Three-dimensional modeling of the P. falciparum genome during the erythrocytic cycle reveals a strong connection between genome architecture and gene expression
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Ferhat Ay,1,7 Evelien M. Bunnik,2,7 Nelle Varoquaux,3,4,5,7 Sebastiaan M. Bol,2 Jacques Prudhomme,2 Jean-Philippe Vert,3,4,5 William Stafford Noble,1,6,8 and Karine G. Le Roch2,8

1Department of Genome Sciences, University of Washington, Seattle, Washington 98195, USA; 2Department of Cell Biology and Neuroscience, University of California, Riverside, California 92521, USA; 3Centre for Computational Biology, Mines ParisTech, Fontainebleau F-77300, France; 4Institut Curie, Paris F-75248, France; 5U900, INSERM, Paris F-75248, France; 6Department of Computer Science and Engineering, University of Washington, Seattle, Washington 98195, USA

The development of the human malaria parasite *Plasmodium falciparum* is controlled by coordinated changes in gene expression throughout its complex life cycle, but the corresponding regulatory mechanisms are incompletely understood. To study the relationship between genome architecture and gene regulation in *Plasmodium*, we assayed the genome architecture of *P. falciparum* at three time points during its erythrocytic (sexual) cycle. Using chromosome conformation capture coupled with next-generation sequencing technology (Hi-C), we obtained high-resolution chromosomal contact maps, which we then used to construct a consensus three-dimensional genome structure for each time point. We observed strong clustering of centromeres, telomeres, ribosomal DNA, and virulence genes, resulting in a complex architecture that cannot be explained by a simple volume exclusion model. Internal virulence gene clusters exhibit domain-like structures in contact maps, suggesting that they play an important role in the genome architecture. Midway during the erythrocytic cycle, at the highly transcriptionally active trophozoite stage, the genome adopts a more open chromatin structure with increased chromosomal intermingling. In addition, we observed reduced expression of genes located in spatial proximity to the repressive subtelomeric center, and colocalization of distinct groups of parasite-specific genes with coordinated expression profiles. Overall, our results are indicative of a strong association between the *P. falciparum* spatial genome organization and gene expression. Understanding the molecular processes involved in genome conformation dynamics could contribute to the discovery of novel antimalarial strategies.

[Supplemental material is available for this article.]

Malaria remains a major contributor to the global burden of disease, with an estimated 219 million infected individuals and 660,000 deaths annually (World Health Organization 2012). One of the main limiting factors for the development of novel therapies is our poor understanding of mechanisms regulating the parasite's complex life cycle, which involves several distinct parasitic stages in the human and mosquito hosts. Regulation of these developmental stages is thought to be controlled by coordinated changes in gene expression. In addition, virulence associated with the human malaria parasite, *Plasmodium falciparum*, is known to be directly linked to the parasite's ability to tightly control the expression of genes involved in antigenic variations on the surface of infected red blood cells. Some progress has been made in elucidating mechanisms controlling the expression of these virulence genes (Duraiasingh et al. 2005; Freitas-Junior et al. 2005). Furthermore, a limited number of putative sequence-specific transcription factors (TFs) has been identified in the parasite genome (Coulson et al. 2004; Balaji et al. 2005), including 27 ApiAP2 plant-like TFs, and drastic changes in chromatin structure related to transcriptional activity have been observed throughout the parasite erythrocytic cycle (Ponts et al. 2010). However, general and specific mechanisms controlling the expression of the 6372 parasite genes remain poorly understood.

In higher eukaryotes, several analyses have emphasized the role of genome architecture in regulating transcription. Compartmentalization of the nucleus, chromatin loops, and long-range interactions contribute to a complex regulatory network (Lieberman-Aiden et al. 2009; Kalhor et al. 2011; Dixon et al. 2012; Homozu and Kudlicki 2013). In *P. falciparum*, little is known about the effect of genome organization on gene expression. Recent data indicate that genes involved in the control of parasite virulence (var genes) are associated with repressive centers at the nuclear periphery (Duraiasingh et al. 2005; Dzikowski et al. 2007;
Lopez-Rubio et al. 2009) and that ribosomal DNA gene clusters are also colocalized (Mancio-Silva et al. 2010; Lemieux et al. 2013). However, a global picture of the nuclear architecture throughout the parasite erythrocytic cycle progression and its role in transcriptional regulation is not yet available.

Chromosome conformation capture coupled with next-generation sequencing (Hi-C) measures the population average frequency of contacts between pairs of DNA fragments in 3D space and can be used to model the spatial architecture of the genome (Lieberman-Aiden et al. 2009; Duan et al. 2010; Kalhor et al. 2011). Here, we performed a variant of the Hi-C protocol, tethered conformation capture (Kalhor et al. 2011), to model at 10-kb resolution the spatial organization of the P. falciparum genome throughout its erythrocytic cycle. Our results indicate that the P. falciparum genome is highly structured, with strong colocalization of centromeres, telomeres, active rDNA genes, and virulence gene clusters. These virulence genes exhibit distinctive contact patterns and may therefore contribute to establishing the three-dimensional structure of the P. falciparum genome. We identified discrete chromosomal territories during the early and late stages of the parasite erythrocytic cycle, which are partially lost in the highly transcriptionally active trophozoite stage. Global chromosome movements during the erythrocytic cycle are coherent with levels of transcriptional activity during the different stages, and the three-dimensional genome architecture shows strong correlation with gene expression levels. Collectively, our results suggest that the P. falciparum genome organization and gene expression are strongly interconnected.

### Results

#### Assaying genome architecture of P. falciparum at three stages using Hi-C

To study the genome architecture of P. falciparum, we harvested parasites at three stages of the infected red blood cell cycle: after invasion of red blood cells at the ring stage (0 h), during high transcriptional activity at the trophozoite stage (18 h), and near the end of the cycle at the schizont stage (36 h), just before the newly formed parasites are released into the bloodstream. Next, we applied the Hi-C protocol (Kalhor et al. 2011) with modifications to accommodate the extremely AT-rich genome of the malaria parasite (Fig. 1A; Supplemental Note 1; Supplemental File 1). As a

![Figure 1](image-url)
control, we prepared a sample for which chromatin contacts were not preserved by cross-linking of DNA and proteins.

We evaluated the quality of the resulting data for each sample. First, we confirmed that the contact probability between two intrachromosomal loci exhibits a log-linear decay with increasing genomic distance (Fig. 1B; Supplemental Fig. 1). Second, we obtained lower numbers of interchromosomal contacts from cross-linked samples relative to both random expectation and our control sample (Supplemental Table 1). Third, we observed that the percentage of long-range contacts (either intrachromosomal or interchromosomal >20 kb) was significantly higher than control and comparable to the numbers observed in yeast (Duan et al. 2010; Supplemental Table 1). Together, these results indicated that we successfully assayed the P. falciparum genome architecture with a high signal-to-noise ratio. We then coalesced the mapped read pairs into a raw contact count matrix at 10-kb resolution, and we corrected for potential technical and experimental biases (Fig. 1C; Supplemental Fig. 2; Imakaev et al. 2012). The resulting normalized contact maps were used to identify a subset of high-confidence contacts for each stage (Methods; Supplemental Note 2; Supplemental File 2; Ay et al. 2014). We identified pairs of genes that show evidence of stage-specific contacts (Methods) and then applied gene set enrichment analysis to the set of genes that participate in such contacts. This analysis identified significant enrichment of VRSM genes for the ring and trophozoite stages (Supplemental Table 2). This observation suggests that the proximity between some VRSM clusters changes from the ring to trophozoite stages, even though both stages show overall colocalization of VRSM clusters. A similar enrichment analysis conducted using contacts that are specific to two out of three stages resulted in no significant enrichment due to the small number of genes involved in such contacts.

