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March 1982

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 ${\bf x}, {\bf y} \in \mathbb{R}^m \times \mathbb{R}^m$, ... ${\bf x}$,

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OFF-NORMAL PHOTOELECTRON DIFFRACTION STUDY OF THE c(2x2) SELENIUM OVERLAYER ON Ni(OOl)

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ABSTRACT

-1-

Off-normal energy-dependent photoelectron diffraction data are presented for the c(2x2)Se-Ni(001) system, and compared with calculations to confirm the accepted fourfold hollow site geometry. The best agreement is found for a d_1 spacing of 1.55Å, confirming earlier normal photoelectron diffraction and low energy electron diffraction results. The size of the photoelectron diffraction modulations decreases with increasing polar angle of emission. An R-factor analysis indicates that the theory-experiment fit is very good, especially at smaller polar angles. Off-normal photoelectron diffraction is shown to be capable of distinguishing the correct site geometry for cases in which theoretical normal photoelectron diffraction curves for two geometries exhibit an "accidental coincidence" in peak positions.

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I. Introduction

Photoe-lectron diffraction (PD) can be observed by measuring the angle-resolved photoemission intensity from a core level of an adsorbate atom or molecule bonded to a single crystal metal surface. If the photon energy hv is varied and the core-level photoelectrons are collected in the direction normal to the crystal face, diffraction of the photoelectrons can yield a strongly oscillatory dependence of the photoelectron intensity on kinetic energy. This specialized case of PO, termed normal photoelectron diffraction (NPD), has been used to determine the structures of overlayers adsorbed on metal surfaces. $1-6$ The first experimental observation of NPD from a core level was made in 1978. $¹$ Dynamical scattering theory with calculated dipole matrix</sup> elements and phase shifts was used to analyze the data and illustrate their usefulness. This effect has now been observed in a large number of adsorbate-substrate systems and is found to be particularly suitable for accurate determination of the spacing between an adsorbate layer and the substrate (d_1) . Structural information has been generally derived from a comparison of experimental and theoretical NPD curves, $1-7$ although a more explicit method has been developed recently. $3,8$ In this paper, we demonstrate for the first time that off-normal energy-dependent PD can also be used to derive accurate surface structures.

In an earlier paper, $4\,$ we observed that the modulations in offnormal PO were not nearly as pronounced as those in NPD, making an accurate structural determination more difficult. In that work, offnormal data for the c(2x2)Se(3d)-Ni(OOl) system, taken at a coarse

-2-

angular mesh, were presented. In this paper, we report off-normal PO curves of the same system, taken at intervals of 5° in polar angle, for two different azimuthal orientations. The finer angular mesh in the new data allows us to follow the evolution of the PD peaks with polar angle more carefully. More importantly, the experimental data have been fitted by multiple scattering theory, allowing an implicit structural determination of the adsorption site of the $c(2x2)$ Se overlayer on Ni(OOl).

Section II contains experimental information. In Section III we briefly discuss the method and inputs of the multiple scattering calculations used to fit the experimental data. In Section IV we present and discuss the PD data. An R-factor analysis of the theoryexperiment fit is presented in Section V, and conclusions from this work are given in Section VI.

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II. Experimental

All the data reported here were obtained with an angle-resolved photoemission (ARP) spectrometer described earlier. 9 The spectrometer has low energy electron diffraction (LEEO) and Auger electron spectroscopy capabilities, as well as an adsorbate gas introduction system which allows for effusive beam dosing. The base pressure of the vacuum chamber was 2×10^{-10} torr during all the measurements. The pressure rose to as high as 5×10^{-9} torr during effusive beam dosing. The Ni(001) crystal was oriented to within 1° of the [001] direction. The crystal was cleaned by hot (1025K) and room temperature cycles of argon-ion sputtering followed by annealing to 875K, resulting in a surface essentially free of impurities with a sharp (lxl) LEEO pattern. The $c(2x2)$ Se overlayer on Ni(001) was prepared by directing an effusive beam of H₂Se at the crystal, which was heated to 500K. An exposure of 20-30 L was required to produce a sharp c(2x2) LEEO pattern on Ni(OOl).

