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### **Journal**

Physical Review Letters, 80(12)

### **Author**

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### **Publication Date**

1997-10-01



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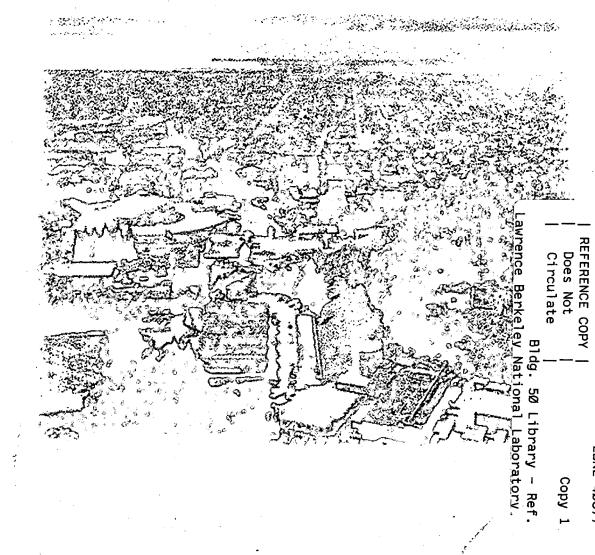
# **Combining Real and Virtual Higgs Boson Mass Constraints**

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**Physics Division** 

October 1997

Submitted to Physical Review Letters



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## Combining real and virtual Higgs boson mass constraints<sup>1</sup>

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#### Abstract

Within the framework of the standard model we observe that there is a significant discrepancy between the most precise Z boson decay asymmetry measurement and the limit from direct searches for Higgs boson production. Using methods inspired by the Particle Data Group we explore the possible effect on fits of the Higgs boson mass. In each case the central value and the 95% confidence level upper limit increase significantly relative to the conventional fit. The results suggest caution in drawing conclusions about the Higgs boson mass from the existing data.

<sup>&</sup>lt;sup>1</sup> This work was supported by the Director, Office of Energy Research, Office of High Energy and Nuclear Physics, Division of High Energy Physics of the U.S. Department of Energy under Contract DE-AC03-76SF00098.

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<u>Introduction</u> Perhaps the most pressing question in particle physics today is the mass scale of the quanta that break electroweak symmetry, giving mass to the particles in the theory, including the quark and lepton constituents of ordinary atomic matter. That scale determines whether the symmetry breaking force is weak or strong and it sets the energy scale future accelerators will need for detailed studies of the mass-generating mechanism. In general the issue can only be resolved by discovering the symmetry breaking quanta at a high energy collider. However, in particular theoretical frameworks, such as for instance the standard model, radiative corrections to already measured quantities can be used to constrain the mass of the symmetry breaking sector.

Interpreted in the standard model framework, beautiful data from LEP, SLAC, and Fermilab appear to favor a light Higgs boson with mass of order 100 GeV.[1] The conclusion emerges from the effect of virtual Higgs bosons, via radiative corrections, on precision measurements of the Z and W bosons. In addition, the four LEP experiments have searched for real Higgs bosons, with negative results that when combined are expected to imply a lower limit  $m_H \geq$  77 GeV at 95% confidence level.[2] Taken together the experiments suggest a window between 80 and a few hundred GeV. The purpose of this note is to suggest that the window may in fact be substantially larger, in part because of well known inconsistencies within the precision data, but more because of equally significant inconsistencies between precision data and the direct searches whose magnitude has gone unnoticed and/or unremarked.

The problem of how to combine inconsistent data has led to the break-up of many beautiful friendships. The mathematical theory of statistics provides no magic bullets and ultimately the discrepancies can only be resolved by future experiments. The Particle Data Group[3] (PDG) has for many years scaled the uncertainty of discrepant results by a factor I will call  $S_{\rm PDG}$ , defined by  $S_{\rm PDG} = \sqrt{\chi^2/(N-1)}$ , where N is the number of data points being combined. They scale the uncertainty of the combined fit by the factor  $S_{\rm PDG}$  if and only if  $S_{\rm PDG} > 1$ . This is a conservative prescription, which amounts to requiring that the fit have a good confidence level, ranging from 32% for N=2 to greater than 40% for larger values of N. If the confidence level is already good, the scale factor has little effect; it only has a major effect on very discrepant data. The PDG argues (see [4]) that low confidence level fits occur historically at a

rate significantly greater than expected by chance, that major discrepancies are often, with time, found to result from underestimated systematic effects, and that the scaled error provides a more cautious interpretation of the data.

