

UC San Diego

UC San Diego Previously Published Works

Title

Transient evaluation of a soil-borehole thermal energy storage system

Permalink

<https://escholarship.org/uc/item/4f99w06n>

Authors

Başer, Tuğçe
McCartney, John S

Publication Date

2020-03-01

DOI

10.1016/j.renene.2018.11.012

Peer reviewed

Energy

Elsevier Editorial System(tm) for Renewable

Manuscript Draft

Manuscript Number: RENE-D-18-02585R1

Title: TRANSIENT EVALUATION OF A SOIL-BOREHOLE THERMAL ENERGY STORAGE SYSTEM

Article Type: SI:Shallow Geothermal Energy

Keywords: Shallow geothermal energy; heat storage; unsaturated soil; solar thermal energy

Corresponding Author: Professor John S McCartney, PhD

Corresponding Author's Institution: University of California San Diego

First Author: Tugce Baser, PhD

Order of Authors: Tugce Baser, PhD; John S McCartney, PhD

Manuscript Region of Origin: USA

Highlights

- The ground temperatures in a field-scale soil-borehole thermal energy storage system were simulated under the boundary conditions associated with heat collection from solar thermal panels.
- A numerical model for coupled heat transfer and water flow considering enhanced vapor diffusion and phase change was calibrated using reconstituted specimens and validated against the measured field temperature data for heating and ambient cooling periods.
- The transient temperature measurements and simulation results indicate the positive aspects of installing thermal energy storage systems in unsaturated soils in the vadose zone.
- The simulation results indicate that a permanent decrease in the degree of saturation near the heat exchangers may have occurred. However, the zone of influence was not significant enough to have an overlapping effect between the heat exchangers for the conditions considered in this study.
- The decrease in degree of saturation led to a decrease in thermal conductivity and volumetric heat capacity near the heat exchangers that may lead to different transient responses upon subsequent heat injection events.

1 **TRANSIENT EVALUATION OF A SOIL-BOREHOLE THERMAL ENERGY STORAGE SYSTEM**

2 by Tuğçe Başer, Ph.D.¹ and John S. McCartney, Ph.D., P.E.²

3 **ABSTRACT:** This study focuses on the simulation of transient ground temperatures in a field-
4 scale soil-borehole thermal energy storage (SBTES) system in San Diego, California. The SBTES
5 system consists of an array of thirteen 15 m-deep borehole heat exchangers installed in
6 conglomerate bedrock at a spacing of approximately 1.5 m. Heat collected from solar thermal
7 panels was injected into the SBTES system over a 4-month period, after which the subsurface
8 was monitored during a 5-month ambient cooling period. The SBTES system is located in the
9 vadose zone above the water table with relatively dry subsurface conditions, so a coupled heat
10 transfer and water flow model was used to simulate the ground response using thermo-
11 hydraulic constitutive relationships and parameters governing vapor diffusion and water phase
12 change calibrated using soil collected from the site. The simulated ground temperatures from
13 the model match well with measurements from thermistors installed at different radial
14 locations and depths in the SBTES system and are greater than those simulated using a
15 conduction-only model for saturated conditions. Significant overlap between the effects of the
16 borehole heat exchangers was observed in terms of the ground temperature. Although the
17 numerical simulations indicate that permanent decreases in degree of saturation and thermal
18 conductivity occurred at the borehole heat exchanger locations, the zone of influence of these
19 changes was relatively small **for the particular site conditions.**

20 **KEYWORDS:** Thermal energy storage; Field-scale testing; Vertical boreholes; Unsaturated soil

¹ Assistant Professor, University of Illinois at Urbana-Champaign, Department of Civil and Environmental Engineering, 205 N. Mathews, Urbana, IL 61801; e-mail: tbaser@illinois.edu.

² Professor and Department Chair, University of California San Diego, Dept. of Structural Engineering, 9500 Gilman Dr., La Jolla, CA 92093-0085, mccartney@ucsd.edu.

21 **1. INTRODUCTION**

22 Soil-borehole thermal energy storage (SBTES) systems are used for storing heat
23 collected from renewable sources in the subsurface so that it can be used later for space or
24 water heating. Heat sources such as solar thermal panels generate heat during the day with a
25 greater energy generation during summer months, so SBTES systems permit storage of the
26 abundant and free thermal resource (Sibbitt et al. 2012, McCartney et al. 2013). SBTES systems
27 function similarly to geothermal heat exchange systems, where a carrier fluid is circulated
28 through a closed-loop pipe network installed in vertical boreholes backfilled with sand-
29 bentonite. Different from boreholes in conventional geothermal heat exchange systems, the
30 boreholes in SBTES systems are spaced relatively close together (1-2 m) in an array to
31 concentrate heat in the subsurface (Claesson and Hellström 1981). SBTES systems are a
32 convenient alternative to other energy storage systems as they are relatively inexpensive,
33 involve storage of renewable energy (solar thermal energy), and are space efficient as they are
34 underground (Başer and McCartney 2015a).

35 Despite the successful use of SBTES systems in community-scale applications (Sibbitt et
36 al. 2012; Nussbicker-Lux 2012; Bjoern 2013), there are still opportunities for engineers to
37 improve the performance of SBTES systems by considering the role of the hydrogeological
38 setting in the subsurface. A goal of this study is to understand the benefits of installing SBTES
39 systems in the vadose zone, the layer of unsaturated soil or rock near the ground surface that
40 may extend to depths greater than 10 meters in some locations. The unsaturated porous
41 material in the vadose zone has a lower thermal conductivity than when saturated, limiting the
42 transient spreading of heat away the subsurface heat storage system (Choi et al. 2011). The

43 volumetric heat capacity of soils in unsaturated conditions is lower than in saturated conditions
44 but is still greater than in dry conditions. For example, the volumetric heat capacity of a silty soil
45 is 2.5 MJ/m³K for saturated conditions, 2.0 MJ/m³K for a degree of saturation of 0.5, and 1.2
46 MJ/m³K for dry conditions (Baser et al. 2016d). One challenge is that the modes of heat transfer
47 in unsaturated porous materials are more complex than when dry or water-saturated.
48 Specifically, in addition to coupling between the thermal and hydraulic properties of
49 unsaturated soils and the effects of temperature on fluid properties (e.g., Lu and Dong 2015),
50 the modes of heat transfer in unsaturated soils include a combination of conduction,
51 convection due to the flow of pore water in liquid and vapor forms under thermal and hydraulic
52 gradients, and latent heat transfer due to phase change. Several studies have developed
53 models to capture these different mechanisms of coupled heat transfer and water flow in
54 unsaturated soils, and have applied them to problems associated with radioactive waste
55 repositories (e.g., Ewen and Thomas 1989; Thomas and Sansom 1995; Gens et al. 1998; Gens et
56 al. 2009), soil-atmosphere interaction (Smits et al. 2011), energy piles (Akrouch et al. 2016), and
57 borehole geothermal heat exchangers (Başer et al. 2018). Başer et al. (2018) found that the
58 zone of influence of temperature changes in silt around a heat exchanger were greater for
59 unsaturated conditions when considering the impact of vapor phase convection. Previous
60 simulations of geothermal heat exchangers in unsaturated soil used conduction alone with a
61 thermal conductivity that varies with the initial degree of saturation (e.g., Choi et al. 2011), but
62 Başer et al. (2018) found that thermally-induced water flow may lead to significant differences
63 in the thermo-hydraulic response of the subsurface.

64 This paper presents a comparison of transient changes in ground temperatures
65 measured in a field-scale SBTES system installed in the vadose zone in San Diego, California with
66 those predicted from a numerical model for coupled heat transfer and water flow. The testing
67 program involved a 4-month period where heat collected from solar thermal panels was
68 injected into the borehole array, followed by a 5-month ambient cooling period. Heat transfer
69 rates into the subsurface measured in the field-scale SBTES system were used to define the
70 dynamic boundary conditions for heat injection in the model, considering the effects of
71 fluctuations in surface air temperature. Although the primary variable from the comparison is
72 the ground temperature, the numerical model also permits evaluation of the effects of thermo-
73 hydraulic interaction between the closely-spaced boreholes in the SBTES system on the degree
74 of saturation. This is important as changes in the degree of saturation **due to thermally-induced**
75 **water flow** may lead to associated changes in the subsurface thermo-hydraulic properties of
76 unsaturated soils.

77 **2. BACKGROUND**

78 Since the concept of borehole thermal energy storage systems was introduced by
79 Claesson and Hellström (1981), several SBTES systems have been installed in Canada and
80 Europe as part of district-scale heat distribution systems. The Drake Landing SBTES system in
81 Okotoks, Alberta, Canada supplies heat from solar thermal panels installed on garage roofs to
82 an array of 144 boreholes in a 35 m-deep, 35-m wide grid (Sibbitt et al. 2012), which is then
83 used to supply approximately 90% of the heat demand of 52 homes. Catolico et al. (2016)
84 simulated the response of the Drake Landing SBTES system, which lies in water-saturated sand
85 deposits overlying glacial till, using a numerical model in TOUGH2 using time-dependent

86 injection fluid temperatures measured at the site over six years of operation as the main
87 boundary condition. Over each year of operation, lateral heat transfer from the borehole array
88 to the surrounding ground was found to decrease due to a reduction in the thermal gradient
89 between the center of the array and the surrounding subsurface, meaning that more thermal
90 energy was concentrated in the center of the array. They found that the annual efficiency of
91 heat extraction (heat extracted divided by heat injected) increases over time, approaching a
92 value of 55%. However, the efficiency of heat recovery was found not to be a good
93 quantification of the SBTES performance because if the demand for heat in a given winter is
94 lower the the efficiency will decrease. Instead, it may be better to evaluate the fractions of heat
95 injected, stored, and lost. For example, in the 6th year of operation, 31.5% of the heat injected
96 into the system was recovered, 21.9% of the heat injected remained in the borehole array, and
97 46.7% of the heat injected escaped the borehole array. Despite the seemingly high fraction of
98 heat loss, the heat stored and recovered was sufficient to provide more than 90% of the
99 community's annual heating demands. Another successful SBTES system was installed in 2007 is
100 in Braedstrup, Denmark (Bjoern 2013). This system supplies heat from 18,000 m² of solar
101 thermal panels to an array of 50 boreholes having a depth of 47 to 50 m installed across a 15 m-
102 wide area. This system provides 20% of the heat to 14,000 homes. Another commercial-scale
103 SBTES was installed in 2008 in Crailsheim, Germany involving of a series of 55 m-deep
104 boreholes that formed a 39,000 m³ subsurface storage volume. This system stores heat from
105 7410 m² of flat plate solar thermal collectors to provide heat for a school and 230 dwellings
106 (Nussbicker-Lux 2012).

107 Although the experience from the commercial-scale systems at Drake Landing,
108 Braedstrup and Crailsheim indicates that SBTES systems are functional and are sufficiently
109 efficient to provide heating to different sizes of communities, simulation studies such as that of
110 Catolico et al. (2016) indicate that the hydrogeological setting is critical for optimizing the
111 thermal energy storage. Although the Drake Landing SBTES system includes instrumentation to
112 evaluate changes in ground temperature within the array (Sibbitt et al. 2012), it is in use for
113 commercial purposes, so the heat injection patterns cannot be varied as part of scientific
114 studies on the performance of SBTES systems. Accordingly, it is advantageous to install smaller
115 SBTES systems for demonstration projects in different hydrogeological settings to understand
116 the roles of different heat transfer processes and heat injection patterns on SBTES system
117 performance. For example, Başer et al. (2016a) reported the ground temperatures monitored
118 during a 75-day heat injection experiment into a small-scale SBTES system in Golden, CO, USA
119 involving an array of 5 borehole heat exchangers. Although the SBTES system in that study was
120 installed in an unsaturated silty soil layer, observations during installation indicate that the
121 bottom 10% of the heat exchanger lengths were in a saturated sand aquifer underlying the site.
122 Transient temperature measurements indicated that a substantial portion of the injected heat
123 left the array due to lateral heat loss associated with both the higher thermal conductivity of
124 the saturated sand layer and possible convection effects associated with groundwater flow in
125 this sand layer. Further, the simulations of Başer and McCartney (2015b) indicate that arrays
126 should have a greater number of boreholes than those considered by Başer et al. (2016a) to
127 effectively concentrate heat in the subsurface.

128 Although simplified design models for SBTES systems have been developed (e.g.,
129 Claesson and Hellström 1981), modeling the transient heat transfer in SBTES systems can be
130 complex because of the dimensions of the problem, the geometry and structure of the
131 borehole network, the process of heat transfer into the ground via circulating fluids in closed-
132 loop pipe networks, and the nonlinear variations in the thermal and hydraulic properties of
133 unsaturated soils with degree of saturation. Marcotte and Pasquier (2014) investigated the
134 effect of the borehole arrangement both analytically and numerically on the thermal response
135 of a heat storage system for the cases in which boreholes are connected in series, parallel, and
136 mixed configurations. They reported significantly lower inlet fluid temperatures for the parallel
137 configuration than for the series configuration, indicating a larger heat transfer to the ground
138 for this arrangement compared to the series configuration. Besides the geometrical
139 configuration of the borehole heat exchangers and the fluid circulation configuration (series,
140 parallel, mixed), there are other factors that affect the thermal response of a storage system,
141 such as the subsurface temperature profile and ambient air temperature, degree of saturation
142 profile of soil and the thermal properties. Thomas and Rees (2009) investigated the effect of
143 water content on heat transfer through unsaturated soils via a series of one and two-
144 dimensional numerical simulations that consider only conduction as the major heat transfer
145 mechanism. They reported 60% and 20% increases in heat flux with increasing water content
146 for one- and two-dimensional models, respectively. Akrouch et al. (2016) proposed an
147 analytical solution based on cylindrical heat source theory that accounts for variable degree of
148 saturation on the heat exchange between the heat source and sand soil and the results
149 indicated a 40% drop in performance of a heat exchanger when the degree of saturation is

150 close to residual conditions. Welsch et al. (2015) studied the impact of borehole length,
151 borehole, spacing, number of boreholes, and the inlet heat transfer fluid temperatures on the
152 behavior of thermal energy storage in crystalline rock. They observed that there was an optimal
153 spacing to reach the highest efficiency of heat recovery, with higher and lower values leading to
154 lower efficiencies. Due to the high thermal conductivity of the crystalline rock, the optimal
155 borehole heat exchanger spacing was 5 m, which is greater than that observed in similar studies
156 the focus on lower thermal conductivity soils (e.g., Baser and McCartney 2015a). Welsch et al.
157 (2015) found that the number of boreholes has a positive influence on the efficiency of heat
158 recovery because the increasing ratio of the storage volume to the size of the boundary of the
159 storage volume results in lower heat losses to the surrounding subsurface outside of the array.

160 Başer and McCartney (2015a) used a conduction-only model to understand the impacts
161 of borehole array geometry, ground properties, heat injection magnitudes, and heat injection
162 duration on the temperature distribution in the SBTES system. Başer et al. (2016b) and Başer et
163 al. (2016c) used a coupled heat transfer and water flow model without considering vapor
164 diffusion or phase change to understand the roles of incorporating a thermal insulation layer
165 and the effect of different unsaturated soil properties on the ground temperatures in SBTES
166 systems, respectively. These studies found that a surface insulation layer does not play a
167 significant role on the thermal energy storage due to the small area around each borehole heat
168 exchanger, but that surface temperature fluctuations should still be considered on the ground
169 temperatures. Bidarmaghz et al. (2016) investigated the effect of surface air temperature
170 changes on the thermal response of geothermal heat exchangers in the shallow subsurface and
171 found that considering ambient air temperatures in the simulations increased the total heat

172 exchanger length by 11%. A similar study by Nguyen et al. (2017) showed that seasonal
173 temperature variation of the subsurface increases the outlet fluid temperature causing a
174 decrease in the heat transfer rate into the ground. Further, they found that burying boreholes
175 at the certain depth from the surface (1-2 m) is not sufficient to hinder the ambient air
176 temperature effects on the ground temperature near the surface. Baser et al. (2017) used a
177 coupled heat transfer and water flow model considering vapor diffusion and phase change to
178 study the response of a single vertical borehole heat exchanger during a heat injection period
179 followed by a, ambient cooling periods. They evaluated the role of different heat transfer
180 mechanisms and observed a permanent drying around the heat exchanger during heat injection
181 that was not recovered during ambient cooling. This drying led to a decrease in thermal
182 conductivity that corresponded to a reduction in the amount of heat loss from the soil near the
183 heat exchanger.

184 **3. NUMERICAL MODEL**

185 **3.1. Model Formulation**

186 This study applies the model for geothermal heat exchangers in unsaturated soils used
187 by Baser et al. (2018), which was originally developed by Smits et al. (2011) and enhanced by
188 Moradi et al. (2016), to simulate the behavior of a field-scale SBTES system installed in San
189 Diego, California. The governing equations for the model are summarized in Table 1, while the
190 key thermo-hydraulic constitutive relationships are summarized in Table 2. Coupling occurs
191 between the different equations in Table 1 due to the effects of temperature on the different
192 fluid properties, which are summarized by Smits et al. (2011) and Baser et al. (2018). Simulation
193 of coupled heat transfer and water flow in unsaturated soils requires simultaneous solution of

194 the governing equations for two-phase flow (Equations 1 and 2) along with the heat transfer
195 based on energy balance (Equation 6). Because liquid and vapor phases are present in
196 unsaturated soils, flow induced by thermal gradients in both liquid and total gas phases are
197 considered and formulated as the convection terms in the energy balance equation (i.e., the
198 second and the third terms in Equation 6). When formulating the model, some assumptions are
199 made: (a) soil framework is homogeneous, isotropic, and non-deformable; (b) fluid phases are
200 immiscible; (c) hysteresis in the constitutive relationships is not considered. The model
201 considers enhanced vapor diffusion described by Equation (4) and a nonequilibrium phase
202 change rate described by Equation (5) that are incorporated into the water vapor mass balance
203 equation in Equation (3) and as source terms in the governing equations for two-phase flow
204 and the heat transfer energy balance. The model was implemented into the finite element-
205 based software COMSOL Multiphysics® version 5.2a (COMSOL 2015) which solved the
206 governing equations for the four primary unknowns: pore water pressure, total pore gas
207 pressure, water vapor concentration, and temperature.

208 **3.2. Model Calibration**

209 The key parameters that must be defined to calibrate the numerical model are the
210 parameters of the thermo-hydraulic constitutive relationships given in Table 2 and the
211 parameters a and b from Table 1 that govern the soil-specific enhanced vapor diffusion rate
212 and the nonequilibrium phase change rate, respectively. The methodology described in this
213 section for parameter calibration was applied to the subsurface in the SBTES array evaluated in
214 this study but could also be applied to design SBTES systems in the vadose zone in other
215 locations.

216 The SBTES system constructed as part of this study was installed in an unsaturated
217 conglomerate bedrock layer at the Englekirk Structural Engineering Center (ESEC) of the
218 University of California San Diego. A site investigation from 2003 indicates approximately 1m of
219 sandy soil overlying the conglomerate bedrock consisting of cemented sand- and gravel-size
220 particles. An undisturbed core of the conglomerate bedrock was not obtained during
221 installation of the SBTES system. However, disturbed cuttings from a hole drilled into the
222 conglomerate using an auger were collected from different depths. Although it is not possible
223 to reconstitute the cuttings into the same cemented structure as the conglomerate, it is
224 assumed that the thermo-hydraulic properties of the conglomerate are predominantly
225 governed by the grain size, mineralogy, and density for the purposes of model calibration so
226 that laboratory calibration of the model parameters is possible. Laboratory calibration permits
227 the use of instrumented specimens under carefully-controlled boundary conditions, but future
228 studies may use inverse analyses from field measurements to consider the role of the
229 cemented structure on the calibrated model parameters. Specimens used to represent the
230 conglomerate properties were reconstituted from cuttings obtained from a depth of 16 m from
231 the surface at the ESEC facility, which were prepared using compaction to a dry density of a
232 1650 kg/m^3 at an initial degree of saturation of 0.49, which corresponds to conditions in the
233 conglomerate measured using sand-cone experiments performed at a depth of 1.5 m from the
234 surface.

235 The thermo-hydraulic constitutive relationships were determined using a modified form
236 of the transient water release and imbibition method (TRIM) of Wayllace and Lu (2012) that
237 included the measurement of the thermal conductivity and volumetric specific heat capacity

238 described by Lu and Dong (2015). Specifically, a specimen was compacted to the conditions
239 mentioned above into a modified Tempe cell that incorporates a dual thermal needle and a
240 dielectric sensor, was saturated with water, then dried monotonically in two stages. The soil
241 water retention curve (SWRC), hydraulic conductivity function (HCF), thermal conductivity
242 function (TCF), and volumetric heat capacity function (VHCF), described by Equations 7
243 through 10 in Table 2, were obtained from inverse analysis of the outflow and thermal property
244 measurements during this drying stage. The SWRC and HCF along with relevant parameters are
245 shown in Figure 1(a), while the TCF and VHCF along with relevant parameters are shown in
246 Figure 1(b). Lu and Dong (2015) presented empirical relationships between the parameters of
247 the thermal constitutive relationships and the hydraulic constitutive relationships, but the
248 properties measured from the experiments in Figure 1 were used in the simulations.

249 The properties governing the vapor diffusion phase change rate and diffusion were
250 calibrated using an evaporation experiment on a reconstituted specimen of the site soil. The
251 soil was compacted in a plastic modified Proctor compaction mold having a diameter of 152
252 mm to a height of 179 mm. The mold, developed by Iezzoni and McCartney (2015), can
253 accommodate a dielectric sensor at mid-height of the soil specimen as shown in the cross-
254 sectional schematic in Figure 2. An evaporation test starting from the initial degree of
255 saturation mentioned above was performed by heating the bottom of the soil layer using a
256 heating pad placed below the mold while leaving the surface of the soil open to the
257 atmosphere. The heating pad applies fluctuating heat pulses to maintain a target temperature.
258 Thus, a thermocouple was placed at the bottom to monitor the applied boundary temperature
259 during heating, which is shown in Figure 3(a). Ambient temperatures were also recorded with a

260 thermocouple so that the ambient air temperatures could be applied as boundary conditions
261 on the outer surfaces of the specimen during the experiment. A temperature of approximately
262 42 °C was maintained over a period of 35 h. The measured values of temperature and degree of
263 saturation at the center of the soil specimen during this period are shown in Figures 3(a) and
264 3(b), respectively. The model of Iezzoni and McCartney (2015) was used to correct the degrees
265 of saturation inferred from the dielectric sensor to account for temperature effects. This
266 calibration test was then simulated using the coupled heat transfer and water flow model, and
267 the parameters a and b in Equations 4 and 5 in Table 1 were varied using a manual parameter
268 sweep to identify the best combination of parameters to match the measured curves. The
269 simulated temperature and degree of saturation curves for $a = 20$ and $b = 2 \times 10^{-7} \text{ s/m}^2$ are
270 shown in Figures 3(a) and 3(b), respectively, which indicate a good match.

271 3.3. Simulation Details for the Field-Scale SBTES System

272 The calibrated model was then used to simulate the response from the field-scale SBTES
273 system demonstration experiment. A plan view of the SBTES system showing the connections
274 between the boreholes in the array, a manifold for control and monitoring of the heat
275 exchanger fluid in the borehole array, a 2400 L water-filled temporary heat storage tank, and a
276 series of solar thermal panels is shown in Figure 4(a). This figure also shows the location a
277 reference borehole for monitoring the undisturbed ground temperature profile. Thirteen of the
278 boreholes in the array include heat exchanger tubing, while four of the boreholes in the array
279 include thermistor strings that monitor the ground temperature. Two of the boreholes include
280 both heat exchangers and thermistor strings. The boreholes were backfilled with sand
281 bentonite after installation of the heat exchangers or thermistor strings. The hexagonal

282 configuration of the borehole array was selected for ease of construction, as the boreholes in
283 the array fall into five co-linear sets that facilitate positioning of the drill rig. The main design
284 variable used to configure the boreholes was the spacing. Baser and McCartney (2015a) found
285 that the borehole spacings should be less than 1.5 m to ensure overlapping effects of the heat
286 exchangers for soil thermal properties and heat transfer rates typical of SBTES systems. The
287 number of boreholes containing heat exchangers was selected so that the boreholes in the
288 array would fall into two annuli, greater than the number in the array tested by Baser et al.
289 (2016a). Although a commercial-scale SBTES system would likely have more heat exchangers in
290 several more annuli (e.g., Sibbitt et al. 2012), this array is still sufficient in scale to investigate
291 the transient heat transfer and heat storage in the subsurface within the array associated with
292 interactions between heat exchangers.

293 An elevation view of the site is shown in Figure 4(b), which highlights the position of the
294 15 m-long boreholes beneath a 1 m-deep excavation. After connection of the heat exchanger
295 tubing following the arrangement shown in Figure 4(a), a thin layer of site soil was placed for
296 leveling-purposes, which was overlain by a hydraulic barrier, an insulation layer, and a
297 compacted layer of site soil. The high-density polyethylene (HDPE) hydraulic barrier has a
298 thickness of 0.01 m and an assumed hydraulic conductivity of 10^{-12} m/s, while the EPS geofom
299 insulation layer has a thickness of 50 mm, a thermal conductivity of 0.03 W/mK, and a specific
300 heat capacity of 0.9 MJ/kgK. The lateral extents of the hydraulic barrier and insulation layer
301 followed the hexagonal boundaries of the array shown in Figure 4(a). Pictures of the SBTES
302 system are shown in Figure 5, highlighting the 1 m-deep excavation and connection of the
303 borehole heat exchangers in Figure 5(a), the hydraulic barrier in Figure 5(b), the insulation layer

304 in Figure 5(c), and the completed set of solar thermal panels and temporary heat storage tank
305 in Figure 5(d).

306 As the hexagonal borehole array is symmetrical, a quarter section was simulated as
307 shown in Figure 6. The temperatures on either side of the two planes of symmetry are assumed
308 to be identical. This simulation strategy was also used by Catolico et al. (2016) to reduce
309 computation times when simulating symmetrical SBTES systems. Figure 6 also includes the
310 labels used to name the thirteen boreholes that include heat exchangers (boreholes A through
311 M) and the four boreholes that include thermistor strings (T-1 to T-4). As will be described
312 below, appropriate fractions of the heat transfer from boreholes A (1/4 of its heat transfer), B
313 (1/2 of its heat transfer) and E (1/2 of its heat transfer) are applied as boundary conditions. The
314 model domain is 15 m x 15 m in plan and has a depth of 20 m and includes 5 borehole heat
315 exchangers. The size of the domain was selected such that the heat exchangers would not
316 affect the temperatures at the boundaries for the heat injection period under investigation.
317 This was confirmed by ensuring that the temperature at the boundaries of the array remained
318 similar to the temperatures from the reference borehole at different depths. The domain was
319 discretized using 756,667 elements with finer discretization around the boreholes. Triangular
320 elements were used on the surfaces of boreholes and insulation layer, and tetrahedral
321 elements were used for the rest of the domain. A maximum element growth rate of 1.4 and a
322 curvature factor of 0.25 were used in discretization in COMSOL.

323 The isometric views of the model domain shown in Figures 7(a) and 7(b) highlight the
324 thermal and hydraulic boundary and initial conditions, respectively. The initial temperature
325 profile was obtained from the ground temperature distribution measured by the reference

326 borehole at the initiation of the heat injection period on April 29th, 2016. To define the initial
327 degree of saturation profile, hydrostatic conditions were assumed. Although the water table
328 was not encountered in the previous geotechnical site investigation which was performed in
329 2003, the San Diego County Water Authority reported that the ground water depth ranges in
330 depth from 14 to 24 m in the area and no groundwater flow was recorded. Accordingly, the
331 water table was fixed at a depth of 20 m from the surface (i.e., at the base of the domain)
332 throughout the simulations for simplicity as its actual location during the experiment is
333 unknown. Although the depth of the groundwater table may be greater than 20 m, this choice
334 of boundary condition was selected to limit the size of the domain in the simulations. Based on
335 the hydrostatic profile shown in Figure 7(b), the initial degree of saturation along most of the
336 length of the heat exchangers was approximately 0.22 which corresponds to residual saturation
337 conditions. Near the bottom of the heat exchangers, the initial degree of saturation increases
338 up to 0.49 due to the proximity of the water table.

