduced cost. For molecules with closed-shell ground states, STEX and 1C-NOCIS are identical.

I. INTRODUCTION

X-ray absorption spectroscopy (XAS) is a highly useful and widely used method, due in large part to its element specificity and sensitivity to chemical environment^{1,2}. Sensitivity to environment also makes XAS a powerful reporter on excited states and electron dynamics^{3,4}. In addition to synchrotron-based experiments, smaller laboratory-scale XAS set-ups are also now being used in time-resolved experiments⁵. In light of this, the identification of characteristic XAS peaks of molecular species is of growing significance for experimentalists and theorists alike. This is especially true for species with an open-shell ground state, which have so far been less studied, and chemists face the difficult job of both assigning peaks and also identifying the source of peak shifts⁶. Theoretical calculations with a good balance of efficiency and accuracy can greatly facilitate the task of assigning XAS spectra.

There are many different approaches to calculations of core-excited states⁷. Early methods used multiple scattering X_{α}^{8} and transition potential calculations⁹, but since then abinitio quantum methods have dominated the field. Currently, the common methods used for core excitations are time-dependent density functional theory (TDDFT)^{10–15}, Δ -SCF and Δ -DFT¹⁶, coupled-cluster methods^{17–28}, algebraic diagrammatic construction (ADC) methods^{29–35}, and configuration interaction singles (CIS)^{36–38}. The general benefits and pitfalls of all these methods have been discussed elsewhere^{11,20,34}, but we would like to focus on multi-state, spin-pure, wavefunction-based methods that are cheaper than ADC and CC methods. To do so, we first look at the static exchange (STEX) method^{39–41}, which has been around for some time. The specific theory will be discussed more later, but of particular relevance is that in molecules with multiple equivalent atoms (eg. the two O 1s K-edges in CO₂) STEX considers the coupling between non-orthogonal determinants to be negligible. This makes STEX an exceptionally efficient method from a computational standpoint.

A natural extension of STEX is to include the coupling between non-orthogonal configurations, which we have termed non-orthogonal configuration interaction singles (NOCIS)^{42–44}. The theory is discussed in Section II. The inclusion of this coupling can be especially important for computing XAS spectra of doublet molecules⁴⁴ and in this work we reiterate this point and show that it is similarly important for triplet molecules. At the same time, the increased complexity of the method means that it is more computationally demanding than STEX. The purpose of this paper is to explore the impact of the coupling between non-orthogonal determinants on the calculation of core-excited states. To do so, we investigate the difference between the fully non-orthogonal method (NOCIS), a method that includes partial non-orthogonality (one-center, or 1C-NOCIS), and a fully orthogonal method (STEX) on molecules with singlet, doublet, and triplet ground states. The theory and implementation of 1C-NOCIS and of NOCIS for molecules with a triplet ground state has not been previously reported. We found that while NOCIS is the most accurate and has the advantage of not breaking spatial symmetry, the 1C-NOCIS method provides the best cost to benefit ratio for computing core-excited states, retaining some important aspects of non-orthogonality at a greatly reduced cost. We also demonstrate the practicality of 1C-NOCIS by computing XAS spectra of some medium-sized open-shell molecules.

II. THEORY

A. NOCIS

The motivation for NOCIS is the desire to improve on CIS while still maintaining a reasonably low computational scaling. It does so by including orbital relaxation, which CIS neglects altogether, and the non-orthogonal interaction between multiple core-hole references, such as the O 1s orbitals in O_2 .

A brief overview of the NOCIS algorithm is as follows: after a ground-state orbital optimization, a Maximum Overlap Method (MOM)⁴⁵ or a Square Gradient Minimization (SGM)⁴⁶ calculation is done for an ionization from each localized core orbital of interest. This introduces orbital relaxation, and also renders the excited states non-orthogonal to the ground state. The Hamiltonian, overlap, and total spin squared matrices are constructed using the Slater-Condon rules for matrix elements between determinants which share a common set of orbitals and NOCI for the remaining matrix elements⁴⁷. Finally, the generalized eigenvalue problem is solved.