The experiments were performed on Beam Line 1-1 at the Stanford Synchrotron Radiation Laboratory (SSRL). Low resolution ARP spectra were taken of the Se(3d) level, which has a binding energy of 62 eV with respect to the vacuum level. Spectra were taken at intervals of 3 eV in photon energy. The angle-resolved relative intensity of this level was deduced by calculating the area of the core level peaks (after background subtraction) and adjusting for photon flux and analyzer transmission. The kinetic energy range of the resulting PO curves was generally 40-200 eV. Experimental geometries are indicated in the figures.

 $-4-$

III. Theory

The multiple scattering theory used to calculate the photoemission intensity versus energy (IE) curves was described earlier.^{7,10} The 3d initial state wavefunction of Sewas obtained from a self-consistent X_{α} scattered-wave calculation of a Ni₅Se cluster. Dipole transition matrix elements were calculated at each photon energy. The final state was calculated at each kinetic energy by a Green's function method corresponding to the $c(2x2)$ Se-Ni(001) slab geometry. All multiple scattering of the photoelectron was included until numerical convergence was reached.

Inputs to the multiple scattering method include: (1) substrate (nickel) phase shifts obtained from the self-consistent band structure potential of Wakoh, 11 and (2) Se phase shifts obtained from the same X_{α} scattered-wave calculation that generated the Se(3d) wavefunction. The imaginary part of the optical potential for the final state was $E+V_0$ 1/3 taken to be V_I (eV) = 3.8 x ($\frac{0}{90+V}$), where E is the energy in o electron volts above the vacuum. The inner potential used was $V_0 =$ 13.2 eV. Earlier, we had used V_o = 11.2 eV for Se on Ni(OO1),¹² but the R-factor analysis described in Section V gave a slightly better value for $V_0 = 13.2$ eV. For example, the normalized R-factor at the optimal structure (see Section V) is 0.789 for $V_0 = 11.2$ eV and 0.760 for $V_o = 13.2$ eV, indicating a 4% improvement. Although the 2 eV shift slightly improved the R-factor, the same d_1 spacing was chosen by either $V_0 = 11.2$ eV or 13.2 eV.

The Se(3d) level was placed at 62 eV below vacuum. Calculations of the IE curves were made for the same energy range as the data, i.e.,

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40-200 eV. The Se atom was placed at the fourfold hollow site at Se-Ni perpendicular spacings (d_1) of 1.45, 1.55, 1.65 and 1.75 Å. Earlier analyses have convincingly shown that the adsorption site is the fourfold hollow. $2, 4, 12-14$ In this study, we did not place the Se at other binding registries, except for $d_1 = 2.34$ Å in the top site (see Section IV and Fig. 4).

IV. Results and Discussion

In an earlier paper, $4\,$ we presented limited off-normal photoelectron diffraction data on c(2x2)Se-Ni(001). In that work, data were taken for emission into the [100] azimuth at polar angles of 15°, 30°, and 45°, and into the [110] azimuth at polar angles 18°, 36°, and 54°. The curves were rich in structure, but the intensity modulations were much smaller than those at normal emission. The PO final state can be thought of as a superposition of time-reversed LEED beams.⁴ If the detector is fixed at normal emission, the high degree of symmetry in the normal direction leads to degeneracies in the timereversed LEED beams. The conditions of constructive and destructive interference are the same for the degenerate beams, and consequently, we expect large modulations in the normal emission cross-section. If the final-state is sampled off-normal, the reduction of symmetry results in an increase in the conditions for constructive and destructive interference. Two consequences emerge: new peaks are seen and the peak-to-valley ratio decreases. The latter can be seen in Fig. 1, where PD curves are shown for emission in the $\lceil 100 \rceil$ azimuth with polar