339 Neumann boundary conditions of zero mass flux and zero heat flux were assigned for
340 the outer lateral boundaries of the domain as well as for the planes of symmetry. Dirichlet
341 boundary conditions for temperature were applied at the bottom and top of the domain. A
342 constant temperature of 21°C was applied at the bottom of the domain, which corresponds to
343 the average measured temperature at the base of the reference borehole. The temperature of
344 the top of the domain was assumed to equal the time-dependent ambient air temperatures
345 that were measured at the site during the duration of the experiment, shown in Figure 8(a).
346 Although the EPS geofoam insulation layer is considered in the simulations, it does not provide
347 a perfect insulation effect so the effects of the ambient air temperature fluctuations on the

348 surface temperature must be considered. It should be noted that the surface ground
349 temperature may differ from the ambient air temperature due to radiative and air convection
350 effects, so the use of the ambient air temperature as a surface boundary condition may be a
351 simplifying assumption. A zero-mass flux boundary condition was applied to the surface
352 boundary. This choice was made to simplify the fluid flow processes in the ground as an
353 infiltration/evaporation boundary condition can be computationally expensive when combined
354 with a coupled heat transfer and water flow model considering vapor diffusion and phase
355 change. However, this assumption is reasonable both due to the relatively low precipitation in
356 San Diego as well as due to the presence of the hydraulic barrier atop the borehole array.
357 However, this boundary condition choice is expected to affect the accurate simulation of the
358 temperature at the location of the reference borehole, as infiltration of water may affect the
359 thermal properties of the surface soil. As mentioned, Dirichlet boundary conditions were
360 assumed for the water table at the base of the domain (pore water pressure equal to zero).

361 Although the heat transfer boundary conditions for geothermal borehole heat
362 exchangers previous simulations of SBTES systems involved control of the inlet fluid
363 temperature and considered convective heat transfer associated with fluid flow through the
364 sequence of borehole heat exchangers in the array (e.g., Welsch et al. 2015; Catolico et al.
365 2016), this study considered the borehole heat exchangers as cylindrical heat sources and
366 applied heat flux values to the outer diameters of the cylinders equal to the measured heat flux
367 values from the site discussed in the next paragraph. The heat transfer boundary conditions
368 associated with fluid flow through heat exchanger pipes were not considered in this study
369 because of long computational times associated with solving the governing equations for

370 coupled heat transfer and water flow processes in the subsurface given in Table 1, which was
371 the primary topic of interest in this study. The simplified heat transfer boundary condition for
372 the borehole heat exchangers still permits validation of the coupled heat transfer and water
373 flow analyses in the subsurface within the array. However, design simulations for SBTES
374 systems require control of the inlet fluid temperature and consideration of convective heat
375 transfer of fluid flow through the heat exchangers as the heat transfer rate will decrease over
376 time as the soil within the array increases in temperature (e.g., Welsch et al. 2015). Another
377 assumption in this study is that a uniform heat flux was applied to each of the heat exchangers
378 based on the measured heat transfer rates in the field. Although the choice of a uniform heat
379 flux along a heat exchanger connected in series through several boreholes may not be suitable
380 when simulating a commercial-scale SBTES system with long overall heat exchanger lengths, the
381 relatively short overall heat exchanger lengths used in this field demonstration project
382 permitted the use of this simplified boundary condition without major discrepancies in
383 matching the measured subsurface temperatures.

384 Eight evacuated tube solar thermal panels having a total area of 33 m² were connected
385 in series to collect heat during the day, which was then transferred to the water in the
386 temporary heat storage tank via a coiled copper tube. A second coiled copper tube in the
387 temporary heat storage tank is used to inject heat into the SBTES system. A second horizontal
388 SBTES system was also installed at the site and was tested at the same time (Baser et al. 2019).
389 Although this horizontal SBTES system is not discussed in this paper, it should be acknowledged
390 as all the heat collected from the solar thermal panels was not injected into the “vertical” SBTES
391 system under evaluation in this study. Nonetheless, the measured heat transfer rate into the

392 subsurface was boundary condition used in the simulations, so the effects of the horizontal
393 SBTES system is not important. Water was used as the heat exchanger fluid in both the solar
394 thermal panels and in the SBTES system as freezing temperatures are not expected in San
395 Diego. The heat transfer rates were calculated as follows:

$$\dot{Q} = \dot{V}_w \rho_w C_w (T_{in} - T_{out}) \quad (11)$$

396 where \dot{V}_w is the measured volumetric flow rate of the heat exchanger fluid (water), ρ_w is the
397 density of water (1000 kg/m³), C_w is the specific heat capacity of water (4183 J/kgK), and T_{in} and
398 T_{out} are the measured temperatures of the water entering and exiting solar thermal panels,
399 respectively. The heat transfer rates for the solar thermal panels over the 120-day period
400 starting on April 29, 2016 are shown in Figure 8(b). The large fluctuations in heat transfer rate
401 observed in this figure occur because heat is only collected during the day. To better
402 understand the transient heat transfer rates from the solar thermal panels and the total heat
403 injected into the vertical SBTES system during 2 days of operation are shown in Figure 8(c). A
404 lag is observed between the heat transfer rates **collected** from the solar thermal panels and
405 **injected into** the vertical SBTES, but the temporary water storage tank provides a buffer to
406 permit heat injection at night as well. A control system has not yet been implemented to ensure
407 that heat is only collected from the solar thermal panels during the day. Specifically, the
408 circulation pumps in the solar thermal panels and SBTES system are operated continuously.
409 Accordingly, fluid is still circulated through the solar panels at night, which may result in a slight
410 extraction of heat from the temporary heat storage system if the outside air is colder than the
411 borehole array. The efficiency of heat transfer in the system can be assessed using the
412 cumulative total energy collected from the solar thermal panels and injected into the vertical

413 and horizontal SBTES systems shown in Figure 8(d). Approximately 80% of the cumulative heat
414 collected from the solar thermal panels is injected into the vertical and horizontal SBTES
415 systems, with the remaining 20% lost due to the circulation of fluid through the solar thermal
416 panels at night. Additional experimental testing is underway to investigate other configurations
417 for flow through the solar thermal panels (series instead of parallel) along with inclusion of a
418 heat transfer fluid control system in the solar thermal panels to increase the efficiency of heat
419 collection from the solar thermal panels and injection into the SBTES systems.

420 As mentioned, the borehole heat exchangers were simulated as cylinder sources having
421 a uniform heat flux with depth with a magnitude that varied according to the measured heat
422 flux interpreted from Equation (11) using the entering and exiting fluid temperatures and fluid
423 flow rates going into the different geothermal loops shown in Figure 4(a). Specifically, the heat
424 exchanger tubing was split into three closed-loop networks of U-tube borehole heat exchangers
425 (referred to as Loops 1, 2, and 3). Each loop is connected to a borehole heat exchanger in the
426 central borehole, which means that the central borehole contains 3 U-tube heat exchangers.
427 Next, the three loops connect to four other borehole heat exchangers in different zones of the
428 array, as shown in the photograph in Figure 9 and the schematic in Figure 4(a). It is expected
429 that the heat exchanger fluid flowing through the loops will be hottest in the center of the
430 array, and the fluid temperature will decrease as it flows through the surrounding four
431 borehole heat exchangers and returns to the manifold. However, as noted above, the relatively
432 short length of the heat exchangers in each loop permits the assumption that the heat flux is
433 the same from each borehole connected to the loop (except for the central borehole which has
434 three times the other boreholes). The use of three loops provides flexibility for changing the

435 heat transfer into different zones of the array, but in this study all three loops had a balanced
436 flow. Specifically, the fluid flow rates in each of the loops were controlled and measured
437 independently to be equal and ensure that heat transfer is balanced into the different zones of
438 the borehole array. The inlet and outlet fluid temperatures for each loop were monitored so
439 that Equation (11) could be applied to obtain the heat transfer rate into the subsurface, which
440 was the main boundary condition applied in the simulations.

441 A challenge encountered when simulating a quarter domain is that boreholes from
442 different loops were included in the domain, and the heat transfer rates in each loop were not
443 the same. Specifically, the borehole heat exchangers that were simulated were A (center
444 borehole, part of loops 1, 2, and 3), B (part of loop 2), C (part of loop 2), and D (part of loop 3), E
445 (part of loop 3) as shown in Figure 9 and Figure 4(a). Further, the heat transfer rates calculated
446 using Equation 11 represent an average heat transfer rate across the five borehole heat
447 exchangers in each loop. Accordingly, some assumptions had to be made regarding the heat
448 transfer rates applied to the different borehole heat exchangers being simulated. Because the
449 different borehole heat exchangers were obtained from different loops, the heat transfer rates
450 for the different borehole heat exchangers were interpreted from the heat transfer rates of
451 Loops 1, 2, and 3 calculated from Equation 11 which are shown in Figure 10. Specifically, the
452 total heat transfer rates from all three loops were first divided by five to represent the heat
453 transfer rate into the five boreholes in the quarter section domain and the transient heat fluxes
454 were applied to each borehole individually depending on its associated loop. The heat transfer
455 rate for the center borehole was equal to the sum of $1/5^{\text{th}}$ of each of the three heat transfer
456 rates, and the heat transfer rates for boreholes B, C, D, and E were equal to $1/5^{\text{th}}$ of the heat

457 transfer rates from the respective loops noted above. Although it is likely that the center
458 borehole A had a higher local heat flux than the outer borehole E it is assumed that the
459 gradients of temperature in the center and edge of the array balanced out over time, so the
460 total heat transfer rate of each loop could be considered as an average of the entire system.

461 The transient heat transfer rates were converted to heat fluxes which were applied to the
462 outside area of each borehole in the quarter section domain. At the end of the heat injection
463 period, the heat flux for each borehole was set to zero to represent the ambient cooling period.
464 Because the coupled heat transfer and water flow processes in the subsurface are relatively
465 slow, a time interval of 1800 s was used in the simulations of the 120-day heat injection period
466 followed by a 155-day ambient cooling period, which was found to lead to sufficiently accurate
467 results when evaluating the changes in ground temperature.

468 **4. COMPARISON OF NUMERICAL RESULTS AND FIELD MEASUREMENTS**

469 A goal of this study is to present the field measurements in a way that the transient heat
470 transfer results at different locations in the borehole array could be understood. Second,
471 because of the simplifying assumptions regarding the subsurface thermo-hydraulic properties
472 (homogeneity and use of reconstituted specimens), the uncertain location of the water table
473 below the heat exchanger array, and the use of a uniform heat flux along the boreholes, it is
474 preferred to show a qualitative comparison between the field measurements and the results
475 from the numerical simulation without a detailed error analysis.

476 As could be expected from the large fluctuations in the heat transfer rate into the
477 geothermal heat exchanger loops due to the variability in the solar thermal heat transfer rate,
478 the temperature at the locations of the borehole heat exchangers are expected to experience

479 significant changes in temperature each day. The temperatures at the center borehole
480 measured using the thermistor string T-1 along with the simulated temperature from the model
481 are shown in Figure 11. The temperature at each depth is shown separately in each sub-figure
482 to differentiate the transient response at the different depths. Although the temperatures at a
483 depth of 16.00 m were underestimated during heating, the temperatures at other depths were
484 captured well by the model. The difference at a depth of 16.00 m may be due to the
485 assumption of the hydrostatic initial conditions based on the assumed location of the water
486 table, which leads to a higher thermal conductivity of the subsurface in the simulations. The
487 differences in the daily fluctuations of each depth occur as the temperatures from the model
488 were obtained in a soil element at the boundary of the heat exchanger, while the measured
489 temperatures are from the thermistor strings inside the borehole and are in contact with the
490 geothermal heat exchanger. The sand-bentonite grout backfill in the boreholes was not
491 considered in the model simulations but may affect the heat transfer process in the field
492 measurements. During the ambient cooling stage, the transient trends appear to be well-
493 captured, although the initial temperature at the start of ambient cooling was occasionally
494 different from that between the measured and simulated values. The two locations closer to
495 the surface show an increase in the rate of cooling on day 210, likely due to the lower ambient
496 air temperatures observed in Figure 8(a).

497 A comparison between the temperatures at the location of thermistor string T-2 shown
498 in Figure 12 indicates less daily fluctuations than at the location of thermistor string T-1. The
499 temperature at the location of thermistor string T-2 depends on overlapping effects of borehole
500 heat exchangers A and B, and heat transfer from these boreholes damps out the daily

501 fluctuations. A good match in the trends and magnitudes at the different depths was observed
502 during both the heat injection and ambient cooling periods, with underestimation of the
503 temperatures at depths of 16.00 m and 1.82 m. The measured temperature values during the
504 heating injection period ranged from 29.5 °C near the bottom of the array to 34.2 °C near the
505 top of the array. The greater increases in measured and simulated temperatures near the
506 surface of the array may be due to greater heat transfer in initially dryer soils due to greater
507 water vapor diffusion and latent heat transfer as well as buoyancy-driven upward movement of
508 water vapor, both of which were observed by Baser et al. (2018) in the simulation of a single
509 geothermal heat exchanger. The measured and simulated temperatures at the location of
510 thermistor string T-3 shown in Figure 13 are similar to those for thermistor string T-1 in Figure
511 11 due to the presence of borehole heat exchanger B, but with lower magnitudes. The lower
512 magnitude is because the heat flux from borehole heat exchanger B was three times smaller
513 than the three loops in borehole heat exchanger A. Finally, the measured and simulated
514 temperatures at the location of thermistor string T-4 shown in Figure 14 show the lowest
515 increases in temperature due to its larger radial location from the center of the borehole array.
516 One of the thermistors at a depth of 12.95m was not functional after installation. Like
517 thermistor string T-2, greater temperatures were noted near the surface.

518 The differences between the simulated and measured ground temperatures could be
519 due to the use of reconstituted specimens to obtain the thermo-hydraulic properties, the
520 possibility that the subsurface does not have homogeneous thermo-hydraulic properties,
521 uncertainty about the actual depth of the groundwater table (which may have affected the
522 initial degree of saturation and thermal properties), and the use of simplified heat exchanger

523 boundary conditions. A general observation regarding the measured and simulated
524 temperature time series is that even though the heat transfer was simulated as an average heat
525 flux at the boundaries of the heat exchangers instead of simulating the heat transfer via
526 circulation of fluid in the borehole loops, a good match with the ground temperatures during
527 both heating and cooling was observed. Although the actual location of the water table was not
528 known a-priori, comparison of the simulation results shown in Figures 11 through 14 at depths
529 near the middle and bottom of the heat exchangers indirectly reflect the importance of the
530 initial degree of saturation on the simulation results from the coupled heat transfer and water
531 flow model. Greater initial degrees of saturation will lead to higher thermal conductivity values
532 and may lead to greater changes in degree of saturation due to enhanced vapor diffusion and
533 latent heat transfer (Baser et al. 2018). The differences in simulated and measured
534 temperatures at the different depths in the soil profile in Figures 11 through 14 could also have
535 been due to variations in subsurface stratigraphy not observed in the installation of the heat
536 exchangers, which would have led to variations in thermo-hydraulic properties with depth.
537 Despite the challenges in validating the numerical model with field data, the numerical model
538 was found to capture the temperature of the subsurface within the array with good accuracy
539 within most of the array.

540 Radial profiles of temperatures at the end of the heat injection period from the
541 numerical model and the field measurements are shown in Figures 15(a) for the depths that
542 thermistors were installed. Temperatures were in good agreement, especially at depths of
543 14.78 and 1.82 m. This figure also includes the ground temperatures from the reference
544 borehole. The shapes of the radial profiles are like those interpreted from the field

545 measurements, although the maximum temperatures at the locations of thermistor strings 1
546 and 3 due to the daily fluctuations in heat transfer rate were not captured as noted in the time
547 series in Figures 11 and 13, respectively. Radial distributions in temperature at the end of the
548 ambient cooling period indicate that some heat (a maximum difference in temperature of 4 °C
549 from the initial value of 21 °C) is still retained within the array after 5 months of ambient
550 cooling. This amount of decrease in temperature due to ambient cooling is expected to
551 decrease if further cycles of heating and cooling were investigated, similar to the observations
552 of Catolico et al. (2016). Temperature profiles at the locations of boreholes 2 and 4 are shown
553 in Figures 16(a) and 16(b), respectively. Both the measured and simulated temperature profiles
554 show an increase in temperature with proximity to the ground surface, likely due to the effects
555 of natural convection. As the pore fluids are heated, their densities decrease causing them to
556 rise and transfer heat upward in the subsurface.

557 **5. ADDITIONAL INSIGHTS FROM MODEL SIMULATIONS**

558 Although it was known that the subsurface at ESEC was unsaturated, and that changes
559 in degree of saturation are expected due to coupled heat transfer and water flow,
560 instrumentation was not incorporated in the subsurface within the borehole array to monitor
561 changes in degree of saturation. This was due to difficulty in installing dielectric sensors into the
562 intact conglomerate through the sides of the boreholes. Installation of these sensors into a soil-
563 bentonite-backfilled borehole would measure the changes in thermo-hydraulic behavior of the
564 backfill, not the conglomerate. Nonetheless, it is still possible to infer the changes in degree of
565 saturation of the subsurface from the numerical simulation results, as well as the effects of
566 these changes on the heat transfer during the heat injection period and heat retention during

567 the ambient cooling period. Time series of the simulated degrees of saturation at the locations
568 of thermistor strings 3 and 2 are shown in Figures 17(a) and 17(b). Due to the boundary
569 conditions associated with borehole heat exchanger B next to thermistor string 3, a steady
570 decrease in degree of saturation was noted during the heat injection period at this location in
571 Figure 17(a). This decrease in degree of saturation is expected due to enhanced vapor diffusion
572 from relatively hot regions to colder regions. During the ambient cooling stage, the degree of
573 saturation at the location of thermistor string T-3 was not observed to recover. A similar
574 observation was made by Baser et al. (2018) for a single borehole heat exchanger in compacted
575 silt that had different thermo-hydraulic properties. The main effect of this decrease in degree of
576 saturation is that the decrease in temperature at this location during ambient cooling should be
577 slower due to the lower thermal conductivity associated with the permanent decrease in
578 degree of saturation. An interesting observation is that this same decrease in degree of
579 saturation during the heat injection period was not observed in Figure 17(b) at the location of
580 thermistor string T-2, which was between borehole heat exchangers A and B. In fact, a slight
581 increase in degree of saturation is observed, likely due to movement of water vapor away from
582 these two heat exchangers to the cooler regions between.

583 The differences in behavior at the locations of thermistor strings T-3 and T-2 indicates
584 that for this particular set of thermo-hydraulic soil properties in Figure 1, the zone of influence
585 of degree of saturation changes is relatively limited in the conglomerate material. The effect of
586 the changes in degree of saturation with heating can be further investigated using the
587 numerical simulation results through the radial distributions in degree of saturation, thermal
588 conductivity, and volumetric heat capacity at the end of the heat injection period shown in

589 Figures 18(a), 18(b), and 18(c), respectively. Decreases in all three variables are noticed at the
590 end of heating, with greater decreases at the locations of the borehole heat exchangers. The
591 radial distributions for degree of saturation differ from those for the temperature observed in
592 Figure 15, which reflect a clear overlapping effect between the borehole heat exchangers.
593 Zones of influence of changes in degree of saturation of approximately 0.3 m is observed
594 around borehole heat exchanger A and of approximately 0.25 m is observed around borehole
595 heat exchanger B, which was not sufficient to cause a significant overlapping effect between
596 the two boreholes. Although not investigated, repeated cycles of heat injection and heat
597 removal may lead to greater zones of influence. Similar to the observations of Baser et al.
598 (2018), greater decreases in degree of saturation are observed for the locations with initially
599 greater degree of saturation and for greater changes in temperature, due to the effects of
600 enhanced vapor diffusion and phase change. Another interesting observation is that the
601 percent decrease in the thermal conductivity in Figure 18(b) is greater than the percent
602 decrease in the volumetric heat capacity in Figure 18(c). This has positive implications on the
603 performance of the heat storage systems as the lower thermal conductivity is expected to lead
604 to decrease in the heat loss from the system while the volumetric heat capacity reflects the
605 total heat that can be stored in the soil for a given increase in ground temperature.

606 Another comparison that can be made is the difference in the simulations expected for
607 the subsurface having thermo-hydraulic properties representative of unsaturated and saturated
608 conditions. When the subsurface is saturated, the governing equations in Table 1 are
609 significantly simplified. Heat transfer will occur primarily due to conduction, but natural
610 convection of the pore water will occur due to decreases in the density of water with

611 temperature. A comparison of the simulations for saturated and unsaturated conditions along
612 with the measured ground temperatures are shown in Figure 19 for a depth near the upper-
613 middle of the array at the location of borehole T-2. The temperature for saturated conditions
614 are generally lower, although they tend to rise sharply near the end of the heat injection
615 period, possibly due to upward water flow due to natural convection. Further comparisons of
616 the model for saturated and unsaturated conditions are shown in Baser et al. (2018) for the
617 case of a single geothermal heat exchanger.

618 **6. CONCLUSIONS**

619 This study focused on the simulation of transient heat transfer and water flow in a field-
620 scale SBTES system installed in the vadose zone. A non-isothermal, coupled heat transfer and
621 water flow model considering enhanced vapor diffusion and nonequilibrium phase change
622 calibrated in the laboratory using reconstituted specimens collected from the field was
623 validated by comparing simulated ground temperatures with those from field-scale SBTES
624 system during both heat injection and ambient cooling. In general, a good match was obtained
625 between the simulated and measured temperature data, reflecting the importance of
626 considering coupled heat transfer and water flow when simulating SBTES systems installed in
627 the vadose zone. During heat injection, ground temperatures were generally greater near the
628 surface in the borehole array, likely due to heat transfer due to buoyancy-driven vapor flow. At
629 the end of 5 months of ambient cooling, some heat was still retained within the array,
630 indicating that further heat injection and cooling cycles would lead to a positive effect on the
631 performance of this heat storage approach.

632 Differences between the simulation and measured data were likely due to differences in
633 how the heat injection boundary conditions were applied, the assumption of a homogenous
634 subsurface, the calibration of the model parameters using reconstituted specimens, and the
635 assumption regarding the depth of the water table (which may vary with time). Heat transfer
636 led to a clear overlapping effect between the closely-spaced geothermal borehole heat
637 exchangers in the SBTES system. However, the simulation results indicate that a significant
638 overlapping effect was not observed in terms of the changes in degree of saturation between
639 the geothermal borehole heat exchangers. Permanent decreases in degree of saturation were
640 observed at the locations of the geothermal heat exchangers, corresponding to a decrease in
641 thermal conductivity, but similar decreases in these variables were not observed in the bulk of
642 the subsurface between the geothermal borehole heat exchangers for the particular conditions
643 at the site. Further study on the effects of heating and cooling cycles of SBTES systems in the
644 vadose zone may better clarify the roles of thermo-hydraulic interaction between closely
645 spaced geothermal borehole heat exchangers for different subsurface materials.

646 **ACKNOWLEDGEMENTS**

647 Funding provided by National Science Foundation grant 1230237 is much appreciated.
648 The opinions presented here belong to authors alone.

649 **REFERENCES**

650 Akrouch, G.A., Sánchez, M., and Briaud, J.L. (2016). "An experimental, analytical and numerical
651 study on the thermal efficiency of energy piles in unsaturated soils." *Computers and*
652 *Geotechnics*. 71, 207-220.

653 Baser, T. and McCartney, J.S. (2015a). "Development of a full-scale soil-borehole thermal
654 energy storage system." Proc. Int. Foundation Conference and Equipment Exposition
655 (IFCEE 2015). ASCE, Reston, VA. pp. 1608-1617.

656 Başer, T. and McCartney, J.S. (2015b). "Thermal energy storage in borehole arrays." Symposium
657 on Energy Geotechnics. Barcelona. Jun. 2-4. pp. 1-2.

658 Baser, T., Lu, N., and McCartney, J.S. (2016a). "Operational response of a soil-borehole thermal
659 energy storage system." ASCE Journal of Geotechnical and Geoenvironmental
660 Engineering. 04015097-1-12. 10.1061/(ASCE)GT.1943-5606.0001432.

661 Baser, T., McCartney, J.S., Moradi, A., Smits, K., and Lu, N. (2016b). "Effect of a thermo-
662 hydraulic insulating layer on the long-term response of soil-borehole thermal energy
663 storage systems". GeoChicago 2016: Sustainability, Energy and the Geoenvironment.
664 Chicago. Aug. 14-18. ASCE, Reston, VA. pp. 125-134.

665 Baser, T., Dong, Y., and McCartney, J.S. (2016c). "Heat content in soil-borehole thermal energy
666 systems in the vadose zone." ICEGT 2016: 1st International Conference on Energy
667 Geotechnics. Kiel. CRC Press, Boca Raton. pp. 195-202.

668 Baser, T., Dong, Y., Lu, N., and McCartney, J.S. (2016d). "Role of considering non-constant soil
669 thermal parameters in the simulation of geothermal heat storage systems in the vadose
670 zone". Proceedings. 8th Asian Young Geotechnical Engineers Conference 2016 (AYGEC
671 2016). Kazakh Geotechnical Society. Astana. pp. 1-6.

672 Başer, T., Dong, Y., Moradi, A.M., Lu, N., Smits, K., Ge, S., Tartakovsky, D., and McCartney, J.S.
673 (2018). "Role of water vapor diffusion and nonequilibrium phase change in geothermal

674 energy storage systems in the vadose zone.” Journal of Geotechnical and
675 Geoenvironmental Engineering. 10.1061/(ASCE)GT.1943-5606.0001910.

676 Baser, T., Hanna, C., and McCartney, J.S. (2019). “Performance of a field-scale shallow
677 horizontal thermal energy storage system.” Geo-Congress 2019: The 8th International
678 Conference on Case Histories in Geotechnical Engineering. Philadelphia, PA. Mar. 24-27.
679 1-10. Accepted.

680 Bear, J. (1972). Dynamics of Fluids in Porous Media. Dover, Mineola, N.Y., 764.

681 Bjoern, H. (2013). “Borehole thermal energy storage in combination with district heating.” EGC
682 2013. Pisa. June 3-7. 1-13.

683 Bixler, N.E. (1985). NORIA: “A Finite Element Computer Program for Analyzing Water, Vapor, Air
684 and Energy Transport in Porous Media.” SAND84-2057, Sandia National Laboratories,
685 Albuquerque, NM.

686 Campbell, G.S. (1985). Soil Physics with BASIC: Transport Models for Soil–Plant Systems.
687 Elsevier, New York.

688 Campbell, G.S., Jungbauer, J.D., Bidlake, W.R., and Hungerford, R.D. (1994). “Predicting the
689 effect of temperature on soil thermal conductivity.” Soil Science. 158, 307–313.

690 Cass, A., Campbell, G.S., and Jones. T.L. (1984.) “Enhancement of thermal water vapor diffusion
691 in soil.” Soil Science Society of America. 48(1), 25–32.

692 Catolico, N., Ge, S., and McCartney, J.S. (2016). “Numerical modeling of a soil-borehole thermal
693 energy storage system.” Vadose Zone Hydrology. 1-17.doi:10.2136/vzj2015.05.0078.

694 Choi, J.S., Lee, S.R., and Lee, D.S. (2011). "Numerical simulation of vertical ground heat
695 exchangers: Intermittent operation in unsaturated soil conditions." *Computers and*
696 *Geotechnics*. 38, 949-958.

697 Claesson, J. and Hellström G. (1981). "Model studies of duct storage systems." *New Energy*
698 *Conservation Technologies and their Commercialization*. J.P. Millhorne and E.H. Willis,
699 Eds. Springer-Verlag, Berlin. 762-778.

700 COMSOL Multiphysics® v. 5.2. (2015). COMSOL AB, Stockholm, Sweden.

701 Ewen, J. and Thomas, H.R. (1989). "Heating unsaturated medium sand." *Géotechnique*. 39(3),
702 455-470.

703 Gens, A., Garcia Molina, A., Olivella, S., Alonso, E.E., and Huertas, F. (1998). "Analysis of a full
704 scale in-situ test simulating repository conditions." *International Journal of Numerical*
705 *and Analytical Methods in Geomechanics*. 22(7), 515-48.

706 Gens, A, Sanchez, M., Guimaraes L., and Huertas, F. (2009). "A full-scale in situ heating test for
707 high-level nuclear waste disposal: Observations, analysis and interpretation."
708 *Géotechnique*, 59(4), 377-399.

709 Grant, S.A. and Salehzadeh, A. (1996). Calculations of temperature effects on wetting
710 coefficients of porous solids and their capillary pressure functions. *Water Resources Res.*
711 32(2), 261-279.

712 Hillel, D. (1980). *Fundamental of Soil Physics*. Academic, San Diego, CA.

713 Iezzoni, H. M. and McCartney, J.S. (2016). "Calibration of Capacitance Sensors for Compacted
714 Silt in Non-Isothermal Applications." *Geotechnical Testing Journal*, Vol. 39(2), 169-180.

715 Lide, D.R. (Ed.) (2001). *Handbook of Chemistry and Physics*, CRC Press, Boca Raton, FL.

716 Lu, N. and Dong, Y. (2015). "A closed form equation for thermal conductivity of unsaturated
717 soils at room temperature." *Journal of Geotechnical and Geoenvironmental*
718 *Engineering*. 141(6), 04015016.

719 Marcotte, D. and Pasquier, P. (2014). "Unit-response function for ground heat exchanger with
720 parallel, series or mixed borehole arrangement." *Renewable Energy*. 68, 14–24.

721 McCartney, J.S., Ge, S., Reed, A., Lu, N., and Smits, K. (2013). "Soil-borehole thermal energy
722 storage systems for district heating." *Proceedings of the European Geothermal Congress*
723 *2013*. Pisa. Jun. 3-7. pp. 1-10.

