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Experiment to demonstrate separation of Cherenkov and scintillation signalsJ. Caravaca,^{1,2} F. B. Descamps,^{1,2} B. J. Land,^{1,2} J. Wallig,² M. Yeh,³ and G. D. Orebi Gann^{1,2}¹*Physics Department, University of California, Berkeley, California 94720-7300, USA*²*Lawrence Berkeley National Laboratory, California 94720-8153, USA*³*Brookhaven National Laboratory, Upton, New York 11973-500, USA*

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The ability to separately identify the Cherenkov and scintillation light components produced in scintillating mediums holds the potential for a major breakthrough in neutrino detection technology, allowing development of a large, low-threshold, directional detector with a broad physics program. The CHESS (CHerenkov/Scintillation Separation) experiment employs an innovative detector design with an array of small, fast photomultiplier tubes and state-of-the-art electronics to demonstrate the reconstruction of a Cherenkov ring in a scintillating medium based on photon hit time and detected photoelectron density. This paper describes the physical properties and calibration of CHESS along with first results. The ability to reconstruct Cherenkov rings is demonstrated in a water target, and a time precision of 338 ± 12 ps FWHM is achieved. Monte Carlo-based predictions for the ring imaging sensitivity with a liquid scintillator target predict an efficiency for identifying Cherenkov hits of $94 \pm 1\%$ and $81 \pm 1\%$ in pure linear alkyl benzene (LAB) and LAB loaded with 2 g/L of a fluor, PPO, respectively, with a scintillation contamination of $12 \pm 1\%$ and $26 \pm 1\%$.

DOI: [10.1103/PhysRevC.95.055801](https://doi.org/10.1103/PhysRevC.95.055801)**I. INTRODUCTION**

Optical photon detection has been a common detection mechanism in neutrino experiments for many decades [1–6] and the technology is well developed. Experiments have historically been optimized to detect one of two types of optical radiation: Cherenkov [7] or scintillation [8] light. Directional Cherenkov light has been successfully used in both high-energy and nuclear physics by large ultra-pure-water experiments such as SuperKamiokande [2] and the Sudbury Neutrino Observatory (SNO) [3], while the more abundant, isotropic scintillation is more commonly used in low-energy detectors such as KamLAND [4] and Borexino [5]. A brief summary of the advantages and limitations of each technique can be found in Table I.

The LSND experiment [6] used a mineral-oil-based scintillator designed to allow detection of both scintillation and Cherenkov light, opening up sensitivity to low-energy particles below Cherenkov threshold. The ratio of created photoelectrons for the two sources of light was approximately 5 to 1 (scintillation to Cherenkov) for a 45-MeV electron created in the detector. Photon timing and charge was used for particle identification and to reconstruct vertex and angle information. Particles emitting Cherenkov radiation produced significant fractions of prompt light and thus particle identification techniques relied on the fraction of prompt light as a tool for discrimination.

Separation of Cherenkov- and scintillation-light components on an event-by-event basis enables a single detector to exploit the advantages of each technique. If this separation can be achieved in a pure liquid scintillator (LS) detector it would substantially improve the sensitivity of low-energy physics programs by adding directional reconstruction capability to a low-threshold detector. Searches for neutrinoless double- β decay (NLDBD) would benefit from rejection of the directional solar neutrino signal, the dominant background in experiments such as SNO+ [9]. Precision solar neutrino measurements

would benefit from separation of the directional signal from isotropic radioactive background events. However, the high scintillation light yield and fast timing of commonly used LS such as linear alkyl benzene (LAB) makes this separation extremely challenging. In addition, liquid scintillator detectors are limited to kiloton scales by the attenuation of light in the scintillator material and also by cost.

The recent development of water-based liquid scintillator (WbLS) [10] allows both the scintillation light yield and timing profile of the target material to be tuned, thus increasing sensitivity to the Cherenkov component. The admixture of water increases the attenuation length, thus improving light collection. For the first time, one can thus envisage a large-scale, low-threshold detector with directional sensitivity. The concept for a large monolithic WbLS detector capable of a very broad program of physics, such as the THEIA experiment, is presented in Refs. [11,12]. The unique capabilities of a large-scale WbLS detector enable both a broad low-energy program, including a sensitive NLDBD search, solar neutrino studies, supernova neutrinos, and diffuse supernova neutrinos (DSNB), as well as sensitivity to nucleon decay and, if sited in a high-energy neutrino beam, to long-baseline physics–neutrino mass hierarchy and Charge-Parity (CP) violation. The high-energy program benefits from the potential to image Cherenkov rings, thus improving particle identification, and the ability to detect particles below Cherenkov threshold, which improves background rejection.

The goals of the CHerenkov/Scintillation Separation (CHESS) experiment are several: to demonstrate Cherenkov and scintillation separation in a pure LS target by deploying ultra-fast-timing photosensors, to study how the separation improves in WbLS, and to quantify the efficiency as a function of the scintillator fraction. These studies will allow optimization of the THEIA detector configuration (WbLS target cocktail, photosensor requirements, detector scale) in order to maximize the physics reach across a broad program.

TABLE I. Comparison of Cherenkov and scintillation light in the context of optical particle detection.

Cherenkov	Scintillation
Directional	Isotropic
Very well understood	Strong dependence on material properties
Good shower and MIP separation	Reasonable particle ID
Minimum energy threshold for light production	No energy threshold for light production
Low light yield	High light yield results in lower detector threshold and improved energy resolution
Occurs in all dielectric materials, some with very good optical properties	Scintillating materials tend to have substantially shorter attenuation lengths
Cost-effective	More expensive materials

Separation of scintillation and Cherenkov components can occur in three domains:

- (1) Wavelength: Cherenkov and scintillation light have different emission spectra (Fig. 1). The Cherenkov signal could be enhanced by selecting photosensors with improved sensitivity in the high-wavelength region above the scintillation emission cutoff.
- (2) Photon density: Depending on the ratio of Cherenkov to scintillation light yield, it may be possible to distinguish the Cherenkov ring structure on top of the background of isotropic scintillation light.
- (3) Time separation: Scintillation light, originating from molecular de-excitation, is typically delayed from the fast Cherenkov light pulse by 1 to tens of ns [7,8]. By combining fast photon detectors and electronics it should be possible to achieve some signal separation using photon detection times.

Each option has the potential to enhance signal separation, but each comes with a cost, such as reduced light yield, reduced light collection efficiency, high-cost photosensors, or limitations on detector size. The challenge for time-based separation is the timing precision of available photosensors.

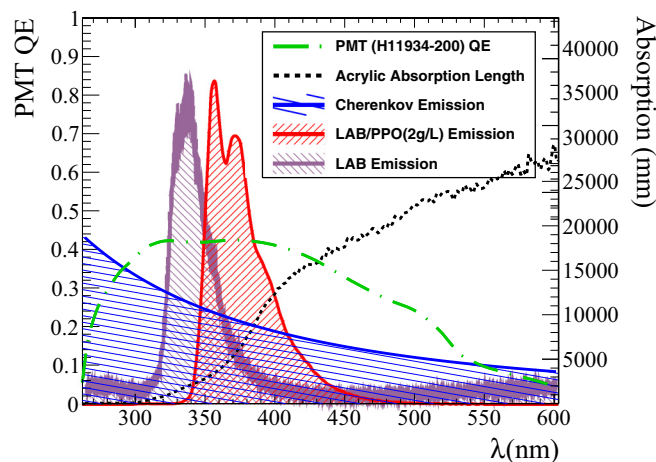


FIG. 1. PMT H11934 quantum efficiency (QE) [13] and ultraviolet-transmitting (UVT) acrylic absorption length compared to the Cherenkov and scintillation emission spectra for pure LAB [14] and LAB loaded with 2 g/L of PPO as a fluor [15]. The normalization of the emission spectra are shown in arbitrary units.

Large photomultiplier tubes (PMTs) typically have worse than ns time precision, making Cherenkov light identification in a scintillation medium extremely difficult. However, newly developed small PMTs [13] can achieve timing precisions of $\lesssim 300$ ps and new microchannel plate (MCP) photosensor technology [16–18] can achieve $\lesssim 100$ ps. In addition, fast and precise commercial electronics are available to digitize these signals without significantly degrading the time resolution. This makes separation in the time domain a theoretical possibility.

This paper describes the CHESSE detector and its sensitivity to Cherenkov and scintillation separation in the time domain. Section II describes the detector itself. Section III describes the detailed Monte Carlo simulation used to model the detector. Section IV describes the general approach to data analysis. Section V describes detector calibrations. Section VI describes event selection and techniques for rejection of instrumental and physics background events. Section IX describes the predicted sensitivity in a pure LS target for both pure LAB and LAB loaded with 2 g/L of PPO (hereafter referred to as LAB-PPO), and Sec. X concludes the paper.

