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A 20MK TEMPERATURE SENSOR

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Abstract
We are developing a 20mK temperature sensor made of neutron transmutation doped (NTD) germanium for use as a phonon detector in a dark matter search. We find that NTD germanium thermistors around 20 mK have resistances which are a strong function of temperature, and have sufficient sensitivity to eventually reach a base line rms energy fluctuation of 6eV at 25mK. Further work is needed to understand the extreme sensitivity of the thermistors to bias power.

Introduction
It is believed that 90% of the mass of the universe does not radiate electromagnetic waves. What this "dark matter" is made of is not known, but there have been many suggestions [1,2]. One group of candidates is exotic particles contained in the halo of our galaxy, for instance photons or heavy neutrinos. Such particles could be detected directly with detectors of a few hundred grams if they can obtain thresholds of a few hundred eV [3]. Phonon detectors appear to be a hopeful technique for the realization of these requirements [4,5].

A thermal detector for phonons [6] in this context consists of an energy absorbing crystal of heat capacity C with an attached temperature sensor of heat capacity C0. The temperature sensor is connected to a heat sink through a thermal link with thermal conductance G. When a particle interacts with the detector it will deposit energy in the absorber, where it appears as phonons. These phonons (which are here presumed to be ballistic, although this has not yet been demonstrated) will then transfer a fraction, ε, of their heat to the sensor, and are thus detected. With given energy threshold and sensor mass requirements, we can make a rough estimate of the necessary operating temperature based on the system noise. There are several noise sources: thermal noise, Johnson noise, amplifier noise and excess noise, but with good sensor responsivity (i.e Vbias/ΔT) and good electronics it should be possible to make the thermal noise dominant. Over a bandwidth B, the latter is given by [7,8] εVn=√(kTεC0/2εB) where C is the effective heat capacity of the system and τ is the thermal time constant (τ = C/G). In order to have a low effective heat capacity and to obtain the thresholds required for dark matter detection, for instance, it may well be necessary to work at temperatures near 20 mK. To our knowledge no one has yet demonstrated proper operation of a sensor in this temperature range with a good responsivity.

One possibility for a temperature sensor is a thermistor. Suppose the resistance of the thermistor is a rapidly varying function of the temperature, R = R(T). If the resistor is biased at a constant current, then the voltage variation due to a temperature change is

\[ ΔV = \frac{dV}{dT} \Delta T \]

where ΔV is the energy deposited in the absorber. For ballistic phonons it could be arranged so that C = C0 (i.e., the effective heat capacity of the sensor) and ε is more specifically defined as the efficiency of energy transfer from ballistic phonons to electrons in the sensor. (If, on the other hand, the phonons turn out to be thermal, then C is the effective heat capacity of the absorber plus sensor, and ε = 1.) We present here the first results on the sensitivity of a thermistor operating at 25 mK.

Sample Preparation
We have tested thermistors made of NTD germanium [9,10] with dopant concentration nA = 6.64 × 10^16 cm^-3. Their dimensions are 1mm x 1mm x 0.25mm. The 1mm^2 faces are covered with 4000 Å of gold for electrical contact. A boron layer approximately 2000 Å thick implanted into the germanium beneath the gold ensures uniform electrical contact. A thin layer (500 Å) of palladium between the gold and boron binds these two together. We have chosen the relatively large surface area of these faces (1mm^2) because we anticipate eventual detection of ballistic phonons. For ballistic phonons a larger surface between the sensor and the absorber yields a greater efficiency of heat transfer, and hence greater sensitivity.

Figure 1 shows the sample installed on a dilution refrigerator. The sensor is glued with conductive epoxy to a copper-kapton-copper sandwich which is indium soldered to the copper sample holder. The kapton (125 microns thick) provides electrical isolation between the sensor and the refrigerator. The sample holder is then screwed to the mixing chamber which has a base temperature around 20 mK. This design maximizes thermal clamping between the sensor and the heat sink. A 0.7 mil aluminum lead is wedge bonded to the sensor. Aluminum is superconducting at the operating temperatures, therefore the thermal conductance of the wire is very small and little heat flows through it. Lastly, the sensor is completely enclosed in a copper radiation shield which is at the mixing chamber temperature.

Experimental Results
The I-V curve is obtained by applying a bias voltage Vbias and measuring the resulting voltages across the bias resistor Rbias and the sensor resistance Rsensor.

I-V Measurements
Figure 3 shows the I-V curves taken at different mixing chamber temperatures. Note the strong dependence of the sensor power resistance on this temperature. It has been suggested that the curve should obey the relation R = R0 exp(ΔT/11). In figure 4 we plot the zero power R against T and find that it obeys this prediction over 5 decades. For the sample shown we found R0
Bias

Figure 2. Schematic of the circuit used for I-V measurements

All the lines going into the screen room are filtered.

Figure 3. I-V curves of NTD Ge at different mixing chamber temperatures.

Figure 4. Dependence of the zero bias resistance of NTD Ge on the mixing chamber temperature. These points are from figure 3 and other measurements we performed on the same sample.