724 Millington, R.J., and Quirk, J.M. (1961). "Permeability of porous solids." *Trans. Faraday Soc.* 57,
725 1200–1207.

726 Moradi, A.M., Smits, K., Lu, N., and McCartney, J.S. (2016). "3-D experimental and numerical
727 investigation of heat transfer in unsaturated soil with an application to soil borehole
728 thermal energy storage (SBTES) systems." *Vadose Zone J.* 15(10), 1-17.

729 Nguyen, A., Pasquier, P., and Marcotte, D. (2017). "Borehole thermal energy storage systems
730 under the influence of groundwater flow and time-varying surface temperature."
731 *Geothermics*. 66, 110-118.

732 Nordell, B. and Hellström, G. (2000). "High temperature solar heated seasonal storage system
733 for low temperature heating of buildings." *Applied Energy*. 69(6), 511–523.

734 Nussbicker-Lux, J. (2012). "The BTES project in Crailsheim (Germany) – Monitoring results."
735 *Proc. 12th Int. Conf. on Energy Storage – Innostock*. IEA Press, Paris. 1-10.

736 Sibbitt, B., McClenahan, D., Djebbar, R., Thornton, J., Wong, B., Carriere, J., Kokko, J. (2012).
737 "The performance of a high solar fraction seasonal storage district heating system - Five
738 years of operation." *Energy Procedia*. 30, 856-865.

739 Smits, K.M., Cihan, A., Sakaki, S., and Illangasekare, T.H. (2011). "Evaporation from soils under
740 thermal boundary conditions: Experimental and modeling investigation to compare
741 equilibrium- and nonequilibrium-based approaches." *Water Resources Research*. 47,
742 W05540, doi:10.1029/2010WR009533.

743 Thomas, H.R. and Sansom, M.R. (1995). "Fully coupled heat, moisture, and air transfer in an
744 unsaturated soil." *J Eng Mech* 1995;12(3):392–405.

745 Thomas, H.R. and Rees, S.W. (2009). "Measured and simulated heat transfer to foundation
746 soils." *Géotechnique*. 59(4), 365–375.

747 van Genuchten, M.T. (1980). "A closed-form equation for predicting the hydraulic conductivity
748 of unsaturated soils." *Soil Sci. Soc. Am. J.* 44(5), 892–898.

749 Wayllace, A. and Lu, N. (2012). "A transient water release and imbibitions method for rapidly
750 measuring wetting and drying soil water retention and hydraulic conductivity functions."
751 *Geotechnical Testing Journal*. 35(1), 103-117.

752 Welsch, B., Rühaak, W., Schulte, D.O., Bär, K., Homuth, S., and Sass, I. (2015). "Comparative
753 study of medium deep borehole thermal energy storage systems using numerical
754 modelling." *Proc. World Geothermal Congress 2015*. International Geothermal
755 Association. Bochum. 1-6.

756 Whitaker, S. (1977). "Simultaneous heat, mass and momentum transfer in porous media: A
757 theory of drying porous media." *Adv. Heat Transf.* 13, 119–203.

758 **TABLE 1.** Equations used in the numerical analyses

Equation	Number	Reference
<p><i>Nonisothermal liquid flow governing equation:</i></p> $nS_{rw} \frac{\partial \rho_w}{\partial t} + n\rho_w \frac{dS_{rw}}{dP_c} \frac{\partial P_c}{\partial t} + \nabla \cdot \left[\rho_w \left(-\frac{k_{rw}\kappa}{\mu_w} \right) \nabla (P_w + \rho_w g z) \right] = -R_{gw}$ <p>n=porosity (m³/m³), S_{rw}=degree of water saturation (m³/m³), ρ_w=temperature-dependent density of water (kg/m³) (Hillel 1980), t=time(s), P_c=P_w-P_g=capillary pressure (Pa), P_w=pore water pressure (Pa), P_g=pore gas pressure (Pa), k_{rw}=relative permeability function for water (m/s); κ=intrinsic permeability (m²); μ_w=temperature-dependent water dynamic viscosity (kg/(ms)) (Lide 2001), g=acceleration due to gravity (m/s²) R_{gw}=Phase change rate (kg/m³s)</p>	(1)	(Bear 1972; Moradi et al. 2016)
<p><i>Nonisothermal gas flow governing equation:</i></p> $nS_{rg} \frac{\partial \rho_g}{\partial t} + n\rho_g \frac{dS_{rg}}{dP_c} \frac{\partial P_c}{\partial t} + \nabla \cdot \left[\rho_g \left(-\frac{k_{rg}\kappa}{\mu_g} \right) \nabla (P_g + \rho_g g z) \right] = R_{gw}$ <p>S_{rg}=degree of gas saturation (m³/m³), ρ_g=temperature-dependent density of gas (kg/m³) (Smits et al. 2011), k_{rg}=relative permeability function for gas (m/s); μ_g=temperature-dependent gas dynamic viscosity (kg/(ms))</p>	(2)	(Bear 1972; Moradi et al. 2016)
<p><i>Water vapor mass balance equation:</i></p> $n \frac{\partial (\rho_g S_{rg} w_v)}{\partial t} + \nabla \cdot (\rho_g u_g w_v - D_e \rho_g \nabla w_v) = R_{gw}$ <p>D_e=D_vτ=effective diffusion coefficient (m²/s), D_v=diffusion coefficient of water vapor in air (m²/s) (Campbell 1985), w_v=mass fraction of water vapor in the gas phase (kg/kg), τ=n^{1/3}S_{rg}^{7/3}η=tortuosity (Millington and Quirk 1961)</p>	(3)	(Smits et al. 2011)
<p><i>Enhancement factor for vapor diffusion, η:</i></p> $\eta = a + 3S_{rw} - (a-1) \exp \left\{ - \left[\left(1 + \frac{2.6}{\sqrt{f_c}} \right) S_{rw} \right]^3 \right\}$ <p>a=empirical fitting parameter representing the soil-specific enhancement in vapor diffusion, f_c= clay content</p>	(4)	(Cass et al. 1984)
<p><i>Nonequilibrium phase change rate, R_{gw}:</i></p> $R_{gw} = \left(\frac{bS_{rw} RT}{M_w} \right) (\rho_{veq} - \rho_v)$ <p>b=empirical fitting parameter representing the soil-specific nonequilibrium phase change rate (s/m²), R=universal gas constant (J/molK), ρ_{veq}=equilibrium vapor density (kg/m³) (Campbell 1985), T=Temperature (K), ρ_v=vapor density (kg/m³), M_w=molecular weight of water (kg/mol)</p>	(5)	(Bixler 1985; Moradi et al. 2016)
<p><i>Heat transfer energy balance:</i></p> $(\rho C_p) \frac{\partial T}{\partial t} + \nabla \cdot ((\rho_w C_{pw}) u_w T + (\rho_g C_{pg}) u_g T - (\lambda \nabla T)) = -LR_{gw} + Q$ <p>ρ=total density of soil (kg/m³), C_p=specific heat of soil (J/kgK), C_{pw}=specific heat capacity of water (J/kgK), C_{pg}=specific heat capacity of gas (J/kgK), λ=thermal conductivity (W/mK), L=latent heat due to phase change (J/kg), u_w=water velocity (m/s), u_g=gas velocity (m/s), Q=heat source (W/m³)</p>	(6)	(Whitaker 1977; Moradi et al. 2016)

761 **TABLE 2.** Constitutive models used in the numerical analyses

Equation	Number	Reference
<p><i>Soil Water Retention Curve (SWRC):</i></p> $S_{rw} = S_{rw,res} + (1 - S_{rw,res}) \left[\frac{1}{1 + (\alpha_{vG} P_c(T))^{NvG}} \right]^{1-1/NvG}$ <p>where $S_{rw,res}$ is the residual degree of saturation to water, α_{vG} and NvG are parameters representing the air entry pressure and the pore size distribution, respectively, and $P_c(T)$ is the temperature-corrected capillary pressure according to the model of Grant and Salehzadeh (1996)</p>	(7)	(van Genuchten 1980)
<p><i>Hydraulic Conductivity Function (HCF):</i></p> $k_{rw} = \sqrt{\left(\frac{S_{rw} - S_{rw,res}}{1 - S_{rw,res}} \right) \left[1 - \left(1 - \left(\frac{S_{rw} - S_{rw,res}}{1 - S_{rw,res}} \right)^{1/(1-1/NvG)} \right)^{1-1/NvG} \right]^2}$ <p>where α_{vG} and NvG are the same parameters as in Equation (7)</p>	(8)	(van Genuchten 1980; Mualem 1970)
<p><i>Thermal Conductivity Function (TCF):</i></p> $\frac{\lambda - \lambda_{dry}}{\lambda_{sat} - \lambda_{dry}} = 1 - \left[1 + \left(\frac{S_e}{S_f} \right)^m \right]^{1/m-1}$ <p>where λ_{dry} and λ_{sat} are the thermal conductivities of dry and saturated soil specimens, respectively, S_e is the effective saturation, S_f is the effective saturation at which the funicular regime is onset, and m is defined as the pore fluid network connectivity parameter for thermal conductivity</p>	(9)	(Lu and Dong 2015)
<p><i>Volumetric Heat Capacity Function (VHCF):</i></p> $\frac{C_v - C_{v,dry}}{C_{v,sat} - C_{v,dry}} = 1 - \left[1 + \left(\frac{S_e}{S_f} \right)^m \right]^{1/m-1}$ <p>where $C_{v,dry}$ and $C_{v,sat}$ are the volumetric heat capacities of dry and saturated soil, respectively, and are similarly treated as fitting parameters, and S_f and m are the same parameters as in Equation (9)</p>	(10)	(Baser et al. 2016b)

762

763

764 **LIST OF FIGURE CAPTIONS**

765 **FIG. 1.** Coupled thermo-hydraulic constitutive relationships for the UCSD conglomerate: (a) SWRC and
766 HCF; (b) TCF and VHCF

767 **FIG. 2.** Schematic of the compaction mold used for calibration of water vapor diffusion and phase
768 change parameters along with the location of the embedded sensor and its zone of influence

769 **FIG. 3.** Calibration of the numerical model parameters using the heating test on compacted soil (soil
770 values at the depth of the dielectric sensor in Fig. 2): (a) Temperature; (b) Degree of saturation

771 **FIG. 4.** Experimental setup for the SBTES system: (a) Plan view; (b) Elevation view

772 **FIG. 5.** Photos of the SBTES system: (a) Excavation with borehole connections; (b) Hydraulic barrier;
773 (c) Insulation layer

774 **FIG. 6.** Plan view of the BTES and the simulated model domain (temperature sensors in boreholes 1, 2,
775 3, and 4, heat exchangers in boreholes A through M)

776 **FIG. 7.** Initial and boundary conditions on the quarter domain model for a field-scale geothermal heat
777 exchanger (JC is mass flux, distances in meters): (a) Thermal; (b) Hydraulic

778 **FIG. 8.** Thermal input boundary conditions to the SBTES system: (a) Ambient air temperature; (b) Solar
779 thermal heat transfer rates; (c) Close-up of daily solar thermal heat transfer rates; (d) Energy
780 balance

781 **FIG. 9.** Picture of borehole heat exchanger configuration highlighting heat injection sequence into Loops
782 1, 2, and 3 (Note: picture taken before inlet/outlet connections to manifold installed);

783 **FIG. 10.** Vertical SBTES loop heat transfer rates used in the calculations of the individual borehole
784 boundary conditions: (a) Loop 1; (b) Loop 2; (c) Loop 3

785 **FIG. 11.** Predicted and measured temperature time series from thermistor string T-1 for different depths
786 (z): (a) 16.00m; (b) 14.78m; (c) 12.95m; (d) 9.29m; (e) 6.85m; (f) 1.82m

787 **FIG. 12.** Predicted and measured temperature time series from thermistor string T-2 for different depths
788 (z): (a) 16.00m; (b) 14.78m; (c) 12.95m; (d) 9.29m; (e) 6.85m; (f) 1.82m

789 **FIG. 13.** Predicted and measured temperature time series from thermistor string T-3 for different depths
790 (z): (a) 16.00 m; (b) 14.78 m; (c) 12.95 m; (d) 9.29 m; (e) 6.85 m; (f) 1.82 m

791 **FIG. 14.** Predicted and measured temperature time series from thermistor string T-4 for different depths
792 (z): (a) 16.00 m; (b) 14.78 m; (c) 12.95 m; (d) 9.29 m; (e) 6.85 m; (f) 1.82 m

793 **FIG. 15.** Radial temperature profiles at different depths (z): (a) At the end of heating; (b) After 5 months
794 of ambient cooling

795 **FIG. 16.** Temperature profiles along the borehole length: (a) Borehole 2; (b) Borehole 4

796 **FIG. 17.** Time series of predicted degrees of saturation at the radial locations of: (a) Borehole 3;
797 (b) Borehole 2

798 **FIG. 18.** Radial profiles of predicted values at the end of heating: (a) Degree of saturation; (b) Thermal
799 conductivity; (c) Volumetric heat capacity

800 **FIG. 19.** Comparison of the transient temperature response of the subsurface having thermo-hydraulic
801 properties representative of saturated and unsaturated conditions

21 **1. INTRODUCTION**

22 Soil-borehole thermal energy storage (SBTES) systems are used for storing heat
23 collected from renewable sources in the subsurface so that it can be used later for space or
24 water heating. Heat sources such as solar thermal panels generate heat during the day with a
25 greater energy generation during summer months, so SBTES systems permit storage of the
26 abundant and free thermal resource (Sibbitt et al. 2012, McCartney et al. 2013). SBTES systems
27 function similarly to geothermal heat exchange systems, where a carrier fluid is circulated
28 through a closed-loop pipe network installed in vertical boreholes backfilled with sand-
29 bentonite. Different from boreholes in conventional geothermal heat exchange systems, the
30 boreholes in SBTES systems are spaced relatively close together (1-2 m) in an array to
31 concentrate heat in the subsurface (Claesson and Hellström 1981). SBTES systems are a
32 convenient alternative to other energy storage systems as they are relatively inexpensive,
33 involve storage of renewable energy (solar thermal energy), and are space efficient as they are
34 underground (Başer and McCartney 2015a).

35 Despite the successful use of SBTES systems in community-scale applications (Sibbitt et
36 al. 2012; Nussbicker-Lux 2012; Bjoern 2013), there are still opportunities for engineers to
37 improve the performance of SBTES systems by considering the role of the hydrogeological
38 setting in the subsurface. A goal of this study is to understand the benefits of installing SBTES
39 systems in the vadose zone, the layer of unsaturated soil or rock near the ground surface that
40 may extend to depths greater than 10 meters in some locations. The unsaturated porous
41 material in the vadose zone has a lower thermal conductivity than when saturated, limiting the
42 transient spreading of heat away the subsurface heat storage system (Choi et al. 2011). The

43 volumetric heat capacity of soils in unsaturated conditions is lower than in saturated conditions
44 but is still greater than in dry conditions. For example, the volumetric heat capacity of a silty soil
45 is 2.5 MJ/m³K for saturated conditions, 2.0 MJ/m³K for a degree of saturation of 0.5, and 1.2
46 MJ/m³K for dry conditions (Baser et al. 2016d). One challenge is that the modes of heat transfer
47 in unsaturated porous materials are more complex than when dry or water-saturated.
48 Specifically, in addition to coupling between the thermal and hydraulic properties of
49 unsaturated soils and the effects of temperature on fluid properties (e.g., Lu and Dong 2015),
50 the modes of heat transfer in unsaturated soils include a combination of conduction,
51 convection due to the flow of pore water in liquid and vapor forms under thermal and hydraulic
52 gradients, and latent heat transfer due to phase change. Several studies have developed
53 models to capture these different mechanisms of coupled heat transfer and water flow in
54 unsaturated soils, and have applied them to problems associated with radioactive waste
55 repositories (e.g., Ewen and Thomas 1989; Thomas and Sansom 1995; Gens et al. 1998; Gens et
56 al. 2009), soil-atmosphere interaction (Smits et al. 2011), energy piles (Akrouch et al. 2016), and
57 borehole geothermal heat exchangers (Başer et al. 2018). Başer et al. (2018) found that the
58 zone of influence of temperature changes in silt around a heat exchanger were greater for
59 unsaturated conditions when considering the impact of vapor phase convection. Previous
60 simulations of geothermal heat exchangers in unsaturated soil used conduction alone with a
61 thermal conductivity that varies with the initial degree of saturation (e.g., Choi et al. 2011), but
62 Başer et al. (2018) found that thermally-induced water flow may lead to significant differences
63 in the thermo-hydraulic response of the subsurface.

64 This paper presents a comparison of transient changes in ground temperatures
65 measured in a field-scale SBTES system installed in the vadose zone in San Diego, California with
66 those predicted from a numerical model for coupled heat transfer and water flow. The testing
67 program involved a 4-month period where heat collected from solar thermal panels was
68 injected into the borehole array, followed by a 5-month ambient cooling period. Heat transfer
69 rates into the subsurface measured in the field-scale SBTES system were used to define the
70 dynamic boundary conditions for heat injection in the model, considering the effects of
71 fluctuations in surface air temperature. Although the primary variable from the comparison is
72 the ground temperature, the numerical model also permits evaluation of the effects of thermo-
73 hydraulic interaction between the closely-spaced boreholes in the SBTES system on the degree
74 of saturation. This is important as changes in the degree of saturation due to thermally-induced
75 water flow may lead to associated changes in the subsurface thermo-hydraulic properties of
76 unsaturated soils.

77 **2. BACKGROUND**

78 Since the concept of borehole thermal energy storage systems was introduced by
79 Claesson and Hellström (1981), several SBTES systems have been installed in Canada and
80 Europe as part of district-scale heat distribution systems. The Drake Landing SBTES system in
81 Okotoks, Alberta, Canada supplies heat from solar thermal panels installed on garage roofs to
82 an array of 144 boreholes in a 35 m-deep, 35-m wide grid (Sibbitt et al. 2012), which is then
83 used to supply approximately 90% of the heat demand of 52 homes. Catolico et al. (2016)
84 simulated the response of the Drake Landing SBTES system, which lies in water-saturated sand
85 deposits overlying glacial till, using a numerical model in TOUGH2 using time-dependent

86 injection fluid temperatures measured at the site over six years of operation as the main
87 boundary condition. Over each year of operation, lateral heat transfer from the borehole array
88 to the surrounding ground was found to decrease due to a reduction in the thermal gradient
89 between the center of the array and the surrounding subsurface, meaning that more thermal
90 energy was concentrated in the center of the array. They found that the annual efficiency of
91 heat extraction (heat extracted divided by heat injected) increases over time, approaching a
92 value of 55%. However, the efficiency of heat recovery was found not to be a good
93 quantification of the SBTES performance because if the demand for heat in a given winter is
94 lower the the efficiency will decrease. Instead, it may be better to evaluate the fractions of heat
95 injected, stored, and lost. For example, in the 6th year of operation, 31.5% of the heat injected
96 into the system was recovered, 21.9% of the heat injected remained in the borehole array, and
97 46.7% of the heat injected escaped the borehole array. Despite the seemingly high fraction of
98 heat loss, the heat stored and recovered was sufficient to provide more than 90% of the
99 community's annual heating demands. Another successful SBTES system was installed in 2007 is
100 in Braedstrup, Denmark (Bjoern 2013). This system supplies heat from 18,000 m² of solar
101 thermal panels to an array of 50 boreholes having a depth of 47 to 50 m installed across a 15 m-
102 wide area. This system provides 20% of the heat to 14,000 homes. Another commercial-scale
103 SBTES was installed in 2008 in Crailsheim, Germany involving of a series of 55 m-deep
104 boreholes that formed a 39,000 m³ subsurface storage volume. This system stores heat from
105 7410 m² of flat plate solar thermal collectors to provide heat for a school and 230 dwellings
106 (Nussbicker-Lux 2012).

107 Although the experience from the commercial-scale systems at Drake Landing,
108 Braedstrup and Crailsheim indicates that SBTES systems are functional and are sufficiently
109 efficient to provide heating to different sizes of communities, simulation studies such as that of
110 Catolico et al. (2016) indicate that the hydrogeological setting is critical for optimizing the
111 thermal energy storage. Although the Drake Landing SBTES system includes instrumentation to
112 evaluate changes in ground temperature within the array (Sibbitt et al. 2012), it is in use for
113 commercial purposes, so the heat injection patterns cannot be varied as part of scientific
114 studies on the performance of SBTES systems. Accordingly, it is advantageous to install smaller
115 SBTES systems for demonstration projects in different hydrogeological settings to understand
116 the roles of different heat transfer processes and heat injection patterns on SBTES system
117 performance. For example, Başer et al. (2016a) reported the ground temperatures monitored
118 during a 75-day heat injection experiment into a small-scale SBTES system in Golden, CO, USA
119 involving an array of 5 borehole heat exchangers. Although the SBTES system in that study was
120 installed in an unsaturated silty soil layer, observations during installation indicate that the
121 bottom 10% of the heat exchanger lengths were in a saturated sand aquifer underlying the site.
122 Transient temperature measurements indicated that a substantial portion of the injected heat
123 left the array due to lateral heat loss associated with both the higher thermal conductivity of
124 the saturated sand layer and possible convection effects associated with groundwater flow in
125 this sand layer. Further, the simulations of Başer and McCartney (2015b) indicate that arrays
126 should have a greater number of boreholes than those considered by Başer et al. (2016a) to
127 effectively concentrate heat in the subsurface.

128 Although simplified design models for SBTES systems have been developed (e.g.,
129 Claesson and Hellström 1981), modeling the transient heat transfer in SBTES systems can be
130 complex because of the dimensions of the problem, the geometry and structure of the
131 borehole network, the process of heat transfer into the ground via circulating fluids in closed-
132 loop pipe networks, and the nonlinear variations in the thermal and hydraulic properties of
133 unsaturated soils with degree of saturation. Marcotte and Pasquier (2014) investigated the
134 effect of the borehole arrangement both analytically and numerically on the thermal response
135 of a heat storage system for the cases in which boreholes are connected in series, parallel, and
136 mixed configurations. They reported significantly lower inlet fluid temperatures for the parallel
137 configuration than for the series configuration, indicating a larger heat transfer to the ground
138 for this arrangement compared to the series configuration. Besides the geometrical
139 configuration of the borehole heat exchangers and the fluid circulation configuration (series,
140 parallel, mixed), there are other factors that affect the thermal response of a storage system,
141 such as the subsurface temperature profile and ambient air temperature, degree of saturation
142 profile of soil and the thermal properties. Thomas and Rees (2009) investigated the effect of
143 water content on heat transfer through unsaturated soils via a series of one and two-
144 dimensional numerical simulations that consider only conduction as the major heat transfer
145 mechanism. They reported 60% and 20% increases in heat flux with increasing water content
146 for one- and two-dimensional models, respectively. Akrouch et al. (2016) proposed an
147 analytical solution based on cylindrical heat source theory that accounts for variable degree of
148 saturation on the heat exchange between the heat source and sand soil and the results
149 indicated a 40% drop in performance of a heat exchanger when the degree of saturation is

150 close to residual conditions. Welsch et al. (2015) studied the impact of borehole length,
151 borehole, spacing, number of boreholes, and the inlet heat transfer fluid temperatures on the
152 behavior of thermal energy storage in crystalline rock. They observed that there was an optimal
153 spacing to reach the highest efficiency of heat recovery, with higher and lower values leading to
154 lower efficiencies. Due to the high thermal conductivity of the crystalline rock, the optimal
155 borehole heat exchanger spacing was 5 m, which is greater than that observed in similar studies
156 the focus on lower thermal conductivity soils (e.g., Baser and McCartney 2015a). Welsch et al.
157 (2015) found that the number of boreholes has a positive influence on the efficiency of heat
158 recovery because the increasing ratio of the storage volume to the size of the boundary of the
159 storage volume results in lower heat losses to the surrounding subsurface outside of the array.

160 Başer and McCartney (2015a) used a conduction-only model to understand the impacts
161 of borehole array geometry, ground properties, heat injection magnitudes, and heat injection
162 duration on the temperature distribution in the SBTES system. Başer et al. (2016b) and Başer et
163 al. (2016c) used a coupled heat transfer and water flow model without considering vapor
164 diffusion or phase change to understand the roles of incorporating a thermal insulation layer
165 and the effect of different unsaturated soil properties on the ground temperatures in SBTES
166 systems, respectively. These studies found that a surface insulation layer does not play a
167 significant role on the thermal energy storage due to the small area around each borehole heat
168 exchanger, but that surface temperature fluctuations should still be considered on the ground
169 temperatures. Bidarmaghz et al. (2016) investigated the effect of surface air temperature
170 changes on the thermal response of geothermal heat exchangers in the shallow subsurface and
171 found that considering ambient air temperatures in the simulations increased the total heat

172 exchanger length by 11%. A similar study by Nguyen et al. (2017) showed that seasonal
173 temperature variation of the subsurface increases the outlet fluid temperature causing a
174 decrease in the heat transfer rate into the ground. Further, they found that burying boreholes
175 at the certain depth from the surface (1-2 m) is not sufficient to hinder the ambient air
176 temperature effects on the ground temperature near the surface. Baser et al. (2017) used a
177 coupled heat transfer and water flow model considering vapor diffusion and phase change to
178 study the response of a single vertical borehole heat exchanger during a heat injection period
179 followed by a, ambient cooling periods. They evaluated the role of different heat transfer
180 mechanisms and observed a permanent drying around the heat exchanger during heat injection
181 that was not recovered during ambient cooling. This drying led to a decrease in thermal
182 conductivity that corresponded to a reduction in the amount of heat loss from the soil near the
183 heat exchanger.

184 **3. NUMERICAL MODEL**

185 **3.1. Model Formulation**

186 This study applies the model for geothermal heat exchangers in unsaturated soils used
187 by Baser et al. (2018), which was originally developed by Smits et al. (2011) and enhanced by
188 Moradi et al. (2016), to simulate the behavior of a field-scale SBTES system installed in San
189 Diego, California. The governing equations for the model are summarized in Table 1, while the
190 key thermo-hydraulic constitutive relationships are summarized in Table 2. Coupling occurs
191 between the different equations in Table 1 due to the effects of temperature on the different
192 fluid properties, which are summarized by Smits et al. (2011) and Baser et al. (2018). Simulation
193 of coupled heat transfer and water flow in unsaturated soils requires simultaneous solution of

194 the governing equations for two-phase flow (Equations 1 and 2) along with the heat transfer
195 based on energy balance (Equation 6). Because liquid and vapor phases are present in
196 unsaturated soils, flow induced by thermal gradients in both liquid and total gas phases are
197 considered and formulated as the convection terms in the energy balance equation (i.e., the
198 second and the third terms in Equation 6). When formulating the model, some assumptions are
199 made: (a) soil framework is homogeneous, isotropic, and non-deformable; (b) fluid phases are
200 immiscible; (c) hysteresis in the constitutive relationships is not considered. The model
201 considers enhanced vapor diffusion described by Equation (4) and a nonequilibrium phase
202 change rate described by Equation (5) that are incorporated into the water vapor mass balance
203 equation in Equation (3) and as source terms in the governing equations for two-phase flow
204 and the heat transfer energy balance. The model was implemented into the finite element-
205 based software COMSOL Multiphysics® version 5.2a (COMSOL 2015) which solved the
206 governing equations for the four primary unknowns: pore water pressure, total pore gas
207 pressure, water vapor concentration, and temperature.

208 **3.2. Model Calibration**

209 The key parameters that must be defined to calibrate the numerical model are the
210 parameters of the thermo-hydraulic constitutive relationships given in Table 2 and the
211 parameters a and b from Table 1 that govern the soil-specific enhanced vapor diffusion rate
212 and the nonequilibrium phase change rate, respectively. The methodology described in this
213 section for parameter calibration was applied to the subsurface in the SBTES array evaluated in
214 this study but could also be applied to design SBTES systems in the vadose zone in other
215 locations.

216 The SBTES system constructed as part of this study was installed in an unsaturated
217 conglomerate bedrock layer at the Englekirk Structural Engineering Center (ESEC) of the
218 University of California San Diego. A site investigation from 2003 indicates approximately 1m of
219 sandy soil overlying the conglomerate bedrock consisting of cemented sand- and gravel-size
220 particles. An undisturbed core of the conglomerate bedrock was not obtained during
221 installation of the SBTES system. However, disturbed cuttings from a hole drilled into the
222 conglomerate using an auger were collected from different depths. Although it is not possible
223 to reconstitute the cuttings into the same cemented structure as the conglomerate, it is
224 assumed that the thermo-hydraulic properties of the conglomerate are predominantly
225 governed by the grain size, mineralogy, and density for the purposes of model calibration so
226 that laboratory calibration of the model parameters is possible. Laboratory calibration permits
227 the use of instrumented specimens under carefully-controlled boundary conditions, but future
228 studies may use inverse analyses from field measurements to consider the role of the
229 cemented structure on the calibrated model parameters. Specimens used to represent the
230 conglomerate properties were reconstituted from cuttings obtained from a depth of 16 m from
231 the surface at the ESEC facility, which were prepared using compaction to a dry density of a
232 1650 kg/m^3 at an initial degree of saturation of 0.49, which corresponds to conditions in the
233 conglomerate measured using sand-cone experiments performed at a depth of 1.5 m from the
234 surface.