II. THE CHESSE DETECTOR

The primary goal of the CHESSE experiment is to demonstrate Cherenkov and scintillation separation by Cherenkov ring imaging in both charge (detected photoelectron density) and time, for different scintillating liquids. A schematic of CHESSE is shown in Fig. 2. An acrylic target vessel is viewed by an array of small, fast PMTs. The setup is designed to detect either cosmic muons or events from deployed radioactive sources. The primary ring imaging measurement is performed using through-going muons. Vertical-going events are selected via a 1-cm-diameter coincidence tag, ensuring a population of events with known orientation and thus a known expectation for the position of the Cherenkov ring. The muons produce Cherenkov and scintillation light in the target material, which is detected on the PMT array. The apparatus has been optimized using a full Monte Carlo simulation (Sec. III), complete with optical ray tracing, such that direct Cherenkov light from vertical muons falls on a distinct set of PMTs, forming a clear ring in the PMT array. This yields two distinct groups of PMTs by construction: those with pure scintillation hits and those with both scintillation and Cherenkov hits. The earliest hits on each PMT can thus be identified as being caused by either Cherenkov or scintillation photons and demonstrate

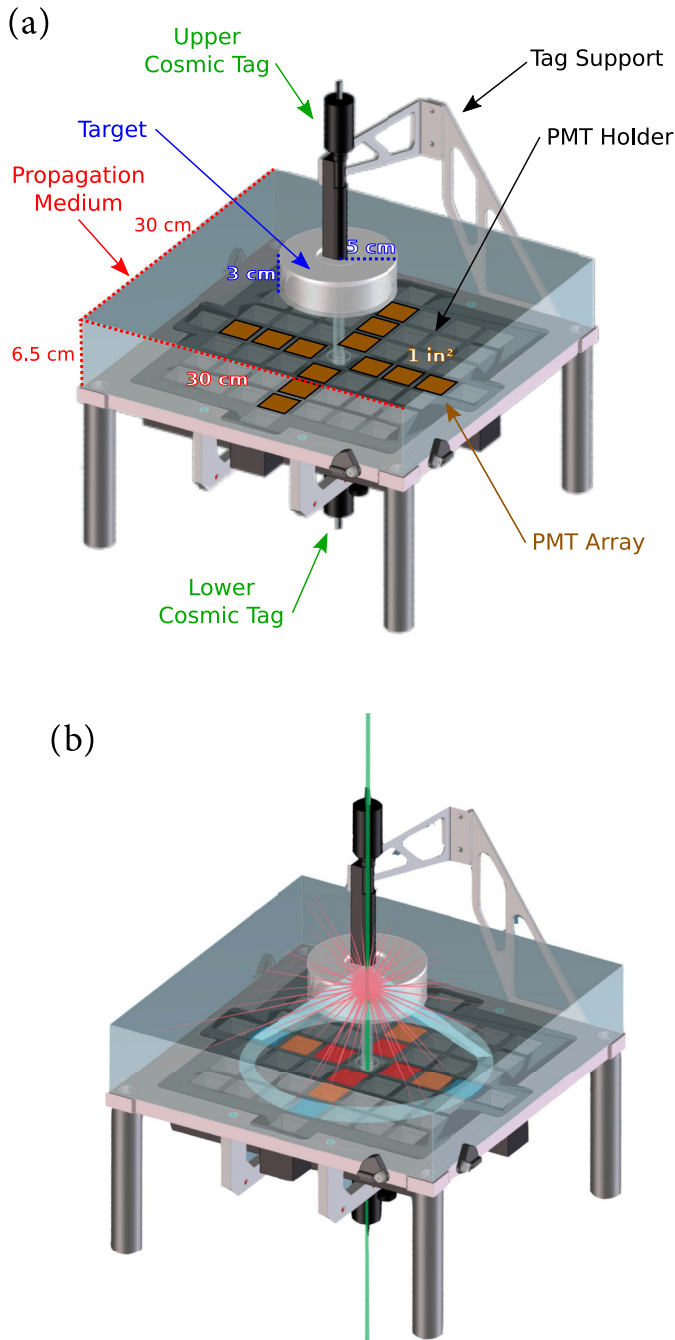


FIG. 2. The CHESSE apparatus. (a) Detailed schematic view with dimensions and (b) demonstration of ring-imaging concept. The PMT array is designed to hold up to 53 PMTs. The dozen slots occupied for this study are color coded by radius: red and orange for those hit primarily by scintillation photons and blue for those in the expected Cherenkov ring for LAB and LAB-PPO. Due to the lower refractive index, the ring from a water target is detected in the middle (orange) PMTs.

the time separation between these two signals to high precision. A measurement of the clarity of the Cherenkov ring imaged in charge on top of the isotropic scintillation light background is also possible.

A. Target vessel

The target vessel consists of a cylinder 5 cm in radius and 3 cm in height, constructed from ultraviolet-transmitting (UVT) acrylic. Three flat faces on the outer surface of the cylinder, each 3 cm in diameter, provide surfaces for attaching a radioactive button source or optical coupling of a PMT as a source tag. A lid made of the same UVT acrylic encloses the target material in an air-tight environment using an FFKM o-ring [19].

Distinct but similarly designed target vessels are used for water, pure LS, and WbLS target materials in order to minimize the risk of cross contamination.

B. PMT array

In the initial phase of CHESSE, one dozen Hamamatsu H11934-200 PMTs [13] were deployed in a cross shape beneath the target, providing three radial rings of four PMTs each for detection of Cherenkov and scintillation light. An additional twelve similar PMTs are available for deployment in a future upgrade. The H11934-200 PMT is a small 1-inch cubic PMT with superb QE peaked at 42% (Fig. 1) and excellent transit time spread (TTS) of 300 ps (FWHM for single photoelectrons).

The PMTs are held in an array that consists of a 7×7 grid, with four additional slots at each compass point, as shown in Fig. 2. The holder is 3D printed from black ABS plastic. The initial deployment positions for the twelve PMTs used in phase I of CHESSE are shown in Fig. 2. The unfilled locations on the grid can be populated with additional PMTs for future expansion.

C. Optical propagation

The target vessel is optically coupled to a propagation medium made of UVT acrylic ($30 \text{ cm} \times 30 \text{ cm} \times 6.5 \text{ cm}$). This coupling eliminates an acrylic-air boundary which would otherwise block all Cherenkov light due to total internal reflection. The propagation medium acts as a light guide to allow photons to propagate from the bottom of the target vessel towards the PMT array. The PMTs in the array are similarly optically coupled to the bottom of the propagation medium. The propagation medium and target vessel have been polished for a better optical coupling and a more accurate simulation of refracted light at the boundaries.

A vertical cylindrical hole 1 cm in diameter is machined through the center of the propagation medium aligned with the center of the target vessel and cosmic tags in order to allow vertical-going muons to interact with the target material, but pass through the propagation medium without producing additional Cherenkov light in the acrylic block that would contaminate the measurement.

Throughout the setup, EJ-550 optical grease [20] is used for optical coupling of components.

D. Cosmic muon tags

Two custom-made cylindrical scintillator tags are positioned above and below the target vessel (Fig. 2) in order to trigger on vertical cosmic muons. An aluminum arm maintains

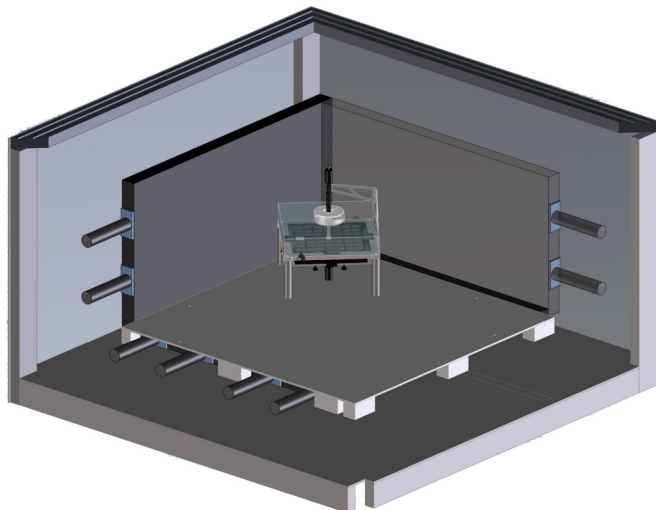


FIG. 3. Layout of veto panels around the CHES apparatus.

the alignment of the upper cosmic muon tag while the bottom is fixed in the PMT array (described in Sec. II B). Each tag consists of a cylindrical 1-cm diameter Hamamatsu PMT [21] optically coupled to EJ-200 plastic scintillator [22] shaped into a cylinder 1 cm in diameter and 5 cm high. The scintillator is coated with white paint to reflect light into the tag PMT and then coated with matte black paint (except for the end that is coupled to the PMT) to shield the remainder of the setup from light contamination. This assembly is held in a custom-built mount.

The small size of the tags results in a low angular acceptance (6° from vertical), ensuring a population of events with known orientation and thus a known expectation for the position of the Cherenkov ring. Given the typical muon flux at the Earth surface ($1 \text{ cm}^{-2} \text{ min}^{-1}$) and the angular acceptance of the tags, a coincidence rate of $\sim 4 \mu/\text{day}$ is predicted.

E. Veto panels

The apparatus is surrounded by four scintillator panels ($50 \text{ cm} \times 100 \text{ cm} \times 5.3 \text{ cm}$), as shown in Fig. 3, fabricated from EJ-200 plastic scintillator [22] (two on the floor and two on the sides in a corner distribution), providing effective 4π coverage. Each panel is instrumented with a PMT [23], which is read out for each event and used for an offline veto. The scintillator panels are used to veto cosmic events during calibration source deployment and to reject cosmic shower events and coincidence of multiple cosmic muons in the ring imaging analysis.