With the top quark mass fixed at the value determined by CDF and D0, the most sensitive probe of  $m_H$  is the effective leptonic weak interaction mixing angle,  $sin^2\theta_{eff}^{lepton}$ , measured in a variety of Z boson decay asymmetries. A few authors[5, 6] (theorists all) have applied  $S_{PDG}$  to the measurements of  $sin^2\theta_{eff}^{lepton}$ , as I will also do here. It increases the uncertainty but not the central value of the combined fit for  $sin^2\theta_{eff}^{lepton}$  and  $m_H$ .

The focus of this paper is on the discrepancies between precision measurements and the limit from the direct searches, which will be addressed by a method analogous to the PDG scale factor. Like the PDG prescription, the idea is to scale the error so that the precision measurement has a significant probability P to be consistent with the direct search limit. I consider P=0.32, corresponding to the PDG's choice, as well as larger and smaller values. To account for uncertainty in the search limits, which may also be subject to unknown systematic errors, I consider a range of different lower limits on  $m_H$ , from a very conservative 50 GeV to a futuristic 90 GeV. In this approach both the central value and the uncertainty of the fit are affected. In addition I present fits using two other methods discussed by the PDG. The results suggest caution in drawing conclusions from the precision data about the value of the Higgs boson mass.

<u>The precision data</u> The relevant values of  $sin^2\theta_{eff}^{lepton}$  and the quoted experimental uncertainties are shown in table 1, from the preliminary values presented at the 1997 summer conferences.[1] For each value the table displays the corresponding value of  $m_H$  and the 95% CL upper  $(m_{95}^{<})$  and lower  $(m_{95}^{>})$  bounds (that is, the symmetric 90% confidence intervals). Also indicated is the probability for  $m_H$  to lie below 77 GeV. Gaussian distributions are assumed.<sup>3</sup>

The values of  $m_H$  are from the state of the art  $\overline{MS}$  computation of reference [6] — see also [7]. To obtain the confidence intervals and probabilities the parametric error is combined in quadrature with the experimental errors. The

<sup>&</sup>lt;sup>3</sup>That is, we make the customary assumption that the distributions in  $sin^2\theta_{eff}^{lepton}$  are Gaussian, which implies that the distributions for  $log(m_H)$  are Gaussian.

parametric error is equivalent to  $\pm 0.00030$  uncertainty in  $sin^2\theta_{eff}^{lepton}$  — see [6, 7]. It is dominated by roughly equal contributions from the uncertainties in the top quark mass,  $m_t = 175 \pm 6$  GeV, and the fine structure constant at the Z mass,  $\alpha^{-1}(m_Z) = 128.896 \pm 0.090$ , in addition to other much smaller contributions, including  $\Delta\alpha_{\rm OCD}(m_Z)$  and uncomputed higher order corrections.<sup>4</sup>

The six LEP measurements in table 1 are each combined from the four LEP experiments, and in each case the combined fit has a good confidence level. The conventional maximum likelihood fit for the LEP measurements is shown in the first row of table 2. The chi-squared per degree of freedom is  $\chi^2/N - 1 = 4.4/5$  corresponding to a robust 0.5 confidence level. The central value is  $m_H = 240$  GeV and the 95% CL upper limit is 860 GeV. There is no entry for the  $S_{\rm PDG}$  fit since  $S_{\rm PDG} < 1$ .

Combining all seven measurements (the conventional LEP + SLC fit in table 2) the central value decreases to 100 GeV and the 95% CL upper limit falls to 310 GeV, demonstrating the effect of the high precision and lower  $sin^2\theta_{eff}^{lepton}$  from  $A_{LR}$ . The chi-squared per degree of freedom now rises to 12.5/6, with a marginal confidence level of 0.05. The PDG scale factor is then  $S_{\rm PDG}=1.45$ . Using it, the combined uncertainty of the fit increases from  $\pm 0.00023$  to  $\pm 0.00033$  and the 95% CL upper limit on  $m_H$  increases modestly to 420 GeV.

surements of  $sin^2\theta_{eff}^{lepton}$ , which are problematic whether we assume the standard model or not, table 1 also reveals a second discrepancy that occurs specifically within the standard model framework. The most precise measurement,  $A_{LR}$ , implies a 95% CL upper limit on  $m_H$  of 77 GeV, while the direct searches at LEP are expected to provide a combined 95% lower limit also at 77 GeV.[2] (The individual 95% CL limits quoted by the four experiments range from 66 to 71 GeV.[2]) The third most precise measurement,  $A_{FB}^l$ , also has significant