NOCIS is spin-pure, size consistent, and maintains spatial symmetry. Like CIS, NOCIS produces excited states with the same m_s as the reference but potentially with larger total spin. For example, performing NOCIS on a molecule with a singlet ground state will produce both singlet and triplet excited states. In previous papers^{42,44}, we implemented NOCIS for



FIG. 1. A visual representation of the Hamiltonian matrices for each method for a two-reference doublet molecule (i.e. containing two atoms of a target element). The peach/diamond components are computed with orthogonal Slater-Condon rules, the blue/diagonal stripe elements are obtained with NOCI from the ionized determinants, and the green/vertical stripe elements are obtained with NOCI from the determinants that are excited into the open-shell orbital. The gray elements are zero.

molecules with singlet and doublet ground states. We provide a brief summary of these methods here.

NOCIS for core excitations from a singlet ground state has the following wavefunction:

$$|\Psi_{NOCIS}\rangle = \sum_{i=1}^{R} \sum_{a=1}^{V} \mathbf{t}_{i}^{a} (1 - \hat{\mathbf{P}}) [\hat{a}_{a}^{\dagger} \hat{a}_{i} \pm \hat{a}_{\bar{a}}^{\dagger} \hat{a}_{\bar{i}}] |\Phi_{i}\rangle \tag{1}$$

In singlet NOCIS, the wavefunction is constructed starting from R different core-ionized determinants corresponding to core electron removal from each identical atom of interest and ROHF optimization of those cation determinants. In the above notation, the core

electron has been added back into the relaxed orbital to form our $|\Phi_i\rangle$. This electron is then excited into each of the V virtual orbitals (different for each cation determinant), and the resulting core-excited configuration is projected against the closed-shell ground state determinant to ensure that the core-excited states are strongly orthogonal to the ground state. In Equation 1, \mathbf{t}_i^a are the amplitudes defining the NOCIS wavefunction of a particular core excited state that we are solving for, $\hat{\mathbf{P}}$ is the ground-state projector, and \hat{a}_a^{\dagger} and \hat{a}_i are the standard creation and destruction operators. A bar over the subscript indicates a beta electron.

In NOCIS for core excitations from doublet ground states, we begin to have to contend with ground-state open-shell orbitals in order to fully consider all possible single excitations. This involves the addition of another reference, which we term DS, indicating an excitation from a doubly occupied (D) core orbital to a singly-occupied (S) valence orbital.

$$|\Psi_{NOCIS}\rangle = \sum_{i=1}^{R} \sum_{a=1}^{V} (1-\hat{\mathbf{P}}) \left(\mathbf{t}_{i}^{a}[a_{a}^{\dagger}a_{i}] + \mathbf{t}_{\bar{i}}^{\bar{a}}[a_{\bar{a}}^{\dagger}a_{\bar{i}}] + \mathbf{t}_{\bar{i}k}^{\bar{k}a}[a_{\bar{k}}^{\dagger}a_{\bar{i}}a_{a}^{\dagger}a_{k}] \right) |\Phi_{i}\rangle + \sum_{i=1}^{R} \mathbf{t}_{i}^{k}(1-\hat{\mathbf{P}})[a_{\bar{k}}^{\dagger}a_{\bar{i}}]|\Phi_{i}^{k}\rangle$$

$$\tag{2}$$

There are a few changes of note when contrasting doublet and singlet NOCIS. The first is within the space of the original reference, $|\Phi_i\rangle$. In order to maintain spin-purity, we now feature an excitation that can be considered a double excitation, which is an XCIS-type extension⁴⁸, and moves us beyond the space of purely single excitations. Additionally, we can see the DS reference separately optimized, with k being the ground-state open-shell orbital. Because of this, the second and first terms are mutually non-orthogonal, which introduces additional non-orthgonality to our matrices. The notation in this equation is identical to that for Eq. 1 for the singlet ground state case.