F. Shielding

CHES is enclosed in a light-tight darkbox of about $1.5 \text{ m} \times 1.5 \text{ m} \times 1 \text{ m}$ wrapped in FINEMET sheets [24] for magnetic field isolation and painted matte black on the inside to minimize reflections.

G. Radioactive source deployment

A ^{90}Sr button source is used to calibrate various aspects of the detector response (Sec. V). The source consists of a 1-inch-

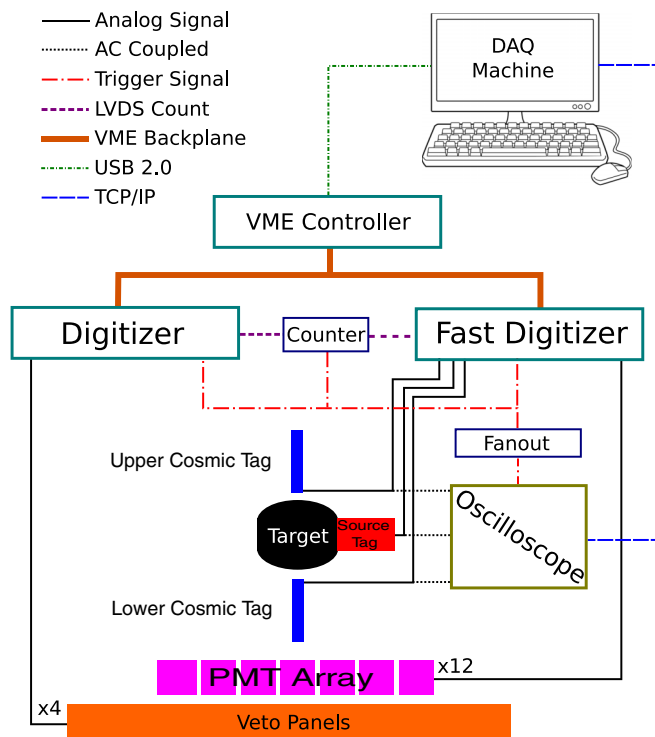


FIG. 4. A schematic diagram of how the DAQ and hardware are connected together with signal and data paths labeled. Omitted are the high voltage supplies, which are connected to the VME backplane, and all PMTs.

diameter acrylic disk with a thickness of 0.125 inches ([25]). A 0.25-inch diameter cylindrical well in the center of the button contains a deposit of $0.1 \mu\text{Ci}$ of ^{90}Sr combined with a resin. The well containing the radioactive material is encapsulated with a 0.02-inch-thick acrylic window. This source is attached to one face of the target vessel with the window facing the target material.

To trigger on source events, a 1-inch-cubic H11934-200 PMT [13] is optically coupled to another of the flat faces on the target vessel. This is the same type of PMT used in the PMT array and was chosen for its high QE and low TTS.

H. The DAQ System

A schematic diagram of the data acquisition (DAQ) hardware is shown in Fig. 4 (high voltage omitted) and described in detail in the following sections. The DAQ software [26] utilizes the CAEN VME library [27] to configure and read out the digitizers and high voltage supplies, and outputs HDF5 [28] formatted files containing raw digitized data and metadata for each triggered event.

1. Readout electronics and high voltage

Three six-channel high-voltage power supplies (CAEN V6533 [29]) power the PMTs. The PMT output signals are connected to two CAEN digitizers: a high-precision V1730 [30] digitizes the veto panels and source tag PMT signals, while a fast V1742 [31] based on the DRS4 [32] chip digitizes

the PMT array and cosmic tag signals. The hardware is housed in a VME crate, and a CAEN V1718 [33] VME to USB bridge is used for communications.

The V1742 card is capable of sub-100-ps resolution, which exceeds the TTS of the PMT array and is therefore not a limiting factor in the time precision. However, on-board buffer size limits the acquisition to a maximum of 1024 samples or 200 ns. This shallow buffer necessitated a low-latency triggering scheme in order to contain the pertinent data in the available event window. The V1730 digitizer is deadtimeless; however, the V1742 introduces dead time on the order of 100 μ s. This is neither a limitation for measurements with cosmic particles, where the trigger rate is approximately 0.2 Hz, nor for measurements with radioactive source data where the trigger rate is approximately 30 Hz.

2. Trigger

A LeCroy 606Zi [34] oscilloscope is used to produce low-latency trigger signals for the setup with programmable coincidence logic. Depending on the operating mode, one of the following three trigger configurations are used:

Bottom-only trigger: A threshold condition is applied to the lower cosmic tag only. This is the normal operating mode for cosmic data, with the coincidence requirement applied offline. A rate of 4 μ /day is expected after the coincidence trigger.

OR trigger: A threshold condition is applied to both of the cosmic tags, and the logical OR of the two is allowed to generate a trigger. This mode is used to acquire unbiased charge distributions for each cosmic tag simultaneously.

Source trigger: A threshold condition is applied to the source tag. This is the configuration used during radioactive source deployment.

The oscilloscope trigger signal is fanned out to the external trigger input on the V1730 and the low-latency trigger inputs on the V1742. The V1742 consists of four DRS4 analog sampling chips recording eight channels each. As these four chips operate on independent high-speed sampling clocks, the trigger signal is also digitized by each chip so that fine time offsets between channels on different chips can be reliably calculated offline.

III. MONTE CARLO SIMULATION

The entire setup is simulated in the RAT-PAC suite [35]. Primary particles are produced (Sec. III A) and tracked in a complete geometry implemented in GEANT4 [36]. When Cherenkov and scintillation processes take place (Sec. III B), individual photons are tracked from the production point to the PMTs (Sec. III C). Once the photon reaches the PMT, a custom model decides whether to produce a photoelectron (PE) based on the photon properties and PMT features (Sec. III D). If a PE is produced, a custom DAQ simulation (Sec. III E) produces a pulse per PE and the total waveform is digitized and stored for posterior analysis. Further details on each of the points are given in the following sections.

A. Cosmic muon generator

Muons and antimuons are generated at 50% ratio following the semiempirical modified Gaisser distribution [37]. The hadronic component at surface is expected to be subdominant by a factor of approximately 50, resulting in a predicted three events within a month's worth of data; thus, this component is not considered. Muons are constrained to pass through the bottom tag volume. There exists the possibility that high-energy electrons produced by muon ionization trigger the bottom cosmic tag. This is reproduced in simulation by including a complete model of the holder material and geometry for both top and bottom tags.

B. Photon production

Cherenkov production is simulated by GEANT4 by the standard class G4Cerenkov. The typical Cherenkov emission spectrum is shown in Fig. 1. Cherenkov photons emitted with a wavelength below a certain value are immediately reabsorbed by the medium and hence are not propagated in the simulation. Scintillation emission is handled by a minimally modified version of the GLG4Sim model [38]. A charged particle passing through a medium deposits an energy E due to ionization. The total number of scintillation photons generated is not expected to behave linearly with E due to quenching effects. This is taken into account by using Birk's law [8] which states that the deposited energy after quenching, E_q , is

$$\frac{dE_q}{dx} = \frac{dE/dx}{1 + k_B dE/dx}, \quad (1)$$

where k_B is Birk's constant. The total number of photons produced, N_γ , is the direct product of E_q and the light yield of the material in question in photons/MeV. *Ex situ* measurements for the scintillation emission spectrum, light yield, and time profile for LAB and LAB-PPO are included in the simulation. N_γ photons are drawn randomly from the emission spectrum of the scintillator under investigation. The spectra for LAB [14] and LAB-PPO [15] are shown in Fig. 1.

The short-term components of the timing profile $\rho(t)$ for the scintillation process is well described by a double exponential model [39], including both a rise time and a decay time. Two further decaying exponentials are included for LAB-PPO, based on Ref. [40]. The simulated time profile is

$$\rho(t) \propto (1 - e^{-t/\tau_r}) \times \sum_i^3 A_i e^{-t/\tau_i}, \quad (2)$$

where τ_r is the rise time and the parameters τ_i and A_i are the decay times and their scale factors.

C. Optical propagation

Optical photons are propagated through different media by GEANT4. Absorption, refraction, and reflection are taken into account according to the material's optical properties. The absorption length of the UVT acrylic used in CHESS (Fig. 1) has been measured with a spectrometer and is included directly in the simulation. The refractive indexes

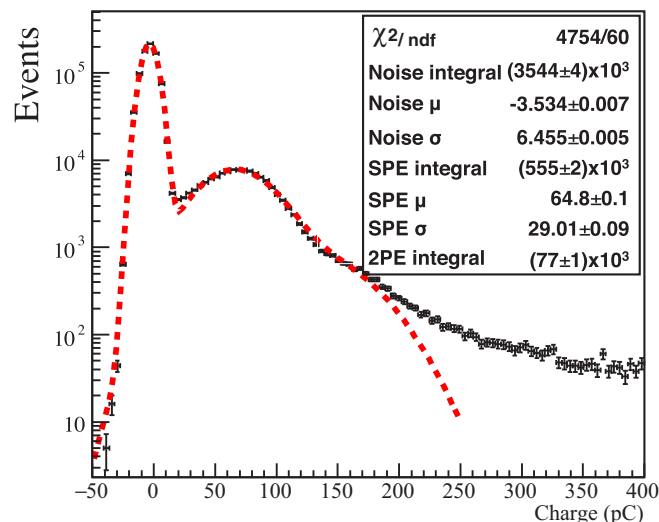


FIG. 5. SPE charge distribution for a single PMT. Data are shown as black points with error bars, and the red dashed line is the result of the fit used to extract the shape of the SPE distribution.

for LAB and LAB-PPO are considered to be the same and are taken from Ref. [15].