Normalized contact count and confidence score matrices exhibit a canonical “X” shape, indicative of a folded chromosome architecture anchored at the centromere, as previously observed in yeast (Duan et al. 2010; Tanizawa et al. 2010) and the bacterium C. crescentus (Fig. 1C,D; Supplemental Fig. 3; Umbarger et al. 2011). However, chromosomes that harbor nonsubtelomeric clusters of genes involved in antigenic variation and immune evasion (Supplemental File 3) (VRSM genes: var, rifin, stevor and Pfmc-2tm)—chromosomes 4, 6, 7, 8, and 12—exhibit additional folding structure (Fig. 1C,D; Supplemental Fig. 3).

Three-dimensional modeling recapitulates known organizational principles of Plasmodium genome

To better characterize the genome architecture, we generated 100 consensus 3D structures for each stage, each of which summarizes the population average (Fig. 2A; Methods), using multidimensional scaling (MDS) with two primary constraints (Duan et al. 2010): (1) the DNA must lie within a sphere with a specified diameter (Bannister et al. 2005; Weiner et al. 2011), and (2) adjacent 10-kb loci must not be separated by more than 91 nm (Bystricky et al. 2004). P. falciparum undergoes an atypical form of cell division, resulting in schizont stage parasites with multiple independent nuclei, each containing 1n chromosomes. Note that our model assumes that a single copy of each chromosome is present in each structure, thus averaging the signal from these multiple nuclei per cell.

We performed a series of experiments to assess the robustness of our 3D inference procedure. Our results showed only slight changes in the inferred 3D models when we varied the parameter used in conversion of contact counts to expected distances (Supplemental Table 3). This was also true when we removed from the inference the two types of spatial constraints related to nuclear volume and to distances between adjacent beads (Supplemental Table 4). Finally, our experiments on the impact of the initialization step (Methods) showed that structures inferred from different initial configurations are highly similar (Supplemental Fig. 4), do not fall into discrete clusters (Supplemental Fig. 5) and all such structures exhibit common organizational hallmarks (Supplemental Fig. 6). Because of the stability of our inference procedure, hereafter we generally present and discuss the results for only one representative structure per stage.

Although the modeling procedure contains no explicit constraints on telomere or centromere locations, we observe strong colocalization of both sets of loci across all three stages (Fig. 2A;
Supplemental Fig. 7; Supplemental Table 5), with centromeres and telomeres localizing in distal regions of the nucleus. To understand further the colocalization patterns of centromeres and telomeres in each stage, we divided each chromosome into three compartments (left−mid−right or telomeric−centromeric−telomeric) using eigenvalue decomposition (Methods) and then performed hierarchical clustering on the matrix of pairwise distances between compartments (Supplemental Fig. 8). At each stage, we observed clusters that are comprised primarily of either centromeric or telomeric compartments. In particular, during the trophozoite stage, all of the centromeric compartments fall into two main clusters suggesting strong colocalization of all centromeres for this stage (Supplemental Fig. 8D). Such strong colocalization has previously been observed by immunofluorescence microscopy at the trophozoite and schizont stages but not at the early ring stage (Hoeijmakers et al. 2012). However, when the size of the nucleus is used as a marker of the parasite asexual cycle stage (Bannister et al. 2005; Weiner et al. 2011), the cells that are presented as trophozoites in this previous study (Hoeijmakers et al. 2012) are more similar to our ring-stage parasites, indicating that centromere clustering also occurs early in the erythrocytic cycle. Furthermore, if the centromeres are stochastically distributed between a small number of foci within a population, then an assay that measures average signal, such as Hi-C, will indeed demonstrate an aggregate clustering for the centromeres and not complete dispersion as suggested by a recent study (Lemieux et al. 2013). These results suggest that *P. falciparum* nuclei are highly structured around centromeres and telomeres, consistent with known organizational principles gathered through multiple independent microscopy experiments (Duraisingham et al. 2005; Dzikowski et al. 2007; Lopez-Rubio et al. 2009; Hoeijmakers et al. 2012).

Virulence gene clusters on different chromosomes colocalize in 3D

In addition to centromeres and telomeres, we observed for all VRSM gene clusters, both internal and subtelomeric, a significant colocalization with one another (Fig. 2A; Supplemental Table 5). The significant colocalization for VRSM clusters as well as for centromeres and telomeres were all reproducible when we used contact counts instead of 3D distances to perform colocalization tests similar to Supplemental Table 5 (data not shown). Given colocalization of the telomeres, colocalization of subtelomeric clusters is not surprising. However, the proximity of internal VRSM clusters with one another and with subtelomeric clusters is unexpected under the random polymer looping model and, to the best of our knowledge, observed experimentally for the first time. To further validate these results inferred from our 3D models, we performed DNA fluorescence in situ hybridization (FISH) (Methods; Supplemental Note 3) on an interchromosomal pair of strongly interacting (at 10-kb resolution) VRSM clusters: the internal cluster from chromosome 7 and a subtelomeric cluster from chromosome 8. We observed strong colocalization by FISH (>90% of cells) (Fig. 2B; Supplemental Fig. 9A; Supplemental Table 6), providing independent support for the clustering of VRSM genes. Although previous FISH results indicated that *var* genes form two to five clusters in 3D per cell (Freitas-Junior et al. 2000; Lopez-Rubio et al. 2009), others recently showed single foci for the VRSM gene-associated repressive histone mark H3K9me3 and heterochromatin protein 1 (PHF1) (Dahan-Pasternak et al. 2013), as well as for H3K36me3 that marks both active and silenced *var* genes (Ukaegbu et al. 2014). Because our experimental strategy (Hi-C) captures a population average, we are unable to distinguish between multiple VRSM gene clusters in 3D if the genes are randomly distributed among clusters from cell to cell. Using FISH experiments, we also observed strong colocalization (>90% of cells) (Fig. 2C; Supplemental Fig. 9B) for a pair of interchromosomal loci located outside VRSM clusters with consistent strong interactions at all three stages, while colocalization was not observed for a pair of noninteracting interchromosomal loci (<10% of cells, Supplemental Fig. 9C). These results demonstrate that our population average Hi-C data agrees with a majority of single cell FISH images.