235 The thermo-hydraulic constitutive relationships were determined using a modified form
236 of the transient water release and imbibition method (TRIM) of Wayllace and Lu (2012) that
237 included the measurement of the thermal conductivity and volumetric specific heat capacity

238 described by Lu and Dong (2015). Specifically, a specimen was compacted to the conditions
239 mentioned above into a modified Tempe cell that incorporates a dual thermal needle and a
240 dielectric sensor, was saturated with water, then dried monotonically in two stages. The soil
241 water retention curve (SWRC), hydraulic conductivity function (HCF), thermal conductivity
242 function (TCF), and volumetric heat capacity function (VHCF), described by Equations 7
243 through 10 in Table 2, were obtained from inverse analysis of the outflow and thermal property
244 measurements during this drying stage. The SWRC and HCF along with relevant parameters are
245 shown in Figure 1(a), while the TCF and VHCF along with relevant parameters are shown in
246 Figure 1(b). Lu and Dong (2015) presented empirical relationships between the parameters of
247 the thermal constitutive relationships and the hydraulic constitutive relationships, but the
248 properties measured from the experiments in Figure 1 were used in the simulations.

249 The properties governing the vapor diffusion phase change rate and diffusion were
250 calibrated using an evaporation experiment on a reconstituted specimen of the site soil. The
251 soil was compacted in a plastic modified Proctor compaction mold having a diameter of 152
252 mm to a height of 179 mm. The mold, developed by Iezzoni and McCartney (2015), can
253 accommodate a dielectric sensor at mid-height of the soil specimen as shown in the cross-
254 sectional schematic in Figure 2. An evaporation test starting from the initial degree of
255 saturation mentioned above was performed by heating the bottom of the soil layer using a
256 heating pad placed below the mold while leaving the surface of the soil open to the
257 atmosphere. The heating pad applies fluctuating heat pulses to maintain a target temperature.
258 Thus, a thermocouple was placed at the bottom to monitor the applied boundary temperature
259 during heating, which is shown in Figure 3(a). Ambient temperatures were also recorded with a

260 thermocouple so that the ambient air temperatures could be applied as boundary conditions
261 on the outer surfaces of the specimen during the experiment. A temperature of approximately
262 42 °C was maintained over a period of 35 h. The measured values of temperature and degree of
263 saturation at the center of the soil specimen during this period are shown in Figures 3(a) and
264 3(b), respectively. The model of Iezzoni and McCartney (2015) was used to correct the degrees
265 of saturation inferred from the dielectric sensor to account for temperature effects. This
266 calibration test was then simulated using the coupled heat transfer and water flow model, and
267 the parameters a and b in Equations 4 and 5 in Table 1 were varied using a manual parameter
268 sweep to identify the best combination of parameters to match the measured curves. The
269 simulated temperature and degree of saturation curves for $a = 20$ and $b = 2 \times 10^{-7} \text{ s/m}^2$ are
270 shown in Figures 3(a) and 3(b), respectively, which indicate a good match.

271 **3.3. Simulation Details for the Field-Scale SBTES System**

272 The calibrated model was then used to simulate the response from the field-scale SBTES
273 system demonstration experiment. A plan view of the SBTES system showing the connections
274 between the boreholes in the array, a manifold for control and monitoring of the heat
275 exchanger fluid in the borehole array, a 2400 L water-filled temporary heat storage tank, and a
276 series of solar thermal panels is shown in Figure 4(a). This figure also shows the location a
277 reference borehole for monitoring the undisturbed ground temperature profile. Thirteen of the
278 boreholes in the array include heat exchanger tubing, while four of the boreholes in the array
279 include thermistor strings that monitor the ground temperature. Two of the boreholes include
280 both heat exchangers and thermistor strings. The boreholes were backfilled with sand
281 bentonite after installation of the heat exchangers or thermistor strings. The hexagonal

282 configuration of the borehole array was selected for ease of construction, as the boreholes in
283 the array fall into five co-linear sets that facilitate positioning of the drill rig. The main design
284 variable used to configure the boreholes was the spacing. Baser and McCartney (2015a) found
285 that the borehole spacings should be less than 1.5 m to ensure overlapping effects of the heat
286 exchangers for soil thermal properties and heat transfer rates typical of SBTES systems. The
287 number of boreholes containing heat exchangers was selected so that the boreholes in the
288 array would fall into two annuli, greater than the number in the array tested by Baser et al.
289 (2016a). Although a commercial-scale SBTES system would likely have more heat exchangers in
290 several more annuli (e.g., Sibbitt et al. 2012), this array is still sufficient in scale to investigate
291 the transient heat transfer and heat storage in the subsurface within the array associated with
292 interactions between heat exchangers.

293 An elevation view of the site is shown in Figure 4(b), which highlights the position of the
294 15 m-long boreholes beneath a 1 m-deep excavation. After connection of the heat exchanger
295 tubing following the arrangement shown in Figure 4(a), a thin layer of site soil was placed for
296 leveling-purposes, which was overlain by a hydraulic barrier, an insulation layer, and a
297 compacted layer of site soil. The high-density polyethylene (HDPE) hydraulic barrier has a
298 thickness of 0.01 m and an assumed hydraulic conductivity of 10^{-12} m/s, while the EPS geofam
299 insulation layer has a thickness of 50 mm, a thermal conductivity of 0.03 W/mK, and a specific
300 heat capacity of 0.9 MJ/kgK. The lateral extents of the hydraulic barrier and insulation layer
301 followed the hexagonal boundaries of the array shown in Figure 4(a). Pictures of the SBTES
302 system are shown in Figure 5, highlighting the 1 m-deep excavation and connection of the
303 borehole heat exchangers in Figure 5(a), the hydraulic barrier in Figure 5(b), the insulation layer

304 in Figure 5(c), and the completed set of solar thermal panels and temporary heat storage tank
305 in Figure 5(d).

306 As the hexagonal borehole array is symmetrical, a quarter section was simulated as
307 shown in Figure 6. The temperatures on either side of the two planes of symmetry are assumed
308 to be identical. This simulation strategy was also used by Catolico et al. (2016) to reduce
309 computation times when simulating symmetrical SBTES systems. Figure 6 also includes the
310 labels used to name the thirteen boreholes that include heat exchangers (boreholes A through
311 M) and the four boreholes that include thermistor strings (T-1 to T-4). As will be described
312 below, appropriate fractions of the heat transfer from boreholes A ($1/4$ of its heat transfer), B
313 ($1/2$ of its heat transfer) and E ($1/2$ of its heat transfer) are applied as boundary conditions. The
314 model domain is 15 m x 15 m in plan and has a depth of 20 m and includes 5 borehole heat
315 exchangers. The size of the domain was selected such that the heat exchangers would not
316 affect the temperatures at the boundaries for the heat injection period under investigation.
317 This was confirmed by ensuring that the temperature at the boundaries of the array remained
318 similar to the temperatures from the reference borehole at different depths. The domain was
319 discretized using 756,667 elements with finer discretization around the boreholes. Triangular
320 elements were used on the surfaces of boreholes and insulation layer, and tetrahedral
321 elements were used for the rest of the domain. A maximum element growth rate of 1.4 and a
322 curvature factor of 0.25 were used in discretization in COMSOL.

323 The isometric views of the model domain shown in Figures 7(a) and 7(b) highlight the
324 thermal and hydraulic boundary and initial conditions, respectively. The initial temperature
325 profile was obtained from the ground temperature distribution measured by the reference

326 borehole at the initiation of the heat injection period on April 29th, 2016. To define the initial
327 degree of saturation profile, hydrostatic conditions were assumed. Although the water table
328 was not encountered in the previous geotechnical site investigation which was performed in
329 2003, the San Diego County Water Authority reported that the ground water depth ranges in
330 depth from 14 to 24 m in the area and no groundwater flow was recorded. Accordingly, the
331 water table was fixed at a depth of 20 m from the surface (i.e., at the base of the domain)
332 throughout the simulations for simplicity as its actual location during the experiment is
333 unknown. Although the depth of the groundwater table may be greater than 20 m, this choice
334 of boundary condition was selected to limit the size of the domain in the simulations. Based on
335 the hydrostatic profile shown in Figure 7(b), the initial degree of saturation along most of the
336 length of the heat exchangers was approximately 0.22 which corresponds to residual saturation
337 conditions. Near the bottom of the heat exchangers, the initial degree of saturation increases
338 up to 0.49 due to the proximity of the water table.

339 Neumann boundary conditions of zero mass flux and zero heat flux were assigned for
340 the outer lateral boundaries of the domain as well as for the planes of symmetry. Dirichlet
341 boundary conditions for temperature were applied at the bottom and top of the domain. A
342 constant temperature of 21°C was applied at the bottom of the domain, which corresponds to
343 the average measured temperature at the base of the reference borehole. The temperature of
344 the top of the domain was assumed to equal the time-dependent ambient air temperatures
345 that were measured at the site during the duration of the experiment, shown in Figure 8(a).
346 Although the EPS geofoam insulation layer is considered in the simulations, it does not provide
347 a perfect insulation effect so the effects of the ambient air temperature fluctuations on the

348 surface temperature must be considered. It should be noted that the surface ground
349 temperature may differ from the ambient air temperature due to radiative and air convection
350 effects, so the use of the ambient air temperature as a surface boundary condition may be a
351 simplifying assumption. A zero-mass flux boundary condition was applied to the surface
352 boundary. This choice was made to simplify the fluid flow processes in the ground as an
353 infiltration/evaporation boundary condition can be computationally expensive when combined
354 with a coupled heat transfer and water flow model considering vapor diffusion and phase
355 change. However, this assumption is reasonable both due to the relatively low precipitation in
356 San Diego as well as due to the presence of the hydraulic barrier atop the borehole array.
357 However, this boundary condition choice is expected to affect the accurate simulation of the
358 temperature at the location of the reference borehole, as infiltration of water may affect the
359 thermal properties of the surface soil. As mentioned, Dirichlet boundary conditions were
360 assumed for the water table at the base of the domain (pore water pressure equal to zero).

361 Although the heat transfer boundary conditions for geothermal borehole heat
362 exchangers previous simulations of SBTES systems involved control of the inlet fluid
363 temperature and considered convective heat transfer associated with fluid flow through the
364 sequence of borehole heat exchangers in the array (e.g., Welsch et al. 2015; Catolico et al.
365 2016), this study considered the borehole heat exchangers as cylindrical heat sources and
366 applied heat flux values to the outer diameters of the cylinders equal to the measured heat flux
367 values from the site discussed in the next paragraph. The heat transfer boundary conditions
368 associated with fluid flow through heat exchanger pipes were not considered in this study
369 because of long computational times associated with solving the governing equations for

370 coupled heat transfer and water flow processes in the subsurface given in Table 1, which was
371 the primary topic of interest in this study. The simplified heat transfer boundary condition for
372 the borehole heat exchangers still permits validation of the coupled heat transfer and water
373 flow analyses in the subsurface within the array. However, design simulations for SBTES
374 systems require control of the inlet fluid temperature and consideration of convective heat
375 transfer of fluid flow through the heat exchangers as the heat transfer rate will decrease over
376 time as the soil within the array increases in temperature (e.g., Welsch et al. 2015). Another
377 assumption in this study is that a uniform heat flux was applied to each of the heat exchangers
378 based on the measured heat transfer rates in the field. Although the choice of a uniform heat
379 flux along a heat exchanger connected in series through several boreholes may not be suitable
380 when simulating a commercial-scale SBTES system with long overall heat exchanger lengths, the
381 relatively short overall heat exchanger lengths used in this field demonstration project
382 permitted the use of this simplified boundary condition without major discrepancies in
383 matching the measured subsurface temperatures.

384 Eight evacuated tube solar thermal panels having a total area of 33 m² were connected
385 in series to collect heat during the day, which was then transferred to the water in the
386 temporary heat storage tank via a coiled copper tube. A second coiled copper tube in the
387 temporary heat storage tank is used to inject heat into the SBTES system. A second horizontal
388 SBTES system was also installed at the site and was tested at the same time (Baser et al. 2019).
389 Although this horizontal SBTES system is not discussed in this paper, it should be acknowledged
390 as all the heat collected from the solar thermal panels was not injected into the “vertical” SBTES
391 system under evaluation in this study. Nonetheless, the measured heat transfer rate into the

392 subsurface was boundary condition used in the simulations, so the effects of the horizontal
393 SBTES system is not important. Water was used as the heat exchanger fluid in both the solar
394 thermal panels and in the SBTES system as freezing temperatures are not expected in San
395 Diego. The heat transfer rates were calculated as follows:

$$\dot{Q} = \dot{V}_w \rho_w C_w (T_{in} - T_{out}) \quad (11)$$

396 where \dot{V}_w is the measured volumetric flow rate of the heat exchanger fluid (water), ρ_w is the
397 density of water (1000 kg/m³), C_w is the specific heat capacity of water (4183 J/kgK), and T_{in} and
398 T_{out} are the measured temperatures of the water entering and exiting solar thermal panels,
399 respectively. The heat transfer rates for the solar thermal panels over the 120-day period
400 starting on April 29, 2016 are shown in Figure 8(b). The large fluctuations in heat transfer rate
401 observed in this figure occur because heat is only collected during the day. To better
402 understand the transient heat transfer rates from the solar thermal panels and the total heat
403 injected into the vertical SBTES system during 2 days of operation are shown in Figure 8(c). A
404 lag is observed between the heat transfer rates collected from the solar thermal panels and
405 injected into the vertical SBTES, but the temporary water storage tank provides a buffer to
406 permit heat injection at night as well. A control system has not yet been implemented to ensure
407 that heat is only collected from the solar thermal panels during the day. Specifically, the
408 circulation pumps in the solar thermal panels and SBTES system are operated continuously.
409 Accordingly, fluid is still circulated through the solar panels at night, which may result in a slight
410 extraction of heat from the temporary heat storage system if the outside air is colder than the
411 borehole array. The efficiency of heat transfer in the system can be assessed using the
412 cumulative total energy collected from the solar thermal panels and injected into the vertical

413 and horizontal SBTES systems shown in Figure 8(d). Approximately 80% of the cumulative heat
414 collected from the solar thermal panels is injected into the vertical and horizontal SBTES
415 systems, with the remaining 20% lost due to the circulation of fluid through the solar thermal
416 panels at night. Additional experimental testing is underway to investigate other configurations
417 for flow through the solar thermal panels (series instead of parallel) along with inclusion of a
418 heat transfer fluid control system in the solar thermal panels to increase the efficiency of heat
419 collection from the solar thermal panels and injection into the SBTES systems.

420 As mentioned, the borehole heat exchangers were simulated as cylinder sources having
421 a uniform heat flux with depth with a magnitude that varied according to the measured heat
422 flux interpreted from Equation (11) using the entering and exiting fluid temperatures and fluid
423 flow rates going into the different geothermal loops shown in Figure 4(a). Specifically, the heat
424 exchanger tubing was split into three closed-loop networks of U-tube borehole heat exchangers
425 (referred to as Loops 1, 2, and 3). Each loop is connected to a borehole heat exchanger in the
426 central borehole, which means that the central borehole contains 3 U-tube heat exchangers.
427 Next, the three loops connect to four other borehole heat exchangers in different zones of the
428 array, as shown in the photograph in Figure 9 and the schematic in Figure 4(a). It is expected
429 that the heat exchanger fluid flowing through the loops will be hottest in the center of the
430 array, and the fluid temperature will decrease as it flows through the surrounding four
431 borehole heat exchangers and returns to the manifold. However, as noted above, the relatively
432 short length of the heat exchangers in each loop permits the assumption that the heat flux is
433 the same from each borehole connected to the loop (except for the central borehole which has
434 three times the other boreholes). The use of three loops provides flexibility for changing the

435 heat transfer into different zones of the array, but in this study all three loops had a balanced
436 flow. Specifically, the fluid flow rates in each of the loops were controlled and measured
437 independently to be equal and ensure that heat transfer is balanced into the different zones of
438 the borehole array. The inlet and outlet fluid temperatures for each loop were monitored so
439 that Equation (11) could be applied to obtain the heat transfer rate into the subsurface, which
440 was the main boundary condition applied in the simulations.

441 A challenge encountered when simulating a quarter domain is that boreholes from
442 different loops were included in the domain, and the heat transfer rates in each loop were not
443 the same. Specifically, the borehole heat exchangers that were simulated were A (center
444 borehole, part of loops 1, 2, and 3), B (part of loop 2), C (part of loop 2), and D (part of loop 3), E
445 (part of loop 3) as shown in Figure 9 and Figure 4(a). Further, the heat transfer rates calculated
446 using Equation 11 represent an average heat transfer rate across the five borehole heat
447 exchangers in each loop. Accordingly, some assumptions had to be made regarding the heat
448 transfer rates applied to the different borehole heat exchangers being simulated. Because the
449 different borehole heat exchangers were obtained from different loops, the heat transfer rates
450 for the different borehole heat exchangers were interpreted from the heat transfer rates of
451 Loops 1, 2, and 3 calculated from Equation 11 which are shown in Figure 10. Specifically, the
452 total heat transfer rates from all three loops were first divided by five to represent the heat
453 transfer rate into the five boreholes in the quarter section domain and the transient heat fluxes
454 were applied to each borehole individually depending on its associated loop. The heat transfer
455 rate for the center borehole was equal to the sum of $1/5^{\text{th}}$ of each of the three heat transfer
456 rates, and the heat transfer rates for boreholes B, C, D, and E were equal to $1/5^{\text{th}}$ of the heat

457 transfer rates from the respective loops noted above. Although it is likely that the center
458 borehole A had a higher local heat flux than the outer borehole E it is assumed that the
459 gradients of temperature in the center and edge of the array balanced out over time, so the
460 total heat transfer rate of each loop could be considered as an average of the entire system.
461 The transient heat transfer rates were converted to heat fluxes which were applied to the
462 outside area of each borehole in the quarter section domain. At the end of the heat injection
463 period, the heat flux for each borehole was set to zero to represent the ambient cooling period.
464 Because the coupled heat transfer and water flow processes in the subsurface are relatively
465 slow, a time interval of 1800 s was used in the simulations of the 120-day heat injection period
466 followed by a 155-day ambient cooling period, which was found to lead to sufficiently accurate
467 results when evaluating the changes in ground temperature.

468 **4. COMPARISON OF NUMERICAL RESULTS AND FIELD MEASUREMENTS**

469 A goal of this study is to present the field measurements in a way that the transient heat
470 transfer results at different locations in the borehole array could be understood. Second,
471 because of the simplifying assumptions regarding the subsurface thermo-hydraulic properties
472 (homogeneity and use of reconstituted specimens), the uncertain location of the water table
473 below the heat exchanger array, and the use of a uniform heat flux along the boreholes, it is
474 preferred to show a qualitative comparison between the field measurements and the results
475 from the numerical simulation without a detailed error analysis.

476 As could be expected from the large fluctuations in the heat transfer rate into the
477 geothermal heat exchanger loops due to the variability in the solar thermal heat transfer rate,
478 the temperature at the locations of the borehole heat exchangers are expected to experience

479 significant changes in temperature each day. The temperatures at the center borehole
480 measured using the thermistor string T-1 along with the simulated temperature from the model
481 are shown in Figure 11. The temperature at each depth is shown separately in each sub-figure
482 to differentiate the transient response at the different depths. Although the temperatures at a
483 depth of 16.00 m were underestimated during heating, the temperatures at other depths were
484 captured well by the model. The difference at a depth of 16.00 m may be due to the
485 assumption of the hydrostatic initial conditions based on the assumed location of the water
486 table, which leads to a higher thermal conductivity of the subsurface in the simulations. The
487 differences in the daily fluctuations of each depth occur as the temperatures from the model
488 were obtained in a soil element at the boundary of the heat exchanger, while the measured
489 temperatures are from the thermistor strings inside the borehole and are in contact with the
490 geothermal heat exchanger. The sand-bentonite grout backfill in the boreholes was not
491 considered in the model simulations but may affect the heat transfer process in the field
492 measurements. During the ambient cooling stage, the transient trends appear to be well-
493 captured, although the initial temperature at the start of ambient cooling was occasionally
494 different from that between the measured and simulated values. The two locations closer to
495 the surface show an increase in the rate of cooling on day 210, likely due to the lower ambient
496 air temperatures observed in Figure 8(a).

497 A comparison between the temperatures at the location of thermistor string T-2 shown
498 in Figure 12 indicates less daily fluctuations than at the location of thermistor string T-1. The
499 temperature at the location of thermistor string T-2 depends on overlapping effects of borehole
500 heat exchangers A and B, and heat transfer from these boreholes damps out the daily

501 fluctuations. A good match in the trends and magnitudes at the different depths was observed
502 during both the heat injection and ambient cooling periods, with underestimation of the
503 temperatures at depths of 16.00 m and 1.82 m. The measured temperature values during the
504 heating injection period ranged from 29.5 °C near the bottom of the array to 34.2 °C near the
505 top of the array. The greater increases in measured and simulated temperatures near the
506 surface of the array may be due to greater heat transfer in initially dryer soils due to greater
507 water vapor diffusion and latent heat transfer as well as buoyancy-driven upward movement of
508 water vapor, both of which were observed by Baser et al. (2018) in the simulation of a single
509 geothermal heat exchanger. The measured and simulated temperatures at the location of
510 thermistor string T-3 shown in Figure 13 are similar to those for thermistor string T-1 in Figure
511 11 due to the presence of borehole heat exchanger B, but with lower magnitudes. The lower
512 magnitude is because the heat flux from borehole heat exchanger B was three times smaller
513 than the three loops in borehole heat exchanger A. Finally, the measured and simulated
514 temperatures at the location of thermistor string T-4 shown in Figure 14 show the lowest
515 increases in temperature due to its larger radial location from the center of the borehole array.
516 One of the thermistors at a depth of 12.95m was not functional after installation. Like
517 thermistor string T-2, greater temperatures were noted near the surface.

518 The differences between the simulated and measured ground temperatures could be
519 due to the use of reconstituted specimens to obtain the thermo-hydraulic properties, the
520 possibility that the subsurface does not have homogeneous thermo-hydraulic properties,
521 uncertainty about the actual depth of the groundwater table (which may have affected the
522 initial degree of saturation and thermal properties), and the use of simplified heat exchanger

523 boundary conditions. A general observation regarding the measured and simulated
524 temperature time series is that even though the heat transfer was simulated as an average heat
525 flux at the boundaries of the heat exchangers instead of simulating the heat transfer via
526 circulation of fluid in the borehole loops, a good match with the ground temperatures during
527 both heating and cooling was observed. Although the actual location of the water table was not
528 known a-priori, comparison of the simulation results shown in Figures 11 through 14 at depths
529 near the middle and bottom of the heat exchangers indirectly reflect the importance of the
530 initial degree of saturation on the simulation results from the coupled heat transfer and water
531 flow model. Greater initial degrees of saturation will lead to higher thermal conductivity values
532 and may lead to greater changes in degree of saturation due to enhanced vapor diffusion and
533 latent heat transfer (Baser et al. 2018). The differences in simulated and measured
534 temperatures at the different depths in the soil profile in Figures 11 through 14 could also have
535 been due to variations in subsurface stratigraphy not observed in the installation of the heat
536 exchangers, which would have led to variations in thermo-hydraulic properties with depth.
537 Despite the challenges in validating the numerical model with field data, the numerical model
538 was found to capture the temperature of the subsurface within the array with good accuracy
539 within most of the array.

540 Radial profiles of temperatures at the end of the heat injection period from the
541 numerical model and the field measurements are shown in Figures 15(a) for the depths that
542 thermistors were installed. Temperatures were in good agreement, especially at depths of
543 14.78 and 1.82 m. This figure also includes the ground temperatures from the reference
544 borehole. The shapes of the radial profiles are like those interpreted from the field

545 measurements, although the maximum temperatures at the locations of thermistor strings 1
546 and 3 due to the daily fluctuations in heat transfer rate were not captured as noted in the time
547 series in Figures 11 and 13, respectively. Radial distributions in temperature at the end of the
548 ambient cooling period indicate that some heat (a maximum difference in temperature of 4 °C
549 from the initial value of 21 °C) is still retained within the array after 5 months of ambient
550 cooling. This amount of decrease in temperature due to ambient cooling is expected to
551 decrease if further cycles of heating and cooling were investigated, similar to the observations
552 of Catolico et al. (2016). Temperature profiles at the locations of boreholes 2 and 4 are shown
553 in Figures 16(a) and 16(b), respectively. Both the measured and simulated temperature profiles
554 show an increase in temperature with proximity to the ground surface, likely due to the effects
555 of natural convection. As the pore fluids are heated, their densities decrease causing them to
556 rise and transfer heat upward in the subsurface.

557 **5. ADDITIONAL INSIGHTS FROM MODEL SIMULATIONS**

558 Although it was known that the subsurface at ESEC was unsaturated, and that changes
559 in degree of saturation are expected due to coupled heat transfer and water flow,
560 instrumentation was not incorporated in the subsurface within the borehole array to monitor
561 changes in degree of saturation. This was due to difficulty in installing dielectric sensors into the
562 intact conglomerate through the sides of the boreholes. Installation of these sensors into a soil-
563 bentonite-backfilled borehole would measure the changes in thermo-hydraulic behavior of the
564 backfill, not the conglomerate. Nonetheless, it is still possible to infer the changes in degree of
565 saturation of the subsurface from the numerical simulation results, as well as the effects of
566 these changes on the heat transfer during the heat injection period and heat retention during

567 the ambient cooling period. Time series of the simulated degrees of saturation at the locations
568 of thermistor strings 3 and 2 are shown in Figures 17(a) and 17(b). Due to the boundary
569 conditions associated with borehole heat exchanger B next to thermistor string 3, a steady
570 decrease in degree of saturation was noted during the heat injection period at this location in
571 Figure 17(a). This decrease in degree of saturation is expected due to enhanced vapor diffusion
572 from relatively hot regions to colder regions. During the ambient cooling stage, the degree of
573 saturation at the location of thermistor string T-3 was not observed to recover. A similar
574 observation was made by Baser et al. (2018) for a single borehole heat exchanger in compacted
575 silt that had different thermo-hydraulic properties. The main effect of this decrease in degree of
576 saturation is that the decrease in temperature at this location during ambient cooling should be
577 slower due to the lower thermal conductivity associated with the permanent decrease in
578 degree of saturation. An interesting observation is that this same decrease in degree of
579 saturation during the heat injection period was not observed in Figure 17(b) at the location of
580 thermistor string T-2, which was between borehole heat exchangers A and B. In fact, a slight
581 increase in degree of saturation is observed, likely due to movement of water vapor away from
582 these two heat exchangers to the cooler regions between.

583 The differences in behavior at the locations of thermistor strings T-3 and T-2 indicates
584 that for this particular set of thermo-hydraulic soil properties in Figure 1, the zone of influence
585 of degree of saturation changes is relatively limited in the conglomerate material. The effect of
586 the changes in degree of saturation with heating can be further investigated using the
587 numerical simulation results through the radial distributions in degree of saturation, thermal
588 conductivity, and volumetric heat capacity at the end of the heat injection period shown in

589 Figures 18(a), 18(b), and 18(c), respectively. Decreases in all three variables are noticed at the
590 end of heating, with greater decreases at the locations of the borehole heat exchangers. The
591 radial distributions for degree of saturation differ from those for the temperature observed in
592 Figure 15, which reflect a clear overlapping effect between the borehole heat exchangers.
593 Zones of influence of changes in degree of saturation of approximately 0.3 m is observed
594 around borehole heat exchanger A and of approximately 0.25 m is observed around borehole
595 heat exchanger B, which was not sufficient to cause a significant overlapping effect between
596 the two boreholes. Although not investigated, repeated cycles of heat injection and heat
597 removal may lead to greater zones of influence. Similar to the observations of Baser et al.
598 (2018), greater decreases in degree of saturation are observed for the locations with initially
599 greater degree of saturation and for greater changes in temperature, due to the effects of
600 enhanced vapor diffusion and phase change. Another interesting observation is that the
601 percent decrease in the thermal conductivity in Figure 18(b) is greater than the percent
602 decrease in the volumetric heat capacity in Figure 18(c). This has positive implications on the
603 performance of the heat storage systems as the lower thermal conductivity is expected to lead
604 to decrease in the heat loss from the system while the volumetric heat capacity reflects the
605 total heat that can be stored in the soil for a given increase in ground temperature.