Photon re-emission from wavelength shifting materials are simulated in a similar fashion as the scintillation process. Once a photon is absorbed in a medium, there is a finite probability that it will be re-emitted following a specified re-emission spectrum.

D. PMT model

A full and precise simulation of the different PMTs is implemented in RAT-PAC. It contains a detailed PMT geometry (glass, photocathode, dynode stack, and case) as well as a dedicated photon tracking simulation inside the PMT volume. Once an optical photon hits the external boundary of the PMT glass, it is propagated through the different internal PMT surfaces according to the relevant material optical properties. The QE of the PMTs is taken from Hamamatsu specifications [13] and used as an input to the simulation to determine whether or not to create a PE for an incident photon at a particular wavelength. An individual normalization can be applied to the efficiency of each tube to allow for a finite collection efficiency. These are set to 90% for each tube [41]. If the incident photon creates a PE, its associated charge and time are extracted from Gaussian distributions that have been previously calibrated to take into account the PMT gain and electronic delays (Sec. V).

1. Charge distribution model

The single-PE (SPE) charge distribution is modeled as a Gaussian truncated for negative charge values. The SPE charge distribution for individual PMTs has been measured (Sec. V) and Fig. 5 shows that the Gaussian model agrees well with the data.

2. Time profile model

Each PMT has a characteristic transit time and TTS that depends on the PMT design. These numbers are taken from the PMT specifications and included in the simulation assuming the time is Gaussian distributed. The PMT specifications [13] show that the Gaussian model is a very good approximation to the time profile. The mean is set to the provided transit time and the width to the provided TTS. Extra time offset parameters allow for individual delays per electronics channel (referring to the PMT, cable, and readout electronics) primarily due to different cable lengths. These are measured on a channel-by-channel basis (Sec. V).

E. DAQ simulation

For each event, an analog waveform is generated per channel by summing the individual pulses created by each PE (Sec. VB). The waveform is then digitized via a process that mimics the characteristics of the two models of CAEN digitizers used in the detector. High-frequency electronics noise is added to these digitized waveforms following a Gaussian distribution centered at zero and with widths of 0.35 and 0.88 mV for the V1730 and V1742 cards, respectively. These widths are measured from data by performing a Gaussian fit to the residuals of pedestal-corrected noise data. In this way, any effects introduced into the dataset by the digitization process are reproduced in the simulation.

The trigger process implements the conditions described in Sec. IIH2 and decides whether to create a triggered detector event. When an event is created, acquisition windows corresponding to the buffer size of the appropriate digitizer are captured from the digitized waveforms. These windows are used to determine photon hit times and charge using the same process as applied to data in Sec. IV. The trigger process then scans the remainder of the digitized waveform to look for additional triggers within the same simulated physics event.

IV. WAVEFORM ANALYSIS

The full waveform is analyzed to extract individual PMT charges and hit times. An analysis window of 135 ns (675 samples) is chosen starting 160 ns (800 samples) prior to the acquisition trigger. This is defined based on when light from the target is expected to hit the PMT array. The charge in picocoulombs is defined as the integral within that window multiplied by a 50- Ω resistance, corrected by the pedestal charge. The pedestal charge is calculated on a trace-by-trace basis by taking an average of sample values across the pedestal region, which is defined by a 25-ns window right before the analysis window. If fluctuations of more than 5 mV peak to valley are detected in the pedestal region, the waveform is not analyzed. The total integrated charge is converted to an estimated number of detected PEs by normalizing by the mean value of the SPE charge distribution measured in Sec. V.

The time of an individual PMT pulse is defined as the time at which the waveform crosses a threshold given by 25% of the height of a single PE pulse. This threshold is determined by modeling the PMT pulse as a log-normal pulse with parameters extracted from the fit in Sec. VB and an integrated charge

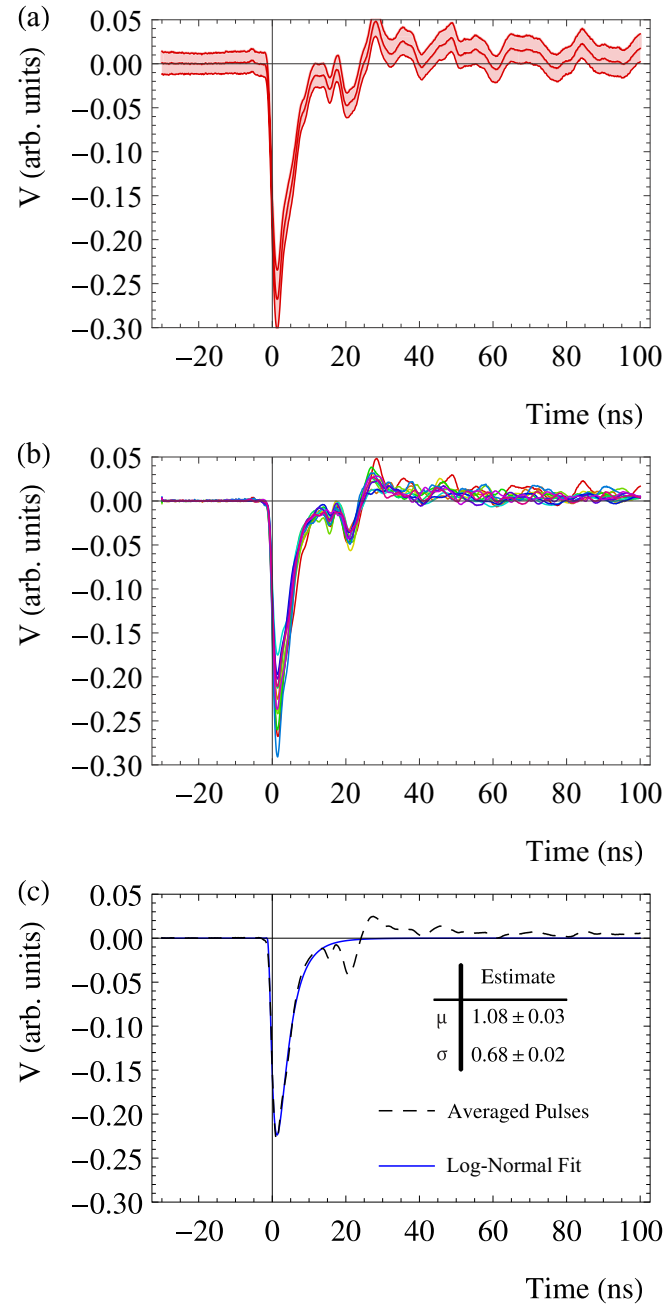


FIG. 6. PMT pulse shape characterization. (a) Mean and RMS spread for one PMT, showing excellent stability in the pulse region. (b) Averaged pulse shapes for SPE pulses for each individual PMT. (c) Log-normal fit to the average pulse shape across all PMTs. In all cases, the pulses are normalized to unit area, so the voltage is reported in arbitrary units.

equivalent to the mean of the SPE distribution for each PMT (Sec. V A). This threshold is well clear of the per-channel noise levels, as can be seen in Fig. 6.

Linear interpolation between ADC samples is used to maximize the time precision. The measured hit time at the PMT array is corrected by the photon time of flight (ToF), assuming that the photons are produced in the center of the target.

V. CALIBRATION

The setup is calibrated using a ^{90}Sr β source in combination with a water-filled target, an LED deployed in the dark box, and a control sample of cosmic muons passing through the acrylic propagation medium. For source data, the veto panels are used to reject coincident cosmic muon events. β decay, muon ionization, and Cherenkov emission are well-understood processes that help to calibrate the optical aspects of the detector. The following sections detail the calibration techniques.

A. PMT gain

PMT gains depend on the supplied voltage and vary tube by tube, so the gain is measured individually for each PMT in the array. The PMT voltages are kept constant between data-taking periods. A direct measurement of the gain is given by the SPE charge distributions. A dim source of light is provided by the ^{90}Sr beta source (Sec. II G) attached to the water target. A small PMT optically coupled to the target is used to trigger the acquisition (Sec. II H 2). The SPE charge distribution for one of the array PMTs is shown in Fig. 5, where a clear SPE peak is identifiable. There is a noticeable population of multi-PE events, which may be due to by-products of muon cosmic events crossing the propagation medium. The muons themselves are easily vetoed using the scintillator panels (Sec. II E), but high-energy electrons and γ s produced by these muons are more difficult to veto and thus cause irreducible tails in the charge distribution.