**Highly transcribed rDNA units colocalize in 3D during the ring stage**

Similar to VRSM genes, the rDNA genes are strictly regulated during the parasite life cycle. In *P. falciparum*, these genes are dispersed on different chromosomes in five rDNA units containing the 18S, 5.8S, and 28S genes and one repeat unit consisting of three copies of the 5S gene. A previous FISH study suggested that all rDNA units localize at a single nucleolus but also claimed that the two units on chromosomes 5 and 7 that are actively transcribed during the ring stage (A-type units) are dispersed in the ring stage (Mancio-Silva et al. 2010). However, a more recent Hi-C study of ring-stage parasites demonstrated strong clustering of these two A-type units in multiple strains (Lemieux et al. 2013). Analysis of our Hi-C data confirmed overall enrichment of contacts between chromosomes 5 and 7 in all three stages and showed a particular peak of enrichment centered at the rDNA unit on chromosome 5 among all interchromosomal contact partners of the rDNA unit on chromosome 7 in the ring stage (3.32×) (Fig. 3A). We observed less striking enrichment of contacts that are not specific to or centered on the rDNA units for the other two stages (trophozoites [1.99×], schizonts [1.23×]) (Fig. 3B,C) during which the two rDNA units are not transcribed (Mancio-Silva et al. 2010). Reanalysis of the Lemieux et al. (2013) data using our processing pipeline also showed this enrichment consistently in three different NF54-derived strains in the ring stage (6.06×, 4.47×, and 4.61×, respectively, Supplemental Fig. 10A–C). Control libraries from both studies do not exhibit this enrichment (Fig. 3D; Supplemental Fig. 10D). Our 3D models for the ring stage place these two A-type rDNA units near the nuclear periphery. Together with the strong colocalization between A-type rDNA, these results suggest the existence of perinuclear transcriptionally active compartments. Such compartments may play a role in separating out the single active *var* gene per cell from compact chromatin around (sub)telomeric regions marked by the repressive H3K9me3 modification (Lopez-Rubio et al. 2009). We did not observe an overall colocalization between all rDNA units in the ring stage, including the three 18S, 5.8S, 28S units and one 5S unit that are not expressed during asexual erythrocytic cycle (Supplemental Table 5). This observation suggests that genomic location may influence rDNA expression by the preferential colocalization of the expressed rDNA units, away from the nonexpressed units.

**Transcriptionally active trophozoite stage exhibits an open chromatin structure**

Assaying three different time points, we observed significant changes in chromatin structure throughout the erythrocytic cycle. To visualize high-level changes, we generated animations showing the movement of chromosomes as the parasite progresses through
We observed that intrachromosomal contacts, even at very large distances, are more prevalent than interchromosomal contacts for all three stages, suggesting the existence and preservation of chromosome territories throughout the erythrocytic cycle. However, the enrichment in intrachromosomal contacts was the lowest for trophozoite stage for distances above 300 kb, suggesting a relative loss of territories in this stage compared with the other two. Second, we quantified how preserved the chromosomal territories are at each stage by estimating the degree of chromosome intermingling in our 3D models. We randomly sampled small spheres in the nucleus and asked, for each chromosome, what percentage of the spheres that contain any locus from chromosome \( i \) also contain a locus from another chromosome \( j \). Our results using different sphere sizes, and controlling for the varying nuclear diameter, consistently exhibited the highest amount of intermingling for the trophozoite stage and the highest territory preservation for the schizont stage (Supplemental Fig. 12).

To understand the architectural dynamics responsible for the systematic changes in chromatin compaction, we computed the relative movements among chromosome compartments during the erythrocytic cycle. Despite the increase in nuclear volume, many interchromosomal compartment pairs came closer together in the transition from the ring to the trophozoite stage (Supplemental Fig. 13A, red). Subsequently, most interchromosomal compartments moved away from each other in the transition to the schizont stage (Supplemental Fig. 13B, blue), resulting in more compact chromatin that favors formation of chromosome territories. These results are consistent with a previously proposed model, in which the \( P. falciparum \) nucleus exhibits a more open chromatin configuration at the trophozoite stage, enabling interchromosomal contacts and high levels of transcriptional activity (Ponts et al. 2010).

**Plasmodium genome architecture cannot be explained by volume exclusion**

We next assessed whether the primary architectural features in \( P. falciparum \) arise from a population of constrained but otherwise random configurations of chromatin following a simple volume exclusion (VE) model, as recently shown for \( Saccharomyces cerevisiae \) (Tjong et al. 2012). We therefore repeated the Tjong et al. simulations using the same set of constraints and successfully recovered the strong correlation between the simulated map and the experimentally observed yeast contact map (raw correlation of 0.91; normalized correlation of 0.57) (Fig. 4A; Methods; Supplemental Note 4; Supplemental Fig. 14). In contrast, our simulations for the ring, trophozoite and schizont stages of \( P. falciparum \) yielded markedly lower correlations (normalized correlation of 0.34, 0.39, and 0.49, respectively) and strikingly different contact maps compared with the experimentally observed maps (Fig. 4B). One significant reason for the observed discrepancy between yeast and \( P. falciparum \) is the...
lack of structure around clusters of VSRM genes in the simulated data (Fig. 4B). Accordingly, we conclude that the simple volume exclusion model, which so convincingly explains the yeast genome architecture, is insufficient to explain the observed architecture of P. falciparum genome, highlighting the need for a genome-wide assay such as Hi-C to obtain accurate structural models.

**VRSM gene clusters form domain-like structures**

Our results from the volume exclusion modeling and from visual inspection of the contact maps suggest that the internal VRSM gene clusters are associated with distinctive structural features. All eight of the internal VRSM clusters induce a striking cross-like shape, both in the contact count and 3D distance matrices (Fig. 5A,B; Supplemental Fig. 3). Quantification of this phenome-

non revealed a consistent contact pattern across all eight internal VRSM clusters (Supplemental Fig. 15), suggesting that VRSM gene clusters adopt a compact, domain-like structure. Although these domain-like structures resemble topologically associated domains (TADs) described in mammals (Dixon et al. 2012; Nora et al. 2012), the VSRM domains are much smaller (10–50 kb) compared with TADs (0.1–1 Mb). Furthermore, because VRSM genes have no orthologs in human and mouse, mechanisms regulating these domain-like structures likely differ from those in mammalian genomes. Further understanding of how these VRSM domains are formed in Plasmodium would shed light on genome architecture associated regulation of VRSM gene expression.

Another interesting pattern involving internal VRSM clusters emerged from further inspection of chromosome compartments. Five of the eight internal VRSM clusters (two on chromosome 4, one on chromosome 7, and both clusters on chromosome 12)
occur at compartment boundaries (third and fourth rows of Supplemental Fig. 3). This striking overlap suggests that VRSM genes may contribute to or rely upon the boundaries of chromosomal compartments. Taken together with the domain-like structures around these VRSM clusters, these results confirm that genome architecture is likely to be involved in the strict regulation of virulence genes during the erythrocytic cycle.