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angles $\theta = 0^\circ$, 5° , 10° , 15° , 20° and 25° . The experimental geometry for this data set is shown in Fig. 2. The NPD curve ($\theta = 0^{\circ}$) exhibits the greatest peak-to-valley ratio. As the detector is rotated offnormal, the modulations get smaller. At $e = 25^\circ$, the modulations are small enough that the underlying atomic cross-section is becoming apparent. An example of a new peak which emerges at off-normal emission is seen in Fig. 1. This peak is first seen at $\theta = 10^{\circ}$ in the [100] azimuth at 111 eV kinetic energy, and becomes the most prominent feature in the NPD curve by $\theta = 25^\circ$. The peak disperses from 111 eV at $\theta = 10^{\circ}$ to 103 eV at $\theta = 25^{\circ}$. The main peaks present in the PD curve at normal emission (kinetic energy 89 and 138) decrease in intensity while dispersing slightly in energy with polar angle.

Similar effects are seen if the crystal is rotated azimuthally about the sample normal by 45°, so that the photon beam and emission direction are both located in the [110] azimuth. This experimental geometry is shown in Fig. 3. These experimental PO curves are also shown in Fig. 1. Again, the peak to valley contrast is greatest at normal emission. The two main peaks in the normal emission curve are at kinetic energy 89 and 137 eV. A new peak at 110 eV appears at $\theta =$ 10° and grows in intensity through $\theta = 25^\circ$.

A comparison between the PO curves for the two azimuths studied is of interest at this point. For core level emission from an adsorbate in a fourfold hollow site $(C_{4v}$ symmetry) the PD intensity at normal emission is independent of the azimuthal angle ϕ of the incident photon beam. Thus, the two curves at $\theta = 0^{\circ}$ of Fig. 1 indicate the high

 $-7-$

degree of reproducibility of the data at equivalent but non-identical conditions. As the detector is moved off-normal, we are comparing two sample geometries which differ by 45° not only in the azimuthal orientation of the photon polarization vector, but also in the azimuthal orientation of photoelectron emission. The second effect induces significant differences between pairs of curves with the same polar angle, especially for $9 \ge 15^\circ$. At $9 = 5^\circ$ the differences are minor and at $\theta = 10^{\circ}$ the major difference is in the position of the first PD peak. At $\theta = 15^{\circ}$ and $\theta = 20^{\circ}$, the curves are still similar above 90 eV kinetic energy. Only at $\theta = 25^{\circ}$ do PD curves for the two azimuths look substantially different at all energies.

We now turn to the theoretical analysis of the data in Fig. 1. The data for the [100J azimuth are reproduced in Fig. 2 and compared with PD calculations for Se in the fourfold hollow site at $d_1 = 1.55\text{\AA}$, where d_1 is the perpendicular distance between the c(2x2)Se overlayer plane and the nickel surface. The agreement is quite good for all angles sampled. Visual inspection indicates that the quality of the fit is extremely good at small polar angles (θ < 15°) but worsens somewhat at the larger polar angles sampled. Theoretical calculations for emission into the [110] azimuth are shown in Fig. 3 along with the experimental curves, which are reproduced from Fig. 1. Calculated PO curves for Se in the fourfold hollow site with $d_1 = 1.55\text{\AA}$ are presented. The fit with the experimental data is again quite good. Just as for the [100] azimuth, the fit is excellent for smaller polar angles and deteriorates as θ gets large. An R-factor analysis was carried out for the d_1 values of 1.45, 1.55, 1.65, and 1.75A using all data from both azimuths studied. The $d_1 = 1.55$ Å spacing was found to give the optimum (lowest) R-factor. Details of the R-factor analysis are given in the next section. The determination of $d_1 = 1.55$ Å is in excellent agreement with our previous NPD study on this system⁴ and with LEED intensity analyses in the literature 13,14 .