A Gaussian fit is used to model the charge distributions. To precisely extract the SPE parameters, the noise distribution and the multi-PE event distributions with up to 3 PEs are included and reweighted by nuisance parameters. A Gaussian is assumed for the noise peak distribution with a mean, width, and integral floated in the fit. For multi-PE events, only the event rates with respect to SPE are floated in the fit, since the mean and width are determined by the SPE distribution. As a result, a fit with seven parameters (SPE mean and width, noise mean, width and integral, multi-PE event rates for two and three PEs) driving a multi-Gaussian model is performed, and the mean and width for the SPE of each single PMT are extracted. Figure 5 shows a sample fit. Before inclusion in the Monte Carlo model, the SPE width is corrected for noise, since this is independently modeled, by subtracting in quadrature the width of the noise peak from the fitted SPE width.

The stability of the PMT gains was checked by taking a second set of water calibration data after LS data taking was complete. The gains for all PMTs in the array were observed to be very stable within measured uncertainties.

B. PMT pulse shapes

The characteristic SPE pulse shapes need to be well modeled in order to accurately reproduce the PMT time response in simulation. Events with an integrated charge from $-\frac{\sigma}{2}$ to $+\sigma$ about the mean of the SPE charge were extracted from the SPE calibration data for each PMT independently. The smaller bound on the negative range was introduced

to avoid including noise events. These pulses were then normalized to unit area and a constant fraction threshold was applied to determine a common point of reference between all pulses from a single PMT. This threshold was used to align pulses on a per-PMT basis, and a mean value along with upper and lower rms values were calculated for the normalized voltage in 100-ps time bins. The result is shown for one PMT in the top panel of Fig. 6. The uncertainty in the pulse region is consistent with the noise of the ADCs; this was true for all PMTs. The extracted mean PMT pulse shapes are shown for all 12 array PMTs in the middle panel of Fig. 6. The PMT-to-PMT variation in pulse shape is attributed to small variations in voltage dividers, signal coupling circuits, and individual PMT construction. A log normal of the form

$$\frac{1}{\sigma\sqrt{2\pi}} \exp\left[-\frac{(\log[t - t_0] - \mu)^2}{2\sigma^2}\right] \quad (3)$$

was fit to the average pulse shape across all 12 PMTs (lower panel of Fig. 6) and the resulting fit parameters were used in the simulation to model PMT pulse shapes.

C. Per-channel time delays

The total time delay due to PMT transit times, electronics, and cable lengths is measured for each individual channel and then corrected for in the data. Time delays are measured relative to the average across all PMTs in the array. Typical relative delays are on the order of 100 ps. The primary calibration is performed by deploying an LED at the top of the dark box, such that the light path to each PMT is similar. A full Monte Carlo simulation of this configuration is run and used to correct the data in order to take into account PMT-to-PMT variations in photon ToF and geometry effects. Several datasets are generated by removing and reattaching the LED in order to quantify any uncertainty in the LED position with respect to the simulated one. Cosmic muons passing through the propagation medium are used to evaluate systematics uncertainties in the calculation of the time delays, as they provide an abundant source of prompt Cherenkov light. Events are selected by requiring a coincidence between the lower muon tag and the bottom scintillator panel. Again, a full Monte Carlo simulation is used to correct for ToF and geometry effects in the calibration.

The time distribution for one channel is shown in the upper panel of Fig. 7, where the offset represents the time delay with respect to the average. The measured time delays with uncertainties for each channel from each calibration are shown in the lower panel of Fig. 7. The two data sets show the same trend across the PMT array. The MC-corrected LED data set is used to define the time delays for the final separation analysis. The difference between the two data sets is taken as a measure of systematic error in this calibration.

VI. COSMIC MUON EVENT SELECTION

A deionized water target was used to optimize event selection criteria in order to select Cherenkov ring events, and to reject backgrounds caused by instrumentals and by other physics events. These criteria are then used to determine the

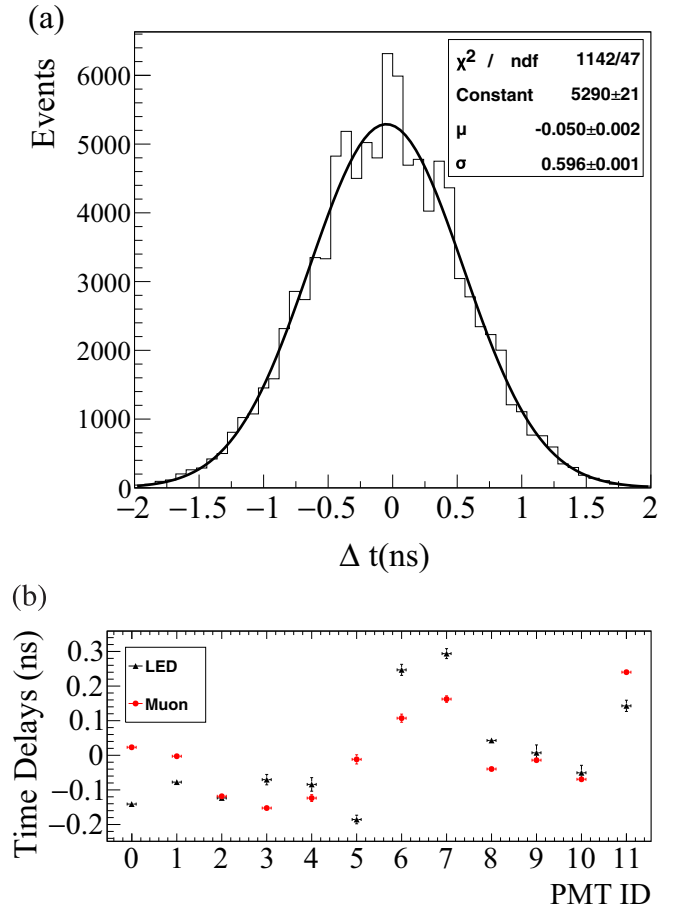


FIG. 7. (a) Time distribution for a single channel relative to a reference channel, overlaid with the Gaussian fit used to extract the relative time delay. (b) Mean and uncertainty on the mean for the per-channel time delays.

sensitivity to identifying ring candidates in LS. The criteria were defined by classifying all events in the water data set according to the clarity of a visible Cherenkov ring (Sec. VI A), and then adjusting relevant cut values to maximize acceptance of good ring candidates and minimize contamination by non-Cherenkov-like events (Sec. VI B).

A. Event classification

Events in the pure water data set were hand scanned in order to understand the different types of event topology and their sources. A classification scheme was developed to sort them according to how well they matched the expected Cherenkov ring geometry, for the purposes of defining a quantitative set of event-selection criteria (Sec. VI B). PMTs with an integrated charge greater than one third of the SPE charge for that PMT were counted as hit. Hits were grouped according to the radius of the hit PMT. The cross-shape PMT deployment results in three radial groupings: the *inner*, *middle*, and *outer* PMTs. The CHES apparatus was designed such that the Cherenkov ring falls on the middle ring for a water target, and the outer ring for a pure LS target. The total number of hit PMTs within each grouping, $N_{\text{Hit}_{\text{inner}}}$, $N_{\text{Hit}_{\text{middle}}}$, and $N_{\text{Hit}_{\text{outer}}}$,

was determined by summing hits across all PMTs within that group. A perfect Cherenkov ring in water is expected to have $N_{\text{Hit}}_{\text{middle}} = 4$ while $N_{\text{Hit}}_{\text{inner}} = N_{\text{Hit}}_{\text{outer}} = 0$. Ring events were selected with the criteria $N_{\text{Hit}}_{\text{middle}} - N_{\text{Hit}}_{\text{inner}} - N_{\text{Hit}}_{\text{outer}} > 2$ to allow either one expected PMT to be missed or one additional PMT to be hit (but not both) to allow for minor noise contamination and increased acceptance.

Background events were sorted into categories according to event topology, in order to understand the primary sources of background. These included instrumental events, which had no clear ring, so-called follower events, in which a secondary particle generated Cherenkov light in the propagation medium, causing unusually high charge on the inner PMTs, and events

in which a cosmic muon shower lit up the majority of PMTs within the array.

B. Cut development

Selection of vertical-going cosmic muon events was achieved using a triple coincidence trigger. The hardware trigger threshold (Sec. II H 2) applied to the lower muon tag was set conservatively low to maximize event acceptance. A software trigger was applied offline by applying a threshold to the charge on both the upper and lower muon tags and to the muon panel directly below the setup in order to select coincidence events.