Expression is highly concordant with 3D localization for *Plasmodium* genes

Next, we investigated the relationship between the three-dimensional genome structure and gene expression using four published expression data sets (Le Roch et al. 2003; Otto et al. 2010; Lopez-Barragan et al. 2011; Bunnik et al. 2013). First, we observed that, for each of the three stages, interchromosomal pairs of genes that strongly interact (contact counts within the top 20%) as well as gene pairs that are in close proximity (<20% of the nuclear diameter) showed more correlated expression profiles than genes that are far apart (Fig. 6A,B), as previously observed in yeast (Homouz and Kudlicki 2013). To assess whether these observed trends are confounded by similarly expressed VRSM genes that strongly interact with each other and are placed together near telomeres by our 3D model, we repeated the above analyses by excluding all VRSM genes (Supplemental Fig. 16). Even though the observed trends are weakened by exclusion of VRSM genes, the decrease in 3D distance and increase in contact count with increasing expression correlation remained significant (Supplemental Fig. 16). It is also important to note that, for these analyses, we excluded intrachromosomal gene pairs to only focus on the relationship between 3D proximity and gene expression by eliminating the confounding effect caused by genes that lie nearby on a chromosome and show similar expression profiles. Second, we analyzed gene expression in relation to the repressive subtelomeric clusters (Duraisingh et al. 2005; Drzalowski et al. 2007; Lopez-Rubio et al. 2009) and other nuclear landmarks. The subset of genes that lie within 20% of the nuclear diameter to the centroid of the telomeres showed significantly lower expression levels than more distal genes (Fig. 6C). The repressive effect of the subtelomeric clusters is apparent in all three stages and is strongest at the trophozoite stage, in which subtelomeric VRSM clusters are known to be tightly repressed (Chen et al. 1998). If we remove the VRSM genes from the analysis, the repressive effect is still significant at the trophozoite stage, which is known to be the most active transcriptional stage of the erythrocytic cycle (Supplemental Fig. 17A,B). Similar analysis showed higher expression levels for genes located near the nuclear center, as well as for genes close to the centroid of the centromeres (Supplemental Fig. 17C,D). Furthermore, we observed significant and consistent colocalization across all three stages for 11 of the 15 expression clusters identified in Le Roch et al. (2003) (Supplemental Table 5). Strikingly, the trophozoite stage showed significant colocalization for clusters associated with genes that are repressed during this stage (clusters 1, 3, 4, and 13–15) as well as genes that exhibit high levels of expression (clusters 6, 9, 10, and 12), confirming the strong relationship between 3D location and gene expression.

To further explore the relationship between gene expression and 3D structure, we utilized an unsupervised learning method known as “kernel canonical correlation analysis” (KCCA) (Bach and Jordan 2002). This methodology identifies a set of orthogonal gene expression profiles that exhibit coherence with respect to the 3D structure (Methods). For all stages, the projection of gene expression patterns onto the first extracted profile exhibits a striking transcriptional gradient across the 3D structure, from the telomere cluster to the opposite side of the nucleus (Fig. 6C; Supplemental Fig. 18A,C,E). The coherence with 3D structure drops significantly in the second component of the KCCA (Supplemental Fig. 18B,D,F), suggesting that gene expression is strongly influenced by distance to the subtelomeric repressive center. To further interpret the KCCA results we used gene set enrichment analysis (Subramanian et al. 2005) on the ranked lists of projections onto the first KCCA component. The results showed, for all three stages, significant enrichment (Q-value < 0.01) of gene sets related to antigenic variation and translation (i.e., ribosome proteins) on the telomeric and nontelomeric side, respectively, of the extracted KCCA expression profile (Supplemental Tables 8, 9, 10). Similar to the colocalization test results for expression clusters of Le Roch et al. (2003), clusters of genes that are repressed (clusters 4, 13, and 14) and expressed (clusters 6 and 9–12) in the trophozoite stage showed consistent enrichment in the strongest KCCA profile (Supplemental Table 11). In addition, genes exclusively expressed in sporozoites (cluster 1) and gametocytes
(cluster 3) were also strongly enriched, indicating that the repression of these genes during the asexual erythrocytic cell cycle may be related to their localization within the nucleus. Finally, for GO terms related to parasite invasion (rhoptry, myosin complex, motor activity; Q-value < 0.1) and for the cluster of invasion genes (cluster 15), we observed an enrichment relative to the second KCCA component, suggesting that expression of invasion genes may also be regulated by the 3D genome structure (Supplemental Tables 11, 12).

Discussion

This study presents the first analysis of genome architecture during the cell cycle of a eukaryotic pathogen. Overall, our data demonstrate that the genome of *P. falciparum* exhibits a higher degree of organization than the similarly sized budding yeast genome. Although localization of chromosomes within the *P. falciparum* nucleus is partially dictated by size constraints, the simple volume exclusion model observed in yeast is insufficient to explain the 3D architecture of the *P. falciparum* genome. In particular, a striking spatial complexity is added by clusters of virulence genes, which function as critical structural elements that shape the genome architecture. Furthermore, our model correlates well with expression levels of parasite-specific gene sets and shows strong clustering of repressed genes and highly transcribed rDNA units, indicative of a nonrandom genomic organization that contributes to gene regulation during the asexual erythrocytic cycle. Considering the strong association between nuclear architecture and gene expression as well as the observed domain-like structures, *Plasmodium* species may be excellent model organisms to study the impact of genome structure on gene regulation. The lower complexity of genome organization in organisms with similarly sized genomes, such as yeast, may indeed be less informative for such investigations.
Assaying multiple time points during the parasite’s erythrocytic cycle revealed intriguing changes in genome structure between the different developmental stages. Our results show that the genome adopts a more open conformation during the trophozoite stage consistent with high transcriptional activity in this stage of the erythrocytic cycle, followed by compaction of chromosomes into discrete chromosome territories before reinvasion of a new host cell. A similar pattern was observed previously for nucleosome occupancy, with strong histone depletions at the trophezoite stage and nucleosome replacement at the schizont stage (Ponts et al. 2010). Based on these observations, we hypothesize that the spatial genome organization of P. falciparum, coupled with its dynamic chromatin structure, acts as an important alternative mechanism of transcriptional regulation, possibly compensating for the lack of a diverse collection of specific transcription factors (Coulson et al. 2004; Balaji et al. 2005) and the low capacity of the parasite to regulate gene expression in response to metabolic stress (Ganesan et al. 2008; Le Roch et al. 2008). These changes in genome architecture could mainly be indicative of differences between the various developmental stages of the parasite, but could also be related to cell cycle progression itself. Given the importance of nuclear architecture for regulation of gene expression, disruption of its genome organization is likely to interfere with parasite development through the erythrocytic cycle and could therefore be lethal to the parasite. Compounds targeting proteins involved in establishing and maintaining the three-dimensional genome structure in P. falciparum may thus have potent antimalarial activity.

A recently published Hi-C study suggested that chromosomal territories are absent in the ring-stage parasites, especially for larger chromosomes (Lemieux et al. 2013). In contrast, our data provides multiple lines of evidence for the existence of chromosome territories throughout the erythrocytic cell cycle. In particular, we observed that intrachromosomal contacts, even at very large distances, are more prevalent than interchromosomal contacts. This observation is supported by our own Hi-C data in three stages as well as by our reanalysis of the Lemieux et al. (2013) data (Supplemental Fig. A18–E). The difference between the two analyses can be traced to our improved method for discretizing the genomic distance axis, which avoids bins with few observations and, hence, high variance (Supplemental Fig. 11, A vs. B). Even though further experiments may be necessary to reconcile these differences, our results strongly suggest that P. falciparum chromosomes occupy distinct territories, similar to other eukaryotic genomes.