In this work we have also implemented the extension of NOCIS to molecules with triplet ground states. As with doublet NOCIS, triplet NOCIS once again expands the number of configurations necessary to maintain spin-purity for the $m_s = +1$ state. This includes an additional reference for the second singly-occupied ground-state orbital. These excitations are visualized in Figure 2. The triplet NOCIS wavefunction is as follows:

$$|\Psi_{NOCIS}\rangle = \sum_{i=1}^{R} \sum_{a=1}^{V} (1 - \hat{\mathbf{P}}) \left(\mathbf{t}_{i}^{a}[a_{a}^{\dagger}a_{i}] + \mathbf{t}_{\bar{i}}^{\bar{a}}[a_{\bar{a}}^{\dagger}a_{\bar{i}}] + \mathbf{t}_{\bar{i}j}^{\bar{j}a}[a_{\bar{j}}^{\dagger}a_{\bar{i}}a_{a}^{\dagger}a_{j}] + \mathbf{t}_{\bar{i}k}^{\bar{k}a}[a_{\bar{k}}^{\dagger}a_{\bar{i}}a_{a}^{\dagger}a_{k}] \right) |\Phi_{i}\rangle$$
$$+ \sum_{i=1}^{R} \mathbf{t}_{i}^{j}(1 - \hat{\mathbf{P}})[a_{\bar{j}}^{\dagger}a_{\bar{i}}]|\Phi_{i}^{j}\rangle + \sum_{i=1}^{R} \mathbf{t}_{i}^{k}(1 - \hat{\mathbf{P}})[a_{\bar{k}}^{\dagger}a_{\bar{i}}]|\Phi_{i}^{k}\rangle \quad (3)$$

The notation in this equation is identical to Eq. 1 for singlet ground states.



FIG. 2. All potential triplet core-excitations for spin-completeness. i is a core orbital, j and k are the singly-occupied ground-state orbitals, and a is a virtual orbital. Three different sets of optimized orbitals are employed: core ionized orbitals for the core-to-virtual excitations and a specifically optimized set for each core-to-singly occupied configuration (DS 1 and DS 2 above).

B. Static Exchange

In the simplest form of STEX³⁹, one computes excitation energies by diagonalizing the virtual space of a Fock matrix for the ionized system. This method is especially attractive for computing x-ray spectra^{40,49} for many of the same reasons as NOCIS: it achieves much-improved results over conventional CIS, while being very computationally cheap, particularly relative to correlated methods such as ADC or EOM-CC. At present, however, STEX is not systematically improvable⁷ in the same way as NOCIS, which has more avenues for the addition of dynamic correlation such as NOCI-MP2⁵⁰.

When using STEX on multiple core-ionized states as done, for example, by Ågren et al.⁴⁹, the underlying assumptions are that the coupling between non-orthogonal determinants is negligible, and that all relevant excited determinants can be formed by single electron-attachment to the core-ionized state. In this way, STEX can be considered to be an approximation to NOCIS.

In our implementation of STEX, we follow an algorithm very similar to NOCIS. Our ground-state calculation includes the Boys localization of the reference orbitals before the MOM/SGM calculation. However, as can be seen in Figure 1, we form the DS reference from the core-ionized reference, instead of optimizing it separately. This renders the DS state orthogonal to the rest of the core-excitations from that particular atom. After the matrix build, we project the orthogonal matrix blocks against the ground state (contrasted with NOCIS, where the whole matrix is projected against the ground state), and solve the eigenvalue problem. Because the basis of excited determinants is not orthogonal to the ground state, NOCI is required to compute the oscillator strengths⁴¹. We also explored a method (referred to as STEX + Single Reference in Figure 1) where we separately optimized the DS reference as in NOCIS, but ignored the coupling between the resulting non-orthogonal determinants.

Like NOCIS, STEX is spin-pure and size-consistent. However, due to the de-coupling of the references, STEX calculations break the spatial symmetry of the final states, which can slightly skew the results (see Section III). It is also important to note that STEX has been known to compress spectra due to a lack of polarization effects, believed to be due to neglecting the screening effects of the excited electron, which causes the lowest core-excited states to be over-screened^{7,51}. NOCIS and 1C-NOCIS do not contain any explicit fix to this problem, and so may also exhibit this behavior (although the results presented later do not appear to be affected in this way).

C. One-Center NOCIS

To explore the effect of different types of non-orthogonality, we introduce another approximate method, one-center NOCIS (1C-NOCIS), which is an intermediate between NOCIS and STEX. The "DS" determinants are separately optimized as in NOCIS, but the coupling between non-orthogonal determinants with core holes on different centers is ignored. This is depicted in Figure 1, and NOCI is used to compute the remaining matrix elements between non-orthogonal determinants. 1C-NOCIS constructs the orthogonal Slater-Condon components of the matrices, and then performs NOCI to obtain the relevant non-orthogonal components. The diagonal blocks are then projected against the ground state.