A major benefit of studying off-normal photoelectron diffraction is that a comparison of many experimental curves to theory provides a self-consistency check of the NPD results, in the same manner that LEED intensity analysis at off-normal incidences can be used to confirm results obtained by studying the LEED beams at normal incidence. At the same time, caution should be taken in examining the PO fits at large polar angles, as both experimental and calculated curves exhibit smaller oscillations and it is more difficult to establish whether a good fit exists. This work indicates that the polar angles closest to the sample normal ($\varphi \leq 15^{\circ}$) provide the most reliable structural information.

The close similarity between all six experimental PO curves with θ < 10° (θ = 0°, 5°, and 10° in both azimuths) presents the possibility that NPD data could be taken into a much larger solid angle of emission (resulting in a dramatic reduction of data collection time) without significantly degrading the structural accuracy of NPD. In a previous paper, ⁴ we used NPD to determine that selenium is situated above the hollow sites on Ni(001) with $d_1 = 1.55 \pm 0.04$ Å. In that study (as well as this work), the angular acceptance of our electron energy analyzer

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was a half-angle of 3° . If the angular acceptance is increased to 10° half-angle, the number of photoelectrons collected will increase by more than 10 times if one assumes an isotropic angular distribution of photoelectrons over the range $0\degree\leq$ $\circ\leq$ $10\degree$. We estimate that the corresponding decrease in structural accuracy will be considerably less than the current experimental error; i.e., the increased angular acceptance should introduce an additional error of about ± 0.02 Å to the d_1 determination for Se on Ni(OO1). We conclude that future NPD experiments could benefit from using a larger angular acceptance of photoelectrons.

Occasionally, the theoretical NPO curves for two different sites exhibit an "accidental coincidence" in peak positions which makes it more difficult to distinguish the correct site geometry. In these cases, most or all of the peaks in one curve have energy positions which differ by 5 eV or less from the energies of peaks in the second curve. For example, in an earlier paper, Li and Tong 15 noted that for normal emission from the $c(2x2)$ Se-Ni(001) system, there is an accidental coincidence of diffraction peaks between $d_1 = 1.55$ Å (hollow site) and $d_1 = 2.34$ Å (top site). These authors expected that this accidental coincidence would be lifted when off-normal emission data became available. This is indeed the case, and we show in Fig. 4 the comparison at $e = 15^\circ$ of experimental data with calculated PD curves for d₁ = 1.55 Å (hollow site) and d₁ = 2.34 Å (top site). The emission direction is along the [100] azimuth. The peak at 88 eV of the hollow site curve is split into two peaks (80 eV and 100 eV) in the top site

curve. Near 88 eV, there is a valley for the top site. This comparison definitely rules out the top site as the binding location of c(2x2)Se on Ni(OOI).

V. R-Factor Analysis

To facilitate comparison between theory and experiment, and to compare the "fit" obtained here with other structural analyses, we performed an R-factor analysis on this system. We used a normalized R-factor, 16 described earlier, which was based on individual R-factors defined by Van Hove et al., 17 Zanazzi and Jona, 18 and Pendry. 19 The normalized R-factor is defined as

$$
RR = \frac{1}{6} (R_1 + R_2 + R_3 + R_4 + R_5 + R_6)
$$
 (1)

where

$$
R_1 = A_1 \times \frac{\text{energy range with slopes of opposite signs}}{\text{total energy range}} \tag{2}
$$

$$
R_2 = A_2 \times \int (I_e - cI_t)^2 dE
$$
 (3)

$$
R_3 = A_3 \times \int (I_e^{\dagger} - cI_t^{\dagger})^2 dE
$$
 (4)

$$
R_{\mathbf{q}} = A_{\mathbf{q}} \times \int (I_{e}^{u} - cI_{t}^{u})^{2} dE
$$
 (5)

$$
R_{5} = A_{5} \times \int \frac{|\mathbf{I}_{e}^{I} - c\mathbf{I}_{t}^{I}| \times |\mathbf{I}_{e}^{II} - c\mathbf{I}_{t}^{II}|}{|\mathbf{I}_{e}^{I}| + \max |\mathbf{I}_{e}^{I}|} dE
$$
 (6)

$$
R_6 = A_6 \times \frac{\int (\Upsilon_e - \Upsilon_t)^2 dE}{\int (\Upsilon_e^2 + \Upsilon_t^2) dE}
$$
 (7)