Clustering of virulence gene families into a distinct nuclear compartment is likely to play an important role in the formation of repressive heterochromatin that controls the silencing of these genes. Heterochromatin around virulence genes is characterized by histone modifications H3K36me3 (Jiang et al. 2013) and H3K9me3 (Duraisingh et al. 2005; Lopez-Rubio et al. 2009), both of which were shown to be essential for maintaining var gene repression. The formation of heterochromatin is directed by the interaction of PSIP2 with specific DNA motifs in promoters of virulence genes and in subtelomeric domains (Flueck et al. 2010), but additional factors are likely to contribute to this process. The question remains, however, how the formation of this repressive center is regulated and whether the colocalization of virulence gene clusters is a cause or a consequence of their transcriptional silencing. One experiment that would shed light on this issue would be to relocate a var gene to a different location in the genome and to monitor how the introduction of this novel var gene locus influences genome structure, although technical challenges that come with manipulation of the P. falciparum genome may prevent such procedures. Virulence genes are expressed on the surface of red blood cells and are therefore important antigens for the humoral immune system. A better understanding of virulence gene silencing will provide us with more opportunities to interfere with this process, which would ultimately benefit vaccine development.

In this study, we modeled the P. falciparum genome architecture based on the average signal from a population of parasites. However, it can be expected that considerable variability in genome conformation exists from cell to cell, as recently demonstrated in mouse (Na\gano et al. 2013). While challenging, it would be interesting to perform Hi-C analysis on individual parasites to reveal the extent of intercellular variation in P. falciparum genome architecture. This experiment would also allow a more detailed analysis of the clustering of var genes in one or multiple repressive centers, as well as the differential localization of the single active var gene.

In conclusion, this study demonstrates the unique role of genome organization in transcriptional regulation in the human malaria parasite. In other eukaryotes such as human and mouse, genome organization has been shown to participate in gene regulation through formation of specific chromatin loops that bring enhancers and enhancer-like elements in proximity to their target promoters. However, a global reorganization of the entire genome correlated with changes in transcriptional capacity, as described here for P. falciparum, has not been observed for any of the genomes studied so far. Therefore, our data proposes a novel mechanism of gene regulation for P. falciparum that can operate without relying on specific transcription factors or enhancer elements. Similar to other eukaryotes, gene expression in P. falciparum is likely to be regulated by multiple layers of control at both transcriptional and translational levels. However, the necessity to transcriptionally repress distinct groups of parasite-specific genes may have driven P. falciparum to adopt this exceptional genome organization.

Methods

Experimental protocols

P. falciparum strain and culture conditions

P. falciparum strain 3D7 was maintained in human O+ erythrocytes in 5% haematocrit according to a previously described protocol (Trager and Jensen 1976). Cultures were synchronized twice at ring stage with 5% D-sorbitol treatments performed 8 h apart (Lambros and Vanderberg 1979). Parasites were harvested 48 h after the first sorbitol treatment (0 h; ring stage), and then 18 h (early trophozoite stage) and 36 h (late schizont stage) thereafter. The developmental stage of the parasites was verified by microscopy using Giemsa-stained blood smears prior to harvesting.

Cross-linking

Aspirated P. falciparum cultures were pooled into 50-mL centrifuge tubes and filled up to 35 mL with phosphate buffered saline (PBS) warmed to 37°C. Cultures were treated with 3 mL 16% formaldehyde (1.25% final concentration) and incubated for 25 min at 37°C while rocking. Formaldehyde was quenched with 5.2 mL 1.25 M glycine (final concentration 150 mM) for 15 min at 37°C while rocking, followed by 15 min at 4°C while rocking. PBS was used instead of formaldehyde and glycine for the not cross-linked control. Cultures were spun at 660g for 20 min at 4°C. Not cross-
linked control parasites were treated with 5 volumes 0.15% saponin in water and incubated 10 min at 4°C while rocking. PBS was used instead of saponin for the cross-linked parasites. Parasites were spun at 660g for 15 min at 4°C. Pellets were washed multiple times until clean and stored at −80°C.

**Tethered conformation capture procedure**

We applied an adapted Hi-C method referred to as tethered conformation capture (TCC) (Kalhor et al. 2011) to map the intra- and interchromosomal contacts in *Plasmodium falciparum*. For a detailed description of the overall protocol see Supplemental Note 1.

**DNA-FISH**

For each 10-kb locus of interest, we determined the location for which, on average, the highest number of contact counts were observed and designed DNA probes targeting the 2-kb region surrounding this location. Probes were prepared using Fluorescein-High Prime and Biotin-High Prime kits (Roche) according to manufacturer’s instructions. Template DNA was prepared by PCR (5 min at 95°C, 35 cycles of 30 sec at 98°C, followed by 150 sec at 62°C, and 5 min at 62°C) using the KAPA HiFi DNA Polymerase HotStart ReadyMix. Sequences of primers used for probe generation are shown in Supplemental Table 6. For a detailed description of the DNA-FISH protocol, see Supplemental Note 3. The percentage of colocalization was determined by visual inspection of >100 cells per condition.

**Computational methods**

**Mapping and filtering of sequence data**

We first trimmed each end of the paired-end reads from all samples to 40 bp. We used FastQC (Andrews 2010) reports of aggregate read qualities for each sample to determine the amount of trimming required from each end of the read to keep the highest quality 40-bp region.

To filter out reads from human DNA, we mapped the trimmed paired-end reads to the human genome (UCSC hg19) using the short read alignment mode of BWA (v0.5.9) (Li and Durbin 2010) with default parameter settings. Each end of the paired reads was mapped individually. We post-processed the alignment results to extract reads that mapped with an edit distance of at most 3. We then eliminated all pairs for which at least one of the ends mapped to the human genome without any filtering on the mapping quality or uniqueness. This loose mapping criteria is used to assure that any read pair that is likely to come from human blood contamination in the parasite samples is filtered out from our further analysis of *Plasmodium* genome architecture.

We mapped the remaining paired-end reads to the *Plasmodium falciparum 3D7* reference genome (PlasmoDB v9.0). We post-processed the alignment results further to extract the reads that mapped (1) uniquely to one location in the reference genome, (2) with an alignment quality score of at least 30 (which corresponds to a one in 1000 chance that the mapping is incorrect), and (3) with an edit distance of at most 2. We extracted the paired-end reads with both ends mapping to the *Plasmodium* genome. We then identified potential PCR duplicates, i.e., pairs of read-pairs with identical genomic coordinates, and retained only one copy of each. We also filtered out reads that map to intrachromosomal loci that are ±1-kb apart. We refer to the remaining reads as “informative reads.” We computed chromosomal contact maps using only these informative reads. Supplemental File 1 summarizes the results of applying this pipeline to our sequencing libraries.

Calculating noise level and percentage of long–range contacts

We calculated two measures that provide estimates of the noise level and efficiency of the assay. The first is the interchromosomal contact probability (ICP) index (Kalhor et al. 2011):

\[
ICP = \frac{\sum \text{interchr contact counts}}{\sum \text{intrachr contact counts} (> 1 \text{ kb})}.
\]

In the denominator, the intrachromosomal contact counts exclude contacts between pairs of loci ±1-kb apart. Smaller ICP values indicate a better signal-to-noise ratio, assuming that the real data (signal) will be enriched for intrachromosomal contacts, whereas noise will be dominated by interchromosomal contacts. The second number is the percent of long-range contacts (PLRC) extracted from the initial set of paired-end reads that remain after filtering the reads that mapped to human genome:

\[
PLRC = \frac{\sum \text{interchr contact counts} + \sum \text{intrachr contact counts} (> 20 \text{ kb})}{\text{Number of raw reads after human DNA filtering}}.
\]

The bigger this percentage is, the more information the data set provides about nonadjacent chromatin contacts for the amount of sequencing in hand.