For singlet NOCIS, 1C-NOCIS is the same as STEX, since there are no open-shell groundstate orbitals. As can be seen in Figure 1, for a doublet ground state this results in a column of matrix elements that must be computed using NOCI. For triplet molecules there are two such columns corresponding to the two open-shell orbitals of the ground state. It is easy to imagine how this could be generalized as the number of ground-state open-shell orbitals increases. There are two main advantages of 1C-NOCIS. First, it is substantially cheaper to evaluate than NOCIS and so enables the treatment of larger molecules. Crucially, in most systems we examine below, the coupling between excited determinants that is neglected in 1C-NOCIS is verified to be very small, so the accuracy of NOCIS is retained. Second, and in contrast to STEX, it allows the DS states to relax separately, which we have already shown to be important in NOCIS for core excitations on molecules with doublet ground states⁴⁴. We will present additional examples below.

D. Computational Implementation

The code for NOCIS, 1C-NOCIS, and STEX is implemented in a development version of Q-Chem 5.0⁵² utilizing the Armadillo linear algebra library⁵³. The NOCI code is a further modified version of the code developed by Sundstrom⁵⁴ and adapted by Oosterbaan et al.⁴². NOCIS scales as $\frac{1}{2}A(A-1)V^2N^2$, where A is the number of atoms of interest, V is the number of virtual orbitals, and N is the number of basis functions. 1C-NOCIS and STEX scale as AVN^2 , which is a substantial improvement.

III. RESULTS

All geometries are obtained from NIST's Computational Chemistry Comparison and Benchmark Database⁵⁵, which are optimized using B3LYP⁵⁶⁻⁵⁸ in the Def2-TZVPD basis set⁵⁹, except those in the Larger Cases section, which are optimized in Q-Chem using the same basis set and functional. Single-reference molecules are defined as molecules with only one equivalent atom (eg. the O K-edge in CO). Multi-reference molecules have more than one of the same atom of interest (eg. the O K-edge in CO₂), and thus result in larger matrix dimensions and a further introduction of non-orthogonality. We defined the K-edge as the lowest state with nonzero oscillator strength.

A. Benchmarks

For singlet molecules with single core-hole references, NOCIS, 1C-NOCIS, and STEX methods are identical. Additionally, 1C-NOCIS and STEX are identical for all sin-

Molecule	Experiment NOCIS STEX/1C-NO		STEX/1C-NOCIS
			(dif. from NOCIS)
$N_2 N(1s)$	400.96^{60}	404.529	0.013
$F_2 F(1s)$	682.2^{61}	685.485	0.015
$C_2H_2 C(1s)$	285.9^{62}	289.747	0.023
$C_2H_4 C(1s)$	284.68^{62}	288.677	0.005
$C_2H_6 C(1s)$	286.9^{62}	292.135	0.006
$\operatorname{CO}_2 \operatorname{O}(1s)$	535.3^{63}	538.045	0.000
$C_3H_8 C(1s)$	-	292.135	0.001
$C_3H_6 C(1s)$	-	288.984	0.000
$C_3H_4^a C(1s)$	-	289.597	0.000
$C_3H_4{}^b C(1s)$	-	290.097	0.003
MSE from NOCIS		-	0.007
RMSE from NOCIS		-	0.010
RMSE from Expt.		3.857	3.867

^a allene

^b propyne

TABLE I. A comparison of NOCIS singlet K-edge energies and 1C-NOCIS/STEX K-edge differences in the 6-31G^{64,65} basis set, and a further comparison to available experimental data. Mean signed error (MSE) and root mean square error (RMSE) are included. For singlet molecules, 1C-NOCIS and STEX are identical.

glet ground-state molecules. Thus, for singlet molecules we compare NOCIS and 1C-NOCIS/STEX for multiple core-hole reference molecules. The results can be seen in Tables 1 and 2.