<sup>&</sup>lt;sup>4</sup>There are also negligible extrapolation errors from reference [6], equivalent to  $\leq 0.00003$  in  $sin^2\theta_{eff}^{lepton}$  for 75  $< m_H < 600$  GeV. Even outside this range they have no real effect on the analysis, since the confidence levels and scale factors only depend on the relationship between  $sin^2\theta_{eff}^{lepton}$  and  $m_H$  for  $m_H = m_H^{limit}$ . The worst case is then  $m_H^{limit} = 50$  GeV, close enough for any additional error to be negligible. The very large values of  $m_{95}^>$  in the tables could be affected but they have no precise significance in any case.

weight (71%) below the direct search limit.<sup>5</sup>

This raises a difficult question: within the standard model framework what role if any should the direct search limits play in extracting the implications of the precision data? There is no single "right" answer to the question. A maximum likelihood fit including both the precision data and the direct search data would replicate the conventional fit if the central value lies above the lower limit,  $m_H^{\text{limit}}$ , from the direct searches. That is a defensible interpretation, since if the true value of  $m_H$  were near  $m_H^{\text{limit}}$  we would expect values of  $m_H$  obtained from measurements of  $\sin^2\theta_{eff}^{\text{lepton}}$  to lie both above and below  $m_H^{\text{limit}}$ . At the same time it is instructive to explore the sensitivity of the fit to the weight ascribed to measurements that are individually in significant contradiction with the direct search limit.

Clearly the direct search results are not irrelevant. If, for instance, the only information available were the direct search limits and the  $A_{LR}$  measurement, we would conclude that the standard model is excluded at 90% CL.<sup>6</sup> Theorists would have flooded the Los Alamos server with papers on the death of the standard model and the birth of new theories W,X,Y,Z... In the actual situation the  $A_{LR}$  measurement causes the fit to  $m_H$  to shift by more than a factor two, from 240 GeV to 100 GeV, and the 95% upper limit to fall from the TeV scale to  $\simeq 400$  GeV. It is fully weighted in the conventional standard model fit despite a significant contradiction with the standard model.

If the discrepancy were even greater — say, for instance, a precision measurement implying  $m_H = 10$  MeV with a 99.99% CL upper limit at 77 GeV — the clear response would be to omit that measurement from a standard model fit, although it could still be considered in a broader framework encompassing the possibility of new physics. On the other hand,  $A_{FB}^l$ , with 31% probability to be consistent with a 95% lower limit at 77 GeV, would surely be retained. The question is how to resolve the intermediate cases in which the discrepancy is significant but not so significant that the data should clearly be excluded.

 $<sup>^{5}</sup>A_{LR}$  and  $A_{FB}^{l}$  are also the only measurements with  $m_{95}^{>}$  below the TeV scale.

<sup>&</sup>lt;sup>6</sup>I thank Lawrence Hall for this perspective.

<sup>&</sup>lt;sup>7</sup>In fact, parity violation in atomic Cesium currently implies  $m_H \sim 11$  MeV (MeV is not a typographical error) though only  $1.2\sigma$  from 77 GeV.[8] Its weight in the combined fit would be negligible.

Consider a prescription, analogous to the PDG scale factor, that interpolates smoothly between the extremes. Imagine a measurement x with experimental error  $\delta_E$  and a quantity y that is related to x with an uncertainty  $x \pm \delta_P$  (the parametric error). Suppose there is an upper limit on y at  $y = y_0$  that translates to an upper limit on x at  $x_0 \pm \delta_P$ , such that the measurement x falls below the implied limit,  $x < x_0$ . The discrepancy between the measurement and the limit is then characterized by a Gaussian distribution centered at x with standard deviation  $\sigma = \sqrt{\delta_E^2 + \delta_P^2}$ , with a computable probability P for  $x > x_0$ . If P is less than a chosen minimal confidence level  $P_{VR}$  (VR for "virtual-real"), then  $\delta_E$  is scaled by a factor  $S_{VR}$  chosen so that the Gaussian centered at x with standard deviation  $\sigma' = \sqrt{(S_{VR}\delta_E)^2 + \delta_P^2}$  has probability  $P_{VR}$  for  $x > x_0$ . If  $x_0 - x$  is small enough, the scale factor has little or no effect. If x is many  $\sigma$  below  $x_0$ ,  $S_{VR}$  will be large and the data point x will have reduced weight in a combined fit with other data. Intermediate cases will interpolate smoothly between the two extremes, depending on the values of  $x - x_0$ ,  $\sigma$ , and  $P_{VR}$ .