**Aggregating data relative to 10-kb windows**

Digesting the DNA with a frequently cutting restriction enzyme yields a very large number of possible pairs of restriction fragments (i.e., locus pairs). In our case, digesting the *Plasmodium* genome with Mbol, which cuts at the 4-bp recognition site “GAATC,” yielded 28,784 fragments (mean length 810 bp) corresponding to 33,114,193 intrachromosomal and 336,629,028 interchromosomal locus pairs. For 3D modeling, we partitioned the *Plasmodium* genome into a collection of nonoverlapping 10-kb windows, and we assigned each restriction fragment to the 10-kb window that covers the majority of the bases in the fragment. This operation reduced the number of possible fragments from 28,784 to 2337 and the number of possible locus pairs from 3.7 × 10³ to 2,715,615 (228,539 intrachromosomal and 2,487,076 interchromosomal).

**Normalizing raw contact maps**

For each possible pair of 10-kb loci, we refer to the total number of informative read pairs that link the two loci as the “contact count,” and we refer to the two-dimensional matrix containing these contact counts as the “raw contact map.” We normalized the raw contact maps in two steps. First, we ranked loci by their percentage of intrachromosomal contacts with zero counts, and we filtered out the top 2% of this list. This removes all loci for which the signal-to-noise ratio is too low (typically, regions of low mappability). Second, we applied an iterative correction and eigenvector decomposition (ICE) method (Imakaev et al. 2012) that attempts to eliminate systematic biases in Hi-C data. The method estimates a bias vector with one entry per locus. The tensor product of the bias vector with itself generates a bias matrix that can be used to convert the raw contact map into a normalized contact map.

**Estimating power–law fits to intrachromosomal contact probabilities**

It has been observed in the literature that for a pair of intrachromosomal loci, the relationship between genomic distance and the expected contact count can be estimated by a log-linear model (Lieberman-Aiden et al. 2009; Fudenberg and Mirny 2012). This log-linear model is captured by a power-law fit of the form \( P(s) \sim s^\alpha \),
where $s$ denotes the genomic distance, $P(s)$ denotes the expected contact probability at distance $s$, and $a$ is the gradient of the log-linear fit. For each stage, we first calculated $P(s)$ by segregating all intrachromosomal locus pairs into $b = 50$ equal-occupancy bins. This procedure involves enumerating all possible intrachromosomal locus pairs (including pairs that have a contact count of zero), sorting the pairs in increasing order according to their genomic distances, and then segregating the resulting list into $b$ quantiles. For each bin $i$, we computed the average number of contact counts per locus pair $c_i$ and the average contact distance $s_i$ over all locus pairs in the bin. Then, for each bin $i$,

$$P(s_i) = \frac{c_i}{N},$$

where $N$ is the sum of all observed intrachromosomal contact counts. We then found the best linear fit to log $P(s)$ versus log $s$ in a given genomic distance range. Note that the control library “TROPIH-cont.” was not subjected to normalization.

**Assigning statistical significance to normalized contact maps**

To obtain a set of high-confidence contacts for each stage, we subjected the contact maps at 10-kb resolution to a statistical confidence estimation procedure (Ay et al. 2014). We first accounted for the effect of genomic distance on the intrachromosomal contact probability by fitting a smoothing spline to capture this effect. We then accounted for biases using the normalization procedure described above. Finally, we calculated $P$-values for intra- and interchromosomal contacts and corrected them jointly for multiple hypothesis testing to compute $Q$-values, which are used to filter contacts at a desired false discovery rate. For a detailed description of the statistical significance estimation procedure see Supplemental Note 2.

**Identifying stage-specific contacts**

We determined the contacts that are specific to only one stage or to two out of three stages as follows. First, we sorted the lists of contacts at 10-kb resolution according to increasing $P$-values computed as described above for each stage. Then, we extracted contacts that are ranked in top 1000 in each stage and checked to see whether they appear among top 10,000 contacts for the other two stages. We labeled these contacts as stage-specific because they are among the strongest contacts for one stage but not among moderately strong contacts for the other two stages. Similarly, we labeled contacts that are in the top 1000 in two out of three stages but not in the top 10,000 for the third stage. To perform gene set enrichment analysis (GSEA), we extracted the lists of genes that are involved in stage-specific contacts (only ring, only trophozoite, or only schizont) as well as contacts common to two stages (common to ring and trophozoite, common to ring and schizont, or common to trophozoite and schizont).

**Inferring the 3D structures**

Our method for inferring the 3D structures is based on the method of Duan et al. (2010). Each chromosome is modeled as a series of beads on a string, spaced ~10-kb apart. We associated with each pair of beads $x_i$ and $x_j$ a physical wish distance $\delta_{ij}$—i.e., the distance that we aim to capture with our 3D model—derived from the bead pair’s contact count $c_{ij}$. We then placed all the beads in 3D space such that the distance $d_{ij}$ between the beads $i$ and $j$ is as close as possible to the wish distance $\delta_{ij}$.

**Wish distances**

To obtain the wish distances, we note that two proximal intrachromosomal loci are likely to come into contact due to random looping of the DNA, and that this “polymer packing” contact likelihood can be expressed as a function of the genomic distance $s$ between the loci. We then assumed that two loci with observed contact count $c_{ij}$ will have the same physical distance $\delta^{0}$ as two intrachromosomal loci with expected contact count $c_{ij}$ by polymer packing. The relationship between the expected contact frequencies and the genomic distances $s$ suggests that $P. falciparum$’s DNA behaves like a fractal globule polymer (Lieberman-Aiden et al. 2009) (Supplemental Fig. 1). Any crumpled polymer exhibits a well-defined relationship between its genomic length $s$ and the physical distance $d$ (Grosberg et al. 1988):

$$d = s^{1/3}.$$

Therefore, using the relationship between genomic distances $s$ and contact frequencies $c$, obtained by the fitting of the linear model, and the relationship between physical distances $d$ and genomic distances $s$ (Equation 1), we inferred a mapping between contact frequencies $c$ and physical distances $d$ up to a factor. We arbitrarily set the distance of the two beads with the smallest non-zero contact count $c_{\text{min}}$ to be at a certain percentage $\beta$ of the nucleus diameter. Note that $c_{\text{min}}$ is not necessarily equal 1 since the contact counts are normalized. The $\beta$ parameter hence sets the scaling of the physical distances. We then obtain

$$\delta_{ij} = \frac{\beta 2r}{c_{\text{min}}} s_{ij}^{1/3},$$

where $r$ is the nucleus radius and $a$ the coefficient obtained in the linear model fitting (range: 30–500 kb, $a = -0.963$ for rings, $a = -1.124$ for trophozoites, $a = -1.013$ for schizonts). We set all distances larger than the nucleus diameter to this value.

**Optimization**

Given the resulting physical wish distances, we defined the following optimization problem to find a structure $X \in R^{3 \times n}$, where $n$ is the number of beads:

$$\text{minimize} \quad \sum_{i,j \in D} \frac{1}{n} (d_{ij} - \delta_{ij})^2$$

subject to

$$x_i^T x_i \leq r_{\text{max}}^{\text{max}}, \quad i = 1:n$$

$$d_{ij} \leq b_{ij}^{\text{max}}, \quad i = 1:n, i j \in (1:n) \cup (\text{chr} r = \text{chr}_{i+1})$$

where $d_{ij}$ is the Euclidean distance between beads $x_i$ and $x_j$, $D = \{d_{ij} \neq 0\}$ is the set of nonzero wish distances, and $b_{ij}^{\text{max}}$ is defined below.