606 Another comparison that can be made is the difference in the simulations expected for
607 the subsurface having thermo-hydraulic properties representative of unsaturated and saturated
608 conditions. When the subsurface is saturated, the governing equations in Table 1 are
609 significantly simplified. Heat transfer will occur primarily due to conduction, but natural
610 convection of the pore water will occur due to decreases in the density of water with

611 temperature. A comparison of the simulations for saturated and unsaturated conditions along
612 with the measured ground temperatures are shown in Figure 19 for a depth near the upper-
613 middle of the array at the location of borehole T-2. The temperature for saturated conditions
614 are generally lower, although they tend to rise sharply near the end of the heat injection
615 period, possibly due to upward water flow due to natural convection. Further comparisons of
616 the model for saturated and unsaturated conditions are shown in Baser et al. (2018) for the
617 case of a single geothermal heat exchanger.

618 **6. CONCLUSIONS**

619 This study focused on the simulation of transient heat transfer and water flow in a field-
620 scale SBTES system installed in the vadose zone. A non-isothermal, coupled heat transfer and
621 water flow model considering enhanced vapor diffusion and nonequilibrium phase change
622 calibrated in the laboratory using reconstituted specimens collected from the field was
623 validated by comparing simulated ground temperatures with those from field-scale SBTES
624 system during both heat injection and ambient cooling. In general, a good match was obtained
625 between the simulated and measured temperature data, reflecting the importance of
626 considering coupled heat transfer and water flow when simulating SBTES systems installed in
627 the vadose zone. During heat injection, ground temperatures were generally greater near the
628 surface in the borehole array, likely due to heat transfer due to buoyancy-driven vapor flow. At
629 the end of 5 months of ambient cooling, some heat was still retained within the array,
630 indicating that further heat injection and cooling cycles would lead to a positive effect on the
631 performance of this heat storage approach.

632 Differences between the simulation and measured data were likely due to differences in
633 how the heat injection boundary conditions were applied, the assumption of a homogenous
634 subsurface, the calibration of the model parameters using reconstituted specimens, and the
635 assumption regarding the depth of the water table (which may vary with time). Heat transfer
636 led to a clear overlapping effect between the closely-spaced geothermal borehole heat
637 exchangers in the SBTES system. However, the simulation results indicate that a significant
638 overlapping effect was not observed in terms of the changes in degree of saturation between
639 the geothermal borehole heat exchangers. Permanent decreases in degree of saturation were
640 observed at the locations of the geothermal heat exchangers, corresponding to a decrease in
641 thermal conductivity, but similar decreases in these variables were not observed in the bulk of
642 the subsurface between the geothermal borehole heat exchangers for the particular conditions
643 at the site. Further study on the effects of heating and cooling cycles of SBTES systems in the
644 vadose zone may better clarify the roles of thermo-hydraulic interaction between closely
645 spaced geothermal borehole heat exchangers for different subsurface materials.

646 **ACKNOWLEDGEMENTS**

647 Funding provided by National Science Foundation grant 1230237 is much appreciated.

648 The opinions presented here belong to authors alone.

649 **REFERENCES**

650 Akrouch, G.A., Sánchez, M., and Briaud, J.L. (2016). "An experimental, analytical and numerical
651 study on the thermal efficiency of energy piles in unsaturated soils." *Computers and*
652 *Geotechnics*. 71, 207-220.

653 Baser, T. and McCartney, J.S. (2015a). "Development of a full-scale soil-borehole thermal
654 energy storage system." Proc. Int. Foundation Conference and Equipment Exposition
655 (IFCEE 2015). ASCE, Reston, VA. pp. 1608-1617.

656 Başer, T. and McCartney, J.S. (2015b). "Thermal energy storage in borehole arrays." Symposium
657 on Energy Geotechnics. Barcelona. Jun. 2-4. pp. 1-2.

658 Baser, T., Lu, N., and McCartney, J.S. (2016a). "Operational response of a soil-borehole thermal
659 energy storage system." ASCE Journal of Geotechnical and Geoenvironmental
660 Engineering. 04015097-1-12. 10.1061/(ASCE)GT.1943-5606.0001432.

661 Baser, T., McCartney, J.S., Moradi, A., Smits, K., and Lu, N. (2016b). "Effect of a thermo-
662 hydraulic insulating layer on the long-term response of soil-borehole thermal energy
663 storage systems". GeoChicago 2016: Sustainability, Energy and the Geoenvironment.
664 Chicago. Aug. 14-18. ASCE, Reston, VA. pp. 125-134.

665 Baser, T., Dong, Y., and McCartney, J.S. (2016c). "Heat content in soil-borehole thermal energy
666 systems in the vadose zone." ICEGT 2016: 1st International Conference on Energy
667 Geotechnics. Kiel. CRC Press, Boca Raton. pp. 195-202.

668 Baser, T., Dong, Y., Lu, N., and McCartney, J.S. (2016d). "Role of considering non-constant soil
669 thermal parameters in the simulation of geothermal heat storage systems in the vadose
670 zone". Proceedings. 8th Asian Young Geotechnical Engineers Conference 2016 (AYGEC
671 2016). Kazakh Geotechnical Society. Astana. pp. 1-6.

672 Başer, T., Dong, Y., Moradi, A.M., Lu, N., Smits, K., Ge, S., Tartakovsky, D., and McCartney, J.S.
673 (2018). "Role of water vapor diffusion and nonequilibrium phase change in geothermal

674 energy storage systems in the vadose zone.” Journal of Geotechnical and
675 Geoenvironmental Engineering. 10.1061/(ASCE)GT.1943-5606.0001910.

676 Baser, T., Hanna, C., and McCartney, J.S. (2019). “Performance of a field-scale shallow
677 horizontal thermal energy storage system.” Geo-Congress 2019: The 8th International
678 Conference on Case Histories in Geotechnical Engineering. Philadelphia, PA. Mar. 24-27.
679 1-10. Accepted.

680 Bear, J. (1972). Dynamics of Fluids in Porous Media. Dover, Mineola, N.Y., 764.

681 Bjoern, H. (2013). “Borehole thermal energy storage in combination with district heating.” EGC
682 2013. Pisa. June 3-7. 1-13.

683 Bixler, N.E. (1985). NORIA: “A Finite Element Computer Program for Analyzing Water, Vapor, Air
684 and Energy Transport in Porous Media.” SAND84-2057, Sandia National Laboratories,
685 Albuquerque, NM.

686 Campbell, G.S. (1985). Soil Physics with BASIC: Transport Models for Soil–Plant Systems.
687 Elsevier, New York.

688 Campbell, G.S., Jungbauer, J.D., Bidlake, W.R., and Hungerford, R.D. (1994). “Predicting the
689 effect of temperature on soil thermal conductivity.” Soil Science. 158, 307–313.

690 Cass, A., Campbell, G.S., and Jones. T.L. (1984.) “Enhancement of thermal water vapor diffusion
691 in soil.” Soil Science Society of America. 48(1), 25–32.

692 Catolico, N., Ge, S., and McCartney, J.S. (2016). “Numerical modeling of a soil-borehole thermal
693 energy storage system.” Vadose Zone Hydrology. 1-17.doi:10.2136/vzj2015.05.0078.

694 Choi, J.S., Lee, S.R., and Lee, D.S. (2011). "Numerical simulation of vertical ground heat
695 exchangers: Intermittent operation in unsaturated soil conditions." *Computers and*
696 *Geotechnics*. 38, 949-958.

697 Claesson, J. and Hellström G. (1981). "Model studies of duct storage systems." *New Energy*
698 *Conservation Technologies and their Commercialization*. J.P. Millhone and E.H. Willis,
699 Eds. Springer-Verlag, Berlin. 762-778.

700 COMSOL Multiphysics® v. 5.2. (2015). COMSOL AB, Stockholm, Sweden.

701 Ewen, J. and Thomas, H.R. (1989). "Heating unsaturated medium sand." *Géotechnique*. 39(3),
702 455-470.

703 Gens, A., Garcia Molina, A., Olivella, S., Alonso, E.E., and Huertas, F. (1998). "Analysis of a full
704 scale in-situ test simulating repository conditions." *International Journal of Numerical*
705 *and Analytical Methods in Geomechanics*. 22(7), 515-48.

706 Gens, A, Sanchez, M., Guimaraes L., and Huertas, F. (2009). "A full-scale in situ heating test for
707 high-level nuclear waste disposal: Observations, analysis and interpretation."
708 *Géotechnique*, 59(4), 377-399.

709 Grant, S.A. and Salehzadeh, A. (1996). Calculations of temperature effects on wetting
710 coefficients of porous solids and their capillary pressure functions. *Water Resources Res.*
711 32(2), 261-279.

712 Hillel, D. (1980). *Fundamental of Soil Physics*. Academic, San Diego, CA.

713 Iezzoni, H. M. and McCartney, J.S. (2016). "Calibration of Capacitance Sensors for Compacted
714 Silt in Non-Isothermal Applications." *Geotechnical Testing Journal*, Vol. 39(2), 169-180.

715 Lide, D.R. (Ed.) (2001). *Handbook of Chemistry and Physics*, CRC Press, Boca Raton, FL.

716 Lu, N. and Dong, Y. (2015). "A closed form equation for thermal conductivity of unsaturated
717 soils at room temperature." *Journal of Geotechnical and Geoenvironmental*
718 *Engineering*. 141(6), 04015016.

719 Marcotte, D. and Pasquier, P. (2014). "Unit-response function for ground heat exchanger with
720 parallel, series or mixed borehole arrangement." *Renewable Energy*. 68, 14–24.

721 McCartney, J.S., Ge, S., Reed, A., Lu, N., and Smits, K. (2013). "Soil-borehole thermal energy
722 storage systems for district heating." *Proceedings of the European Geothermal Congress*
723 *2013*. Pisa. Jun. 3-7. pp. 1-10.

724 Millington, R.J., and Quirk, J.M. (1961). "Permeability of porous solids." *Trans. Faraday Soc.* 57,
725 1200–1207.

726 Moradi, A.M., Smits, K., Lu, N., and McCartney, J.S. (2016). "3-D experimental and numerical
727 investigation of heat transfer in unsaturated soil with an application to soil borehole
728 thermal energy storage (SBTES) systems." *Vadose Zone J.* 15(10), 1-17.

729 Nguyen, A., Pasquier, P., and Marcotte, D. (2017). "Borehole thermal energy storage systems
730 under the influence of groundwater flow and time-varying surface temperature."
731 *Geothermics*. 66, 110-118.

732 Nordell, B. and Hellström, G. (2000). "High temperature solar heated seasonal storage system
733 for low temperature heating of buildings." *Applied Energy*. 69(6), 511–523.

734 Nussbicker-Lux, J. (2012). "The BTES project in Crailsheim (Germany) – Monitoring results."
735 *Proc. 12th Int. Conf. on Energy Storage – Innostock*. IEA Press, Paris. 1-10.

736 Sibbitt, B., McClenahan, D., Djebbar, R., Thornton, J., Wong, B., Carriere, J., Kokko, J. (2012).
737 "The performance of a high solar fraction seasonal storage district heating system - Five
738 years of operation." *Energy Procedia*. 30, 856-865.

739 Smits, K.M., Cihan, A., Sakaki, S., and Illangasekare, T.H. (2011). "Evaporation from soils under
740 thermal boundary conditions: Experimental and modeling investigation to compare
741 equilibrium- and nonequilibrium-based approaches." *Water Resources Research*. 47,
742 W05540, doi:10.1029/2010WR009533.

743 Thomas, H.R. and Sansom, M.R. (1995). "Fully coupled heat, moisture, and air transfer in an
744 unsaturated soil." *J Eng Mech* 1995;12(3):392–405.

745 Thomas, H.R. and Rees, S.W. (2009). "Measured and simulated heat transfer to foundation
746 soils." *Géotechnique*. 59(4), 365–375.

747 van Genuchten, M.T. (1980). "A closed-form equation for predicting the hydraulic conductivity
748 of unsaturated soils." *Soil Sci. Soc. Am. J.* 44(5), 892–898.

749 Wayllace, A. and Lu, N. (2012). "A transient water release and imbibitions method for rapidly
750 measuring wetting and drying soil water retention and hydraulic conductivity functions."
751 *Geotechnical Testing Journal*. 35(1), 103-117.

752 Welsch, B., Rühaak, W., Schulte, D.O., Bär, K., Homuth, S., and Sass, I. (2015). "Comparative
753 study of medium deep borehole thermal energy storage systems using numerical
754 modelling." *Proc. World Geothermal Congress 2015*. International Geothermal
755 Association. Bochum. 1-6.

756 Whitaker, S. (1977). "Simultaneous heat, mass and momentum transfer in porous media: A
757 theory of drying porous media." *Adv. Heat Transf.* 13, 119–203.

758 **TABLE 1.** Equations used in the numerical analyses

Equation	Number	Reference
<p><i>Nonisothermal liquid flow governing equation:</i></p> $nS_{rw} \frac{\partial \rho_w}{\partial t} + n\rho_w \frac{dS_{rw}}{dP_c} \frac{\partial P_c}{\partial t} + \nabla \cdot \left[\rho_w \left(-\frac{k_{rw}\kappa}{\mu_w} \right) \nabla (P_w + \rho_w g z) \right] = -R_{gw}$ <p>n=porosity (m³/m³), S_{rw}=degree of water saturation (m³/m³), ρ_w=temperature-dependent density of water (kg/m³) (Hillel 1980), t=time(s), P_c=P_w-P_g=capillary pressure (Pa), P_w=pore water pressure (Pa), P_g=pore gas pressure (Pa), k_{rw}=relative permeability function for water (m/s); κ=intrinsic permeability (m²); μ_w=temperature-dependent water dynamic viscosity (kg/(ms)) (Lide 2001), g=acceleration due to gravity (m/s²) R_{gw}=Phase change rate (kg/m³s)</p>	(1)	(Bear 1972; Moradi et al. 2016)
<p><i>Nonisothermal gas flow governing equation:</i></p> $nS_{rg} \frac{\partial \rho_g}{\partial t} + n\rho_g \frac{dS_{rg}}{dP_c} \frac{\partial P_c}{\partial t} + \nabla \cdot \left[\rho_g \left(-\frac{k_{rg}\kappa}{\mu_g} \right) \nabla (P_g + \rho_g g z) \right] = R_{gw}$ <p>S_{rg}=degree of gas saturation (m³/m³), ρ_g=temperature-dependent density of gas (kg/m³) (Smits et al. 2011), k_{rg}=relative permeability function for gas (m/s); μ_g=temperature-dependent gas dynamic viscosity (kg/(ms))</p>	(2)	(Bear 1972; Moradi et al. 2016)
<p><i>Water vapor mass balance equation:</i></p> $n \frac{\partial (\rho_g S_{rg} w_v)}{\partial t} + \nabla \cdot (\rho_g u_g w_v - D_e \rho_g \nabla w_v) = R_{gw}$ <p>D_e=D_vτ=effective diffusion coefficient (m²/s), D_v=diffusion coefficient of water vapor in air (m²/s) (Campbell 1985), w_v=mass fraction of water vapor in the gas phase (kg/kg), τ=n^{1/3}S_{rg}^{7/3}η=tortuosity (Millington and Quirk 1961)</p>	(3)	(Smits et al. 2011)
<p><i>Enhancement factor for vapor diffusion, η:</i></p> $\eta = a + 3S_{rw} - (a-1) \exp \left\{ - \left[\left(1 + \frac{2.6}{\sqrt{f_c}} \right) S_{rw} \right]^3 \right\}$ <p>a=empirical fitting parameter representing the soil-specific enhancement in vapor diffusion, f_c= clay content</p>	(4)	(Cass et al. 1984)
<p><i>Nonequilibrium phase change rate, R_{gw}:</i></p> $R_{gw} = \left(\frac{bS_{rw} RT}{M_w} \right) (\rho_{veq} - \rho_v)$ <p>b=empirical fitting parameter representing the soil-specific nonequilibrium phase change rate (s/m²), R=universal gas constant (J/molK), ρ_{veq}=equilibrium vapor density (kg/m³) (Campbell 1985), T=Temperature (K), ρ_v=vapor density (kg/m³), M_w=molecular weight of water (kg/mol)</p>	(5)	(Bixler 1985; Moradi et al. 2016)
<p><i>Heat transfer energy balance:</i></p> $(\rho C_p) \frac{\partial T}{\partial t} + \nabla \cdot ((\rho_w C_{pw}) u_w T + (\rho_g C_{pg}) u_g T - (\lambda \nabla T)) = -LR_{gw} + Q$ <p>ρ=total density of soil (kg/m³), C_p=specific heat of soil (J/kgK), C_{pw}=specific heat capacity of water (J/kgK), C_{pg}=specific heat capacity of gas (J/kgK), λ=thermal conductivity (W/mK), L=latent heat due to phase change (J/kg), u_w=water velocity (m/s), u_g=gas velocity (m/s), Q=heat source (W/m³)</p>	(6)	(Whitaker 1977; Moradi et al. 2016)

761 **TABLE 2.** Constitutive models used in the numerical analyses

Equation	Number	Reference
<p><i>Soil Water Retention Curve (SWRC):</i></p> $S_{rw} = S_{rw,res} + (1 - S_{rw,res}) \left[\frac{1}{1 + (\alpha_{vG} P_c(T))^{NvG}} \right]^{1-1/NvG}$ <p>where $S_{rw,res}$ is the residual degree of saturation to water, α_{vG} and NvG are parameters representing the air entry pressure and the pore size distribution, respectively, and $P_c(T)$ is the temperature-corrected capillary pressure according to the model of Grant and Salehzadeh (1996)</p>	(7)	(van Genuchten 1980)
<p><i>Hydraulic Conductivity Function (HCF):</i></p> $k_{rw} = \sqrt{\left(\frac{S_{rw} - S_{rw,res}}{1 - S_{rw,res}} \right) \left[1 - \left(1 - \left(\frac{S_{rw} - S_{rw,res}}{1 - S_{rw,res}} \right)^{1/(1-1/NvG)} \right)^{1-1/NvG} \right]^2}$ <p>where α_{vG} and NvG are the same parameters as in Equation (7)</p>	(8)	(van Genuchten 1980; Mualem 1970)
<p><i>Thermal Conductivity Function (TCF):</i></p> $\frac{\lambda - \lambda_{dry}}{\lambda_{sat} - \lambda_{dry}} = 1 - \left[1 + \left(\frac{S_e}{S_f} \right)^m \right]^{1/m-1}$ <p>where λ_{dry} and λ_{sat} are the thermal conductivities of dry and saturated soil specimens, respectively, S_e is the effective saturation, S_f is the effective saturation at which the funicular regime is onset, and m is defined as the pore fluid network connectivity parameter for thermal conductivity</p>	(9)	(Lu and Dong 2015)
<p><i>Volumetric Heat Capacity Function (VHCF):</i></p> $\frac{C_v - C_{vdry}}{C_{vsat} - C_{vdry}} = 1 - \left[1 + \left(\frac{S_e}{S_f} \right)^m \right]^{1/m-1}$ <p>where C_{vdry} and C_{vsat} are the volumetric heat capacities of dry and saturated soil, respectively, and are similarly treated as fitting parameters, and S_f and m are the same parameters as in Equation (9)</p>	(10)	(Baser et al. 2016b)

762

763

764 **LIST OF FIGURE CAPTIONS**

765 **FIG. 1.** Coupled thermo-hydraulic constitutive relationships for the UCSD conglomerate: (a) SWRC and
766 HCF; (b) TCF and VHCF

767 **FIG. 2.** Schematic of the compaction mold used for calibration of water vapor diffusion and phase
768 change parameters along with the location of the embedded sensor and its zone of influence

769 **FIG. 3.** Calibration of the numerical model parameters using the heating test on compacted soil (soil
770 values at the depth of the dielectric sensor in Fig. 2): (a) Temperature; (b) Degree of saturation

771 **FIG. 4.** Experimental setup for the SBTES system: (a) Plan view; (b) Elevation view

772 **FIG. 5.** Photos of the SBTES system: (a) Excavation with borehole connections; (b) Hydraulic barrier;
773 (c) Insulation layer

774 **FIG. 6.** Plan view of the BTES and the simulated model domain (temperature sensors in boreholes 1, 2,
775 3, and 4, heat exchangers in boreholes A through M)

776 **FIG. 7.** Initial and boundary conditions on the quarter domain model for a field-scale geothermal heat
777 exchanger (JC is mass flux, distances in meters): (a) Thermal; (b) Hydraulic

778 **FIG. 8.** Thermal input boundary conditions to the SBTES system: (a) Ambient air temperature; (b) Solar
779 thermal heat transfer rates; (c) Close-up of daily solar thermal heat transfer rates; (d) Energy
780 balance

781 **FIG. 9.** Picture of borehole heat exchanger configuration highlighting heat injection sequence into Loops
782 1, 2, and 3 (Note: picture taken before inlet/outlet connections to manifold installed);

783 **FIG. 10.** Vertical SBTES loop heat transfer rates used in the calculations of the individual borehole
784 boundary conditions: (a) Loop 1; (b) Loop 2; (c) Loop 3

785 **FIG. 11.** Predicted and measured temperature time series from thermistor string T-1 for different depths
786 (z): (a) 16.00m; (b) 14.78m; (c) 12.95m; (d) 9.29m; (e) 6.85m; (f) 1.82m

787 **FIG. 12.** Predicted and measured temperature time series from thermistor string T-2 for different depths
788 (z): (a) 16.00m; (b) 14.78m; (c) 12.95m; (d) 9.29m; (e) 6.85m; (f) 1.82m

789 **FIG. 13.** Predicted and measured temperature time series from thermistor string T-3 for different depths
790 (z): (a) 16.00 m; (b) 14.78 m; (c) 12.95 m; (d) 9.29 m; (e) 6.85 m; (f) 1.82 m

791 **FIG. 14.** Predicted and measured temperature time series from thermistor string T-4 for different depths
792 (z): (a) 16.00 m; (b) 14.78 m; (c) 12.95 m; (d) 9.29 m; (e) 6.85 m; (f) 1.82 m

793 **FIG. 15.** Radial temperature profiles at different depths (z): (a) At the end of heating; (b) After 5 months
794 of ambient cooling

795 **FIG. 16.** Temperature profiles along the borehole length: (a) Borehole 2; (b) Borehole 4

796 **FIG. 17.** Time series of predicted degrees of saturation at the radial locations of: (a) Borehole 3;
797 (b) Borehole 2

798 **FIG. 18.** Radial profiles of predicted values at the end of heating: (a) Degree of saturation; (b) Thermal
799 conductivity; (c) Volumetric heat capacity

800 **FIG. 19.** Comparison of the transient temperature response of the subsurface having thermo-hydraulic
801 properties representative of saturated and unsaturated conditions

Figure 1

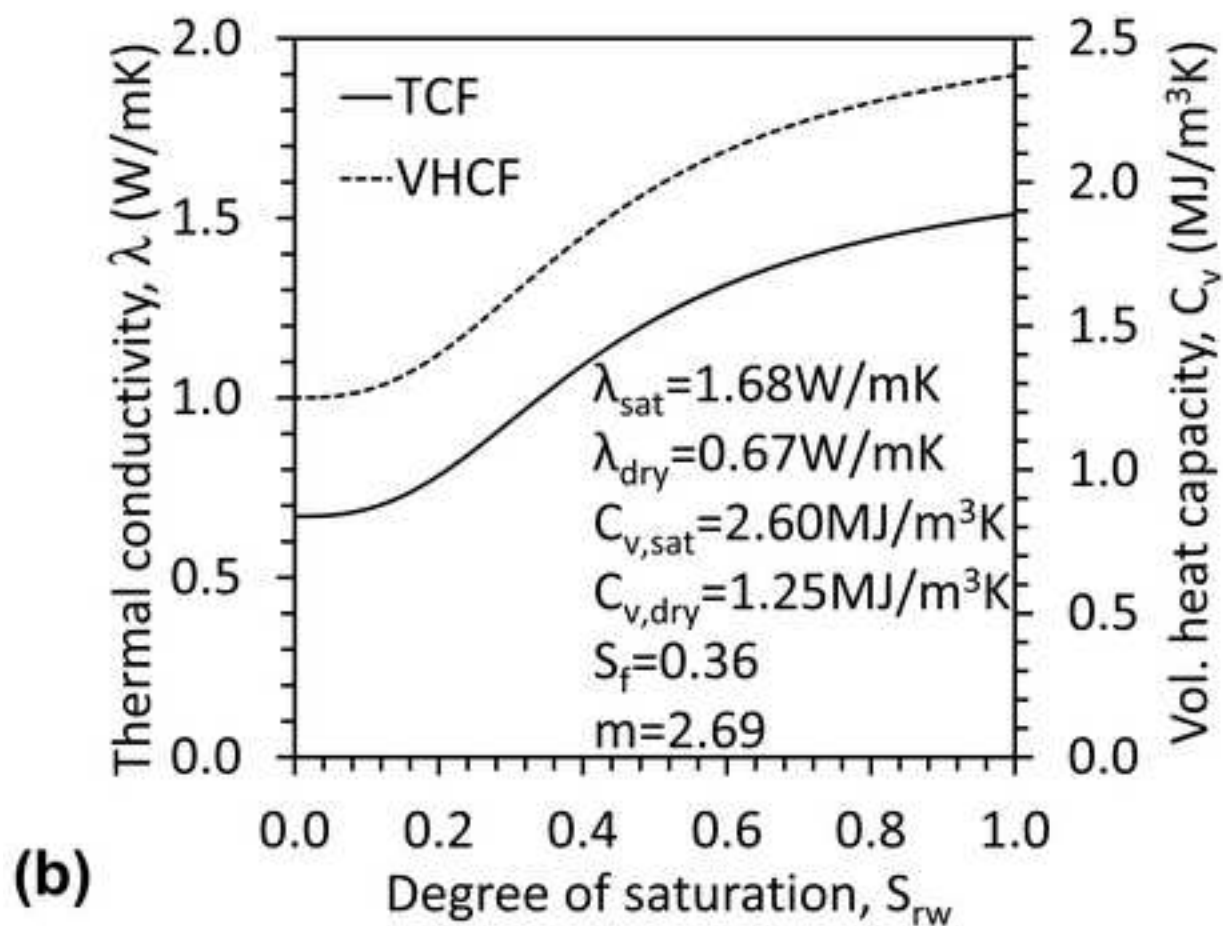
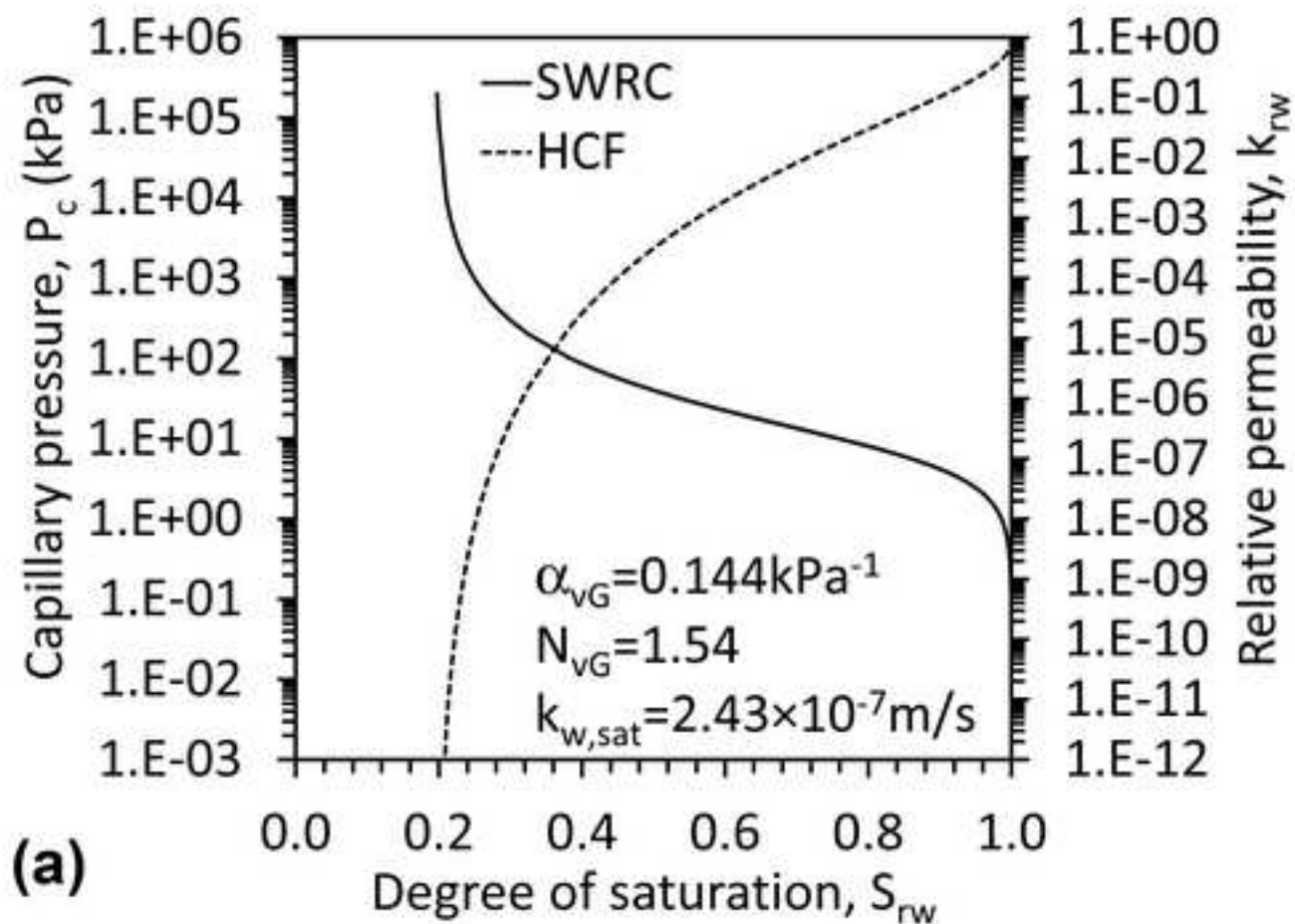
[Click here to download high resolution image](#)