The value of  $P_{VR}$  is of course arbitrary. One plausible choice is  $P_{VR} = 0.32$  (or 0.3173 to the cognoscenti), since that is the confidence level implicit in the PDG scale factor for N=2. A plausible choice for the lower limit on  $m_H$  is  $m_H^{\rm limit}=70$  GeV, which has a 95% CL from just one LEP experiment and a combined CL probably in excess of 97%. The resulting fits are shown in table 2. The fit to the LEP data is affected only modestly, with an increase of 10% in  $m_H$ . For the LEP + SLC fit, the central value of  $m_H$  and the 90% confidence interval increase significantly, to nearly the values of the LEP fit. The scale factors are  $S_{VR}(A_{FB}^l)=1.1$  and  $S_{VR}(A_{LR})=4.3$ .

Table 3 displays the results of varying  $P_{VR} = 0.20$ , 0.32, 0.40 and  $m_H^{\text{limit}} = 50$ , 60, 70, 80, 90 GeV. Though not reported by the experimental groups, the confidence levels at 50 and 60 GeV are probably much tighter than 97%, both because the LEP II cross sections increase for smaller  $m_H$  and because the LEP I data contributes to the confidence level at those masses — the 95% CL upper bound from LEP I alone is  $m_H < 66$  GeV. The value 80 GeV is close to the presently projected 95% combined limit of the four LEP experiments, while 90 GeV is the anticipated limit if no discovery emerges from currently planned LEP II running. Vacant entries in table 3 indicate that the fits are unmodified,  $S_{VR} \leq 1$ , and that the conventional fit, line 1 of table 2, applies. For the

LEP data, the Higgs mass scale varies by no more than a factor 1.5 from the conventional fit over the entire range of table 3. For the LEP + SLC data, the difference is a factor 1.5 for  $(P_{VR}, m_H^{\text{limit}}) = (0.20, 50 \text{ GeV})$  and becomes as large as a factor 4.

Though it has no deep significance, it is interesting that the fits with  $P_{VR} = 0.32$  in table 3 have 95% CL lower limits that match the corresponding 95% CL lower limits from the direct searches, i.e.,  $m_{95}^{>} \simeq m_H^{\rm limit}$ , for  $m_H^{\rm limit}$  varying between 60 and 90 GeV. In that sense they resemble the Bayesian fit described below.

<u>Other methods</u> In this section I will briefly present results using methods discussed by the PDG[9] for combining measurements that conflict with a limit. They are no less arbitrary than the  $S_{VR}$  scale factor method discussed above.

Consider a collection of measurements  $x_i \pm \delta_{E,i}$ ,  $i=1,\ldots,N$ , some of which are nominally inconsistent with an upper limit at  $x_0$ . The "Bayesian" method is to combine all data points in the conventional way and to multiply the combined Gaussian distribution by a step function  $C\theta(x-x_0)$ , so that the distribution vanishes below  $x_0$ . C is a normalization factor to guarantee total unit probability. I have modified the usual Bayesian method to account for the fact that the lower limit is not absolute but has 95% confidence, by choosing C to give the distribution probability 0.95 for  $x > x_0$ . The 50%- and 95%-tiles of the resulting distributions are shown in table 2 for  $m_H^{\text{limit}} = 70$  GeV.

Three "frequentist" prescriptions are also discussed by the PDG, of which two are considered here. For  $x_i < x_0$  one prescription assigns  $x_i \pm \delta_{E,i} \to x_0 \pm \delta_{E,i}$  when the limit  $x_0$  is known exactly. Including the parametric uncertainty, I modify this to  $x_i \pm \delta_{E,i} \to x_0 \pm \sigma_i$  where  $\sigma_i = \sqrt{\delta_{E,i}^2 + \delta_P^2}$ . The readjusted points are then combined as usual (including  $S_{\text{PDG}}$  if applicable) with the other measurements. An extremely conservative variation, intended only to obtain the 95% CL upper limit, replaces  $x_i \to \min(x_i, x_0 + 1.64\sigma_i)$ , so that 95% of the probability distribution is above the limit  $x_0$ . The results are illustrated in table 2 for  $m_H^{\text{limit}} = 70 \text{ GeV}$ .

<u>Conclusion</u> Several related points are deferred to a more detailed report, including the following: (1) There are indications, depending on how the data is grouped, that the confidence level of the conventional fit may be even less than 0.05. Dependence on how the data is grouped reflects the uncertainty

in the confidence level for fits of small data samples. (2) Though definitive conclusions can only come from the experimental groups, two estimates suggest that improved b-tagging methods are not likely to cause a big shift in  $A_{FB}^b$ . (3) The W boson mass measurement currently has a sensitivity to  $m_H$  at roughly the middle of the pack of the asymmetry measurements. It does not qualitatively alter the conclusions.