Here, I_e are the experimental intensity data, I_e and I_e refer to the first and second derivatives of I_e with respect to energy. I_t , I_t^{\dagger} and $\overline{I}^{\text{u}}_{\text{t}}$ are the corresponding quantities for the calculated intensities. Also,

$$
c = \frac{\int I_e dE}{\int I_t dE}
$$
\n
$$
Y_{e,t} = \frac{I_e^t, t^l e, t}{1 + V_I^2 \left(\frac{I_e^t, t}{I_{e,t}}\right)^2}
$$
\n(9)

where V_I is defined in Section III.

The weights A_1,\ldots,A_6 are chosen such that the average value of each R-factor over the geometries considered in this work is 1.0. This ensures that the influence of each R-factor is roughly the same, so that in RR, no one R-factor dominates the other.

The value of RR, evaluated over the 11 PO curves shown in Figs. 2 and 3 (the two $\theta = 0^{\circ}$ curves are degenerate, so we took only the one in Fig. 2), is plotted as a function of d_1 in Fig. 5. A well-defined minimum is seen at $d_1 = 1.55~\text{Å}$. This result agrees with the determination by visual judgment, and it also agrees with earlier PO analysis at normal emission and with LEED.^{13,14}

To compare the degree of fit with other structural analyses, the value of the Zanazzi-Jona R-factor $(R_{7,1})^{20}$ for $d_1 = 1.55$ Å is 0.05.

From previous experience, a structural analysis is acceptable if R_{ZJ} < 0.2. With this criterion, the overall fit here is substantially above average.

VI. Conclusions

In this paper, we have demonstrated, for the first time, the use of off-normal energy-dependent photoelectron diffraction curves to determine surface structure. Off-normal PD curves show smaller oscillation amplitudes than NPD curves, but these curves can nevertheless be used to accurately determine the structural parameter d_1 . In the event of an accidental coincidence at normal emission, we have demonstrated that off-normal PO curves can be used to resolve the coincidence. Due to the rapid decrease of the amplitude of the oscillations at larger e, the most useful range seems to be between $\theta = 0^{\circ}$ and $\theta = 15^{\circ}$.

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- 20. Our R_5 is derived from the Zanazzi-Jona R-factor (Ref. 18), except for a different coefficient A_{κ} .

Figure Captions

- Figure 1. Experimental PO data for c(2x2)Se(3d)-Ni(001) for emission in the [100] azimuth (solid curves) and the [110] azimuth (dashed curves) as a function of polar angle e. The experimental geometries for the [100] and [110] azimuths are shown in Figs. 2 and 3, respectively.
- Figure 2. Experimental PO data for the [100J azimuth (solid curves) compared with theoretical calculations for the hollow site with $d_1 = 1.55$ Å (dashed curves).
- Figure 3. Experimental PO data for the [110J azimuth (solid curves) compared with theoretical calculations for the hollow site with $d_1 = 1.55$ Å (dashed curves).
- Figure 4. Comparison of (a) experimental PO data for c(2x2)Se(3d)-Ni(OOl) with calculated curves for (b) Se in the hollow site, $d_1 = 1.55$ Å and (c) Se in the top site, $d_1 = 2.34$ Å. The polar angle of emission is $\theta = 15^\circ$ in the [100] azimuth.

Figure 5. Plot of the normalized R-factor versus d_i spacing.

-17-

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-19-

Figure 3

 $-20-$

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Figure 4

Figure 5

XBL 822-153

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 $\sim 10^7$

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 $\mathcal{A}^{\mathcal{A}}$