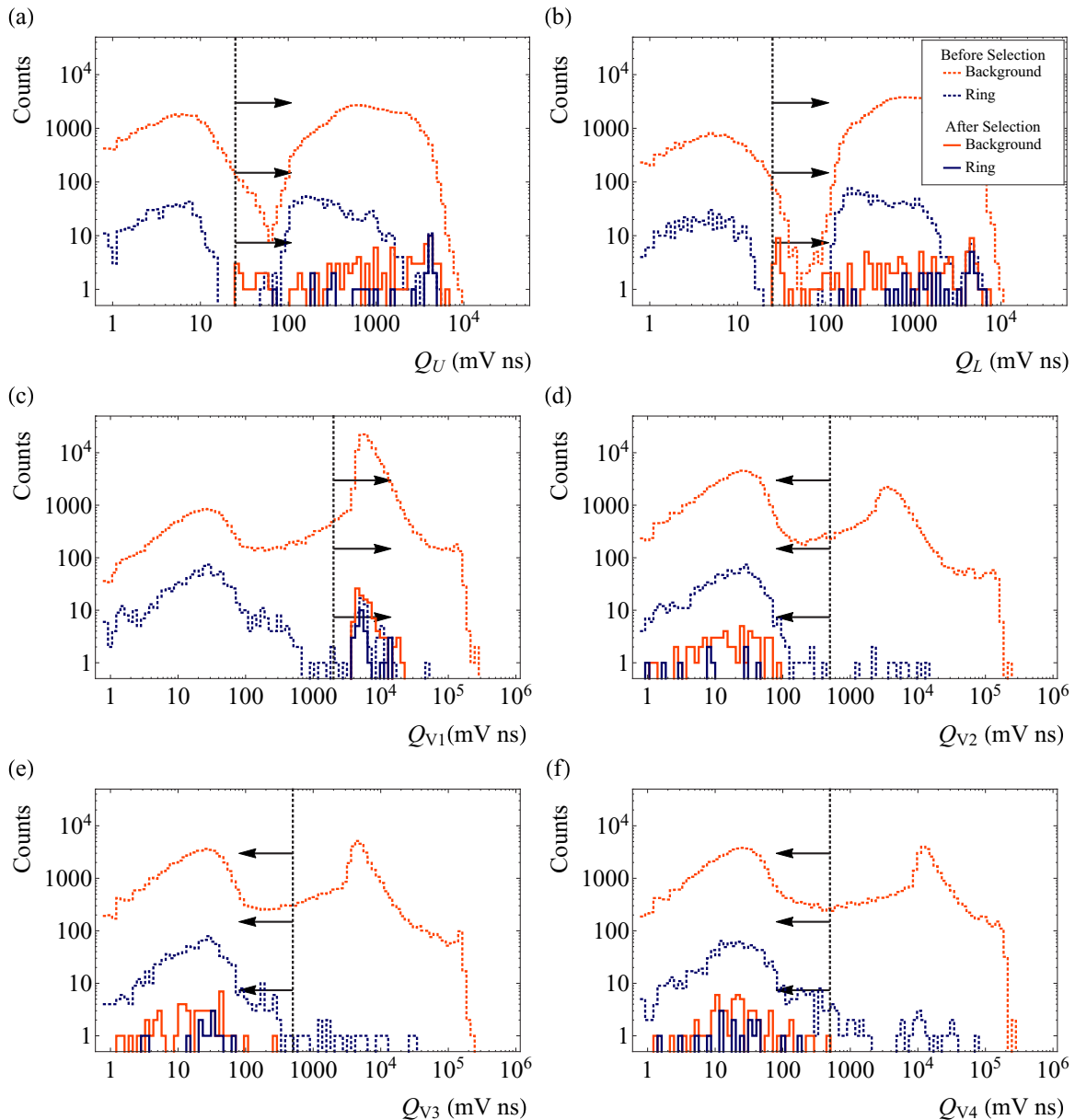


FIG. 8. (Top to bottom, left to right) Charge distribution of events on the upper and lower cosmic tags (Q_U and Q_L) and the four muon panels (Q_{V1} – Q_{V4}). Panel 1 is located directly below the CHESSE apparatus. Events are separated into ring (blue, lower line) and background (red, upper line) according to the criterion in Sec. VI A. Vertical black dashed lines show the cut values in each case with arrows indicating the acceptance region. Distributions are shown before (dashed) and after (solid) application of cuts on these six parameters.

Rejection of events containing either multiple muons or secondary particles was achieved by requiring the charge on all veto panels except the panel directly below the setup to be consistent with zero.

The threshold values applied to the charge seen on the cosmic tags (Q_U and Q_L for the upper and lower tags, respectively), and for each of the muon panels ($Q_{V1}-Q_{V4}$) were selected by optimizing acceptance of ring events and rejection of background events, according to the classification described in Sec. VI A. The data before and after application of these cuts are shown in Fig. 8.

Cuts were also applied to remove so-called follower events, in which muons or muon followers generated Cherenkov light in the acrylic propagation medium, which contaminated the sample of single Cherenkov ring events. This occurred in two cases:

- (1) *Electron contamination*: The cosmic muon triggered the acquisition, but a secondary particle passed through the propagation medium.
- (2) *Muon contamination*: The secondary particle triggered the lower muon tag and the muon itself passed through the propagation medium.

The secondary particles do not always make it to the muon panels and therefore cannot be vetoed directly; thus, the only information available for rejecting these events is the PMT array. Clean cosmic muon events are expected to produce hits only on the middle PMTs (for a water target, or outer PMTs for LS). In both cases of follower events, the majority of Cherenkov light generated in the propagation medium was observed to fall primarily on the innermost PMTs within the array. This was confirmed by Monte Carlo simulations of each event type, which demonstrated that muon followers do produce events with this topology. Simulations of these events show a clear tail in the PE distribution observed on the inner PMT group for both water and LAB-PPO targets (Fig. 9). These events typically create between 30 and 400 PEs in the innermost PMTs, making their identification in both water and LS possible by analysis of the charge on these PMTs.

A cut was designed to reject these events based on event topology: Since the Cherenkov ring geometry is not expected to produce hits on the inner PMTs for either a water or LS target, the total number of estimated PEs on the inner PMTs was used to identify clean rings. In water this charge is expected to be very low (consistent with noise), whereas in LS the total charge will be higher due to scintillation photons. However, as demonstrated in Fig. 9, a large fraction of follower events can still be removed with a high-charge cut. A cut was placed at a summed PE count of 40 for water and LAB targets and 500 for LAB-PPO. These cuts were conservatively chosen based on the simulations to reject events with high light contamination due to secondary particles with a minimal impact on the efficiency. Performance of this cut in water is shown in the top panel of Fig. 9. The high-charge tail due to follower events is similar to that seen in the simulation, supporting use of the simulation for defining this cut for both water and LS targets. The cut value selected for a water target

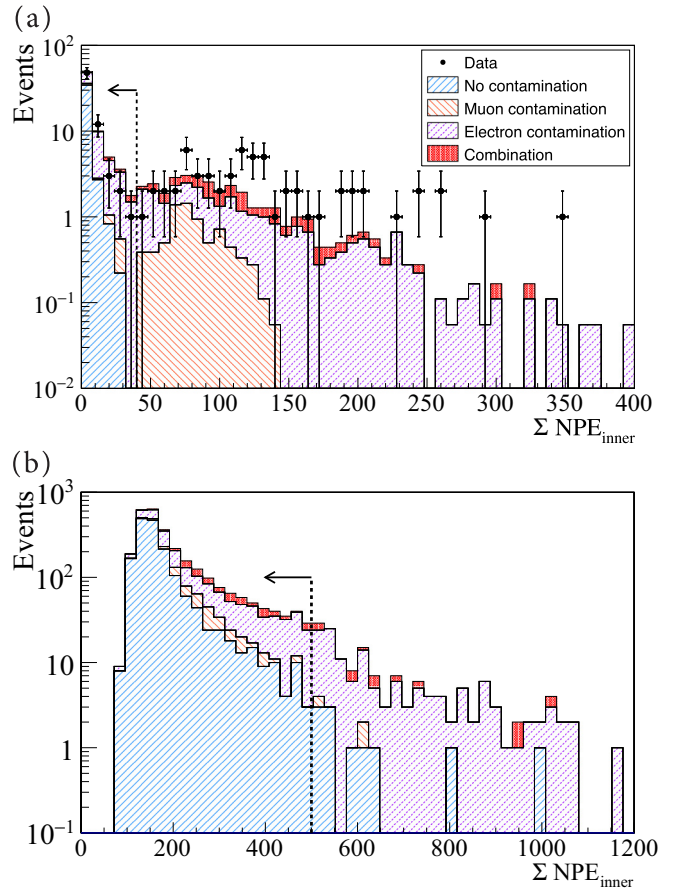


FIG. 9. Monte Carlo simulation of the summed PE distribution on the inner PMT group due to cosmic muon events with perfect rings (turquoise, right diagonal hatching), muon contamination (orange, left diagonal hatching), electron contamination (purple, right diagonal dashed hatching), and the total (red, solid). (a) Water target, with water data overlaid to show the agreement, and (b) LAB-PPO target. The vertical black dashed line represents the chosen cut value, with arrows to illustrate the acceptance region.

removes a large fraction of the remaining background events, with zero sacrifice in the control sample.

VII. EVENT-LEVEL ANALYSIS

Time separation of the Cherenkov and scintillation photon populations is based on the hit time residual distributions for each radial PMT grouping (inner, middle, and outer). The hit time residuals are evaluated as the PMT hit times with respect to the event time, corrected by per-channel delays (Sec. V C) and by the photon ToF. The ToF depends on the distance between the target and the PMTs and on the refractive indices of the different media. It is estimated for each PMT radial group to be 626, 536, and 473 ps for the inner, middle, and outer PMT rings, respectively.