Figure 5. Power (P=IV) vs. static resistance (R=V/I) for NTD Ge at different mixing chamber temperatures.

\[ R(\Omega) \]

\[ R(T) = 0.0474 \exp \left( \frac{8.151}{T} \right) \]

\[ I/sqrt(T(K)) \]

\[ T=19.0mK \]

\[ T=24.7mK \]

\[ T=28.3mK \]

\[ T=36.5mK \]

\[ P(pW) \]

= 0.0474 Ohm and \( \Delta = 8.151K \), which is the straight line on the plot. The horizontal error bars reflect a 2% uncertainty in the temperature of the mixing chamber.

More puzzling is the marked deviation from linear behavior at non-zero bias powers, despite the fact that our sensor is well thermally clamped to the heat sink. This is evident in figure 3 and also in figure 5 where we plot the static resistance, V/I, as a function of bias power, IV. Both the degree of curvature of the IV plots and the bias power at which this curvature begins depend strongly on the mixing chamber temperature. Further experiments (to be described elsewhere) suggest that this is indeed not a problem of a poor heat link between the sensor and the heat sink, but rather an intrinsic property of our thermistors. Other groups have seen this effect at higher temperatures [12].

**Responsivity \( \text{d}V/\text{d}T \)**

These nonlinearities in the IV curves mean that the choice of bias current is very important to obtain maximum thermistor sensitivity. A quantity of interest is the change in voltage with temperature for fixed current, \( \text{d}V/\text{d}T \), which we shall refer to as the responsivity. It has been obtained from the IV curves by considering the voltage as function of temperature for fixed current. Figure 6 shows the responsivity as a function of the bias power. At each heat sink temperature there is evidently a bias condition which yields optimum sensitivity. In figure 7 we plot this maximum responsivity as a function of heat sink temperature.

**AC Measurement**

In addition to an understanding of the IV curve, optimum use of thermistors requires knowledge of the thermal noise and thermal conductance, \( C_s \) and \( G_s \), of the sensor. These can be obtained from the heat capacity, \( C_v \), and the thermal time constant, \( \tau \), which we determined experimentally using an AC pulse measurement technique [13]. A schematic of the circuit is shown in figure 8a. Data was taken with a mixing chamber temperature of 24 mK, and the sensor DC biased at 1.0 nA when the resistance \( R=V/I \) was \( \approx 2 \) MΩ. Figure 8b shows the bias current as a function of time with an applied square wave. The response of the sensor voltage to this bias current is shown in figure 8c. For a thermistor of heat capacity \( C_v \) and thermal conductance \( G_s \), using the small signal approximation, the time constant for the voltage relaxation is

\[ \tau = \frac{C_v}{G_s} \]

and the initial pulse height \( \Delta V \) divided by the time constant is

\[ \frac{\Delta V}{\tau} = \frac{2122R}{C_s} \frac{\Delta T}{R} \]

Although we are clearly not in the small signal regime and obviously observe strong nonlinearities, such formulas give us order of magnitude estimates for our sensor of \( C_v = 0.8 \times 10^{-3} \text{J/K} \) and \( G_s = 2 \times 10^{-8} \text{W/K} \).
Minimum Detectable Energy

From the measured responsivity, heat capacity, and thermal time constant, we may estimate the sensitivity of our device. If there is no excess noise, then as mentioned above there are three contributions to the baseline energy fluctuation. Fluctuations in phonon number produce energy fluctuations with spectral density $(\delta E)^2 = 4k_B G T^2/(4(\pi f)^2+1/\tau^2)$ per Hz, where $k_B$ is Boltzmann's constant, $T$ is the sensor temperature, and $G_s$ is the sensor thermal conductance. For the electronics noise we assume an amplifier noise level of $e_n^2 = (2nV)^2/Hz$ (which should be obtainable.) The thermistor, since it has resistance $R$, also has Johnson noise $(\delta V)^2 = 4k_B T R/Hz$. If we neglect thermal feedback effects, it can be shown in a manner analogous to Mather's noise treatment [7,8], that the energy fluctuation obtained with optimal filtering is

$$\delta E = \left[\frac{1}{2} G_s \frac{(\delta V)^2}{\delta T} - \frac{1}{2} k_B \frac{1}{\tau^2} + \frac{1}{2} k_B \frac{T}{R} \right]^{1/2}$$

Using the measured values of $G_s$, $C_g$, $\tau$, and the responsivity at 24 mK of $dV/dT = .25 V/K$, we predict an rms energy fluctuation $\delta E = 6 eV$. This can be compared, for instance, with the thermal noise alone (integrated over a bandwidth $B = 1/2\tau$) of $\delta E = \sqrt{k_B T C_g^2} = 1.6 eV$.

Conclusion

We have tested a temperature sensor made of NTD germanium at temperatures around 20 mK. We found that the sensor resistance at zero bias as a function of mixing chamber temperature follows the relation $R = R_0 \exp(\sqrt{\Delta/T})$ as low as 19 mK. From the observed responsivity $dV/dT$, the thermal time constant $\tau$, and the sensor heat capacity $C_g$ all at 25 mK, we infer an rms energy fluctuation of 6 eV. We are still limited by the responsivity of our device, but our results show that these type of sensors are promising at temperatures as low as 20 mK. More research is needed to determine the nature of the extreme sensitivity of thermistor resistance on bias power, and to find ways to improve the responsivity.

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References