The outcome of this is quite clear: while the NOCIS results are always lower in energy, the 1C-NOCIS/STEX results are very close to or the same as the NOCIS numbers, and in all cases are the same up to one decimal place, which is enough to identify a potential XAS K-edge. Thus, we conclude that multiple core-hole reference singlet molecules have a low degree of configuration interaction between configurations corresponding to core excitations from different atoms, and 1C-NOCIS/STEX is a more efficient way to obtain reasonably

Molecule	Experiment NOCIS STEX/1C-NO		STEX/1C-NOCIS
			(dif. from NOCIS)
$N_2 N(1s)$	400.96	402.119	0.019
$F_2 F(1s)$	682.2	683.601	0.014
$C_2H_2 C(1s)$	285.9	287.164	0.028
$C_2H_4 C(1s)$	284.68	286.380	0.007
$C_2H_6 C(1s)$	286.9	287.423	0.007
$\operatorname{CO}_2 \operatorname{O}(1s)$	535.3	536.096	0.000
$C_3H_8 C(1s)$	-	287.420	0.001
$C_3H_6 C(1s)$	-	286.749	0.001
$C_3H_4^a C(1s)$	-	287.330	0.003
$C_3H_4{}^b C(1s)$	-	287.517	0.003
MSE from NOCIS		-	0.008
RMSE from NOCIS		-	0.012
RMSE from Expt.		1.204	1.217

^a allene

^b propyne

TABLE II. A comparison of NOCIS singlet K-edge energies and 1C-NOCIS/STEX K-edge differences in the aug-cc-pCVTZ^{66–68} basis setand a further comparison to available experimental data. Mean signed error (MSE) and root mean square error (RMSE) are included. For singlet molecules, 1C-NOCIS and STEX are identical.

accurate results.

For doublet molecules with single core-hole references, 1C-NOCIS and NOCIS are identical. For multiple core-hole reference cases, the 1C-NOCIS matrices take the form of diagonal blocks as seen in Figure 1. This dramatic reduction of NOCI calculations provides a substantial speedup in computation time. The comparison results in the 6-31G^{64,65} and aug-cc-pCVTZ basis sets can be seen in Tables 3 and 4, respectively. There does not appear to be an appreciable change in the 1C-NOCIS/NOCIS differences on increasing the basis set size.

There are a few items of note in these results. The first is that the NOCIS-STEX

Molecule	Experiment	NOCIS	STEX	1C-NOCIS
			(dif. from NOCIS)	(dif. from NOCIS)
$HO_2 O(1s)$	528.6^{6}	531.710	1.179	0.000
$N_2^+ N(1s)$	-	397.679	0.341	-0.031
$C_2H_3 C(1s)$	-	285.601	0.493	0.000
NO $N(1s)$	399.7^{69}	403.316	0.946	0
NO $O(1s)$	532.7^{69}	534.956	0.000	0
$NO_2 N(1s)$	401.04^{70}	404.610	0.842	0
$NO_2 O(1s)$	530.32^{70}	532.775	0.966	0.001
OH $O(1s)$	525.8^{6}	529.833	1.654	0
$CH_3 C(1s)$	281.35^{71}	284.967	1.036	0
CN C(1s)	-	283.797	0.076	0
CN N(1s)	-	396.910	0.706	0
HCO $C(1s)$	-	288.470	0.697	0
HCO $O(1s)$	-	534.023	0.504	0
$N_2O^+ O(1s)$	-	531.955	1.148	0
$\mathrm{CO}_2^+ \mathrm{C}(1s)$	-	292.651	0.000	0
$\mathrm{CO}_2^+ \mathrm{O}(1s)$	-	530.433	0.955	-0.001
MSE from NOCIS		-	0.721	-0.002
RMSE from NOCIS		-	0.850	0.007
RMSE from Expt.		3.294	4.301	3.294

TABLE III. A comparison of NOCIS doublet K-edge energies and STEX K-edge and 1C-NOCIS differences in the 6-31G^{64,65} basis set, and a further comparison to available experimental data. Mean signed error (MSE) and root mean square error (RMSE) are included. A 0 in the 1C-NOCIS column indicates that 1C-NOCIS and NOCIS are identical in that case.

differences are markedly larger for doublet molecules than for singlet ones. This is due to the fact that the DS reference state is not optimized alone, and is instead formed from the coreionized reference. In previous work⁴⁴, we found that doing this substantially decreased the accuracy of our results, and that far more accurate results could be obtained by separately