The time at which the cosmic muon passes through the target, referred as the event time, is calculated using two different approaches. The most straightforward is using the time at which the lower muon tag goes above threshold, since this triggers the acquisition. Nevertheless, the cosmic tags

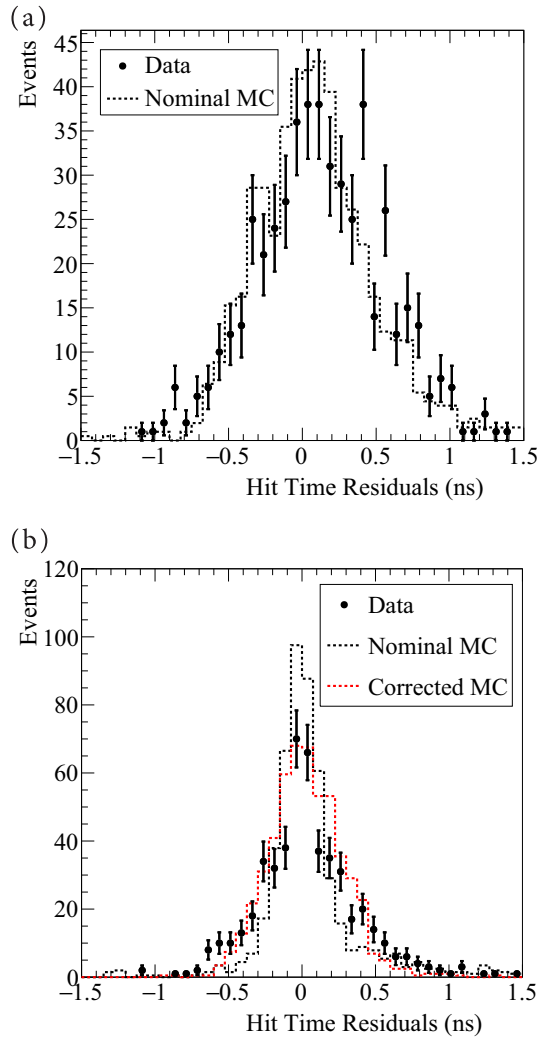


FIG. 10. Distribution of hit time residuals for ring candidate events in water for middle PMTs, where the Cherenkov ring is expected. Data points are shown with statistical errors, with the Monte Carlo prediction overlaid (dashed lines). (a) Hit times with respect to the lower muon tag time and (b) hit times with respect to the reconstructed event time.

suffer from a worse time resolution than the fast PMTs in the array due both to the scintillator response and the larger PMT TTS. Hence, a higher precision event time is defined using the PMT hit times by using the median of the four earliest hits in the event, after time calibration and photon ToF correction. This provides a robust time reference since the prompt hits are due to Cherenkov light, whose time profile is very sharp.

The hit time residual distributions evaluated using each option for the event time are shown in Fig. 10, overlaid with the Monte Carlo prediction in each case. The residual distribution with respect to the lower muon tag time is extremely well reproduced by the Monte Carlo, demonstrating the precision of the model. The simulation slightly underpredicts the width of the higher precision distribution of residuals with respect to the reconstructed event time. This could be explained by multiphoton effects, small differences in the PMT pulse shape,

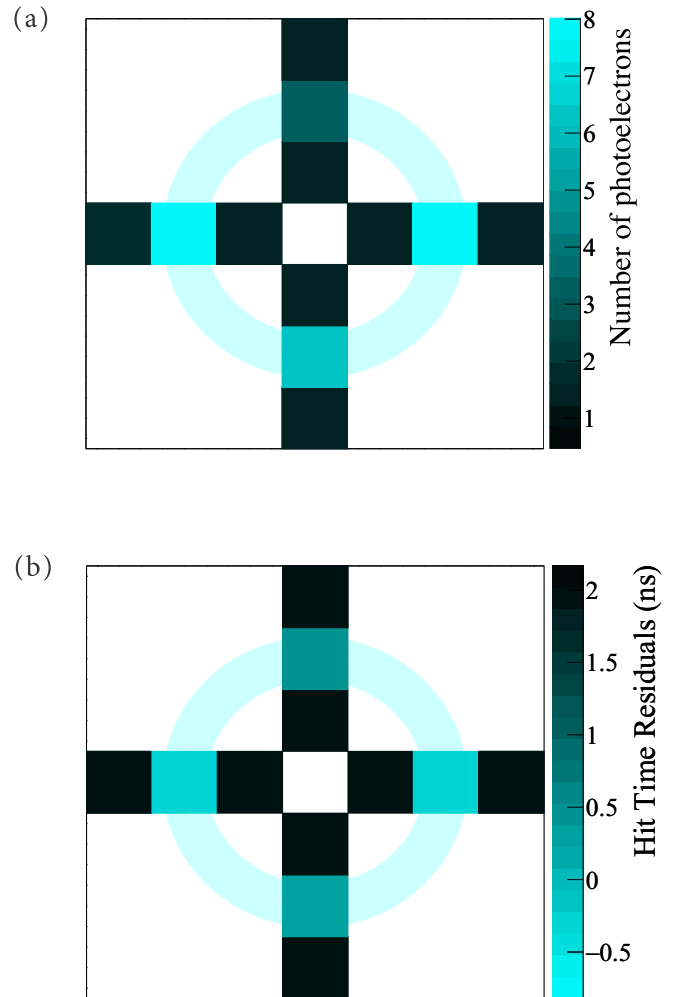


FIG. 11. Typical ring event in the water data set. (a) Estimated number of detected PEs and (b) hit time residuals.

and underestimated PMT TTS. A Gaussian correction of $\sigma = 214$ ps is included in the Monte Carlo in order to take these effects into account and to better reproduce the time resolution seen in data.

VIII. CHERENKOV RING IMAGING IN WATER

After application of the event selection criteria described in Sec. VI, 137 ring candidates were selected in the water dataset. The number of detected PEs and first photon hit time residuals for a typical event are shown in Fig. 11. The averages across the data set for both the number of detected PEs per PMT and the hit time residuals are shown in Fig. 12; both show a clear ring structure.

The distributions of hit time residuals for each PMT radial group (inner, middle, and outer PMTs) are shown in Fig. 13, with the Monte Carlo prediction overlaid (with the additional smearing described in Sec. VII). The middle PMTs are the only ones detecting a sizable amount of light, and their time distribution is very sharp, compatible with the expected Cherenkov rings in water. The inner and outer PMTs are rarely hit.

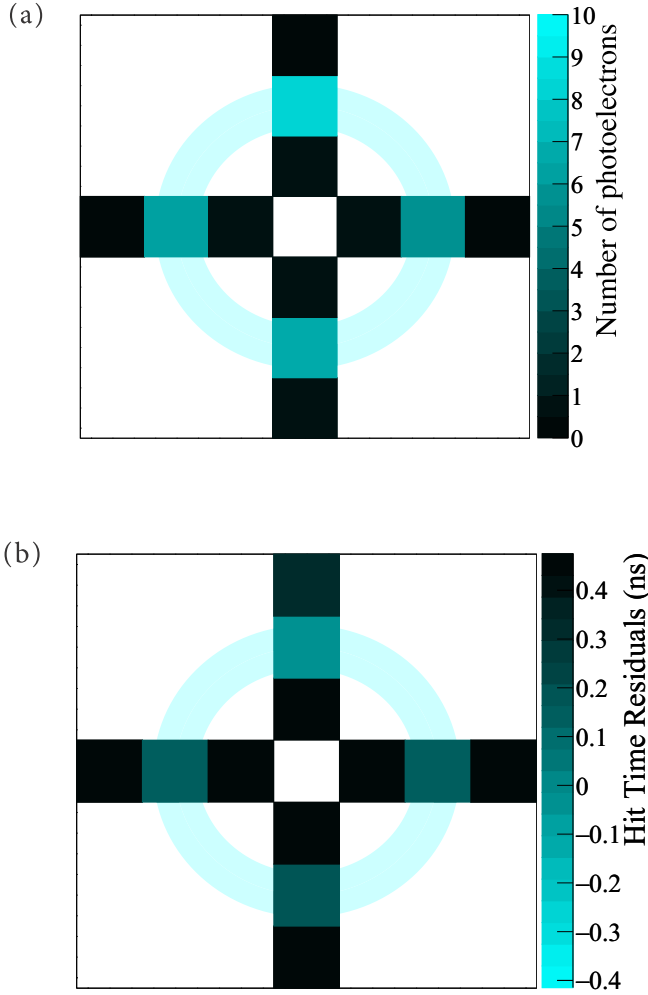


FIG. 12. (a) Averaged number of detected PE and (b) averaged first-photon hit time residual per individual PMT for ring candidates in water data.

The characteristic sharp time distribution of Cherenkov light provides an excellent source for estimating the CHESSTIME resolution. The time distribution of the observed Cherenkov rings provides a measurement of 338 ± 12 ps FWHM for the time precision of the CHESSTIME detector. The limiting factor in this precision is the PMT TTS (300 ps FWHM).