Figure 2
[Click here to download high resolution image](#)

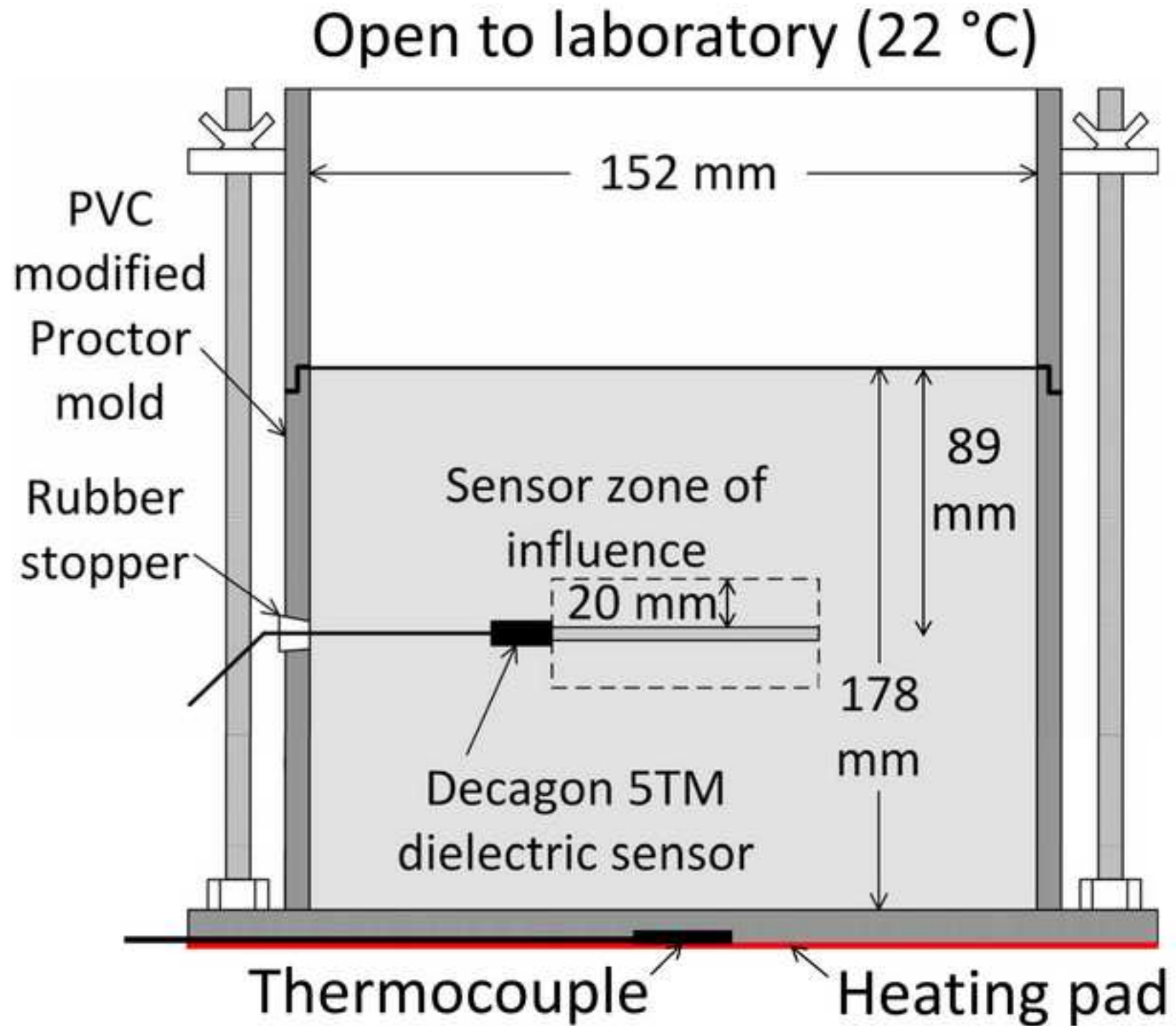
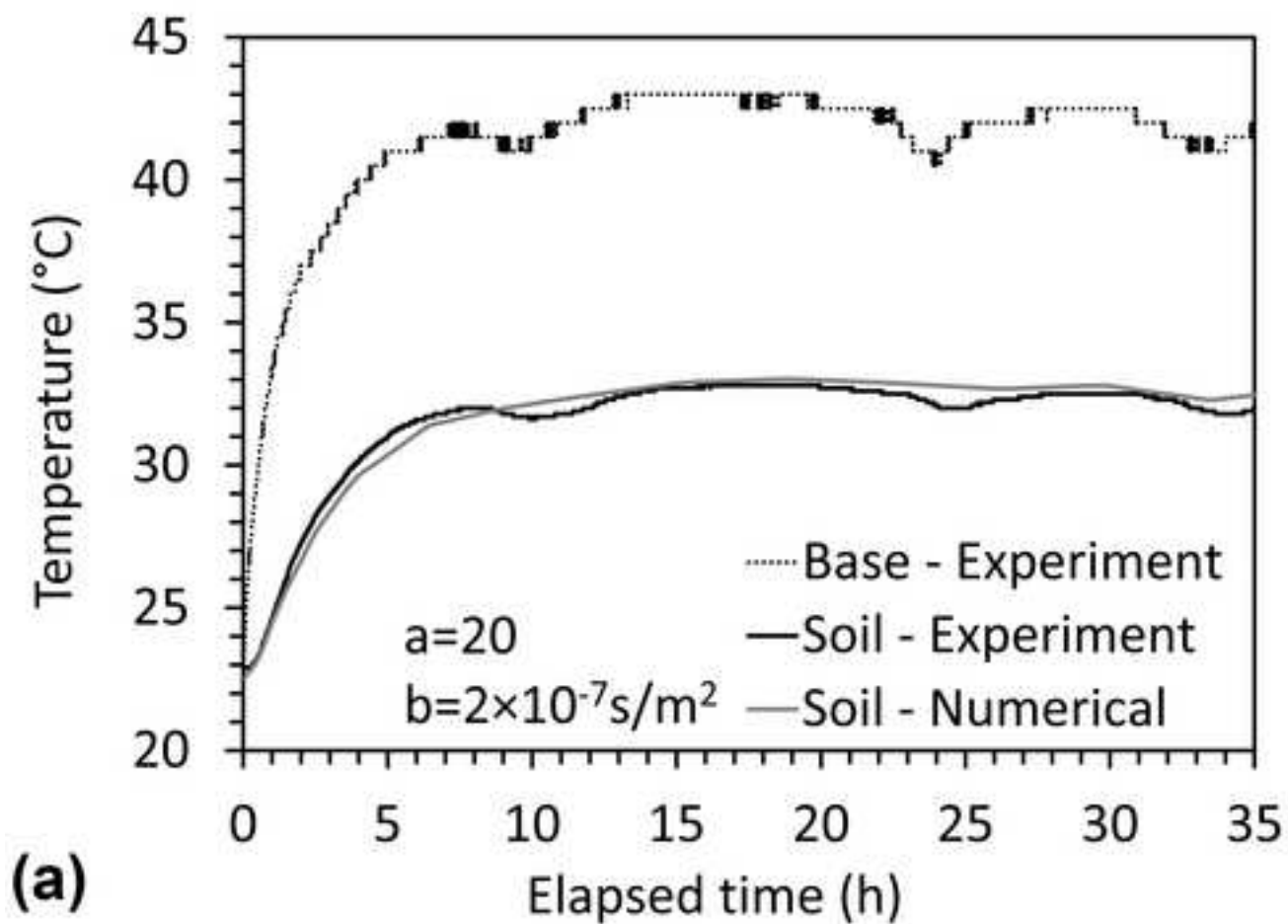
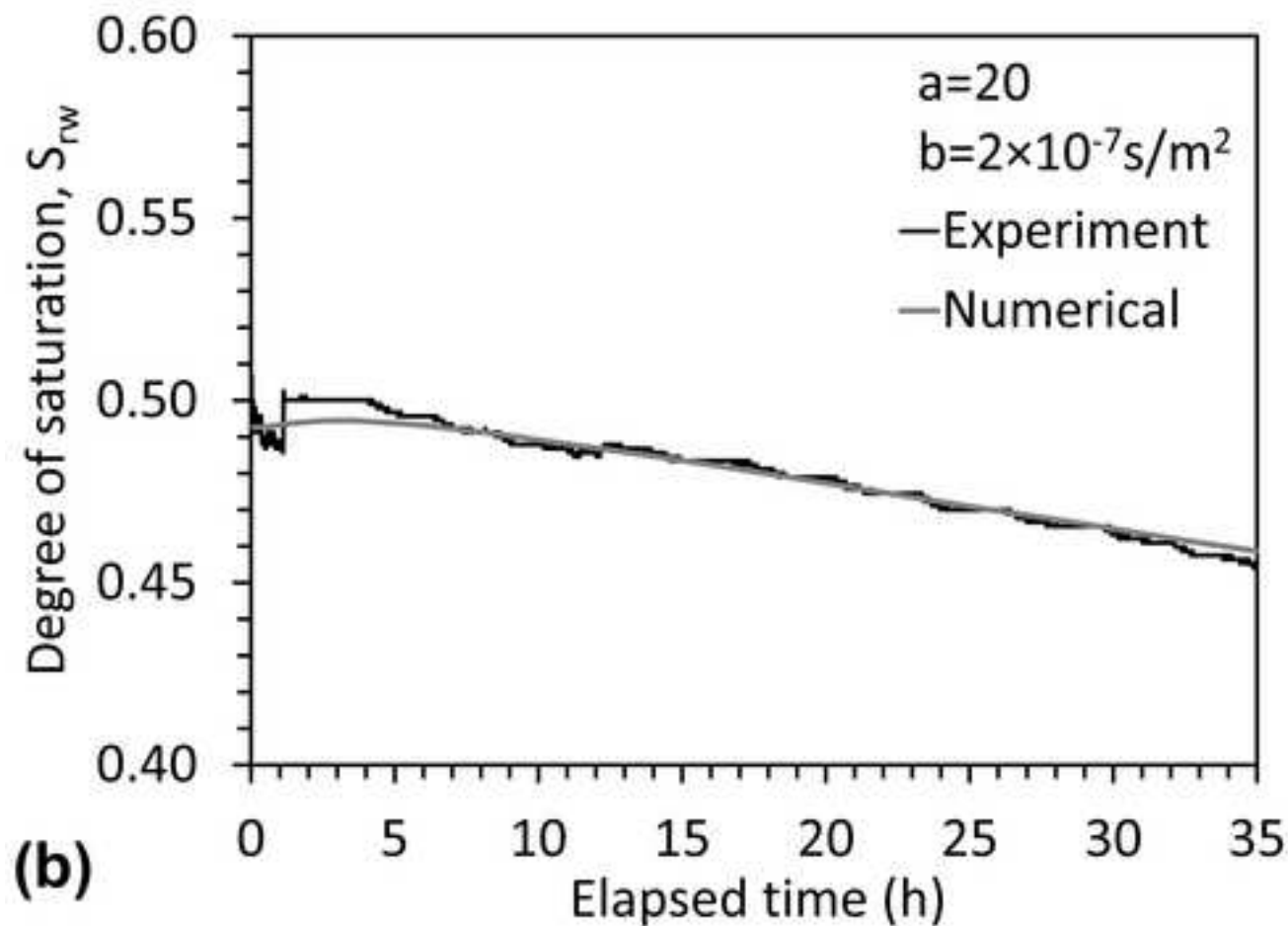


Figure 3
[Click here to download high resolution image](#)



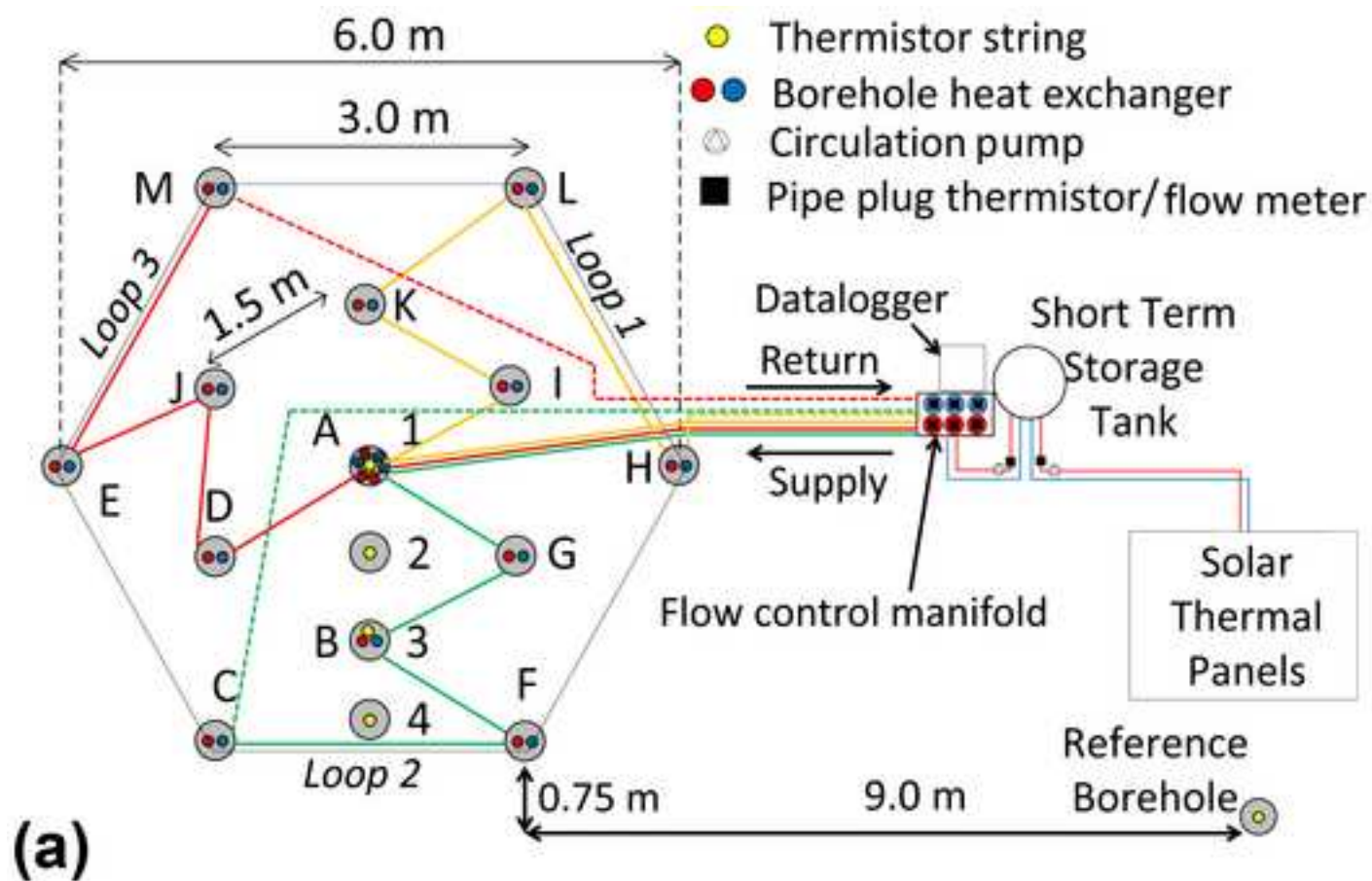
(a)



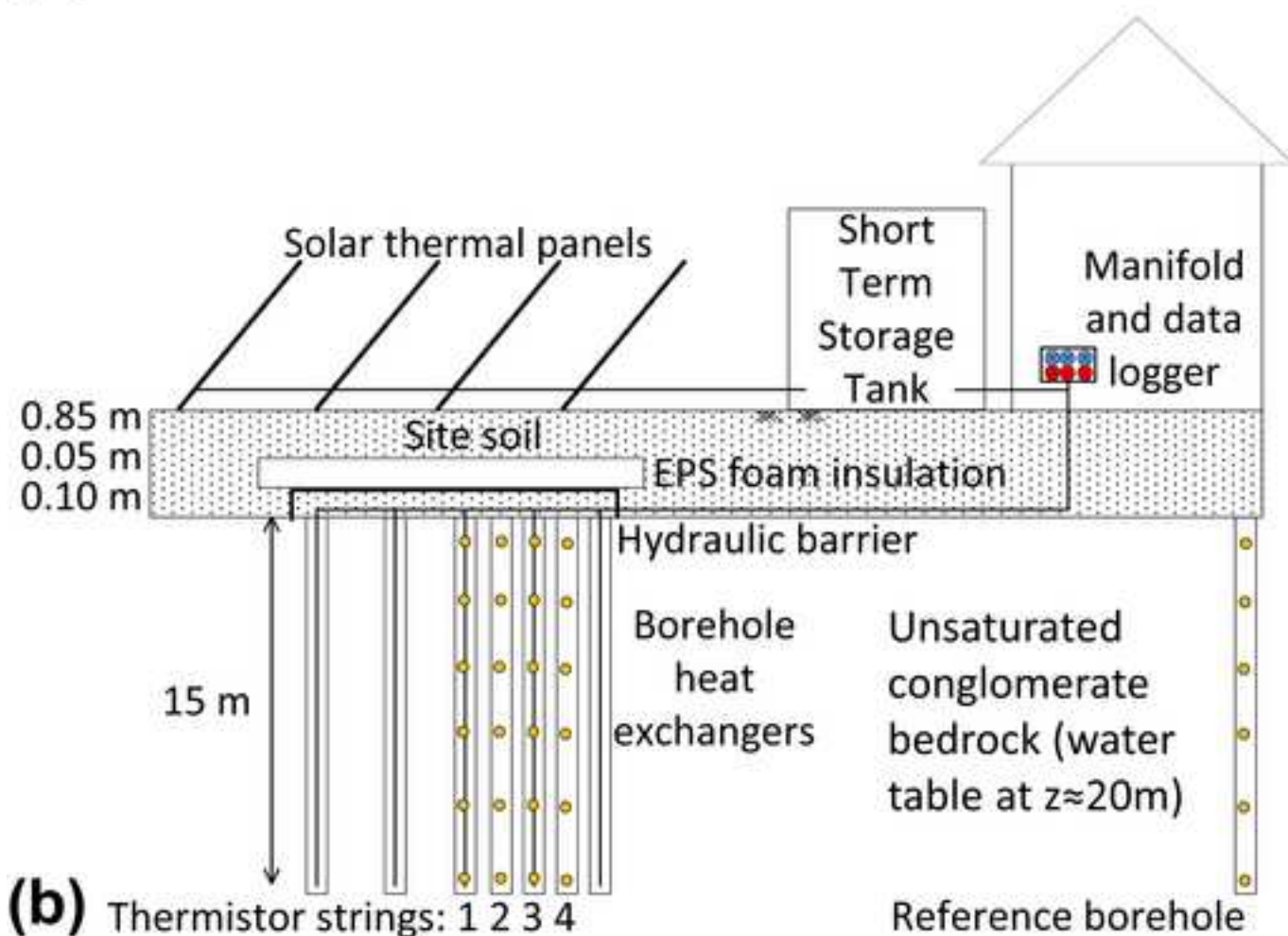
(b)

Figure 4

[Click here to download high resolution image](#)



(a)



(b)

Figure 5
[Click here to download high resolution image](#)



(a)



(c)



(b)



(d)

Figure 6
[Click here to download high resolution image](#)

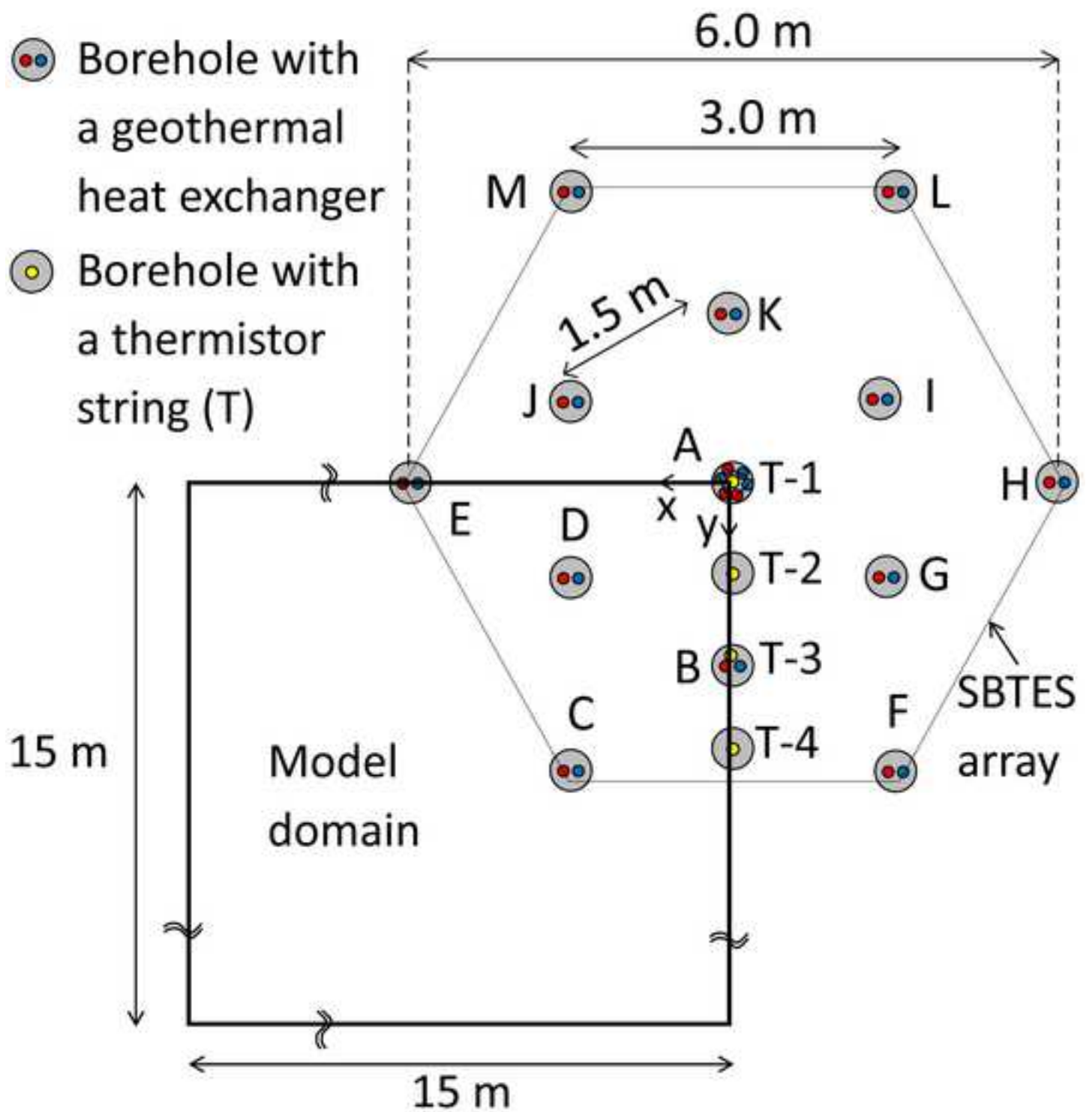


Figure 7
[Click here to download high resolution image](#)

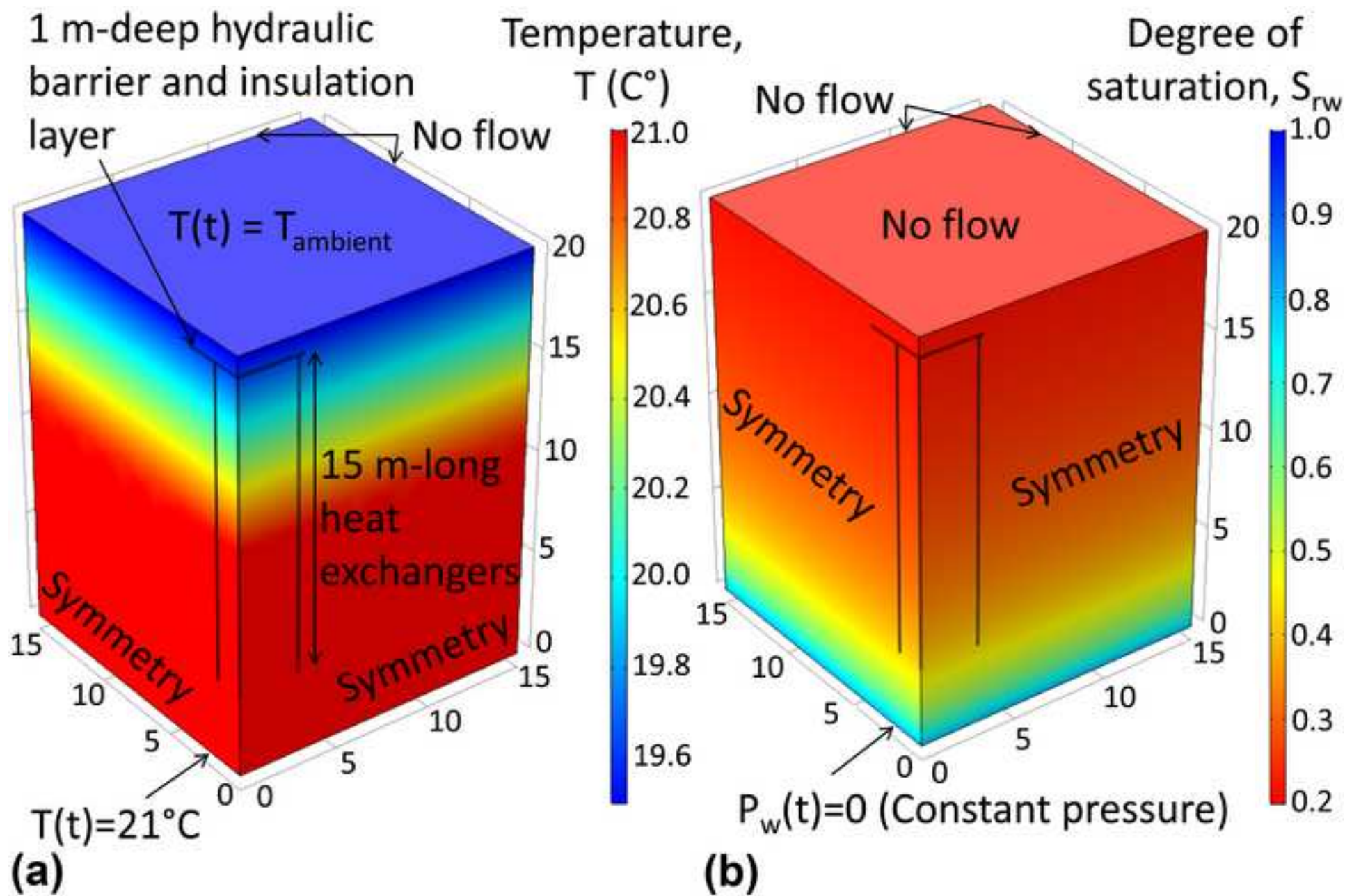


Figure 8
[Click here to download high resolution image](#)