In summary, the  $A_{LR}$  measurement is inconsistent at 95% CL both with the LEP asymmetry measurements and, in the standard model, with the Higgs boson search limits, while its precision causes it to have a profound effect on the combined standard model fit. The analysis presented here is meant as a warning signal, a yellow if not a red flag, suggesting caution in drawing conclusions from the precision data about the mass of the standard model Higgs boson. Applying methods inspired by the Particle Data Group to these discrepancies, we find that the central value of  $m_H$  increases by factors from  $\sim 1.5$  to  $\sim 3$  while the 95% CL upper limit increases toward the TeV scale. Only future experimental results can resolve the discrepancies in the present experimental situation.

Acknowledgements: I wish to thank Michael Barnett, Robert Cahn, Donald Groom, Lawrence Hall, and Gerry Lynch for useful discussions. This work was supported by the Director, Office of Energy Research, Office of High Energy and Nuclear Physics, Division of High Energy Physics of the U.S. Department of Energy under Contracts DE-AC03-76SF00098 and DE-AC02-76CHO3000.

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### **Tables**

Table 1. Values for  $sin^2\theta_{eff}^{lepton}$  from asymmetry measurements[1] with  $1\sigma$  experimental errors. The corresponding Higgs boson masses, the 95% CL upper and lower limits, and the confidence level for  $m_H < 77$  GeV are given for each measurement.

	$\sin^2\! heta_{ m eff}^{ m lepton} (1\sigma)$	$m_{H}$ (GeV)	$\mathbf{m_{95}^{>}},\ \mathbf{m_{95}^{<}}$	<b>P</b> (< <b>77</b> GeV)
$\overline{A_{LR}}$	0.23055 (41)	16	3, 80	0.95
$A_{FB}^b$	0.23236 (43)	520	100, 2700	0.03
$\overline{A_{FB}^{l}}$	0.23102 (56)	40	5, 290	0.71
$A_{ au}$	0.23228 (81)	440	30, 6700	0.14
$A_e$	0.23243 (93)	590	28, 13000	0.14
$Q_{FB}$	0.23220 (100)	380	14, 10000	0.21
$A_{FB}^c$	0.23140 (111)	83	2, 3000	0.48

Table 2. Fits to the LEP and LEP + SLC data as described in the text. The Bayesian and frequentist fits assume  $m_H^{\rm limit}=70$  GeV.

Data set	Fit	$\sin^2\! heta_{ ext{eff}}^{ ext{lepton}}(1\sigma)$	m <sub>H</sub> (GeV)	$m_{95}^{<}, m_{95}^{>}$
LEP	Conventional $S_{PDG}$ $S_{VR}(0.32, 70 \text{ GeV})$	0.23196 (28) 0.23201 (28)	240 260	67, 860 72, 960
11131	Bayes	0.23201 (28)	240	< 870 (95%)
	Frequentist (1)	0.23203 (28)	280	77, 990
	Frequentist (2)	< 0.23301 (95%)		1800 (95%)
	Conventional	0.23152 (23)	100	32, 340
	$S_{PDG}$	0.23152 (33)	100	26, 420
LEP + SLC	$S_{VR}(0.32,70~{ m GeV})$	0.23197 (28)	250	68, 890
	Bayes	0.23168	140	< 480 (95%)
	Frequentist (1)	0.23181 (23)	180	55, 590
	Frequentist (2)	< 0.23280 (95%)		< 1200 (95%)

Table 3. Fits to LEP and LEP + SLC data using the  $S_{VR}$  scale factor with various values of  $P_{VR}$  and  $m_H^{\text{limit}}$ . Each entry displays the central value of  $m_H$  and  $m_{95}^{\leq}$ ,  $m_{95}^{\geq}$ , the 95% CL lower and upper limits, in GeV. Empty entries indicate that no measurement is far enough below threshold to be modified by the scale factor and that the conventional fit of table 2 applies.

	LEP			LEP + SLC		
$m_H^{ m limit}$	$P_{VR} = 0.20$	0.32	0.40	0.20	0.32	0.40
50				150	220	230
			•	45, 530	61, 770	65, 830
60			310	170	220	300
			82, 1100	47, 640	62,790	80, 1100
70		260	360	190	250	350
		72, 960	94, 1400	51, 680	68, 890	91, 1300
80		310	380	190	290	370
ļ		83, 1200	99, 1500	55, 680	78, 1100	96,1400
90		340	390	200	320	380
		90, 1300	100, 1500	56, 710	84, 1200	100, 1500

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