IX. PROSPECTS WITH LIQUID SCINTILLATOR TARGETS

An analysis of Monte Carlo data has been performed to predict the performance of CHESSTIME for ring imaging and Cherenkov and scintillation separation with a pure LS target, using both LAB and LAB-PPO. The targets are simulated using properties from [14,15,40,42,43]. The scintillation light yield is set to 1010 photons/MeV for LAB [42] and 10 800 photons/MeV for LAB-PPO [15]. Quenching is modeled using values for Birk’s constant of $k_B = 0.0798$ mm/MeV in LAB and LAB-PPO [43]. The emission spectra are shown in Fig. 1. The time profile is modeled in the simulation as described in Sec. III B, with a rise time of $\tau_r = 1$ ns for LAB-PPO and $\tau_r = 7.7$ ns for LAB, and decay times of

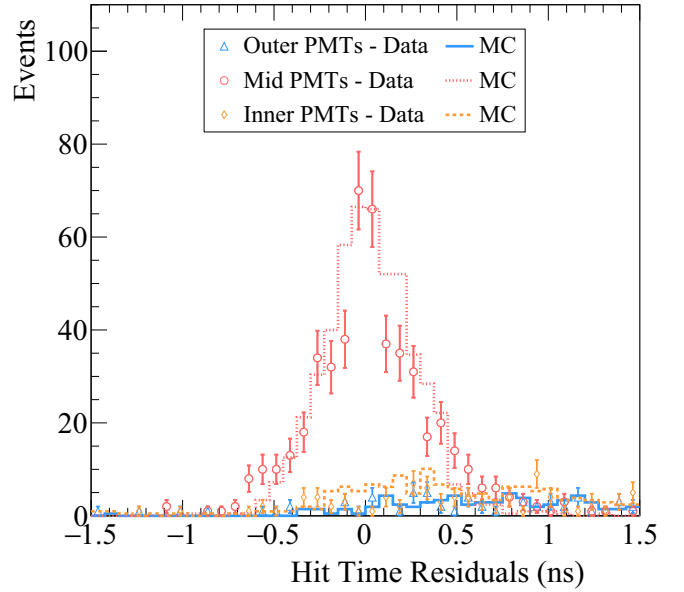


FIG. 13. Distribution of hit time residuals for ring candidate events in water for each PMT grouping. Data points are shown with statistical errors, with the Monte Carlo prediction overlaid (dashed lines).

$\tau_1 = 4.3$ ns, $\tau_2 = 16$ ns, $\tau_3 = 166$ ns [40] for LAB-PPO, and $\tau_1 = 36.6$ ns, $\tau_2 = \tau_3 = 0$ [42] for LAB.

Several thousand cosmic muon events are simulated for each target, producing the hit time residual distributions shown in Fig. 14 for LAB and Fig. 15 for LAB-PPO.

The small peak on the inner and middle PMTs seen in LAB is due to Cherenkov light contamination from follower events. The earliest hits are registered in the outer PMTs, where the Cherenkov ring is expected, while later features are due to

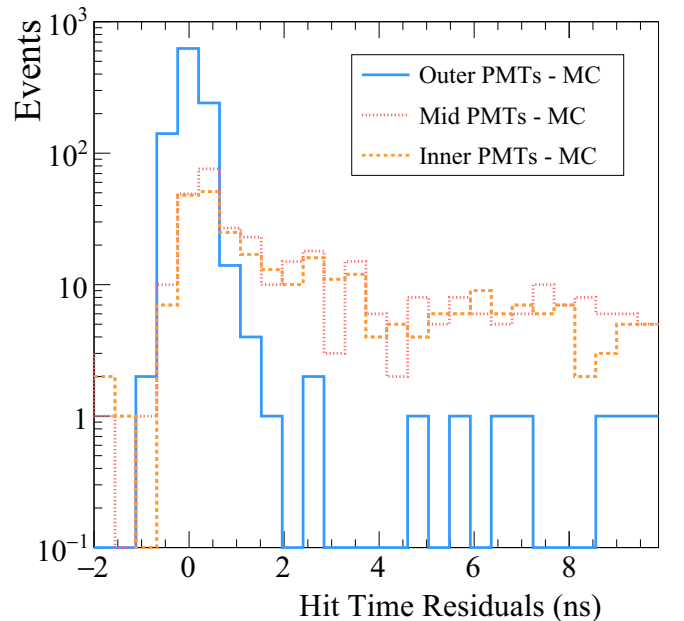


FIG. 14. Projected hit time residual distributions for LAB as predicted from the Monte Carlo simulation.

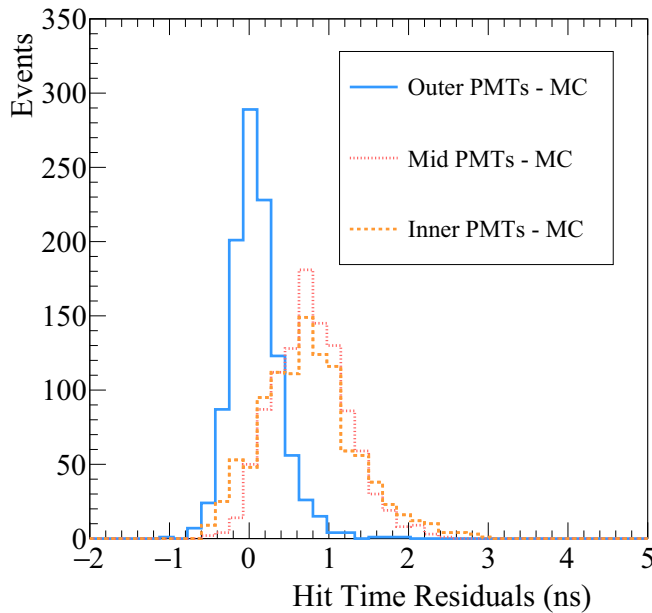


FIG. 15. Projected hit time residual distributions for LAB-PPO as predicted from the Monte Carlo simulation.

scintillation light. Between 5 and 10 PE are expected on each PMT within the Cherenkov ring due to Cherenkov light alone. The PMT hit time residual is based on the first photon hit time for each channel, thus with high confidence the hit time of each PMT within the Cherenkov ring can be assigned to Cherenkov photon hits. Hits outside the Cherenkov ring are due to scintillation light. The separation of Cherenkov and scintillation photons can thus be defined by comparing the distributions of hit time residuals on PMTs within the expected Cherenkov ring location (the outer PMTs for LAB and LAB-PPO) and those outside the ring (inner and middle PMTs).

A timing cut can be developed to optimize this separation, selecting hits that occur before a time threshold, t_c . The efficiency of identifying Cherenkov hits is defined as the fraction of outer PMT hits (Cherenkov hits) that occur before t_c . The contamination due to scintillation photons is evaluated as the fraction of all PMT hits occurring before t_c that are due to scintillation photons, i.e., the number of inner and middle PMT hits occurring before t_c divided by the total number of hits before t_c .

A value of $t_c = 0.4$ ns results in Cherenkov efficiencies of $94 \pm 1\%$ in LAB and $81 \pm 1\%$ in LAB-PPO, with contaminations of $12 \pm 1\%$ and $26 \pm 1\%$, respectively.

A study has been performed in Ref. [11] of the impact of such separation on a potential large-scale NLDBD search. This paper finds that solar neutrinos become a limiting background in a next-generation detector. This dominant background can be rejected by use of the directional Cherenkov component, if separation of Cherenkov and scintillation light can be achieved. Assuming a conservative rejection factor of two for these events, the study shows that sensitivity can be achieved down to the bottom of the inverted hierarchy (15 meV). This study assumed a conservatively low light yield, based on the assumption that a WbLS target would be required in order to

achieve the Cherenkov separation. However, the work in this paper demonstrates the potential to identify the Cherenkov component even in a pure LS target, thus allowing directional sensitivity in a high light yield detector. Such an experiment could have increased sensitivity to NLDBD, even into the normal hierarchy [44]. Reference [45] discusses an idea for how to use this separation to extract particle direction in a scintillator detector.

X. CONCLUSIONS

The time resolution of the CHES experiment has been demonstrated to achieve the sub-ns precision required for successful separation of Cherenkov and scintillation light. The principle of Cherenkov ring imaging has been demonstrated using a deionized water target. A time resolution of 338 ± 12 ps FWHM has been achieved and clear Cherenkov rings have been detected in both charge and time on an event-by-event basis. A detailed simulation with LAB and LAB-PPO shows that, with this time resolution, time-based separation of the Cherenkov component from the scintillation light is possible with an efficiency of 94% and 81%, respectively, with scintillation contamination of 12% and 26%.

If this separation can indeed be demonstrated in the experimental data, then it would have significant implications for next-generation neutrino experiments. Successful Cherenkov and scintillation separation would benefit a broad physics program, including low-energy physics such as NLDBD and solar neutrinos; astrophysics topics such as supernova neutrinos and the diffuse supernova neutrino background; and high-energy physics such as nucleon decay, neutrino mass hierarchy, and CP violation. Understanding the degree of separation that can be achieved and quantifying how this varies with the specifics of the target cocktail will be critical steps in developing the program for a future large-scale experiment such as THEIA [12].

The next phase of CHES will deploy pure LS in the target, followed by WbLS samples with varying LS fractions. This will enable a full understanding of how the signal separation varies with cocktail. In a future phase, CHES will be upgraded by populating the array with 12 additional fast PMTs. CHES can also be used as a test bench for studies of next-generation MCP-based photon detectors [16–18]. The narrow pulse width of these detectors (tens of ps, compared to 5–10 ns for a typical PMT) could substantially improve the potential for charge-based separation by allowing much higher precision PE counting.

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