Molecule	Experiment	NOCIS	STEX	1C-NOCIS
			(dif. from NOCIS)	(dif. from NOCIS)
$HO_2 O(1s)$	528.6	529.022	1.259	0.000
$N_2^+ N(1s)$	-	394.800	3.414	-0.036
$C_2H_3 C(1s)$	-	283.002	0.951	0.089
NO N $(1s)$	399.7	400.593	0.807	0
NO $O(1s)$	532.7	532.857	0.000	0
$NO_2 N(1s)$	401.04	401.886	0.000	0
$NO_2 O(1s)$	530.32	530.135	0.001	0.001
OH $O(1s)$	525.8	526.883	1.548	0
CH3 $C(1s)$	281.35	282.637	0.808	0
CN C(1s)	-	280.537	0.841	0
CN N(1s)	-	393.404	0.741	0
HCO $C(1s)$	-	285.823	0.680	0
HCO $O(1s)$	-	531.213	0.427	0
$N_2O^+ O(1s)$	-	528.943	1.234	0
$\mathrm{CO}_2^+ \mathrm{C}(1s)$	-	290.997	0.000	0
$\mathrm{CO}_2^+ \mathrm{O}(1s)$	-	527.253	0.604	-0.137
MSE from NOCIS		-	0.832	-0.012
RMSE from NOCIS		-	1.163	0.035
RMSE from Expt.		0.809	1.595	0.809

TABLE IV. A comparison of NOCIS doublet K-edge energies and STEX K-edge and 1C-NOCIS differences in the aug-cc-pCVTZ basis set, and a further comparison to available experimental data. Mean signed error (MSE) and root mean square error (RMSE) are included. A 0 in the 1C-NOCIS column indicates that 1C-NOCIS and NOCIS are identical in that case.

optimizing the DS reference. A more accurate DS determinant obtained from a separate orbital optimization has a large impact, as the DS reference is usually lower in energy than a core-to-virtual excitation, and would be expected to play a large role in core excitations. This is further borne out in cases where the DS state does not play a large role in the

Molecule	NOCIS	STEX	1C-NOCIS
$O_2 O(1s)$	532.784	1.146	0.027
$\operatorname{CH}_2 \operatorname{C}(1s)$	285.274	0.864	0
NH N $(1s)$	399.233	1.225	0
$CH_3N N(1s)$	408.604	0.752	0
HCF $C(1s)$	286.762	2.027	0
HCF $F(1s)$	688.240	0.534	0
HCCl $C(1s)$	293.396	0.756	0
$F_2C C(1s)$	287.956	0.971	0
$F_2C F(1s)$	687.485	0.622	0.000
$Cl_2C C(1s)$	295.463	0.532	0
MSE		0.957	0.003
RMSE		0.997	0.008

TABLE V. A comparison of NOCIS triplet K-edge energies and STEX K-edge and 1C-NOCIS differences in the 6-31G basis set. Mean signed error (MSE) and root mean square error (RMSE) are included. A 0 in the 1C-NOCIS column indicates that 1C-NOCIS and NOCIS are identical in that case.

K-edge due to symmetry, such as the NO O 1s K-edge. In this case, the K-edge is not a DS excitation, and NOCIS and STEX results are identical.

1C-NOCIS provides a significant improvement over STEX, with its error relative to NO-CIS being an order of magnitude smaller. This data also exposes a second item of note: some of these numbers are lower than the NOCIS results. This can be explained by realizing that both STEX and 1C-NOCIS break spatial symmetry. STEX and 1C-NOCIS do not allow localized states to mix.

In sum, for doublet molecules, 1C-NOCIS provides a relatively substantial increase in accuracy for a reasonable computational cost, which can be especially valuable when potential molecules of interest have K-edges that are very close in energy. If accurate spatial symmetry is desired, the only option of these three methods is NOCIS.