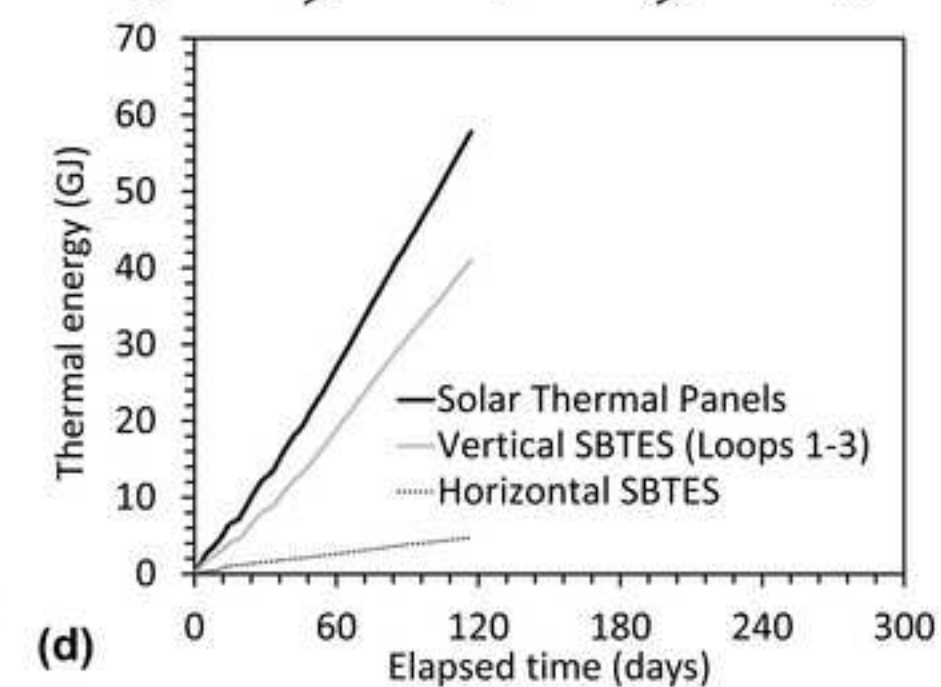
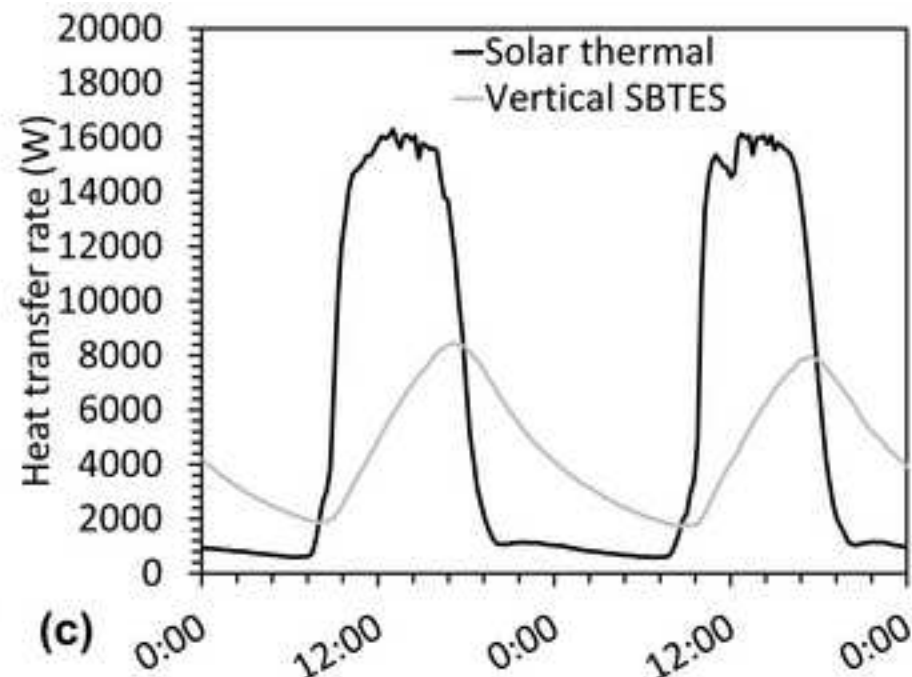
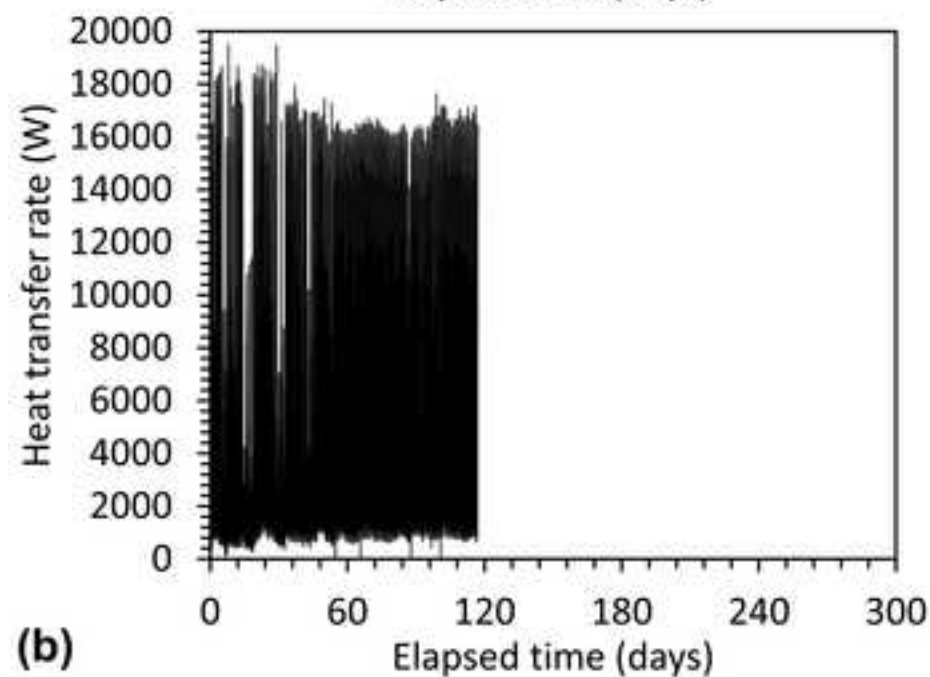
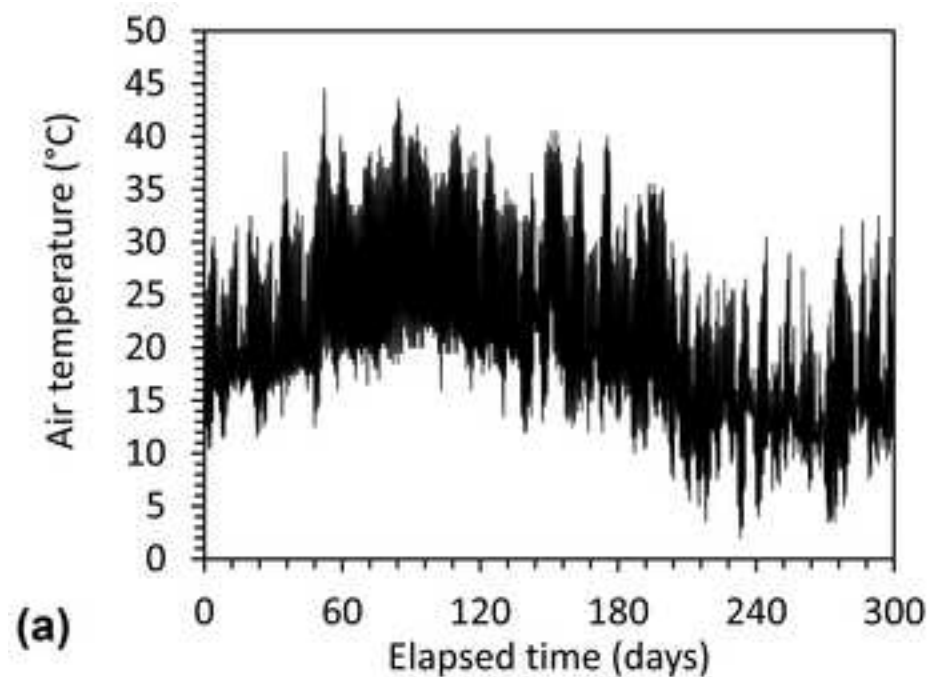


Figure 9
[Click here to download high resolution image](#)

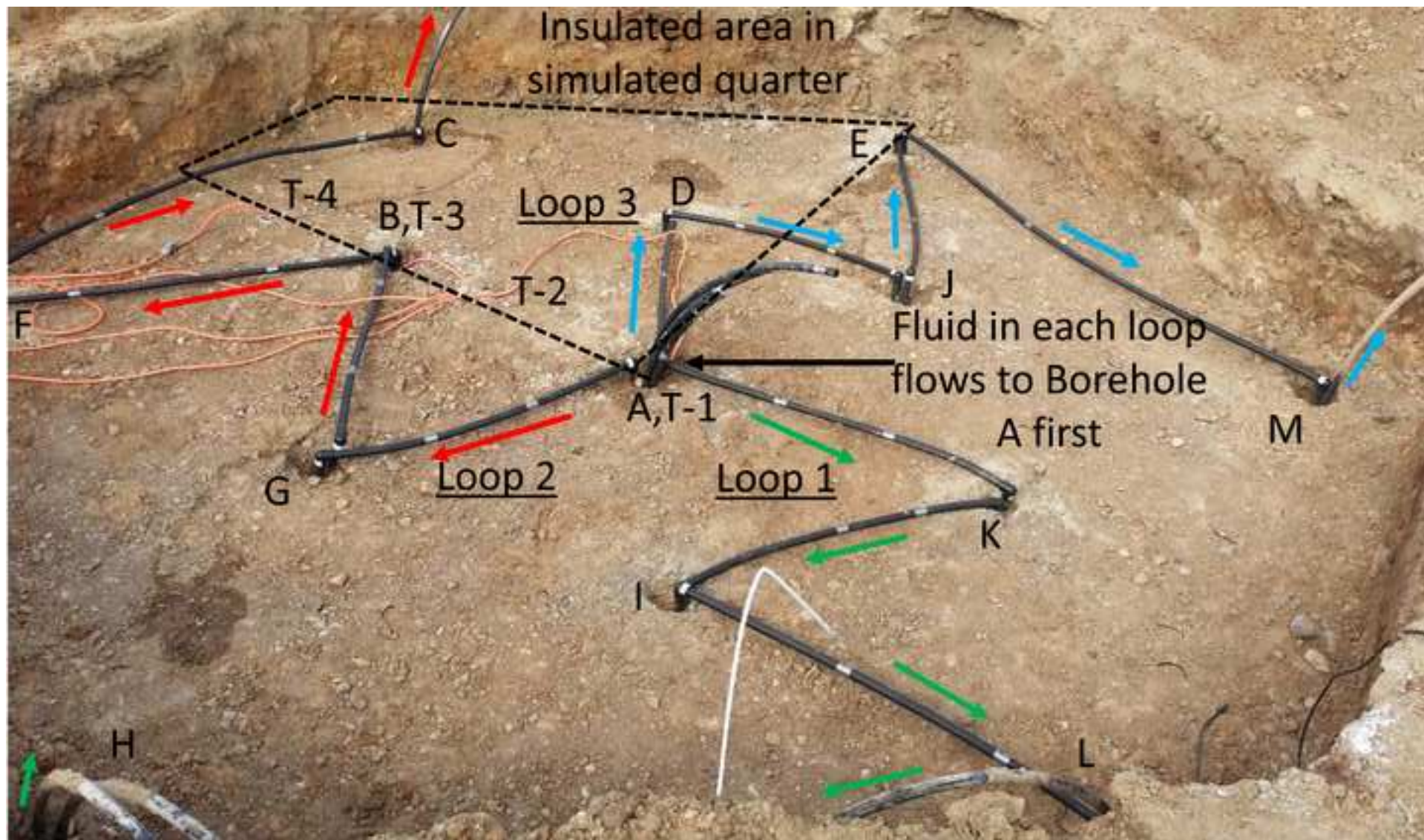


Figure 10

[Click here to download high resolution image](#)

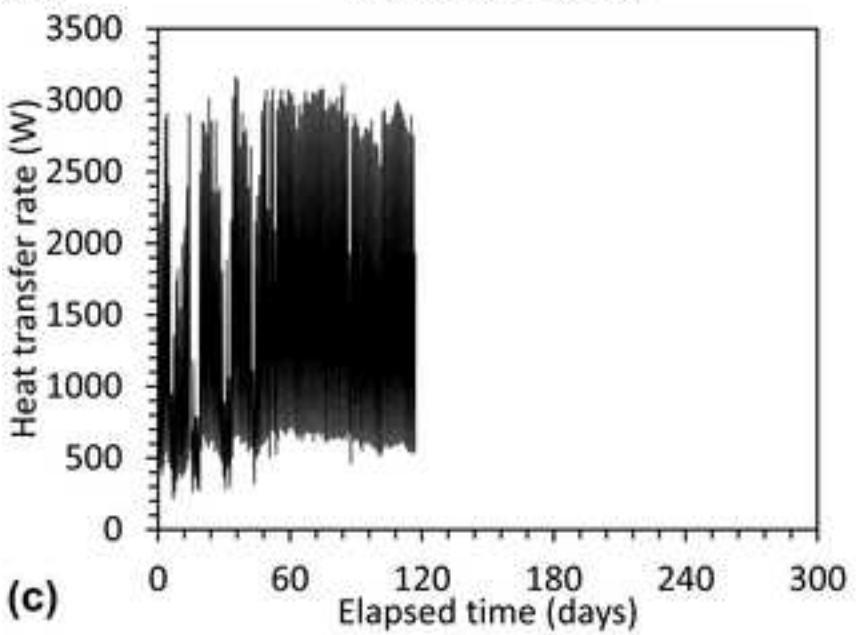
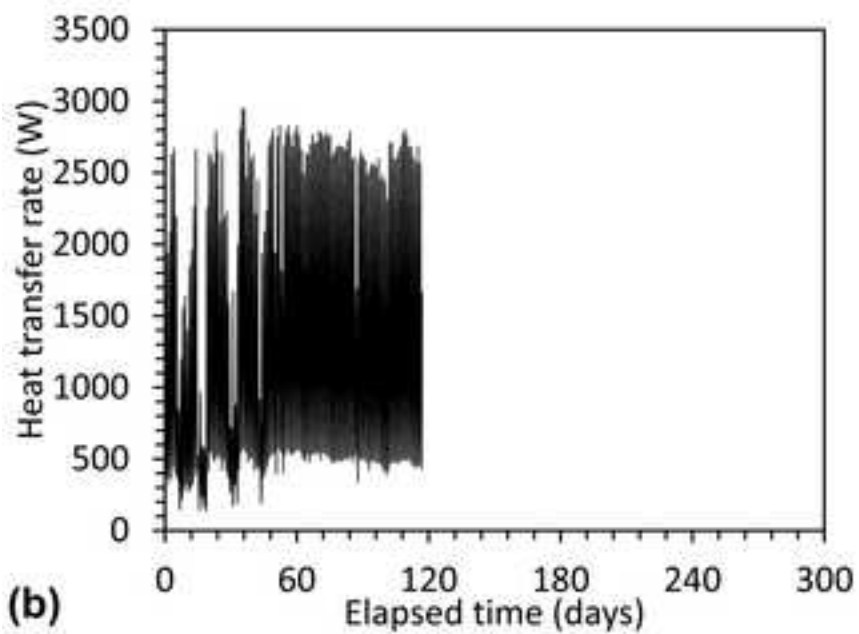
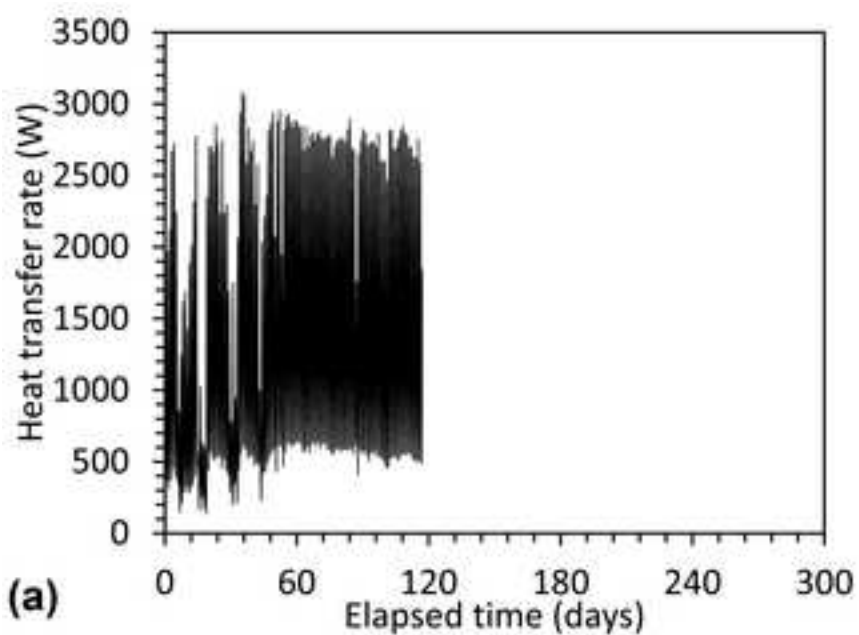


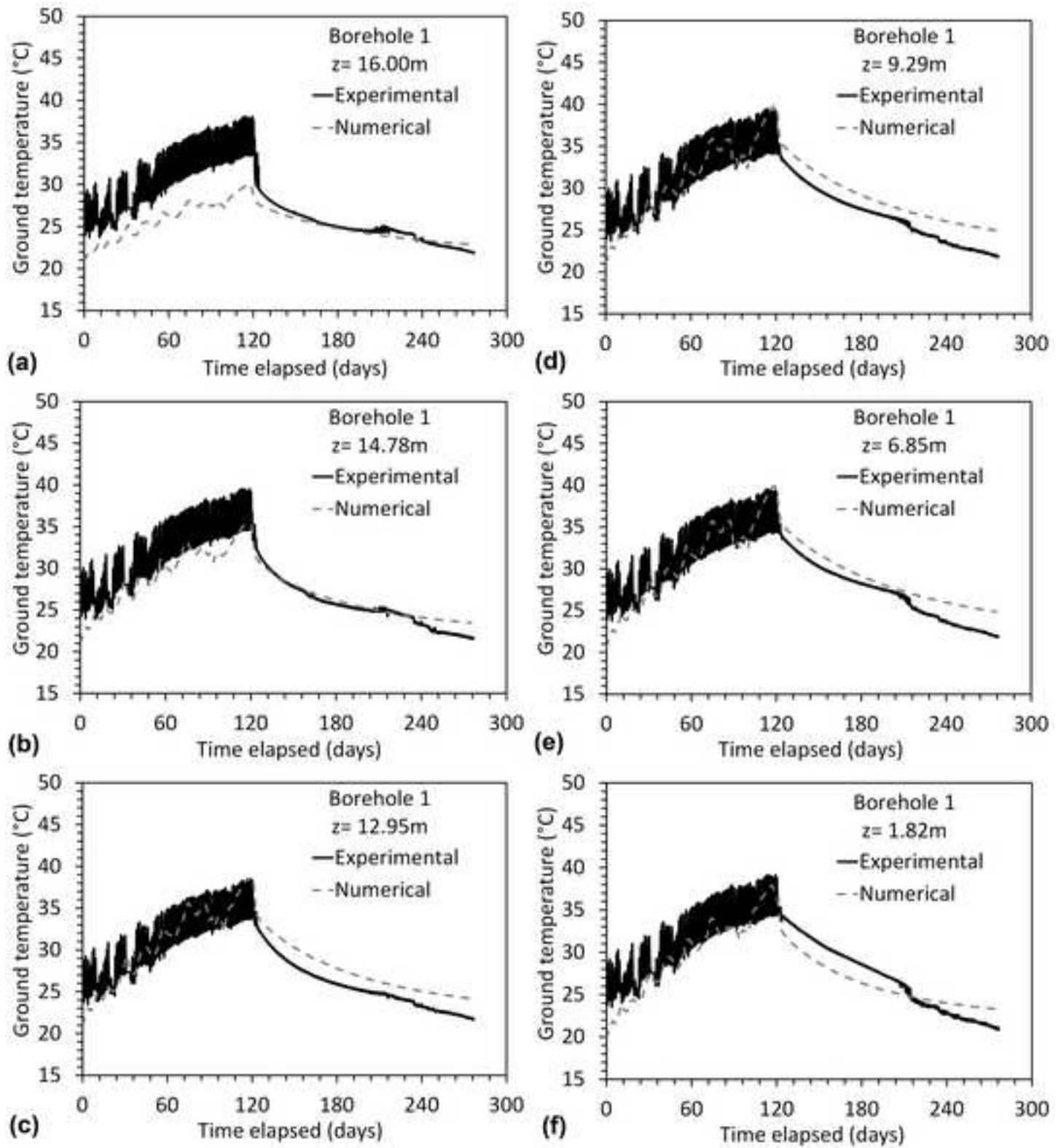
Figure 11[Click here to download high resolution image](#)

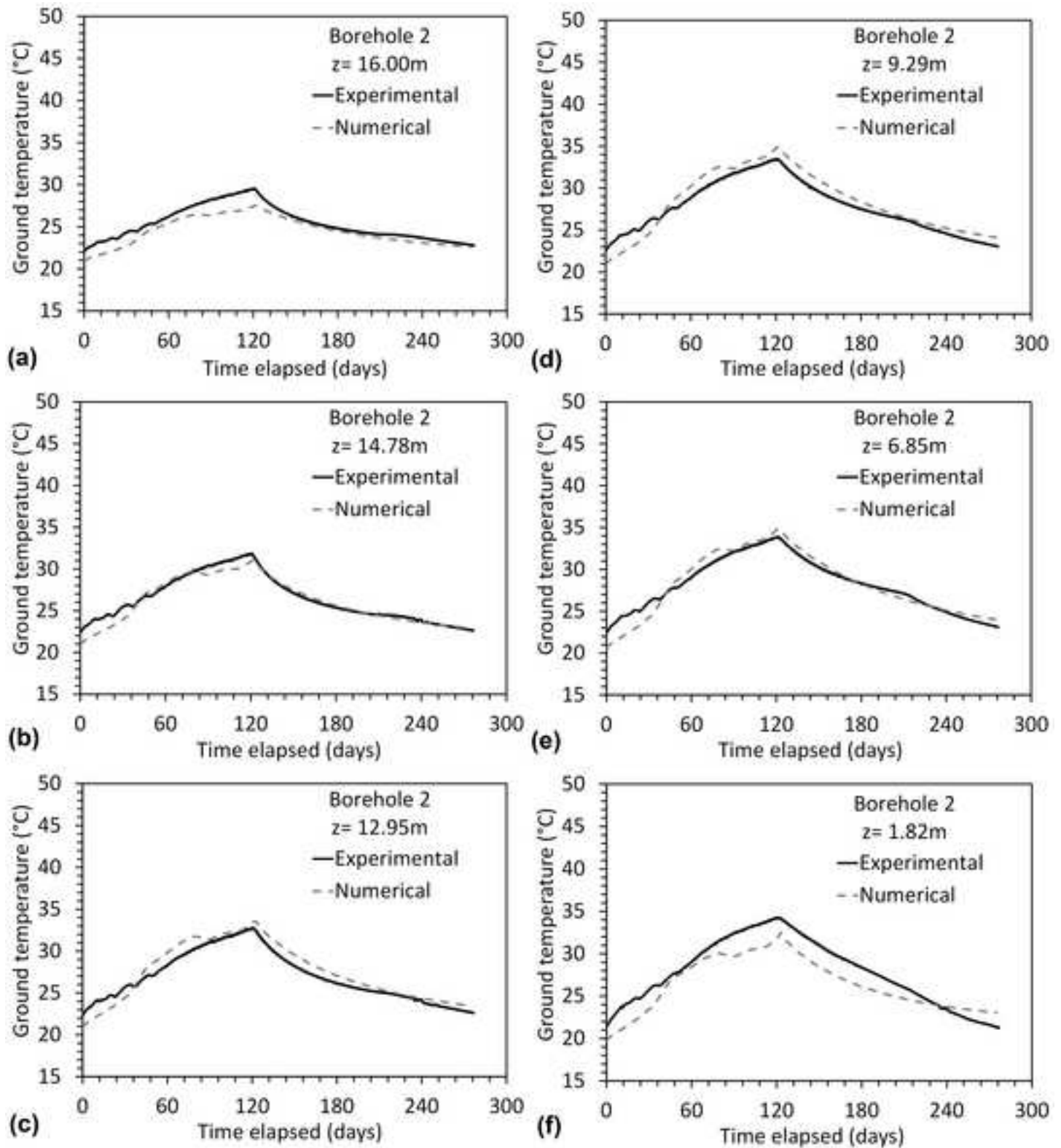
Figure 12[Click here to download high resolution image](#)

Figure 13

[Click here to download high resolution image](#)

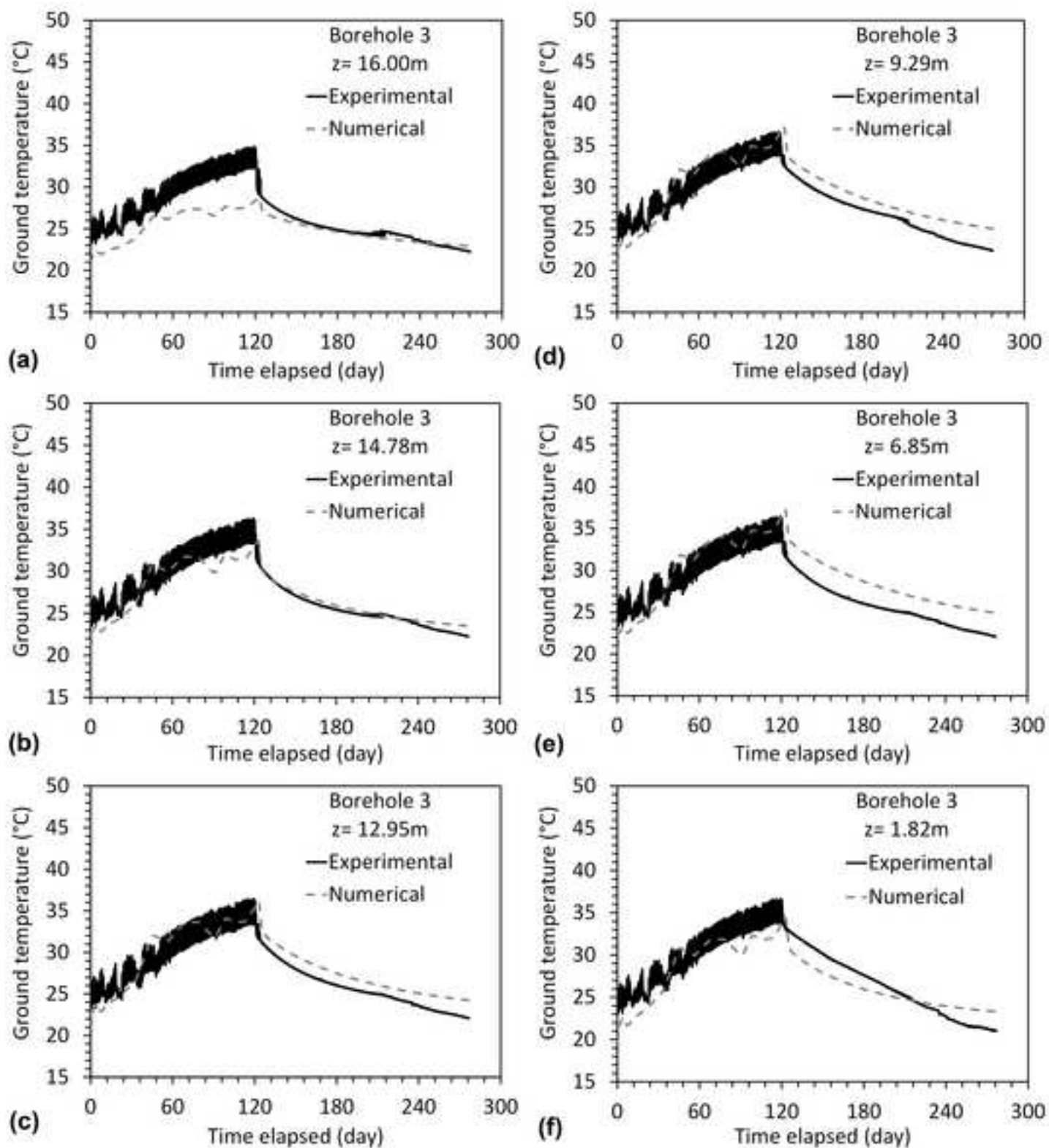


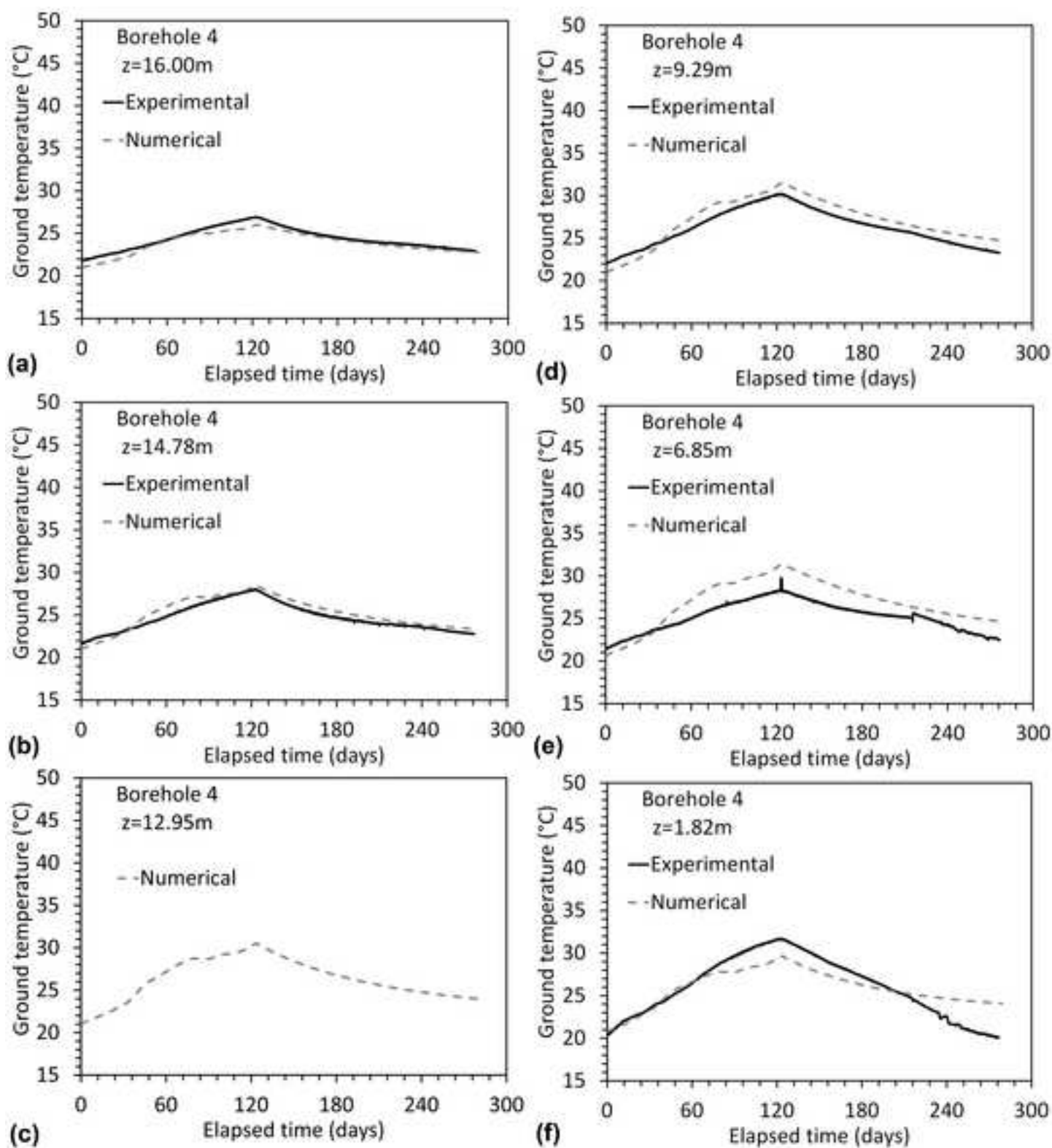
Figure 14[Click here to download high resolution image](#)