The constraints are as follows:

1. All loci must lie within a spherical nucleus centered on the origin. Electron microscopy experiments show that the nucleus roughly resembles a sphere, with the radius depending on the stage of the organism. In this work, we use a nuclear radius of $r = 350$ nm for the ring stage, $r = 850$ nm for the trophozoite stage, and $r = 425$ nm for the schizont stage (Bannister et al. 2005; Weiner et al. 2011).
2. Two adjacent loci must not be too far apart. A total of 1000 bp of chromatin occupies a distance between 6.6–9.1 nm (Berger et al. 2008). Because we use 10-kb resolution, we set $b_{ij}^{\text{max}} = 91$ nm.

**Initialization**

We create a population of 100 independently optimized structures by initializing $X$ randomly from a standard normal distribution.

**Measuring similarities between structures**

To compare pairs of structures $(X, Y)$ we used the standard RMSD measure:
we first created an intermediate function distribution. That yields a chromatin density as close as possible to a uniform chromatin should also occupy the center of the nucleus, we ran the abut the nuclear envelope (Weiner et al. 2011). Assuming the Tures is the average difference of their pairwise distance difference’’:

\[ \text{distance difference} = \frac{1}{n(n-1)/2} \sum_{i<j} |d^X_{ij} - d^Y_{ij}|, \]

where \( d^X \) and \( d^Y \) are the Euclidean distance matrices of the structures \( X \) and \( Y \).

**Clustering the population of structures**

In order to see whether the structures fall into discrete groups, we computed the RMSD between pairs of structures and performed hierarchical clustering on the resulting 100 \( \times \) 100 distance matrix for each stage (Supplemental Fig. 5).

**Choosing the parameter \( \beta \)**

As noted above, the parameter \( \beta \) controls the scaling of the inferred 3D structure. A small value of \( \beta \) will yield a structure with a very dense center, and a large value of \( \beta \) will push all beads against the nuclear envelope. The literature suggests that chromatin should abut the nuclear envelope (Weiner et al. 2011). Assuming the chromatin should also occupy the center of the nucleus, we ran the entire optimization multiple times, and we selected a value of \( \beta \) that yields a chromatin density as close as possible to a uniform distribution.

This procedure required that we estimate the density of chromatin at a distance \( \ell \) from the center of the nucleus. To do so, we first created an intermediate function

\[ f(\ell) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left( \frac{-\ell^2}{2\sigma^2} \right), \]

where \( g(\cdot) \) is a Gaussian (\( \mu = 0, \sigma = 10 \) nm). The standard deviation \( \sigma \) of the Gaussian corresponds to the uncertainty of the position of each bead. The estimated density \( D(\ell) \) was then computed as a generalized histogram, using discretized distance bins \( \ell_i \). To ensure that the volume was constant for each bin, the bin spacings were defined as \( \ell_i = \sqrt{\frac{\ell_{i+1}^2 - \ell_i^2}{2}} \), where we chose \( \ell_1 = \frac{\ell}{4} \). We then normalized the histogram to sum to one.

Let \( D_i \) be the density of bin \( i \) and let \( n_{\text{bins}} \) be the number of bins. To select \( \beta \), we defined the scoring function

\[ \text{score} = \frac{\sum_{i=1}^{n_{\text{bins}}} \left(D_i - \frac{1}{n_{\text{bins}}}\right)^2}{\sum_{i=1}^{n_{\text{bins}}} \left(D_i - \frac{1}{n_{\text{bins}}}\right)^2}, \]

which corresponds to the mean squared error between the estimated density and the expected density. The resulting density scores are shown in Supplemental Table 13, with the minimal value for each stage in boldface.

**Eigenvalue decomposition and chromatin compartments**

To identify chromatin compartments, for each stage, we carried out eigenvalue decomposition on the matrix of Euclidean distances between locus pairs. For each chromosome we used the intrachromosomal 3D distance matrix at a resolution of 10 kb, where each 10-kb locus is represented by the 3D coordinate of its midpoint. We then calculated the Spearman correlation between each pair of rows of the 3D distance matrix and applied eigenvalue decomposition (using the eig function in MATLAB) to this correlation matrix. The sign of the first eigenvector defined a compartment assignment for each 10-kb locus at each stage. We also aggregated all three stages and calculated a set of aggregate compartments (Supplemental Fig. 3, fourth row of figures on each page) which divided each chromosome into three main compartments (i.e., telomeric-centromeric-telomeric or left[L]-mid[M]-right[R]).

**Kernel canonical correlation analysis**

We used an approach based on kernel canonical correlation analysis (KCCA) (Bach and Jordan 2002; Vert and Kanehisa 2003a,b) to extract gene expression profiles that simultaneously capture the variance of the gene expression data and exhibit coherence with respect to the 3D structure.

Let \( \mathcal{G} \) be the set of \( n \) genes. Each gene \( g \in \mathcal{G} \) is characterized by its log expression profile \( e(g) = [e_1(g), \ldots, e_p(g)] \in \mathbb{R}^p \) at \( p \) timepoints and by its position \( x(g) \in \mathbb{R}^3 \) in 3D space. We assume that the set of gene expression profiles is centered and univariate scaled, i.e., \( \sum_{g \in \mathcal{G}} e_i(g) = 0 \) and

\[ \frac{1}{|\mathcal{G}|} \sum_{g \in \mathcal{G}} e_i(g)^2 = 1 \]

for \( i = 1, \ldots, p \).

Let \( v \in \mathbb{R}^p \) be a direction in the expression profile space. To assess whether \( v \) is representative of the observed expression profiles, we computed the percentage of variance explained among the gene expression profiles once they are projected onto \( v \), defined by

\[ V(v) = \frac{\sum_{g \in \mathcal{G}} (v^T e_i(g))^2}{\|v\|^2}. \]

The larger \( V(v) \) is, the more \( v \) explains the differences between gene expression profiles, and the more likely \( v \) is to correspond to some biological event which influences the expression of many genes. \( V(v) \) is, for example, maximized by principal component analysis.

Instead of just asking the profile \( v \) to capture variance among gene expression, we simultaneously asked it to exhibit coherence with respect to the 3D structure. For that purpose, we defined for every \( f \in \mathbb{R}^3 \) a function \( S(f) \) that quantifies how smoothly \( v \) varies in 3D. \( f \) can be thought of as a vector of scores, one score being assigned to each gene. Because we know the 3D coordinates of each gene we can imagine \( f \) as a set of scores in 3D. Following a standard approach in kernel methods (Schölkopf and Smola 2002), we quantified the smoothness of \( f \) with the function

\[ S(f) = \int K_{3D}^{-1} f \|f\|^2, \]

where \( K_{3D} \) is the \( n \times n \) matrix whose \((i, j)\) entry is the Gaussian kernel between genes \( i \) and \( j \), namely, \( \exp[-\|x(i) - x(j)\|^2/2\sigma^2] \). The smaller \( S(f) \) is, the more smoothly \( f \) is distributed in 3D.