As in the doublet case, for triplet molecules with with single core-hole references, 1C-

Molecule	NOCIS	STEX	1C-NOCIS
${ m O}_2 { m O}(1s)$	530.338	1.265	0.016
$\operatorname{CH}_2 \operatorname{C}(1s)$	282.526	0.736	0
NH N $(1s)$	396.266	1.079	0
$CH_3N C(1s)$	286.538	0.824	0
HCF $C(1s)$	283.996	0.888	0
HCF $F(1s)$	685.429	0.570	0
HCCl $C(1s)$	283.460	1.022	0
$F_2C C(1s)$	285.372	0.773	0
$F_2C F(1s)$	685.059	0.430	0.075
$Cl_2C C(1s)$	284.443	1.183	0
MSE		0.877	0.009
RMSE		0.912	0.024

TABLE VI. A comparison of NOCIS triplet K-edge energies and STEX K-edge and 1C-NOCIS differences in the aug-cc-pCVTZ basis set. Mean signed error (MSE) and root mean square error (RMSE) are included. A 0 in the 1C-NOCIS column indicates that 1C-NOCIS and NOCIS are identical in that case.

NOCIS and NOCIS are identical. The comparison results in the $6-31G^{64,65}$ and aug-ccpCVTZ basis sets can be seen in Tables 5 and 6, respectively. Due to a lack of experimental data, we have not included a comparison column. Our results are largely consistent with the results from doublets: with the addition of another DS excitation, the difference between NOCIS and STEX further increases. It appears that this difference is further exacerbated when the molecules are charged, which is why the doublet average errors are higher than the triplet ones.

When exploring the STEX + single core-hole reference implementation for doublet and triplet molecules, we found that it improved on STEX, but remained about 0.1 eV on average higher than 1C-NOCIS at a comparable cost. This is consistent with our expectation that the addition of the singly-occupied orbital reference would improve the results. This is effectively a Δ -SCF calculation using the DS-optimized determinant, and this method may

	Wall Time (s)			CPU Time (s)		
	1C-NOCIS	ADC	EOM-CCSD	1C-NOCIS	ADC	EOM-CCSD
Methyl	23.6	315.5	382.2	365.5	1420.4	939.5
Ethyl	103.6	1779.1	969.9	1615.9	16010.6	6399.3
1-propyl	345.1	14113	1988.8	5382.3	147203.7	17283.6
1-butyl	970.1	125374.6	5261.3	15235.1	1468947.2	60654.5

TABLE VII. A comparison of 1C-NOCIS, ADC-CVS(2)-x, and EOM-CCSD timings for computing core excited states of alkyl radicals. Calculations were done on Q-Chem 5.2⁵², employing the cc-pCVDZ basis and run on 16 cores (on a 64 core node based on AMD Opteron 6134 processors running at a clock speed of 3.2 GHz).

not be suitable for higher excitations as there is no mixing between the DS state and the other core-to-valence determinants.

B. Applications

1. Computation Time

While NOCIS calculations grow unfeasibly long starting around 4 reference atoms, 1C-NOCIS does not suffer from such constraints. Table VII presents timings for post-SCF 1C-NOCIS for doublet alkyl radicals in the cc-pCVDZ basis⁶⁶ (along with a comparison to ADC-CVS(2)-x and CVS-EOM-CCSD). We found a minimum 3-fold speedup in CPU time for one-center NOCIS versus ADC/EOM-CCSD, and a far greater comparative speedup when parallelization is introduced. We also note that 1C-NOCIS computed *all* core excited states while ADC/EOM-CCSD solved for only the first twenty. We note that the very high ADC timings resulted from the need to perform many hundreds (or even thousands) of iterations to converge roots. This suggests that 1C-NOCIS is an attractive method to use for larger molecules.



FIG. 3. (2,2,6,6-tetramethylpiperidin-1-yl)oxyl (TEMPO)

2. TEMPO

With the significantly decreased computational time of 1C-NOCIS, we are now able to generate K-edges for larger molecules. As an example, we look at (2,2,6,6-tetramethylpiperidin-1-yl)oxyl, more succinctly known as TEMPO. TEMPO and its fellow free radicals are widely used in fields such as biochemistry and paramagnetic resonance spectroscopy, and may show promise for future use in medicine and organic synthesis⁷². With nine carbons, one nitrogen, and one oxygen, TEMPO is an ideal test for 1C-NOCIS.