Figure 15

[Click here to download high resolution image](#)

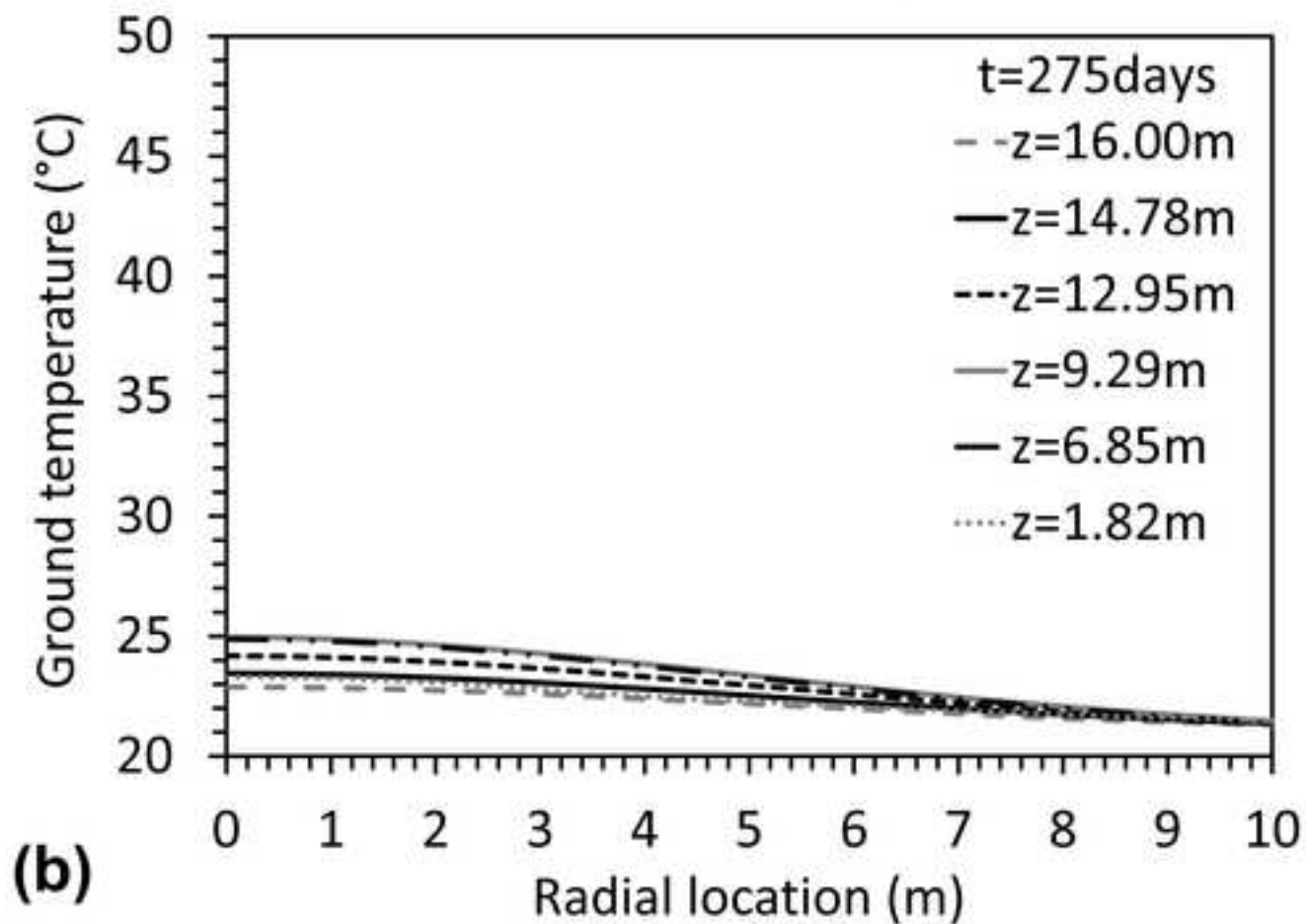
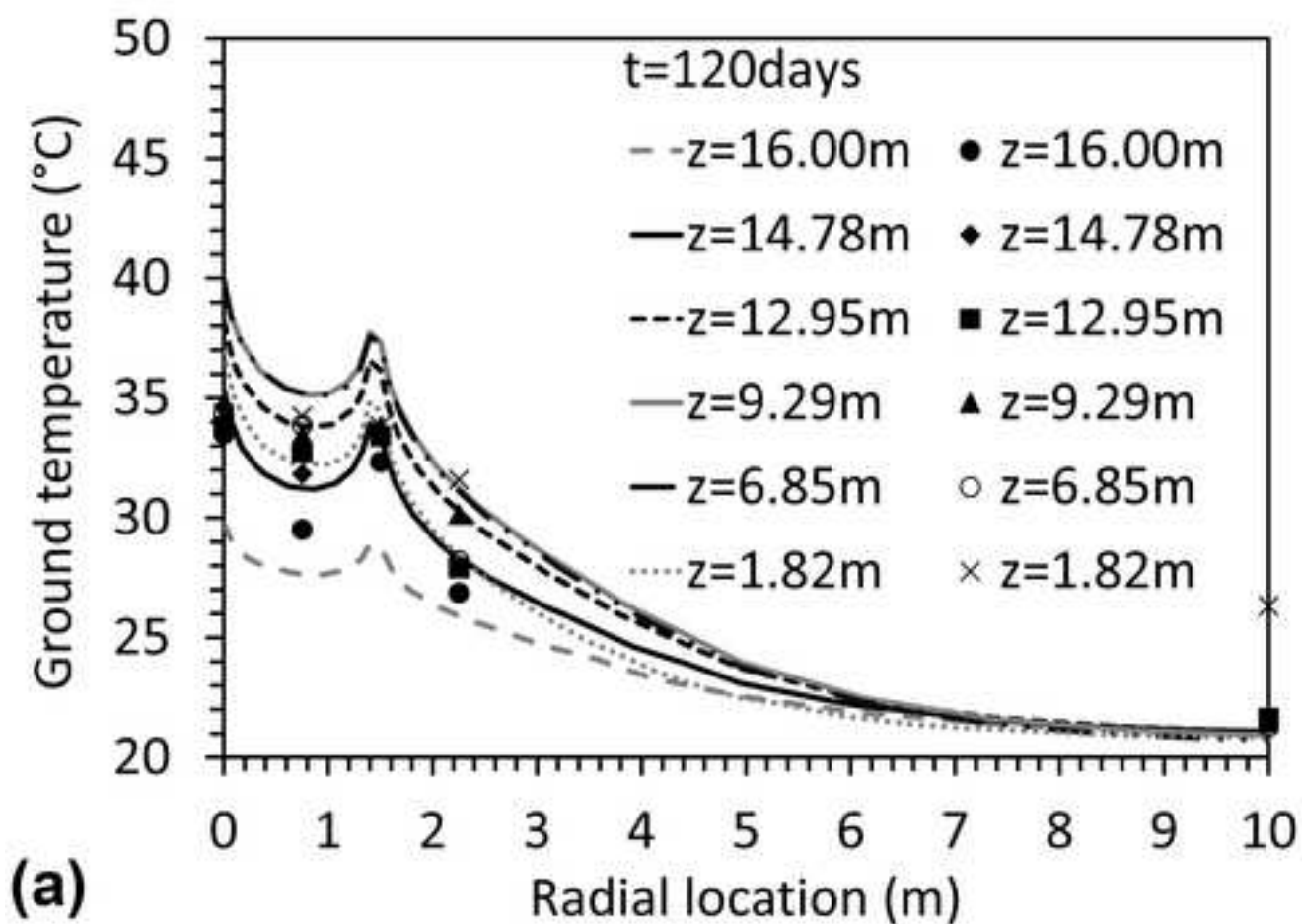


Figure 16

[Click here to download high resolution image](#)

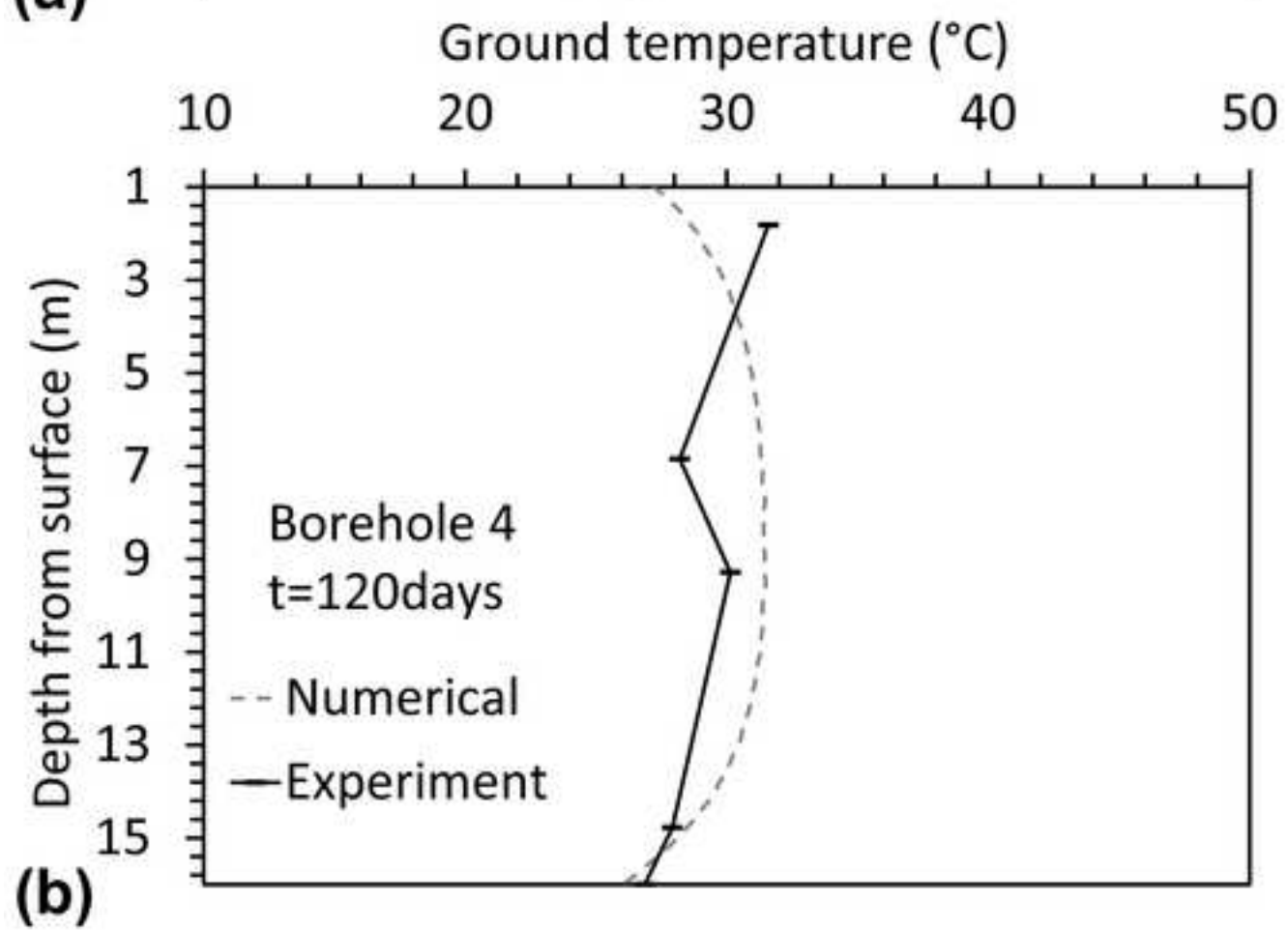
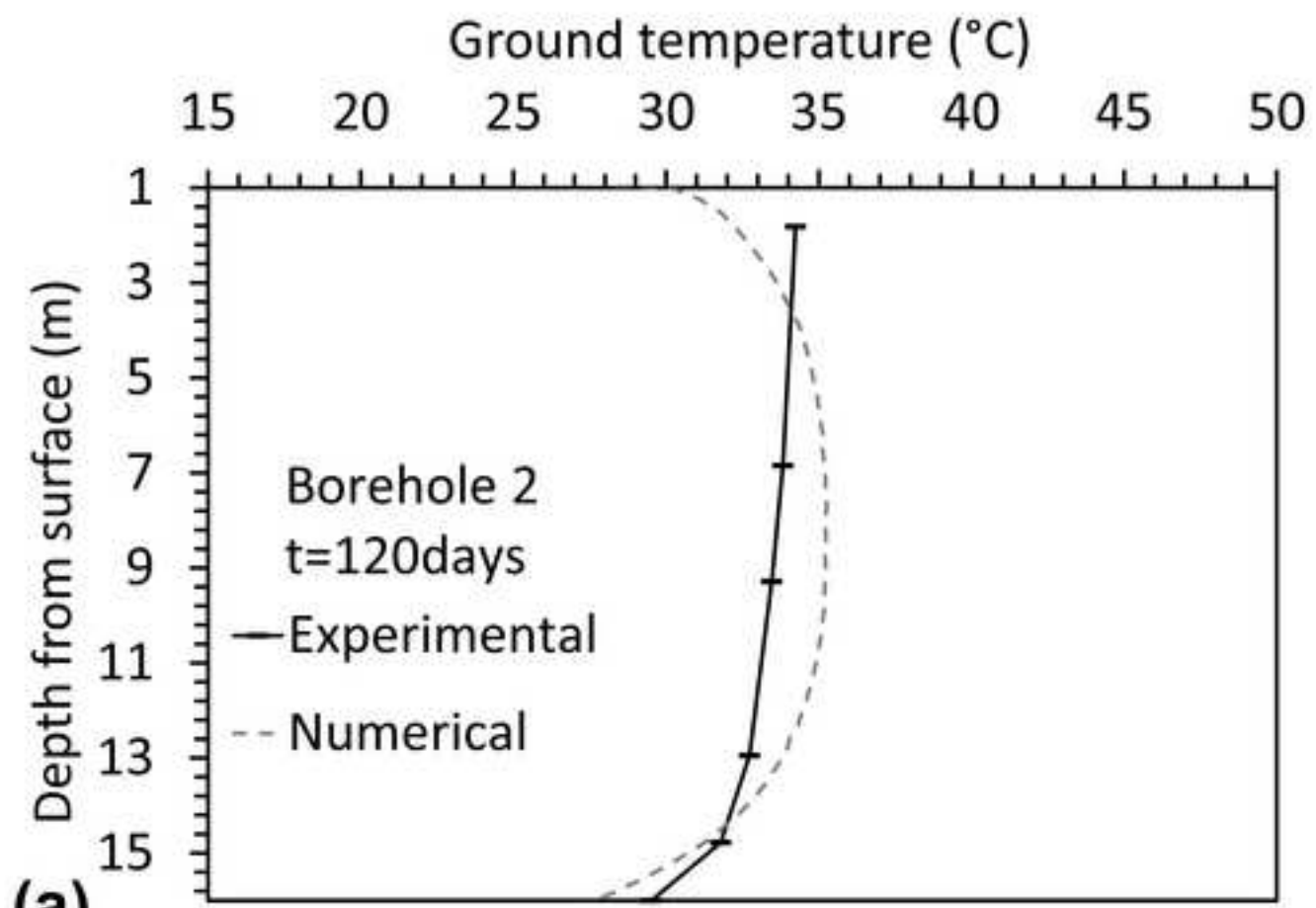


Figure 17

[Click here to download high resolution image](#)

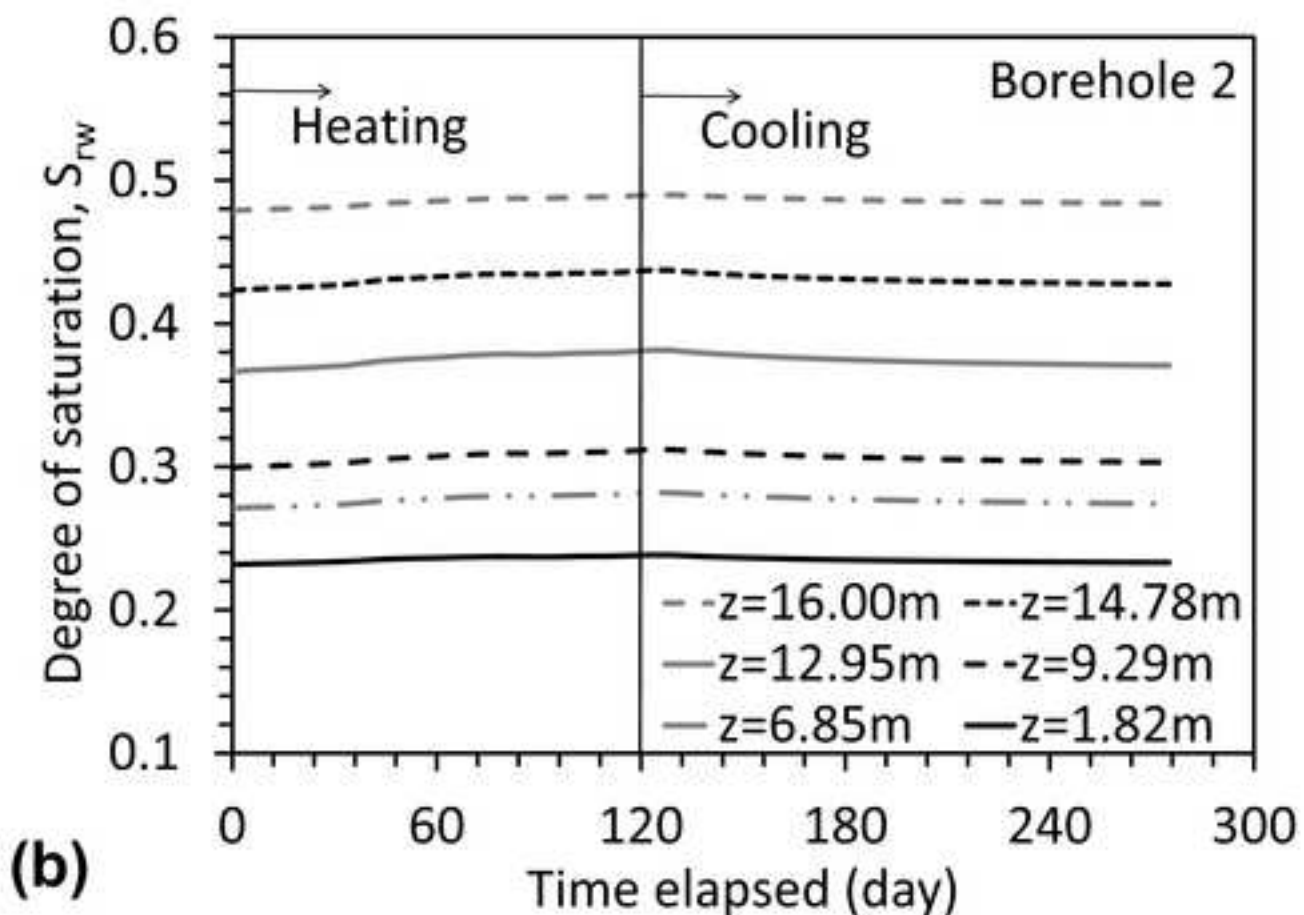
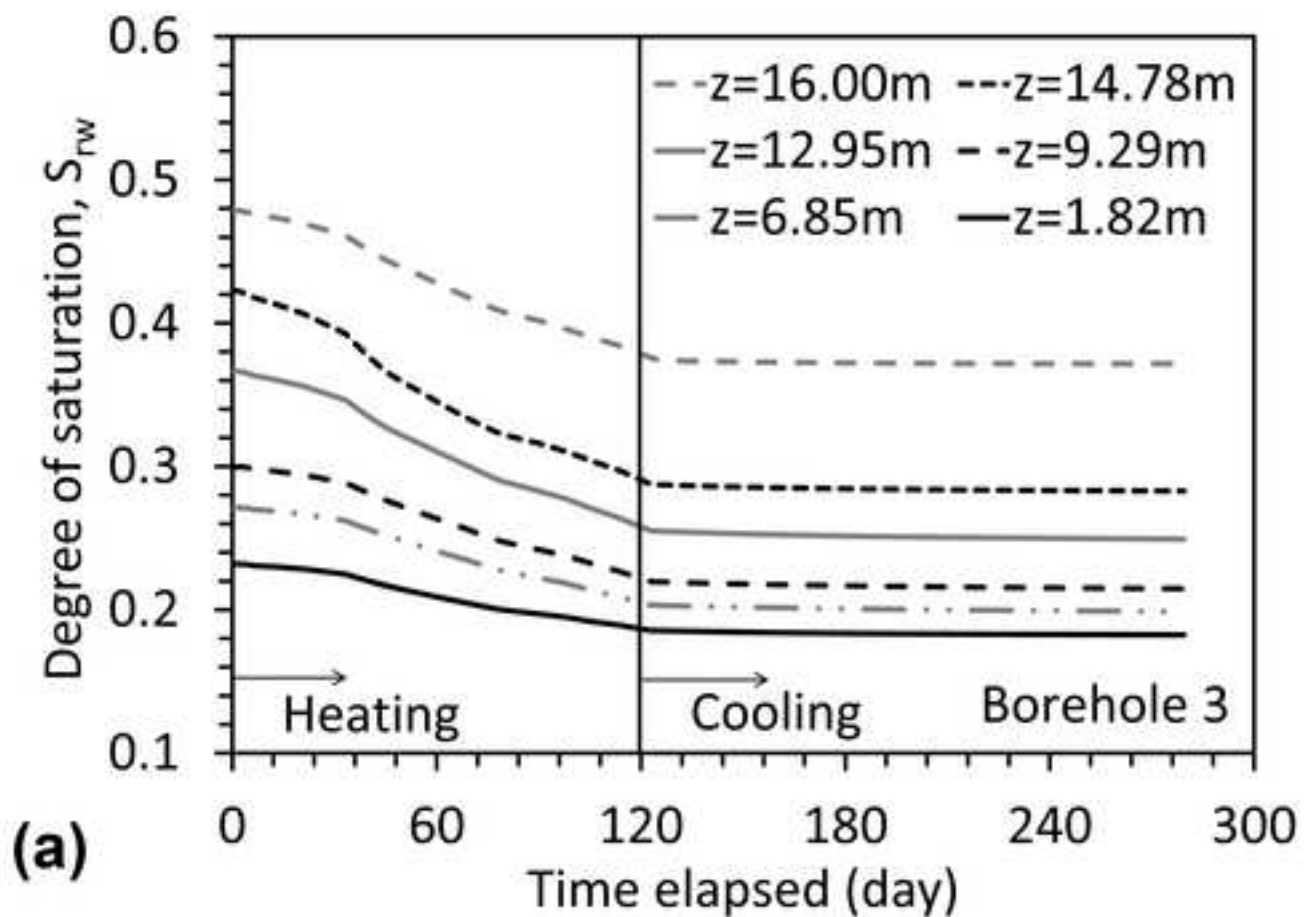


Figure 18

[Click here to download high resolution image](#)

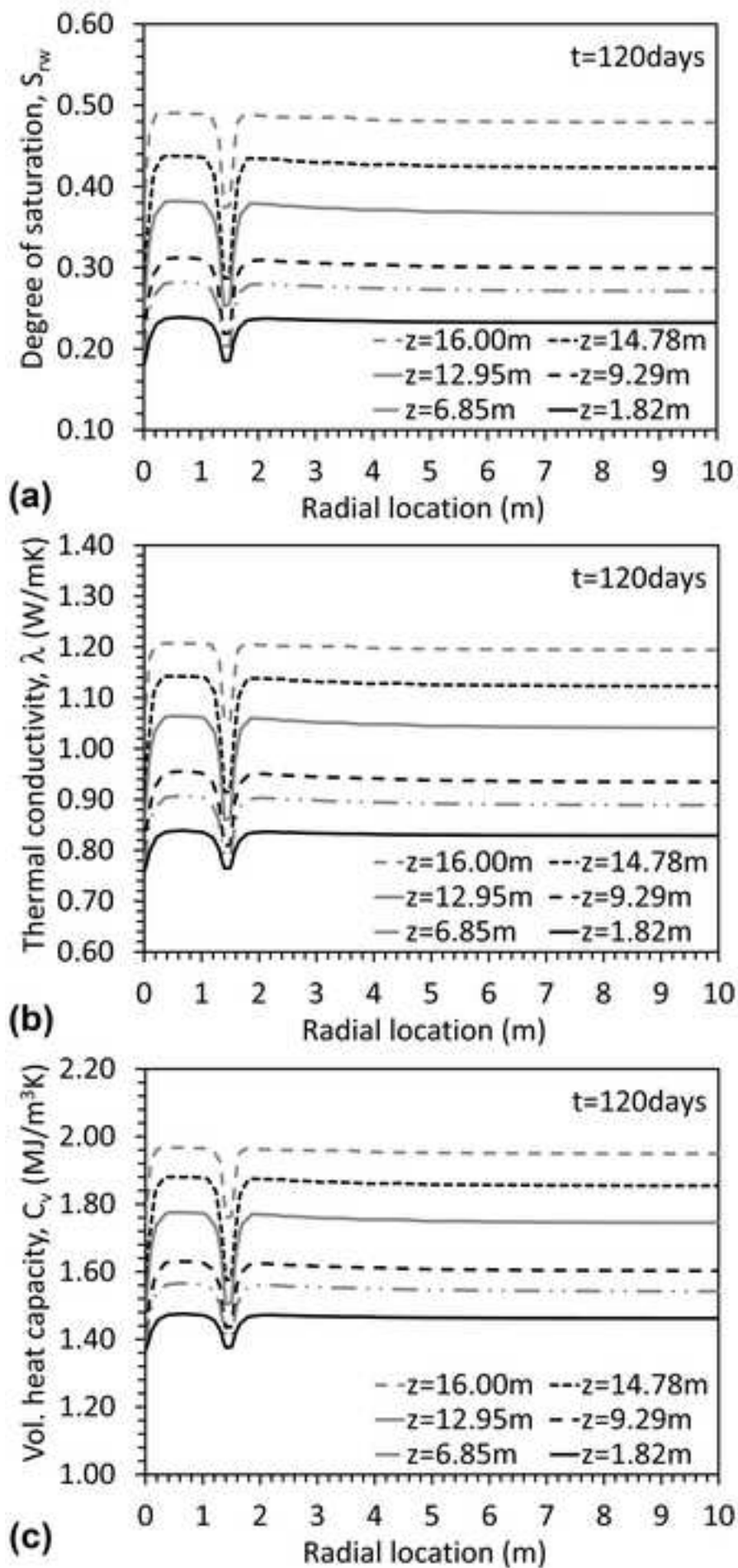


Figure 19
[Click here to download high resolution image](#)