We then combined the ideas of capturing variance (Equation 6) and being smooth in 3D (Equation 7) by designing a joint objective function over \( v \) and \( f \) to ensure that (1) \( v \) captures a lot of variance, (2) \( f \) is smooth in 3D, and (3) \( f \) is maximally correlated with the vector \( [v^T e_i(g)]_{g \in \mathcal{G}} \). In other words, we aimed to ensure that genes that are positively correlated with \( v \) (and those which are negatively correlated) tend to be colocализed in 3D. We designed the function by following the approach of Bach and Jordan (2002),
who show that \( v \) and \( f \) can be found by solving a KCCA problem equivalent to the following generalized eigenvalue problem:

\[
\begin{pmatrix}
0 & K_{ij}K_{ij} \\
K_{ij} & 0
\end{pmatrix}
\begin{pmatrix}
\alpha \\
\beta
\end{pmatrix}
= \rho
\begin{pmatrix}
(K_{ij} + \delta)^2 & 0 \\
0 & (K_{ij} + \delta)^2
\end{pmatrix}
\begin{pmatrix}
\alpha \\
\beta
\end{pmatrix}.
\]

where \( K_{ij} \) is the \( n \times n \) matrix whose \((i,j)\)-th entry is \( e(i)^T e(j)\), and \( \delta \) is a small regularization parameter. Once we found the generalized eigenvectors \((\alpha, \beta)\), ranked by decreasing eigenvalue \( \rho \), we recovered a pair \((v, f)\) by \( v = \sum_{i} \alpha_i e(i) \) and \( f = K_{ij}\beta \).

We computed the profiles for several values of \( \sigma \) (0.01, 0.02, 0.05, 0.1) and \( \delta \) (0.01, 0.02, 0.04, 0.06) and obtained highly correlated results (correlation >0.99 for all pairs of profiles). Therefore, we chose \( \sigma = 0.01 \) and \( \delta = 0.02 \) for the rest of the analysis.

**Gene set enrichment analysis**

To detect set of genes highly or poorly correlated KCCA profiles, we apply gene set enrichment analysis (GSEA) (Subramanian et al. 2005). Unlike a traditional GO term enrichment analysis, this method takes as input a ranked list of genes rather than a set of genes; hence, GSEA takes full advantage of the results of the KCCA. The procedure detects sets of genes enriched at the top or at the bottom of the ranked list of genes. We applied GSEA to the ranked list of projections of expression profiles on the first and second extracted profile. Corresponding \( P \)-values were computed using 4000 permmutations. We also used GSEA in our comparison gene sets that are involved in contacts that are specific to either one stage or two out of three stages.

**Volume exclusion model**

Following the methodology of Tjong et al. (2012), we constructed a population of three-dimensional structures by modeling chromosomes as random configurations subject to the following constraints:

1. Each chromosome is modeled as a series of \( N \) beads spaced 3.2-kb apart, with consecutive beads restrained to be 30-nm apart.
2. Overlaps between beads are prevented by imposing a volume exclusion constraint for all pairs of beads.
3. All chromosomes lie within a spherical nucleus of a specified radius.
4. All centromeres are colocalized in a small sphere of radius 50 nm abutting the nuclear envelope.
5. All telomeres are located within 50 nm of the nuclear envelope.

We formulated an optimization problem that includes, in addition to the constraints, a penalty term that accounts for chromatin stiffness by placing an angular restraint between three consecutive beads:

\[
\frac{1}{2} k_{\text{angle}} \sum_{i=1}^{N} \left( 1 - \frac{x_{i+1} - x_i}{||x_{i+1} - x_i||} \cdot \frac{x_{i+2} - x_{i+1}}{||x_{i+2} - x_{i+1}||} \right)^2,
\]

where \( x_i \in \mathbb{R}^3 \) is the coordinate vector of bead \( i \). We used the Integrated Modeling Platform (IMP) (Bau et al. 2011) to generate 5000 budding yeast structures with a nuclear radius of 1000 nm and 5000 Plasmodium falciparum structures for each of the three stages with nuclear radii of 350, 850, and 425 nm, respectively.

Following Tjong et al. (2012), we used the population of structures to generate a volume exclusion (VE) contact frequency matrix \( C_{\text{VE}} \), considering that two beads are in contact when they are ≤45-nm apart. The contact frequency matrix was then aggregated to a resolution of 32 kb and normalized following the ICE procedure as described above, resulting in a contact frequency matrix \( c_{ij}^{\text{VE}} \) for \( i, j = 1, \ldots, N \) according to the VE model.

In order to compare the VE contact matrix to experimental Hi-C data, we similarly computed the Hi-C contact count matrix at a resolution of 3.2 kb, aggregated it at 32 kb, and normalized the same way as the VE contact frequency matrix to get a Hi-C contact matrix \( c_{ij}^{\text{HiC}} \), for \( i, j = 1, \ldots, N \).

We then compared both matrices by computing the row-based Pearson correlation (Tjong et al. 2012) defined as the average Pearson correlation between their rows.

\[
1 \frac{\sum_{i<j} N_{ij}^{\text{HiC}} c_{ij}^{\text{HiC}} - \left( \sum_{i<j} N_{ij}^{\text{HiC}} c_{ij}^{\text{HiC}} \right) \left( \sum_{i<j} N_{ij}^{\text{HiC}} c_{ij}^{\text{HiC}} \right)}{\sqrt{\sum_{i<j} N_{ij}^{\text{HiC}} c_{ij}^{\text{HiC}} - \left( \sum_{i<j} N_{ij}^{\text{HiC}} c_{ij}^{\text{HiC}} \right)^2} \sqrt{\sum_{i<j} N_{ij}^{\text{HiC}} c_{ij}^{\text{HiC}} - \left( \sum_{i<j} N_{ij}^{\text{HiC}} c_{ij}^{\text{HiC}} \right)^2}}.
\]

Furthermore, we also computed a “normalized” row-based Pearson correlation between the matrices by replacing the counts \( c_{ij}^{\text{HiC}} \) and \( c_{ij}^{\text{VE}} \) in Equation 9 by their ratio to an expected count \( c_{ij}^{\text{E}} \) that we would expect if there was no structural information in the matrix, besides the obvious decrease of contacts between loci at increasing genomic distance. To estimate the expected frequencies \( c_{ij}^{\text{E}} \) used to define the ratios, we fit an isotonic regression to the mapping between genomic distance and the average contact frequency at this genomic distance. The isotonic regression allows us to fit a non-increasing mapping between genomic distance and contact frequency, thus correcting the effect of enrichment of contact frequencies at chromosome ends. This mapping allowed us to define \( c_{ij}^{\text{E}} \) as the expected count corresponding to the genomic distance between loci \( i \) and \( j \) in the case of intrachromosomal contacts, and to the genome-wide average of interchromosomal contacts in case of interchromosomal contacts.

**Data access**

The sequences and processed data files have been submitted to the NCBI Gene Expression Omnibus (GEO; http://www.ncbi.nlm.nih.gov/geo/) under accession number GSE50199. Additional supplementary data is available in the Supplemental Material and at http://noble.gs.washington.edu/proj/plasmo3d.

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procedures. F.A. and N.V. analyzed the data under the supervision of W.S.N. and J.V. F.A. E.M.B., N.V., W.S.N., and K.G.L.R. wrote the manuscript. All authors discussed and edited the manuscript.

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Plasmodium falciparum genome


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