For these calculations, we chose to use the recently developed SGM approach⁴⁶ to obtain the target core-ionized state energies. We used SGM instead of MOM for all our calculations of the C, N, and O K-edges of TEMPO, and the results can be seen in Figure 4. A comparison of the MOM and SGM results showed that both converged to identical ionized determinant energies. We used the cc-pCVDZ basis set.

Before discussing the results, it is first important to point out some features of the experimental spectra⁷². In the nitrogen spectrum, the second large peak at around 401.5 eV is actually the N₂ peak from the air, and so should not be seen in any calculated spectra. In the oxygen spectrum, the small peak next to the main peak at around 531 eV is the O₂ peak from the air, and should also not be seen in calculated spectra. All our spectra are simulated using a Voigt profile.

As can be seen from the comparisons, 1C-NOCIS agrees very well with the experimental spectra for TEMPO. It is somewhat puzzling, however, that the carbon spectrum requires a substantially larger shift than the nitrogen and oxygen ones. We have ruled out both relativistic and basis-set effects as the cause of this, and our hypothesis is that it is due to a difference in correlation. It is possible that the missing dynamic correlation is more significant for this system, and this is something we plan to explore further as we add dynamic correlation to our methods. Despite this, these results continue to provide encouragement



FIG. 4. A comparison of TEMPO experimental spectra (black)⁷² to 1C-NOCIS spectra for the carbon (green), nitrogen (blue), and oxygen(red) K-edges. Calculated spectra are shifted (C -3.4 eV, N -1.2 eV, O -1.1 eV) and use Gaussian and Lorentzian broadening (.2 Gaussian, .25 Lorentzian for N and O, .1 Gaussian, .15 Lorentzian for C).

for the use of 1C-NOCIS for use in identifying experimental spectra for doublet radicals.

3. Singlet and Triplet States of MBA

As more NEXAFS spectra are taken, it will become increasingly useful to be able to distinguish between the ground singlet and excited triplet state of a molecule, for example in studying the signatures of electronic dynamics. To this end, we looked at the singlet versus triplet states of 4-mercaptobenzoic acid (MBA), which has been examined using XAS, but only in its solid state⁷³.

After optimizing the singlet and triplet state geometries separately, we then performed 1C-NOCIS calculations for the oxygen K-edge, again using the SGM algorithm. We used



FIG. 5. 4-mercaptobenzoic acid (MBA), singlet geometry.

the cc-pCVDZ basis set. The results can be seen in Figure 6.



FIG. 6. A comparison of the 1C-NOCIS spectra for singlet (black) and triplet (red) MBA. Spectra use Gaussian and Lorentzian broadening (.2 G, .25 L).

Triplet MBA has a distinctive lower energy peak that singlet MBA does not, which is a signature that should be useful in identifying the presence of triplet MBA. The configuration of the excited state for the K-edge is the same for both the singlet and triplet species, so the peak shift is therefore a measure of the singlet-triplet splitting in the ground state.

Inspecting the available solid-state experimental spectrum⁷³ reveals that the general qualitative shape of the experimental curve is reproduced. However, the K edge of the triplet is either very faint or absent. It is possible that our intensity is overestimated or there are some experimental considerations that are unknown. It would be highly desirable to see gas-phase experiments for a direct assessment of the quality of our data.

IV. CONCLUSIONS

This paper explores the impact of varying levels of inclusion of non-orthogonality on core-excitation calculations, and also presents the implementation of one-center and triplet NOCIS. Overall, we found that the impact of non-orthogonality increased as the number of singly-occupied orbitals increased, but that it had a limited effect on molecules with multiple of the same atom of interest. However, full NOCIS is the only method to retain spatial symmetry, so it is still recommended in cases where this is important.

This motivated the development of an approximation to NOCIS, 1C-NOCIS, which includes non-orthogonality only in regard to the core excitations to singly-occupied groundstate orbitals. 1C-NOCIS dramatically reduces the number of NOCI calculations, the method's computational bottleneck, and enables the treatment of far larger molecules than full NOCIS. Methods based on open-shell NOCIS provide a very promising framework for core-excited states. Extensions to include dynamical correlation and spin orbit coupling are promising future directions. Already, these methods provide a convenient way to simulate XAS spectra of first-row atoms in concert with experiment at an acceptable cost.

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